

# Improving Public Transit Systems through Clustering and Polynomial Regression

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**Abstract**—As urban mass transportation systems worldwide evolve, they adapt to the ever-changing needs of their residents. This paper explores a machine-learning approach by using clustering and polynomial regression. This model fits transportation corridors and hubs to optimize the population served using points of interest and hotspots. Scoring of station and line candidates is performed through a summation of Gaussian distributions between the candidate and each point of interest. A novel approach to generating transportation interchanges through heuristics is also explored.

## I. INTRODUCTION

Public transit systems around the world vary significantly, fitting the needs of locals and adapting to the local geography. Urban and city planners spend countless hours finding the optimal routes to operate different modes of transit such as busses, trams, subways, and ferries to fulfil the commuting requirements of the public. Often, this process takes years to plan and decades to execute, all while the urban compositions and needs of the public continue to evolve. This results in building transit based on now outdated information. Building transit for the future is more important than ever as population centres continue to grow, and road infrastructure increasingly becomes more congested for personal vehicles. The biggest reason why people end up buying a car instead of taking public transit is because of the inconvenience associated with using the system – a symptom of poor and outdated public transit planning.

### A. Motivation

With the vast amount of geographical data that is publicly available, artificial intelligence could be applied to these large datasets to generate ideas for urban planners. The main idea of this project was to create an application that can give realistic solutions to rapid transit lines in any given city. As the need for better and more efficient transit grows around the world, it is imperative to make use of artificial intelligence tools.

### B. Related Works

There have been numerous attempts related to our approach to transit route planning. "Improving Transit Accessibility with Machine Learning" by Google AI Blog is one of them, this project uses k-means clustering and regression techniques to predict transit demand and optimize route planning for increased accessibility which gives us inspirations [1]. And there is a guidebook about transit center site selection study

to address some good plans in public transit station location settings and amenities important to planning [2].

### C. Problem Definition

The objective of the project is to design an optimized subway system for any city in the world using machine learning. Specifically, K-Means Clustering and Regression algorithms will be used to determine the most efficient subway lines. Data sets on points of interests, schools, restaurants and other high traffic locations will be collected to ensure the lines generated are truly the most effective/efficient. The minimum viable product is to generate an optimized transit system for the city of Toronto.

The project will provide a tool for urban and city planners to make informed decisions when designing and implementing a new subway system. It will also give people the opportunity to compare any given subway system with what the most efficient/effective version would be. The final product will be a system that can improve the subway infrastructure of cities, so a greater percentage of the population can be reached.

Overall, the success of this project will be measured by the percentage of people each implemented station serves. This will then be compared to the data provided by the city of Toronto on what percentage of the population the current system services. If the generated system reaches a greater percentage of the population then the project can be deemed a success.

## II. METHODOLOGY

The datasets obtained were data from OpenStreetMap, via API requests. The desired data was to find all amenities (e.g. community centres, library, restaurants) in a city, and save them into individual CSV files for further analysis. For example, a query would just be a coordinate, which will convert into an Overpass API query, (a read-only API that serves up custom selected parts of the OSM map data) finding the name of the city. Another request is based off the previous city name, then finding all amenities within the city. It then writes the latitude, longitude, and name of each amenity to a CSV file at the given file path and returns a Pandas dataframe containing the latitude and longitude of each amenity.

The result of the query returns many metadata tags, such as name, date added, and other OpenStreetMap data. Most of the

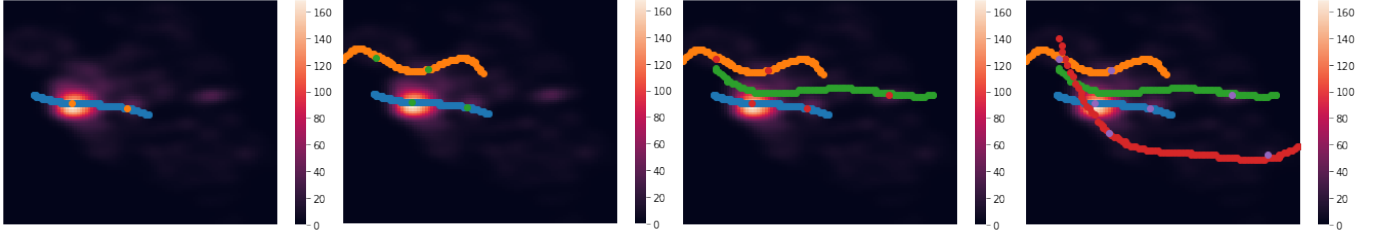


Fig. 1. Line Progression with  $C = 4$  in the City of Toronto

extra metadata was filtered out to a table of only the longitude and latitude, being returned to a CSV file.

TABLE I  
EXAMPLE OF PROCESSED DATA OF RESTAURANTS IN VANCOUVER.

Longitude	Latitude
49.2772564	-123.1187370
49.2630345	-123.1012040
49.2629465	-123.0967703
49.2621476	-123.1007434
49.2567053	-123.1018939

A score function was created to assign every coordinate a measure of usefulness. The score function was based off a Gaussian Distribution as this allowed for locations within a radius of a desired grid point to have a higher score while as the radius between the grid point and location increased the score moved to zero. This scoring function was used alongside the grid search function, which is discussed below, to give scores to each point throughout a city when compared with a data set of the locations of Points of interest, schools, restaurants, etc. Scoring is performed using a Gaussian distribution, defined as

$$f(d) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{d}{\sigma}\right)^2}$$

where  $d$  is the 2D euclidean distance between two points, and  $\sigma$  is the standard deviation. This allowed for hyper-parameter tuning as the standard deviation could be altered depending on what radius around a certain grid point should result in the largest scores.

To be able to determine which locations throughout a city are seen as high scoring areas a grid search was performed. This involved breaking the city up into an  $N \times N$  grid of squares. This grid would then be looped through with the distance of each square and the locations of each point in the data sets being calculated. These distances would be put into the scoring function and the scores for each grid point would be summed up, given a total score. The grid points and associated scores would then be stored in data frame would be stored for later use. A mathematical interpretation of the grid search can be seen below,

$$s_{i,j} = \sum_{k=0}^N f(d)$$

where  $s_{i,j}$  is score at  $(i,j)$ ,  $N$  is the number of points of interest,  $f(d)$  is the scoring function. The generated grid points for Toronto is shown below.

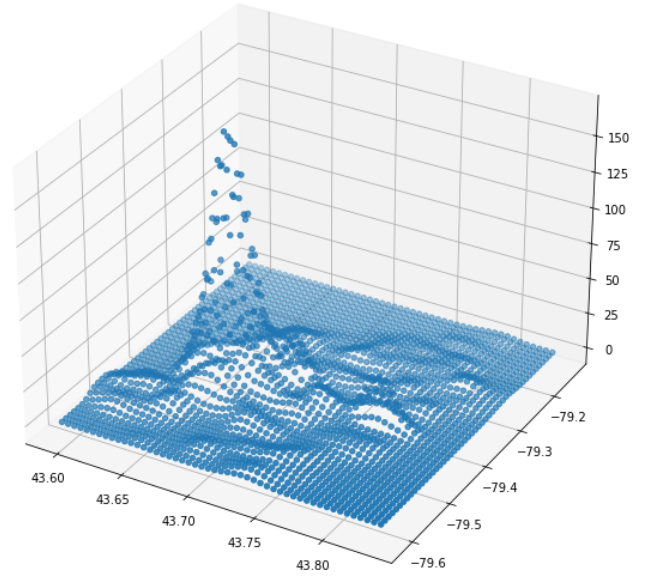


Fig. 2. Scored grid points from the City of Toronto

In any mass urban transportation system, lines in a system should be dispersed throughout the urban area, with additional level of concentration in the densest part (often the downtown area). Dispersing these lines is achieved through clustering. A slightly modified k-means algorithm is used, that considers the scores of each point as a weight  $w_i$ .

$$\sum_{i=0}^n \min_{\mu_j \in C} (w_i * ||x_i - \mu_j||^2)$$

This weighted k-means algorithm converges on a solution where cluster centers are distributed densely in high score areas, and more sparsely distributed in low score areas. This is synonymous to having more stations and lines in downtown areas, and less stations and lines in suburbs. The clusters represents the neighborhoods each line will go through. This

implies the number of lines in the system is equal to the number of clusters. The clusters are numbered at random from 0 to  $C - 1$ , where  $C$  is the number of clusters. Sorting of these clusters by average score is important for generating interchanges. After sorting, cluster 0 has points that make up the highest average score, cluster 1 has the next highest, etc. The clusters for  $C = 6$  in the City of Toronto is shown below.

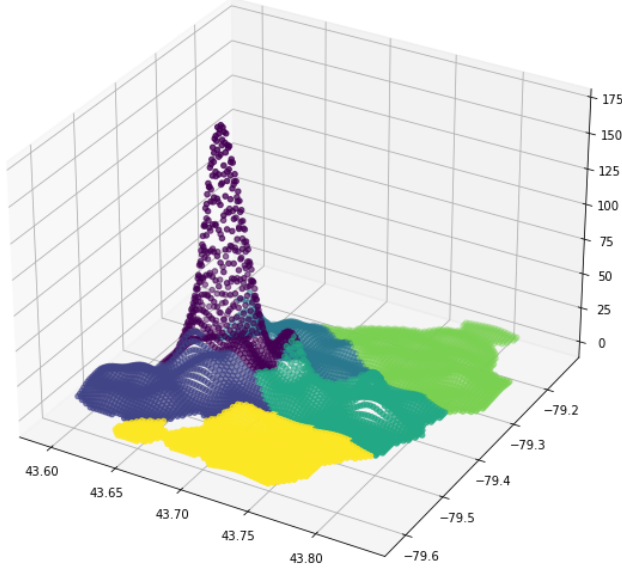


Fig. 3. Scored and clustered grid points from the City of Toronto

After the creations of cluster the problem of fitting subway lines needed to be solved. The solution to this was to isolate each cluster and perform weighted polynomial linear regression on each cluster. Weighted polynomial regression was chosen as it allowed for a prediction of locations based of the scores. Polynomial regression was chosen over linear regression as it allowed for a better coverage of the grid points compared to a straight line. It also allowed for manipulation of the degree of the polynomial to ensure maximum coverage. The points of the regression lines were snapped onto the existing grid to ensure working with the data would be simpler later on.

Interchanges are an important feature in designing mass public transit systems. By running polynomial regression on each cluster separately, the resulting system of lines will not overlap as each line is designed to optimize for its constituent grid points. This implies that there are no interchanges on the system. To address this, an iterative approach to generating lines is considered. Each line is generated successively from previous lines, and utilizes information from previously generated lines. Line generation starts from cluster 0 - the cluster with the highest cumulative score. Potential interchanges, or interchange candidates are identified on each line generation

through

$$I_l = \underset{i \in L_l}{\operatorname{argmax}}(s_i)$$

where  $I_l$  is the interchange candidate for line  $l$ ,  $L_l$  is the set of points in line  $l$ ,  $s_i$  is the score for the  $i^{th}$  point on the line. The value of the grid point associated with  $I_l$  is multiplied by a factor  $A$  such that the new value  $V$  is more favourable to the regression of the next line. This modified grid point is added to the set of points for all future lines, i.e.

$$\forall k \in \{0, \dots, C - 1\}, L_{l+k} = L_{l+k} \cup \{V\}$$

The interchange candidates also decay after each iteration. This is to encourage future line generation to consider other interchanges and not just the first interchange. After each iteration, each interchange candidate is divided by a decay factor  $\rho$ .

To find the locations of each station a function was created that would loop through the points for each one of the subway lines. A station was placed at the end point and from there the distance between that point and the next one was compared to see if they were a certain distance apart. This distance is a parameter passed into the function. If the distance wasn't met the station would be compared with the next point after. If the distance requirement was met then a station would be placed at this location and the comparison process would begin again. This process would continue until all points on the subway line are checked.

The interface the website was built on was React.js. Within the website, the final visualization of the processed data would be displayed in React Leaflet, a JavaScript library that displays interactive maps. A JSON file would be passed into code, iteratively creating lines and stations based off of a general schema.

### III. RESULTS

As stated in the problem definition the percentage of the population the final design reaches will be compared to the current transit system for the desired city. By the minimal viable product a comparison will be performed with the city of Toronto.

To determine the percentage of the population the generated subway system reached a function was created that went through each station of each line and calculated the distance between the station and all the grid points from the grid search function. If the distance was less than some max distance then the score would be stored in a separate array for that line. From here the mean score for each line would be calculated. The figure below shows a generated system for Toronto that consists of four lines.

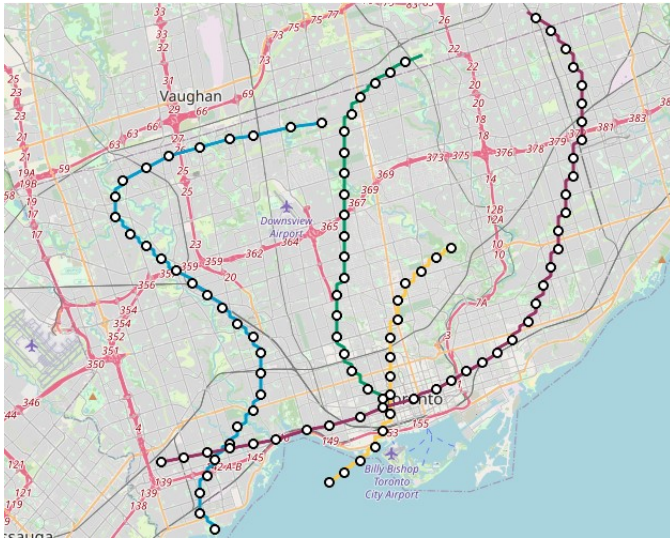


Fig. 4. Generated System for the City of Toronto,  $C = 4$

The mean scores for each line was then compared to the mean score of the each TTC line. The results showed that the predicted transit system was 50% less optimal than the TTC system. This is a result of not considering enough data points to ensure that the stations were reaching all highly populated areas.

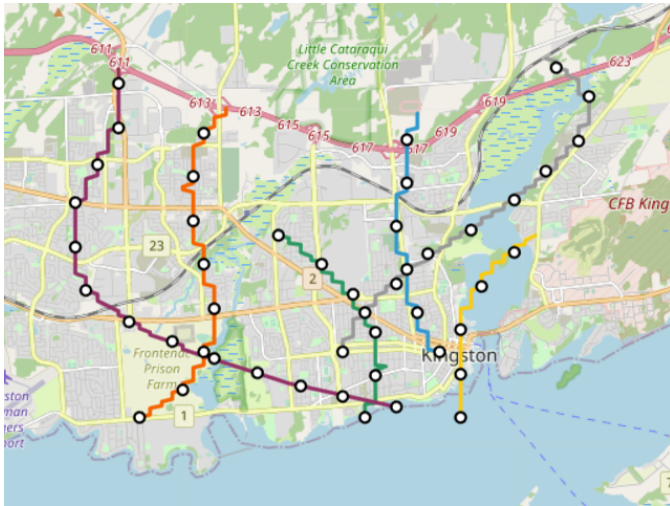


Fig. 5. Generated System for the City of Kingston,  $C = 6$

A subway system for Kingston was also generated with all the scripts available. Although a subway system may never be viable in Kingston, predictions were ran to demonstrate the flexibility of the models.

#### IV. CONCLUSION

In conclusion an optimized subway system generator was created for any city in the world using machine learning. This involved combining a K-means clustering and polynomial

regression algorithm together to be able to determine line placement throughout a city. These algorithms were used on a set of scored grid points that were calculated using a grid search alongside a created score function. A novel approach to generating interchanges through heuristics was also explored. In the end a subway system generated for the city of Toronto that was 50% less optimal than the current TTC model.

For future improvements a larger data set will be used to ensure that all high traffic areas are considered when running the algorithms. On top of this there will need to be improvement on the function that bounds the desired city that the lines are being generated for. This will ensure that when the lines are generated there won't be lines that end up crossing over the water. On top of this the function that determines station location can be improved to not place stations in regions that are water or residential locations.

#### REFERENCES

- [1] Wisconsin Department of Transportation. <https://wisconsin.gov/Documents/doing-bus/local-gov/astnce-pgms/transit/ec-site.pdf>.
- [2] Google AI Blog. "Improving Transit Accessibility with Machine Learning."