

TEMA 9

1. Pentru fiecare din irurile următoare, decideți dacă este supercrescător și determinați toate soluțiile problemei knapsacului cu "volumul" corespunzător:

a) (2, 3, 7, 20, 35, 69)

$V = 45$

c) (1, 3, 7, 12, 22, 45)

$V = 67$

b) (1, 2, 5, 9, 20, 49)

$V = 73$

d) (2, 3, 6, 11, 21, 40)

$V = 39$

e) (4, 5, 10, 30, 59, 101)

$V = 186$

f) (3, 5, 8, 15, 28, 60)

$V = 43$

a) $2+3 = 5 < 7$

$5+7 = 12 < 20$

$12+20 = 32 < 35$

$32+35 = 67 < 69$

\Rightarrow Sirul este supercrescător

$2+3+7+20+35+69 > 45$

$V = 45$

$v = (2, 3, 7, 20, 35, 69)$

$k = 6$

$i_0 = 5 \quad (v[5] = 35 \leq 45)$

$\varepsilon_5 = 1$

$\varepsilon_6 = 0$

$V = 45 - 35 = 10$

$v = (2, 3, 7, 20)$

$$i_0 = 3 \quad (v[3] = 7 \leq 10)$$

$$\varepsilon_3 = 1$$

$$\varepsilon_4 = 0$$

$$V = 10 - 7 = 3$$

$$v = (2, 3)$$

$$i_0 = 2 \quad (v[2] = 3 \leq 3)$$

$$\varepsilon_2 = 1$$

$$\varepsilon_1 = 0$$

$$\varepsilon = (0, 1, 1, 0, 1, 0)$$

$$b) \quad 1+2 = 3 < 5$$

$$3+5 = 8 < 9$$

$$8+9 = 17 < 20$$

$$17+20 = 37 < 49$$

\Rightarrow Șirul este supercrescător

$$V = 73$$

$$v = (1, 2, 5, 9, 20, 49)$$

$$k = 6$$

$$i_0 = 49 \quad (v[6] = 49 \leq 73)$$

$$\varepsilon_6 = 1$$

$$V = 73 - 49 = 24$$

$$v = (1, 2, 5, 9, 20)$$

$$i_0 = 20 \quad (v[5] = 20 \leq 24)$$

$$\varepsilon_5 = 1$$

$$V = 24 - 20 = 4$$

$$v = (1, 2, 5, 9)$$

$$i_0 = 2 \quad (v[2] = 2 \leq 4)$$

$$\varepsilon_2 = 1$$

$$\varepsilon_3 = 0$$

$$\varepsilon_4 = 0$$

$$V = 4 - 2 = 2$$

$$v = (1)$$

$$i_0 = 1 \quad (v[1] = 1 \leq 2)$$

$$E_1 = 1$$

$$E = (1, 1, 0, 0, 1, 1)$$

c) $1 + 3 = 4 \leq 7$

$$4 + 7 = 11 < 12$$

$$11 + 12 = 23 > 22$$

\Rightarrow First rule superrescator

$$V = 39$$

$$v = (1, 3, 7, 12, 22, 45)$$

$$k = 6$$

$$i_0 = 5 \quad (v[5] = 22 \leq 39)$$

$$E_5 = 1$$

$$E_6 = 0$$

$$V = 39 - 22 = 17$$

$$v = (1, 3, 7, 12)$$

$$i_0 = 4 \quad (v[4] = 12 \leq 17)$$

$$E_4 = 1$$

$$V = 17 - 12 = 5$$

$$v = (1, 3, 7)$$

$$i_0 = 2 \quad (v[2] = 3 \leq 5)$$

$$E_2 = 1$$

$$E_3 = 0$$

$$V = 5 - 3 = 2$$

$$v = (1)$$

$$i_0 = 1 \quad (v[1] = 1 \leq 2)$$

$$E_1 = 1$$

$$E = (1, 1, 0, 1, 1, 0)$$

$$d) 2+3=5 < 6$$

$$5+6=11 \leq 11$$

$$11+11=22 > 21$$

\Rightarrow spiral nu e supercrescator

$$V=39$$

$$v=(2, 3, 6, 11, 21, 40)$$

$$k=6$$

$$i_0=5 \quad (v[5]=21 \leq 39)$$

$$E_5=1$$

$$E_6=0$$

$$V=39-21=18$$

$$v=(2, 3, 6, 11)$$

$$i_0=4$$

$$E_4=1$$

$$V=18-11=7$$

$$v=(2, 3, 6)$$

$$i_0=3$$

$$E_3=1$$

$$V=7-6=1$$

$$E_1=0$$

$$E_2=0$$

$$E=(0, 0, 1, 1, 1, 0)$$

$$e) \quad 4+5=9 < 10$$

$$9+10=19 < 30$$

$$19+30=49 < 50$$

$$49+50=99 < 101$$

⇒ *Șirul este supercrescător*

$$V = 186$$

$$v = (4, 5, 10, 30, 50, 101)$$

$$i_0 = 6$$

$$E_6 = 1$$

$$V = 186 - 101 = 85$$

$$v = (4, 5, 10, 30, 50)$$

$$i_0 = 5$$

$$E_5 = 1$$

$$V = 85 - 50 = 35$$

$$v = (4, 5, 10, 30)$$

$$i_0 = 4$$

$$E_4 = 1$$

$$V = 35 - 30 = 5$$

$$v = (4, 5, 10)$$

$$i_0 = 2$$

$$E_2 = 1$$

$$E_3 = 0$$

$$V = 5 - 5 = 0$$

$$E_1 = 0$$

$$E = (0, 1, 0, 1, 1, 1)$$

$$f) \quad 3+5=8 \leq 8$$

$$8+8=16 > 15$$

\Rightarrow *șirul nu este supercrescător*

$$V = 43$$

$$v = (3, 5, 8, 15, 28, 60)$$

$$k = 6$$

$$i_0 = 5$$

$$E_5 = 1$$

$$E_6 = 0$$

$$V = 43 - 28 = 15$$

$$v = (3, 5, 8, 15)$$

$$i_0 = 4$$

$$E_4 = 1$$

$$E_3 = 0$$

$$E_2 = 0$$

$$E_1 = 0$$

$$V = 15 - 15 = 0$$

$$E = (0, 0, 0, 1, 1, 0)$$