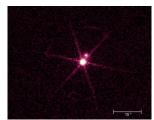


White Dwarfs



Sirius A+B: Chandra (X-rays; WD is bright)



McDonald Observatory (optical; WD is faint)

White Dwarfs

White Dwarfs: Sirius B

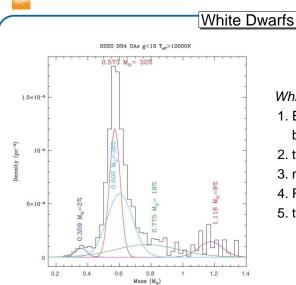
- Companion to the brightest star Sirius
- cannot be seen with the naked eye.
- Analyzing the motion of Sirius from 1833 to 1844, Friedrich Wilhelm Bessel (1844) concluded that Sirius must have an unseen companion.

11-2

- Sirius B was not actually observed until 1862 January 31 by Alvan Graham Clark.
- Star B's peculiar high temperature, small size, and great density were not established until 1925 by Walter Adams.

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11–3



mass distribution of 1733 white dwarfs (Kepler et al. 2007, MNRAS 375, 1315)

White Dwarfs

- 1. End stages of evolution of stars born with $M\lesssim$ 8 M_{\odot}
- 2. typically $M \sim$ 0.6 M_{\odot}
- 3. mainly consist of C and O
- 4. Radius \sim Earth
- 5. typical density $ho \sim 10^6\,\mathrm{g\,cm^{-3}}$

White Dwarf Stars in M4
PRC95-32 · ST Sci OPO · August 28, 1995 · H. Bond (ST Sci), NASA

HST · WFPC2

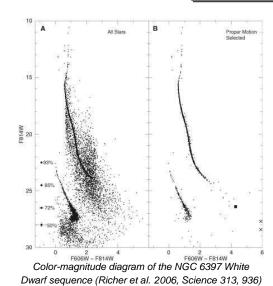
White Dwarfs

End-Stages of Stellar Evolution



11-6

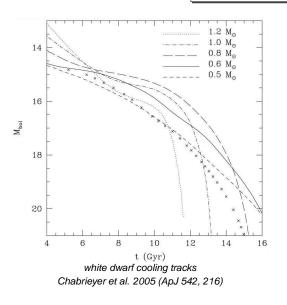
White Dwarfs



globular clusters are the oldest building blocks of the Galaxy

- \Longrightarrow many stars have already died
- ⇒ GCs must host a large number of white dwarfs





- white dwarfs are stabilized by the pressure of the degenerate electron gas
- they can not shrink
- cooling of the ionic gas takes a very long time
- at low temperature: crystalization, crystal structure similar to diamond

White dwarfs are diamonds in the sky

White Dwarfs



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11-7

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White Dwarfs

11-8

5

White Dwarfs

For a degenerate gase, the equation of state: $(P = P(T, \rho))$ is

$$P \propto \begin{cases} \rho^{5/3} & \text{(non-relativistic)} \\ \rho^{4/3} & \text{(relativistic)} \end{cases} \tag{11.1}$$

independent of T!

WD structure can be determined from hydrostatic equilibrium alone:

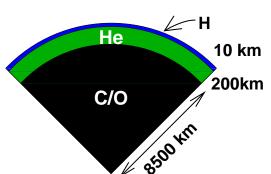
Mass structure (mass conservation)

$$\frac{\mathrm{d}M}{\mathrm{d}r} = 4\pi r^2 \rho(r)$$

Pressure structure (hydrostatic equilibrium)

$$\frac{\mathrm{d}P}{\mathrm{d}r} = -\rho(r)\frac{GM(r)}{r^2}$$

White Dwarfs



White dwarfs come in two flavors:

DA: H present in spectrum $(\sim 80\% \text{ of all WD})$

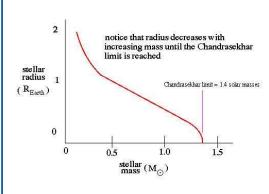
DB: He present in spectrum (\sim the rest) plus a few oddballs

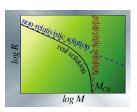
Structure: gravitationally settled, so DB's really do not have any H since it would "swim on top"

⇒ layered, "onion-like" structure

White Dwarfs

Mass-Radius Relation for White Dwarfs





- Subrahmanyan Chandrasekhar, 1910–1995
- Nobel prize 1983
- \bullet Radius decreases with increasing mass: $R \propto M^{-1/3}$
- Chandrasekhar limit: relativistic limit:

Mass must be less than 1.4 M_{\odot}

White Dwarfs



11-11

Neutron Stars

Neutron stars form after the core collapse of massive stars.

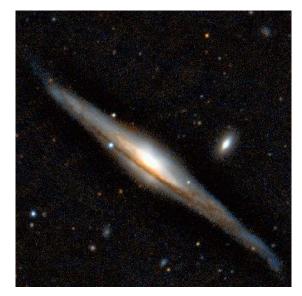
See later for physics of supernovae.

During the collapse the densities get so high that neutronization sets in:

$$p + e^- \longrightarrow n + \nu_e$$

General properties:

- Pressure mainly through degenerate neutrons (similar to degenerate electrons for WD!).
- ullet Typical density: $ho \sim 10^{14}\,\mathrm{g\,cm^{-3}}$ (nuclear densities)
- Typical radius: 10...15 km (Innsbruck-Wattens)
- surface gravity ~10¹¹ × Earth
- Detailed structure not yet fully understood



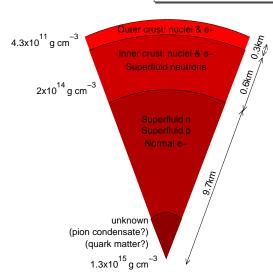
Type II SN2001cm in NGC5965 (2.56 m NOT, Håkon Dahle; NORDITA)

Evolution of more massive stars: fusion up to 56 Fe, then no energy gain \implies no pressure balance in centre \implies supernova explosion of type II. energy release: 10^{46} W ($10^{20}L_{\odot}$; about 1% in light, rest in neutrinos)



11-12

Neutron Stars: Structure



Crust: perhaps crystallized?

Atoms become elongated along B-field line on surface

Internal structure unclear:

- Supraconducting matter
- Suprafluidity (i.e., fluid with no viscosity)
- central composition unknown

(after Shapiro & Teukolsky)

Neutron Stars: Rotation

During collapse, angular momentum is conserved (Explosion: symmetric) Total angular momentum of homogeneous sphere:

$$J = I\omega$$
 where $I = \frac{2}{5}MR^2$

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$$\frac{2}{5} M_{\rm before} R_{\rm before}^2 \omega_{\rm before} = \frac{2}{5} M_{\rm NS} R_{\rm NS}^2 \omega_{\rm NS}$$

$$\omega_{\rm NS} = \left(\frac{M_{\rm before}}{M_{\rm NS}}\right) \left(\frac{R_{\rm before}}{R_{\rm NS}}\right)^2 \omega_{\rm before} \quad {\rm or} \quad P_{\rm NS} \sim \left(\frac{R_{\rm NS}}{R_{\rm before}}\right)^2 P_{\rm before}$$

(where *P*: rotation period)

Neutron Stars



11 - 13

3

Neutron Stars



11-14

Neutron Stars: Rotation

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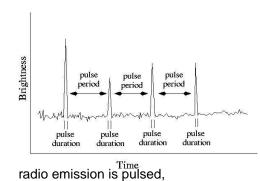
(where P: rotation period)

Example: $R_{\rm before} =$ 700000 km (Sun), $R_{\rm NS} =$ 15 km, $P_{\rm Sun} =$ 27 d $\Longrightarrow P_{\rm NS} =$ 0.001 s

Neutron Stars are extremely fast rotators.

close to break-up speed!

Pulsars



very short periods: milliseconds to a few seconds

Neutron Stars

5

Neutron Stars

Radio Pulsar

Discovery: Bell & Hewish (1967):

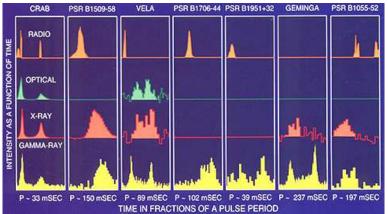
6

11–15



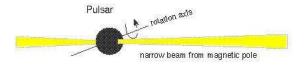
Pulsars

Pulsars at different wavelengths



Pulsations not only in the radio regime, but also at optical, X-ray, and γ -ray wavelength, but not in all cases.

Pulsars



If the narrow synchrotron beam passes over the Earth, we see the neutron star flash on and off like a lighthouse beam does for ships at sea.

Pulses due to the lighthouse effect caused by rapid rotation.

Rotation period:

$$P = \frac{2\pi R}{v_{\text{rot}}} \tag{11.2}$$

Earth

Rotation speed at the surface must be smaller the speed of light. $\Longrightarrow R < \frac{Pc}{2\pi}$

Shortest periods observed: $P\sim$ 1 ms

 $\Longrightarrow R <$ 50 km

Pulsars are neutron stars!

Neutron Stars





Neutron Stars



11–18

Pulsars

Another conserved observable: magnetic flux: $\Phi = BR^2$

Magnetic field after SN:

$$B_{\rm NS} = \left(\frac{R_{\rm before}}{R_{\rm NS}}\right)^2 B_{\rm before}$$

 \Longrightarrow neutron stars have strong magnetic fields (typical: $B \sim 10^6 \dots 10^8 \, \text{T}$)

Radio pulsars are fast rotating (isolated) neutron stars with strong magnetic fields.

Black Holes

Degenerate neutron gas: Chandrasekhar theory applies.

However, modified hydrostatic equation (GRT)

equation of state much more complicated than for white dwarfs

Neutron stars also have upper mass limit: Oppenheimer Volkoff limit.

Detailed mass limit unknown, causality considerations give $M\sim 3\,M_\odot$ (for "stiff equation of state" the sound speed becomes greater than speed of light at this mass)

Compact objects with mass above Oppenheimer Volkoff limit: Black Holes

More conservative astronomers: "Black Hole Candidates".

"Lighthouse model" for pulsars

Axis of

Rotation

Radiation beam

Radiation

beam

11–19

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11-20

Black Holes

In more modern usage (but still Newtonian!):

Total energy of a mass m:

$$E = E_{\text{pot}} + E_{\text{kin}} = -\frac{GMm}{R} + \frac{1}{2}mv^2$$

Mass m is unbound if E > 0, i.e., for

$$v \ge v_{\rm escape} = \sqrt{\frac{2GM}{R}}$$

Black Hole: Body of mass M and radius R for which $v_{\rm escape}>c$, where c is the speed of light.

This is the case if

$$R \leq R_{\rm S} = \frac{2GM}{c^2} \sim 3\,{\rm km}\frac{M}{M_{\odot}}$$

the Schwarzschild Radius.

Einstein

Special Relativity (1905):

- Speed of light has the same value in all frames of reference
- Observer with constant velocity measure the same physical laws

From these axioms follows:

- \Longrightarrow Space and time are relative ("4D-space-time")
- $\Longrightarrow E = mc^2$

("Mass and Energy are equivalent")



Albert Einstein (1879-1955)

Black Holes



Black Holes

2

11-20

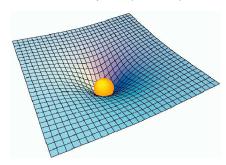


11-20

Einstein

General relativity (1916):

Mass curves space ("Metric")





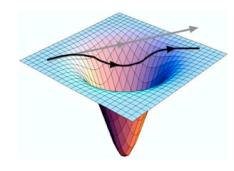


Albert Einstein (1879-1955)

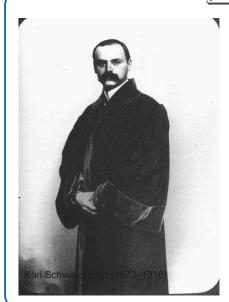
Einstein

General relativity (1916):

- Mass curves space ("Metric")
- Light moves through curved space



post-Einstein



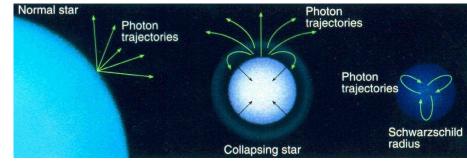
Directly after publication of GRT:

$$\mathrm{d}s^2 = \left(1 - \frac{2GM}{c^2r}\right)c^2\mathrm{d}t^2 - \left(1 - \frac{2GM}{c^2r}\right)^{-1}\mathrm{d}r^2$$

(Schwarzschild Metric).

Describes "shape of space" in vicinity of mass M.

post-Einstein



 $R > R_{\rm S}$

 $R \sim R_{\rm S}$

 $R < R_{\rm S}$

11-22

Behavior of light is determined from location of emission, in dependence from the Schwarzschild Radius:

$$R_{\mathrm{S}} = rac{2GM}{c^2} \sim 3\,\mathrm{km}\,rac{M}{M_{\odot}}$$

Same value as in Newtonian derivation!

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Black Holes



11-22

6

Normal star Photon trajectories Photon trajectories Photon trajectories Schwarzschild radius Collapsing star

post-Einstein

 $R>R_{\rm S}$

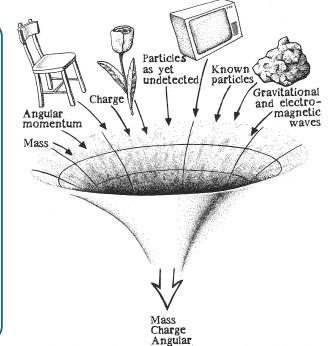
 $R \sim R_{\rm S}$

 $R < R_{\rm S}$

Black hole in GRT: Bodies smaller than their Schwarzschild radius.

J.N. Imamura

Black Holes



momentum

Black holes are very simple physical objects, determined

- Mass
- (Charge)
- Angular momentum

Black Holes