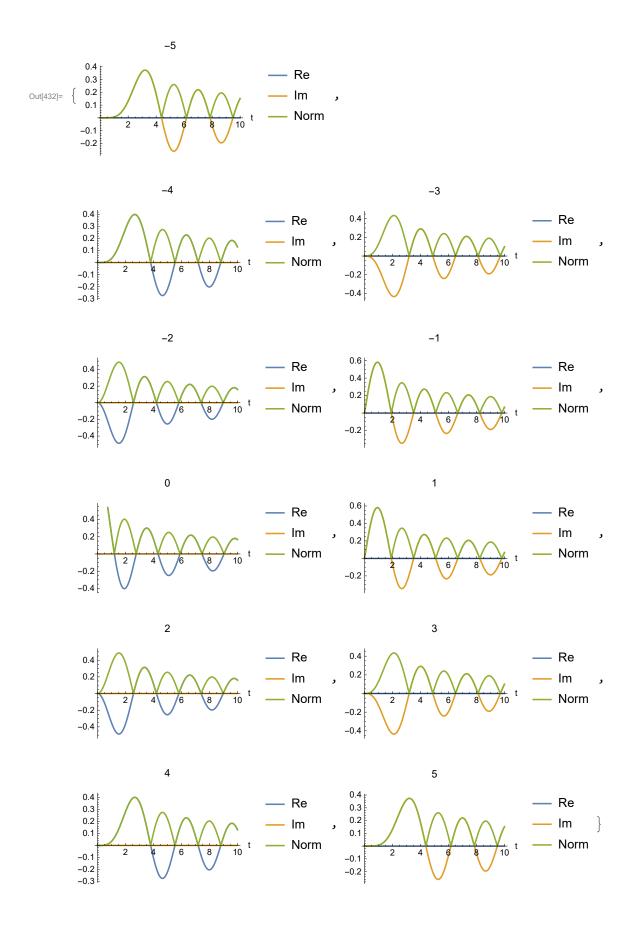
Hopping only

```
In[398]:= H[Nl_] := Table[If[Abs[i-j] == 1, -1, 0], {i, 1, Nl}, {j, 1, Nl}];
       H[10] // MatrixForm
Out[399]//MatrixForm=
         0 \ \ -1 \ \ 0 \ \ 0 \ \ 0 \ \ 0 \ \ 0 \ \ 0
                                              a
         -\, \boldsymbol{1} \quad \boldsymbol{0} \quad -\, \boldsymbol{1} \quad \boldsymbol{0} \quad \boldsymbol{0}
                             0 0 0
                                          0
                                              0
         a
                                              0
         0 0 0 0 -1 0 -1 0 0
                                              0
         0 0 0 0 0 -1 0 -1 0
                                              а
         0 0 0 0 0 0 -1 0 -1
                                              0
           0 0 0 0 0 0 -1 0 -1
  Info]:= (*{EVals, EVecs}=Eigensystem[N[H[100]]];
       sortedEVecs=(EVecs)[[Ordering[EVals]]];
       sortedEVals=Sort[EVals];
       ListPlot[sortedEVals]
        {ListPlot[sortedEVecs[[1]]],ListPlot[sortedEVecs[[2]]],
         ListPlot[sortedEVecs[[3]]],ListPlot[sortedEVecs[[98]]],
         ListPlot[sortedEVecs[[99]]], ListPlot[sortedEVecs[[100]]]}
        {ListLinePlot[
           RotateRight[Abs[Fourier[sortedEVecs[[1]]]],50],PlotRange→All,Frame→True],
         ListLinePlot[RotateRight[Abs[Fourier[sortedEVecs[[2]]]],50],PlotRange→All,
           Frame - True], ListLinePlot [RotateRight [Abs [Fourier [sortedEVecs [[3]]]], 50],
           PlotRange→All,Frame→True],ListLinePlot[
           RotateRight[Abs[Fourier[sortedEVecs[[100]]]],50],PlotRange→All,Frame→True]}*)
 In[424]:= ClearAll@ψ;
       H[Nl_] := Table[If[Abs[i-j] == 1, -1, 0], {i, 1, Nl}, {j, 1, Nl}];
       N1 = 400;
       tf = 50;
       \psi 0 = \text{Table}[\text{If}[i = \text{Nl}/2, 1, 0], \{i, 1, \text{Nl}\}];
       s = NDSolve[{ID[\psi[t], t] == H[N1].\psi[t], \psi[0] == \psi0}, \psi, {t, 0, tf}];
       \psi[t_{-}] = \text{Evaluate}[\psi[t] /. s];
 ln[431] := tmax = 10;
       Table \lceil Plot \lceil \{Re[\psi[t][[1, i]]\}, Im[\psi[t][[1, i]]\}, Norm[\psi[t][[1, i]]] \}
          {t, 0, tmax}, PlotLegends → {"Re", "Im", "Norm"},
         AxesLabel \rightarrow {"t", ""}, PlotLabel \rightarrow i - N1/2], {i, N1/2-5, N1/2+5}]
       (*Manipulate ListLinePlot Abs [\psi[t]]^2, PlotRange \rightarrow \{0,1\}, PlotLabel \rightarrow t, \{t,0,5\} \*)
```



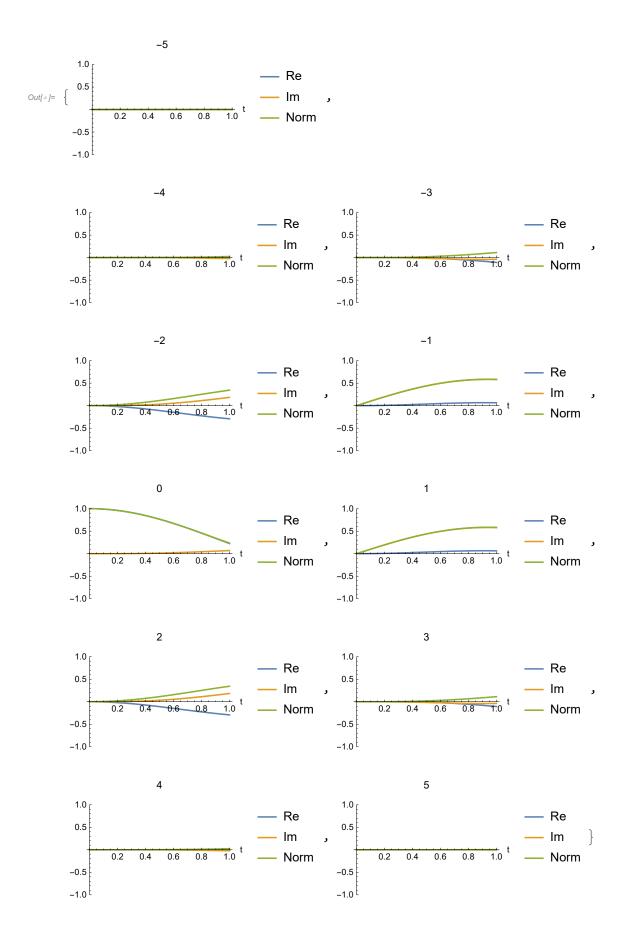
```
In[433]:= sitenum = 398;
         tmax = 8;
        \texttt{MatrixPlot} \big\lceil \texttt{Table} \big\lceil \texttt{Abs} [\psi[\texttt{t}][[\texttt{1, i}]]],
            {t, 0, tmax, 0.1}, \{i, N1/2 - sitenum/2, N1/2 + sitenum/2\}],
          FrameLabel → {t, "site"}, ImageSize → Full]
                                                                                                                                    399
                                                                                                       300
            20
                                                                                                                                         20
                                                                                                                                         40
            40
Out[435]=
            60
                                                                                                                                         60
            81
                                             100
                                                                          200
                                                                                                       300
                                                                                                                                    399
                                                                          site
```

With Trap

```
In[400] := H[N1_, \omega_] :=
          Table \left[ \text{If} \left[ i = j, \left( i - \text{Nl} / 2 \right)^2 \omega^2, \text{If} \left[ \text{Abs} \left[ i - j \right] = 1, -1, 0 \right] \right], \{i, 1, \text{Nl}\}, \{j, 1, \text{Nl}\} \right];
       H[10, 0.5] // MatrixForm
Out[401]//MatrixForm=
               - 1
                     0
                          0
                                                           0
         4.
          -1
              2.25
                    -1
                          0
                                0
                                     0
                                           0
                                                      0
                                                           0
                                0
                                                           0
               - 1
                    1.
                          - 1
                        0.25
                               -1
                                     0
                                                           0
          0
                     0
                          - 1
                               0.
                                     - 1
                                           0
                                                0
                                                           0
          0
                                   0.25
                                                0
               0
                     0
                          0
                                                      0
                                                           0
                               - 1
                                          - 1
          0
               0
                     0
                                                      0
                                                           0
                          0
                                0
                                               - 1
                                     - 1
                                          1.
          0
               0
                     0
                          0
                                0
                                     0
                                              2.25
                                                     - 1
                                                           0
                                          - 1
          0
                     0
                          0
                                0
                                     0
                                                - 1
                                                     4.
                                                0
                                                     - 1
                                                         6.25
  In[@]:= (*{EVals, EVecs}=Eigensystem[N[H[100,1]]];
        sortedEVecs=(EVecs)[[Ordering[EVals]]];
        sortedEVals=Sort[EVals];
       ListPlot[sortedEVals]
         {ListPlot[sortedEVecs[[1]],PlotRange→All],
          ListPlot[sortedEVecs[[2]],PlotRange→All],
          ListPlot[sortedEVecs[[3]],PlotRange→All],
          ListPlot[sortedEVecs[[99]],PlotRange→All],
          ListPlot[sortedEVecs[[100]],PlotRange→All]}
         {ListLinePlot[
           RotateRight[Abs[Fourier[sortedEVecs[[1]]]],50],PlotRange→All,Frame→True],
          ListLinePlot[RotateRight[Abs[Fourier[sortedEVecs[[2]]]],50],PlotRange→All,
            Frame - True], ListLinePlot[RotateRight[Abs[Fourier[sortedEVecs[[3]]]]],50],
           PlotRange→All,Frame→True],ListLinePlot[
            RotateRight[Abs[Fourier[sortedEVecs[[100]]]],50],PlotRange→All,Frame→True]}*)
```

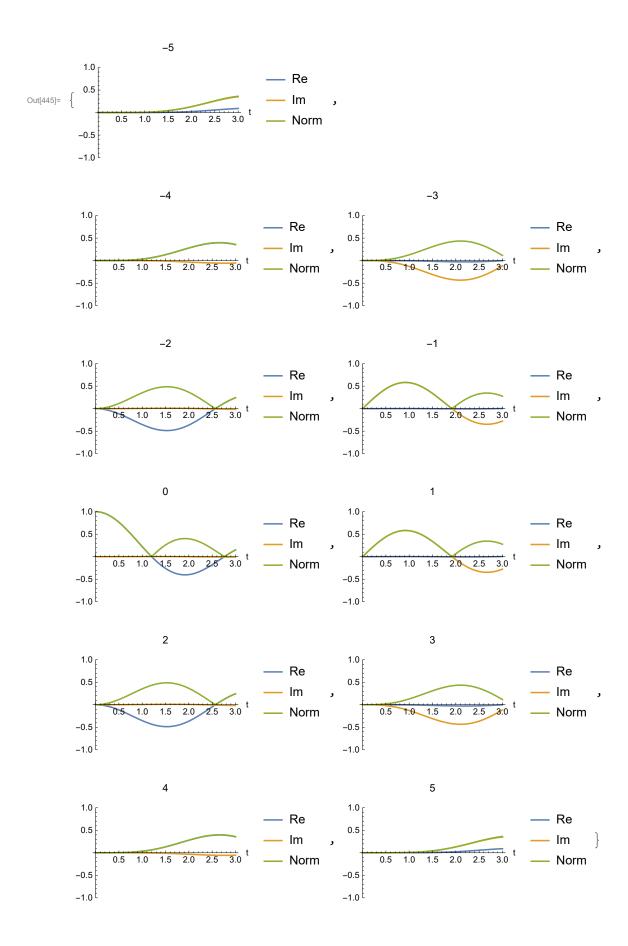
Blue Detuned

```
ClearAll@\psi;
      H[N1_, \omega_] :=
         Table [If[i = j, (i-Nl/2)^2 \omega^2, If[Abs[i-j] == 1, -1, 0]], \{i, 1, Nl\}, \{j, 1, Nl\}];
      \omega = 0.6;
      N1 = 200;
      tf = 8;
      \psi 0 = \text{Table}[\text{If}[i = Nl/2, 1, 0], \{i, 1, Nl\}];
      s = NDSolve[\{ID[\psi[t], t] == H[N1, \omega] . \psi[t], \psi[0] == \psi 0\}, \psi, \{t, 0, tf\}];
      \psi[t_] = \text{Evaluate}[\psi[t] /. s];
      NDSolve: Maximum number of 111926 steps reached at the point t == 6.929466769420081.
ln[ \circ ] := tmax = 1;
      Table \lceil Plot \lceil \{Re[\psi[t][[1, i]]\}, Im[\psi[t][[1, i]]], Norm[\psi[t][[1, i]]]\}, \rceil \rceil
          \label{eq:theorem} \{\texttt{t, 0, tmax}\}, \ \texttt{PlotLegends} \rightarrow \{\texttt{"Re", "Im", "Norm"}\}, \ \texttt{PlotRange} \ \rightarrow \{\texttt{-1, 1}\},
         AxesLabel \rightarrow {"t", ""}, PlotLabel \rightarrow i - Nl / 2], {i, Nl / 2 - 5, Nl / 2 + 5}]
```



```
In[*]:= sitenum = 198;
      tmax = 0.9;
      MatrixPlot[Table[Abs[\psi[t][[1, i]]],
         {t, 0, tmax, 0.1}, {i, N1/2 - sitenum/2, N1/2 + sitenum/2}],
       FrameLabel → {"t (100ms)", "site"}, ImageSize → Full]
                                                        100
                                                                              150
                                  50
                                                        100
                                                                              150
                                                        site
In[436]:= ClearAll@ψ;
      H[N1_, \omega_] :=
        Table [If[i = j, (i-Nl/2)^2 \omega^2, If[Abs[i-j] == 1, -1, 0]], \{i, 1, Nl\}, \{j, 1, Nl\}];
      \omega = 0.1;
      N1 = 200;
      tf = 20;
```

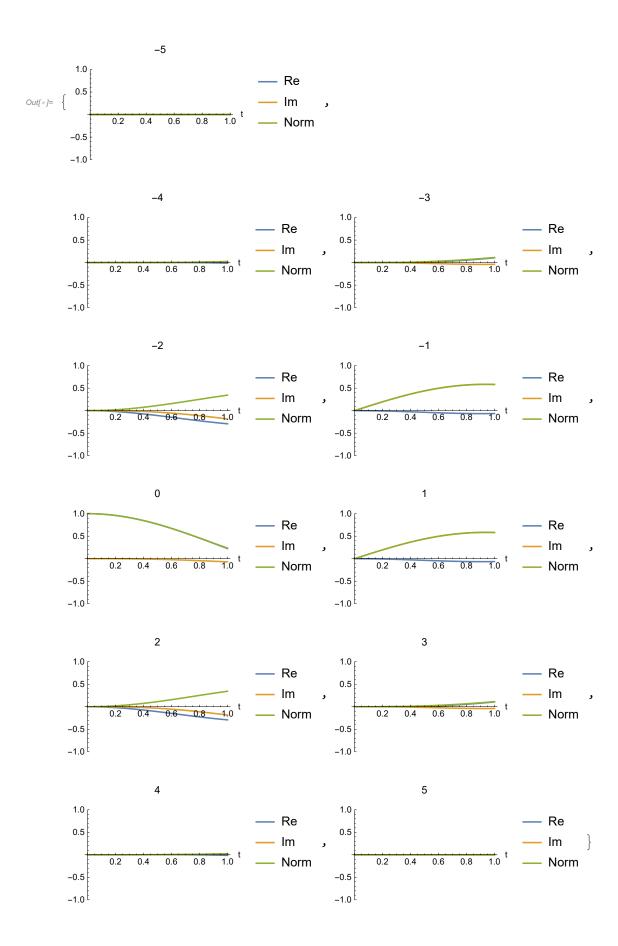
 $\psi 0 = Table \Big[If \Big[i = Nl / 2, 1, 0 \Big], \{i, 1, Nl\} \Big];$ $s = NDSolve \Big[\{ID[\psi[t], t] = H[Nl, \omega] . \psi[t], \psi[0] = \psi 0 \}, \psi, \{t, 0, tf\} \Big];$ $\psi[t_{-}] = Evaluate[\psi[t] /. s];$ In[444] := tmax = 3; $Table \Big[Plot \Big[\{Re[\psi[t][[1, i]]], Im[\psi[t][[1, i]]], Norm[\psi[t][[1, i]]] \},$ $\{t, 0, tmax\}, PlotLegends \rightarrow \{"Re", "Im", "Norm"\}, PlotRange \rightarrow \{-1, 1\},$ $AxesLabel \rightarrow \{"t", ""\}, PlotLabel \rightarrow i - Nl / 2 \Big], \{i, Nl / 2 - 5, Nl / 2 + 5 \} \Big]$



```
In[*]:= sitenum = 198;
      tmax = 3;
      \texttt{MatrixPlot} \big\lceil \texttt{Table} \big\lceil \texttt{Abs} [\psi[\texttt{t}][[\texttt{1, i}]]],
         \{t, 0, tmax, 0.1\}, \{i, Nl/2 - sitenum/2, Nl/2 + sitenum/2\}],
        FrameLabel → {"t (100ms)", "site"}, ImageSize → Full]
                                                                                                  150
                                                                                                                              199
         10
                                                                                                                                   10
                                                                                                                                  20
                                                                                                                                  31
                                          50
                                                                      100
                                                                                                  150
                                                                                                                              199
```

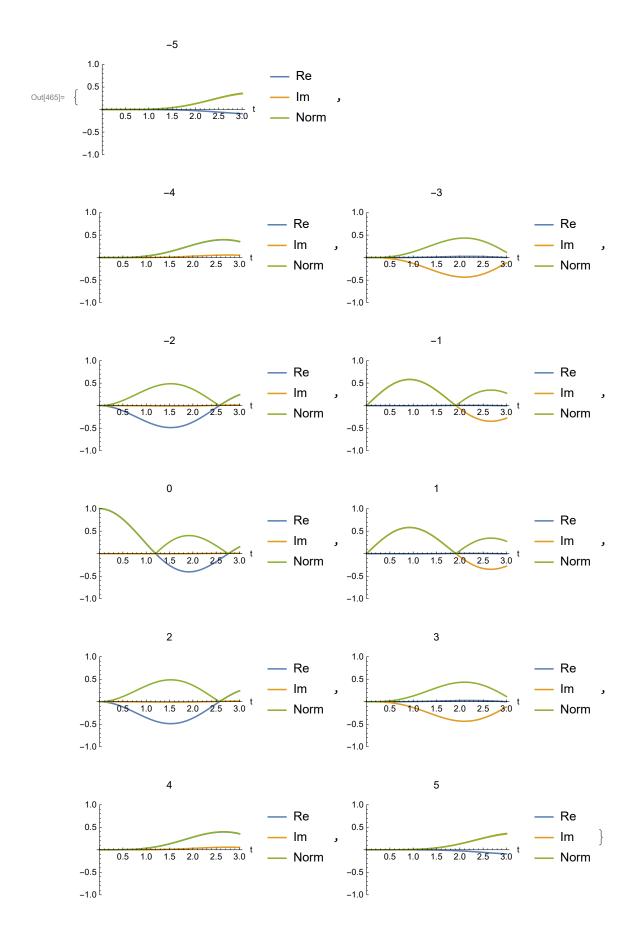
Red Detuned

```
In[*]:= ClearAll@ψ;
          Table \left[ \text{If} \left[ i = j, -1 * \left( i - \text{Nl} / 2 \right)^2 \omega^2, \text{If} \left[ \text{Abs} \left[ i - j \right] = 1, -1, 0 \right] \right], \{i, 1, \text{Nl}, \{j, 1, \text{Nl}\} \right];
      \omega = 0.6;
      N1 = 200;
      tf = 20;
      \psi 0 = \text{Table}[\text{If}[i = \text{Nl}/2, 1, 0], \{i, 1, \text{Nl}\}];
      s = NDSolve[{ID[\psi[t], t] == H[N1, \omega].\psi[t], \psi[0] == \psi0}, \psi, {t, 0, tf}];
      \psi[t_{-}] = \text{Evaluate}[\psi[t] /. s];
ln[*]:= (*\lambda[t_]):= MatrixExp[I H[N1] t].\psi0;
      Table[Plot[\{Re[\lambda[t][[\ i]]],\ Im[\lambda[t][[\ i]]],\ Norm[\lambda[t][[i]]]\},\ \{t,\ 0,\ tf\},
           PlotLegends \rightarrow \{"Re", "Im", "Norm"\}, \ AxesLabel \rightarrow \{"t", ""\}, \ PlotLabel \rightarrow i], \ \{i, 1, Nl\}] \star) 
In[*]:= tmax = 1;
      Table [Plot | \{Re[\psi[t][[1, i]]\}, Im[\psi[t][[1, i]]\}, Norm[\psi[t][[1, i]]]\},
          \{t, 0, tmax\}, PlotLegends \rightarrow \{"Re", "Im", "Norm"\}, PlotRange \rightarrow \{-1, 1\},
          AxesLabel \rightarrow {"t", ""}, PlotLabel \rightarrow i - Nl/2], {i, Nl/2-5, Nl/2+5}]
```



```
In[*]:= sitenum = 198;
        tmax = 0.9;
       MatrixPlot[Table[Abs[\psi[t][[1, i]]],
           {t, 0, tmax, 0.1}, {i, N1/2 - sitenum/2, N1/2 + sitenum/2}],
         FrameLabel → {"t (100ms)", "site"}, ImageSize → Full]
                                                                                                 150
                                          50
                                                                      100
                                                                                                 150
                                                                      site
In[456]:= ClearAll@ψ;
       H[N1_, \omega_] :=
           Table \left[ \text{If} \left[ i = j, -1 * \left( i - \text{Nl} / 2 \right)^2 \omega^2, \text{If} \left[ \text{Abs} \left[ i - j \right] = 1, -1, 0 \right] \right], \{i, 1, \text{Nl}\}, \{j, 1, \text{Nl}\} \right];
       \omega = 0.1;
       N1 = 200;
       tf = 20;
        \psi 0 = \text{Table}[\text{If}[i = \text{Nl}/2, 1, 0], \{i, 1, \text{Nl}\}];
        s = NDSolve[{ID[\psi[t], t] == H[N1, \omega].\psi[t], \psi[0] == \psi0}, \psi, {t, 0, tf}];
        \psi[t_{-}] = Evaluate[\psi[t] /.s];
ln[464]:= tmax = 3;
        Table [Plot] {Re[\psi[t][[1, i]]], Im[\psi[t][[1, i]]], Norm[\psi[t][[1, i]]]},
           \{t, 0, tmax\}, PlotLegends \rightarrow \{"Re", "Im", "Norm"\}, PlotRange \rightarrow \{-1, 1\},
```

AxesLabel \rightarrow {"t", ""}, PlotLabel \rightarrow i - N1/2, {i, N1/2-5, N1/2+5}]



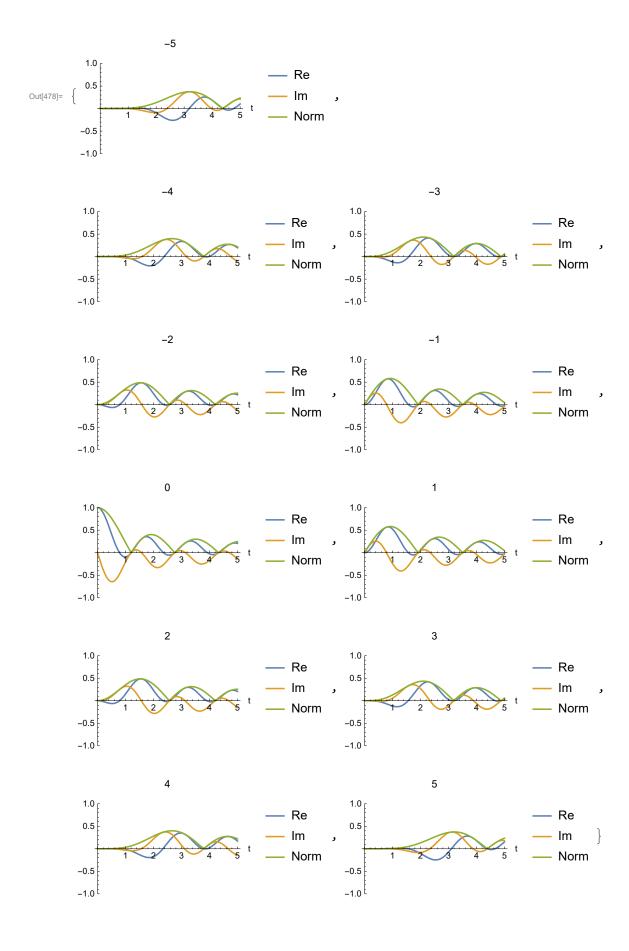
```
In[466]:= sitenum = 198;
       tmax = 3;
       MatrixPlot[Table[Abs[\psi[t][[1, i]]],
          {t, 0, tmax, 0.1}, \{i, N1/2 - sitenum/2, N1/2 + sitenum/2\}],
        FrameLabel → {"t (100ms)", "site"}, ImageSize → Full]
                                                                                 150
                                                                                                        199
          10
                                                                                                            10
Out[468]= (100ms)
         20
                                                                                                            20
                                                                                                           31
                                    50
                                                           100
                                                                                 150
                                                                                                        199
                                                           site
```

With force term

```
I_{I[408]} = H[Nl_{j}, F_{j}] := Table[If[i == j, F*i, If[Abs[i - j] == 1, -1, 0]], \{i, 1, Nl\}, \{j, 1, Nl\}];
      H[10, 0.5] // MatrixForm
Out[409]//MatrixForm=
        0.5
             - 1
                 0
                      0
                          0
                              0
                                  0
                                           0
                                               0
                      0
                              0
                                  0
         - 1
             1.
                 - 1
                          0
                                       a
                                           0
                                               0
                1.5
                          0
                              0
                                  0
         a
                     _ 1
                                       a
                                           a
                                               a
             _ 1
         0
                         - 1
                              0
                                  0
                                       0
                                           0
                                               0
             0
                     2.
                 - 1
         0
             0
                  0
                     - 1
                         2.5
                              - 1
                                  0
                                       0
                                           0
                                               0
         0
             0
                  0
                      0
                                  - 1
                                       0
                                               0
         0
             0
                  0
                      0
                          0
                              - 1
                                  3.5
                                      -1
                                               0
         0
             0
                              0
                  0
                      0
                          0
                                  - 1
                                      4.
                                           - 1
                                               0
         0
                                          4.5
             0
                  0
                      0
                          0
                              0
                                  0
                                      - 1
                                              - 1
                                               5.
                          0
                              0
                                  0
                                       0
                                           - 1
  In[*]:= (*{EVals, EVecs}=Eigensystem[N[H[100, 0.2]]];
      sortedEVecs=(EVecs)[[Ordering[EVals]]];
      sortedEVals=Sort[EVals];
      ListPlot[sortedEVals]
        {ListPlot[sortedEVecs[[1]],PlotRange→All],
         ListPlot[sortedEVecs[[2]],PlotRange→All],
         ListPlot[sortedEVecs[[3]],PlotRange→All],
         ListPlot[sortedEVecs[[99]],PlotRange→All],
         ListPlot[sortedEVecs[[100]],PlotRange→All]}
        {ListLinePlot[
          RotateRight[Abs[Fourier[sortedEVecs[[1]]]],50],PlotRange→All,Frame→True],
         ,PlotRange→All, [2]]],50],PlotRange→All, [2]
          Frame - True], ListLinePlot[RotateRight[Abs[Fourier[sortedEVecs[[3]]]], 50],
          PlotRange→All,Frame→True],ListLinePlot[
          RotateRight[Abs[Fourier[sortedEVecs[[100]]]],50],PlotRange→All,Frame→True]}*)
```

Small Force

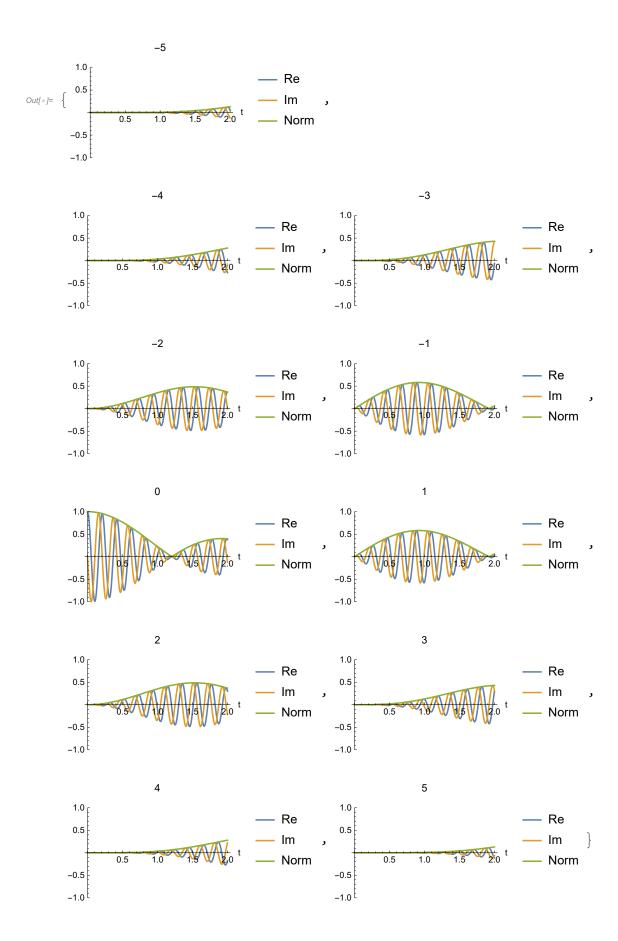
```
In[469]:= ClearAll@ψ;
     N1 = 400;
     tf = 10;
     F = 0.01;
     \psi 0 = \text{Table}[\text{If}[i = \text{Nl}/2, 1, 0], \{i, 1, \text{Nl}\}];
      s = NDSolve[{ID[\psi[t], t] == H[N1, F].\psi[t], \psi[0] == \psi0}, \psi, {t, 0, tf}];
      \psi[t_] = \text{Evaluate}[\psi[t] /. s];
In[477]:= tmax = 5;
     Table [Plot[Re[\psi[t][[1, i]]], Im[\psi[t][[1, i]]], Norm[\psi[t][[1, i]]]],
        \{t, 0, tmax\}, PlotLegends \rightarrow \{"Re", "Im", "Norm"\}, PlotRange \rightarrow \{-1, 1\},
        AxesLabel \rightarrow {"t", ""}, PlotLabel \rightarrow i - Nl/2, {i, Nl/2 - 5, Nl/2 + 5}]
```



```
ln[*]:= (*\lambda[t_]:= MatrixExp[I H[Nl] t].\psi0;
        Table[Plot[{Re[λ[t][[ i]]], Im[λ[t][[ i]]], Norm[λ[t][[i]]]}, {t, 0, tf},
           PlotLegends \rightarrow \{"Re", "Im", "Norm"\}, \ AxesLabel \rightarrow \{"t", ""\}, \ PlotLabel \rightarrow i], \ \{i, 1, Nl\}] *) 
 In[479]:= sitenum = 398;
       tmax = 5;
       MatrixPlot[Table Abs [\psi[t][[1, i]]],
          \{t, 0, tmax, 0.1\}, \{i, Nl/2 - sitenum/2, Nl/2 + sitenum/2\}],
         FrameLabel → {"t (100ms)", "site"}, ImageSize → Full]
                                      100
                                                                                      300
                                                                                                              399
          10
                                                                                                                  10
Out[481]= (100ms)
          20
          30
                                                                                                                  30
          40
                                                                                                                  40
                                                                                                                  51
                                      100
                                                                                      300
                                                              200
                                                                                                              399
                                                              site
```

Larger force

```
In[482]:= ClearAll@ψ;
       H[Nl_{j}, F_{j}] := Table[If[i := j, F * i, If[Abs[i - j] := 1, -1, 0]], {i, 1, Nl}, {j, 1, Nl}];
       N1 = 600;
       tf = 10;
       F = 0.15;
       \psi 0 = \text{Table}[\text{If}[i = \text{Nl}/2, 1, 0], \{i, 1, \text{Nl}\}];
       s = NDSolve[{ID[\psi[t], t] == H[N1, F].\psi[t], \psi[0] == \psi0}, \psi, {t, 0, tf}];
       \psi[t_{-}] = \text{Evaluate}[\psi[t] /. s];
 ln[ \circ ] := tmax = 2;
       Table [Plot] {Re[\psi[t][[1, i]]], Im[\psi[t][[1, i]]], Norm[\psi[t][[1, i]]]},
          \{t, 0, tmax\}, PlotLegends \rightarrow \{"Re", "Im", "Norm"\}, PlotRange \rightarrow \{-1, 1\},
         AxesLabel \rightarrow {"t", ""}, PlotLabel \rightarrow i - Nl/2], {i, Nl/2 - 5, Nl/2 + 5}]
```



```
In[*]:= sitenum = 398;
      tmax = 2;
      MatrixPlot[Table[Abs[\psi[t][[1, i]]],
         \{t, 0, tmax, 0.1\}, \{i, Nl/2 - sitenum/2, Nl/2 + sitenum/2\}],
        FrameLabel → {"t (100ms)", "site"}, ImageSize → Full]
                    \frac{2.99558 \times 10^{-308}}{2} is too small to represent as a normalized machine number; precision may be lost.
                    \frac{2.90704 \times 10^{-308}}{} is too small to represent as a normalized machine number; precision may be lost.
      General: \frac{4.14107 \times 10^{-308}}{2} is too small to represent as a normalized machine number; precision may be lost.
      General: Further output of General::munfl will be suppressed during this calculation.
                                                                                                300
                                                                                                                           399
                                                                                                                                15
                                        100
                                                                    200
                                                                                                300
                                                                    site
```

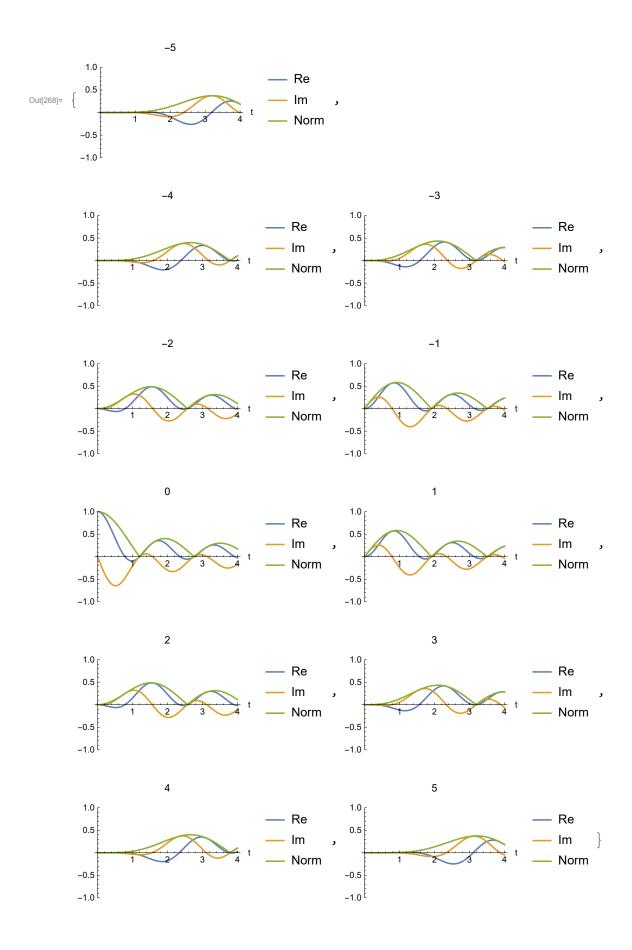
Time dependent force term - NDSolve

```
ln[412]:= Ht[Nl_, \omega_, F_, t_] :=
          Table[If[i == j, F * i * Cos[\omega * t], If[Abs[i - j] == 1, -1, 0]], {i, 1, Nl}, {j, 1, Nl}];
        Ht[10, 0.5, 0.5, t] // MatrixForm
Out[413]//MatrixForm=
         0.5 Cos [0.5 t]
                                                   0
                           1. Cos[0.5t]
                                                                    0
                                                                                     0
                                                                                                       0
                - 1
                                                  - 1
                                            1.5 Cos [0.5 t]
                                                                                     0
                                                                                                       0
                                 - 1
                                                                   - 1
                                  0
                                                              2. Cos[0.5t]
                                                  _ 1
                                                                              2.5 Cos [0.5 t]
                                                                    - 1
                                                                                                3. Cos [0.5 t]
                                                                    0
                                                                                                      - 1
                                                                                                                3.
                                                                    0
                                                                                                       0
                                                                                                       0
```

Low freq, Low A

```
In[332]:= ClearAll@\psi;
      Ht[N1_, \omega_, F_, t_] :=
         Table[If[i = j, F*i*Cos[\omega*t], If[Abs[i-j] == 1, -1, 0]], \{i, 1, Nl\}, \{j, 1, Nl\}];
      N1 = 600;
       tf = 10;
       \omega = 0.01;
       \psi 0 = \text{Table}[\text{If}[i = Nl/2, 1, 0], \{i, 1, Nl\}];
       s = NDSolve[\{ID[\psi[t], t] == Ht[Nl, F, \omega, t].\psi[t], \psi[0] == \psi 0\}, \psi, \{t, 0, tf\}];
       \psi[t_{-}] = Evaluate[\psi[t] /.s];
```

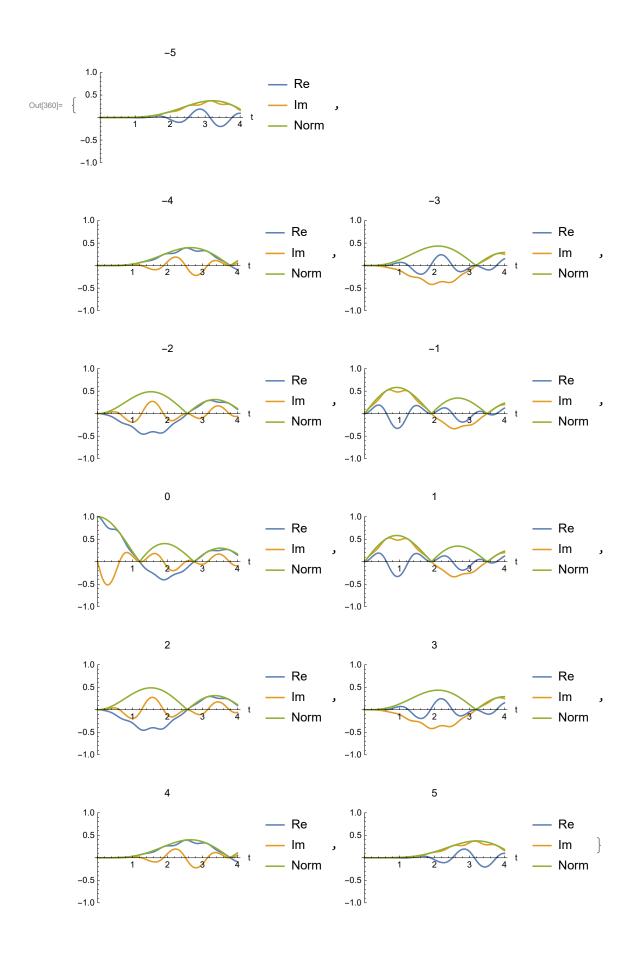
```
In[267]:= tmax = 4;
     {\sf Table} \Big[ {\sf Plot} \Big[ \{ {\sf Re} [\psi[t][[1, \ i]]], \ {\sf Im} [\psi[t][[1, \ i]]], \ {\sf Norm} [\psi[t][[1, \ i]]] \}, \\
        {t, 0, tmax}, PlotLegends \rightarrow {"Re", "Im", "Norm"}, PlotRange \rightarrow {-1, 1},
```



```
In[347]:= sitenum = 598;
       tmax = 7;
       MatrixPlot[Table[Abs[\psi[t][[1, i]]],
          \{t, 0, tmax, 0.1\}, \{i, Nl/2 - sitenum/2, Nl/2 + sitenum/2\}],
         FrameLabel \rightarrow {"t (100ms)", "site"}, ImageSize \rightarrow Full]
                                              200
                                                                               400
                                                                                                                599
Out[349]= (100ms)
          20
                                                                                                                    20
          40
                                                                                                                    40
                                                                                                                    60
                                              200
                                                                               400
                                                                                                                599
                                                               site
```

Low freq, High A

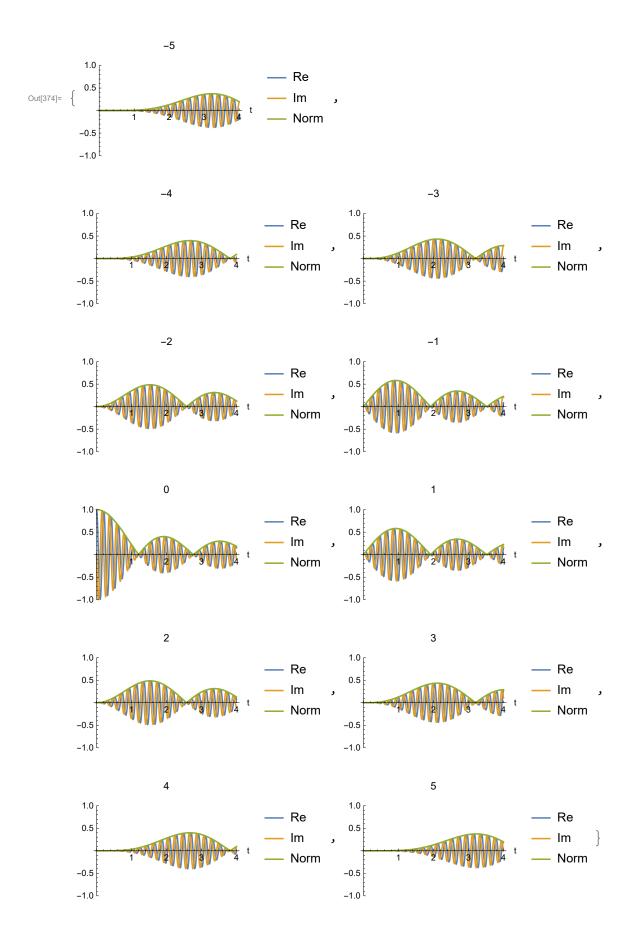
```
In[350]:= ClearAll@\psi;
       \mathsf{Ht}\,[\mathsf{Nl}_{\_},\,\omega_{\_},\,\,\mathsf{F}_{\_},\,\,\mathsf{t}_{\_}]\,:=\,
          Table[If[i = j, F*i*Cos[\omega*t], If[Abs[i-j] == 1, -1, 0]], \{i, 1, Nl\}, \{j, 1, Nl\}];
       N1 = 600;
       tf = 10;
       \omega = 0.01;
       F = 5;
       \psi 0 = \text{Table}[\text{If}[i = Nl/2, 1, 0], \{i, 1, Nl\}];
       s = NDSolve[\{ID[\psi[t], t] = Ht[Nl, F, \omega, t].\psi[t], \psi[0] = \psi0\}, \psi, \{t, 0, tf\}];
       \psi[t_{-}] = \text{Evaluate}[\psi[t] /. s];
In[359]:= tmax = 4;
       Table [Plot] {Re[\psi[t][[1, i]]], Im[\psi[t][[1, i]]], Norm[\psi[t][[1, i]]]},
           {t, 0, tmax}, PlotLegends \rightarrow {"Re", "Im", "Norm"}, PlotRange \rightarrow {-1, 1},
          AxesLabel \rightarrow {"t", ""}, PlotLabel \rightarrow i - N1/2, {i, N1/2 - 5, N1/2 + 5}]
```



```
In[361]:= sitenum = 598;
       tmax = 7;
       MatrixPlot[Table[Abs[\psi[t][[1, i]]],
          \{t, 0, tmax, 0.1\}, \{i, Nl/2 - sitenum/2, Nl/2 + sitenum/2\}],
        FrameLabel → {"t (100ms)", "site"}, ImageSize → Full]
                                           200
                                                                          400
                                                                                                        599
Out[363]= (100ms)
         20
                                                                                                           20
         40
                                                                                                           40
                                                                                                            60
                                           200
                                                                          400
                                                                                                        599
                                                          site
```

High freq, low A

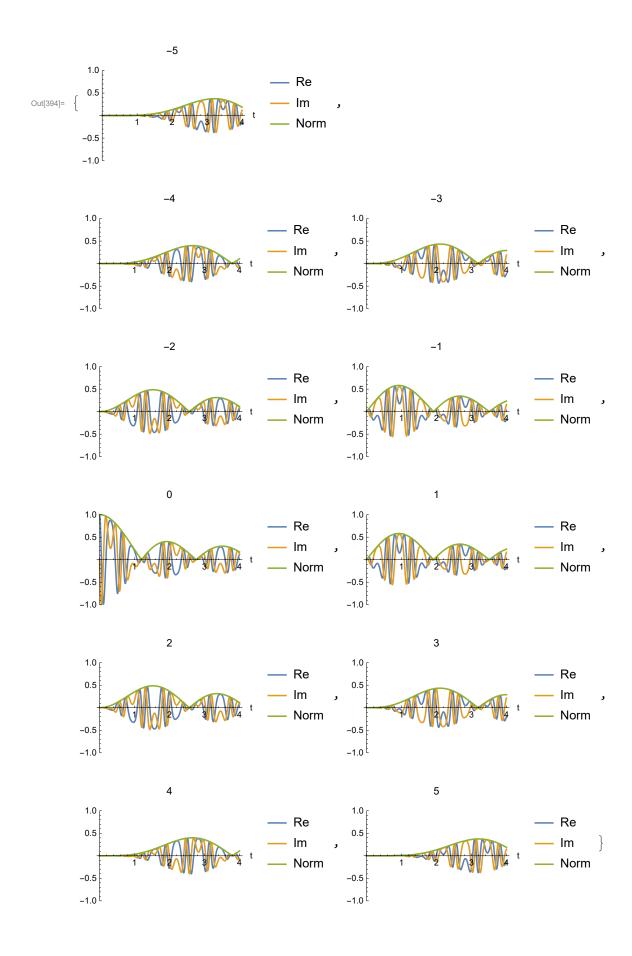
```
In[364]:= ClearAll@ψ;
       \mathsf{Ht}\,[\mathsf{Nl}_{\_},\,\omega_{\_},\,\,\mathsf{F}_{\_},\,\,\mathsf{t}_{\_}]\,:=\,
          Table[If[i = j, F*i*Cos[\omega*t], If[Abs[i-j] == 1, -1, 0]], \{i, 1, Nl\}, \{j, 1, Nl\}];
       tf = 10;
       \omega = 0.1;
       F = 0.01;
       \psi 0 = \text{Table}[\text{If}[i = Nl/2, 1, 0], \{i, 1, Nl\}];
       s = NDSolve[\{ID[\psi[t], t] = Ht[Nl, F, \omega, t].\psi[t], \psi[0] = \psi0\}, \psi, \{t, 0, tf\}];
       \psi[t_{-}] = \text{Evaluate}[\psi[t] /. s];
In[373]:= tmax = 4;
       Table [Plot] {Re[\psi[t][[1, i]]], Im[\psi[t][[1, i]]], Norm[\psi[t][[1, i]]]},
           {t, 0, tmax}, PlotLegends \rightarrow {"Re", "Im", "Norm"}, PlotRange \rightarrow {-1, 1},
          AxesLabel \rightarrow {"t", ""}, PlotLabel \rightarrow i - N1/2, {i, N1/2 - 5, N1/2 + 5}]
```



```
In[378]:= sitenum = 598;
       tmax = 7;
       MatrixPlot[Table[Abs[\psi[t][[1, i]]],
          \{t, 0, tmax, 0.1\}, \{i, Nl/2 - sitenum/2, Nl/2 + sitenum/2\}],
        FrameLabel → {"t (100ms)", "site"}, ImageSize → Full]
                                           200
                                                                         400
                                                                                                       599
Ont[380]= (100ms)
         20
                                                                                                           20
         40
                                                                                                           40
                                                                                                           60
                                           200
                                                                         400
                                                          site
```

High freq, high A

```
In[384]:= ClearAll@\psi;
       \mathsf{Ht}\,[\mathsf{Nl}_{\_},\,\omega_{\_},\,\,\mathsf{F}_{\_},\,\,\mathsf{t}_{\_}]\,:=\,
          Table[If[i = j, F * i * Cos[\omega * t], If[Abs[i - j] == 1, -1, 0]], {i, 1, Nl}, {j, 1, Nl}];
       tf = 10;
       \omega = 0.1;
       F = 5;
       \psi 0 = \text{Table}[\text{If}[i = Nl/2, 1, 0], \{i, 1, Nl\}];
       s = NDSolve[\{ID[\psi[t], t] = Ht[Nl, F, \omega, t].\psi[t], \psi[0] = \psi0\}, \psi, \{t, 0, tf\}];
       \psi[t_{-}] = \text{Evaluate}[\psi[t] /. s];
In[393]:= tmax = 4;
       Table [Plot] {Re[\psi[t][[1, i]]], Im[\psi[t][[1, i]]], Norm[\psi[t][[1, i]]]},
           {t, 0, tmax}, PlotLegends \rightarrow {"Re", "Im", "Norm"}, PlotRange \rightarrow {-1, 1},
          AxesLabel \rightarrow {"t", ""}, PlotLabel \rightarrow i - N1/2, {i, N1/2 - 5, N1/2 + 5}]
```



```
In[395]:= sitenum = 598;
       tmax = 7;
       MatrixPlot[Table[Abs[\psi[t][[1, i]]],
          {t, 0, tmax, 0.1}, {i, N1/2 - sitenum/2, N1/2 + sitenum/2}],
        FrameLabel → {"t (100ms)", "site"}, ImageSize → Full]
                                           200
                                                                         400
                                                                                                        599
Out[397]= (100ms)
         20
                                                                                                           20
         40
                                                                                                           40
                                                                                                           60
                                           200
                                                                         400
                                                          site
```

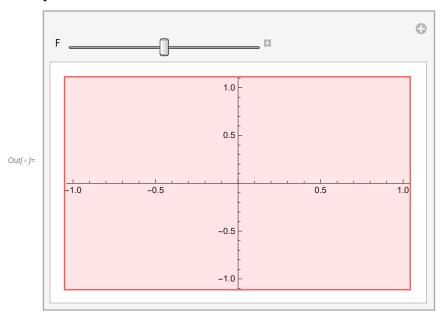
Random below..

```
(*Table[Plot[{Re[\psi[t][[i]]/.s}], Im[\psi[t][[i]]/.s], Norm[\psi[t][[i]]/.s]), Norm[[\psi[t][[i]]/.s]), Norm[[\psi[t][[i]]/.s]
                     {t, 0, 1}, PlotLegends→{"Re","Im","Norm"}], {i, 1, Nl}]
               Table [Plot[{Re[\psi[t][[i]]/.s], Im[\psi[t][[i]]/.s],Abs[\psi[t][[i]]/.s],
                       Norm[\psi[t][[i]]/.s]}, {i, 1, Nl}], {t, 0, 1, 0.1}]*)
 In[*]:= tt = Range[0, 1, 0.1]
            ww = Flatten[Evaluate[Abs[\psi[#]] /. s]] & /@ tt
            Plot[tt, ww[[All, 2]]]
             (*ListPlot[Table[Transpose[{tt, ww[[All, i]]}], {i, 3}]]
Outf = \{0., 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.\}
Out[*] = \{\{0., 0., 0., 0., 1., 0., 0., 0., 0., 0.\},\
                \{4.15962 \times 10^{-6}, 0.000166245, 0.00498335, 0.0995007, 0.990025, \}
                  0.0995007, 0.00498335, 0.000166245, 4.1582 \times 10<sup>-6</sup>, 8.34361 \times 10<sup>-8</sup>},
                \{0.0000662139, 0.00132003, 0.0197345, 0.196026, 0.960398, 0.196026,
                  0.0197345, 0.00132004, 0.0000661251, 2.65111 \times 10^{-6}},
                {0.000332449, 0.0043995, 0.0436643, 0.286699, 0.912006, 0.286699, 0.0436644,
                 0.00439955, 0.000331447, 0.0000199874, {0.00103847, 0.010246, 0.0758154,
                 0.368837, 0.846292, 0.368837, 0.0758154, 0.0102463, 0.0010329, 0.0000833934},
                {0.0024973, 0.0195605, 0.114898, 0.440042, 0.765209, 0.440042, 0.114898,
                 0.019562, 0.00247628, 0.000251213, {0.00508345, 0.0328656, 0.159339,
                 0.498277, 0.671155, 0.498277, 0.159339, 0.032871, 0.00502154, 0.000615288
                {0.00921334, 0.0504753, 0.20734, 0.541935, 0.566894, 0.541935, 0.207338,
                 0.0504908, 0.00905977, 0.00130516}, {0.0153233, 0.0724723, 0.256945,
                 0.569885, 0.455463, 0.569885, 0.256941, 0.072511, 0.0149876, 0.00248993,
                {0.0238457, 0.098695, 0.306117, 0.581513, 0.340075, 0.581514, 0.306107,
                  0.0987815, 0.0231796, 0.00437753, {0.0351842, 0.128736, 0.352809,
                  \{0.576736, 0.224011, 0.576738, 0.352787, 0.128913, 0.0339609, 0.00721095\}
             Plot: Range specification
```

{0., 0.000166245, 0.00132003, 0.0043995, 0.010246, 0.0195605, 0.0328656, 0.0504753, 0.0724723, 0.098695, 0.128736} is not of the form {x, xmin, xmax}.

Out[*]= Plot[tt, ww[All, 2]]

```
ln[\cdot]:= Manipulate [Module [\{\psi, \text{ sol, tmax = 20}\},
        sol = First@NDSolve[{ID[\psi[t], t] ==
               Ht[10, 0.05, F, t] .\psi[t], \psi[0] == psi0}, \psi, {t, 0, 1}];
        Plot [Chop[#] &@ (\psi /. sol) [t],
         \{t, 0, 1\}, PlotRange \rightarrow All\}
       ],
       {{F, 1}, 0, 2}
```



Dot: Tensors

 $0., -1, 0, 0, 0, 0\}, \{0, 0, 0, 0, -1, 0., -1, 0, 0, 0\}, \{0, 0, 0, 0, 0, -1, 0., 0., 0., 0., -1, 0.,$ incompatible shapes.

Dot: Tensors

NDSolve: Encountered non-numerical value for a derivative at t == 0.`.

ReplaceAll:

and so cannot be used for replacing.

{(0.

```
}} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for
```

replacing. ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0\} is neither a list of replacement rules nor a valid dispatch table, and so
 cannot be used for replacing.
```

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: There are more dependent variables, $\{Ht[10, 0.05, 0., t], \psi $10492[t]\}$, than equations, so the system is underdetermined.

ReplaceAll:

neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

 $\{(0.$

+1.i) ψ \$10492'[0.0000204286] == Ht[10., 0.05, 0., 0.0000204286]. ψ \$10492[0.0000204286], ψ \$10492[0.] == {0., 0. , 0,, 0., 1., 0., 0., 0., 0., 0., 0.} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

--- ReplaceAll:

 $\{i, \psi \} = \{i, \psi \} = \{i,$ list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- **NDSolve:** There are more dependent variables, {Ht[10, 0.05, 0., t], ψ \$21062[t]}, than equations, so the system is underdetermined.

ReplaceAll:

 $\{i, \psi$ \$21062'[0.0000204286] == Ht[10, 0.05, 0., 0.0000204286]. ψ \$21062[0.0000204286], ψ \$21062[0] == {0, 0, 0, 0, 1, 0, 0, 0, 0, 0} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

{(0.

- +1.i) ψ \$21062'[0.0000204286] == Ht[10., 0.05, 0., 0.0000204286]. ψ \$21062[0.0000204286], ψ \$21062[0.] == {0., 0. , 0., 0., 1., 0., 0., 0., 0., 0.} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

 $\{i, \psi$ 21062'[0.0204286] == Ht[10, 0.05, 0., 0.0204286]. ψ 221062[0.0204286], ψ 21062[0] == $\{0, 0, 0, 0, 1, 0, 0, 0, 0, 0\}$ is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- ... NDSolve: There are more dependent variables, {Ht[10, 0.05, 1.005, t], ψ \$21634[t]}, than equations, so the system is underdetermined.

ReplaceAll:

 $\{i, \psi$ 21634 $[0.0000204286] = Ht[10, 0.05, 1.005, 0.0000204286], <math>\psi$ 21634 $[0.0000204286], <math>\psi$ \$21634[0.0000204286]} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

 $\{(0, 0)\}$

+ 1.i) ψ \$21634'[0.0000204286] == Ht[10., 0.05, 1.005, 0.0000204286], ψ \$21634[0.0000204286], ψ \$21634[0.] == { 0., 0., 0., 0., 1., 0., 0., 0., 0., 0., 0.} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

 $\{i, \psi$ 21634'[0.0204286] == Ht[10, 0.05, 1.005, 0.0204286]. ψ 21634[0.0204286], ψ 21634[0] == $\{0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0\}$ is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
1, 0, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}\}. \\ \psi \$31817
       [0.0000204286], \psi$31817[0] == psi0} is neither a list of replacement rules nor a valid
  dispatch table, and so cannot be used for replacing.
```

{(0.

+1.i) ψ \$31817'[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0., 0.}, {0., -1. 0., 0., -1., 9.045, -1., $\{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}$. ψ \$31817[0.0000204286], ψ \$31817[0.] == psi0

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}, \psi$31817[
      0.0204286], \psi$31817[0] == psi0} is neither a list of replacement rules nor a valid dispatch
```

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- **NDSolve:** Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$40649
       [0.0000204286], \psi$40649[0] == psi0 is neither a list of replacement rules nor a valid
  dispatch table, and so cannot be used for replacing.
```

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

 $\{(0.$

```
0., 0., -1., 9.045, -1., \{0., 0., 0., 0., 0., 0., 0., 0., 1., 10.05\}. \psi$40649[0.0000204286], \psi$40649[0.] == psi0}
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

--- ReplaceAll:

```
0}, {0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0}, {0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1}, {0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05}}.\psi$40649[
      0.0204286], \psi$40649[0] == psi0} is neither a list of replacement rules nor a valid dispatch
```

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

```
1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$50407
       [0.0000204286], \psi$50407[0] == psi0} is neither a list of replacement rules nor a valid
  dispatch table, and so cannot be used for replacing.
```

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

{(0.

```
0., 0., -1., 9.045, -1.\}, \{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}\}.\psi \$50407[0.0000204286], \psi \$50407[0.] == psi0\}
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

--- ReplaceAll:

```
0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}\}. \\ \psi \$50407[
       0.0204286], \psi$50407[0] == psi0} is neither a list of replacement rules nor a valid dispatch
```

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}, \psi$31845
       [0.0000204286], \psi$31845[0] == psi0} is neither a list of replacement rules nor a valid
  dispatch table, and so cannot be used for replacing.
```

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

{(0.

```
+1.i) \psi$31845′[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
0., 0., -1., 9.045, -1.}, \{0., 0., 0., 0., 0., 0., 0., 0., 0., 1., 10.05}. \psi$31845[0.0000204286], <math>\psi$31845[0.] == psi0
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$31845[
       0.0204286], \psi$31845[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

```
General: Further output of ReplaceAll::reps will be suppressed during this calculation.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
General: Further output of ReplaceAll::argx will be suppressed during this calculation.
  NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.
ReplaceAll:
 [0.0000204286], \psi$35202[0] == psi0} is neither a list of replacement rules nor a valid
   dispatch table, and so cannot be used for replacing.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
ReplaceAll:
 {(0.
          +1.i) \psi$35202'[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
          0, 0, -1, 9.045, -1., \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$35202[0.0000204286], <math>\psi$35202[0.] == psi0
   is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
ReplaceAll:
 0}, {0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0}, {0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1}, {0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05}}.\psi$35202[
        0.0204286], \psi$35202[0] == psi0} is neither a list of replacement rules nor a valid dispatch
   table, and so cannot be used for replacing.
General: Further output of ReplaceAll::reps will be suppressed during this calculation.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
General: Further output of ReplaceAll::argx will be suppressed during this calculation.
NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.
ReplaceAll:
 1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}}. \psi$35375
        [0.0000204286], \psi$35375[0] == psi0} is neither a list of replacement rules nor a valid
   dispatch table, and so cannot be used for replacing.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
ReplaceAll:
 {(0.
```

0., 0., -1., 9.045, -1., $\{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}$. ψ \$35375[0.0000204286], ψ \$35375[0.] == psi0

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

```
0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}, \psi$35375[
       0.0204286], \psi$35375[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- ••• NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
1, 0, 0}, {0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0}, {0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1}, {0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05}}.\psi $35546
       [0.0000204286], \psi$35546[0] == psi0\} is neither a list of replacement rules nor a valid
  dispatch table, and so cannot be used for replacing.
```

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

 $\{(0.$

```
+1.i) \psi$35546′[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
0., 0., -1., 9.045, -1., \{0., 0., 0., 0., 0., 0., 0., -1., 10.05\}. \psi$35546[0.0000204286], \psi$35546[0.] == psi0
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$35546[
       0.0204286], \psi$35546[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
-1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}\}. \psi$3561[
       0.0000204286], \psi$3561[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

 $\{(0.$

0., -1., 9.045, -1., $\{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}$. ψ3561[0.0000204286]$, ψ3561[0.] == psi0$

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0}, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}}. \psi$3561[
      0.0204286], \psi$3561[0] == psi0} is neither a list of replacement rules nor a valid dispatch
```

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
-1, 0, 0}, {0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0}, {0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1}, {0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05}}.\psi$5884[
       0.0000204286], \psi$5884[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

 $\{(0.$

```
0., -1., 9.045, -1., \{0., 0., 0., 0., 0., 0., 0., -1., 10.05\}. \psi$5884[0.0000204286], <math>\psi$5884[0.] == psi0
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

--- ReplaceAll:

```
0}, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}}. \psi$5884[
      0.0204286], \psi$5884[0] == psi0} is neither a list of replacement rules nor a valid dispatch
```

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

1, 0, 0, $\{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}$, $\{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}$, $\{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}$. ψ \$11990 [0.0000204286], ψ \$11990[0] == psi0} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

{(0.

```
0., 0., -1., 9.045, -1.\}, \{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}\}.\psi \$11990[0.0000204286], \psi \$11990[0.] == psi0\}
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

--- ReplaceAll:

```
0\}, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}\}. \\ \psi\$11990[
       0.0204286], \psi$11990[0] == psi0} is neither a list of replacement rules nor a valid dispatch
```

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
[0.0000204286], \psi$16791[0] == psi0} is neither a list of replacement rules nor a valid
 dispatch table, and so cannot be used for replacing.
```

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

{(0.

```
+1.i) \psi$16791′[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
0., 0., -1., 9.045, -1.}, \{0., 0., 0., 0., 0., 0., 0., 0., 0., 1., 10.05}. \psi$16791[0.0000204286], \psi$16791[0.] == psi0}
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}, \psi$16791[
       0.0204286], \psi$16791[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

```
General: Further output of ReplaceAll::reps will be suppressed during this calculation.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
General: Further output of ReplaceAll::argx will be suppressed during this calculation.
  NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.
ReplaceAll:
 1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}, \psi$24418
         [0.0000204286], \psi$24418[0] == psi0} is neither a list of replacement rules nor a valid
    dispatch table, and so cannot be used for replacing.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
ReplaceAll:
 {(0.
          +1.i) \psi$24418'[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
          0, 0, -1, 9.045, -1., \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$24418[0.0000204286], \psi$24418[0.] == psi0
   is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
ReplaceAll:
 0}, {0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0}, {0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1}, {0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05}}.\psi$24418[
         0.0204286], \psi$24418[0] == psi0} is neither a list of replacement rules nor a valid dispatch
    table, and so cannot be used for replacing.
General: Further output of ReplaceAll::reps will be suppressed during this calculation.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
General: Further output of ReplaceAll::argx will be suppressed during this calculation.
NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.
ReplaceAll:
 1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}}. \psi$24524
         [0.0000204286], \psi$24524[0] == psi0} is neither a list of replacement rules nor a valid
    dispatch table, and so cannot be used for replacing.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
ReplaceAll:
 {(0.
```

0., 0., -1., 9.045, -1., $\{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}$. ψ \$24524[0.0000204286], ψ \$24524[0.] == psi0

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

```
0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$24524[
       0.0204286], \psi$24524[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- ••• NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
[0.0000204286], \psi$24632[0] == psi0} is neither a list of replacement rules nor a valid
 dispatch table, and so cannot be used for replacing.
```

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

 $\{(0.$

```
+1.i) \psi$24632'[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
0., 0., -1., 9.045, -1., \{0., 0., 0., 0., 0., 0., 0., -1., 10.05\}. \psi$24632[0.0000204286], \psi$24632[0.] == psi0
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$24632[
       0.0204286], \psi$24632[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$25687
       [0.0000204286], \psi$25687[0] == psi0} is neither a list of replacement rules nor a valid
  dispatch table, and so cannot be used for replacing.
```

 $\{(0.$

+1.i) ψ \$25687'[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0., 0.}, {0., -1. 0., 0., -1., 9.045, -1., $\{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}$. ψ \$25687[0.0000204286], ψ \$25687[0.] == psi0

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

0, $\{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}$, $\{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}$, $\{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}$. ψ \$25687[0.0204286], ψ \$25687[0] == psi0} is neither a list of replacement rules nor a valid dispatch

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- **NDSolve:** Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

1, 0, 0, $\{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}$, $\{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}$, $\{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}$. ψ \$25887 [0.0000204286], ψ \$25887[0] == psi0} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

 $\{(0.$

0., 0., -1., 9.045, -1., $\{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}$. ψ \$25887[0.0000204286], ψ \$25887[0.] == psi0

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

--- ReplaceAll:

```
0}, {0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0}, {0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1}, {0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05}}.\psi$25887[
      0.0204286], \psi$25887[0] == psi0} is neither a list of replacement rules nor a valid dispatch
```

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

1, 0, 0}, {0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0}, {0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1}, {0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05}}.\psi \psi 26085 [0.0000204286], ψ \$26085[0] == psi0} is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

{(0.

 $+\ 1.\ \emph{i})\ \psi\$26085'[0.0000204286] == \{\{1.005, -1., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0.\}, \\ \{-1., \, 2.01, \, -1., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0.\}, \\ \{0., \, -1., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0.\}, \\ \{0., \, -1., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0., \, 0.\}, \\ \{0., \, -1., \, 0., \,$ $0., 0., -1., 9.045, -1.\}, \{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}\}.\psi\$26085[0.0000204286], \psi\$26085[0.] == psi0\}$

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

--- ReplaceAll:

```
0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}\}. \\ \psi \$26085[
       0.0204286], \psi$26085[0] == psi0} is neither a list of replacement rules nor a valid dispatch
```

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
[0.0000204286], \psi$26256[0] == psi0} is neither a list of replacement rules nor a valid
 dispatch table, and so cannot be used for replacing.
```

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

{(0.

```
+1.i) \psi$26256′[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
0, 0, -1, 9.045, -1., \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$26256[0.0000204286], \psi$26256[0.] == psi0
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$26256[
       0.0204286], \psi$26256[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

```
General: Further output of ReplaceAll::reps will be suppressed during this calculation.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
General: Further output of ReplaceAll::argx will be suppressed during this calculation.
   NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.
ReplaceAll:
 1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}, \psi$28828
         [0.0000204286], \psi$28828[0] == psi0} is neither a list of replacement rules nor a valid
    dispatch table, and so cannot be used for replacing.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
ReplaceAll:
 {(0.
           +1.i) \psi$28828'[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
           0, 0, -1, 9.045, -1., \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$28828[0.0000204286], \psi$28828[0.] == psi0
    is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
ReplaceAll:
 0}, {0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0}, {0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1}, {0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05}}.\psi$28828[
         0.0204286], \psi$28828[0] == psi0} is neither a list of replacement rules nor a valid dispatch
    table, and so cannot be used for replacing.
General: Further output of ReplaceAll::reps will be suppressed during this calculation.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
General: Further output of ReplaceAll::argx will be suppressed during this calculation.
NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.
ReplaceAll:
 1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}}. \psi$28997
         [0.0000204286], \psi$28997[0] == psi0} is neither a list of replacement rules nor a valid
    dispatch table, and so cannot be used for replacing.
ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
ReplaceAll:
 {(0.
```

0., 0., -1., 9.045, -1., $\{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}$. ψ \$28997[0.0000204286], ψ \$28997[0.] == psi0 is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

```
0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}, \psi$28997[
       0.0204286], \psi$28997[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- ••• NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$30141
       [0.0000204286], \psi$30141[0] == psi0} is neither a list of replacement rules nor a valid
  dispatch table, and so cannot be used for replacing.
```

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

 $\{(0.$

```
+1.i) \psi$30141′[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
0, 0, -1, 9.045, -1., \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}, \psi$30141[0.000204286], <math>\psi$30141[0.] == psi0
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}, \psi$30141[
       0.0204286], \psi$30141[0] == psi0} is neither a list of replacement rules nor a valid dispatch
  table, and so cannot be used for replacing.
```

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: Initial condition psi0 is not a number or a rectangular array of numbers.

ReplaceAll:

```
1, 0, 0, \{0, 0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$30273
       [0.0000204286], \psi$30273[0] == psi0} is neither a list of replacement rules nor a valid
  dispatch table, and so cannot be used for replacing.
```

```
ReplaceAll:
```

{(0.

```
+1.i) \psi$30273′[0.0000204286] == {{1.005, -1., 0., 0., 0., 0., 0., 0., 0., 0., 0.}, {-1., 2.01, -1., 0., 0., 0., 0., 0., 0., 0., 0.}, {0., -1.
0., 0., -1., 9.045, -1., \{0., 0., 0., 0., 0., 0., 0., 0., -1., 10.05\}. \psi$30273[0.0000204286], <math>\psi$30273[0.] == psi0
```

is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.

ReplaceAll:

```
0, \{0, 0, 0, 0, 0, 0, -1, 8.04, -1, 0\}, \{0, 0, 0, 0, 0, 0, 0, -1, 9.045, -1\}, \{0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1, 10.05\}. \psi$30273[
      0.0204286], \psi$30273[0] == psi0} is neither a list of replacement rules nor a valid dispatch
```

table, and so cannot be used for replacing.

- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.

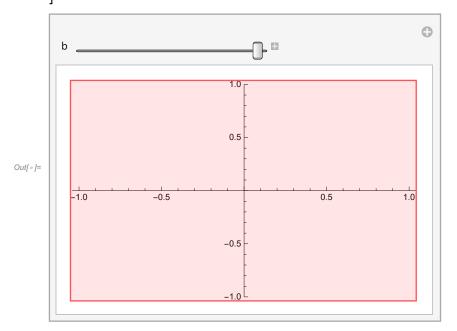
Create U

```
In[*]:= ClearAll@constructU;
    constructU[h_, tinit_, tfinal_, n_] := Module[{dt = N[(tfinal - tinit) / n],
        curVal = IdentityMatrix[Length@h[0]]},
       Do[curVal = MatrixExp[-I*h[t]*dt].curVal, {t, tinit, tfinal - dt, dt}];
       curVal]
    N1 = 10;
    psi0 = Table[If[i == N1 / 2, 1, 0], {i, 1, N1}];
    constructU[Ht[Nl, 0.01, 0. x 10], 0, 0.1, 10].psi0
     (*ListLinePlot[
     Chop[constructU[Ht[Nl,0.01, 0, 10], 0, 0.1, 10]].psi0, PlotRange \rightarrow All] *)
     (*ListPlot[sortedEVecs[[1]],PlotRange→All],*)
In[@]:= ListPlot[
     Table[Chop[constructU[Ht[Nl, 0.01, 0.01, #].psi0 &, 0, upt, 100]],
       {upt, .1, 1, .1}
     ],
     Joined → True,
     PlotRange \rightarrow \{-1, 1\}
    ]
```

```
ListPlot[
   Table
     Chop[#] &@ (constructU[
         Ht[N1, 0.05, F, #] &, 0, upt, 100].psi0),
     {upt, .01, 20, .1}
    ,
   Joined → True,
   PlotRange \rightarrow {-1, 1}
  ham[e1_, e2_, b_, omega_, t_] := \{\{e1, b*Cos[omega*t]\}, \{b*Cos[omega*t], e2\}\};
  Module[\{\psi, \text{ sol, tmax} = 20\},
   sol = NDSolve[
       \{ID[\psi[t], t] = Ht[10, 0.05, 0.05, t] \cdot \psi[t], \psi[0] = psi0\}, \psi, \{t, 0, tMax\}];
  Module [\{\psi, \text{ sol, tmax} = 20\},
   sol = First@NDSolve[{ID[\psi[t], t] ==
          Ht[10, 0.05, 0.05, t] .\psi[t], \psi[0] = psi0, \psi, {t, 0, tMax}];
   Plot Chop [#*. PauliMatrix [3].#] &@ (\psi /. sol) [t],
     \{t, 0, tMax\}, PlotRange \rightarrow \{-1, 1\}
  1
Create U (2x2)
  ham[e1_, e2_, b_, omega_, t_] := \{ \{e1, b * Cos[omega * t]\}, \{b * Cos[omega * t], e2\} \}
  ClearAll@constructU;
  constructU[h_, tinit_, tfinal_, n_] := Module[{dt = N[(tfinal - tinit) / n],
      curVal = IdentityMatrix[Length@h[0]]},
     Do[curVal = MatrixExp[-I*h[t]*dt].curVal, {t, tinit, tfinal - dt, dt}];
     curVal]
  ClearAll[cU, psi0];
  psi0 = \{1., 0\};
  Manipulate[
   ListPlot[
     Table
      Chop[#*.PauliMatrix[3].#] &@(constructU[
          ham[-1., 1., b, 1., #] &, 0, upt, 100].psi0),
      {upt, .01, 20, .1}
     ],
     Joined → True,
     PlotRange \rightarrow {-1, 1}
    ],
    {b, 0, 2}
```

NDsolve (2x2)

```
ln[\cdot]:= Manipulate [Module [\{\psi, \text{ sol, tmax = 20}\},
        sol = First@NDSolve[{ID[\psi[t], t] ==
               ham[-1, 1, b, 1, t] \cdot \psi[t], \psi[0] = \{1, 0\}\}, \psi, \{t, 0, 1\}];
        Plot Chop [#*. PauliMatrix [3].#] &@ (\psi /. sol) [t],
          \{t, 0, 1\}, PlotRange \rightarrow \{-1, 1\}
       ],
       {{b, 1}, 0, 2}
```



- NDSolve: There are more dependent variables, {ham[-1, 1, 2., 1, t], ψ\$3484[t]}, than equations, so the system is
- ReplaceAll: $\{i \ \psi$3484'[0.0000204286] == \text{ham}[-1, 1, 2, 1, 0.0000204286].\psi$3484[0.0000204286], \psi$3484[0] == \{1, 0\}\} \text{ is }$ neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- ReplaceAll:
- $\{(0. + 1.i)\ \psi$3484'[0.000204286] == ham[-1., 1., 2., 1., 0.0000204286].\psi$3484[0.0000204286], \psi$3484[0.] == \{1., 0.\}\}$ is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- ReplaceAll:
- $\{(0.+1.\bar{n})\ \psi\$3484'[0.0000204286] == ham[-1.,1.,2.,1.,0.0000204286].\psi\$3484[0.0000204286],\ \psi\$3484'[0.] == \{1.,0.\}\}\ is\ neither\ all the properties of t$ list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.
- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- General: Further output of ReplaceAll::argx will be suppressed during this calculation.
- NDSolve: There are more dependent variables, $\{\text{ham}[-1, 1, 2., 1, t], \psi$23790[t]\}$, than equations, so the system is underdetermined.
- ReplaceAll: $\{i, \psi$23790'[0.0000204286] == \text{ham}[-1, 1, 2., 1, 0.0000204286]. \psi$23790[0.0000204286], \psi$23790[0] == \{1, 0\}\}$ is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.

- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- ReplaceAll:
- $\{(0. + 1.i) \ \psi \$23790'[0.0000204286] == ham[-1, 1., 2., 1., 0.0000204286]. \\ \psi \$23790[0.0000204286], \ \psi \$23790[0.] == \{1., 0.\} \}$ is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- ReplaceAll:
- $\{(0. + 1.i) \ \psi \$23790'[0.0000204286] == ham[-1, 1., 2., 1., 0.0000204286]. \\ \psi \$23790[0.0000204286], \ \psi \$23790[0.] == \{1., 0.\} \}$ is neither a list of replacement rules nor a valid dispatch table, and so cannot be used for replacing.
- General: Further output of ReplaceAll::reps will be suppressed during this calculation.
- ReplaceAll: ReplaceAll called with 2 arguments; 1 argument is expected.
- ... General: Further output of ReplaceAll::argx will be suppressed during this calculation.