



# Real-Time Geological Inversion for Subsurface Decision-Making

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# Outline

- Lecture 1: Geological inversion for geosteering
  - Overview of geosteering
  - Different types of data and inverse problems
  - Reference problem of sequential inversion
  - Simple inversion
  - Regularization
- Exercise
- Lecture 3: Filtering and multi-modal inversion
  - Particle filter
  - Direct multimodal inversion with machine learning

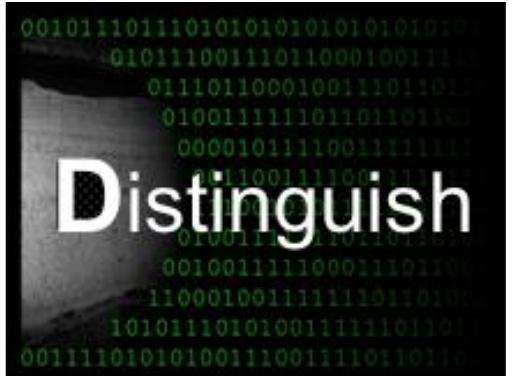


# Acknowledgments



The Research Council of Norway

sfi  
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Research-based  
Innovation  
The Research Council of Norway



The Research  
Council of Norway

# Thanks

- Organizers – for invitation
- Anna Kvashchuk – taking the kids and feedback on content
- Kristian Fossum – feedback on content
- Nazanin Jahani – slides
- Ressi Muhammad – slides
- Yasaman Cheraghi – slides
- ROGII Inc. – for Geosteering World Cup Data and animations

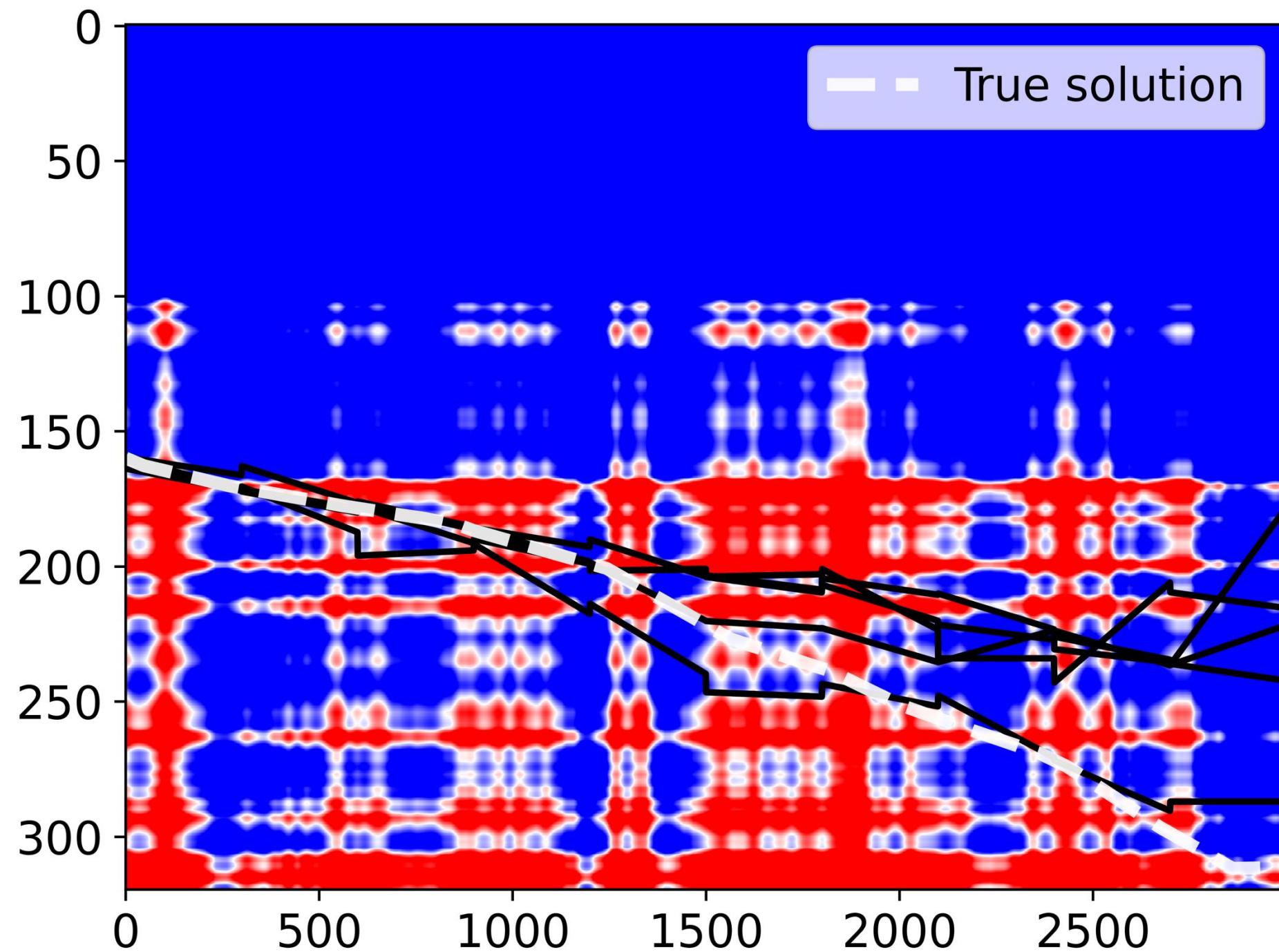


## Exercise 1: results

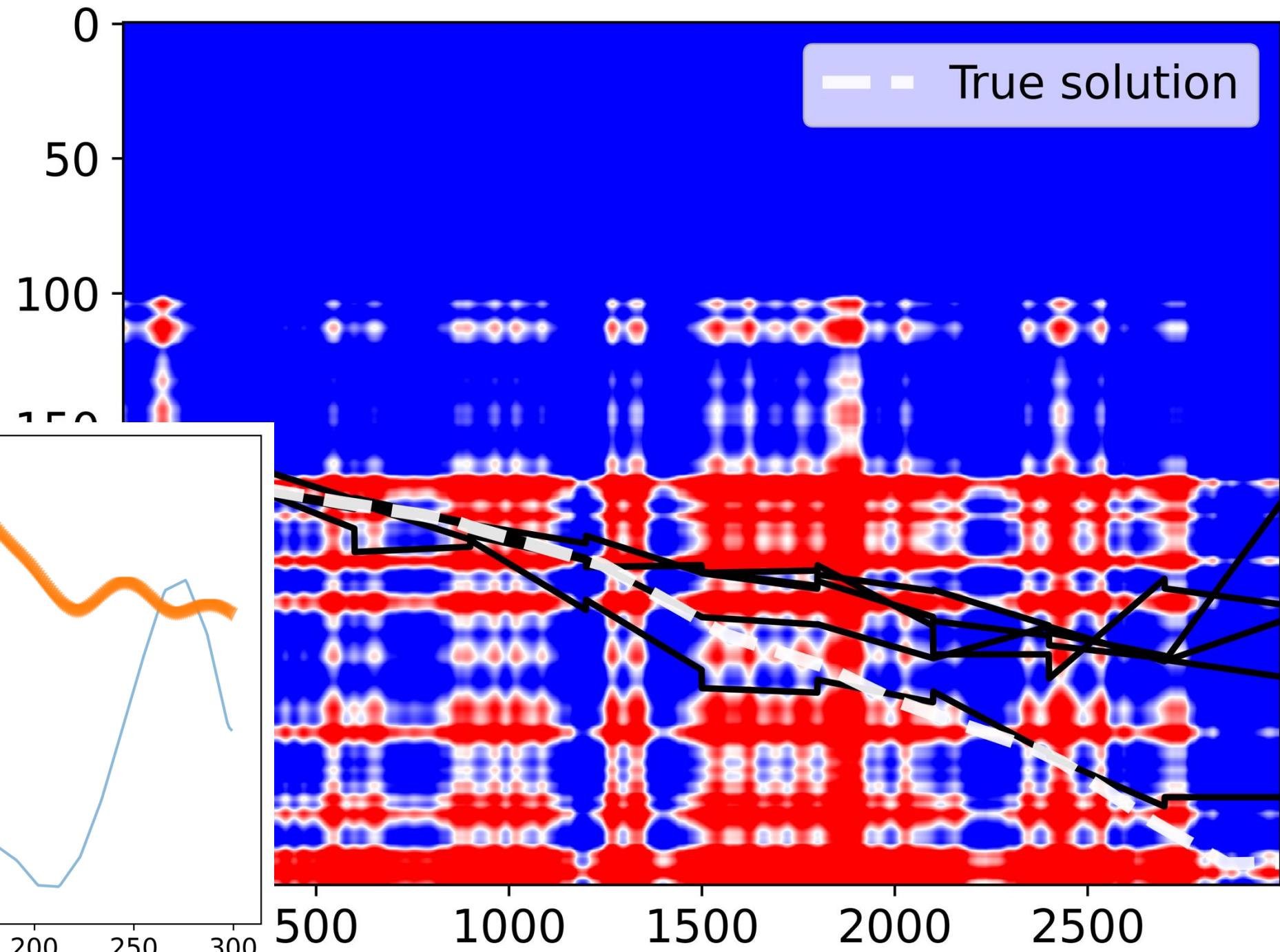
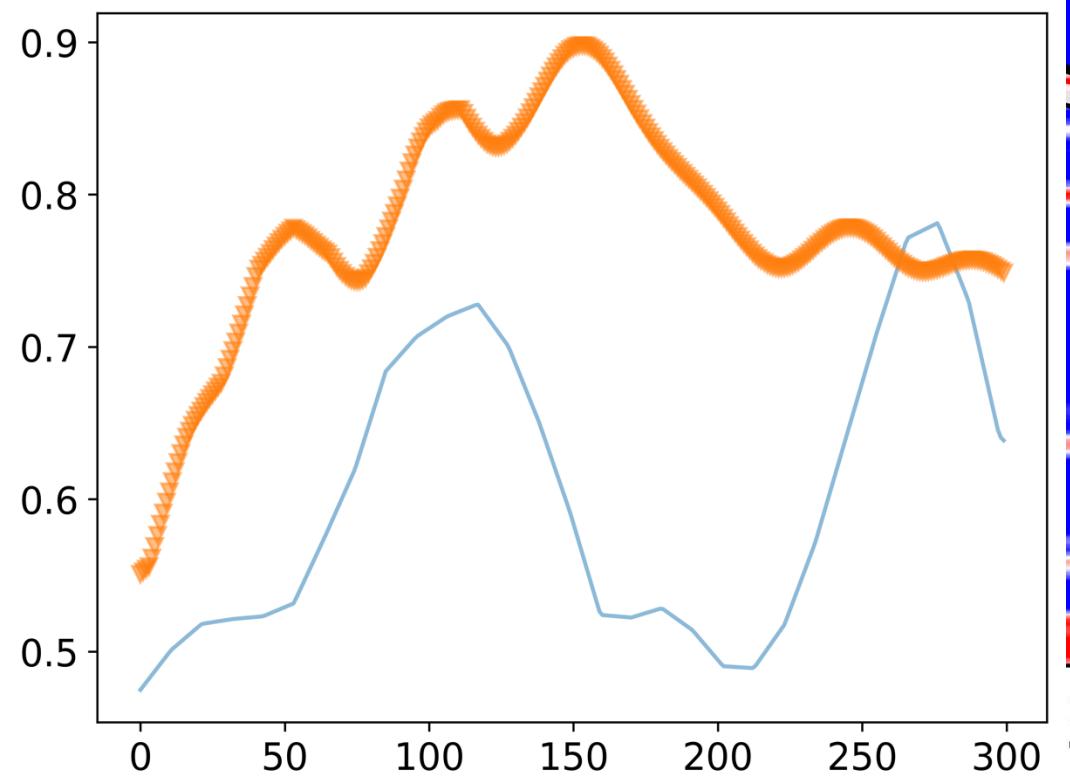
Stratigraphic inversion



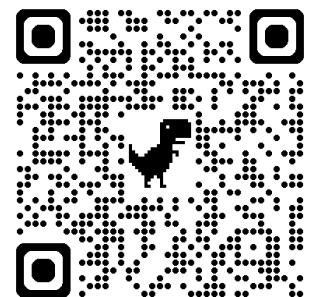
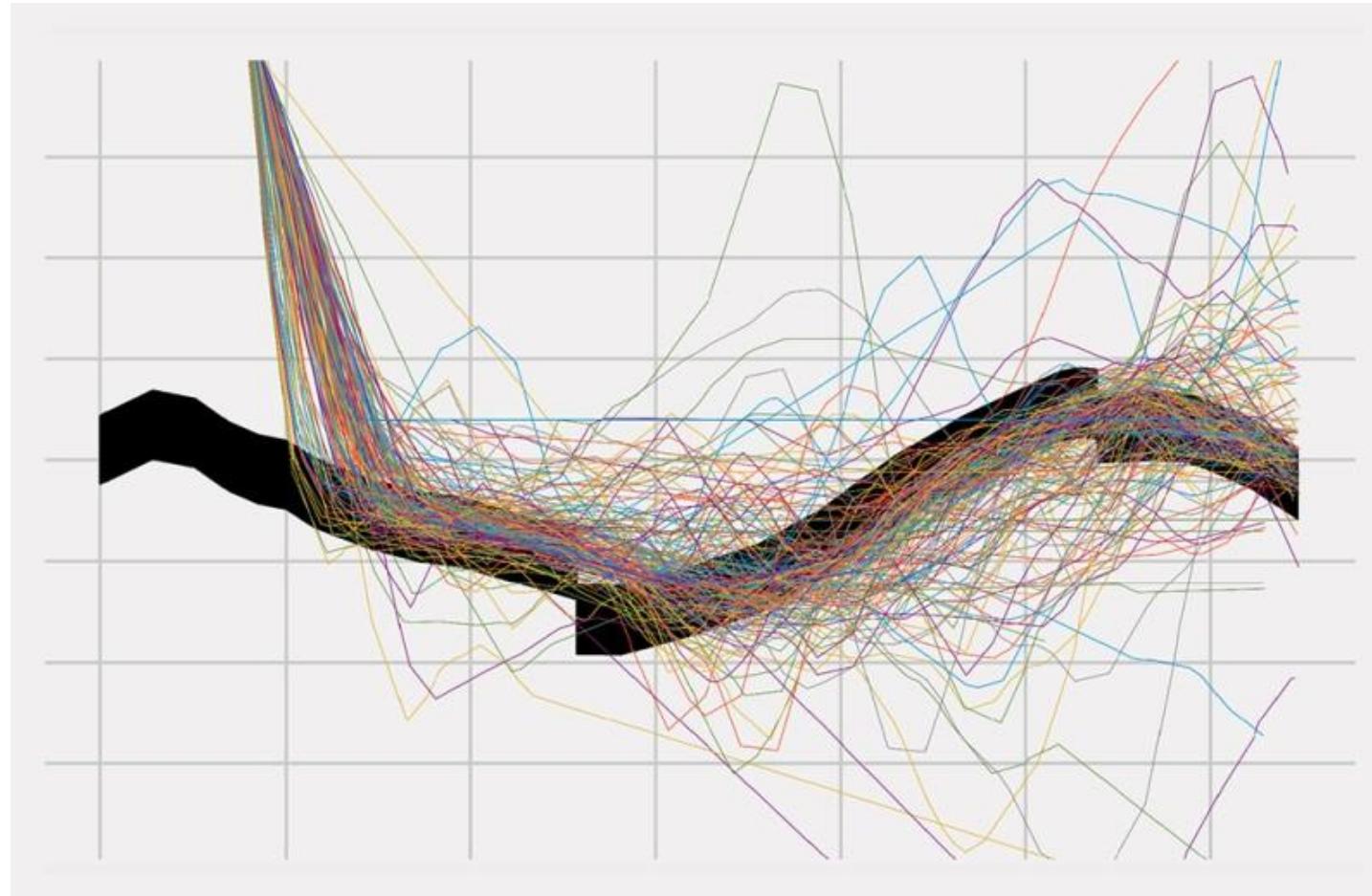
# Competition results



# Competition results



# Geosteering decisions are challenging





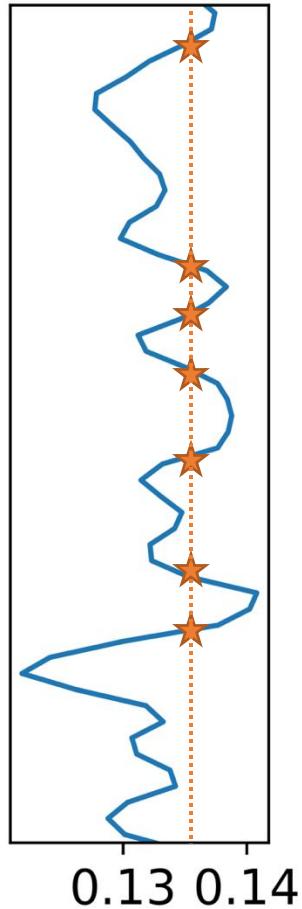
# Lecture 3.1:

## Filtering problem



Interpretations  
of a single data point

Offset log



# Difficulty with low-data geosteering

- Log data has multiple depth interpretations
- Picking one interpretation or averaging leads to errors

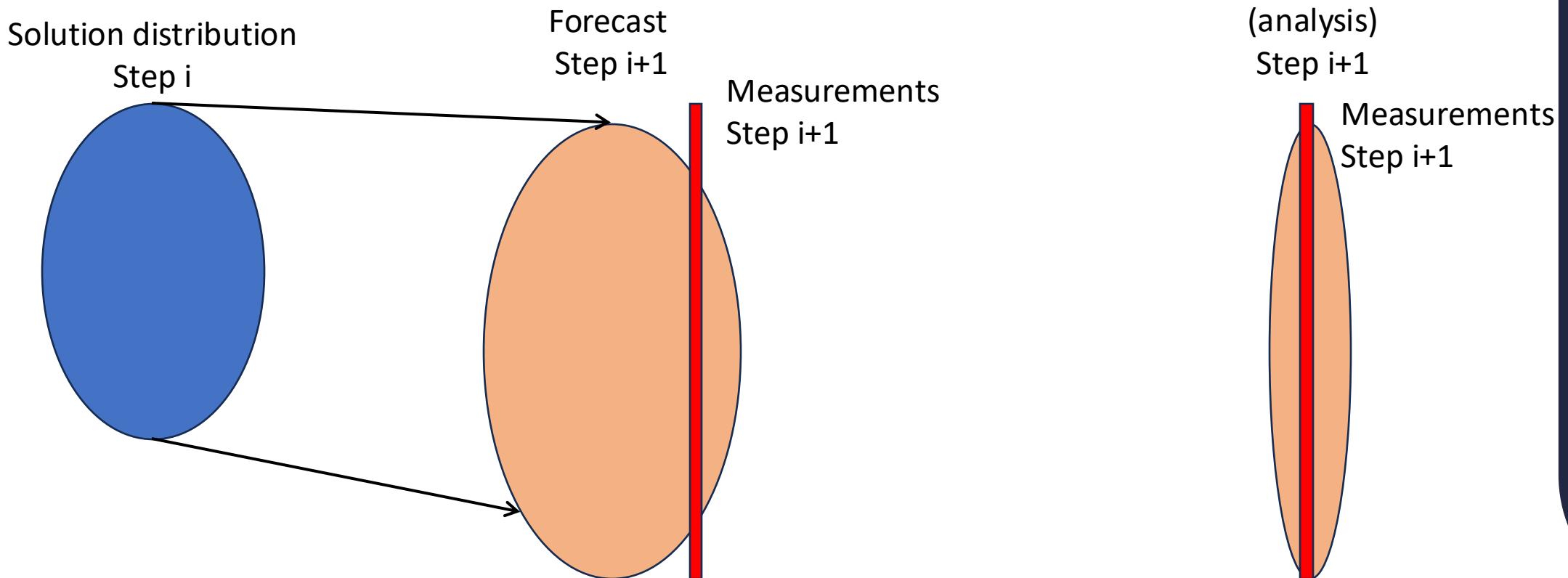
## Multi-modal probabilistic inversion

can improve

- Geological understanding
- Geosteering decisions

# Filtering problem

determining the state of a system from an incomplete and potentially noisy set of observations



# Filtering problem for boundary function

[with some abuse of notation]

- $b_{k,i+1}^f \equiv b_k^f(x_{i+1}) = B(x_i, w_{i,k})$ 
  - $b_k$  form a distribution of solutions
  - $B(x_i, w_{i,k})$  - probabilistic “forward” model of geology
- $f_k(x_{i+1}) = f(b_k(x_{i+1})) + v_{i+1}$ 
  - $f_k$  form a distribution of measurement prediction

# Filtering problem for boundary function

[with some abuse of notation]

- $b_k(x_{i+1}) = B(x_i, w_{i,k})$ 
    - $b_k$  form a distribution of solutions
    - $B(x_i, w_{i,k})$  - probabilistic “forward” model of geology
  - $f_k(x_{i+1}) = f(b_k(x_{i+1})) + v_{i+1}$ 
    - $f_k$  form a distribution of measurement predictions
    - $v_{i+1}$  - added measurement errors
  - $g_{i+1} \equiv g(x_{i+1})$  - observations
- Filtering task is to find
- $\widetilde{b_{k,i+1}} \equiv b_k(\widetilde{x_{i+1}}) \sim \rho(\widetilde{b_{i+1}} | g_{0:i+1}) \propto \rho(g_{i+1} | \tilde{b}_{i+1}^f) \cdot \rho(\tilde{b}_{i+1}^f)$

# Filtering problem for boundary function

[with some abuse of notation]

Filtering task is to find

$$\bullet \tilde{b_{i+1}} \sim \rho(\tilde{b_{i+1}} | g_{0:i+1}) \propto \rho(g_{i+1} | \tilde{b}_{i+1}^f) \cdot \rho(\tilde{b}_{i+1}^f)$$

Density of  
New distribution  
of predictions  
corrected to data

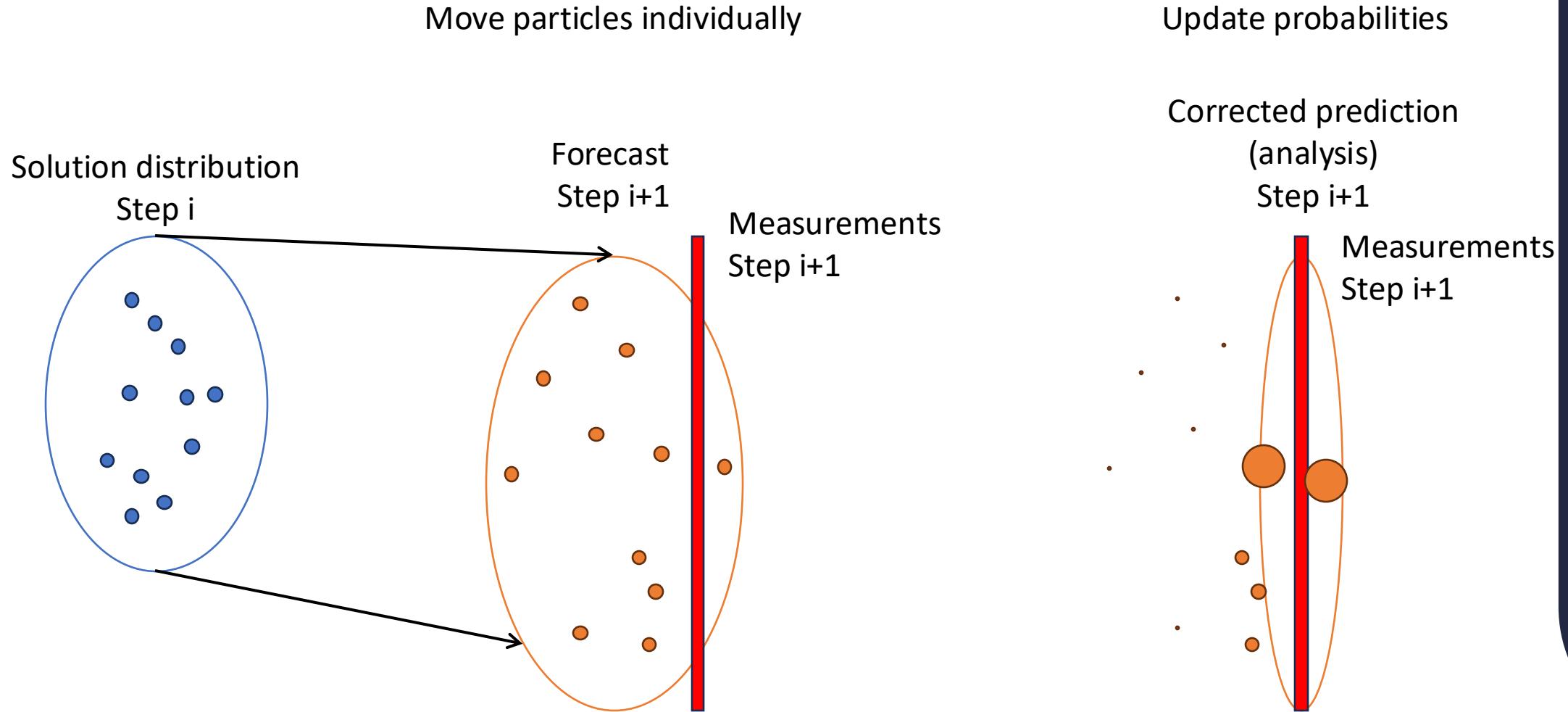
Likelihood of  
data  $g$  given the  
*forecast*

Density of  
the forecast  
distribution

Bayes' theorem:

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

# Particle filter



# Particle filter

Propagation

- $b_{k,i+1}^f \equiv b_k^f(x_{i+1}) = B(x_i, w_{i,k})$

Measurement estimation

- $f_k(x_{i+1}) = f(b_k(x_{i+1})) + v_{i+1}$

Update of weights

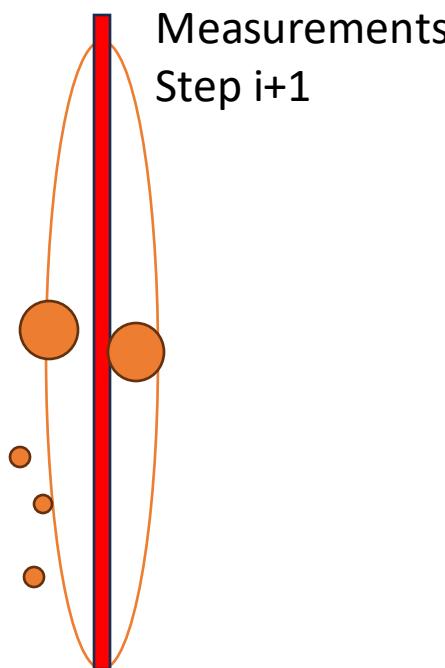
- $w_{k,i+1} \propto w_{k,i+1} C \exp\left(-\frac{(f_{k,i+1} - g_{i+1})^2}{2\sigma^2}\right)$

Gaussian distance to measurements

# There is a problem with the new distribution

Update probabilities

Corrected prediction  
(analysis)  
Step i+1

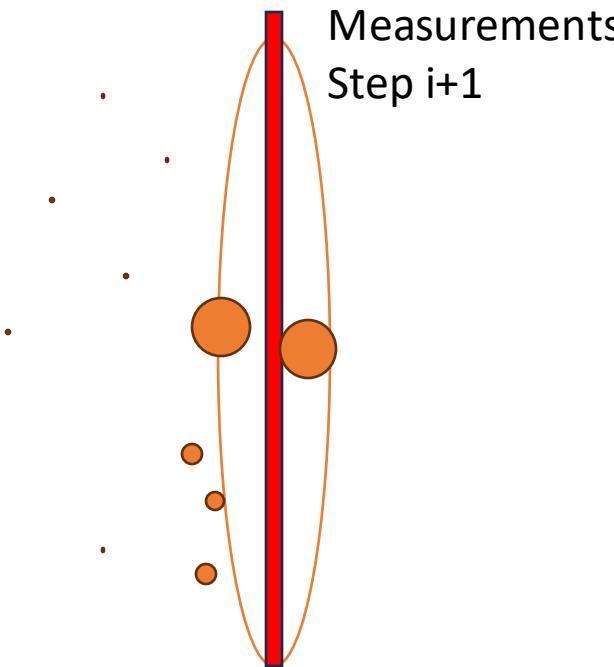


# There is a problem with the new distribution

Update probabilities

Corrected prediction  
(analysis)  
Step i+1

Measurements  
Step i+1

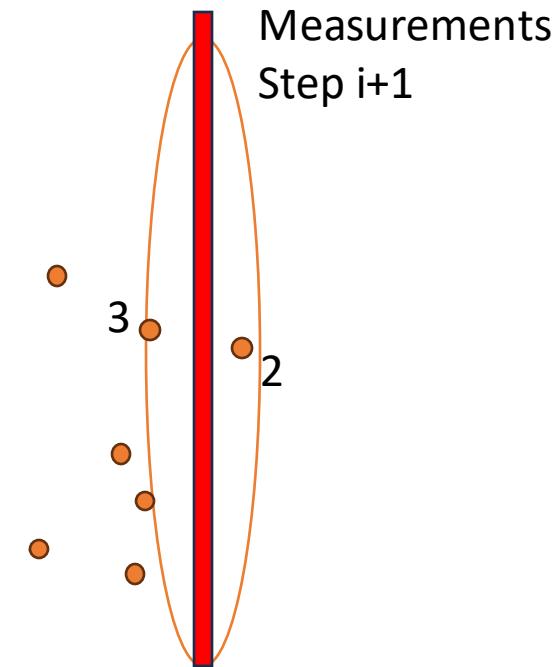


## Resampling

Update probabilities

Corrected prediction  
(analysis)  
Step i+1

Measurements  
Step i+1



# Resampling

- Pick particles proportional to their weight
- The duplicates will naturally drift apart during next step

A better more detailed tutorial on particle filters:

- <https://ieeexplore.ieee.org/document/978374>

A filtering library from colleagues in Bergen:

- <https://github.com/nansencenter/DAPPER>

# Filtering for the geosteering problem

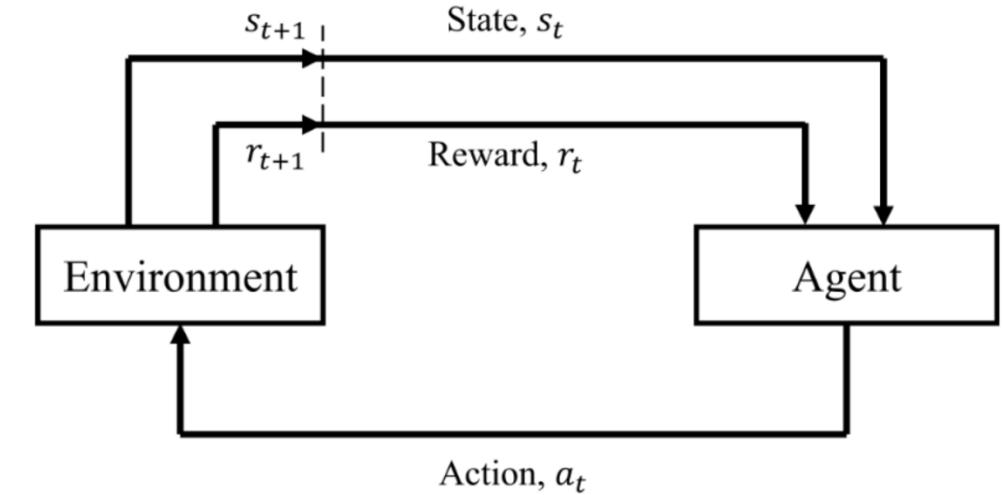
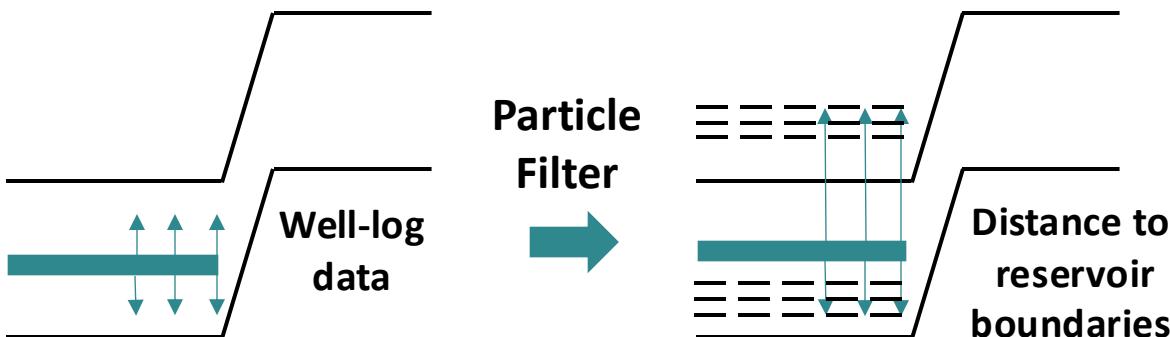
- Forecast
  - Predictive model of geology
  - Measurement model
- Analysis
- Resampling
- Tricky
  - Not available
  - Simple for low-data
- Standard
- Standard

# PF-based Pluralistic Geosteering Robot

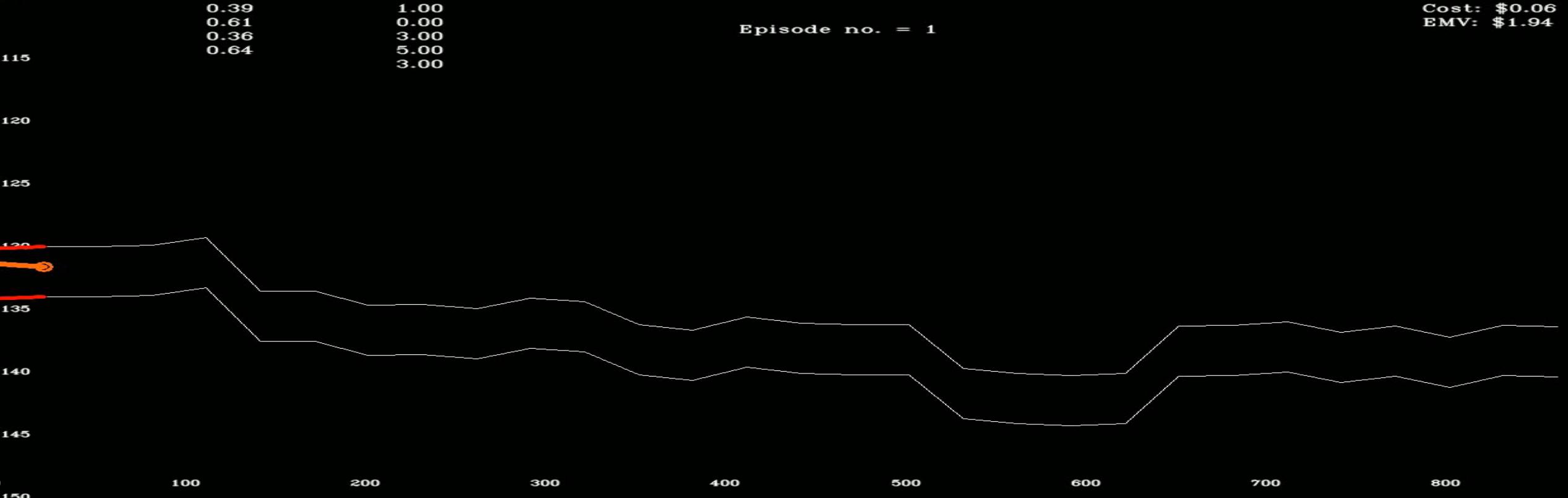
- From papers
  - by Ressi B. Muhammad; Yasaman Cheraghi; Sergey Alyaev; Apoorv Srivastava; Reidar B. Bratvold,
  - SPE J. (2025) <https://doi.org/10.2118/218444-PA>
  - Conference (2024) <https://dx.doi.org/10.2118/218444-MS>

# Pluralistic Geosteering Robot

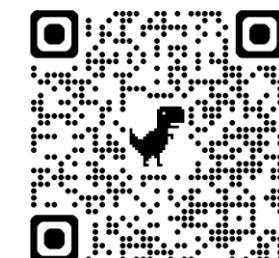
- Pluralistic robot parts
- PF processes real-time well-log data **to make inferences about stratigraphic layers around the bit**
- RL uses multiple estimates **to make decisions**



# RL learning process on a simple example



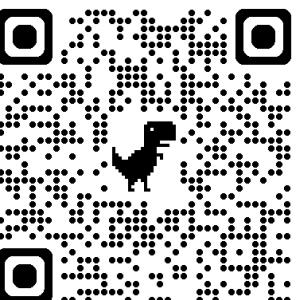
[2310.04772] Optimal Sequential Decision-Making in Geosteering: A Reinforcement Learning Approach (arxiv.org)





**PF + RL beats  
PF + Rule-based method  
Pure RL-based AI solution**

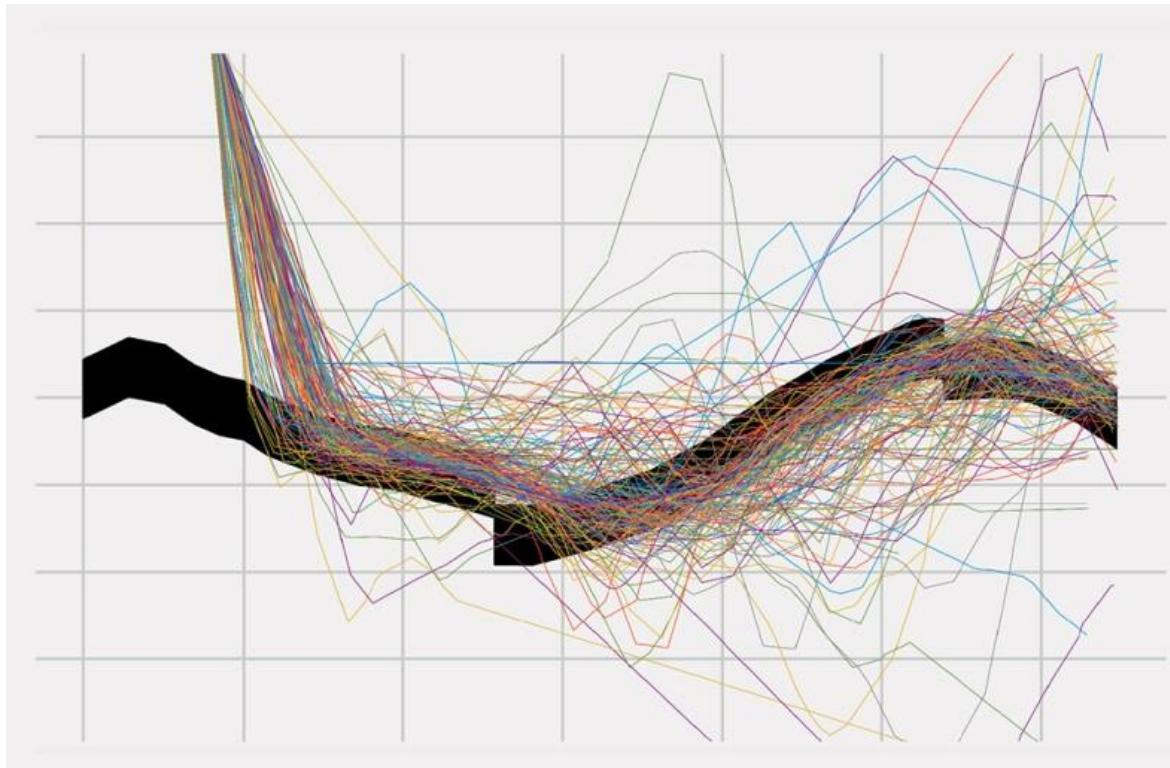
Methods	Input	Rewards	Reservoir contact (%)	MAE of Input
Rule-based <sup>13</sup>	1 Look-ahead	-101.36	54.75	4.27
Rule-based <sup>13</sup>	5 Look-ahead	-105.95	52.70	4.27
RL-Log	Gamma-ray	-74.27	66.84	-
RL-Estimation	1 PF	-25.36	88.67	1.29
RL-Estimation	5 PF	-24.99	88.91	1.31



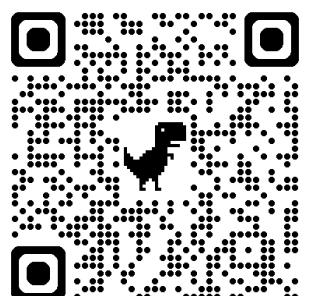
[\[2402.06377\] High-Precision Geosteering via Reinforcement Learning and Particle Filters \(arxiv.org\)](https://arxiv.org/abs/2402.06377)

# Comparison Against Human Experts

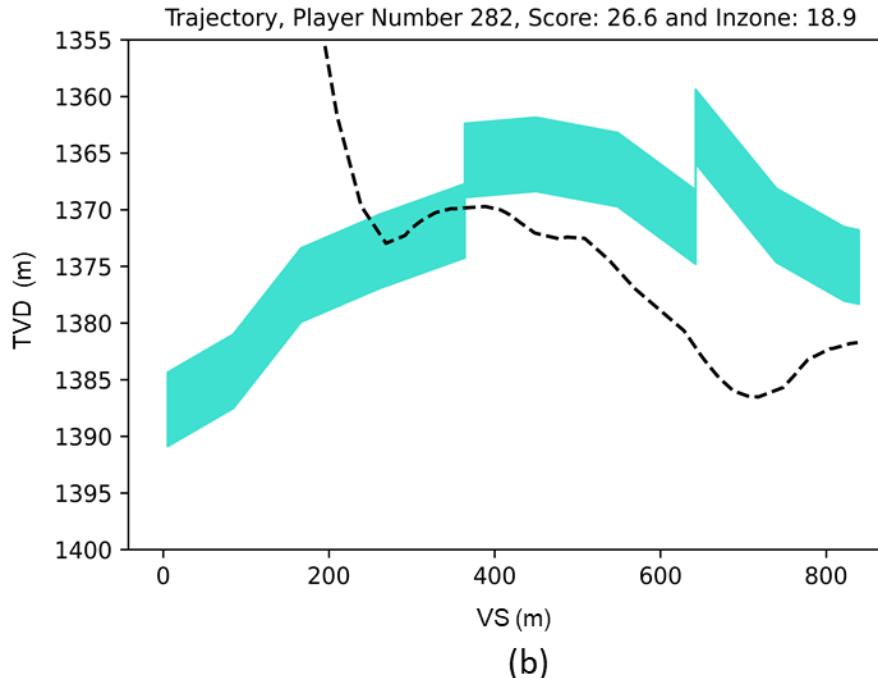
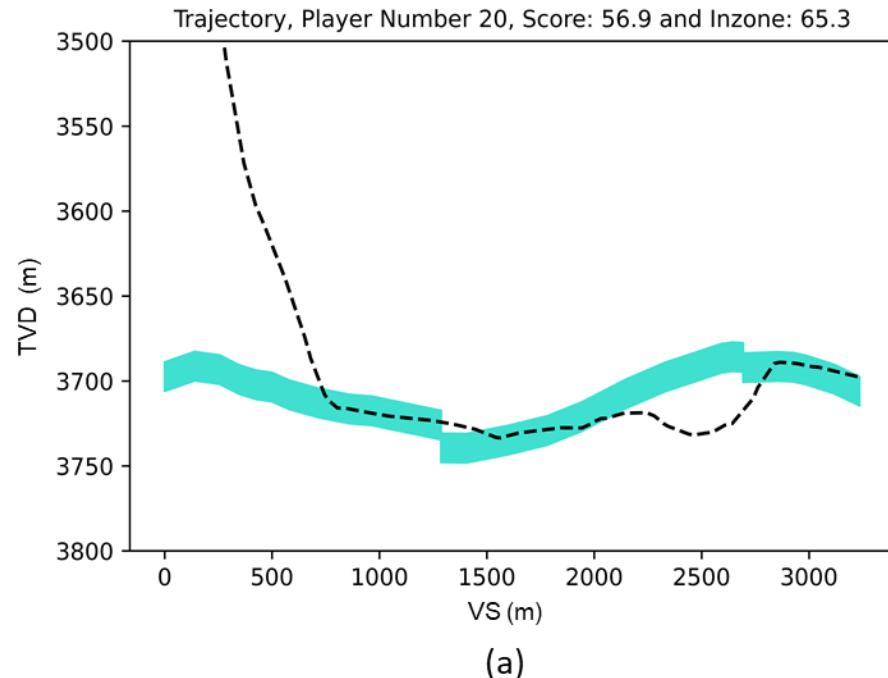
- Challenge: Surpass the performance of **the top quartile** of competitors **in the Geosteering World Cup (GWC) 2021.**



[What Can We Learn After 10,000 Geosteering Decisions? | SPE/AAPG/SEG](#)  
[Unconventional Resources Technology Conference | OnePetro](#)

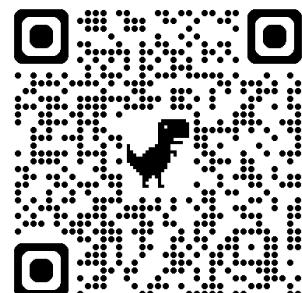


# Training data from geosteering experts



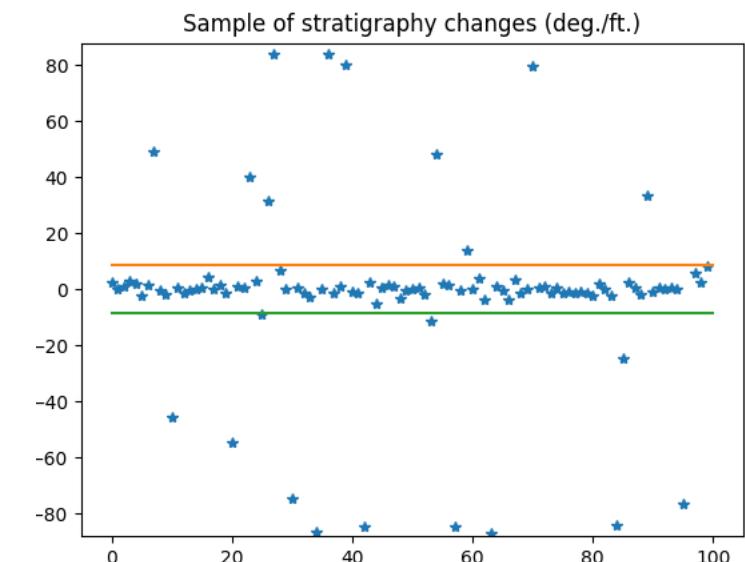
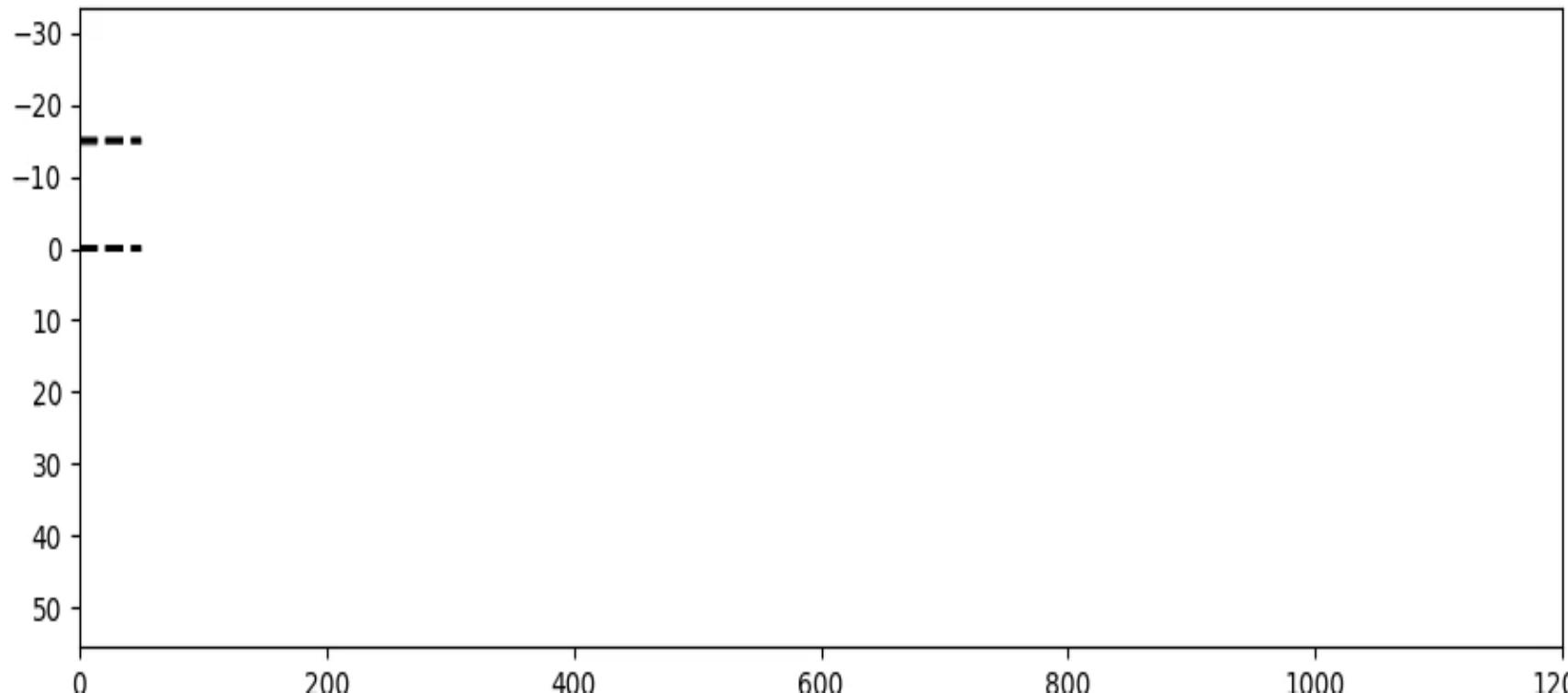
- Over 100 participants
- Over 50 decisions to make
- Almost 10000 near-well interpretations

[What Can We Learn After 10,000 Geosteering Decisions?](#) |  
[SPE/AAPG/SEG Unconventional Resources Technology Conference](#) |  
OnePetro



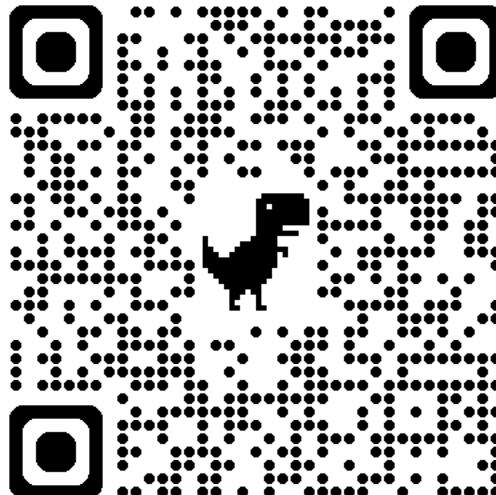
# Stochastic Model for Geological Changes

- Kernel Density Estimation (KDE) based on geological interpretations made by experts during GWC 2021.



# Can you do better?

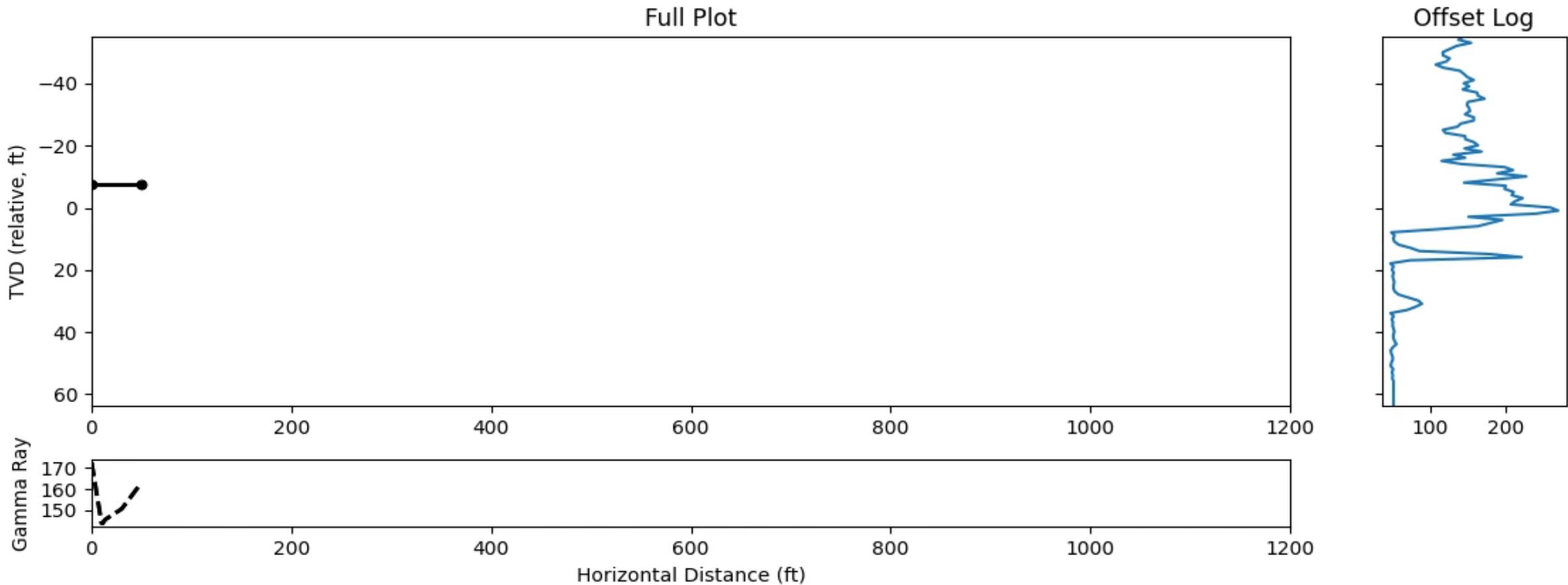
- As a mathematician I would like to know that too...
- Data competition for generating 1D geology on Kaggle:
  - Small monetary prizes
  - Possibility to publish your work in a benchmark journal article
  - Submission deadline in the end of Spring Semester 2025



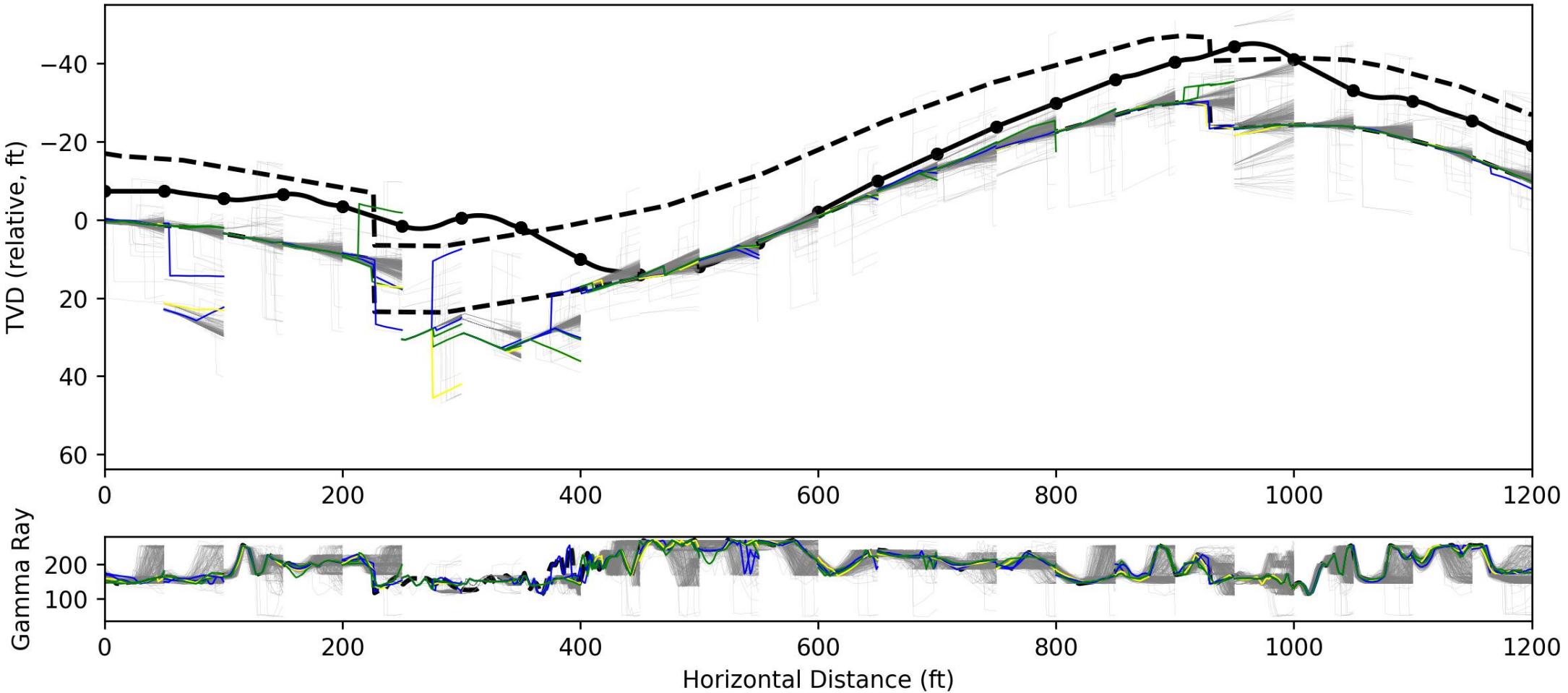
<https://www.kaggle.com/competitions/geology-forecast-challenge/overview>

# Results when starting from within the layer

## Illustration of “Pluralistic” Robot



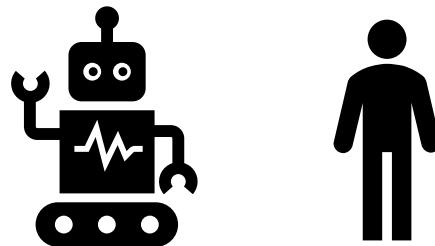
# Results when starting from within the layer



# Stability of the robot

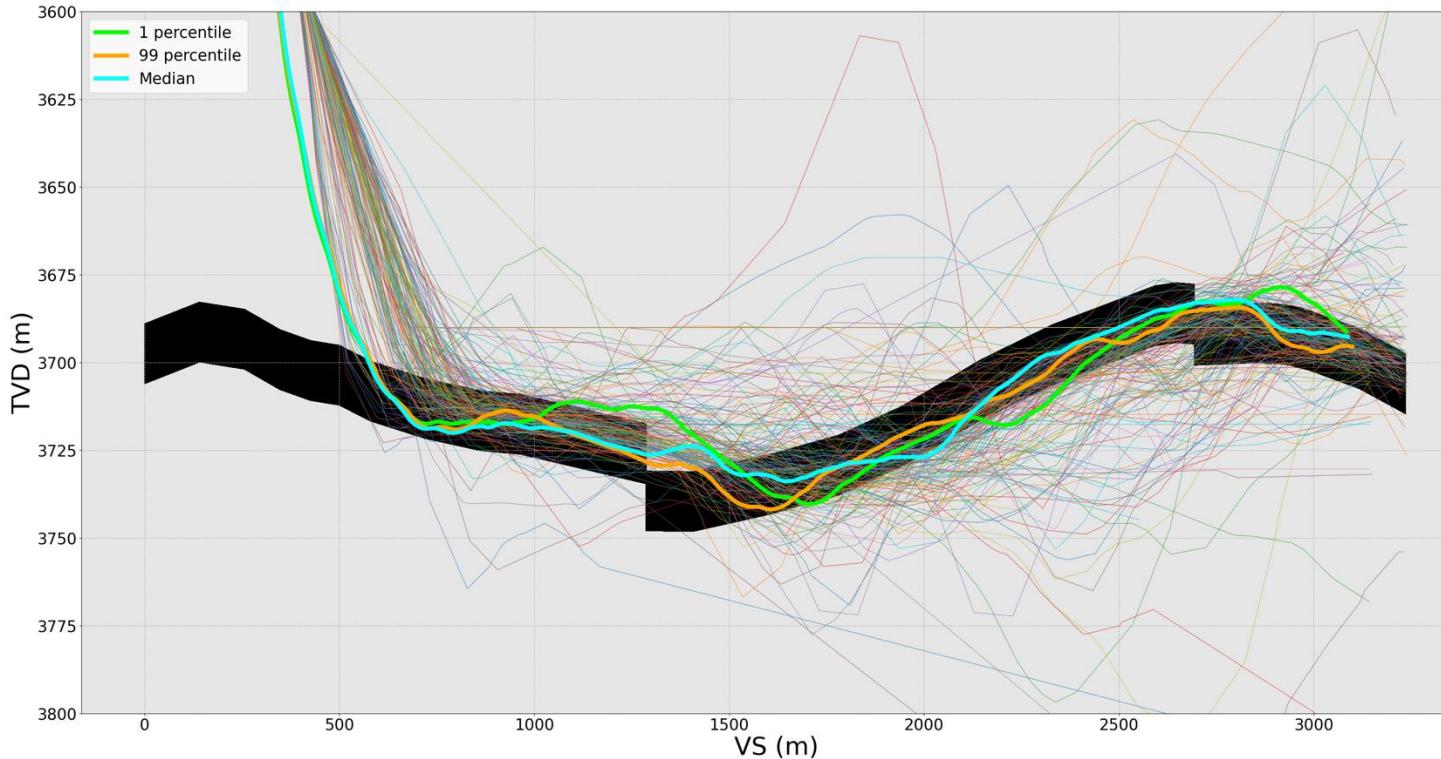
- In mathematics, **stability** refers to a property of a system to **remain unchanged or return to equilibrium** after experiencing small perturbations or disturbances.

Does the robot give **consistent and stable** results?



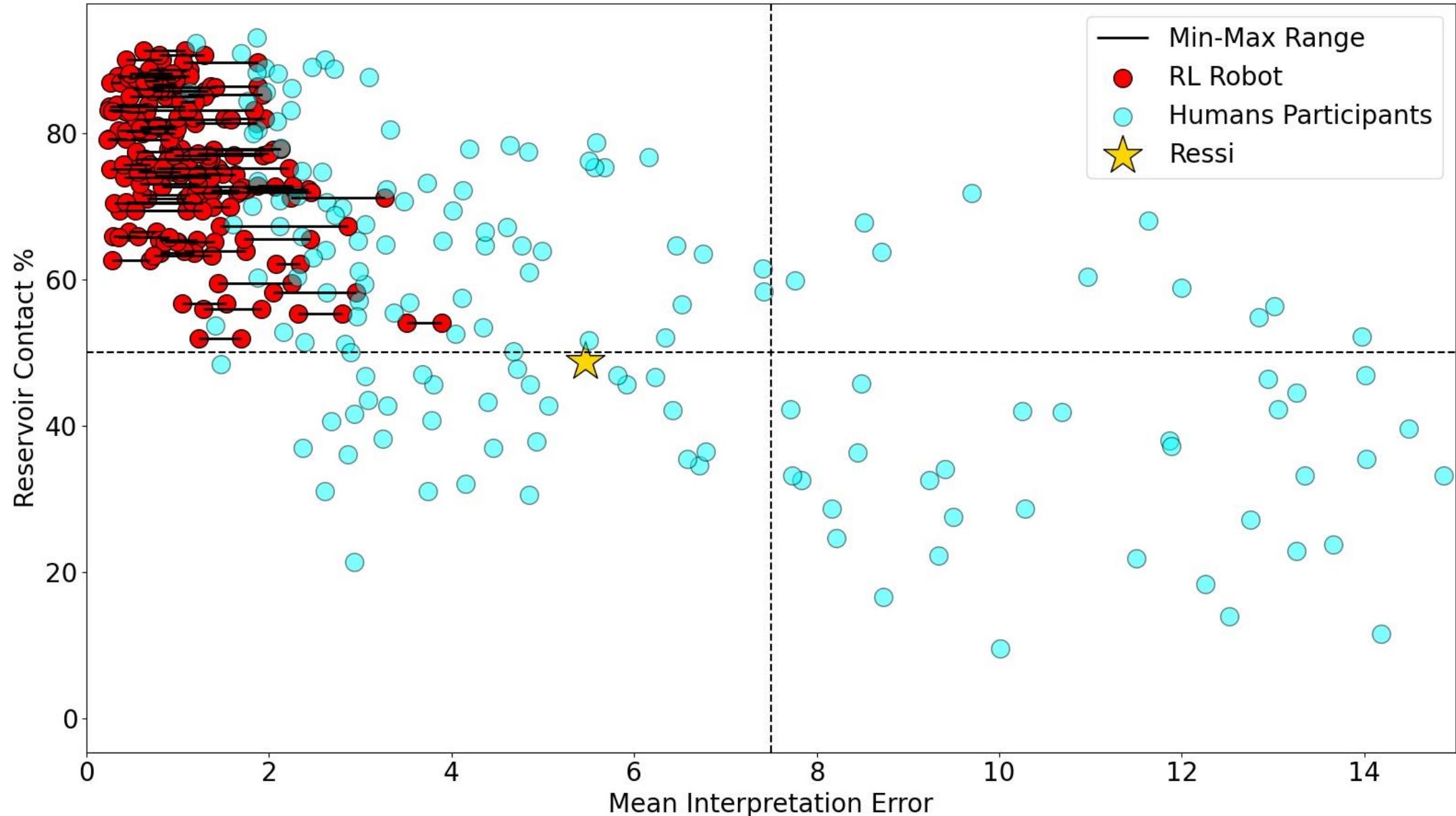
*(humans do not)*

# 3 Trajectories Comparison



1st percentile fails at all sections  
(first fault, incline, second fault)  
due to PF misinterpretations.

99th percentile manages to  
steer inside the layer except for  
the first fault



# Conclusions

- Pluralistic robot
  - **can outperform geosteering experts (with some cheating)**
  - **does outperform them most of the time**
- In low-data geosteering contexts **luck influences robots** as well as humans in terms of decision outcomes
- Ongoing work:
  - Make the robot work in the actual World Cup environment using API



# Lecture 3.2:

## Direct Multi-modal inversion with machine learning



# Direct Multi-modal inversion with machine learning for geosteering



Our MDN paper 2022

“Direct multi-modal inversion  
of geophysical logs using deep learning”

S Alyaev, AH Elsheikh

[Earth and Space Science, 2022](#)



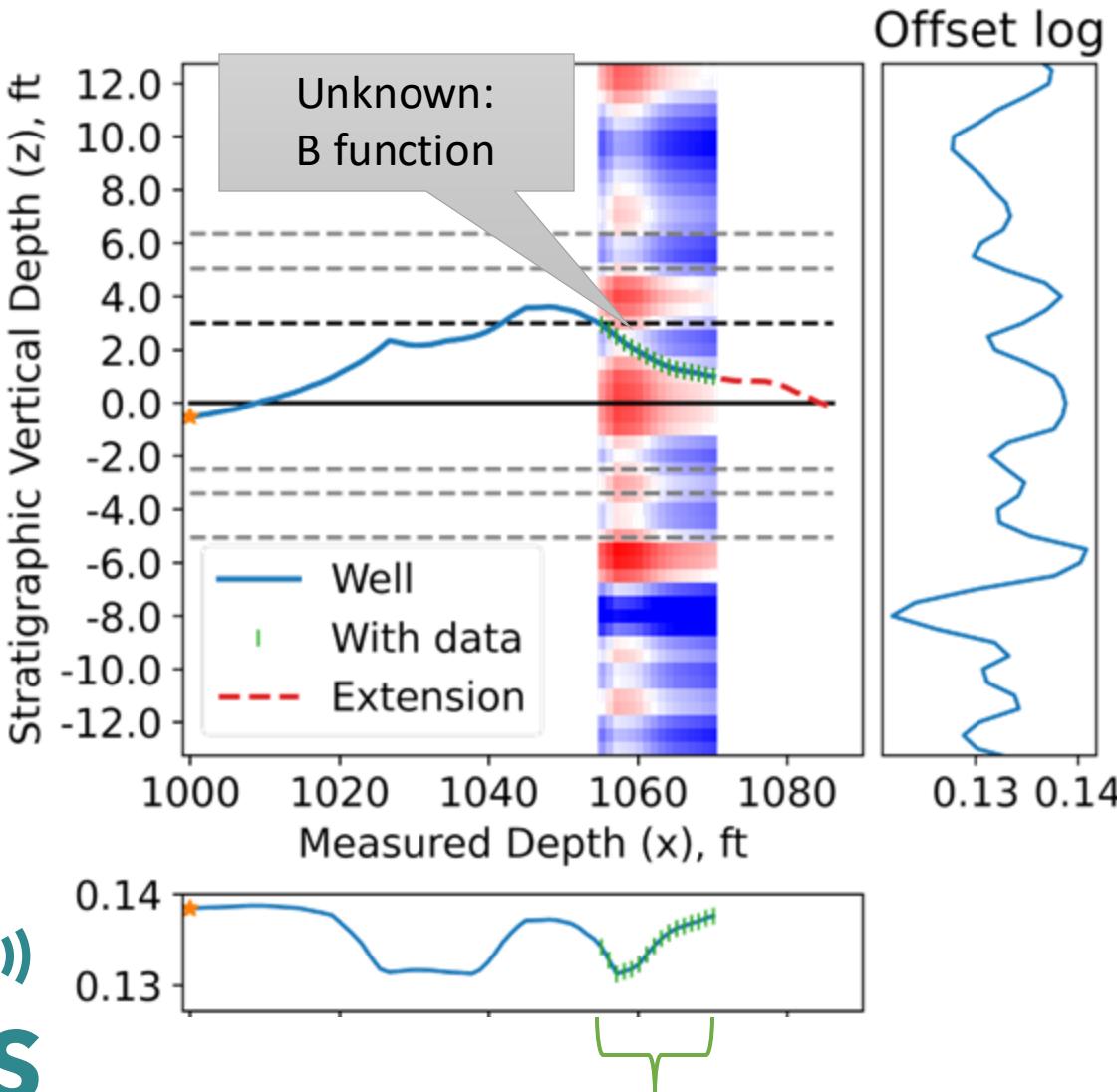
Our sequencial paper

SPWLA-2022-0112

“Sequential Multi-Realization...”

S Alyaev; A Ambrus; N Jahani; AH Elsheikh

# Inputs and Outputs for Direct Multi-modal DNN



Find the well trajectory **B function**  
relative geology

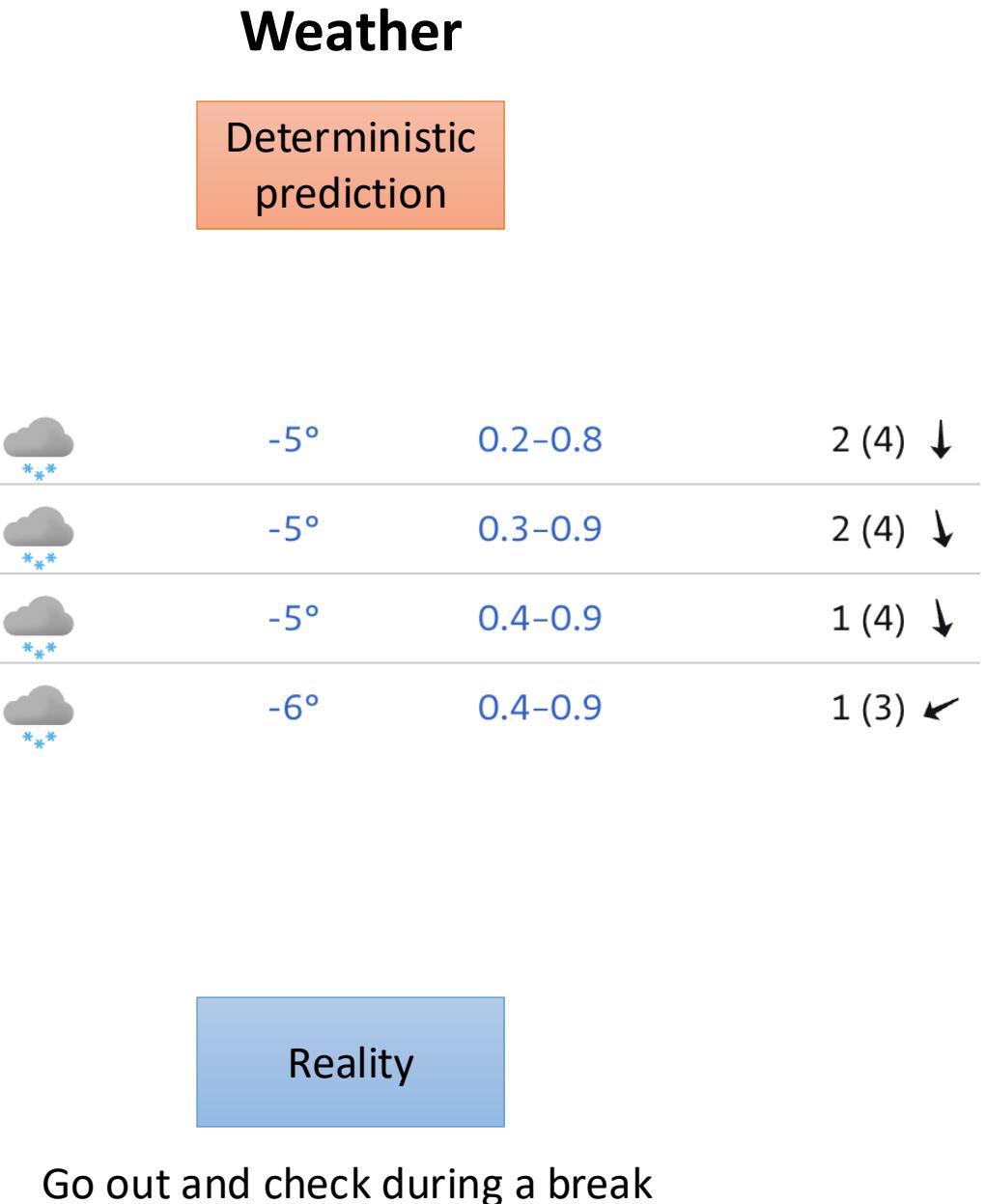
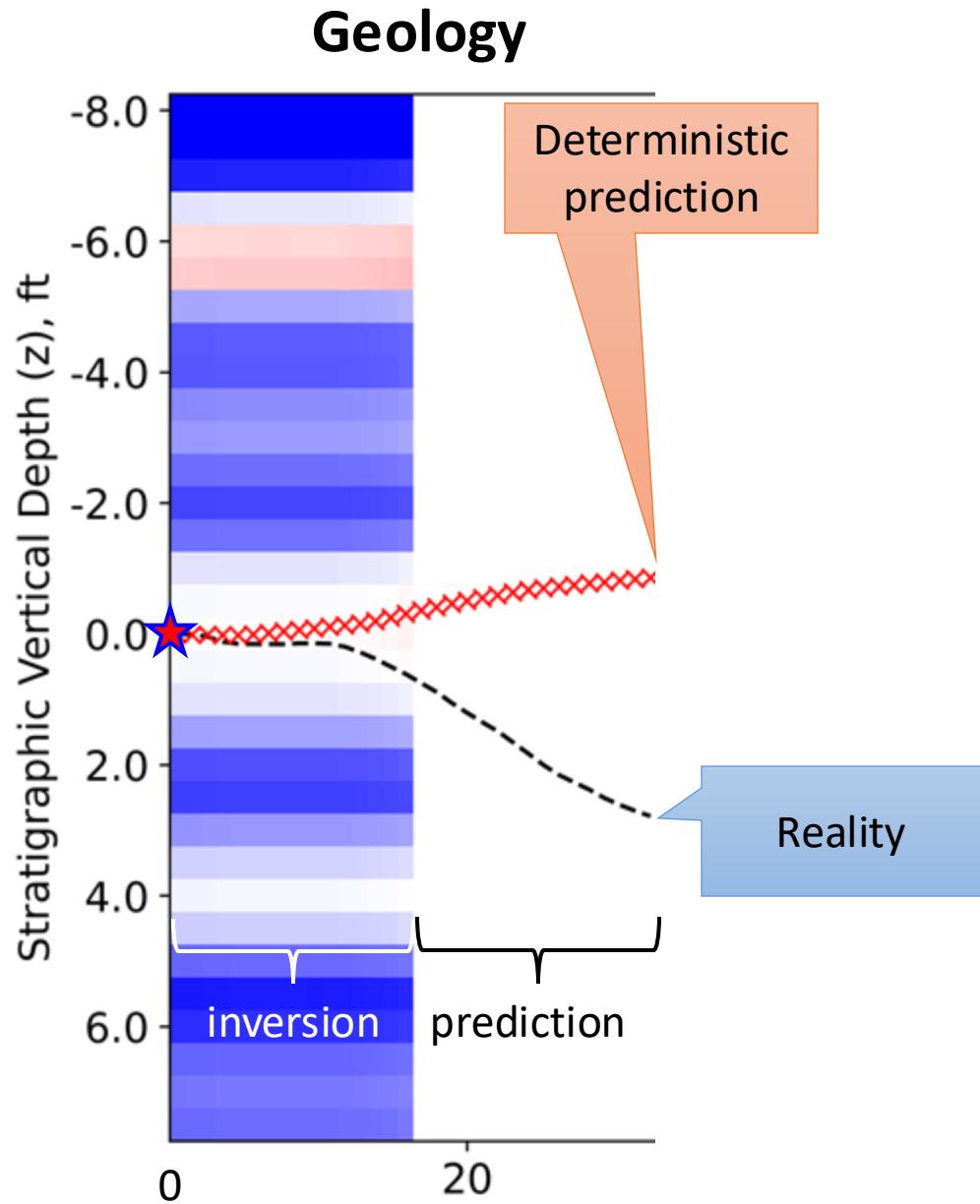
## Outputs of the Mixed Density Network

- $N$  likely B functions
  - Along data: INVERSION
  - Ahead of data: PREDICTION
- $N$  probability values

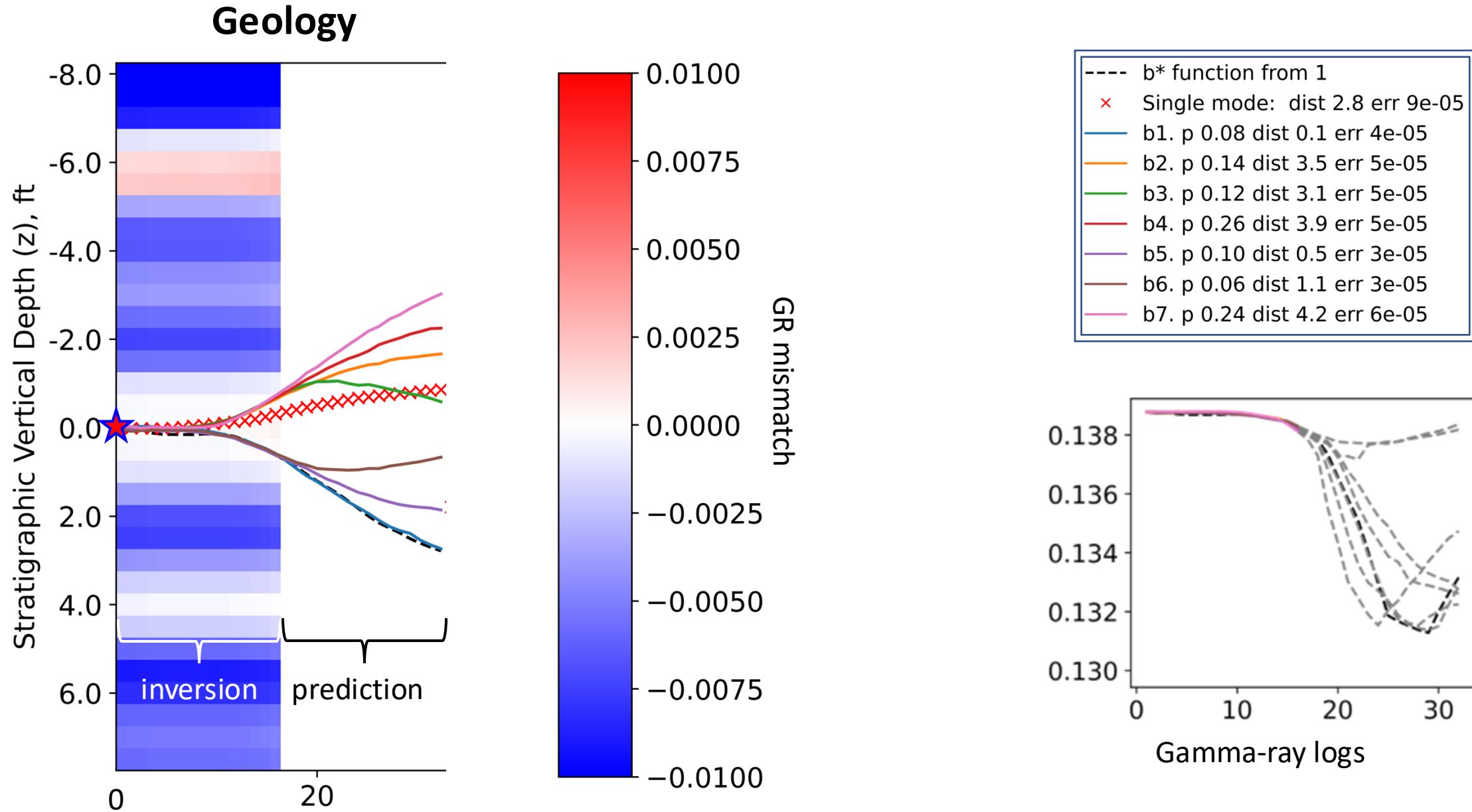
Inputs  
Offset well log  
Current well log

→ Heatmap  
image

# Examples of deterministic prediction

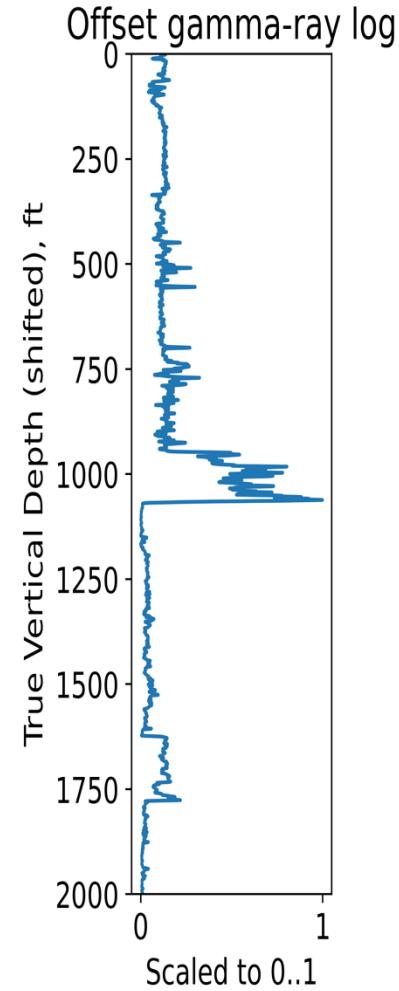
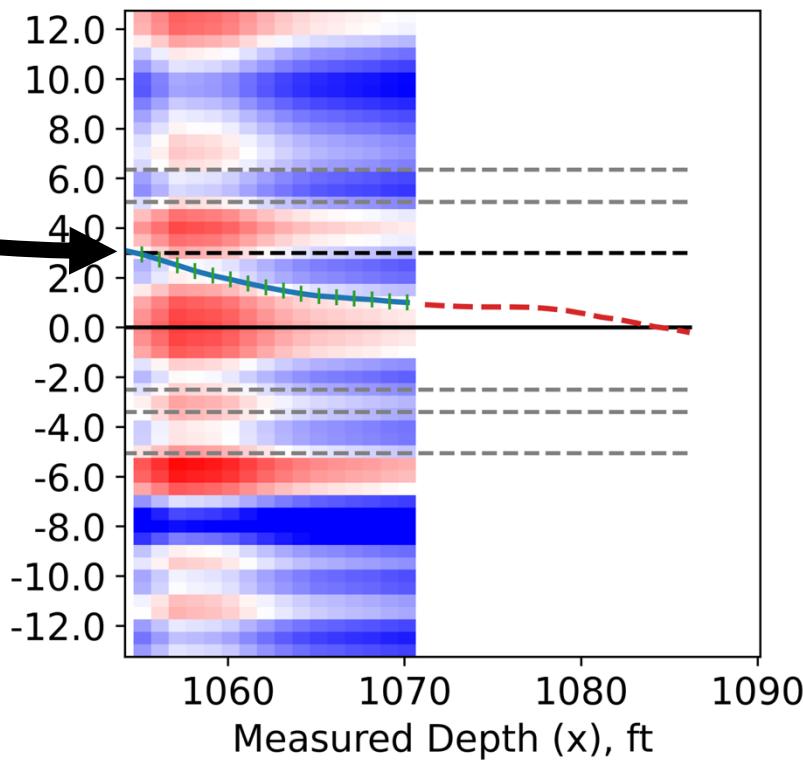
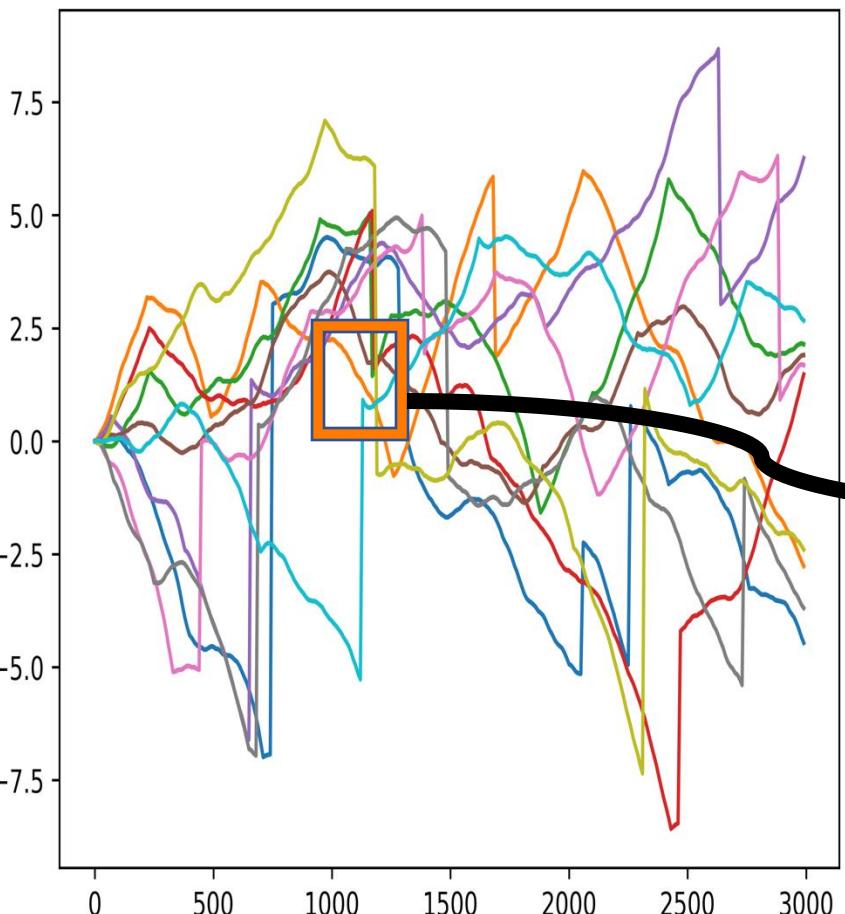


# Seven-mode inversion of a segment with MDN



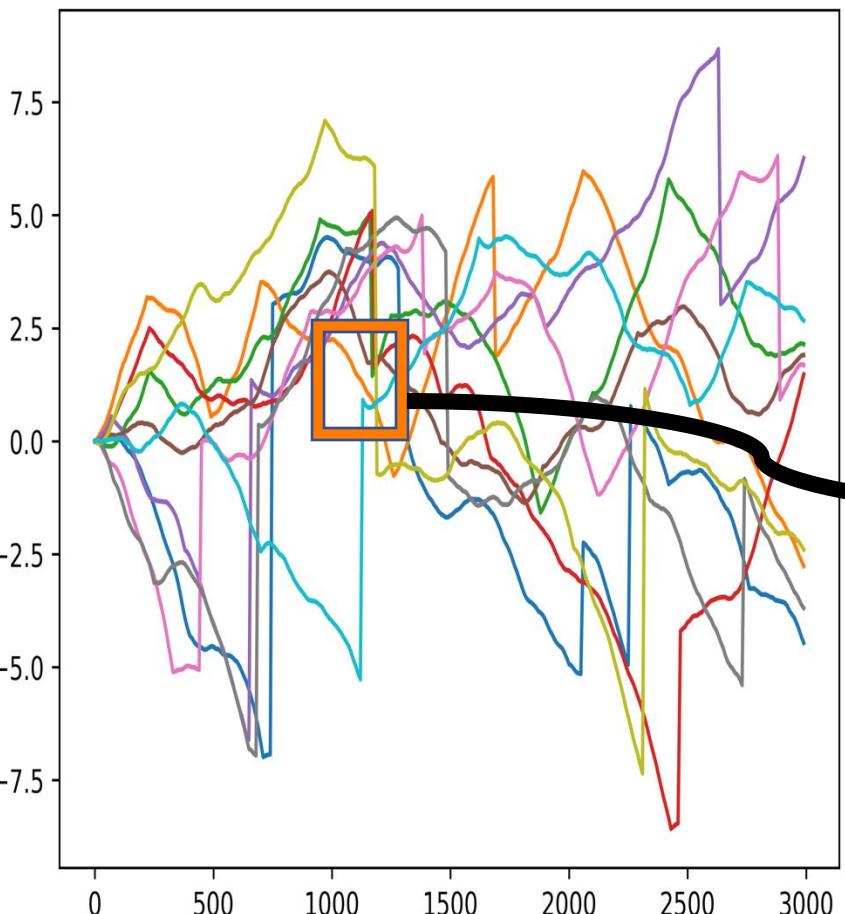
# How did the model learn? Training data

Generated stratigraphic curves

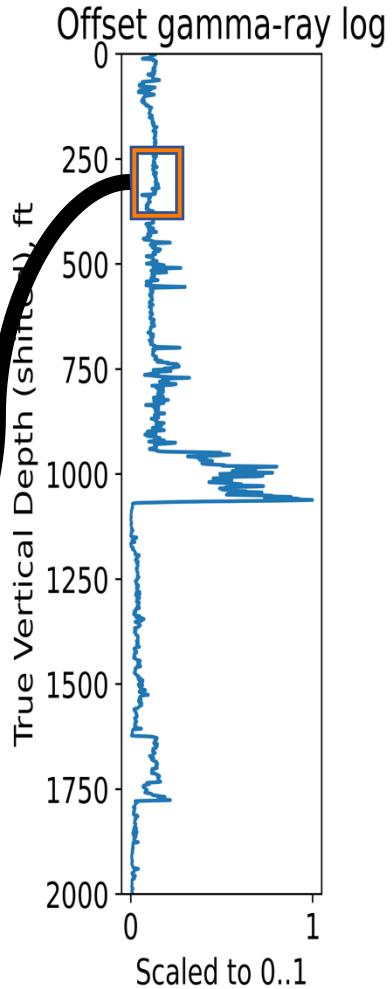
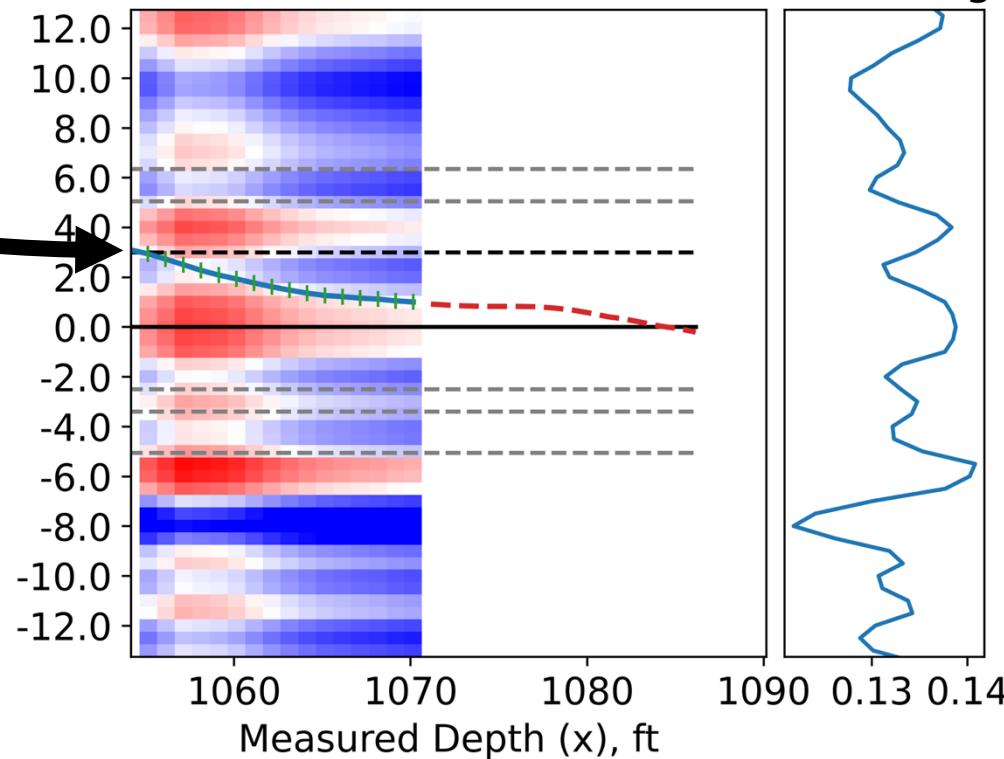


# How did the model learn? Training data

Generated stratigraphic curves

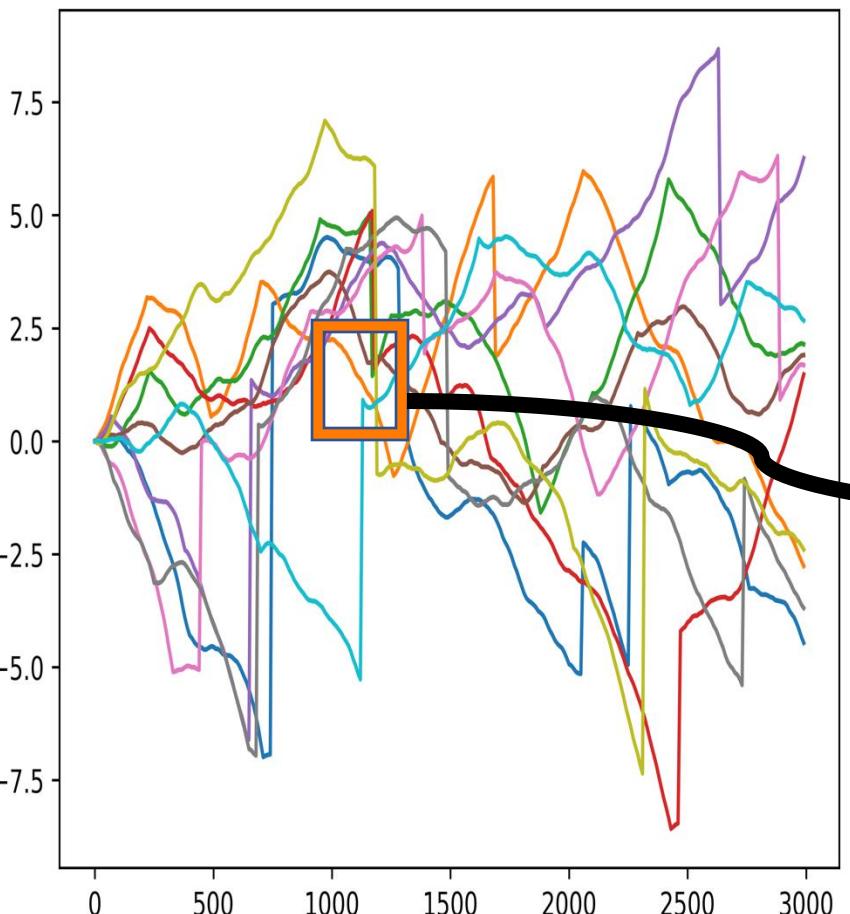


Offset log

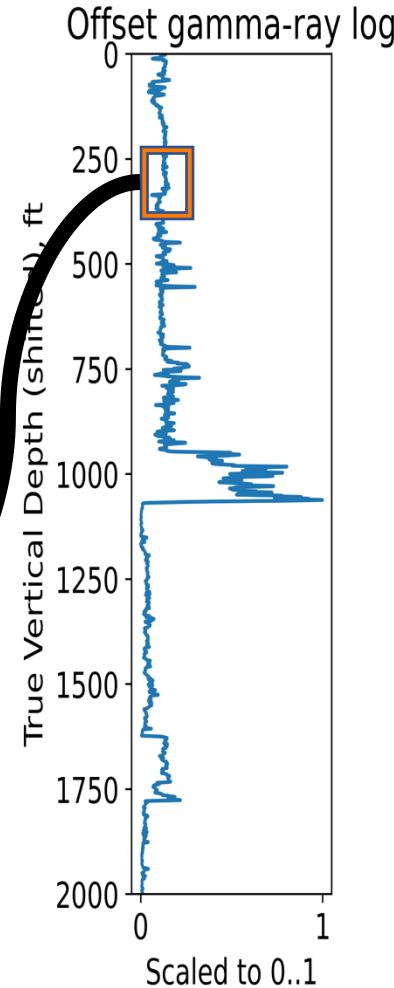
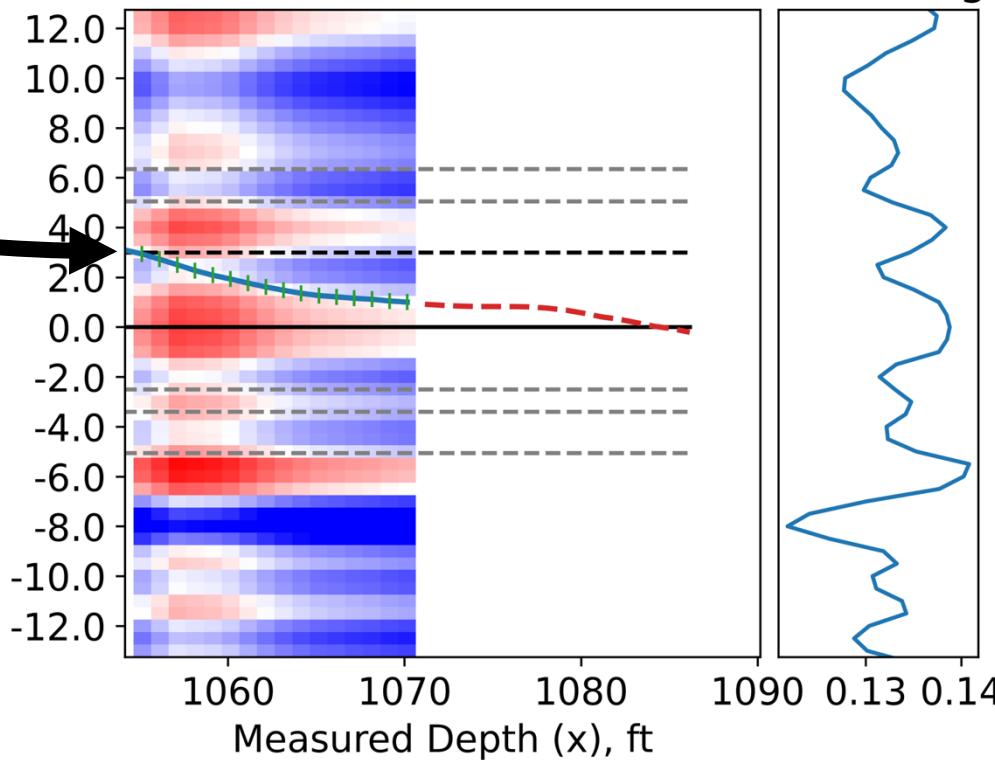


# How did the model learn? Training data

Generated stratigraphic curves

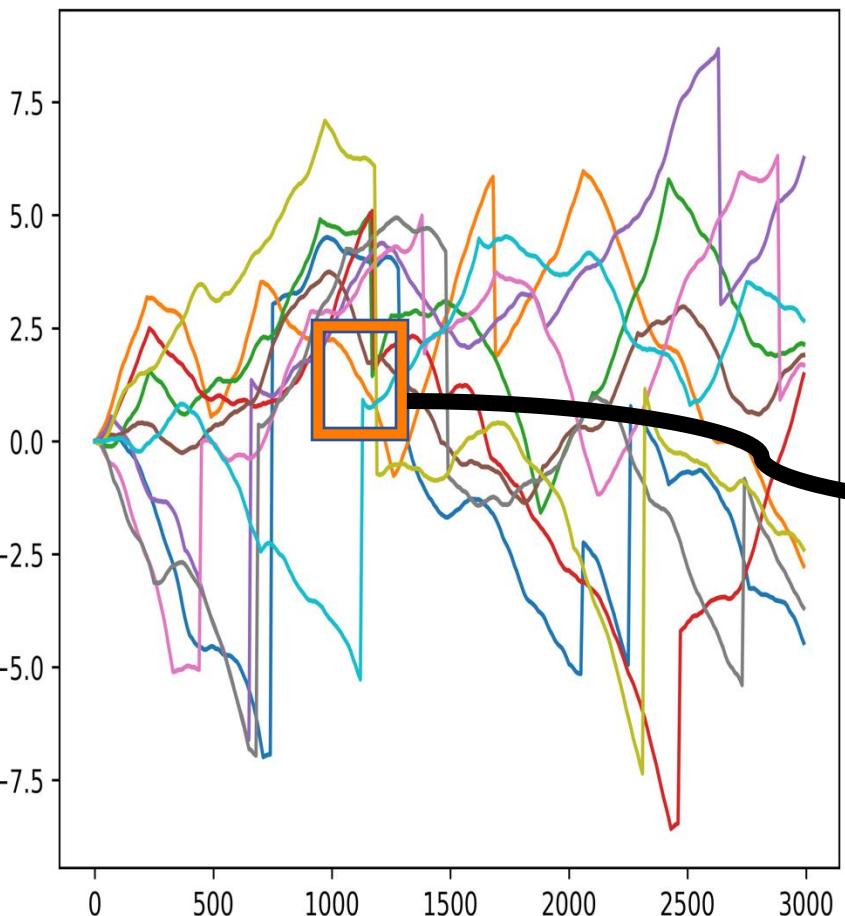


Training data:  
28M log-log-curve samples

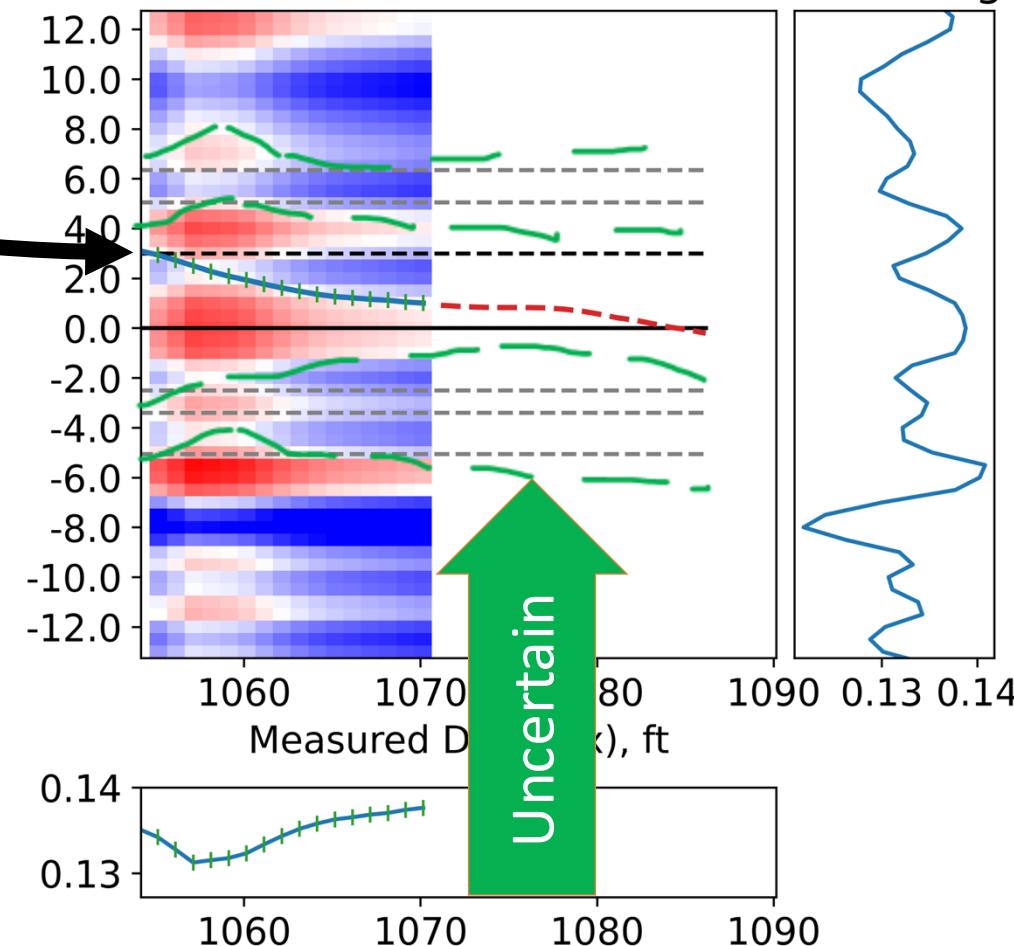


# How did the model learn? Training data

Generated stratigraphic curves



Training data:  
28M log-log-curve samples



Deterministic  
lateral log

# Training Multiple-Trajectory-Prediction loss

$$loss = \alpha_{probability} I_{probability} + I_{prediction}$$

$$I_{probability} = -\log \left( \frac{\exp(x_{m^*})}{\sum_m \exp(x_m)} \right)$$
$$I_{prediction} = \frac{\|b^* - b^{m^*}\|}{l^+}$$

Probability misfit and Prediction quality of the “best mode”  
**minimized simultaneously**

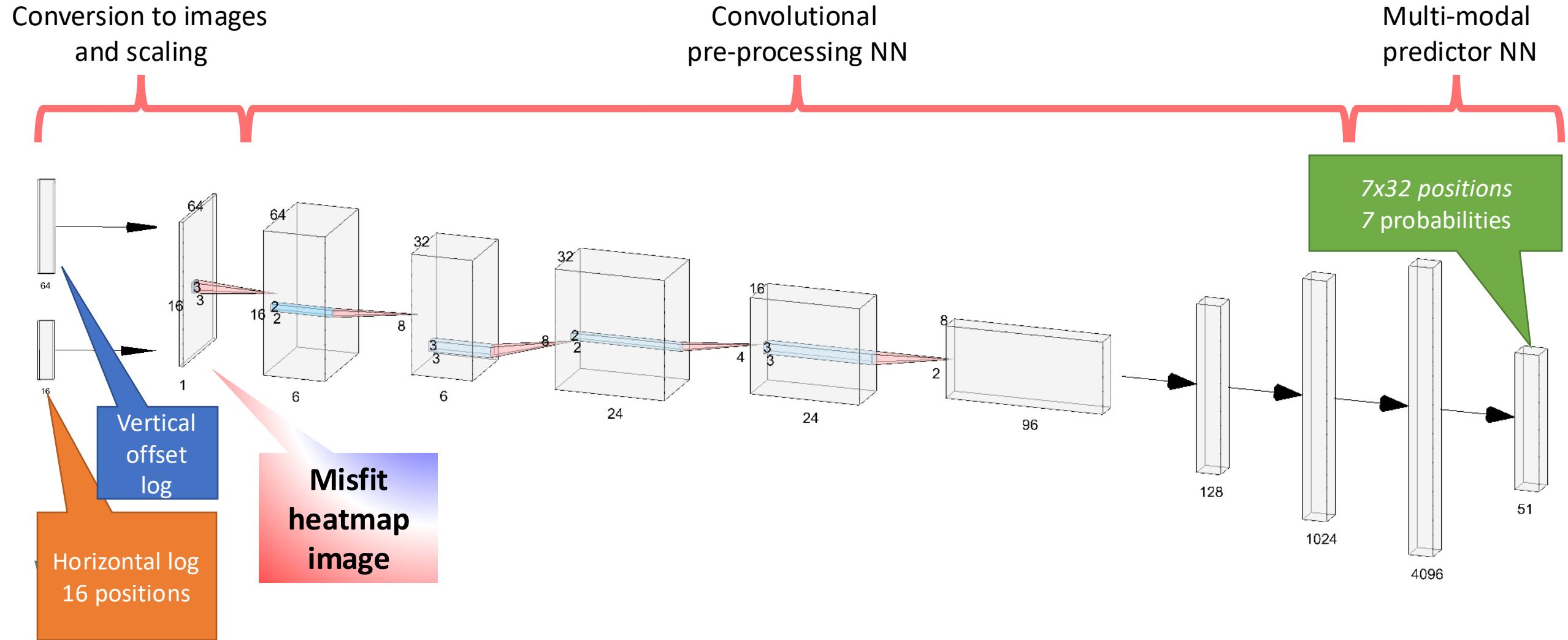
Best mode:  $m^* = \arg \min_{1 \leq m \leq m_+} \|b^* - b^m\|$

# Training Multiple-Trajectory-Prediction loss

$$loss = \alpha_{probability} I_{probability} + I_{prediction}$$

**Note: No explicit fitting to measurements**

# CNN Mixture Density Network (MDN) Architecture

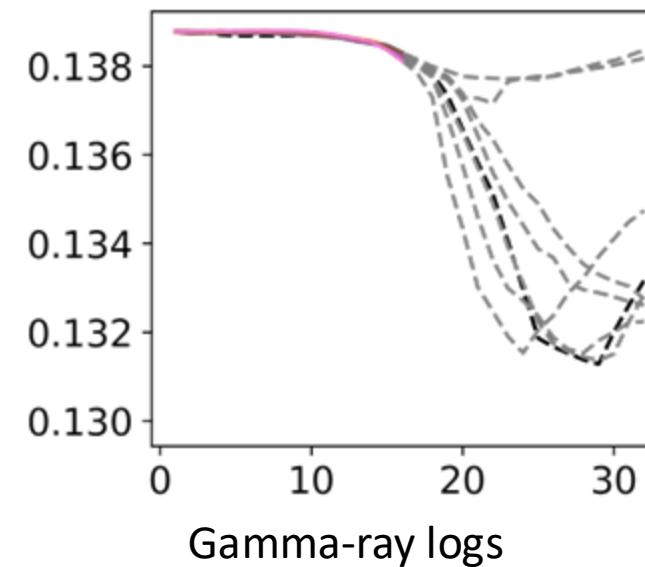
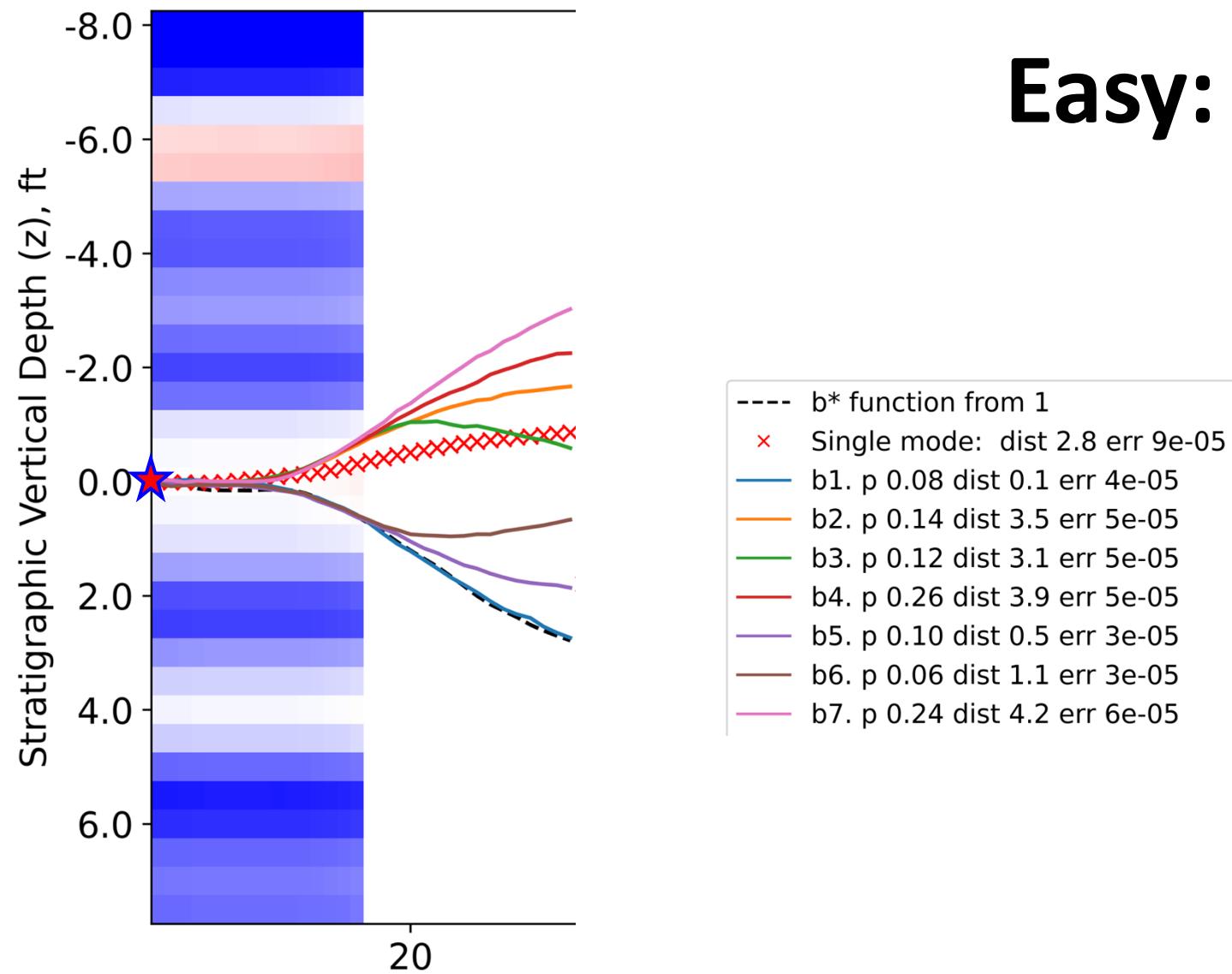


# Mixture Density Network (MDN)

- A neural network that tries to reconstruct distribution from the data
- The distribution is represented as a sum of kernels
  - (similar to particles),
  - each having its own parameters

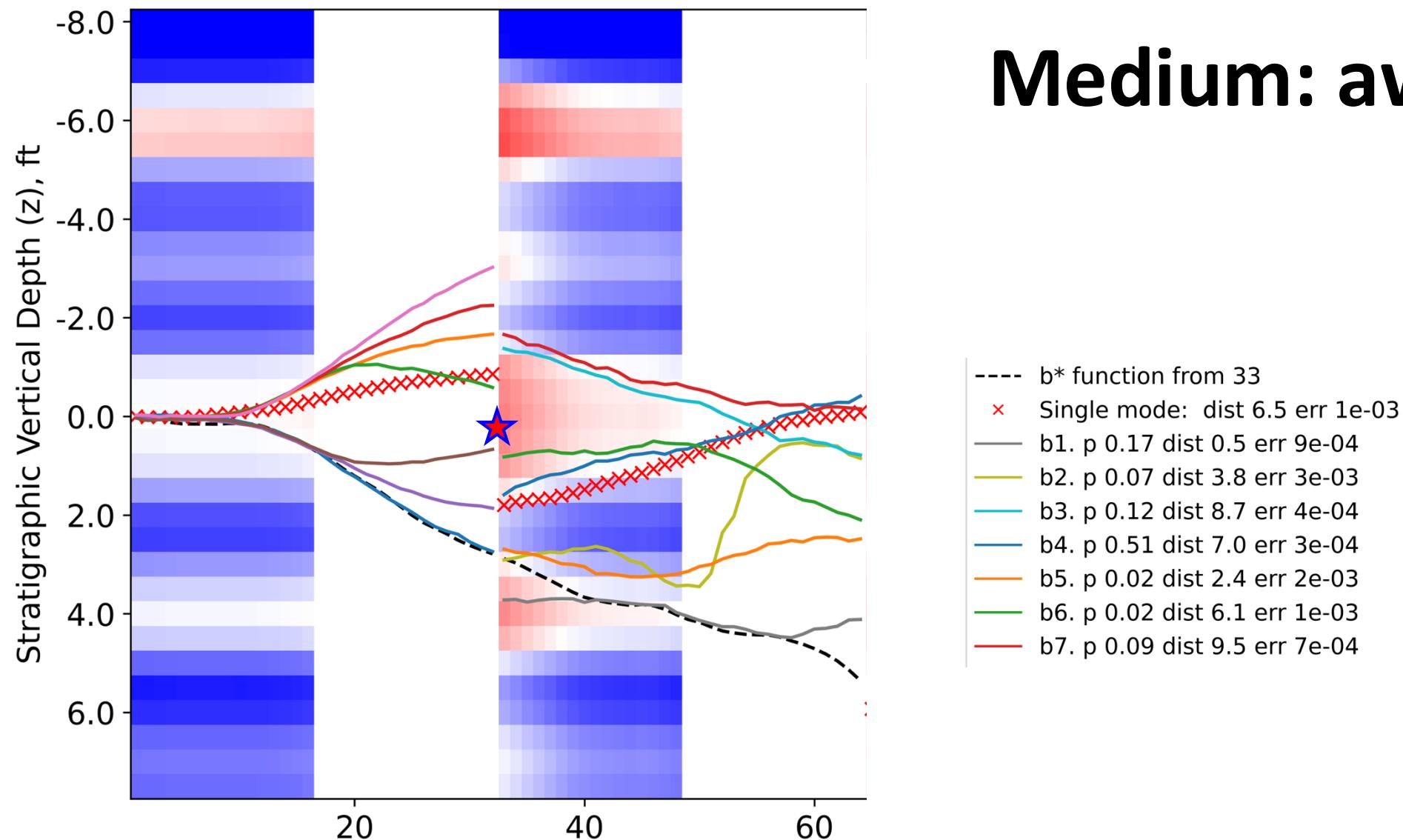
# The results

## Easy: prediction around 0



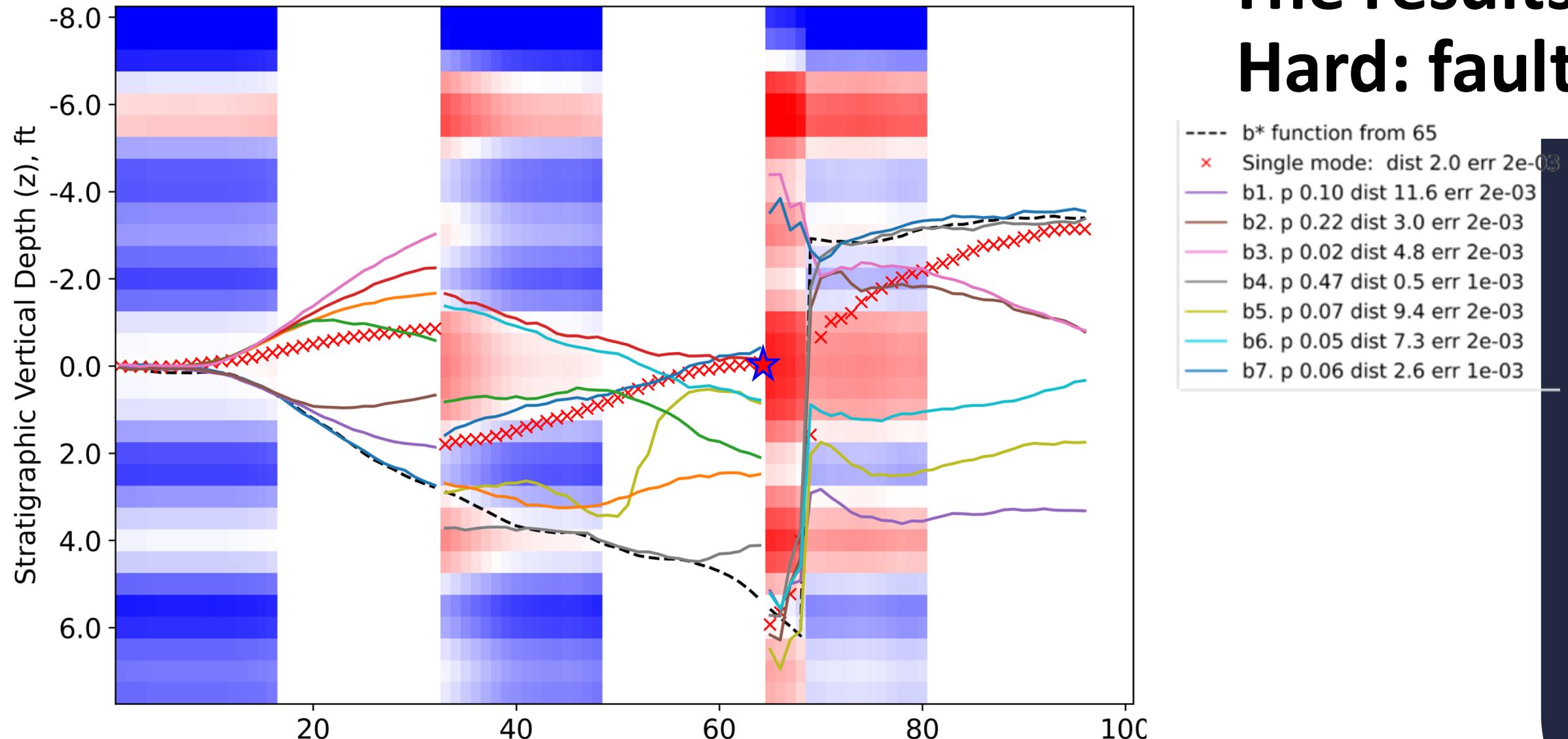
# The results

## Medium: away from 0



# The results

## Hard: fault



# To invert a full well...

## We need to apply MDN iteratively

- Needs to be robust outside training dataset
- Requires a heuristic algorithm for tracking previous inversions' end points and their probabilities

Challenge:

Possible curse of dimensionality:

- 1 point → 7 predictions → 49 prediction → 343 predictions
- Can loose computational efficiency

# Sequential predictor (aka filter)

## Inputs

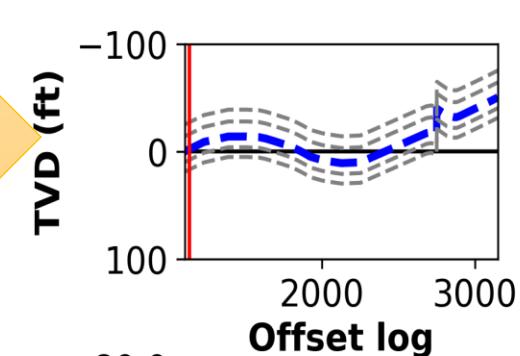
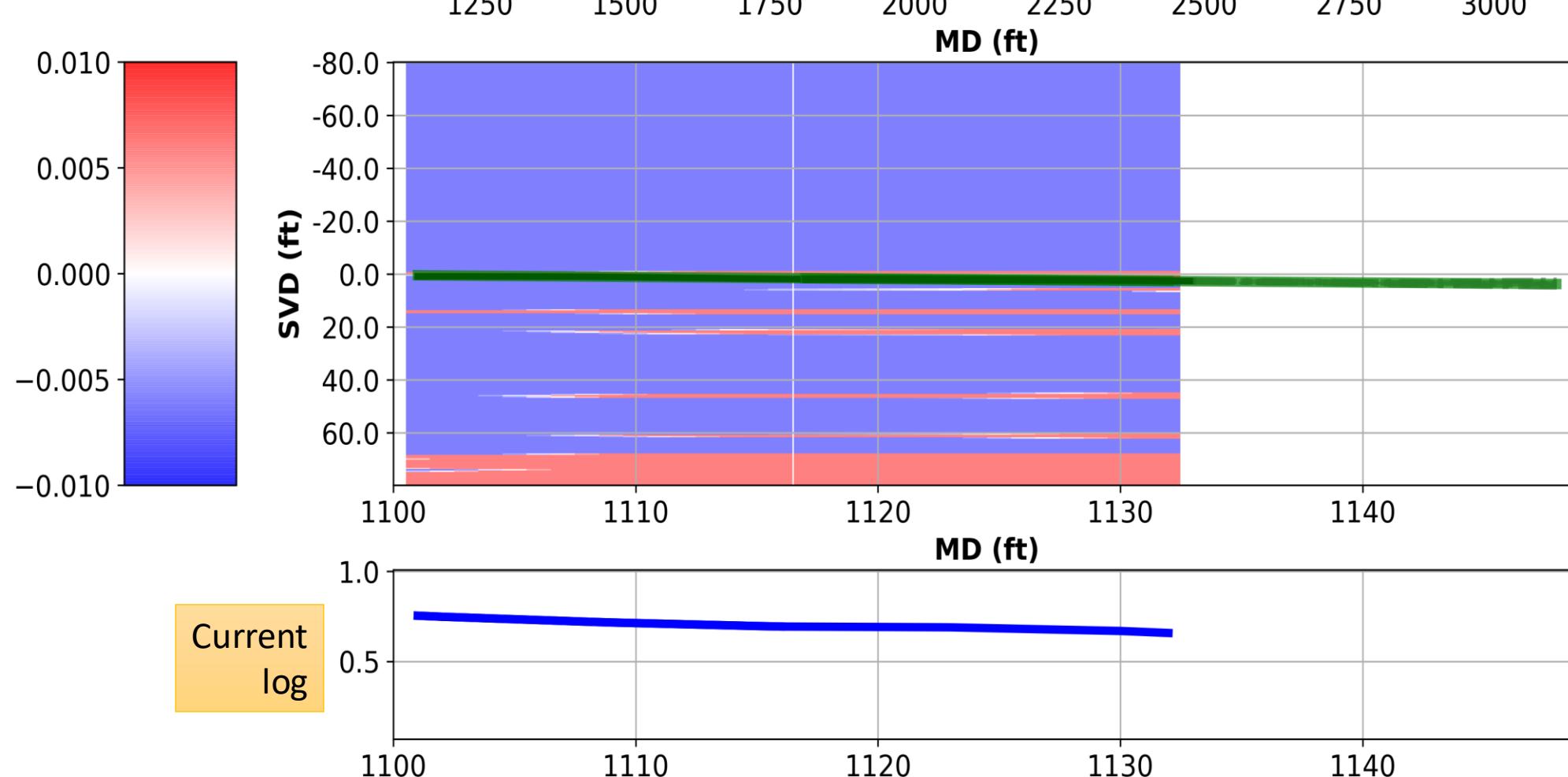
- Offset well log (**any size**)
- Horizontal well log
- Starting points and probabilities (**any number  $M$** )

## Outputs

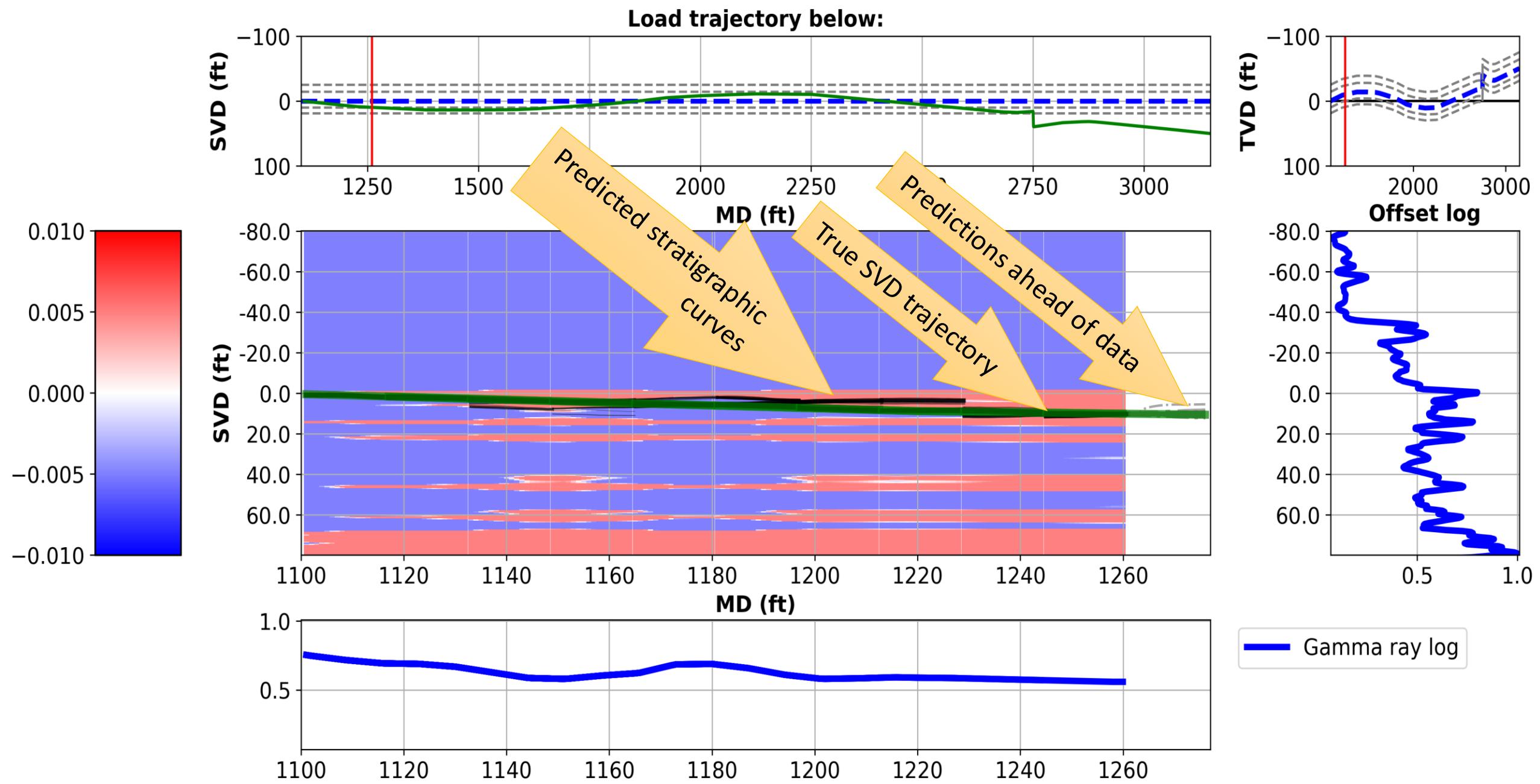
- $N^*M$  likely stratigraphic curves
  - Along well: INVERSION
  - Ahead of well: PREDICTION
- $N^*M$  probability values

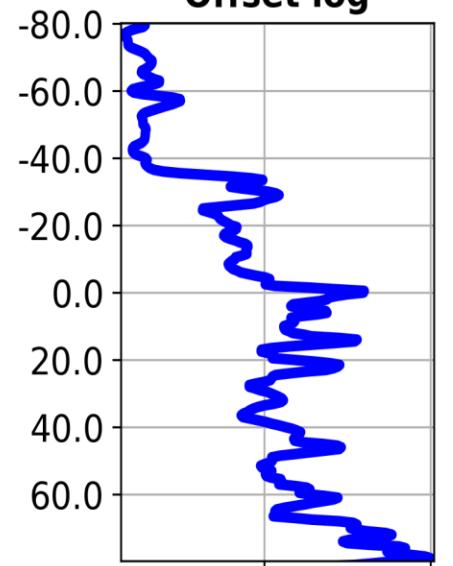
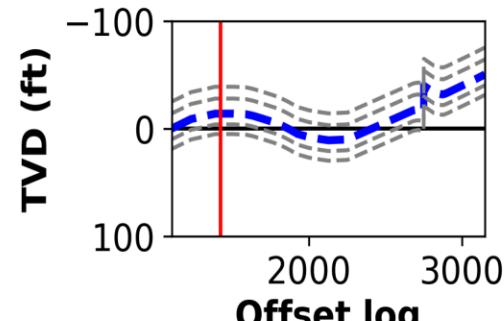
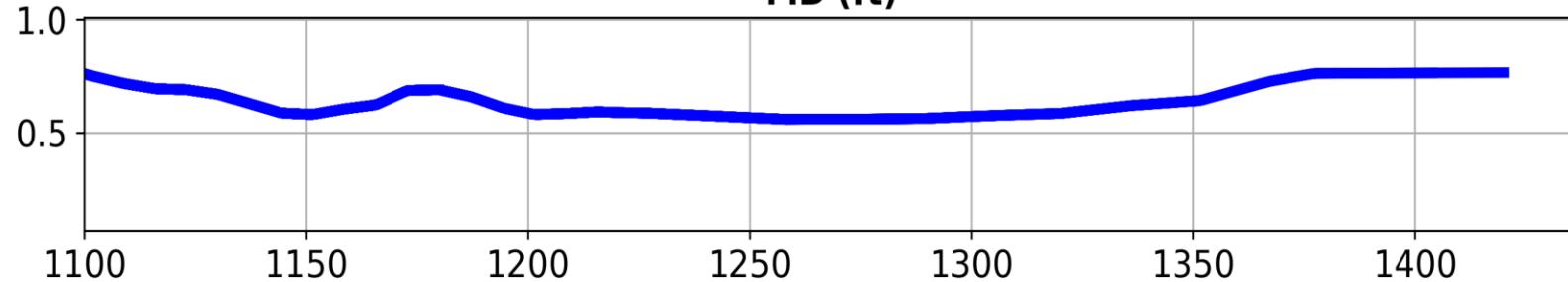
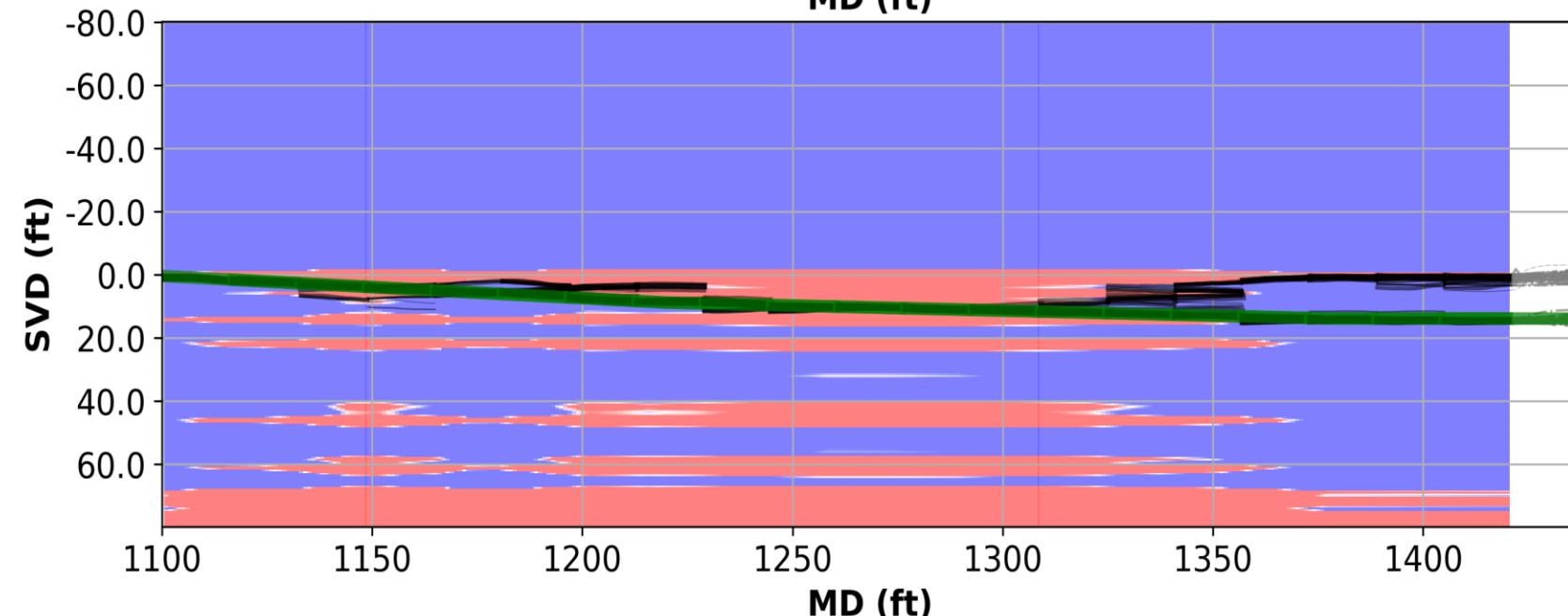
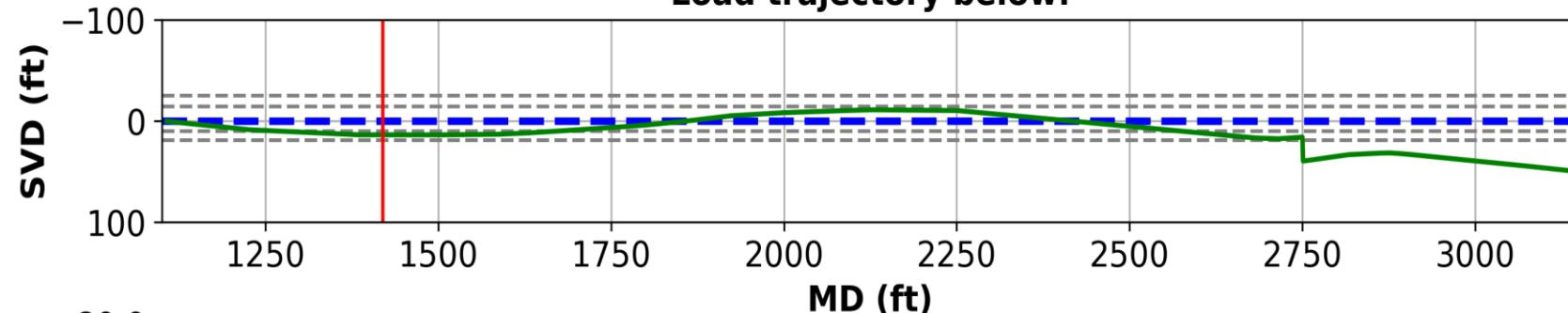
Geological ‘truth’ and logs from GWC 2020  
based on Middle Woodford formation in South Central Oklahoma Oil Province

Coordinates  
linked  
to stratigraphy

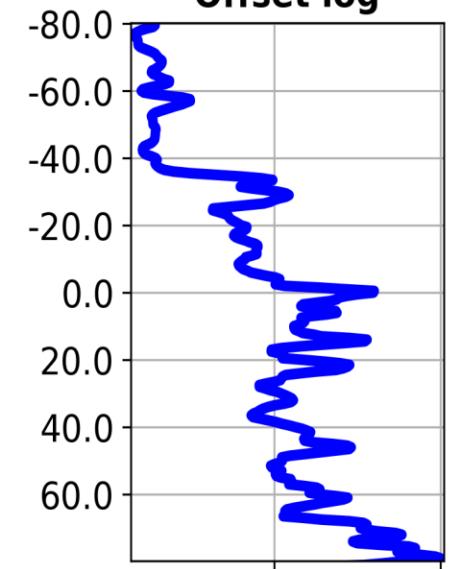
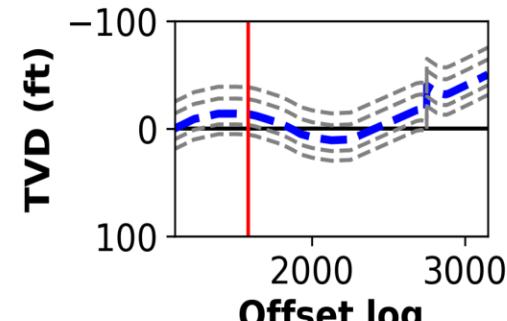
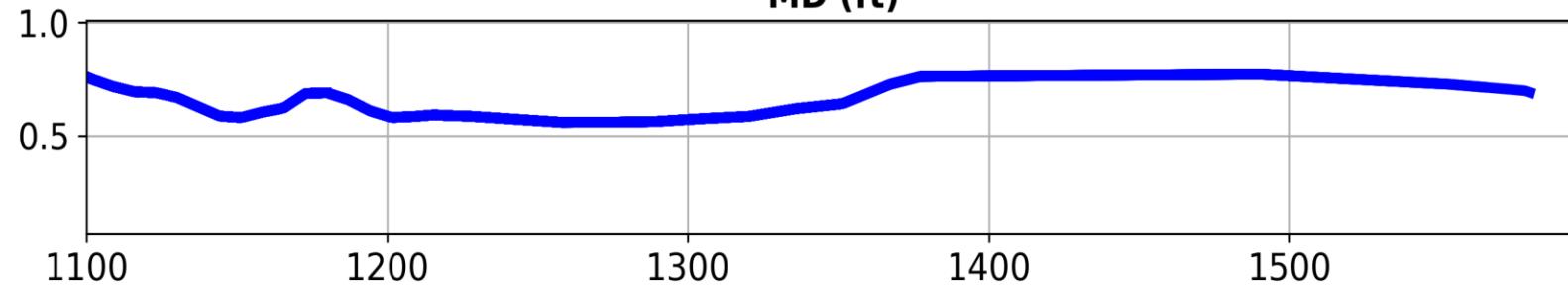
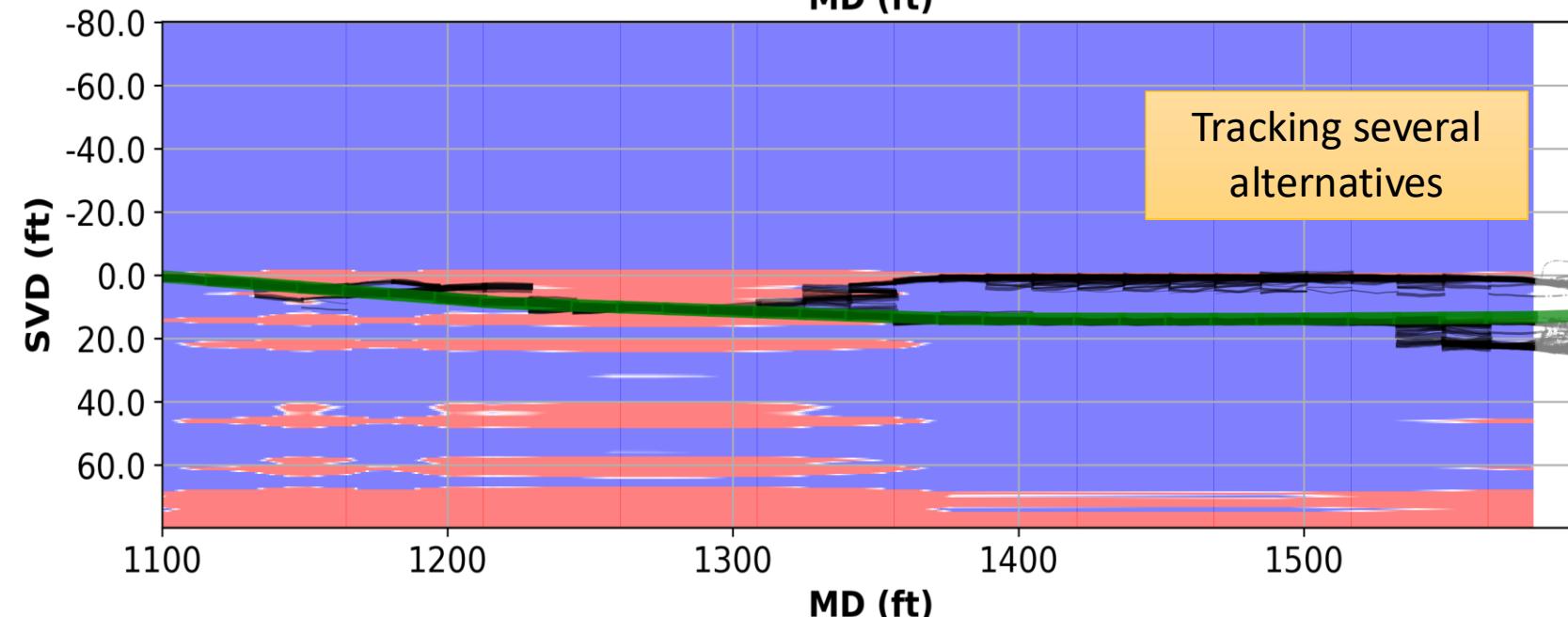
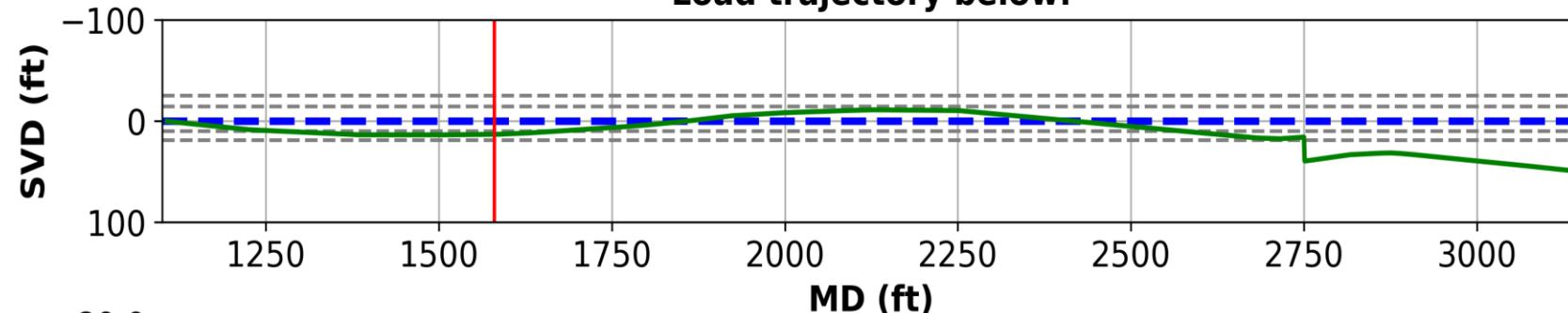


Offset  
well log

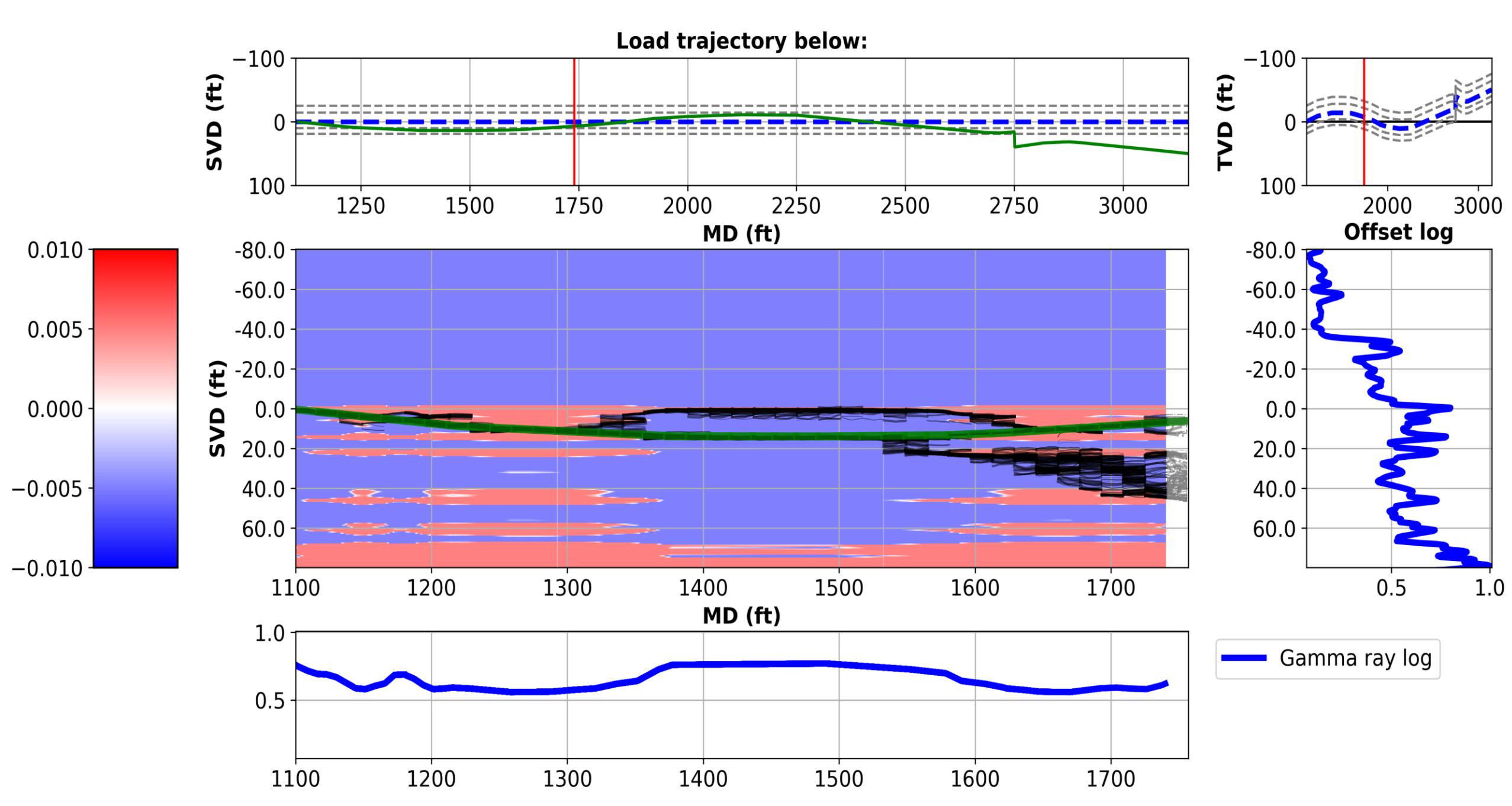


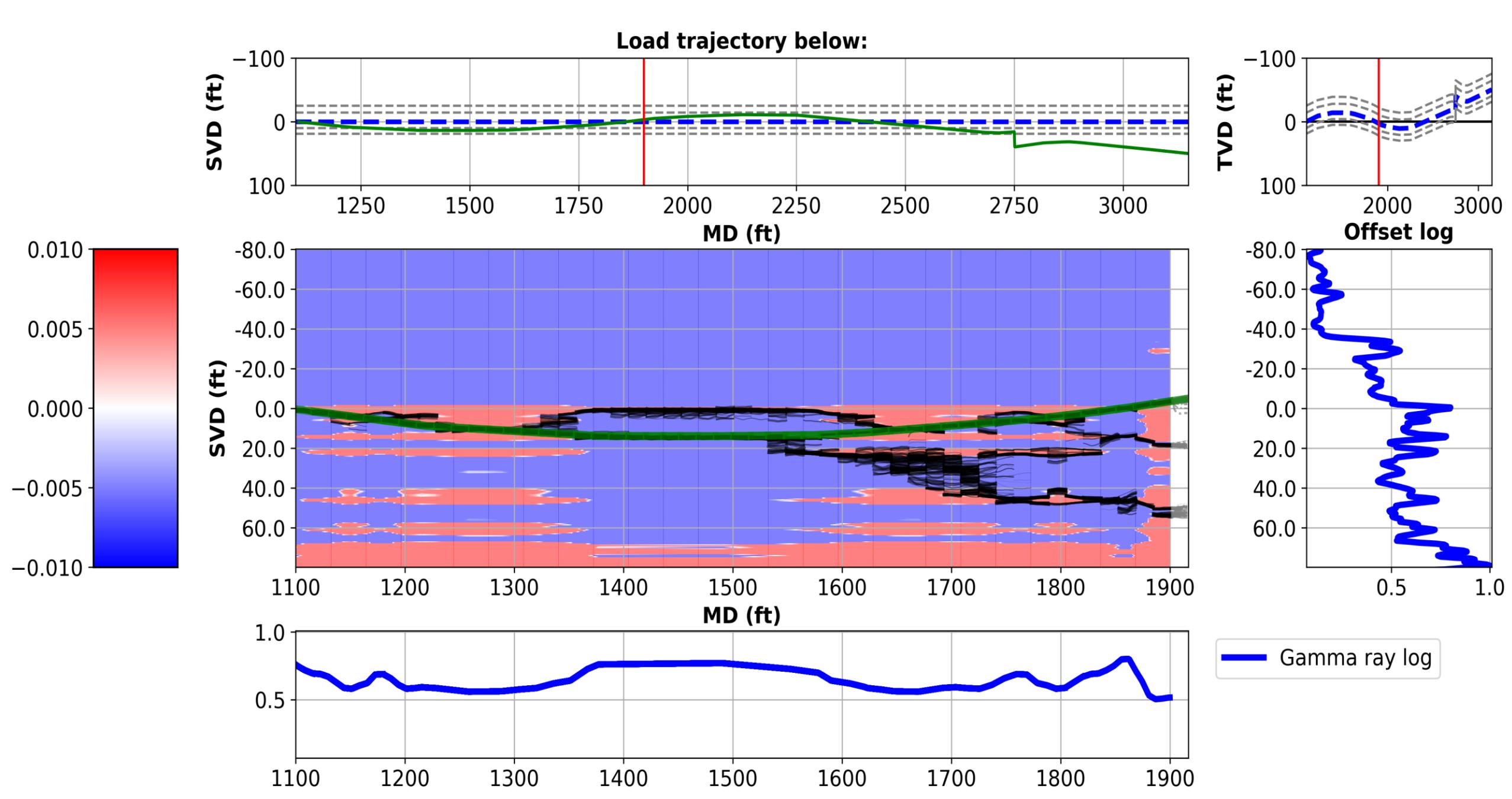


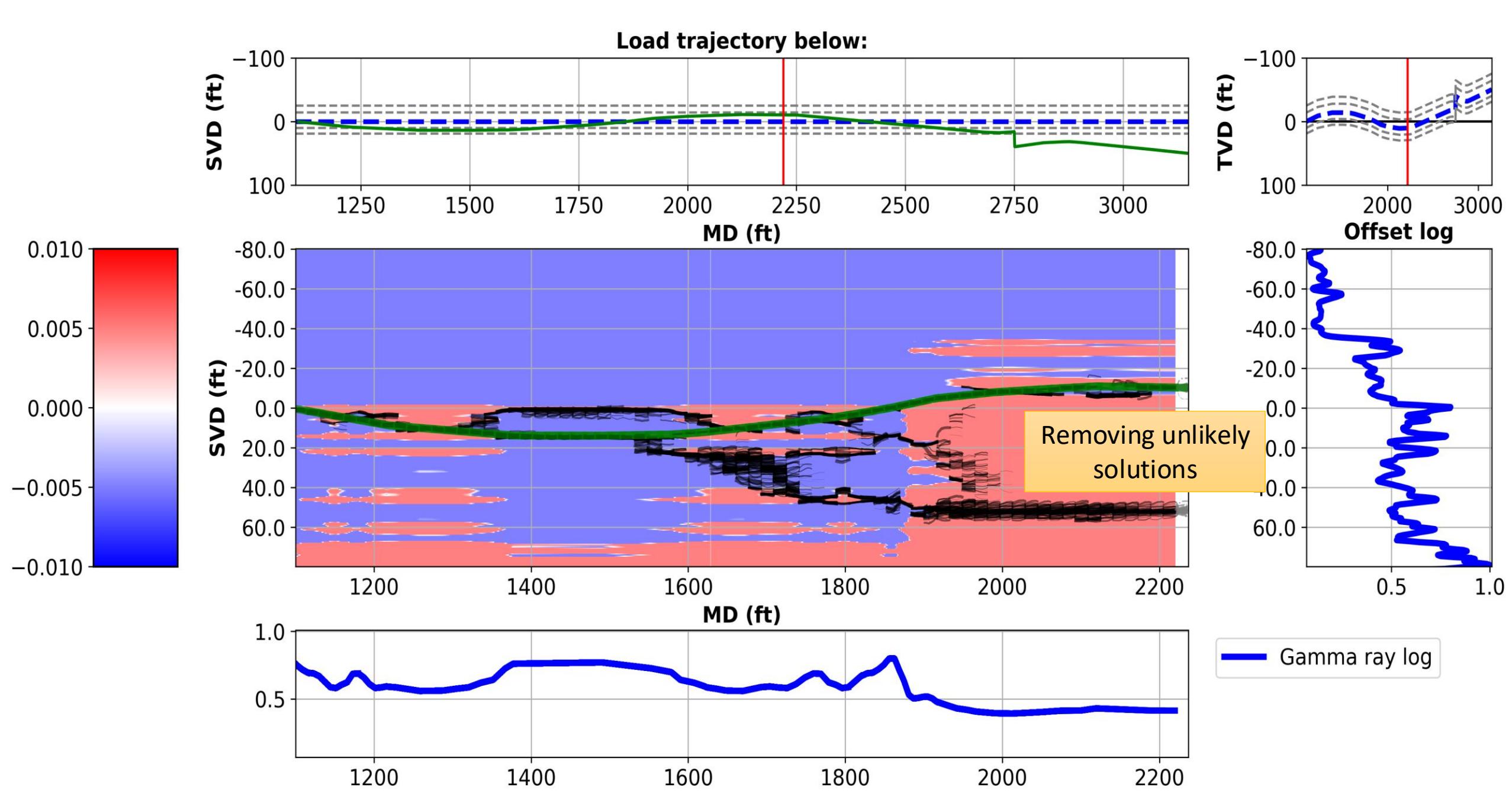
### — Gamma ray log

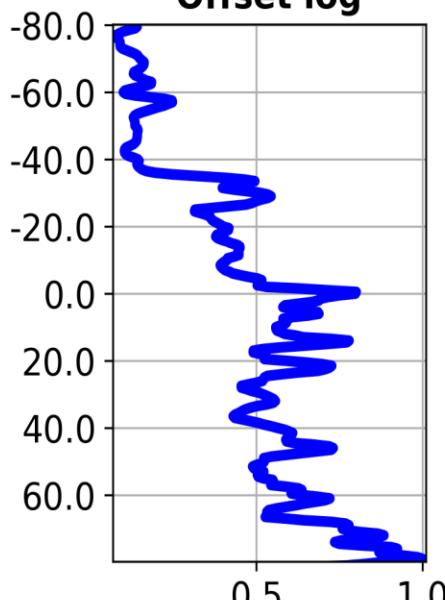
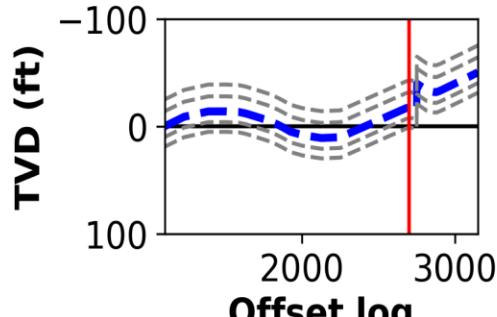
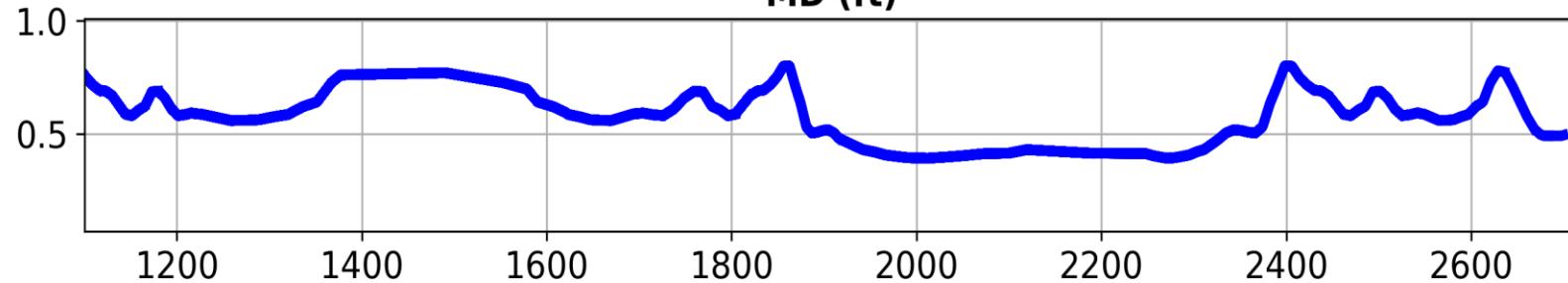
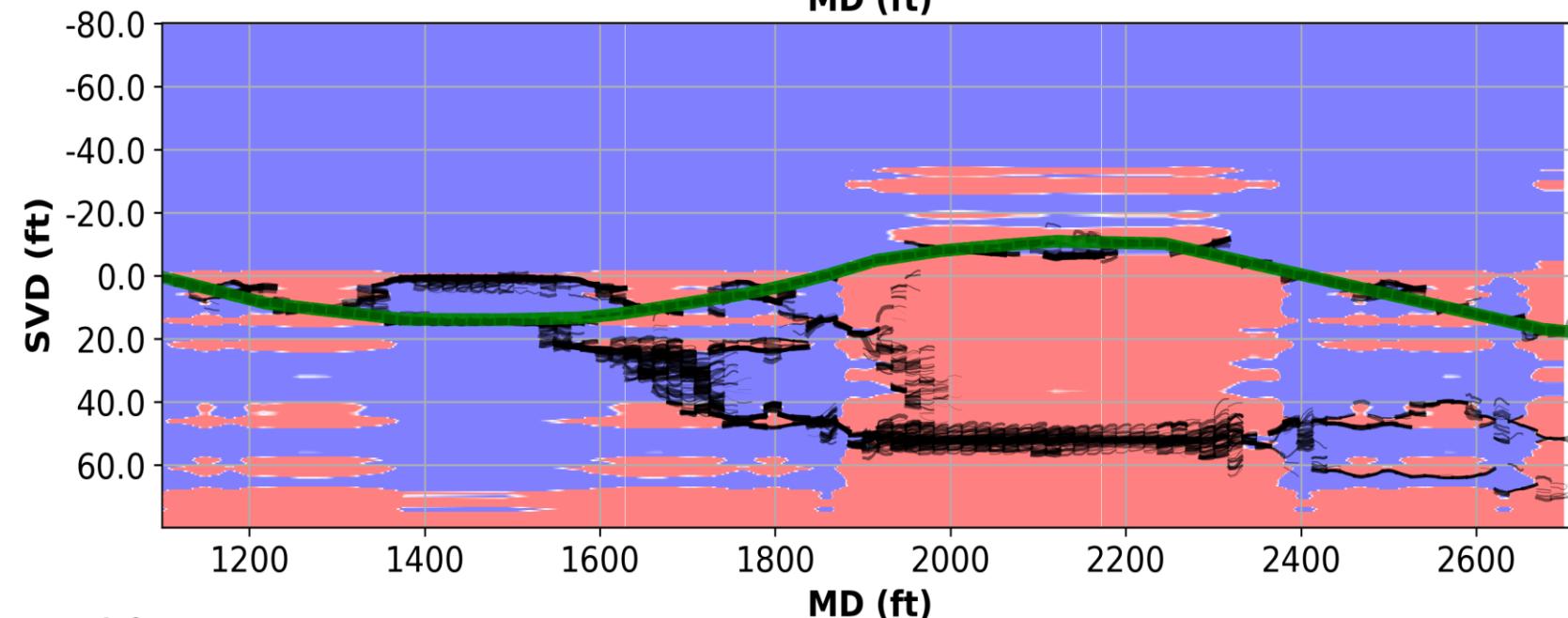
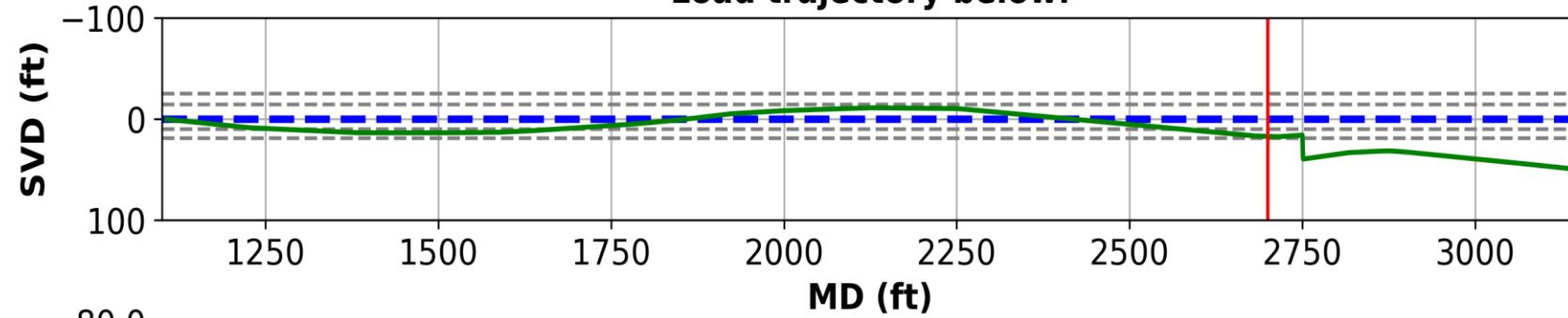


## Tracking several alternatives

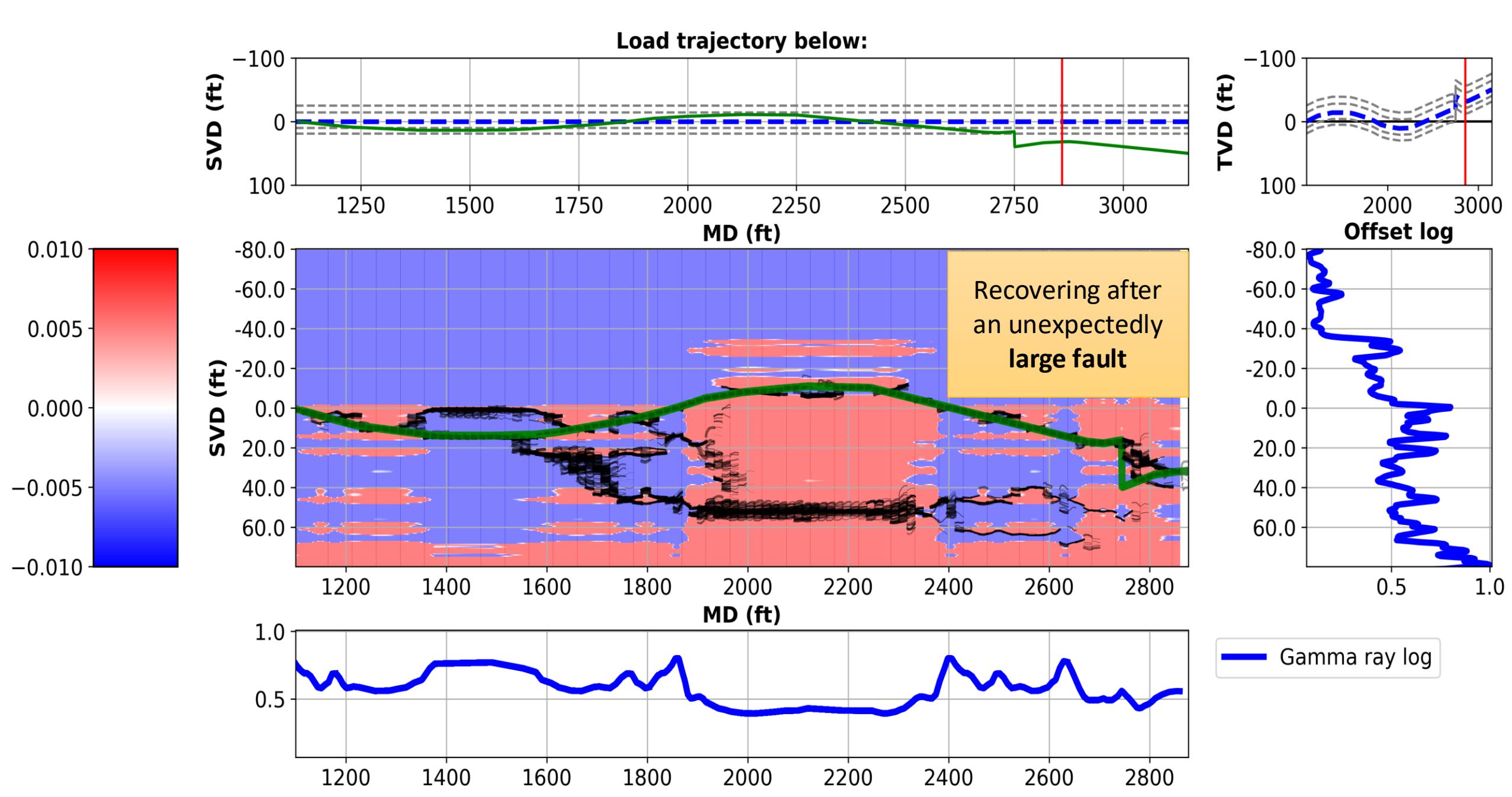


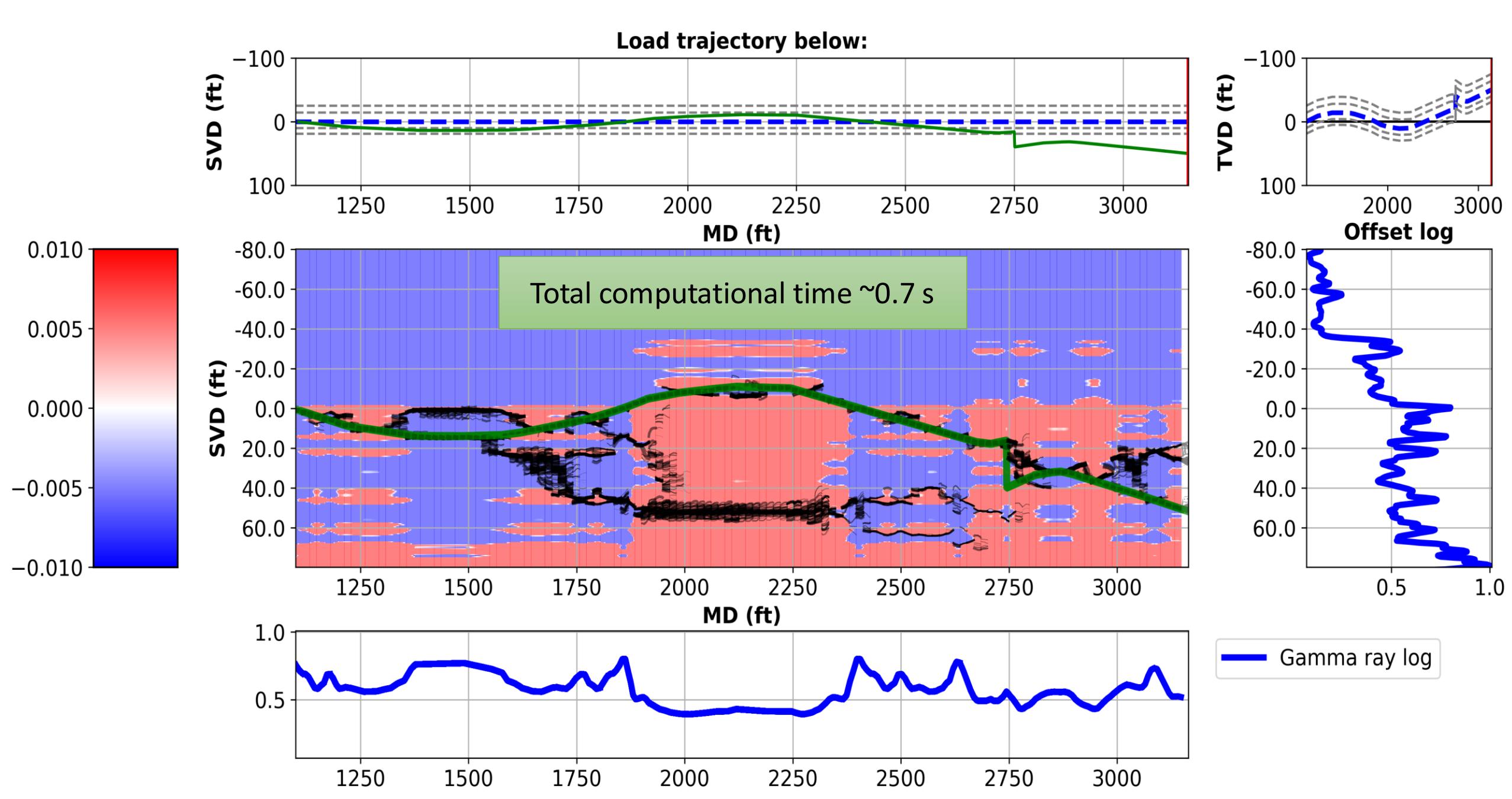






— Gamma ray log

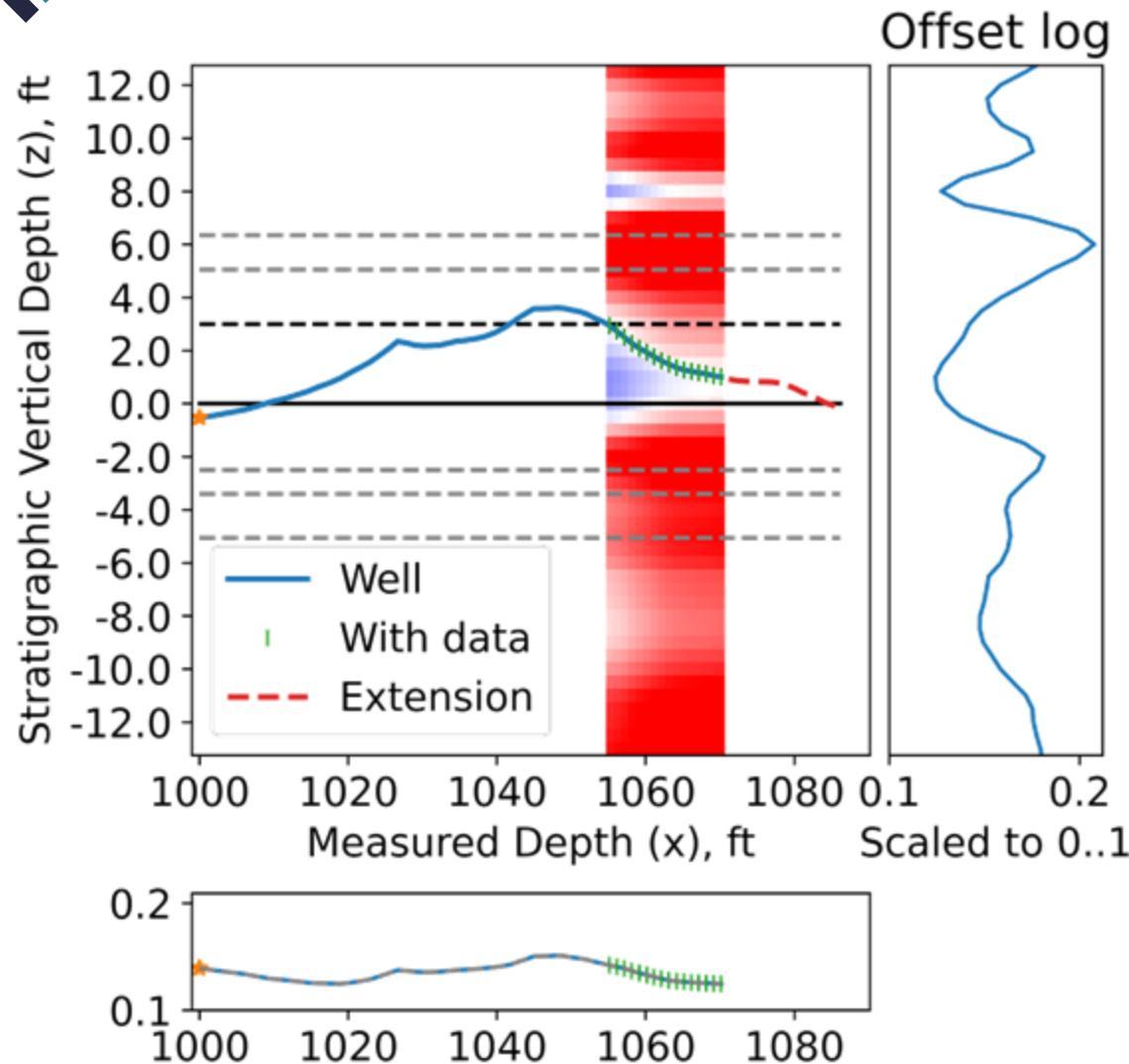




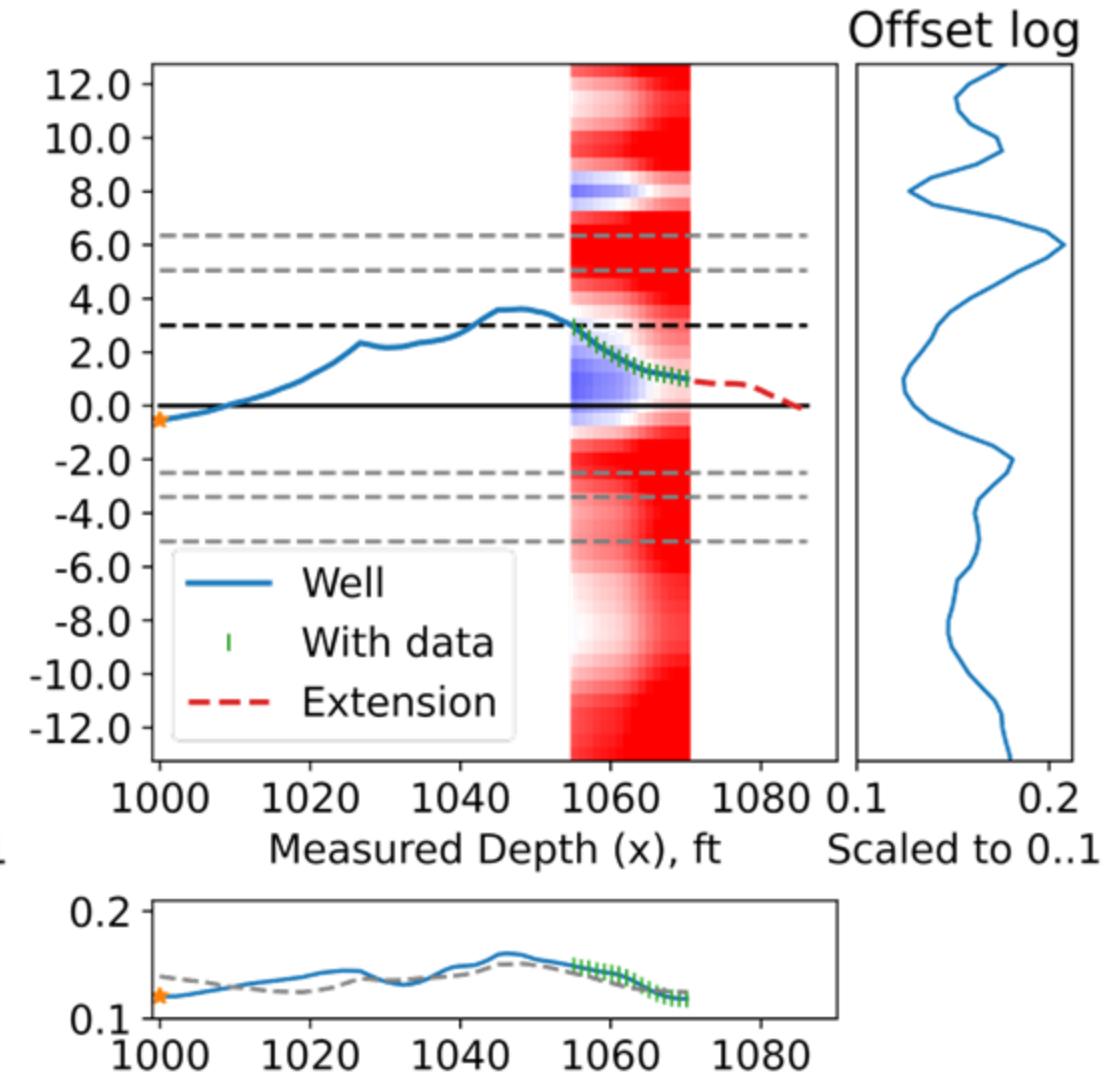
# The MDN deep-learning method

- Two orders of magnitude faster than other current methods
- Can predict and track several realizations in ‘low-data’ environment
- Assumption: noiseless data

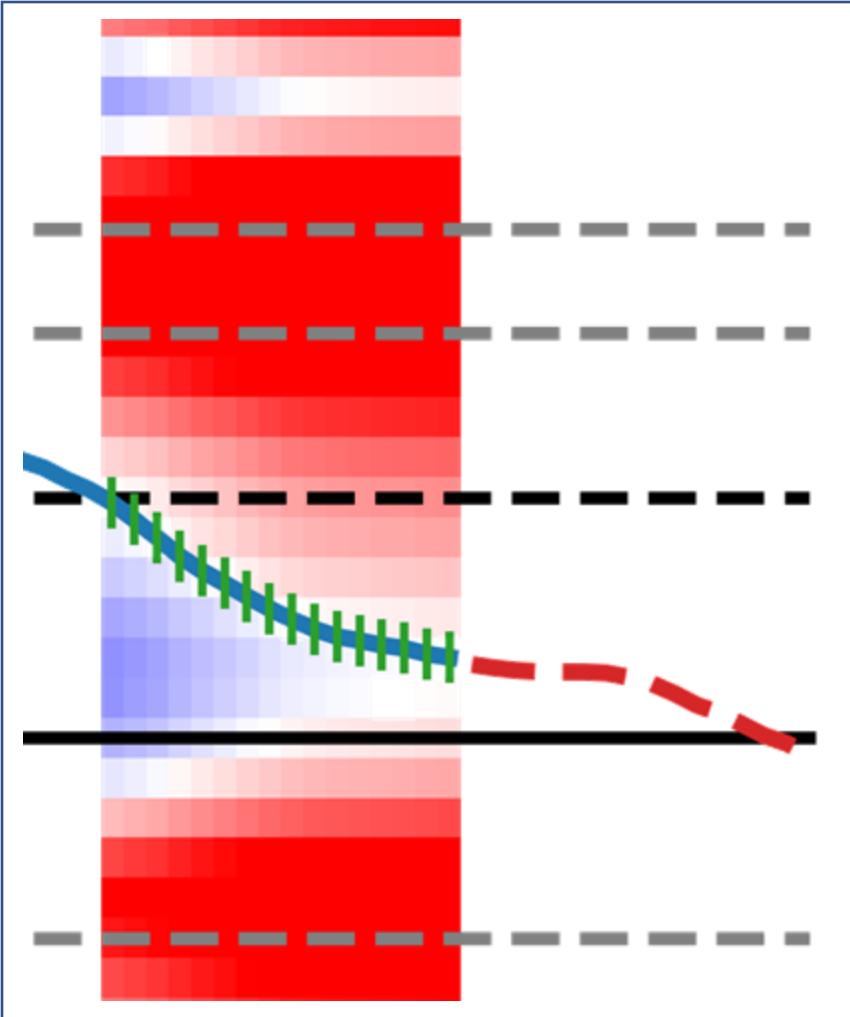
No noise



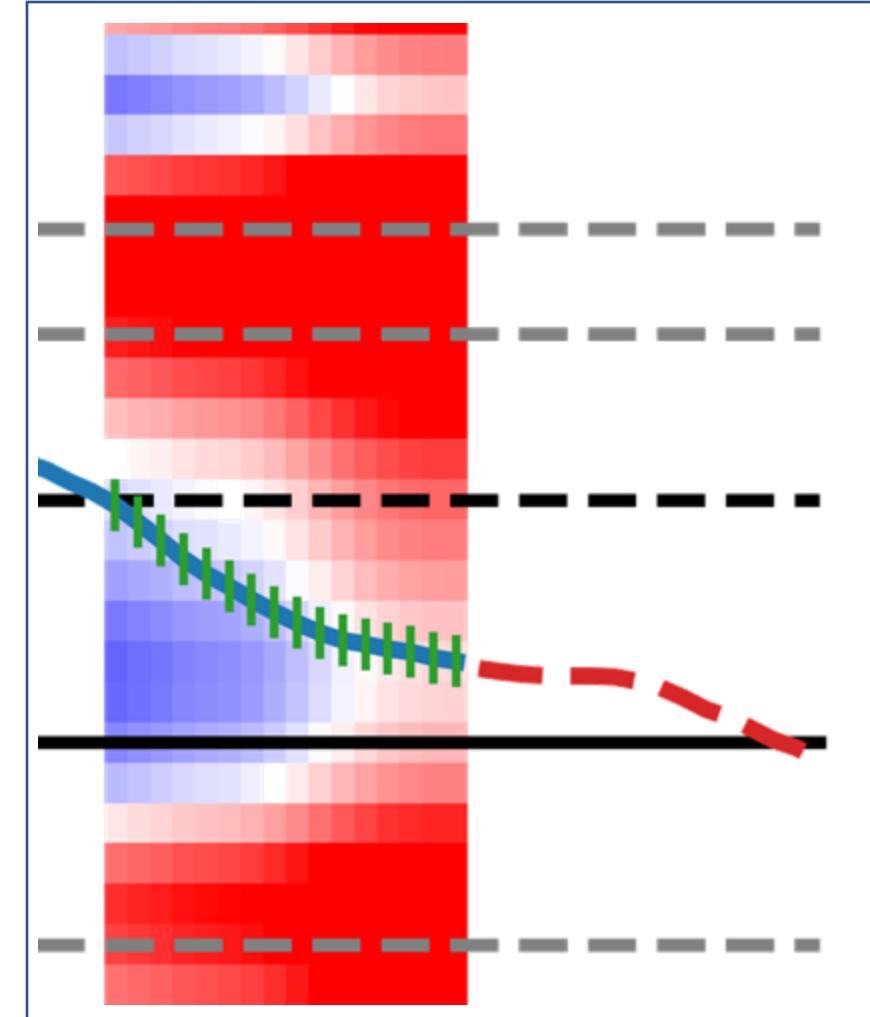
With noise



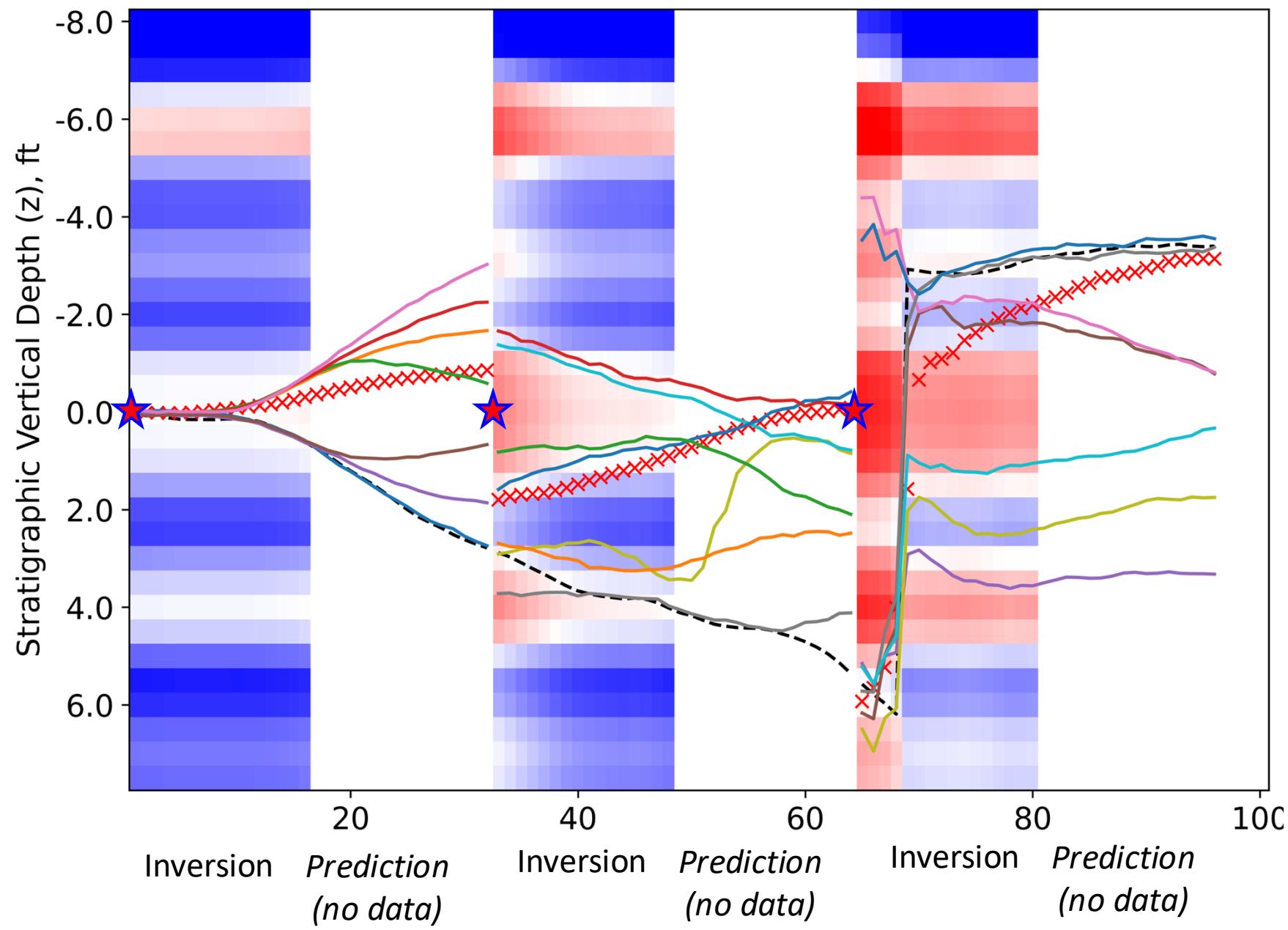
No noise



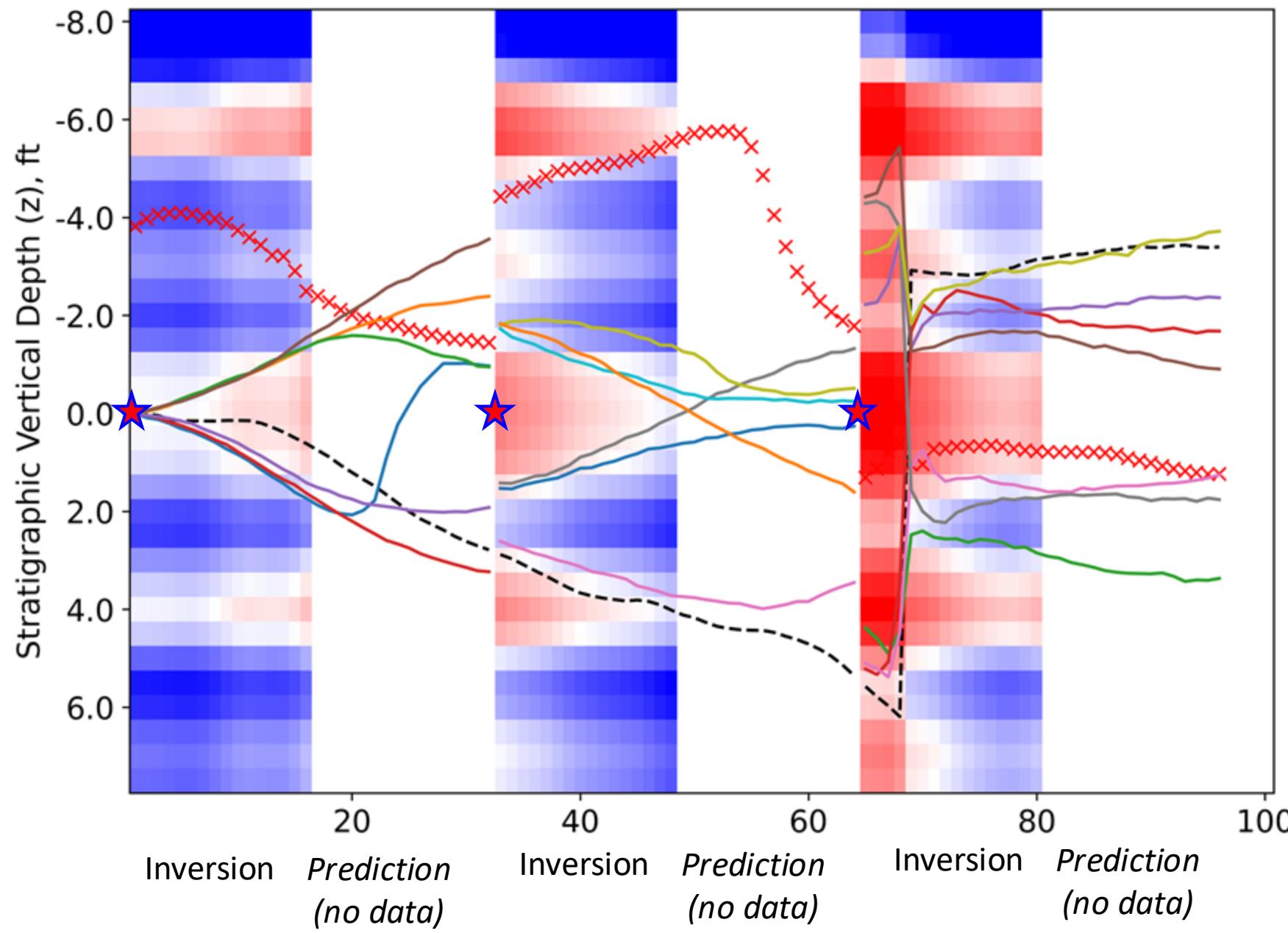
With noise



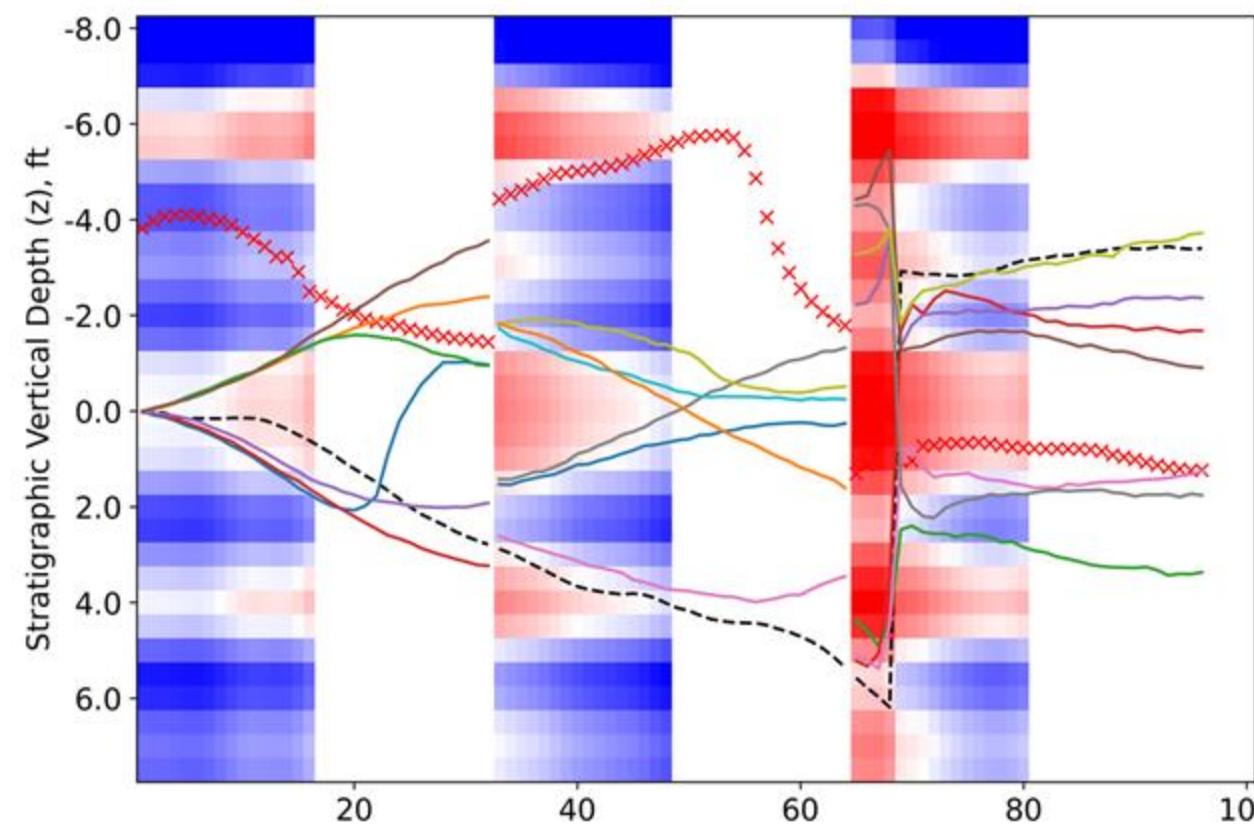
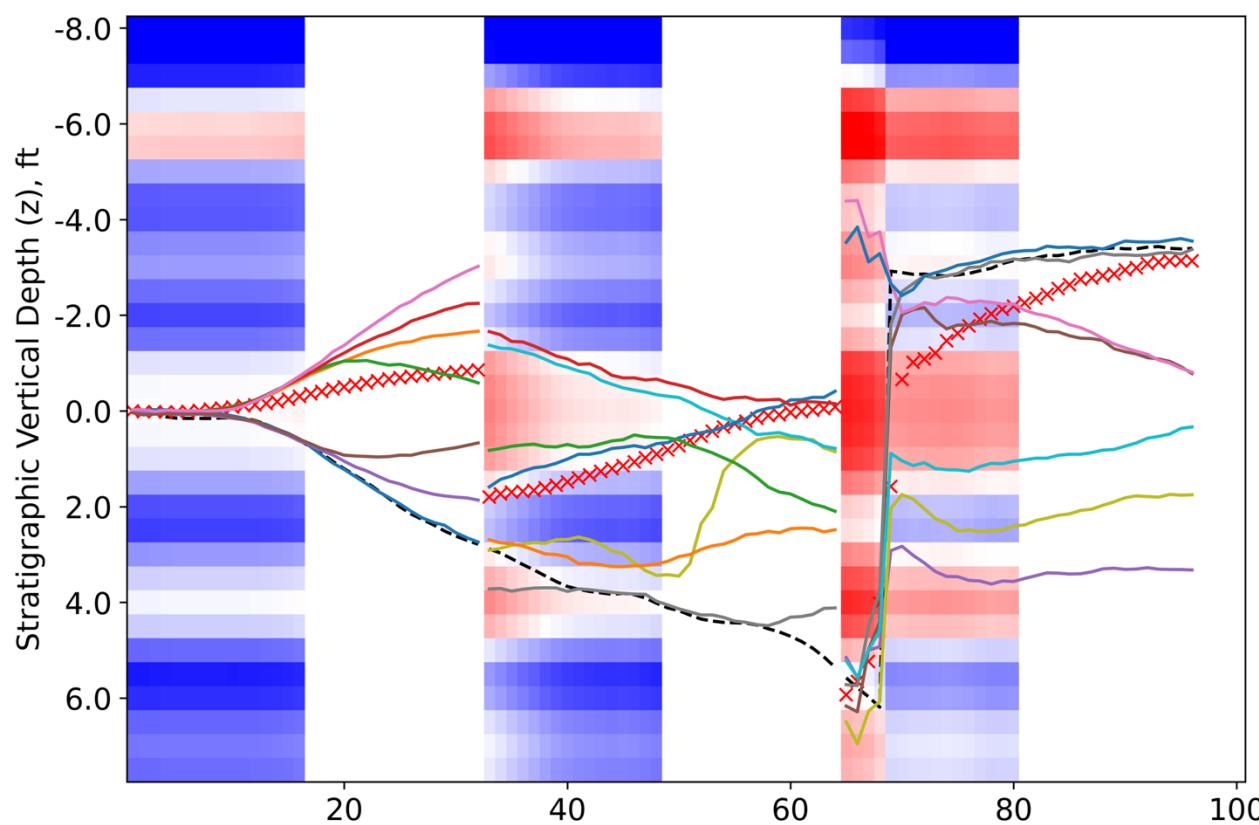
# Summary No noise



# Summary 4% noise



# Effect of 4% noise on prediction (right)



# Measuring fit quality

$$I_{NLL} = -\log \sum_m p_m \exp \left( \frac{-\|b^* - b^m\|}{\sigma^*} \right)$$


The diagram shows the formula for the Negative-Log-Likelihood ( $I_{NLL}$ ). It consists of two main parts: a probability term, represented by a blue U-shaped bracket under the sum, and a mismatch term scaled by a kernel width, represented by a blue bracket under the exponential term.

Probability      Mismatch for one mode  
scaled with kernel 'width'

Negative-Log-Likelihood misfit goes to zero if

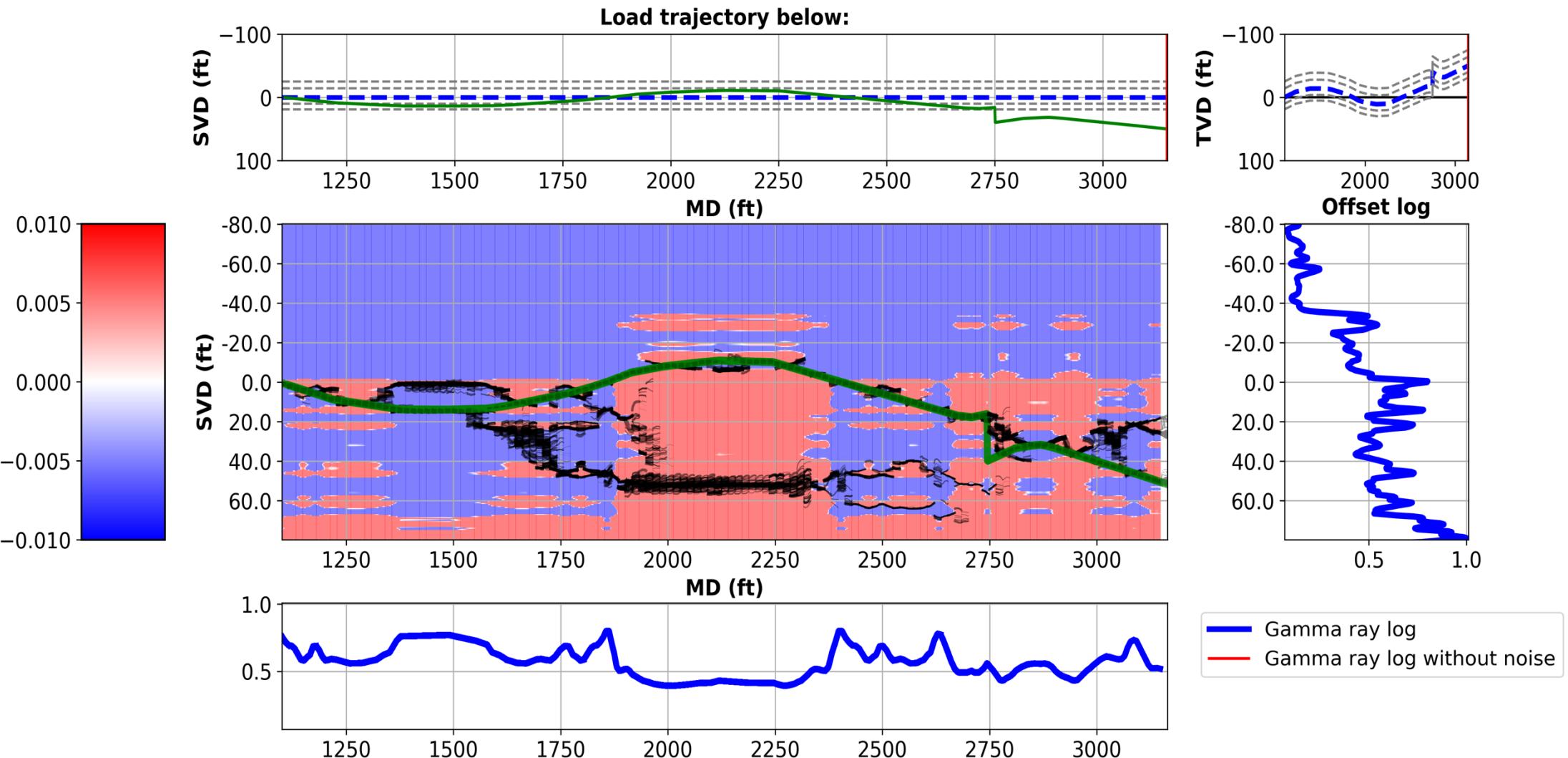
- the mode kernel coincides with the solution  $b^* == b^m$  and
- has  $p=1$

# Results on noisy data revisited

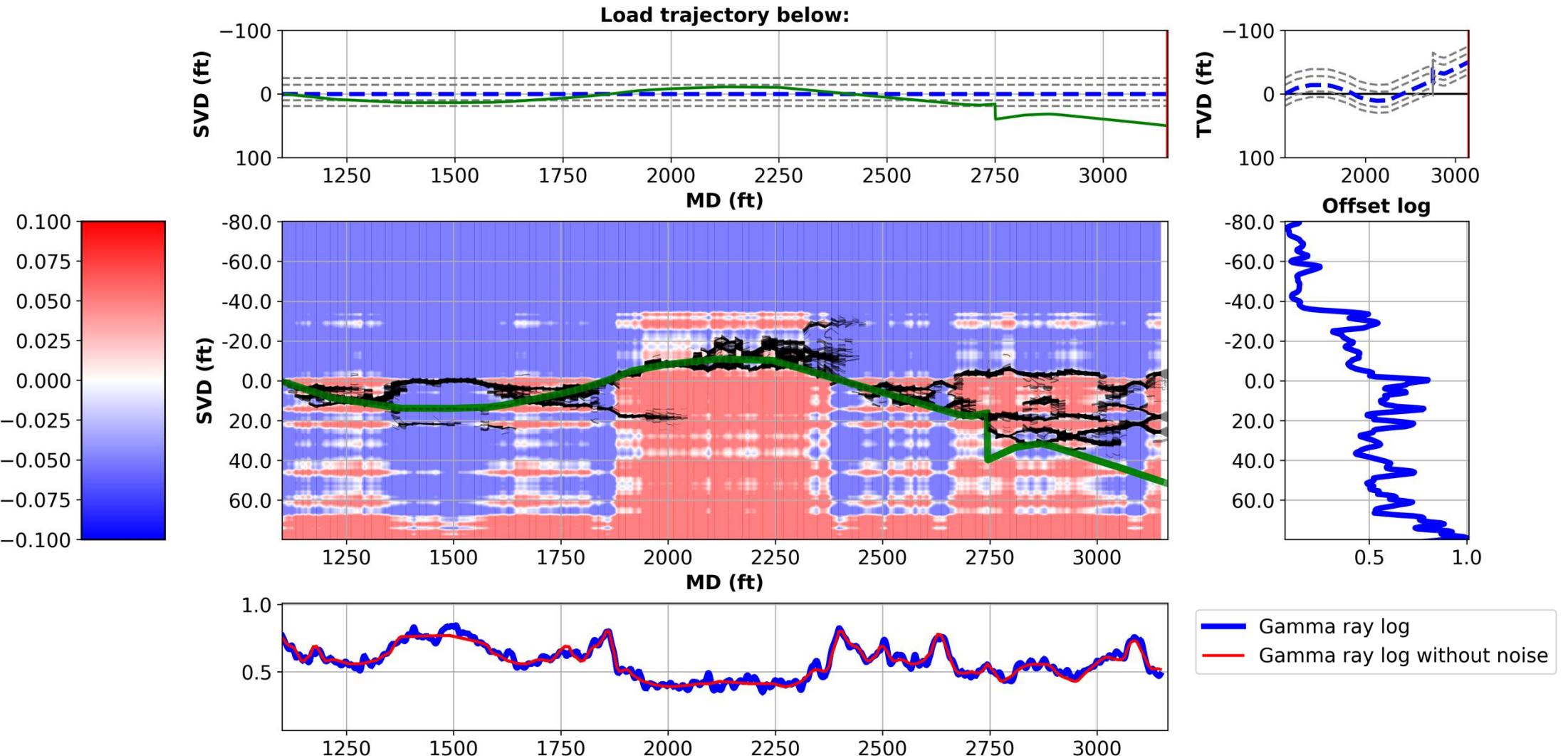
7-mode predictor	Evaluation noise			
	1%	2%	4%	10%
Noise, training ↓				
<i>0-base-case</i>	0.9444	0.9444	0.9444	0.9444
*0%	0.7687	1.0673	1.4507	1.8966
1%	0.5609	0.6824	1.0129	1.5737
2%	0.5592	0.6008	0.7497	1.2594
4%	0.6226	0.6354	0.6809	0.9458
10%	0.7290	0.7322	0.7429	0.7996

- Best results in a column when training noise is equal to evaluation noise
- Best results in a row when noise is smallest
- Trained with 10% noise is on-par noiseless model tested with 1% noise
  - Our method can handle the log noise above the industry standard 6-7%.

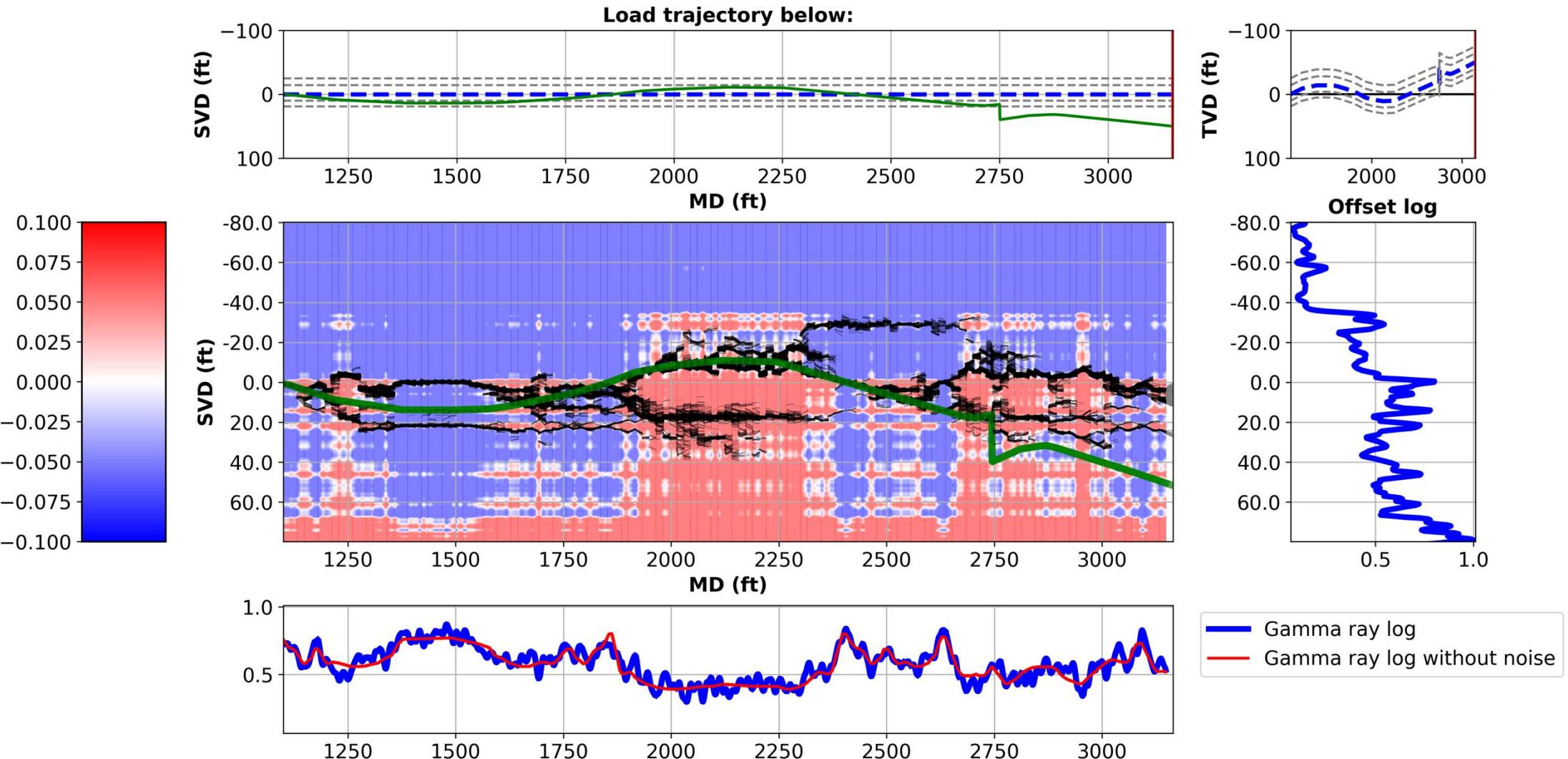
# GWC dataset 0% noise



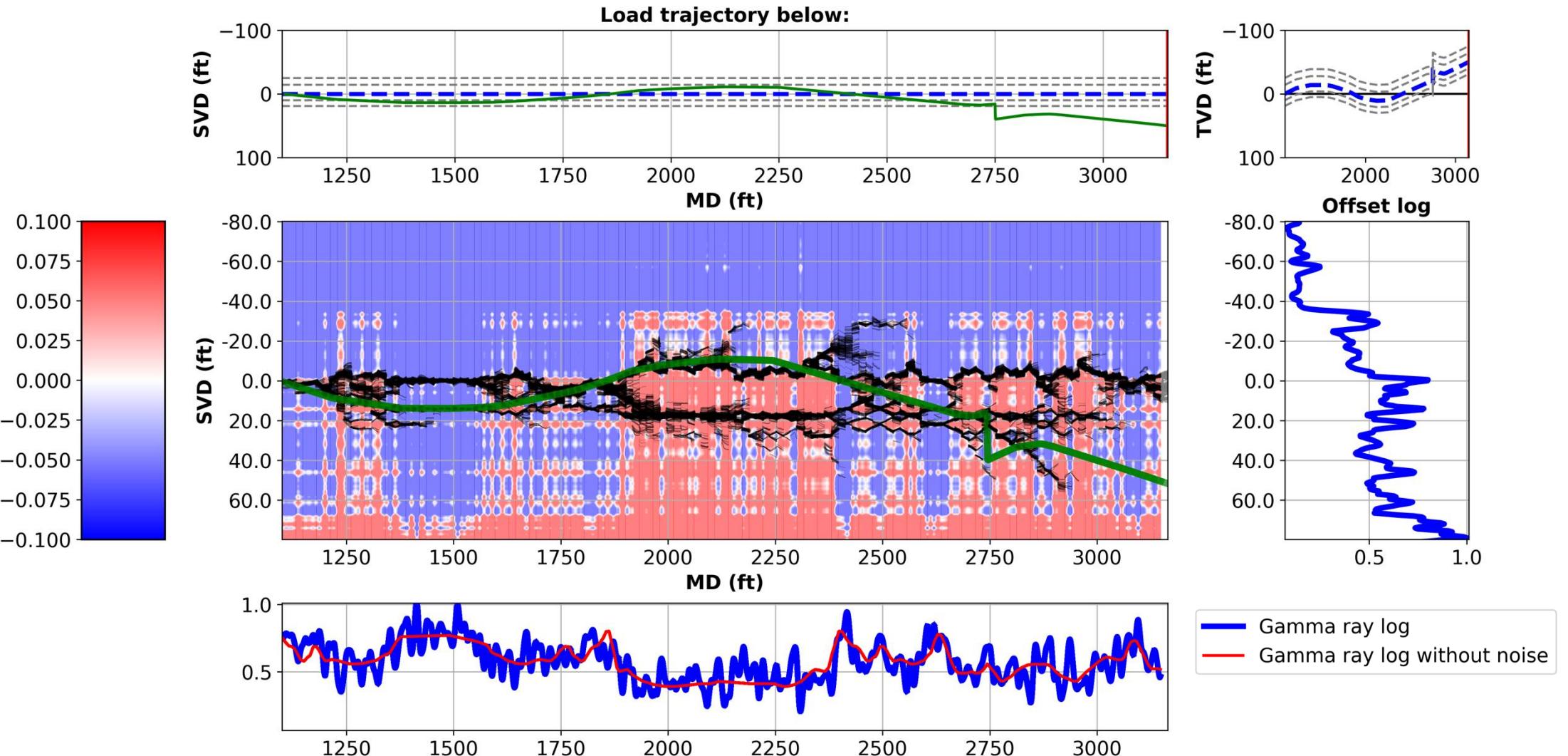
# GWC dataset 1% noise



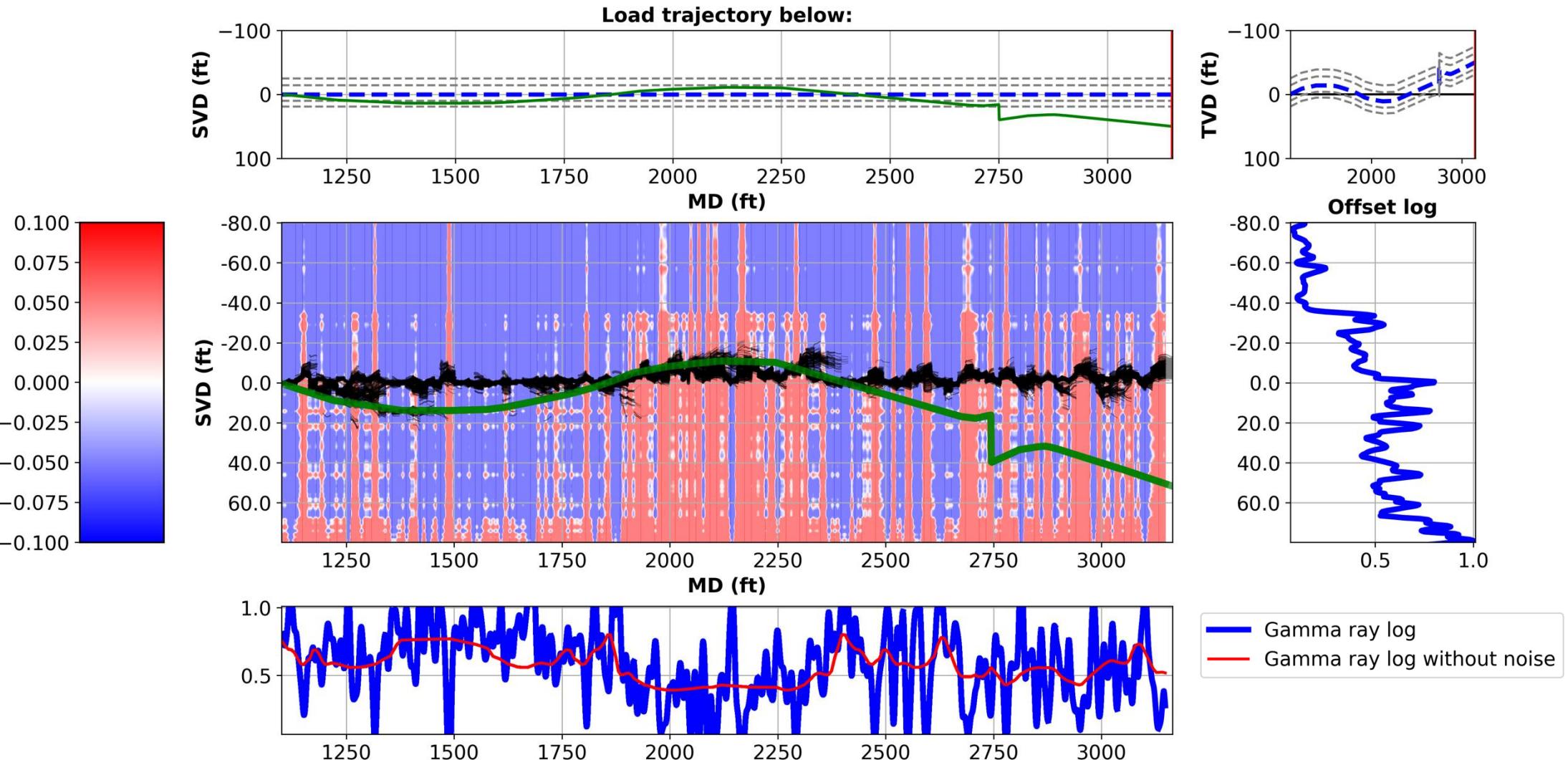
# GWC dataset 2% noise



# GWC dataset 4% noise



# GWC dataset 10% noise



# Conclusions

- New MDN learns
  1. **ability to interpret logs**
  2. **geological information to quantify likelihoods**
  3. **handles realistic 4% noise**
- Probabilistic interpretation tracks several solutions
  - Robust even in complex environment
  - At 800 m/s **100 times faster** than earlier probabilistic methods
- Current status:
  - Waiting for more funding since my parental leave ☺

