

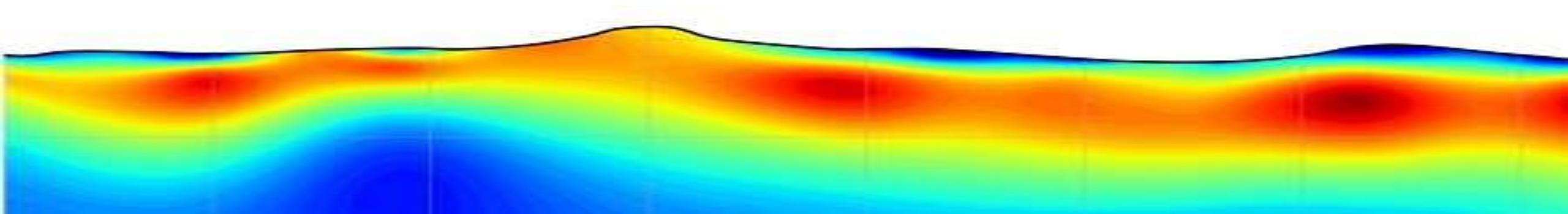
# ESS302 Applied Geophysics II

Gravity, Magnetic, Electrical, Electromagnetic and Well Logging

## Gravity Wrap-up

Instructor: Dikun Yang

Feb – May, 2020



# The Amazing World of Gravity

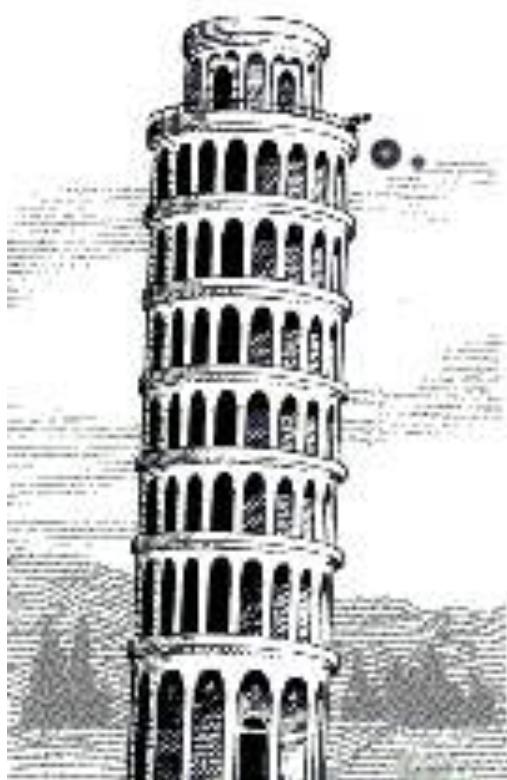
Learn from YouTube [https://youtu.be/2\\_p2ELD7npw](https://youtu.be/2_p2ELD7npw)



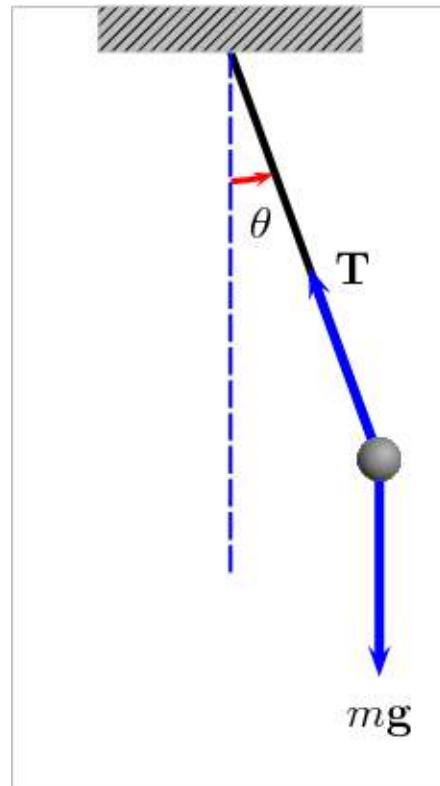
# How to Measure the Gravity Field



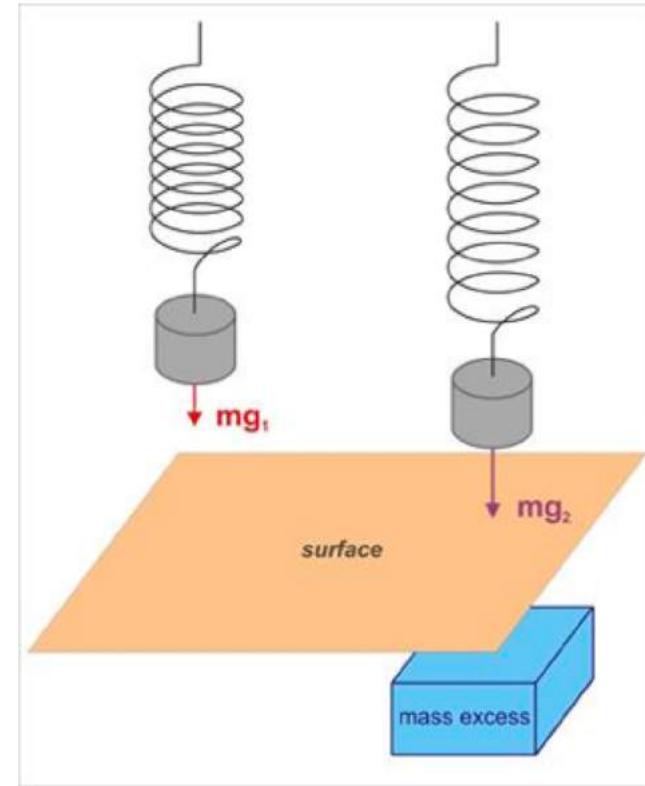
# Measurement of Gravity Field



Free fall  
(absolute)

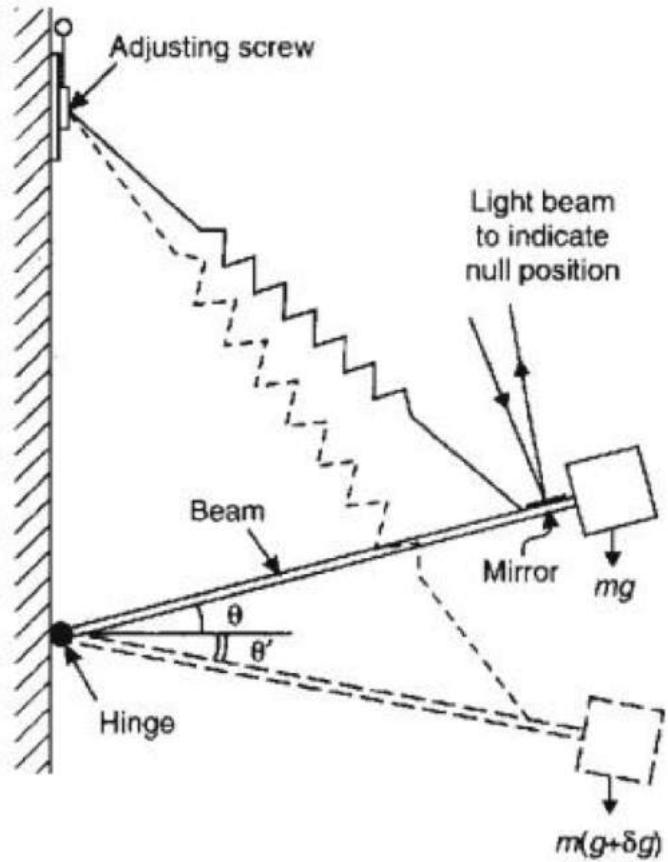


Pendulum  
(absolute)



Spring  
(relative)

# LaCoste-Romberg Gravimeter



# The Amazing World of Gravity

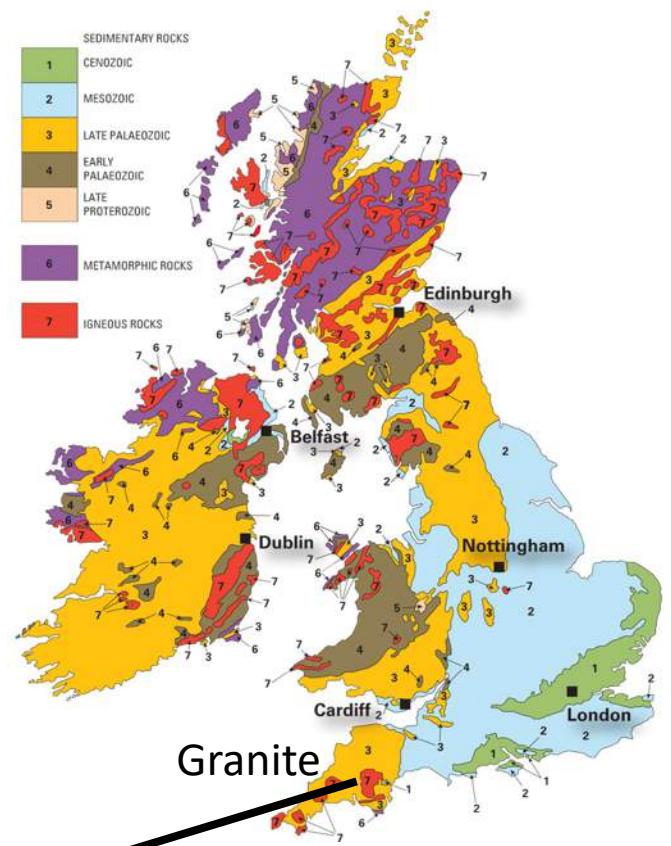


Learn from YouTube

[https://youtu.be/2\\_p2ELD7npw](https://youtu.be/2_p2ELD7npw)

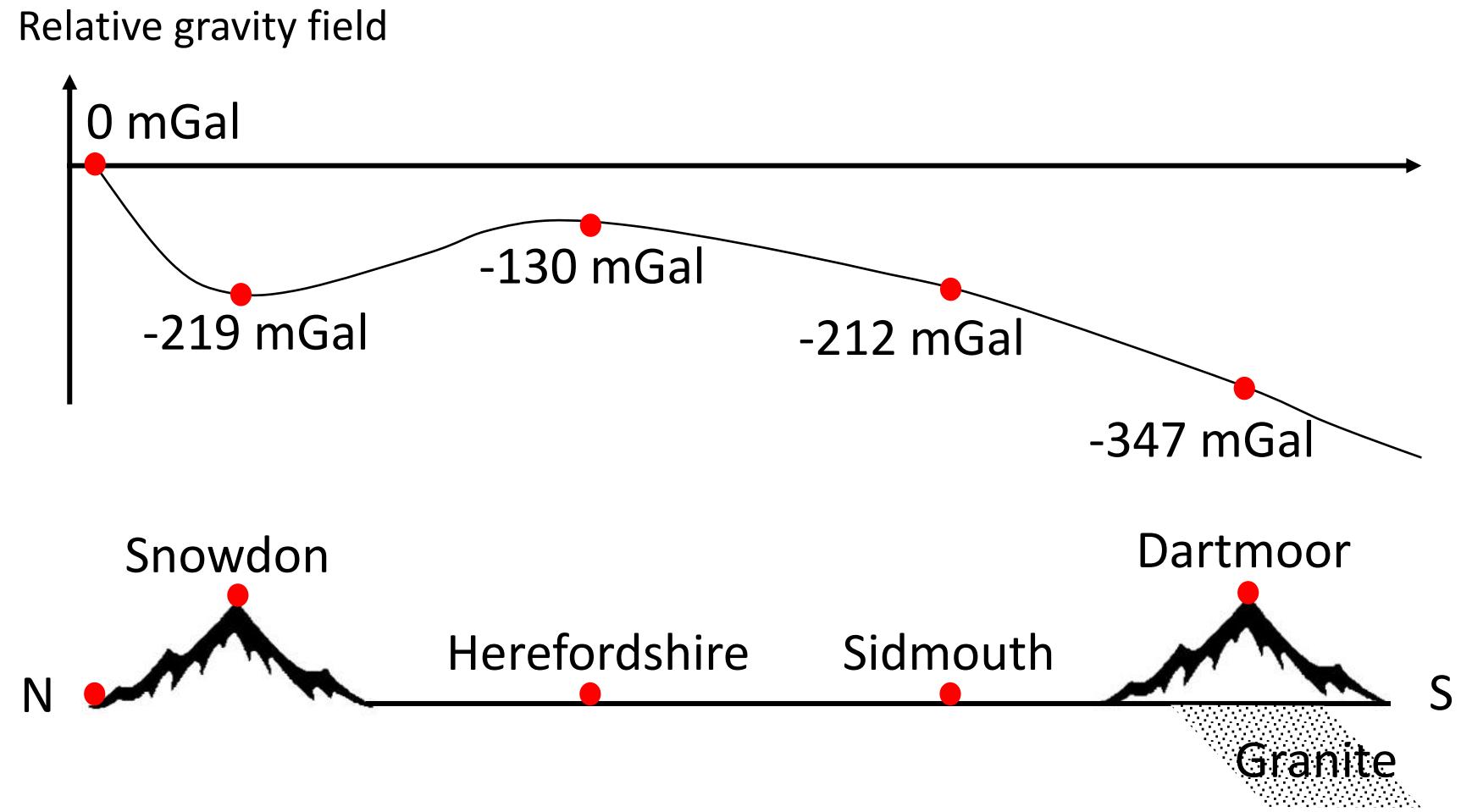
According to the video, what are the factors that affect the gravitational force exerted on us?

# The Amazing World of Gravity



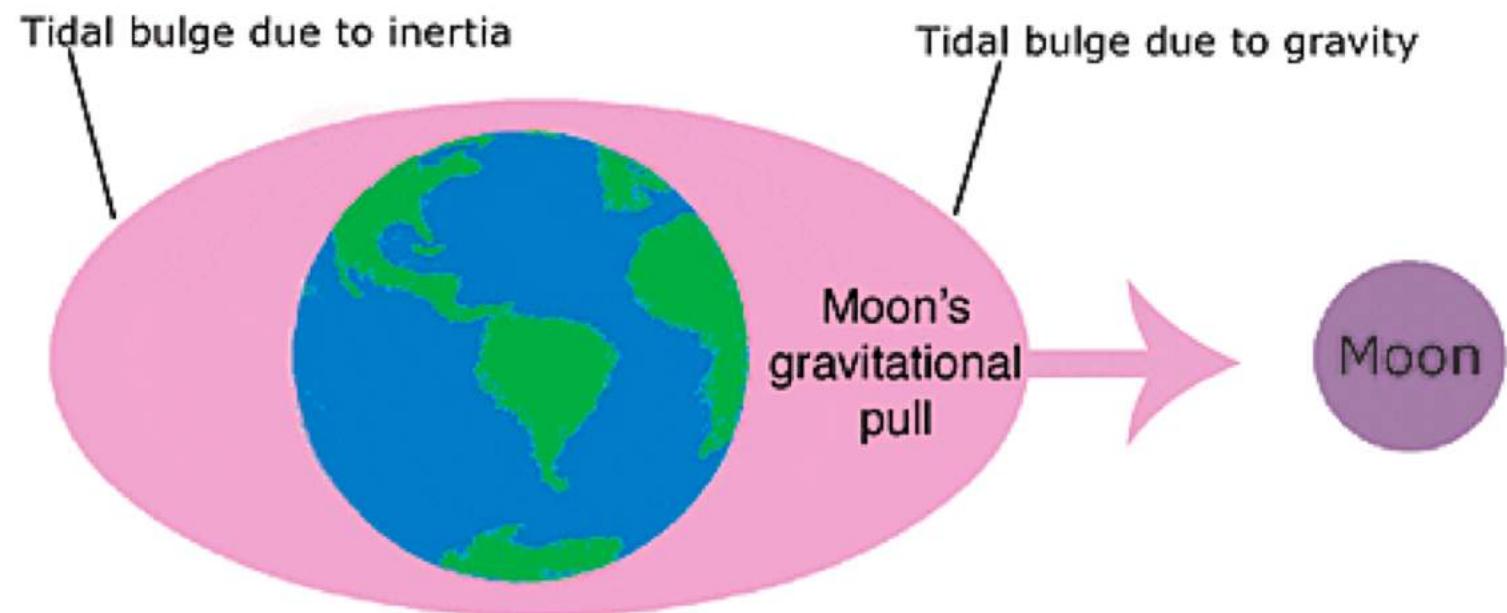
Applied geophysicist:  
Maybe we can use the gravity field to  
find something that is not as apparent  
as altitude and latitude?

# The Amazing World of Gravity



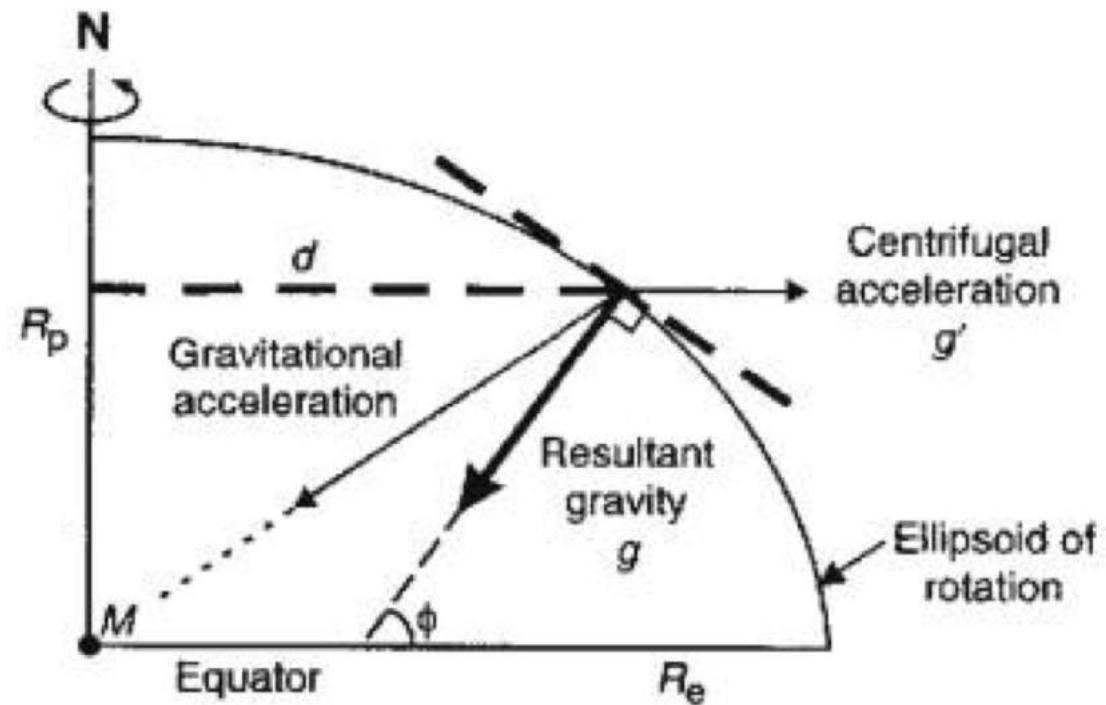
# Gravity Data Correction

- Tidal correction



# Gravity Data Correction

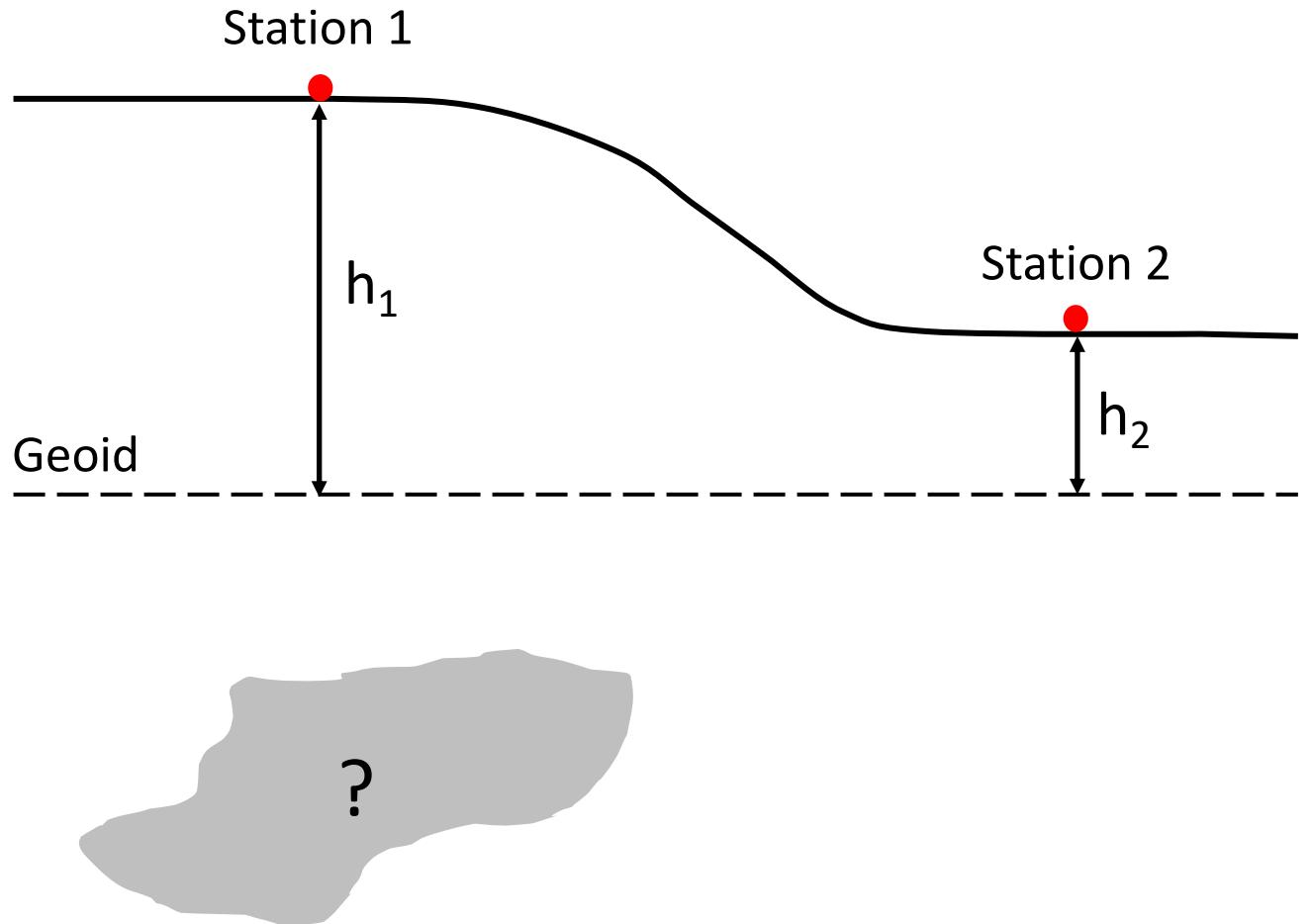
- Tidal correction
- Latitude correction



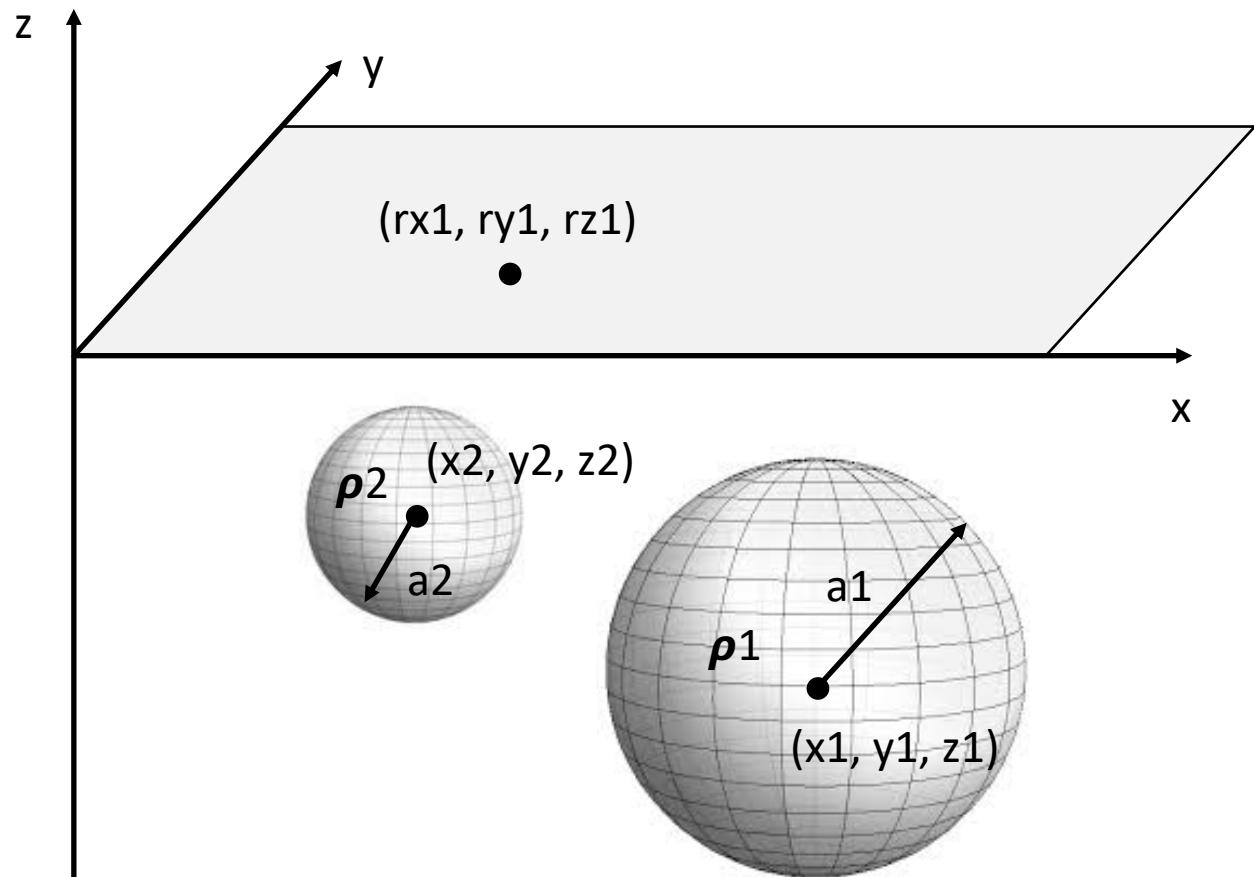
Earth: A spinning ellipsoid

# Gravity Data Correction

- Tidal correction
- Latitude correction
- Elevation correction (get only the effect of density)
  - a) Free-air (back to geoid)
  - b) Bouguer (remove rock slab)
  - c) Terrain (remove pull-up of mountains on side)



# Gravity of Two (or N) Spheres

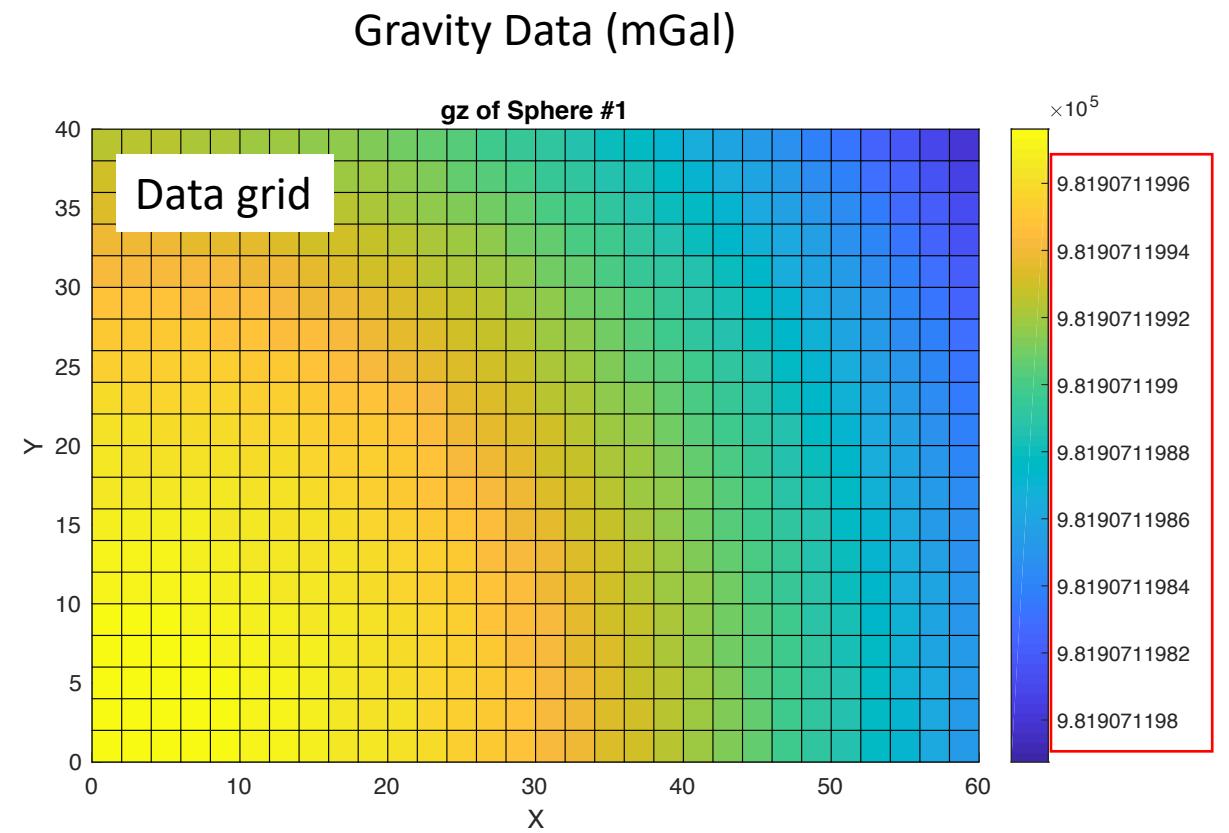
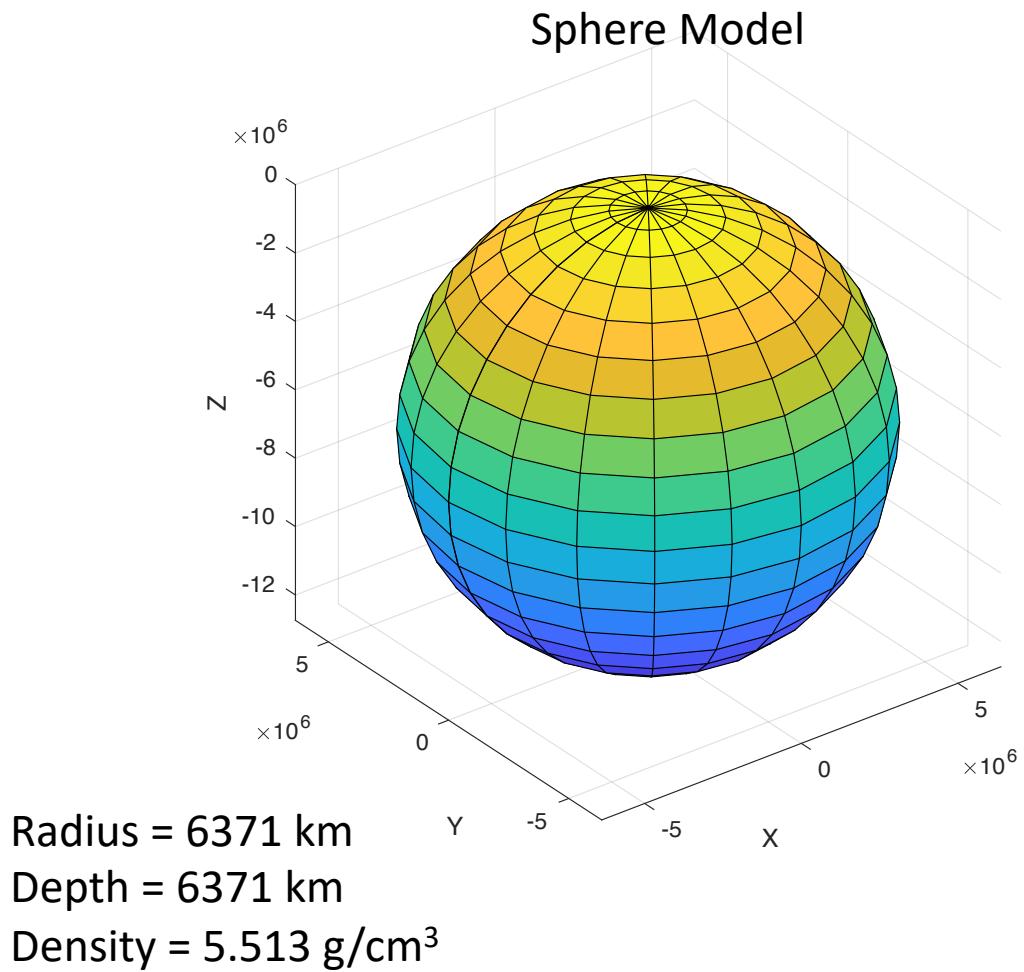


N uniform spheres of different densities located in the 3D space

Be able to calculate the gravitational field  $F$  anywhere in the 3D space outside of the spheres

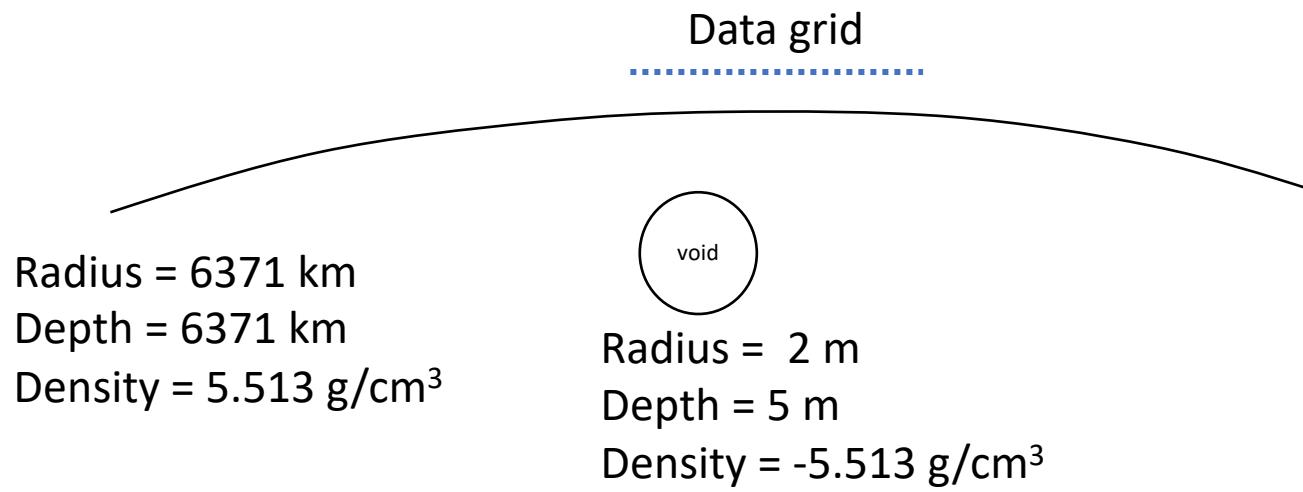
Bury the two spheres underground and compute  $g_z$  over a data grid on the surface and make the plot

# Experiment 1: One Really Big Sphere

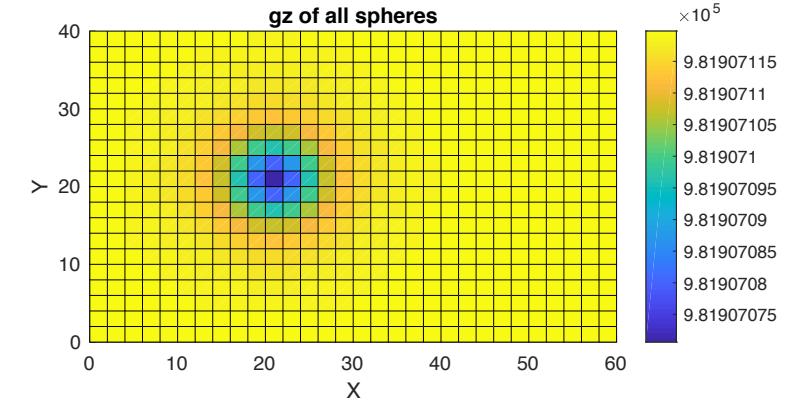
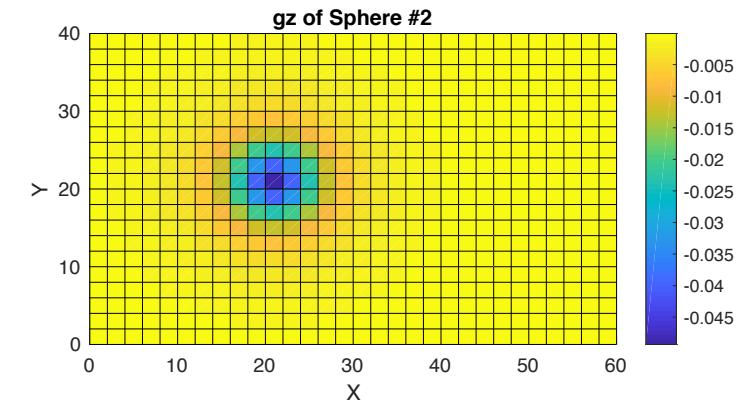
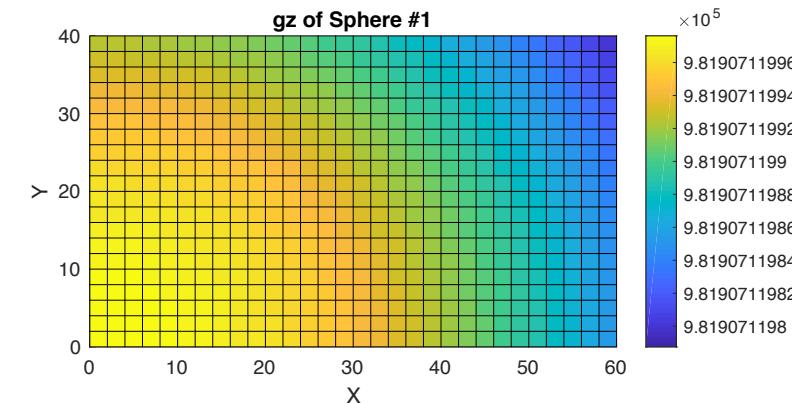


Conclusion: Big numbers but almost constant

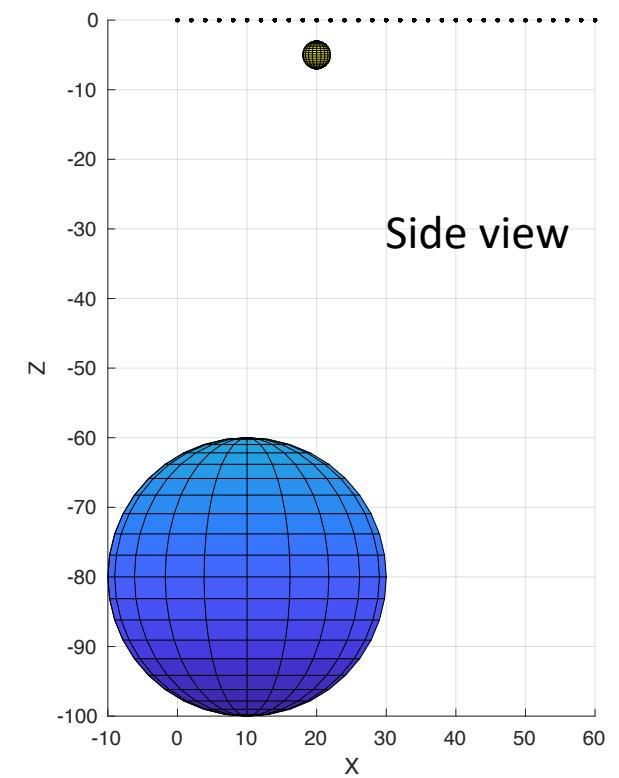
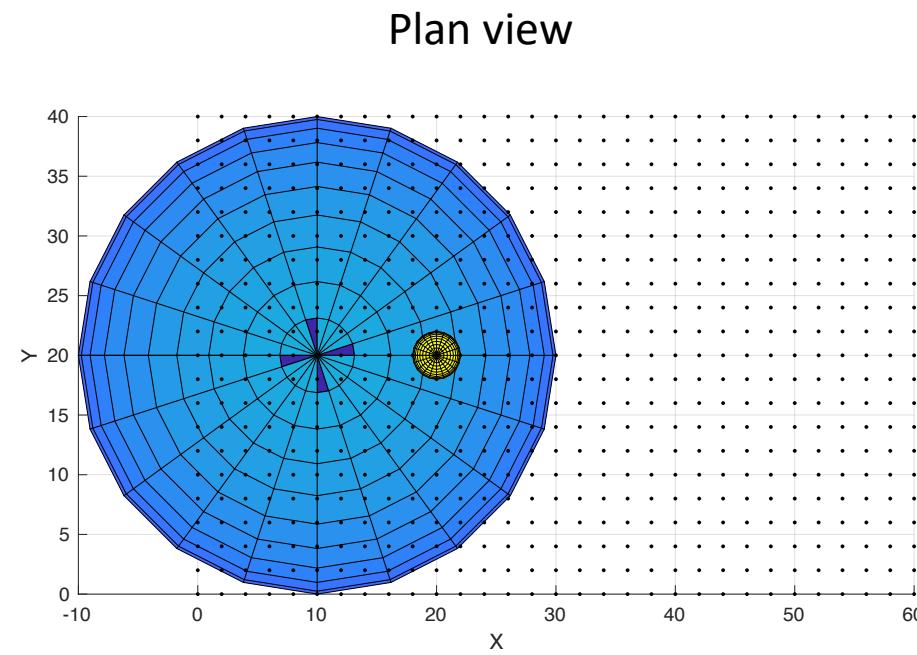
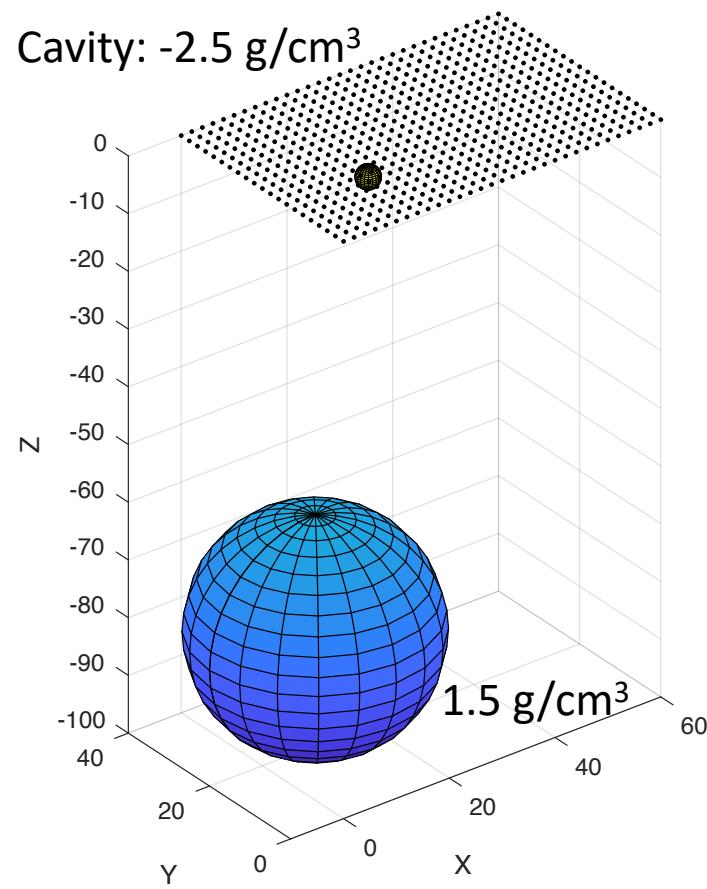
# Experiment 2: A Small Cavity in a Large Sphere

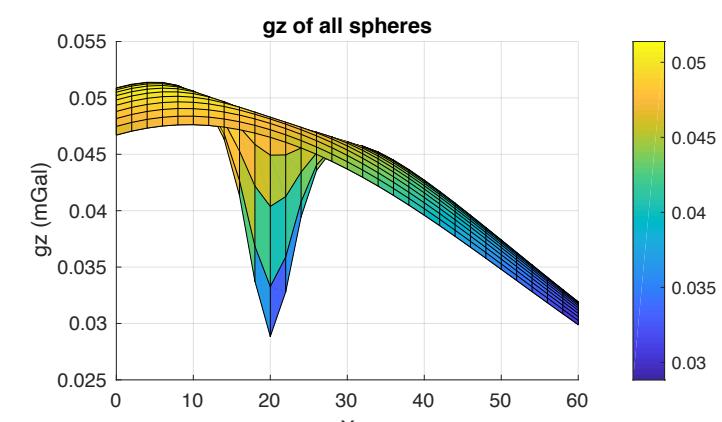
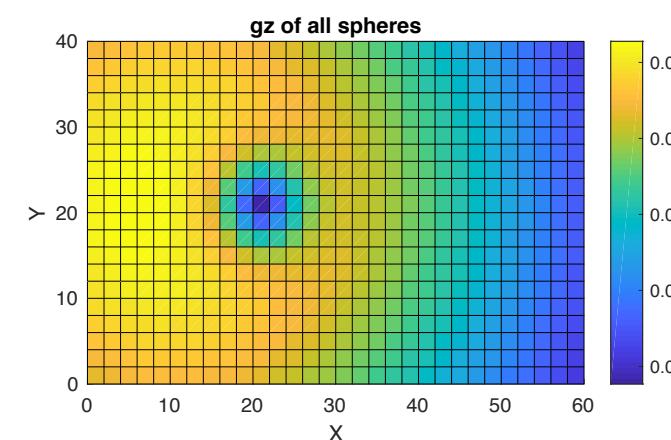
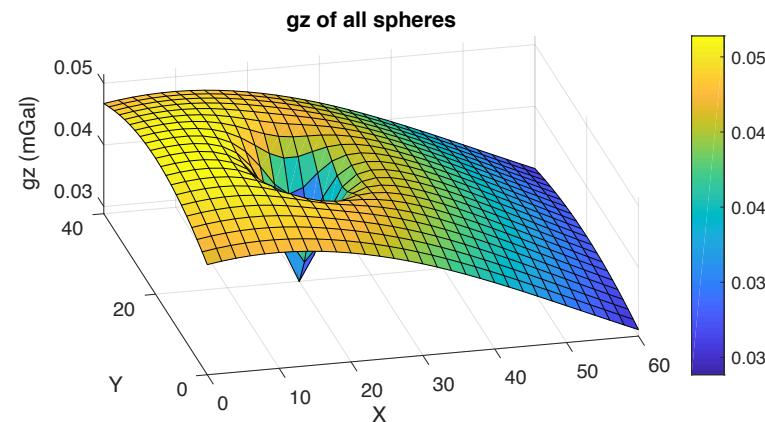
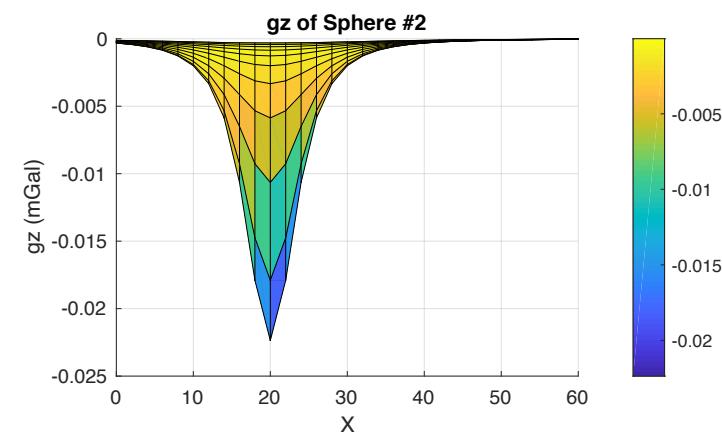
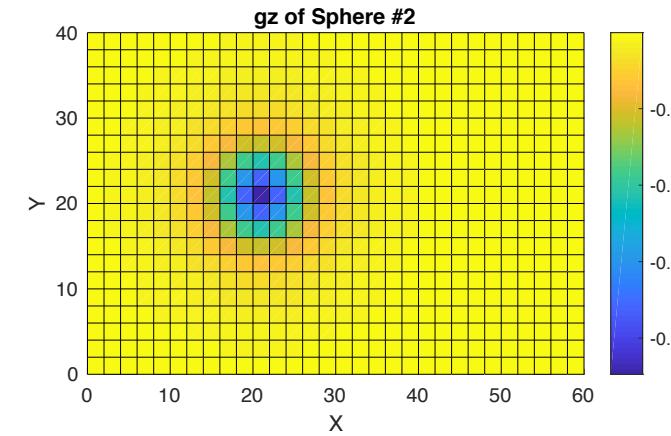
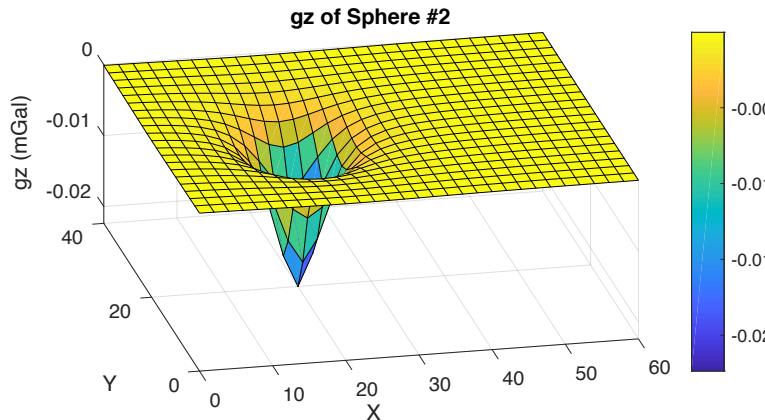
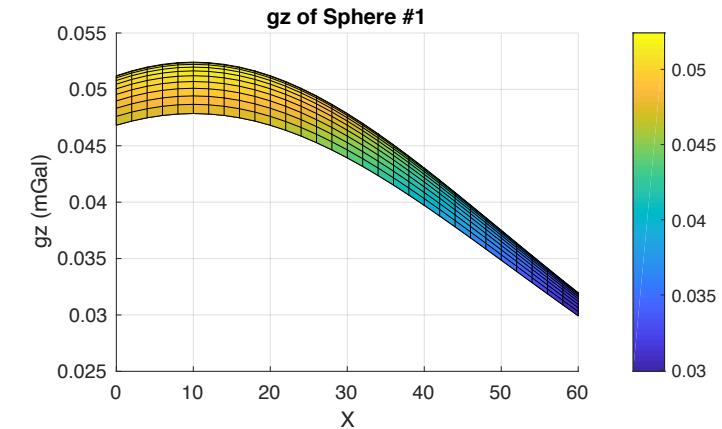
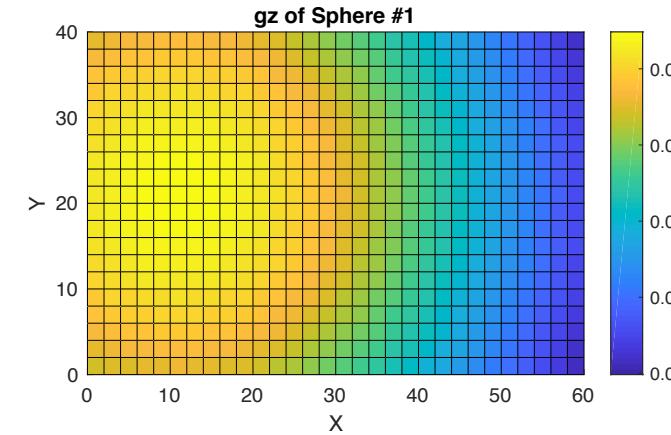
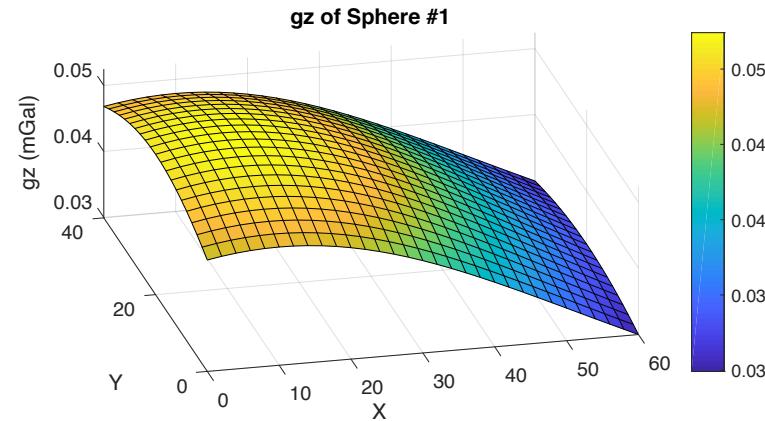


Conclusion: The field from the entire earth does not help us in finding buried objects



# Experiment 3: Two Spheres in Different Sizes



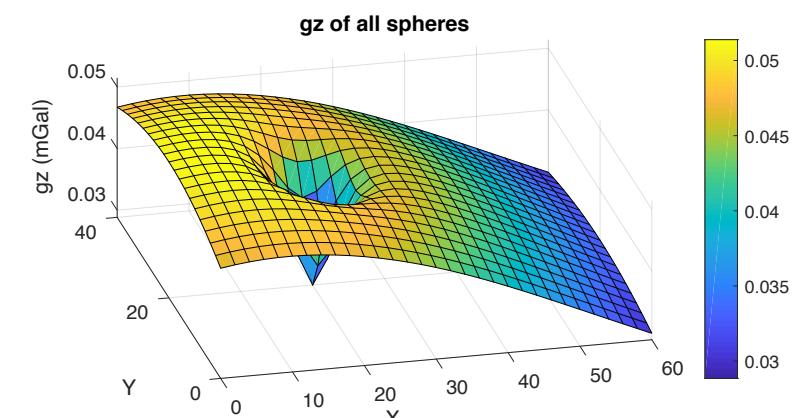
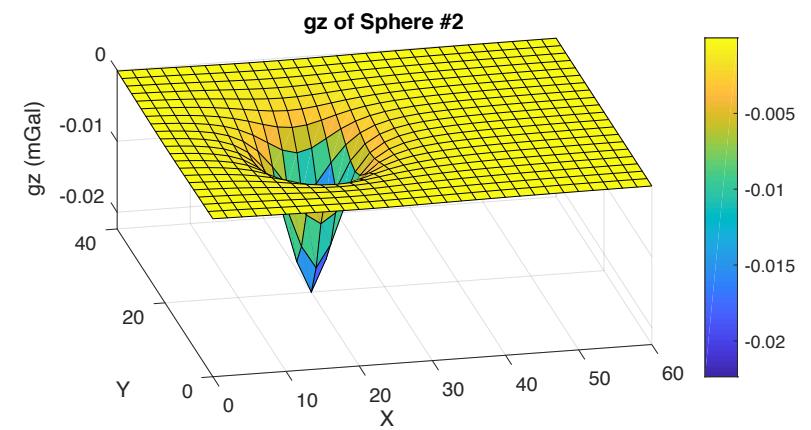
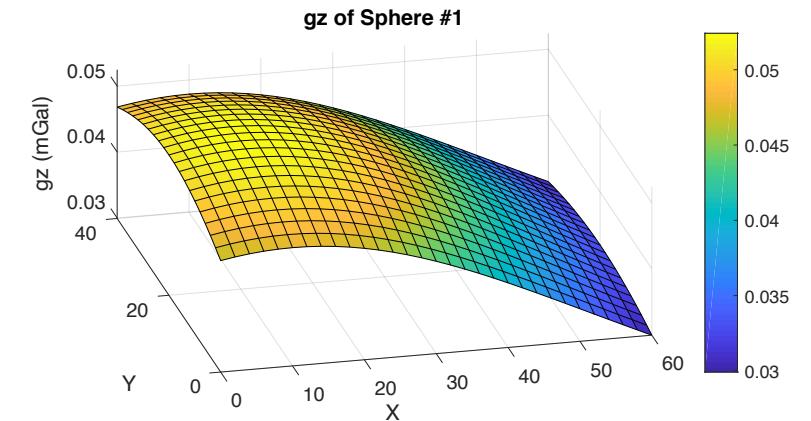
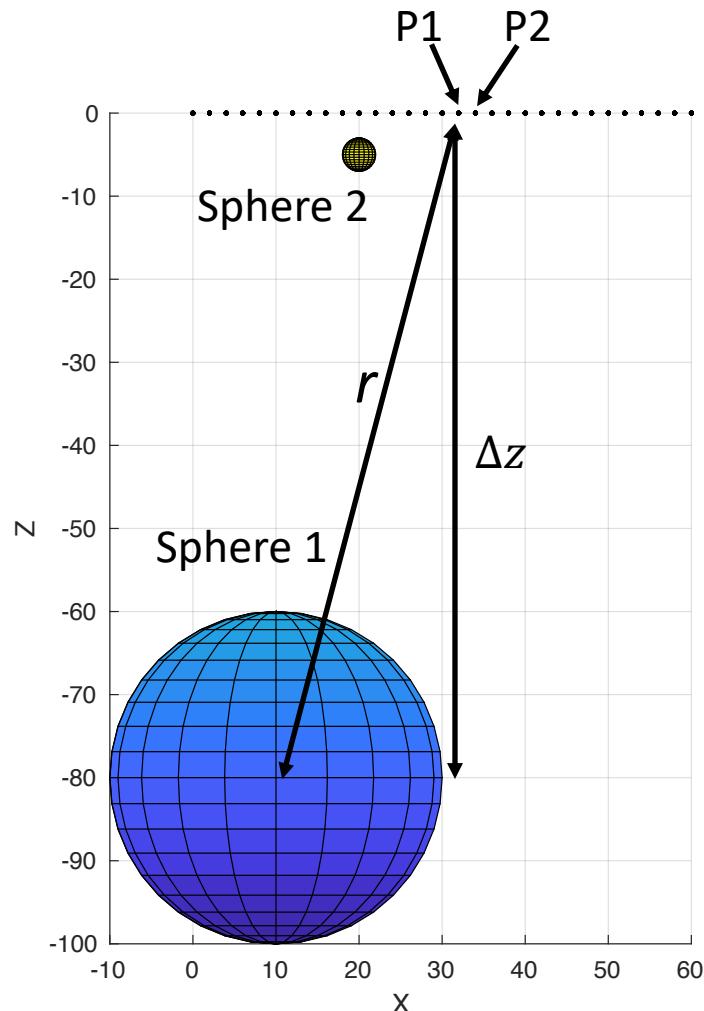


# Gravity Signal Decays as $1/r^2$

We measure the vertical component of  $g$  on the surface

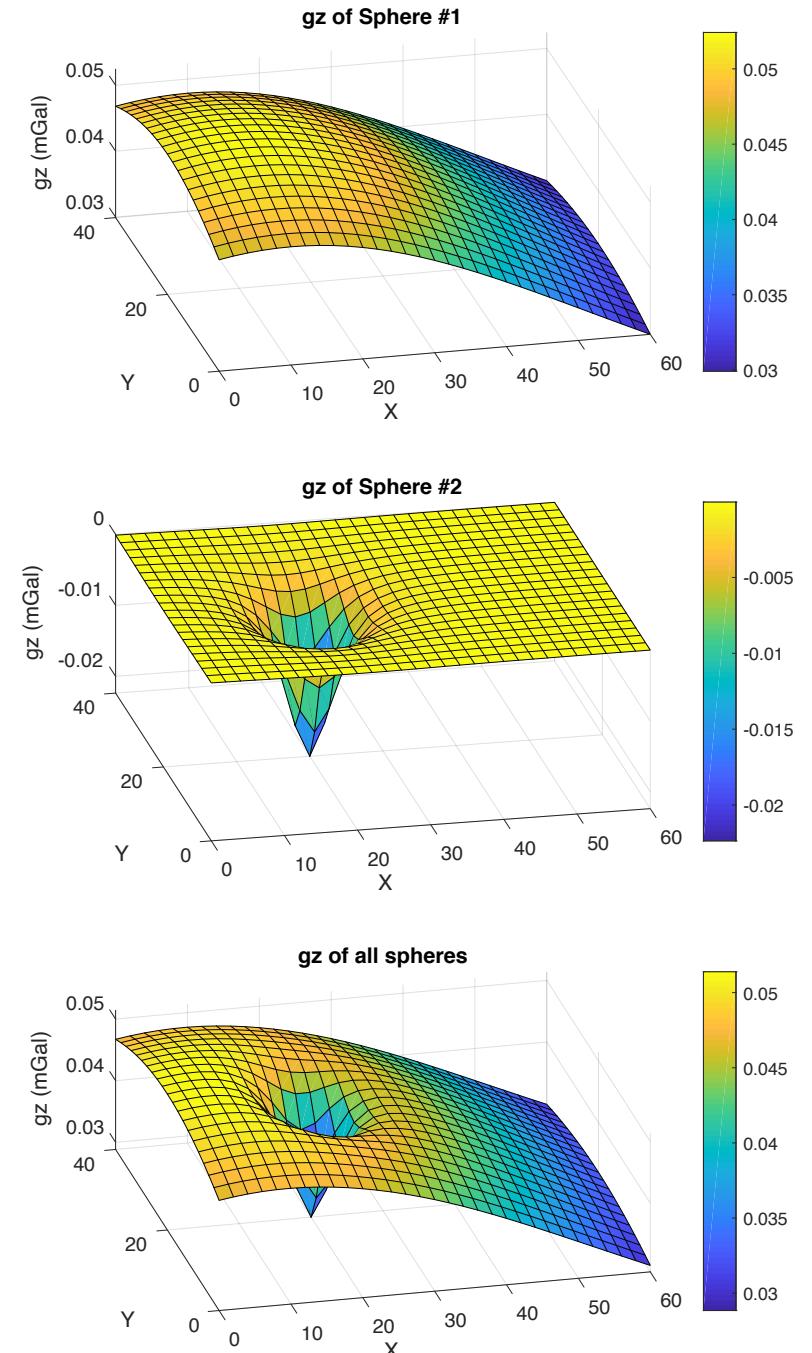
$$g_z = \frac{GM \Delta z}{r^3}$$

Large distance: long-wavelength  
Small distance: short-wavelength

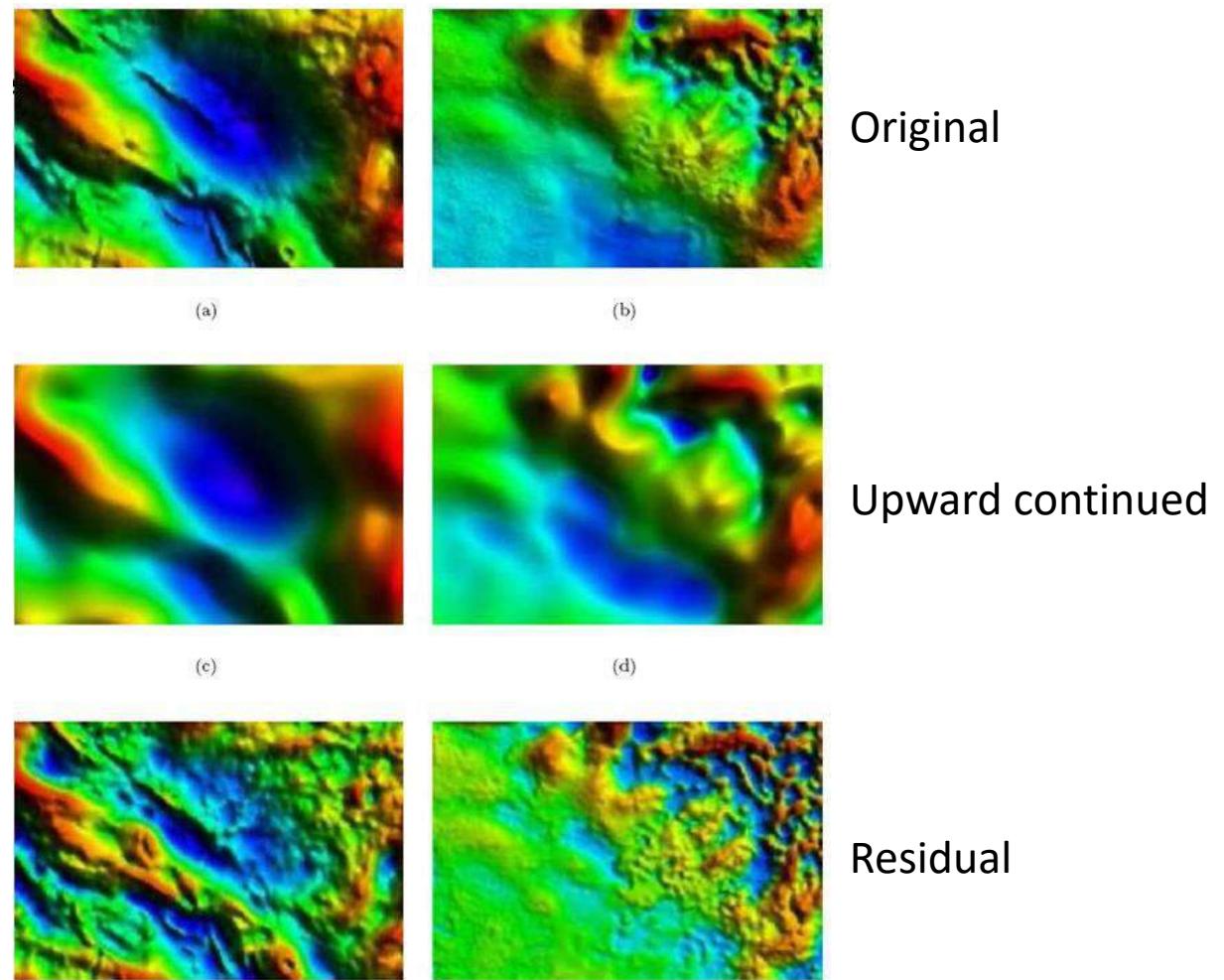
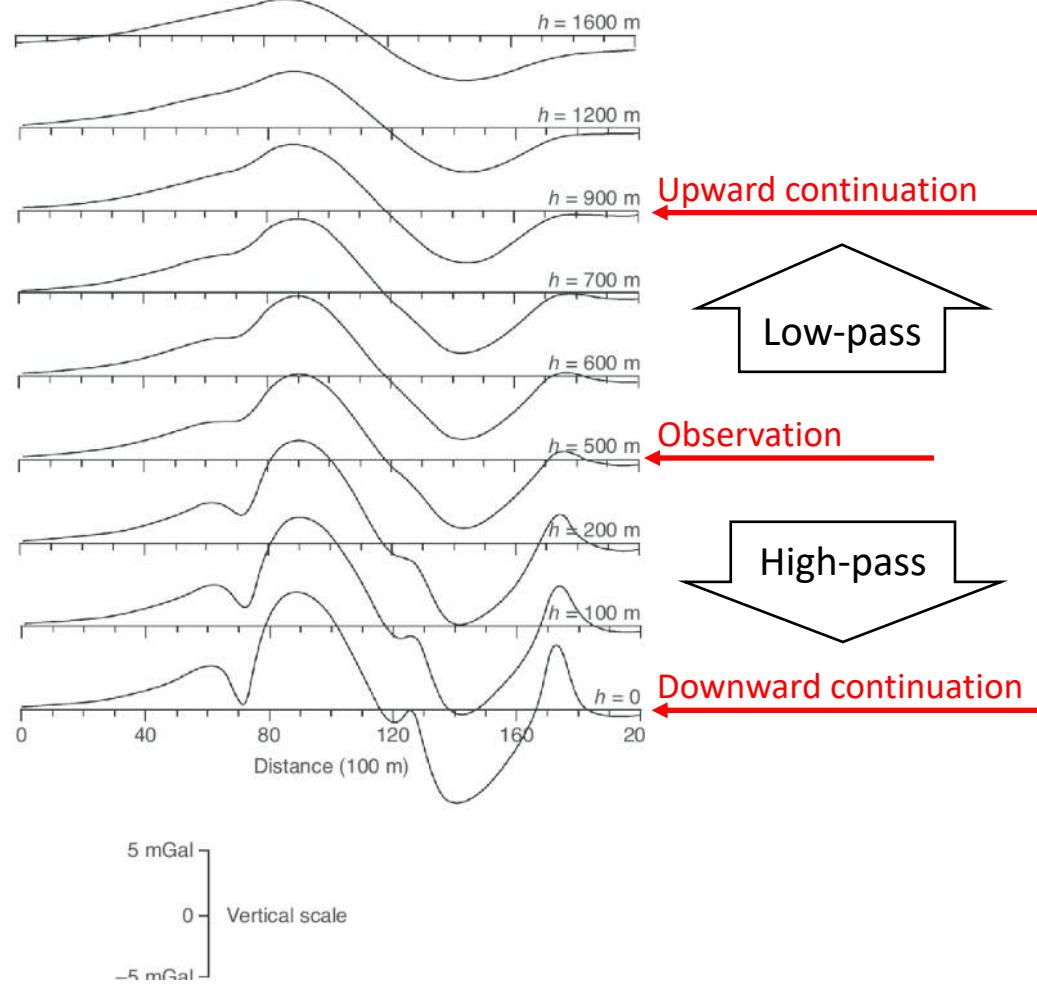


# Regional Removal

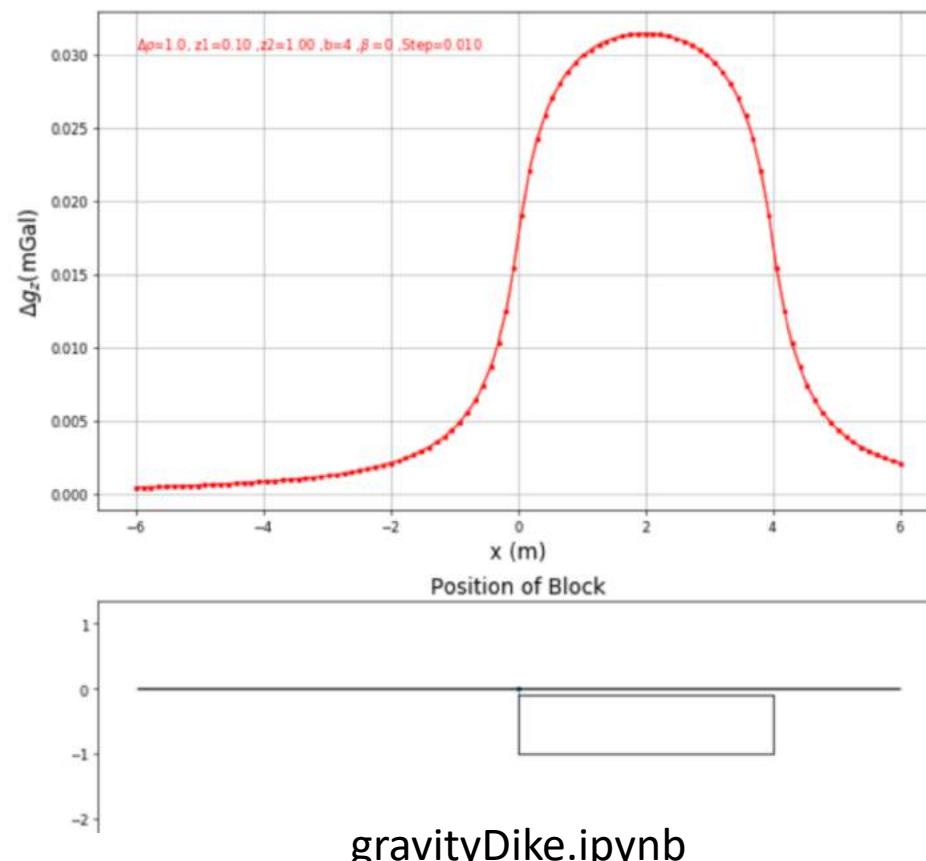
- Separate signals with different wavelengths
- Isolate anomalies at the scales of our interest
  - Small and shallow: Near-surface cavity
  - Large and deep: Basin basement
- What are the approaches that can be used to carry out regional removal?
  - Moving window averaging
  - Wavenumber domain filtering
  - Best-fitting large sphere
  - Surface fitting – low-order polynomials



# Upward and Downward Continuation

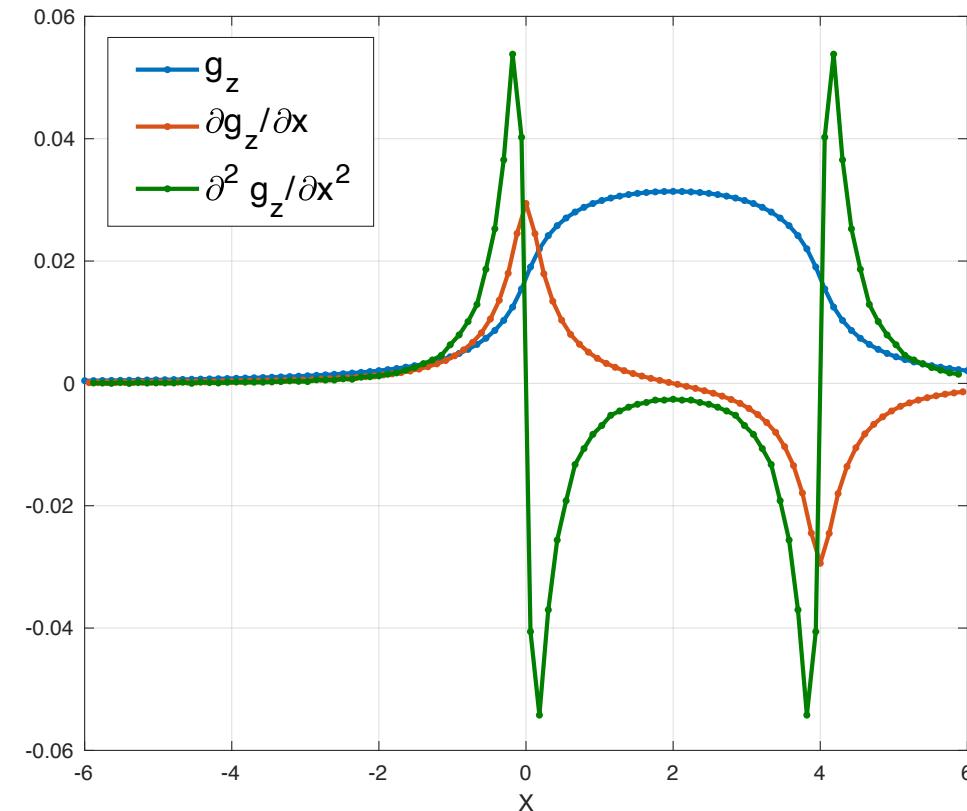


# Horizontal Derivative

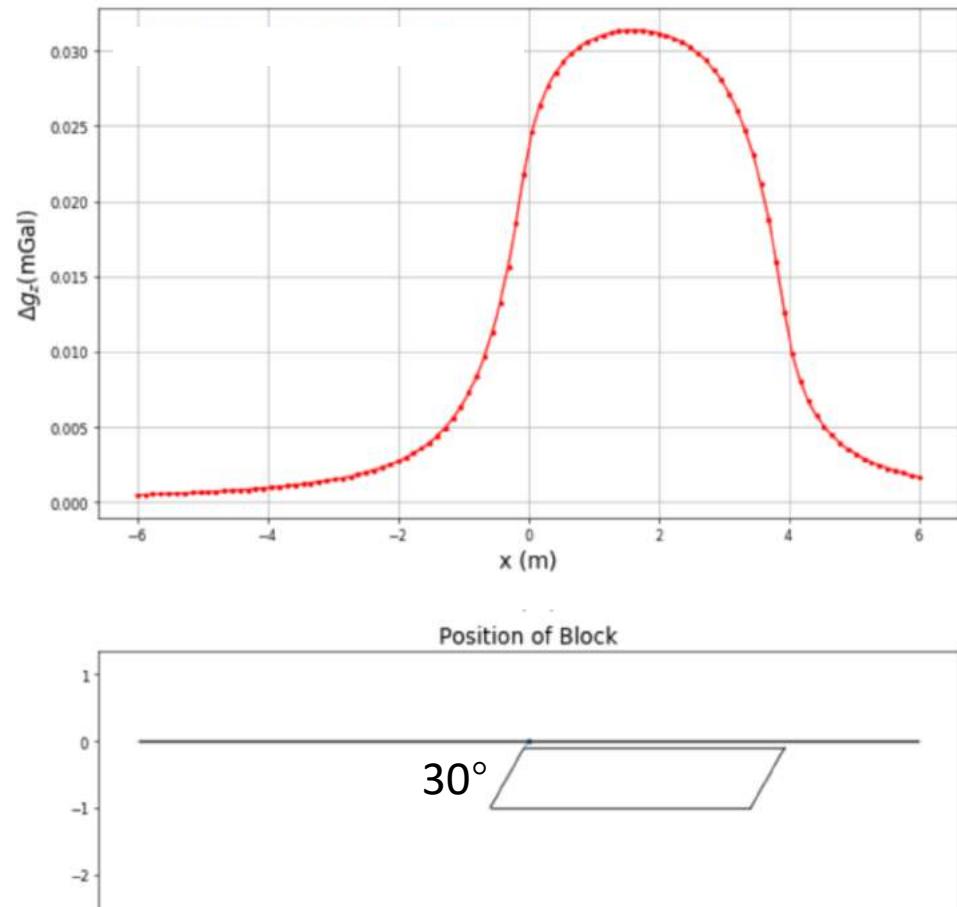


Draw the first and second horizontal derivatives

Which derivative is more useful in defining the edges?

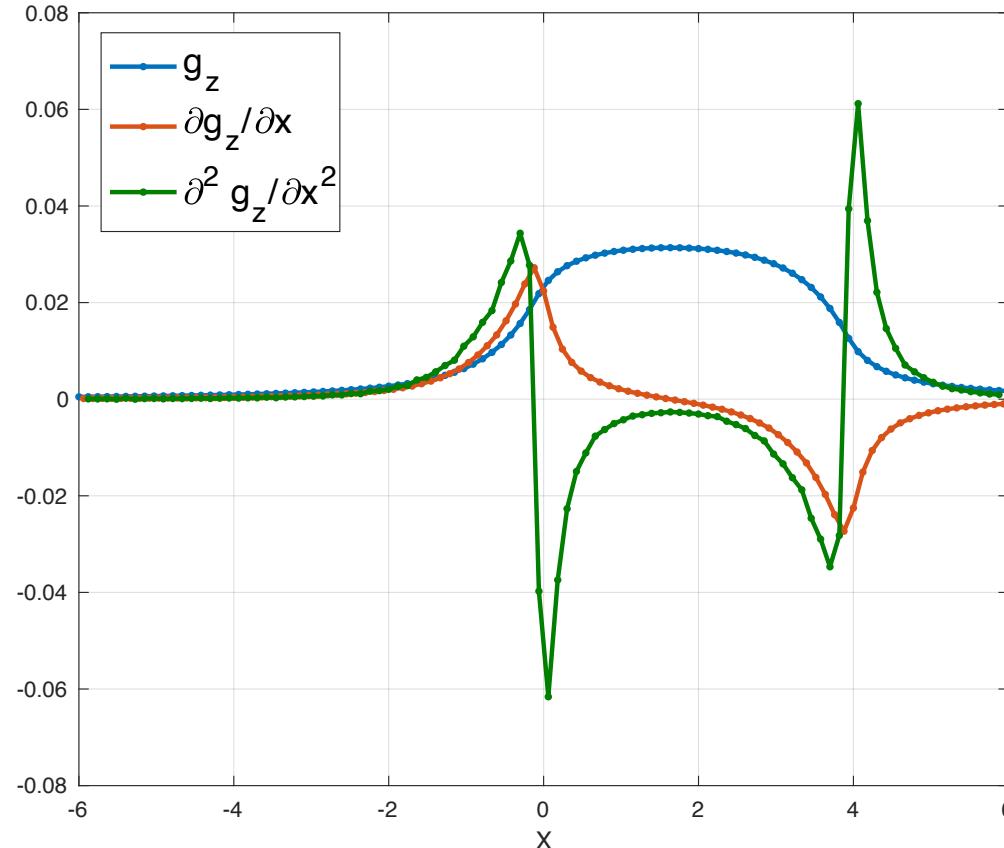


# Horizontal Derivative

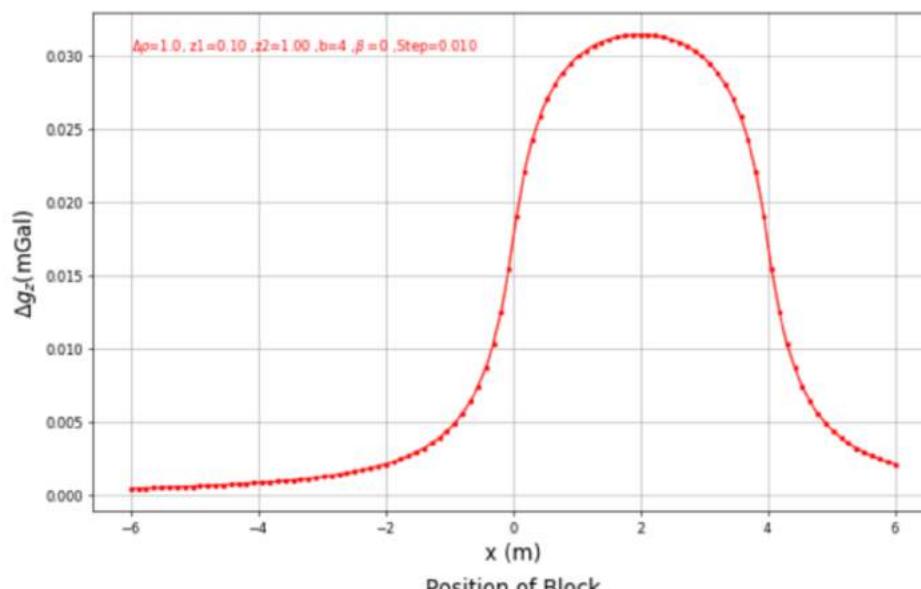
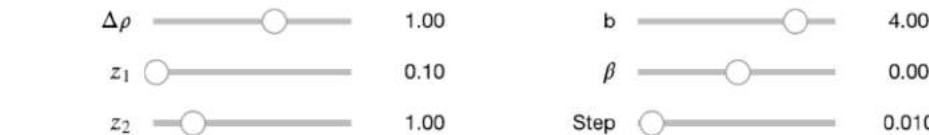


Can you tell the dipping direction from  $g_z$ ?

Which derivative is more useful in finding the dip?

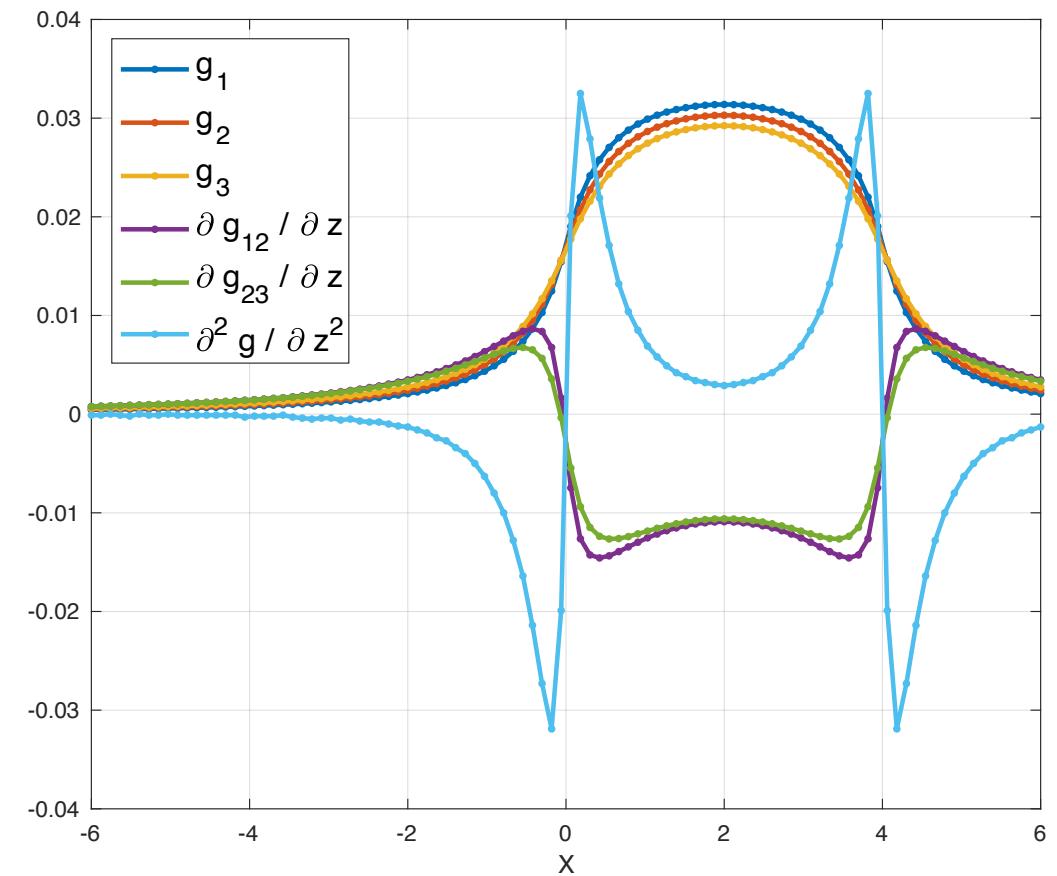


# Vertical Derivatives

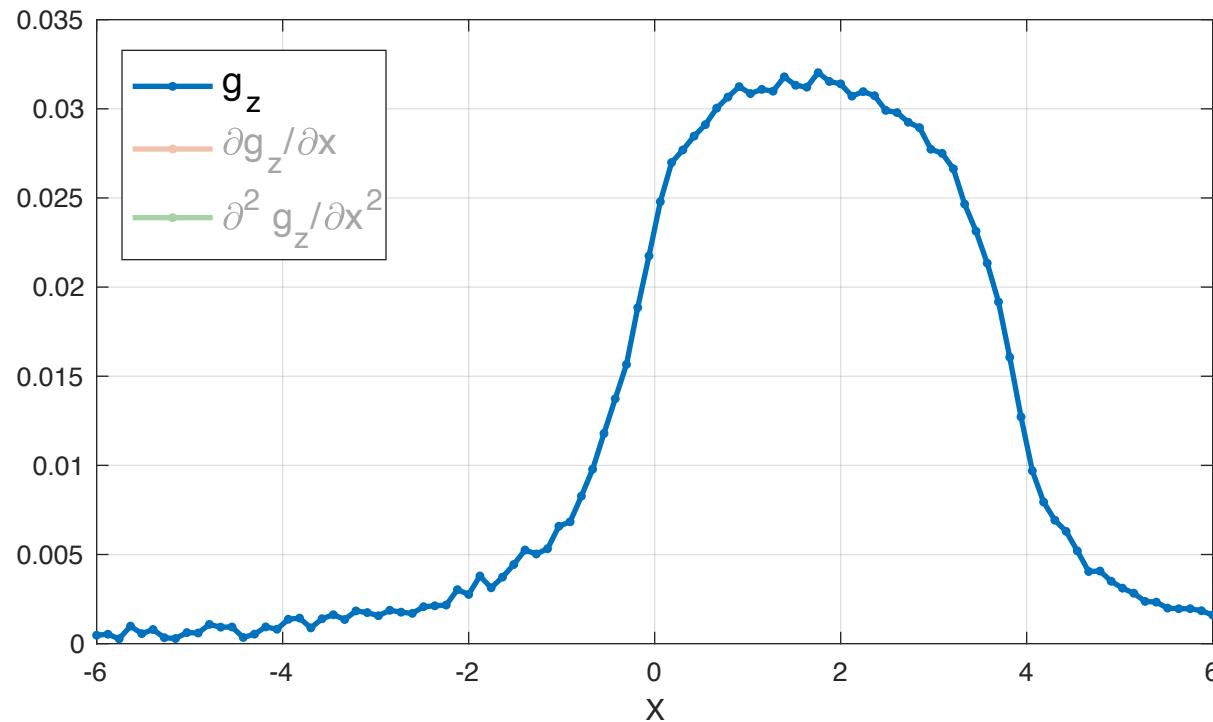


gravityDike.ipynb

$g_1$ : 0 m above surface  
 $g_2$ : 0.1 m above surface  
 $g_3$ : 0.2 m above surface

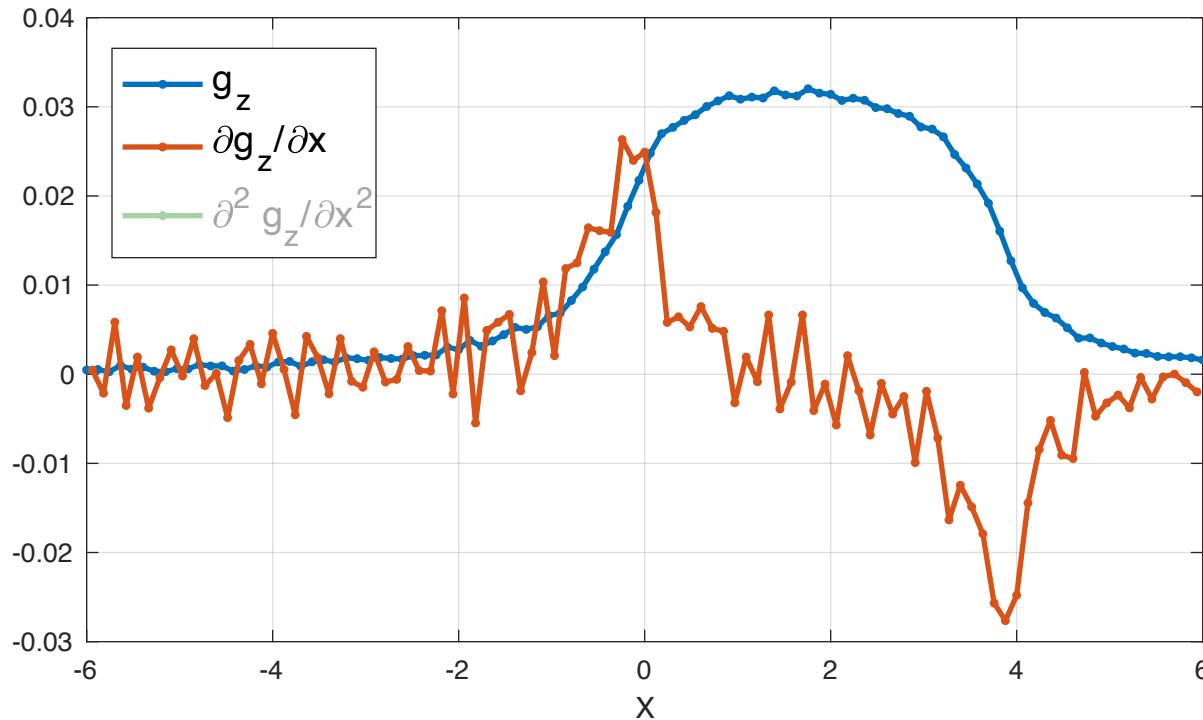


# High Order Derivative?



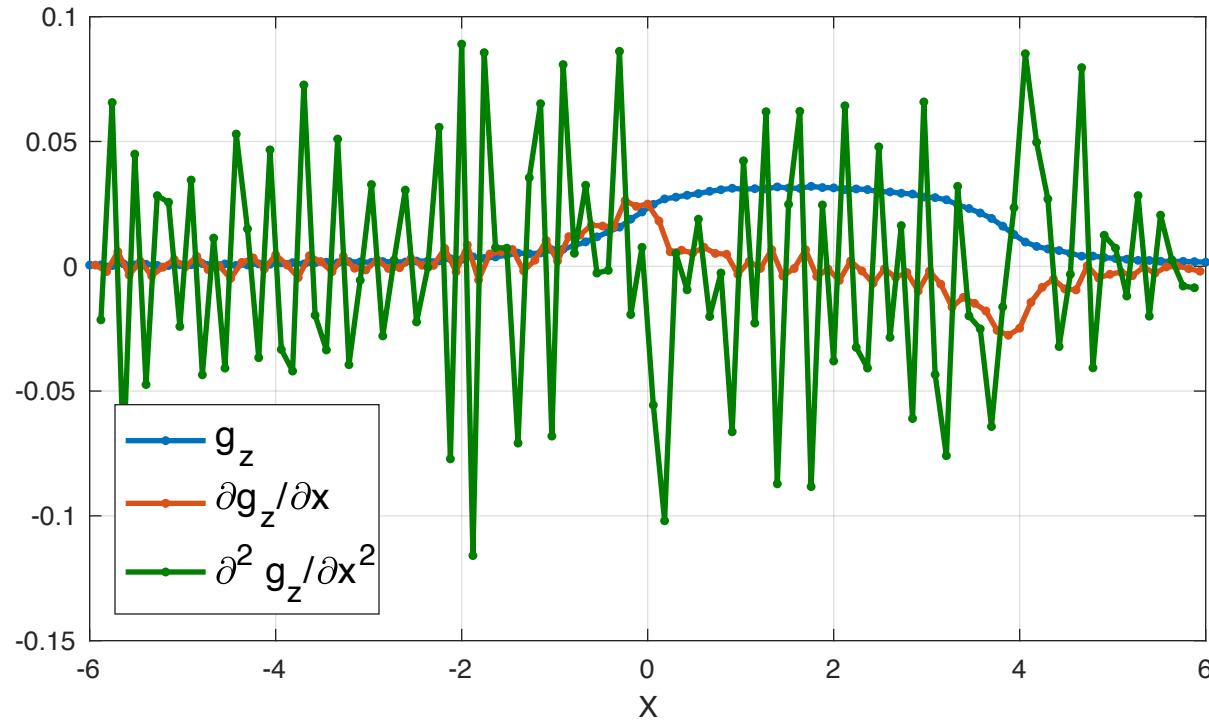
1% Gaussian noise in data

# High Order Derivative?



Horizontal 1<sup>st</sup> derivative: Not too bad

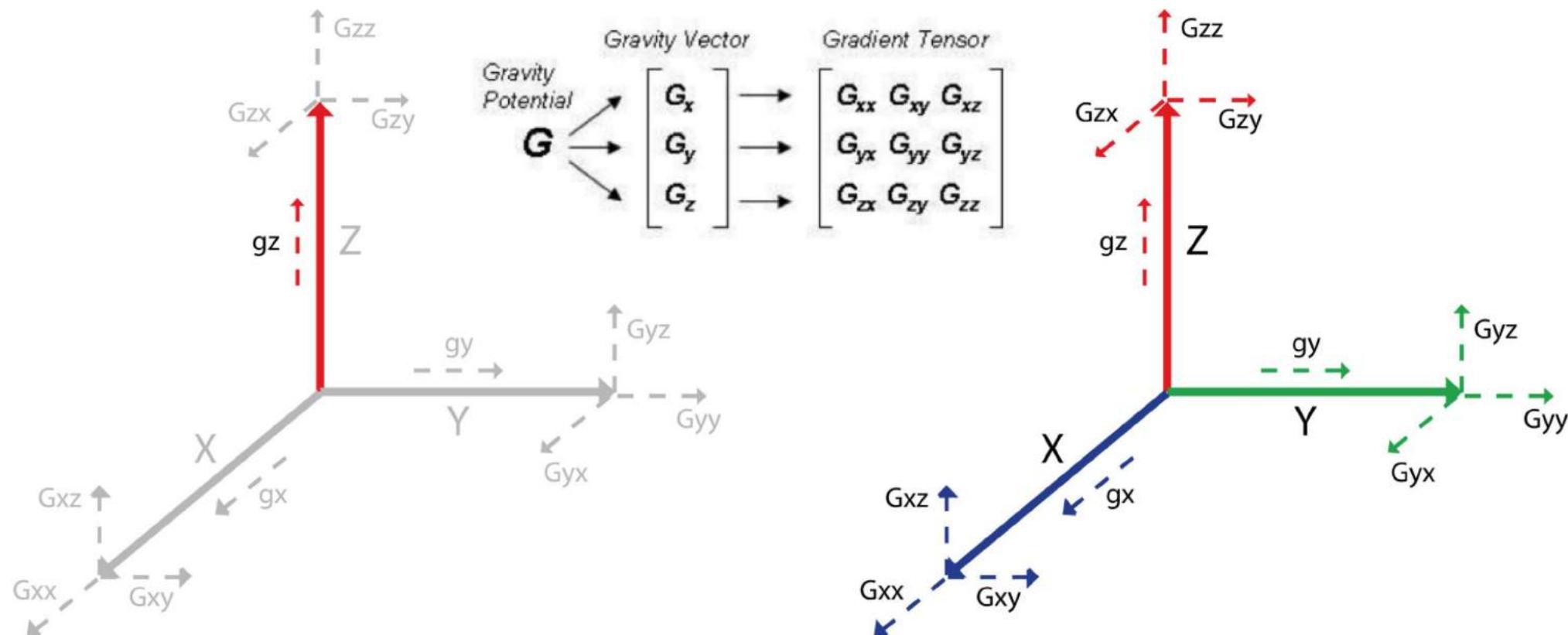
# High Order Derivative?



Horizontal 2<sup>nd</sup> derivative: Caution!

Derivative magnifies noise in data

# Full Tensor Gradient: More from $g_x$ and $g_y$



# 3D-FTG

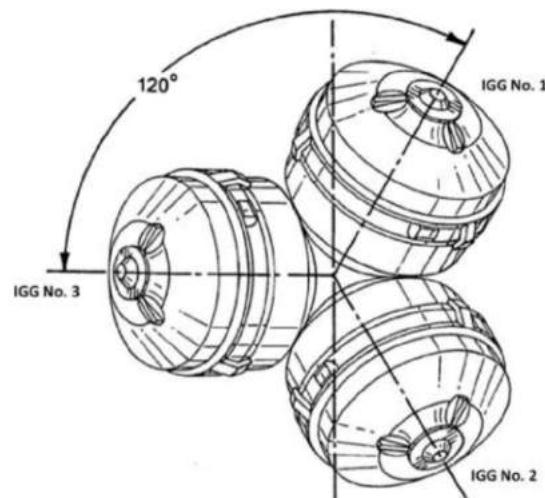


Figure 3 – Umbrella-like arrangement of Gravity Gradient Instruments (GGI) according to Brett & Brewster (2010).

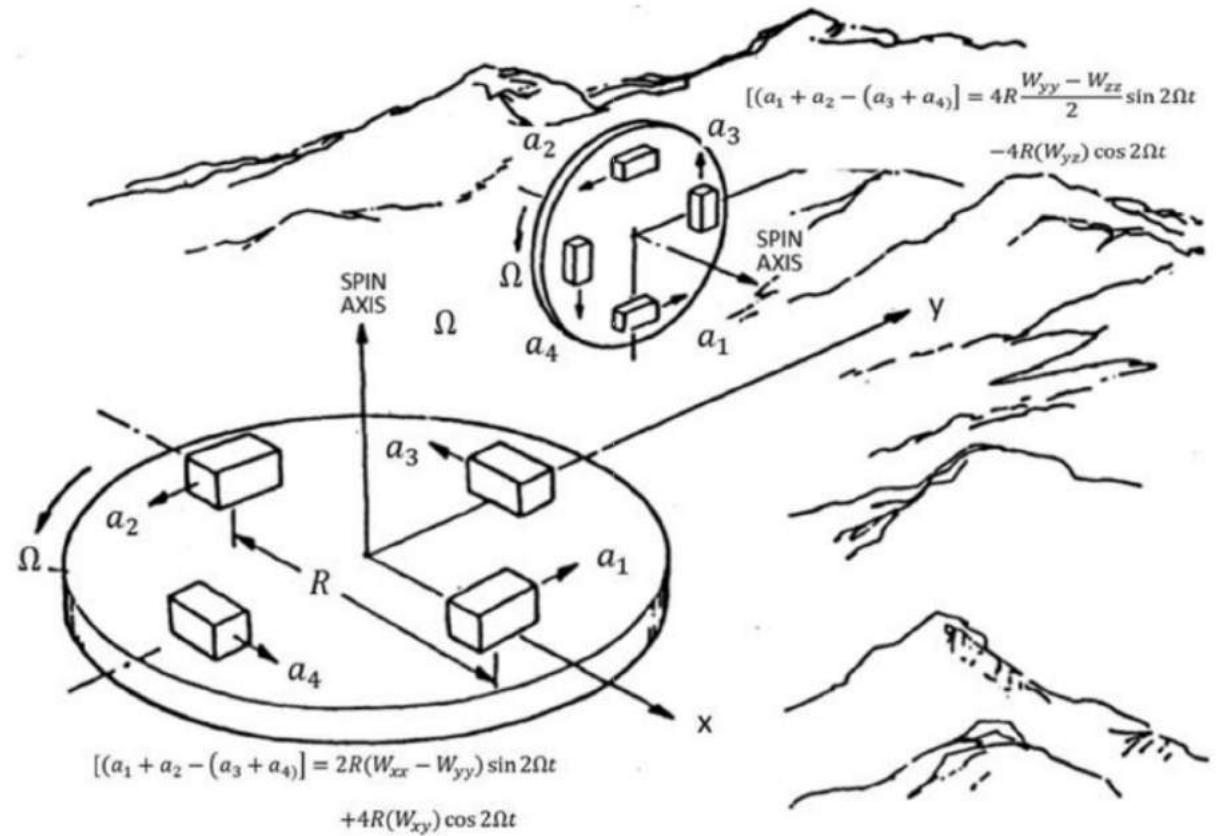
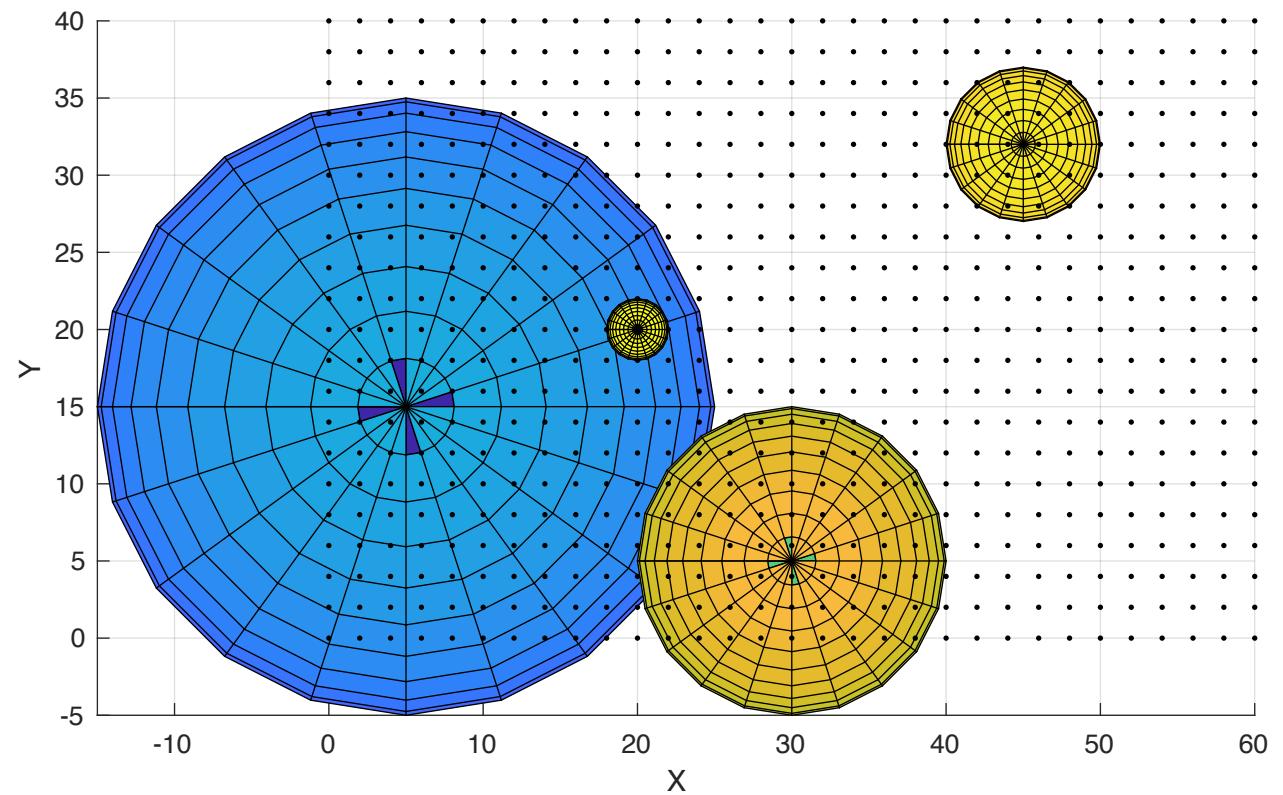
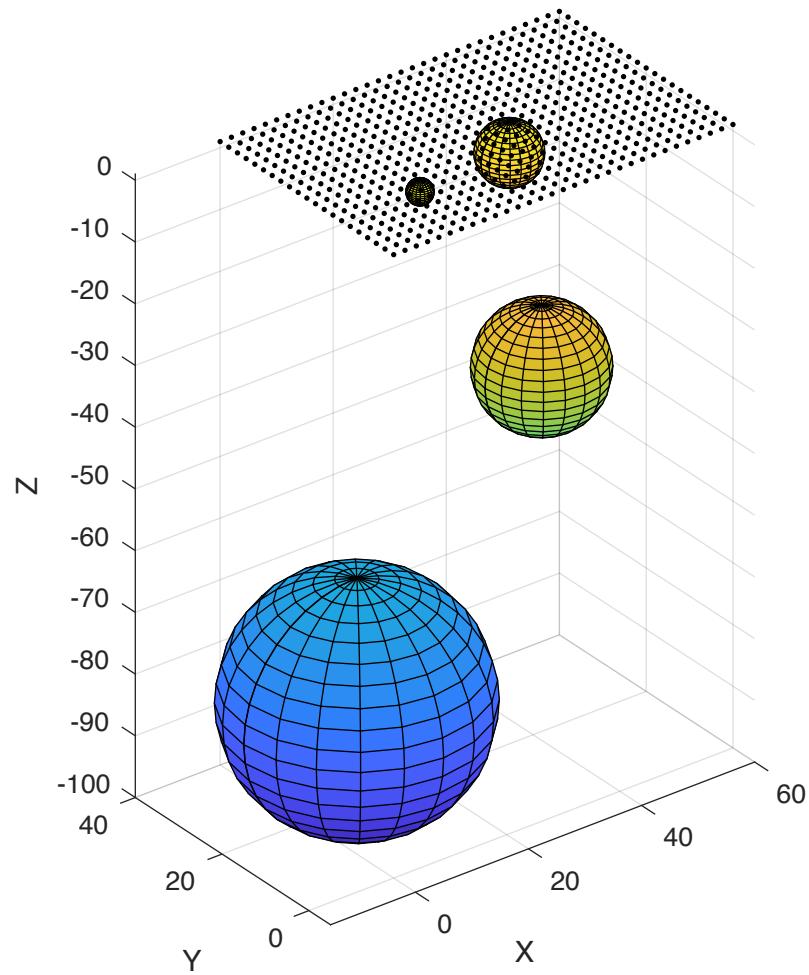
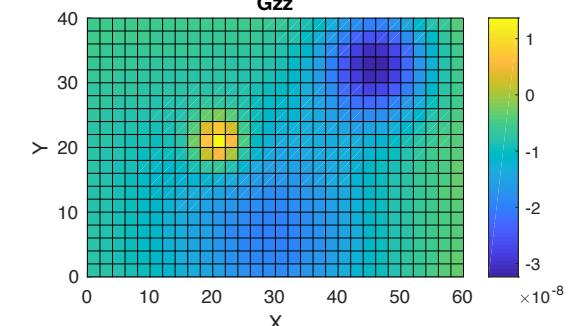
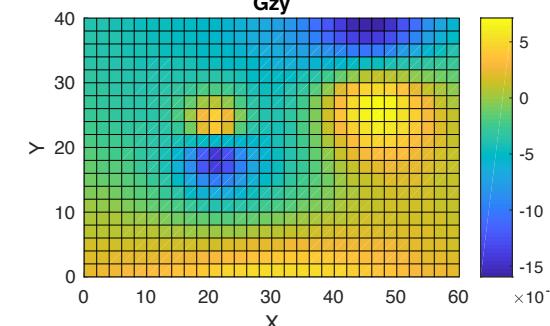
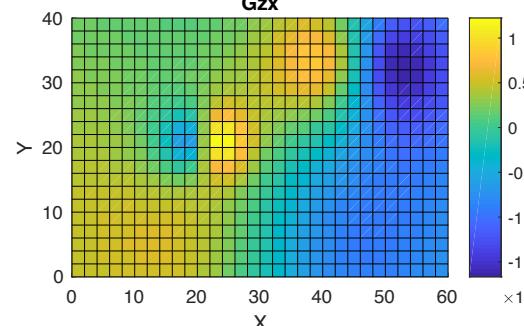
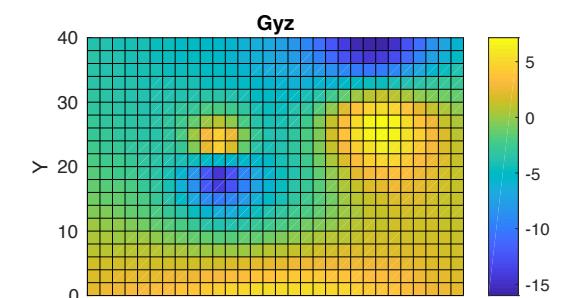
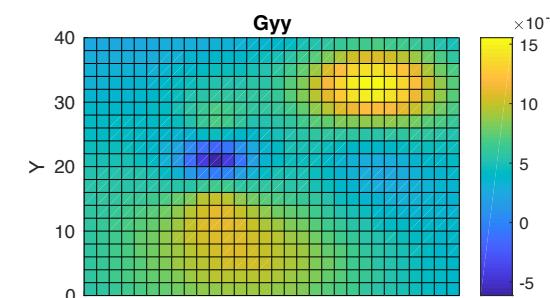
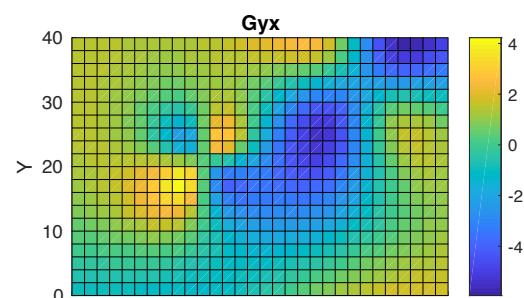
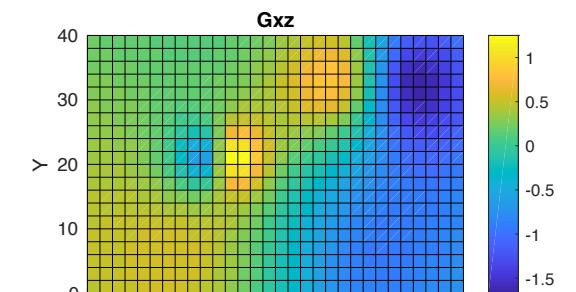
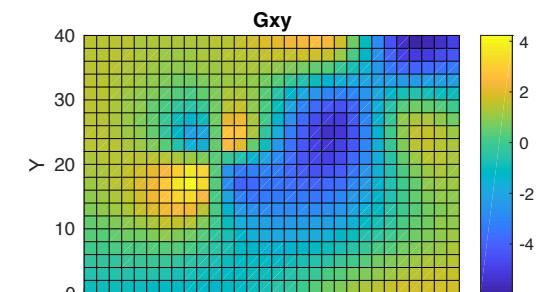
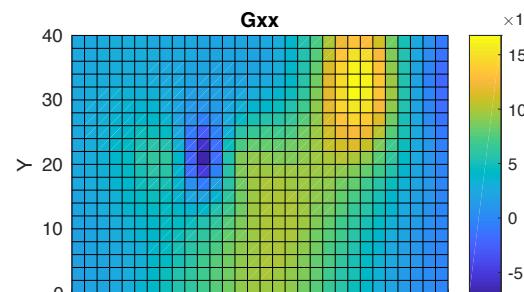
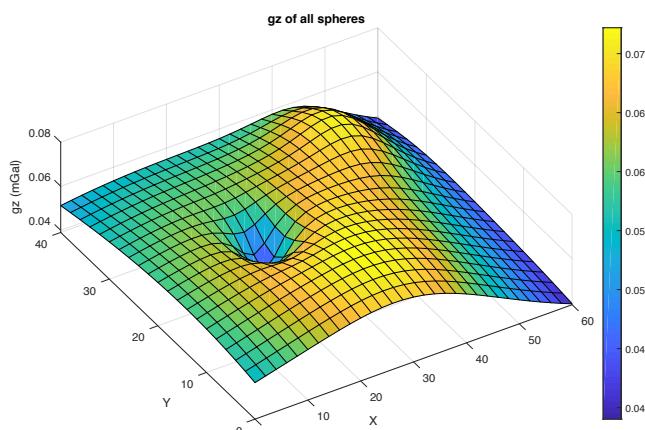
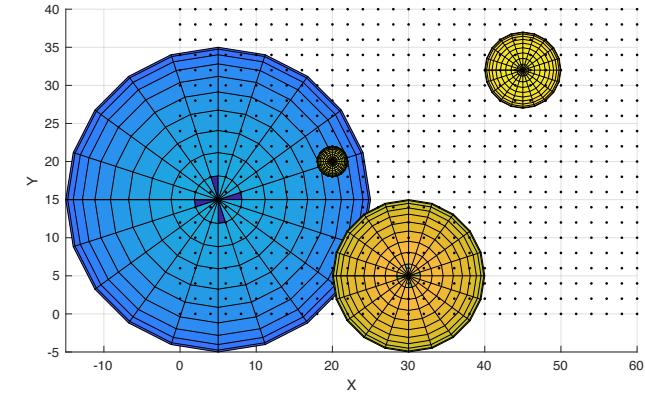


Figure 2 – Representation of rotational accelerometers gravity gradient according to Metzger (1986).

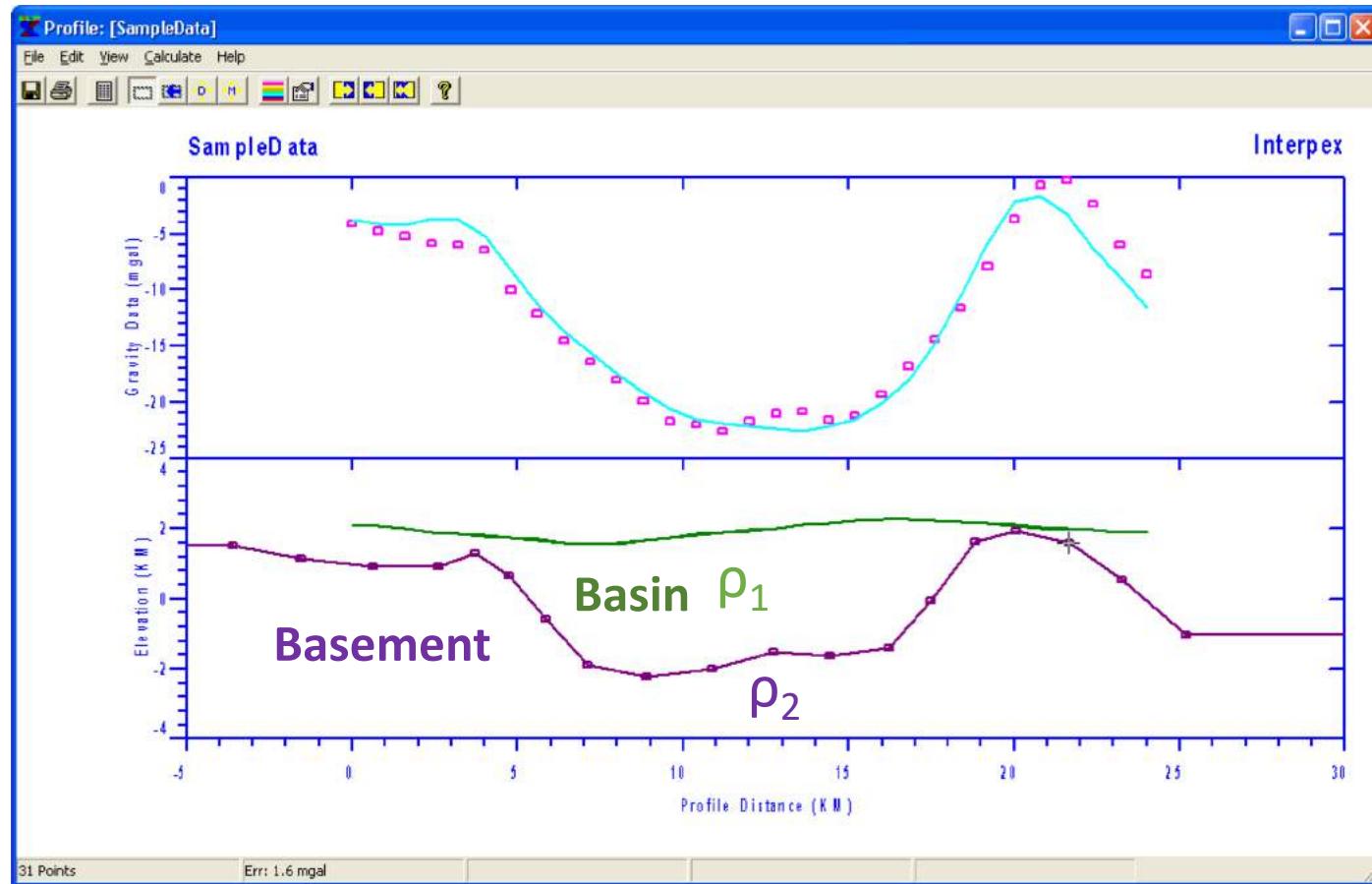
# The Four-Sphere Model



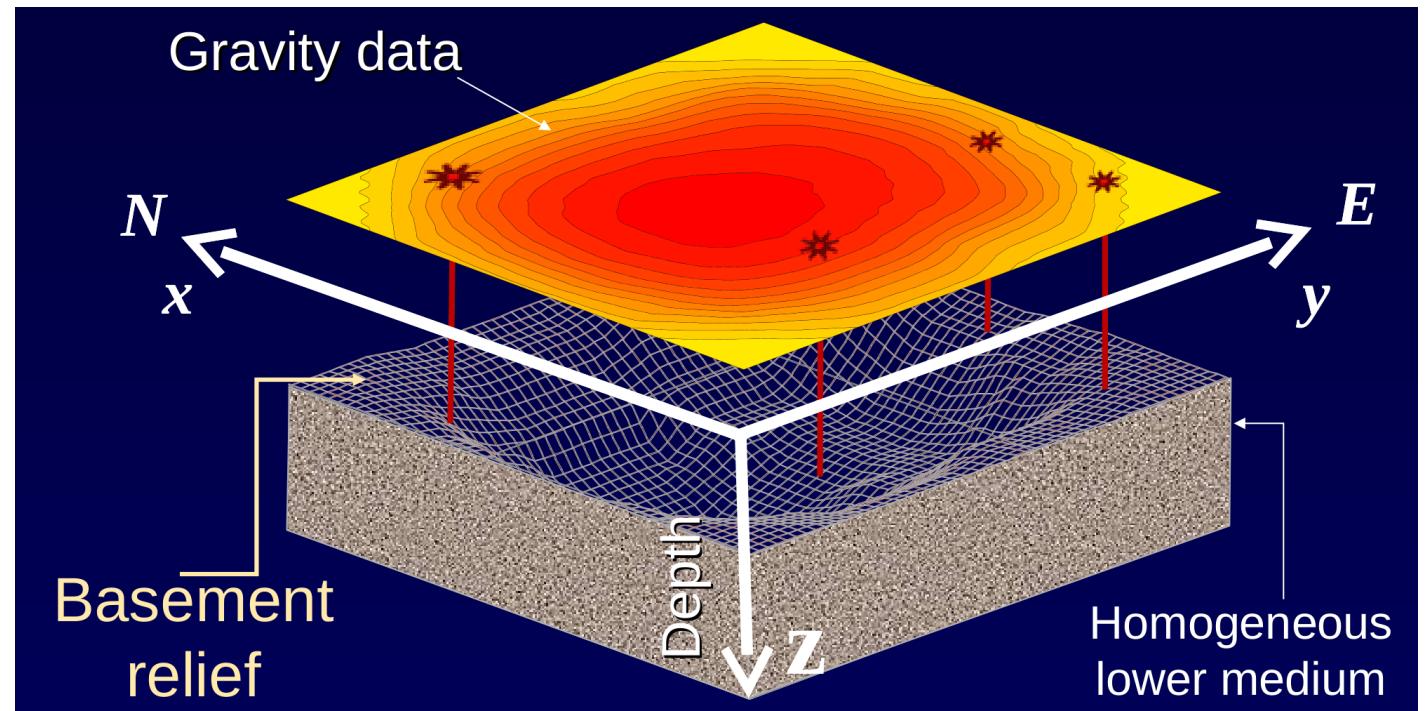
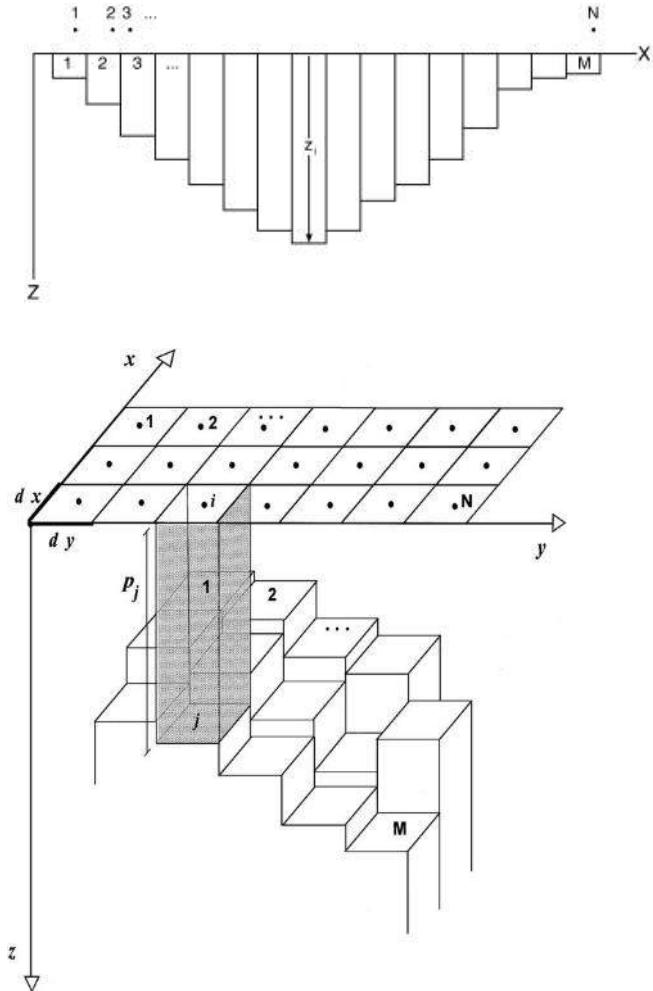
# Full Tensor Gravity Gradient



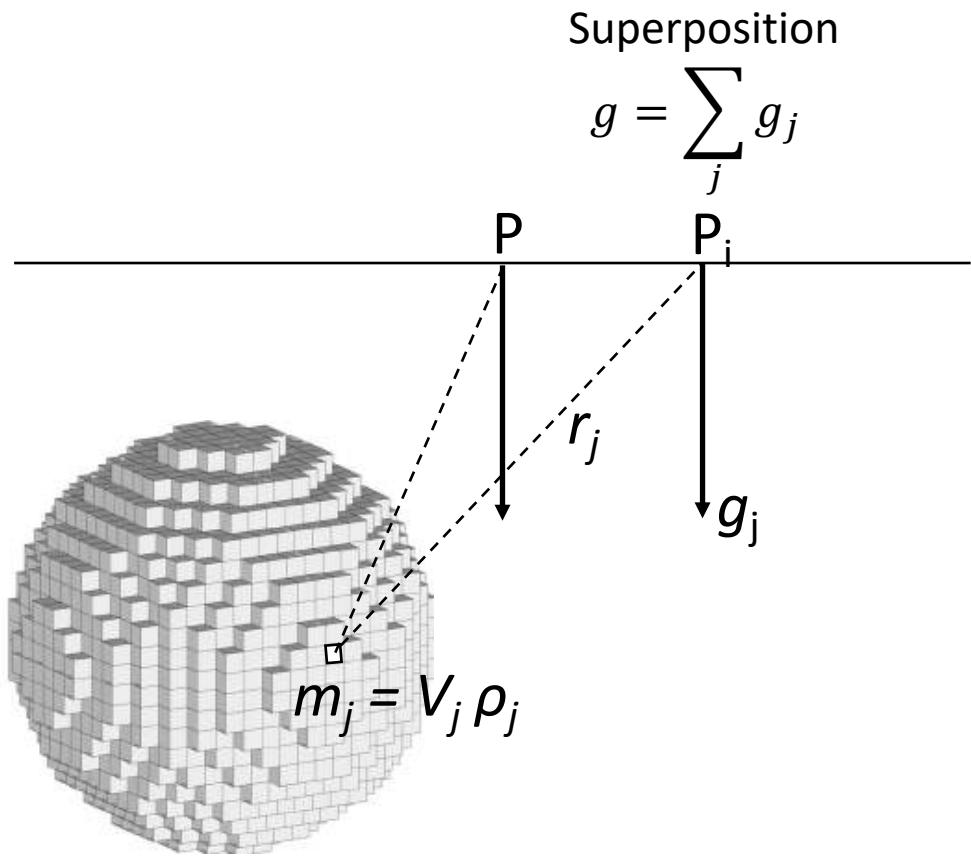
# Geometric Inversion - Interactive



# Geometric Inversion - Basement Relief



# Pixel/Voxel Inversion



**Data = Integration over a volume:**  
Not enough information to fully recover the true model

$$\left[ \begin{array}{c} \\ \\ \\ \end{array} \right] \left[ \begin{array}{c} A \\ \\ \\ \end{array} \right] \left[ \begin{array}{c} \rho \\ \\ \\ \end{array} \right] = \left[ \begin{array}{c} \\ \\ \\ \end{array} \right] \left[ \begin{array}{c} d \\ \\ \\ \end{array} \right]$$

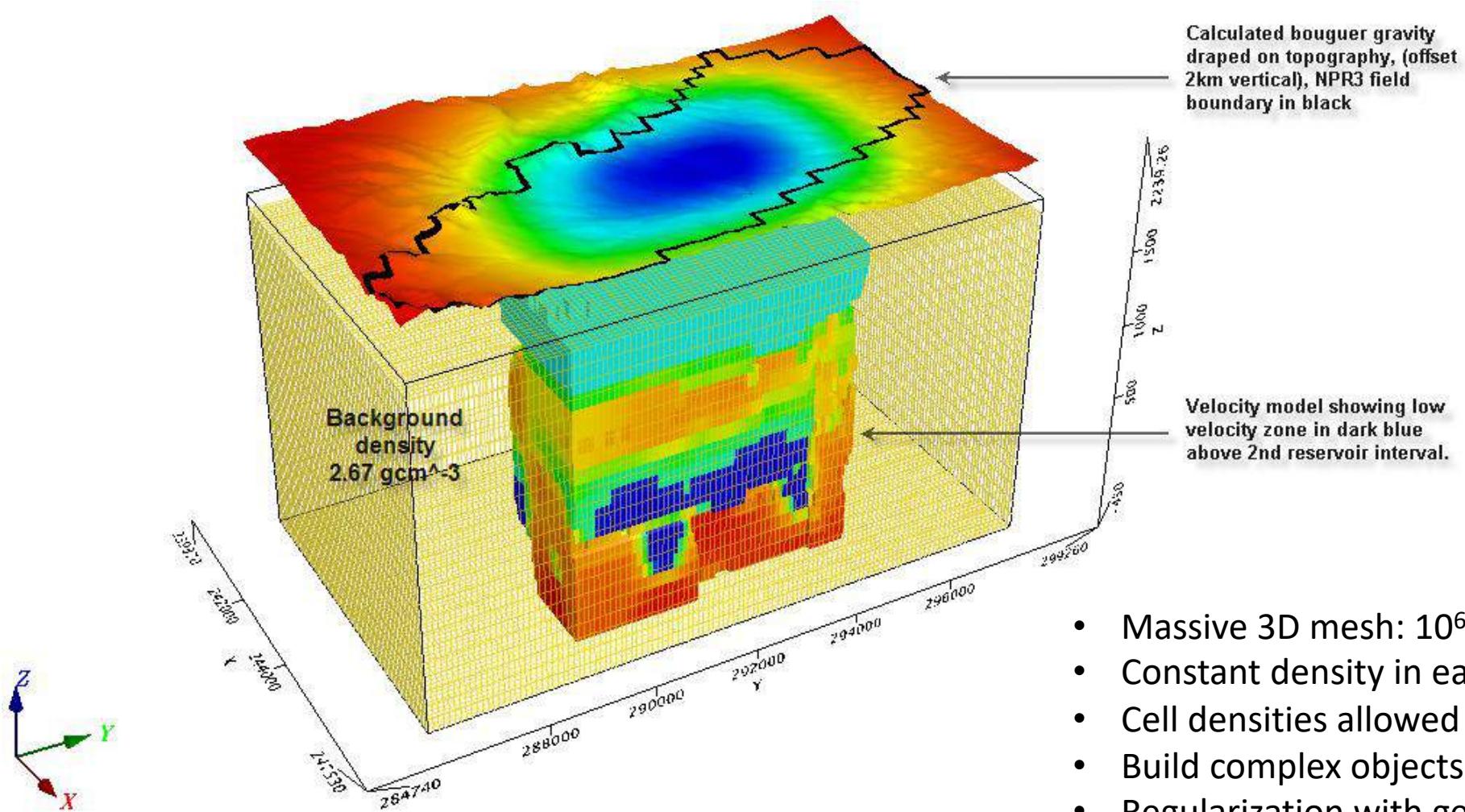
$A_{ij}$ : Contribution of the  $j^{\text{th}}$  element to the  $i^{\text{th}}$  datum

Linear problem but the **inverse problem is ill-posed!**

So the piece-wise constant density model  $\rho$  is

$$\left[ \begin{array}{c} \rho \\ \\ \\ \end{array} \right] = \left[ \begin{array}{c} \\ \\ \\ \end{array} \right]^{-1} \left[ \begin{array}{c} A \\ \\ \\ \end{array} \right] \left[ \begin{array}{c} d \\ \\ \\ \end{array} \right]$$

# 3D Voxel Inversion



# Planetary Science – Crater on Moon



## Gravity field of the Orientale basin from the Gravity Recovery and Interior Laboratory Mission

Maria T. Zuber<sup>1,\*</sup>, David E. Smith<sup>1</sup>, Gregory A. Neumann<sup>2</sup>, Sander Goossens<sup>3</sup>, Jeffrey C. Andrews-Hanna<sup>4,5</sup>, James W. Head<sup>6</sup>, Walter S. Kiefer<sup>7</sup>, Sami W. Asmar<sup>8</sup>, Alexander S. Konopliv<sup>8</sup>, Frank G. Lemoine<sup>2</sup>, Isamu Matsuyama<sup>9</sup>, H. Jay Melosh<sup>10</sup>, Patrick J. McGovern<sup>7</sup>, Francis Nimmo<sup>11</sup>, Roger J. Phillips<sup>5</sup>, Sean C. Solomon<sup>12,13</sup>, G. Jeffrey Taylor<sup>14</sup>, Michael M. Watkins<sup>8,15</sup>, Mark A. Wieczorek<sup>16</sup>, James G. Williams<sup>8</sup>, Johanna C. Jansen<sup>4</sup>, Brandon C. Johnson<sup>1,6</sup>, James T. Keane<sup>9</sup>, Erwan Mazarico<sup>2</sup>, Katarina Miljkovic<sup>1,17</sup>, Ryan S. Park<sup>8</sup>, Jason M. Soderblom<sup>1</sup>, Dah-Ning Yuan<sup>8</sup>

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<sup>4</sup>Department of Geophysics and Center for Space Resources, Colorado School of Mines, Golden, CO 80401, USA.

<sup>5</sup>Southwest Research Institute, Boulder, CO 80302, USA.

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<sup>7</sup>Lunar and Planetary Institute, Houston, TX 77058, USA.

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<sup>14</sup>Hawaii Institute of Geophysics and Planetology, University of Hawaii, Honolulu, HI 96822, USA.

<sup>15</sup>Center for Space Research, University of Texas, Austin, TX 78712 USA.

<sup>16</sup>Institut de Physique du Globe de Paris, Sorbonne Paris Cité, Université Paris Diderot, 75205 Paris Cedex 13, France.

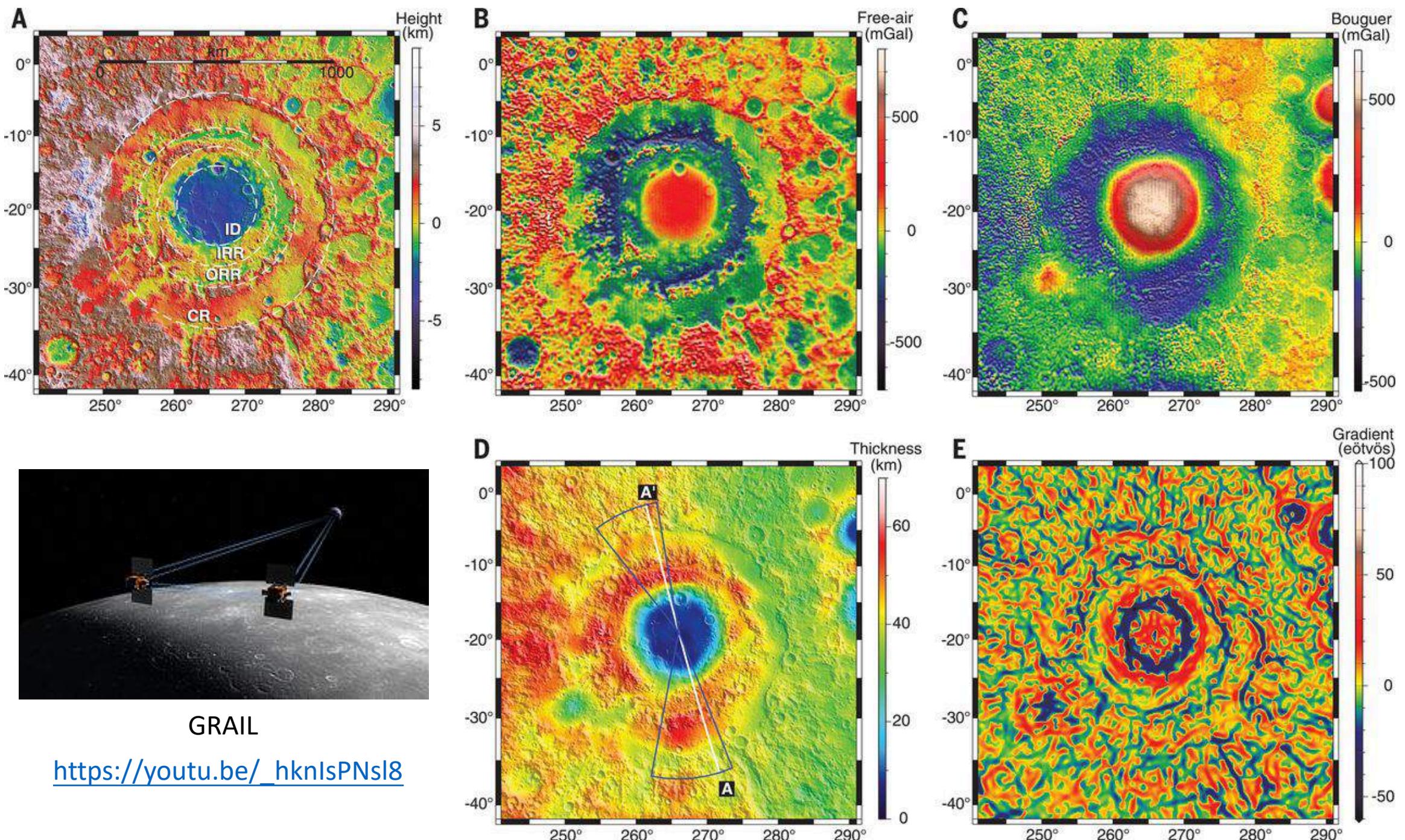
<sup>17</sup>Department of Applied Geology, Curtin University, Perth, Western Australia 6845, Australia.

\*Corresponding author. Email: zuber@mit.edu

– Hide authors and affiliations

Science 28 Oct 2016;  
Vol. 354, Issue 6311, pp. 438-441  
DOI: 10.1126/science.aag0519

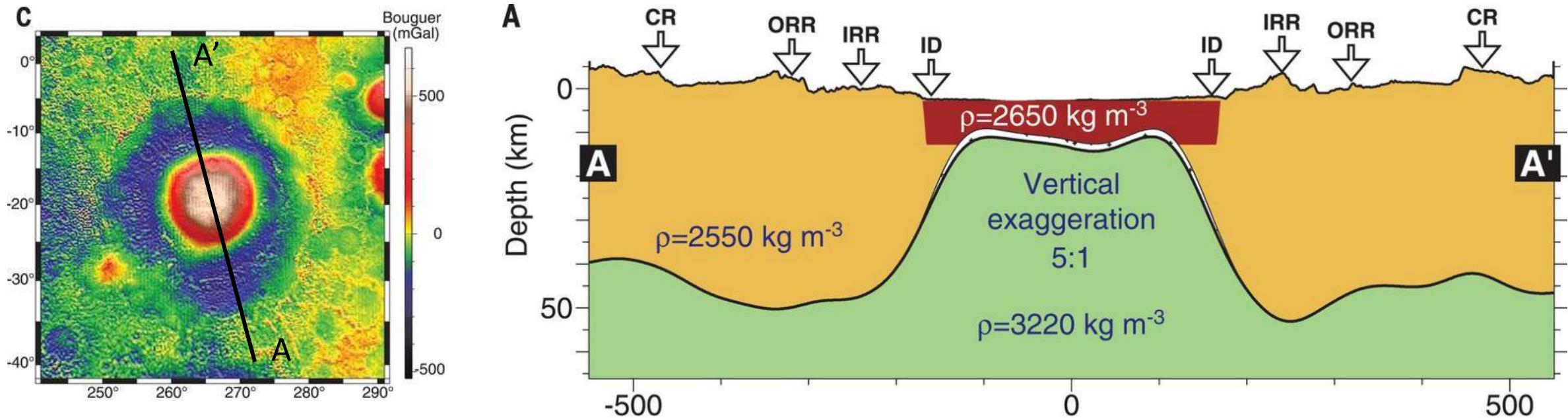
<http://science.scienmag.org/content/354/6311/438>



GRAIL

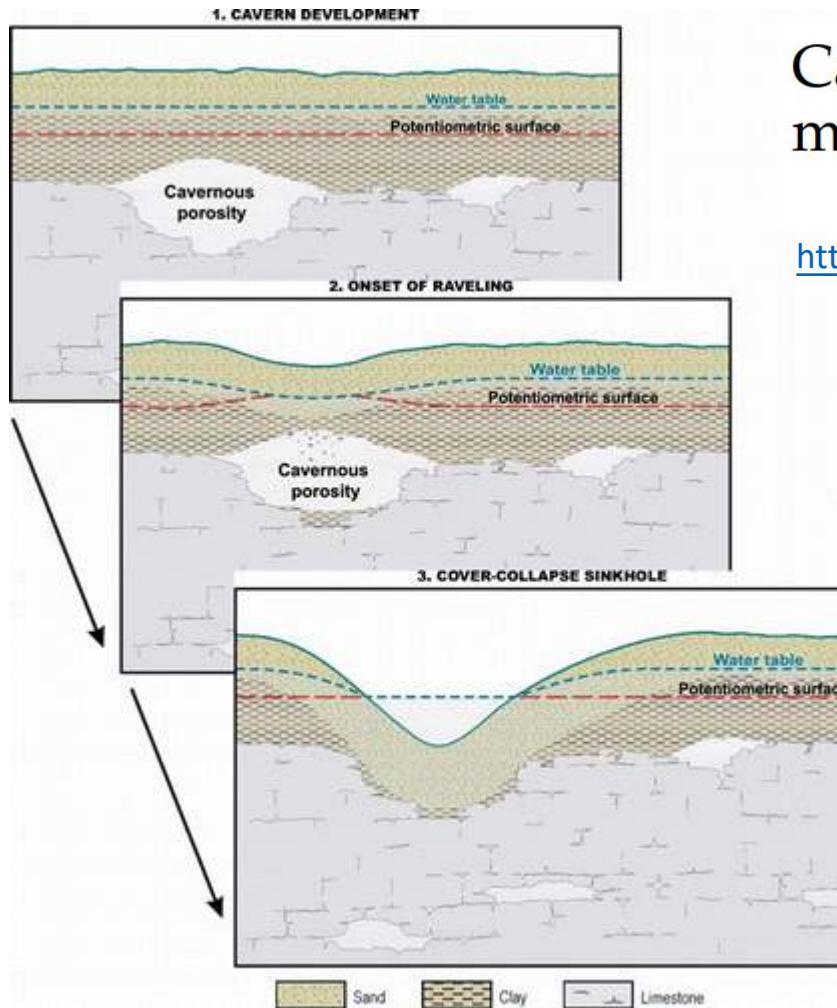
[https://youtu.be/\\_hknlsPNsl8](https://youtu.be/_hknlsPNsl8)

# Density of the Moon's Interior



Can you sketch a density structure along the cross section A-A'?

# Environmental – Sinkholes



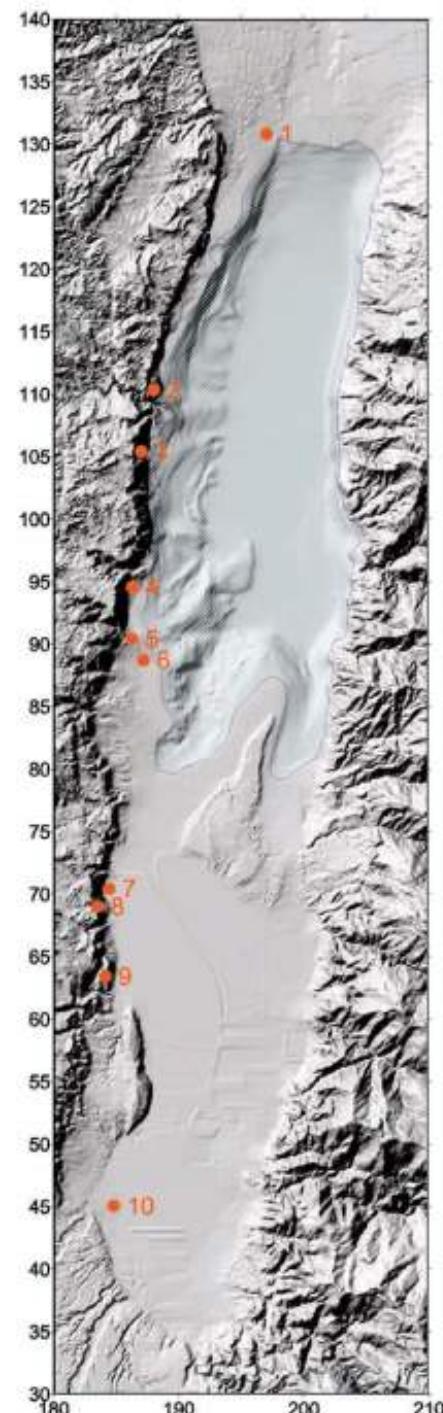
Cave detection and 4-D monitoring: A microgravity case history near the Dead Sea

M. RYBAKOV, V. GOLDSHMIDT, L. FLEISCHER, and Y. ROTSTEIN, *The Geophysical Institute of Israel*

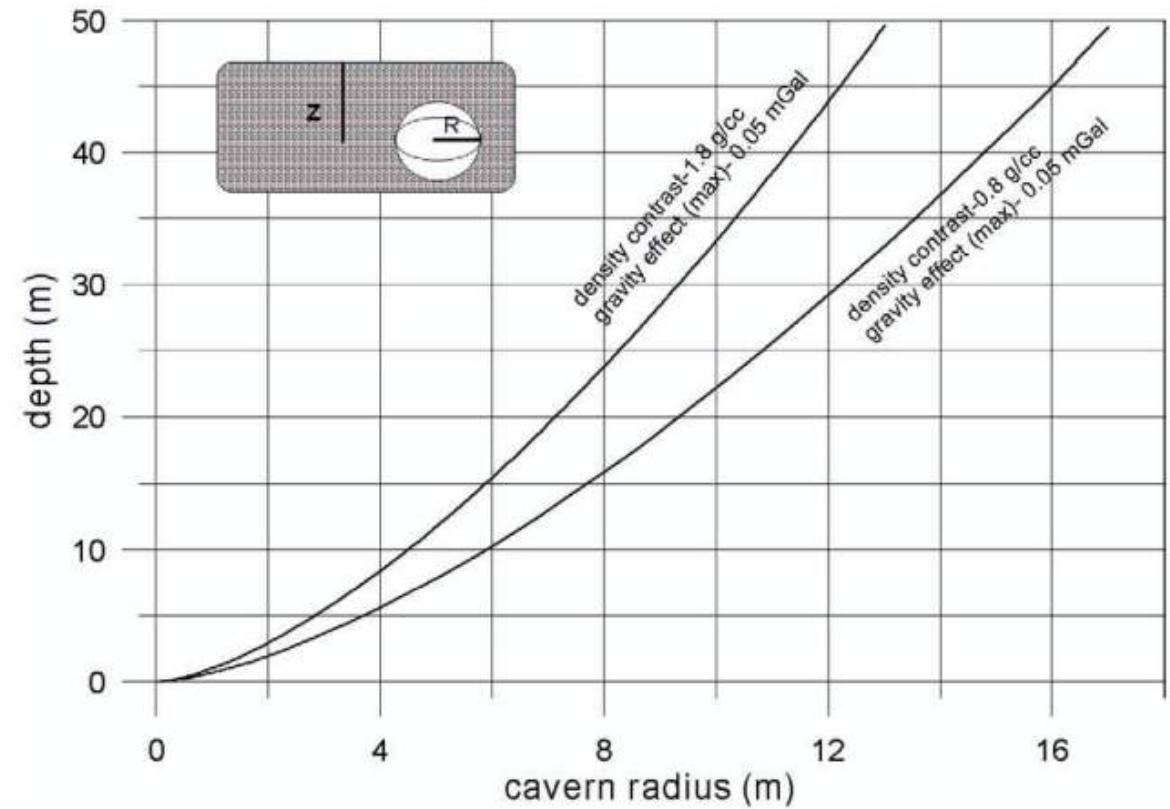
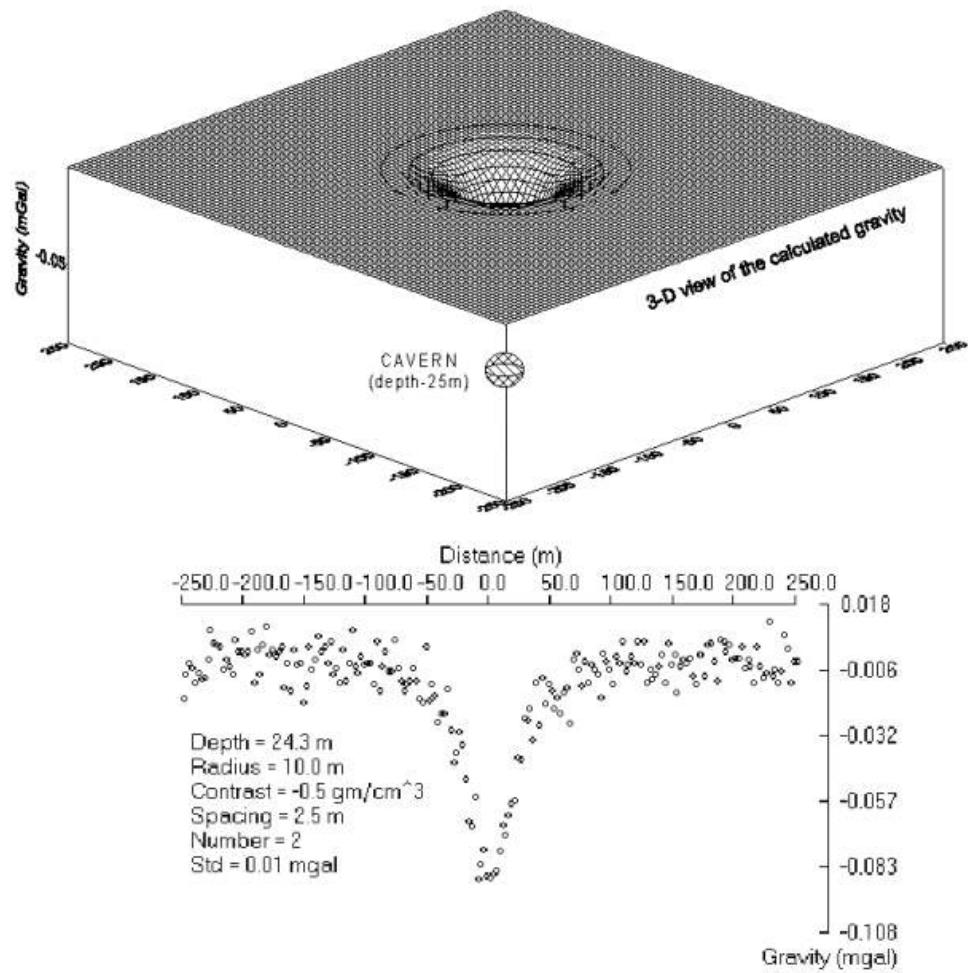
<https://library.seg.org/doi/pdf/10.1190/1.1487303n>



Figure 2. One of largest sinkholes in the Dead Sea area (after Gilat, 1999).

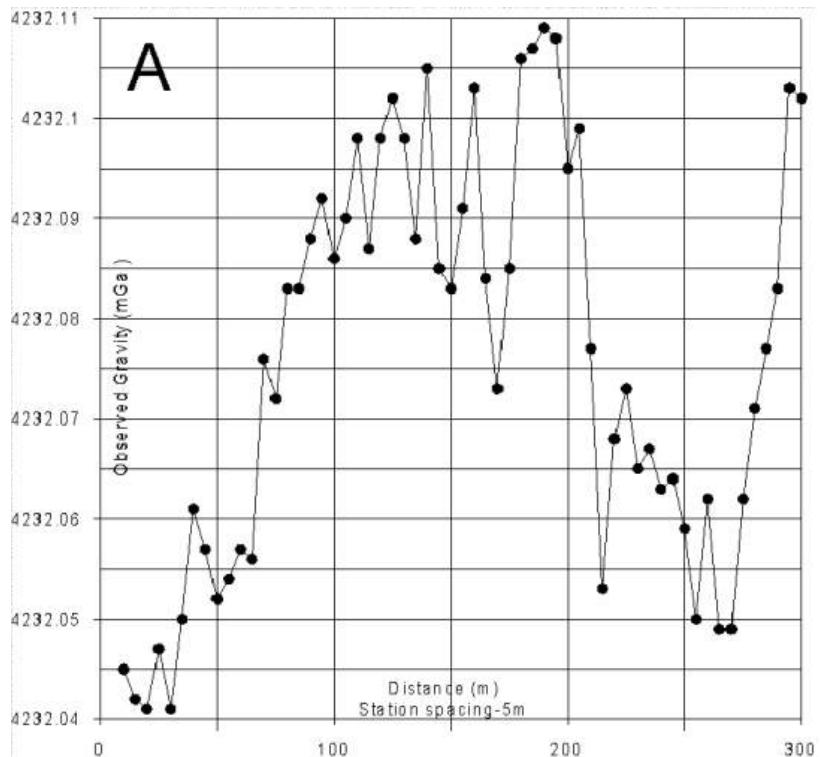


# Forward Modeling: Feasibility Study



**Figure 6. Effect of detectability threshold level and density contrast—maximum depth for detection of spherical concealed cavern. Large density contrast corresponds to air-filled cavern and small density contrast to saltwater-filled cavern.**

# Cavern Mapping Result



Raw gravity data along a line

- Gravimeter accuracy 0.005 mGal
- Scintrex CG-3M: 0.001 mGal
- Geodetic control: Laser Total Station (a few mm)
- Real-time elevation of the instrument
- Base station repeated hourly
- Repeat measurement: 10% of all stations
- Fully terrain corrected: 25-m grid DTM + precise local survey near the station

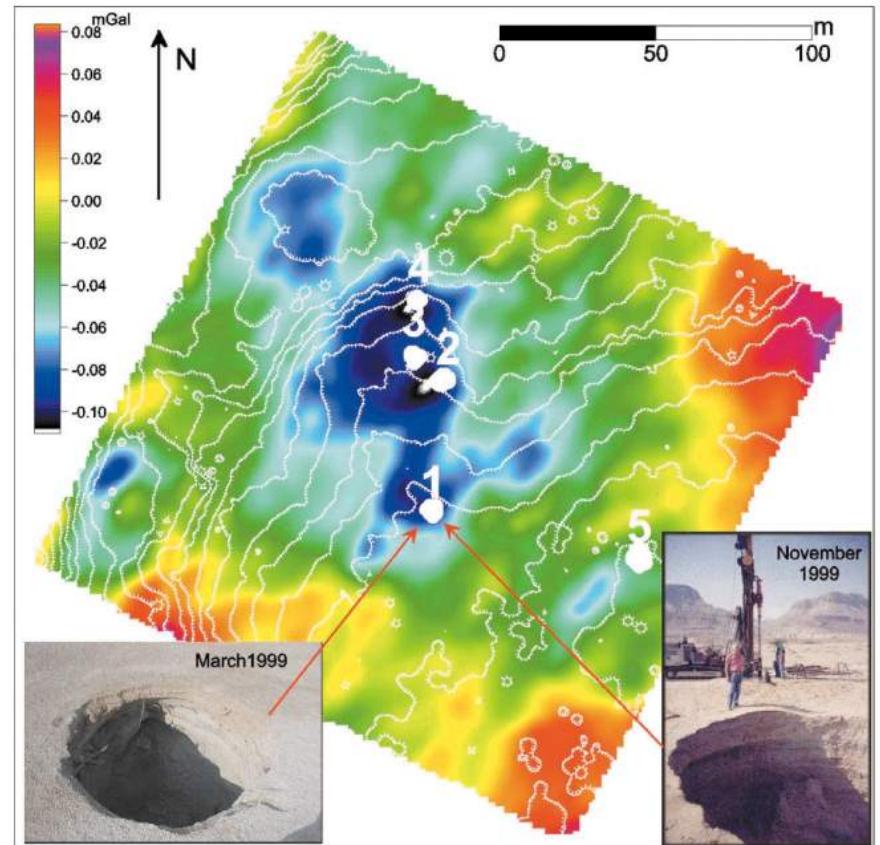


Figure 9. Residual gravity map of the Hever site superimposed by detailed topography (white contours - 0.25-m interval). White circles denote open sinkholes. Photos show growth of sinkhole 1 between March and November 1999.

# Military – Submarine Navigation

**How do submarines use gravity gradients to avoid collisions with underwater mountains?**

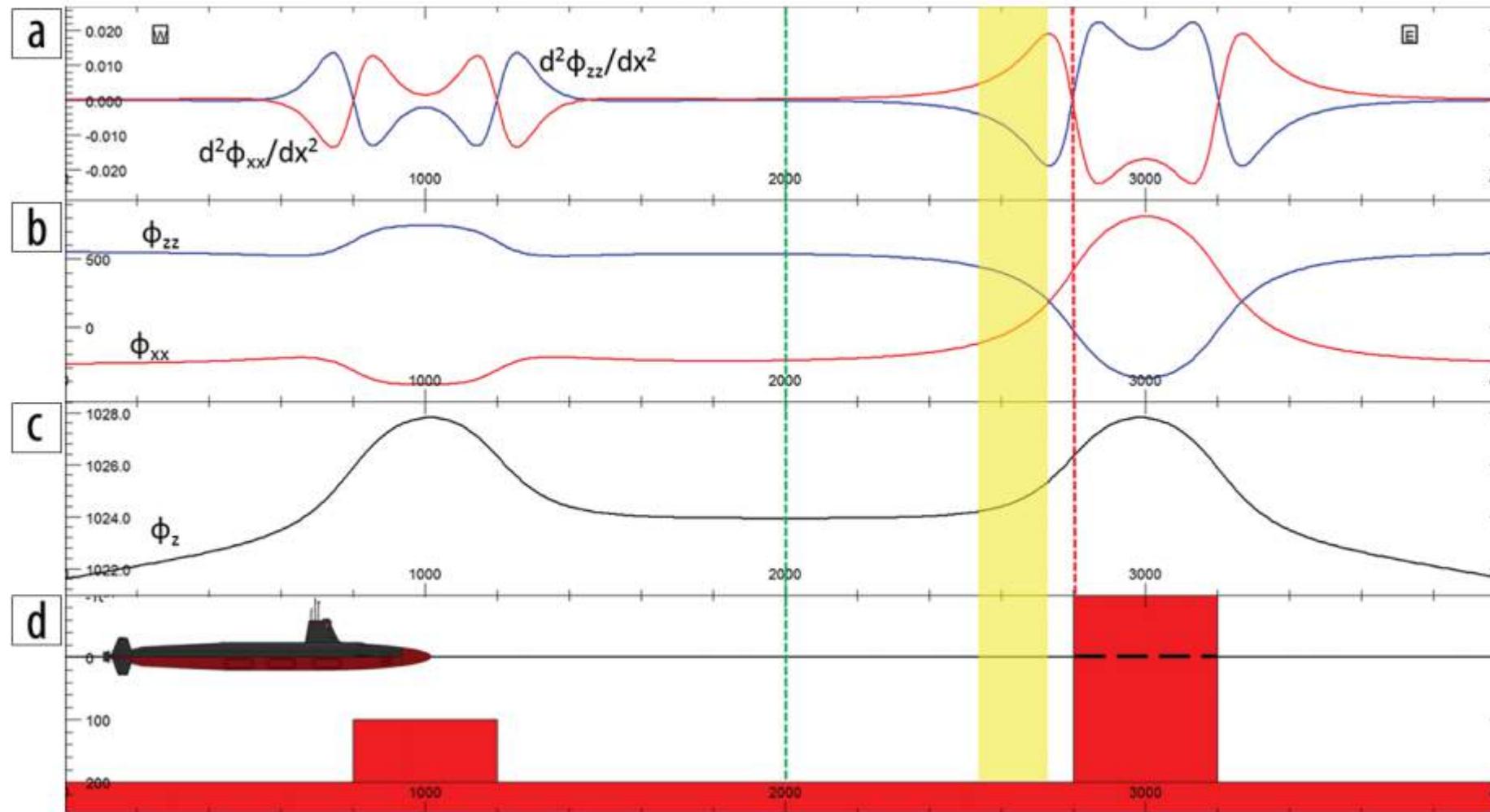
Carlos Cevallos<sup>1</sup>

<https://library.seg.org/doi/pdf/10.1190/tle34121498.1>

Gradient Tensor

$$\begin{bmatrix} G_{xx} & G_{xy} & G_{xz} \\ G_{yx} & G_{yy} & G_{yz} \\ G_{zx} & G_{zy} & G_{zz} \end{bmatrix}$$

# Military – Submarine Navigation



## Collision warning:

- $\Phi_{xx}$  is increasing
- $\Phi_{zz}$  is diminishing
- The second horizontal derivatives of  $\Phi_{xx}$  and  $\Phi_{zz}$  attain a maximum and a minimum, respectively

Can gravity gradient be used to detect another submarine?

# Summary of Gravity

- Density: Which heavy? Which light?
- How to detect an object (like cavity) below subsurface?
- Properties of gravity data: Superposition, ambiguity,  $1/r^2$  decay
- Approaches to identify sources of signals:
  - Regional removal
  - Upward/downward continuation
  - Derivatives
  - Full tensor gradients
- Gravity inversion
- Applications: Planetary science, environmental, military, basin, etc.