Introduction To Programming With MathRider And MathPiper

by Ted Kosan

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1 1 Preface

2 1.1 Dedication

- 3 This book is dedicated to Steve Yegge and his blog entry "Math Every Day"
- 4 (http://steve.yegge.googlepages.com/math-every-day).

5 1.2 Acknowledgments

- 6 The following people have provided feedback on this book (if I forgot to include
- 7 your name on this list, please email me at ted.kosan at gmail.com):
- 8 Susan Addington
- 9 Matthew Moelter
- 10 Sherm Ostrowsky

11 1.3 Support Email List

- 12 The support email list for this book is called **mathrider-**
- 13 **users@googlegroups.com** and you can subscribe to it at
- 14 <u>http://groups.google.com/group/mathrider-users</u>.

15 1.4 Recommended Weekly Sequence When Teaching A Class With This

16 **Book**

- 17 Week 1: Sections 1 6.
- 18 Week 2: Sections 7 9.
- 19 Week 3: Sections 10 13.
- 20 Week 4: Sections 14 15.
- 21 Week 5: Sections 16 19.

22 2 Introduction

32

- 23 MathRider is an open source mathematics computing environment for
- 24 performing numeric and symbolic computations (the difference between numeric
- 25 and symbolic computations are discussed in a later section). Mathematics
- 26 computing environments are complex and it takes a significant amount of time
- 27 and effort to become proficient at using one. The amount of power that these
- 28 environments make available to a user, however, is well worth the effort needed
- 29 to learn one. It will take a beginner a while to become an expert at using
- 30 MathRider, but fortunately one does not need to be a MathRider expert in order
- 31 to begin using it to solve problems.

2.1 What Is A Mathematics Computing Environment?

- 33 A Mathematics Computing Environment is a set of computer programs that 1)
- 34 automatically execute a wide range of numeric and symbolic mathematics
- 35 calculation algorithms and 2) provide a user interface which enables the user to
- 36 access these calculation algorithms and manipulate the mathematical objects
- 37 they create (An algorithm is a step-by-step sequence of instructions for solving a
- 38 problem and we will be learning about algorithms later in the book).
- 39 Standard and graphing scientific calculator users interact with these devices
- 40 using buttons and a small LCD display. In contrast to this, users interact with
- 41 MathRider using a rich graphical user interface which is driven by a computer
- 42 keyboard and mouse. Almost any personal computer can be used to run
- 43 MathRider, including the latest subnotebook computers.
- 44 Calculation algorithms exist for many areas of mathematics and new algorithms
- 45 are constantly being developed. Software that contains these kind of algorithms
- 46 is commonly referred to as "Computer Algebra Systems (CAS)". A significant
- 47 number of computer algebra systems have been created since the 1960s and the
- 48 following list contains some of the more popular ones:
- 49 http://en.wikipedia.org/wiki/Comparison of computer algebra systems
- 50 Some environments are highly specialized and some are general purpose. Some
- allow mathematics to be entered and displayed in traditional form (which is what
- 52 is found in most math textbooks). Some are able to display traditional form
- 53 mathematics but need to have it input as text and some are only able to have
- 54 mathematics displayed and entered as text.
- 55 As an example of the difference between traditional mathematics form and text
- 56 form, here is a formula which is displayed in traditional form:

$$a = x^2 + 4hx + \frac{3}{7}$$

57 and here is the same formula in text form:

 $a = x^2 + 4*h*x + 3/7$

- 59 Most computer algebra systems contain a mathematics-oriented programming
- 60 language. This allows programs to be developed which have access to the
- 61 mathematics algorithms which are included in the system. Some mathematics-
- oriented programming languages were created specifically for the system they
- 63 work in while others were built on top of an existing programming language.
- 64 Some mathematics computing environments are proprietary and need to be
- 65 purchased while others are open source and available for free. Both kinds of
- systems possess similar core capabilities, but they usually differ in other areas.
- 67 Proprietary systems tend to be more polished than open source systems and they
- often have graphical user interfaces that make inputting and manipulating
- 69 mathematics in traditional form relatively easy. However, proprietary
- 70 environments also have drawbacks. One drawback is that there is always a
- 71 chance that the company that owns it may go out of business and this may make
- 72 the environment unavailable for further use. Another drawback is that users are
- variable to enhance a proprietary environment because the environment's source
- 74 code is not made available to users.
- 75 Some open source computer algebra systems do not have graphical user
- 76 interfaces, but their user interfaces are adequate for most purposes and the
- 77 environment's source code will always be available to whomever wants it. This
- 78 means that people can use the environment for as long as they desire and they
- 79 can also enhance it.

80 2.2 What Is MathRider?

- 81 MathRider is an open source Mathematics Computing Environment which has
- 82 been designed to help people teach themselves the STEM disciplines (Science.
- 83 Technology, Engineering, and Mathematics) in an efficient and holistic way. It
- 84 inputs mathematics in textual form and displays it in either textual form or
- 85 traditional form.
- 86 MathRider uses MathPiper as its default computer algebra system, BeanShell as
- 87 its main scripting language, jEdit as its framework (hereafter referred to as the
- 88 MathRider framework), and Java as it overall implementation language. One
- 89 way to determine a person's MathRider expertise is by their knowledge of these
- 90 components. (see Table 1)

98

Level	Knowledge
MathRider Developer	Knows Java, BeanShell, and the MathRider framework at an advanced level. Is able to develop MathRider plugins.
MathRider Customizer	Knows Java, BeanShell, and the MathRider framework at an intermediate level. Is able to develop MathRider macros.
MathRider Expert	Knows MathPiper at an advanced level and is skilled at using most aspects of the MathRider application.
MathRider Novice	Knows MathPiper at an intermediate level, but has only used MathRider for a short while.
MathRider Newbie	Does not know MathPiper but has been exposed to at least one programming language.
Programming Newbie	Does not know how a computer works and has never programmed before but knows how to use a word processor.

Table 1: MathRider user experience levels.

- 91 This book is for MathRider and Programming Newbies. This book will teach you
- 92 enough programming to begin solving problems with MathRider and the
- 93 language that is used is MathPiper. It will help you to become a MathRider
- Novice, but you will need to learn MathPiper from books that are dedicated to it
- 95 before you can become a MathRider Expert.
- 96 The MathRider project website (http://mathrider.org) contains more information
- 97 about MathRider along with other MathRider resources.

2.3 What Inspired The Creation Of Mathrider?

- 99 Two of MathRider's main inspirations are Scott McNeally's concept of "No child 100 held back":
- 101 http://weblogs.java.net/blog/turbogeek/archive/2004/09/no_child_held_b_1.html
- and Steve Yegge's thoughts on learning mathematics:
- 1) Math is a lot easier to pick up after you know how to program. In fact, if you're a halfway decent programmer, you'll find it's almost a snap.
- 105 2) They teach math all wrong in school. Way, WAY wrong. If you teach yourself math the right way, you'll learn faster, remember it longer, and it'll be much more valuable to you as a programmer.
- 3) The right way to learn math is breadth-first, not depth-first. You need to survey the space, learn the names of things, figure out what's what.
- http://steve-yegge.blogspot.com/2006/03/math-for-programmers.html

- 111 MathRider is designed to help a person learn mathematics on their own with
- little or no assistance from a teacher. It makes learning mathematics easier by
- focusing on how to program first and it facilitates a breadth-first approach to
- 114 learning mathematics.

115 3 Downloading And Installing MathRider

116 3.1 Installing Sun's Java Implementation

- 117 MathRider is a Java-based application and therefore a current version of Sun's
- 118 Java (at least Java 6) must be installed on your computer before MathRider can
- 119 be run.

120 3.1.1 Installing Java On A Windows PC

- 121 Many Windows PCs will already have a current version of Java installed. You can
- test to see if you have a current version of Java installed by visiting the following
- 123 web site:
- 124 <u>http://java.com/</u>
- 125 This web page contains a link called "Do I have Java?" which will check your Java
- version and tell you how to update it if necessary.

127 3.1.1.1 The 64 Bit Version Of Windows Needs The 64 Bit Version Of Java

- 128 If you are using the 64 bit version of Windows, then you will need the 64 bit
- version of Java. The 64 bit version of Java can be obtained here:
- 130 https://cds.sun.com/is-bin/INTERSHOP.enfinity/WFS/CDS-CDS Developer-
- 131 <u>Site/en_US/-/USD/ViewProductDetail-Start?ProductRef=jre-6u16-oth-JPR@CDS-</u>
- 132 <u>CDS Developer</u>

133 3.1.2 Installing Java On A Macintosh

- 134 Macintosh computers have Java pre-installed but you may need to upgrade to a
- 135 current version of Java (at least Java 6) before running MathRider. If you need
- to update your version of Java, visit the following website:
- 137 <u>http://developer.apple.com/java.</u>

138 3.1.3 Installing Java On A Linux PC

- 139 Locate the Java documentation for your Linux distribution and carefully follow
- 140 the instructions provided for installing a Java 6 compatible version of Java on
- 141 your system.

142 3.2 Downloading And Extracting

One of the many benefits of learning MathRider is the programming-related

- knowledge one gains about how open source software is developed on the
- 145 Internet. An important enabler of open source software development are
- websites, such as sourceforge.net (http://sourceforge.net) and java.net
- 147 (http://java.net) which make software development tools available for free to
- 148 open source developers.
- 149 MathRider is hosted at java.net and the URL for the project website is:
- 150 <u>http://mathrider.org</u>

173

- 151 MathRider can be obtained by selecting the **download** tab and choosing the
- 152 correct download file for your computer. Place the download file on your hard
- drive where you want MathRider to be located. For Windows users, it is
- 154 recommended that MathRider be placed somewhere on c: drive.
- 155 The MathRider download consists of a main directory (or folder) called
- 156 **mathrider** which contains a number of directories and files. In order to make
- downloading guicker and sharing easier, the mathrider directory (and all of its
- 158 contents) have been placed into a single compressed file called an **archive**. For
- 159 **Windows** systems, the archive has a .zip extension and the archives for Unix-
- 160 **based** systems have a .tar.bz2 extension.
- 161 After an archive has been downloaded onto your computer, the directories and
- 162 files it contains must be **extracted** from it. The process of extraction
- uncompresses copies of the directories and files that are in the archive and
- places them on the hard drive, usually in the same directory as the archive file.
- 165 After the extraction process is complete, the archive file will still be present on
- 166 your drive along with the extracted **mathrider** directory and its contents.
- 167 The **archive file** can be easily copied to a CD or USB drive if you would like to
- install MathRider on another computer or give it to a friend. However, don't
- 169 try to run MathRider from a USB drive because it will not work correctly.
- 170 (Note: If you already have a version of MathRider installed and you want
- to install a new version in the same directory that holds the old version,
- 172 you must delete the old version first or move it to a separate directory.)

3.2.1 Extracting The Archive File For Windows Users

- 174 Usually the easiest way for Windows users to extract the MathRider archive file
- is to navigate to the folder which contains the archive file (using the Windows
- 176 GUI), right click on the archive file (it should appear as a folder with a
- vertical zipper on it), and select Extract All... from the pop up menu.
- 178 After the extraction process is complete, a new folder called **mathrider** should
- 179 be present in the same folder that contains the archive file. (Note: be careful
- 180 not to double click on the archive file by mistake when you are trying to
- 181 open the mathrider folder. The Windows operating system will open the
- archive just like it opens folders and this can fool you into thinking you

- 183 are opening the mathrider folder when you are not. You may want to
- move the archive file to another place on your hard drive after it has
- been extracted to avoid this potential confusion.)

186 3.2.2 Extracting The Archive File For Unix Users

- One way Unix users can extract the download file is to open a shell, change to
- the directory that contains the archive file, and extract it using the following
- 189 command:

193

- 190 tar -xvjf <name of archive file>
- 191 If your desktop environment has GUI-based archive extraction tools, you can use
- 192 these as an alternative.

3.3 MathRider's Directory Structure & Execution Instructions

194 The top level of MathRider's directory structure is shown in Illustration 1:

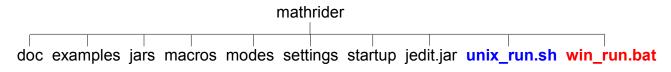


Illustration 1: MathRider's Directory Structure

- 195 The following is a brief description this top level directory structure:
- 196 **doc** Contains MathRider's documentation files.
- 197 **examples** Contains various example programs, some of which are pre-opened
- 198 when MathRider is first executed.
- iars Holds plugins, code libraries, and support scripts.
- 200 **macros** Contains various scripts that can be executed by the user.
- 201 **modes** Contains files which tell MathRider how to do syntax highlighting for
- 202 various file types.
- 203 **settings** Contains the application's main settings files.
- 204 **startup** Contains startup scripts that are executed each time MathRider
- 205 launches.
- 206 **jedit.jar** Holds the core jEdit application which MathRider builds upon.
- 207 **unix run.sh** The script used to execute MathRider on Unix systems.
- win run.bat The batch file used to execute MathRider on Windows systems.

209 3.3.1 Executing MathRider On Windows Systems

- 210 Open the mathrider folder (not the archive file!) and double click on the
- 211 **win run** file.

212 3.3.2 Executing MathRider On Unix Systems

- 213 Open a shell, change to the **mathrider** folder, and execute the **unix run.sh**
- 214 script by typing the following:
- sh unix run.sh
- 216 **3.3.2.1 MacOS X**
- 217 Make a note of where you put the Mathrider application (for example
- 218 **/Applications/mathrider**). Run Terminal (which is in /Applications/Utilities).
- 219 Change to that directory (folder) by typing:
- 220 cd /Applications/mathrider
- 221 Run mathrider by typing:
- sh unix run.sh

223

4 The Graphical User Interface

- 224 MathRider is built on top of jEdit (http://jedit.org) so it has the "heart" of a
- 225 programmer's text editor. Programmer's text editors are similar to standard text
- 226 editors (like NotePad and WordPad) and word processors (like MS Word and
- OpenOffice) in a number of ways so getting started with MathRider should be
- 228 relatively easy for anyone who has used a text editor or a word processor.
- 229 However, programmer's text editors are more challenging to use than a standard
- 230 text editor or a word processor because programmer's text editors have
- 231 capabilities that are far more advanced than these two types of applications.
- 232 Most software is developed with a programmer's text editor (or environments
- 233 which contain one) and so learning how to use a programmer's text editor is one
- of the many skills that MathRider provides which can be used in other areas.
- 235 The MathRider series of books are designed so that these capabilities are
- 236 revealed to the reader over time.
- 237 In the following sections, the main parts of MathRider's graphical user interface
- 238 are briefly covered. Some of these parts are covered in more depth later in the
- 239 book and some are covered in other books.
- 240 As you read through the following sections, I encourage you to explore
- 241 each part of MathRider that is being discussed using your own copy of
- 242 **MathRider.**

243

254

4.1 Buffers And Text Areas

- In MathRider, open files are called **buffers** and they are viewed through one or
- 245 more **text areas**. Each text area has a tab at its upper-left corner which displays
- 246 the name of the buffer it is working on along with an indicator which shows
- 247 whether the buffer has been saved or not. The user is able to select a text area
- 248 by clicking its tab and double clicking on the tab will close the text area. Tabs
- can also be rearranged by dragging them to a new position with the mouse.

250 **4.2 The Gutter**

- 251 The gutter is the vertical gray area that is on the left side of the main window. It
- 252 can contain line numbers, buffer manipulation controls, and context-dependent
- 253 information about the text in the buffer.

4.3 Menus

- 255 The main menu bar is at the top of the application and it provides access to a
- 256 significant portion of MathRider's capabilities. The commands (or **actions**) in
- 257 these menus all exist separately from the menus themselves and they can be
- 258 executed in alternate ways (such as keyboard shortcuts). The menu items (and

- even the menus themselves) can all be customized, but the following sections
- 260 describe the default configuration.

261 **4.3.1 File**

- 262 The File menu contains actions which are typically found in normal text editors
- and word processors. The actions to create new files, save files, and open
- 264 existing files are all present along with variations on these actions.
- 265 Actions for opening recent files, configuring the page setup, and printing are
- also present.

267 **4.3.2** Edit

- 268 The Edit menu also contains actions which are typically found in normal text
- 269 editors and word processors (such as **Undo**, **Redo**, **Cut**, **Copy**, and **Paste**).
- 270 However, there are also a number of more sophisticated actions available which
- are of use to programmers. For beginners, though, the typical actions will be
- 272 sufficient for most editing needs.

273 **4.3.3 Search**

- 274 The actions in the Search menu are used heavily, even by beginners. A good way
- 275 to get your mind around the search actions is to open the Search dialog window
- by selecting the **Find...** action (which is the first actions in the Search menu). A
- 277 **Search And Replace** dialog window will then appear which contains access to
- 278 most of the search actions.
- 279 At the top of this dialog window is a text area labeled **Search for** which allows
- 280 the user to enter text they would like to find. Immediately below it is a text area
- labeled **Replace with** which is for entering optional text that can be used to
- 282 replace text which is found during a search.
- 283 The column of radio buttons labeled **Search in** allows the user to search in a
- 284 **Selection** of text (which is text which has been highlighted), the **Current**
- 285 **Buffer** (which is the one that is currently active), **All buffers** (which means all
- opened files), or a whole **Directory** of files. The default is for a search to be
- 287 conducted in the current buffer and this is the mode that is used most often.
- 288 The column of check boxes labeled **Settings** allows the user to either **Keep or**
- 289 **hide the Search dialog window** after a search is performed, **Ignore the case**
- 290 of searched text, use an advanced search technique called a **Regular**
- 291 **expression** search (which is covered in another book), and to perform a
- 292 **HyperSearch** (which collects multiple search results in a text area).
- 293 The **Find** button performs a normal find operation. **Replace & Find** will replace
- 294 the previously found text with the contents of the **Replace with** text area and
- 295 perform another find operation. Replace All will find all occurrences of the

- 296 contents of the **Search for** text area and replace them with the contents of the
- 297 **Replace with** text area.

298 4.3.4 Markers, Folding, and View

299 These are advanced menus and they are described in later sections.

300 **4.3.5 Utilities**

- 301 The utilities menu contains a significant number of actions, some that are useful
- 302 to beginners and others that are meant for experts. The two actions that are
- 303 most useful to beginners are the **Buffer Options** actions and the **Global**
- 304 **Options** actions. The **Buffer Options** actions allows the currently selected
- 305 buffer to be customized and the **Global Options** actions brings up a rich dialog
- 306 window that allows numerous aspects of the MathRider application to be
- 307 configured.
- Feel free to explore these two actions in order to learn more about what they do.

309 **4.3.6 Macros**

310 This is an advanced menu and it is described in a later sections.

311 **4.3.7 Plugins**

- 312 Plugins are component-like pieces of software that are designed to provide an
- 313 application with extended capabilities and they are similar in concept to physical
- 314 world components. The tabs on the right side of the application which are
- labeled "GeoGebra", "Jung', "MathPiper", "MathPiperDocs", etc. are all plugins
- and they can be **opened** and **closed** by clicking on their **tabs**. **Feel free to close**
- 317 any of these plugins which may be opened if you are not currently using
- them. MathRider pPlugins are covered in more depth in a later section.

319 **4.3.8 Help**

- 320 The most important action in the **Help** menu is the **MathRider Help** action.
- 321 This action brings up a dialog window with contains documentation for the core
- 322 MathRider application along with documentation for each installed plugin.

323 4.4 The Toolbar

- 324 The **Toolbar** is located just beneath the menus near the top of the main window
- 325 and it contains a number of icon-based buttons. These buttons allow the user to
- 326 access the same actions which are accessible through the menus just by clicking
- on them. There is not room on the toolbar for all the actions in the menus to be

- 328 displayed, but the most common actions are present. The user also has the
- option of customizing the toolbar by using the **Utilities->Global Options->Tool**
- 330 **Bar** dialog.

331 **4.4.1 Undo And Redo**

- 332 The **Undo** button on the toolbar is able to undo any text was entered since the
- 333 current session of MathRider was launched. This is very handy for undoing
- mistakes or getting back text which was deleted. The **Redo** button can be used
- 335 if you have selected Undo too many times and you need to "undo" one ore more
- 336 Undo operations.

5 MathPiper: A Computer Algebra System For Beginners

- 338 Computer algebra systems are extremely powerful and very useful for solving
- 339 STEM-related problems. In fact, one of the reasons for creating MathRider was
- 340 to provide a vehicle for delivering a computer algebra system to as many people
- 341 as possible. If you like using a scientific calculator, you should love using a
- 342 computer algebra system!
- 343 At this point you may be asking yourself "if computer algebra systems are so
- 344 wonderful, why aren't more people using them?" One reason is that most
- 345 computer algebra systems are complex and difficult to learn. Another reason is
- that proprietary systems are very expensive and therefore beyond the reach of
- most people. Luckily, there are some open source computer algebra systems
- that are powerful enough to keep most people engaged for years, and yet simple
- 349 enough that even a beginner can start using them. MathPiper (which is based on
- a CAS called Yacas) is one of these simpler computer algebra systems and it is
- 351 the computer algebra system which is included by default with MathRider.
- 352 A significant part of this book is devoted to learning MathPiper and a good way
- 353 to start is by discussing the difference between numeric and symbolic
- 354 computations.

355

5.1 Numeric Vs. Symbolic Computations

- 356 A Computer Algebra System (CAS) is software which is capable of performing
- 357 both **numeric** and **symbolic** computations. **Numeric** computations are
- 358 performed exclusively with numerals and these are the type of computations that
- are performed by typical hand-held calculators.
- 360 **Symbolic** computations (which also called algebraic computations) relate "...to
- 361 the use of machines, such as computers, to manipulate mathematical equations
- and expressions in symbolic form, as opposed to manipulating the
- 363 approximations of specific numerical quantities represented by those symbols."
- 364 (http://en.wikipedia.org/wiki/Symbolic mathematics).
- 365 Since most people who read this document will probably be familiar with
- 366 performing numeric calculations as done on a scientific calculator, the next
- section shows how to use MathPiper as a scientific calculator. The section after
- that then shows how to use MathPiper as a symbolic calculator. Both sections
- 369 use the console interface to MathPiper. In MathRider, a console interface to any
- 370 plugin or application is a text-only **shell** or **command line** interface to it. This
- means that you type on the keyboard to send information to the console and it
- 372 prints text to send you information.

5.2 Using The MathPiper Console As A Numeric (Scientific) Calculator

- Open the MathPiper plugin by selecting the **MathPiper** tab in the lower left part
- of the MathRider application. The MathPiper **console** interface is a text area
- which is inside this plugin. Feel free to increase or decrease the size of the
- 377 console text area if you would like by dragging on the dotted lines which are at
- 378 the top side and right side of the console window.
- When the MathPiper console is first launched, it prints a welcome message and
- 380 then provides **In>** as an input prompt:
- 381 MathPiper version ".76x".
- 382 In>
- 383 Click to the right of the prompt in order to place the cursor there then type **2+2**
- 384 followed by **<shift><enter>** (or **<shift><return>** on a Macintosh):
- 385 In> 2+2
- 386 Result> 4
- 387 In>
- 388 When **<shift><enter>** was pressed, 2+2 was read into MathPiper for
- **evaluation** and **Result>** was printed followed by the result **4**. Another input
- 390 prompt was then displayed so that further input could be entered. This **input**,
- 391 **evaluation, output** process will continue as long as the console is running and
- 392 it is sometimes called a **Read, Eval, Print Loop** or **REPL**. In further examples,
- 393 the last **In>** prompt will not be shown to save space.
- 394 In addition to addition, MathPiper can also do subtraction, multiplication,
- 395 exponents, and division:
- **396** In> 5-2
- 397 Result> 3
- 398 In> 3*4
- 399 Result> 12
- 400 In> 2^3
- 401 Result> 8
- 402 In> 12/6
- 403 Result> 2
- 404 Notice that the multiplication symbol is an asterisk (*), the exponent symbol is a
- 405 caret (^), and the division symbol is a forward slash (/). These symbols (along
- 406 with addtion (+), subtraction (-), and ones we will talk about later) are called

- 407 **operators** because they tell MathPiper to perform an operation such as addition
- 408 or division.
- 409 MathPiper can also work with decimal numbers:

```
410
     In > .5 + 1.2
411
     Result> 1.7
412
    In> 3.7-2.6
413
    Result> 1.1
    In> 2.2*3.9
414
415
     Result> 8.58
416
    Tn > 2.2^3
417
     Result> 10.648
418
    In> 9.5/3.2
419
     Result> 9.5/3.2
```

- 420 In the last example, MathPiper returned the fraction unevaluated. This
- 421 sometimes happens due to MathPiper's symbolic nature, but a result in **numeric**
- 422 **form** can be obtained by using the **N() function**:

```
423 In> N(9.5/3.2)
424 Result> 2.96875
```

- 425 As can be seen here, when a result is given in numeric form, it means that it is
- 426 given as a decimal number. The N() function is discussed in the next section.

427 **5.2.1 Functions**

- 428 **N()** is an example of a **function**. A function can be thought of as a "black box"
- 429 which accepts input, processes the input, and returns a result. Each function
- has a name and in this case, the name of the function is **N** which stands for
- 431 "numeric". To the right of a function's name there is always a set of
- parentheses and information that is sent to the function is placed inside of
- 433 them. The purpose of the **N()** function is to make sure that the information that
- 434 is sent to it is processed numerically instead of symbolically. Functions are used
- by **evaluating** them and this happens when <shift><enter> is pressed. Another
- 436 name for evaluating a function is **calling** it.

437 5.2.1.1 The Sqrt() Square Root Function

- 438 The following example show the N() function being used with the square root
- 439 function **Sqrt()**:

- Notice that Sqrt(9) returned 3 as expected but Sqrt(8) returned Sqrt(8). We
- 447 needed to use the N() function to force the square root function to return a
- 448 numeric result. The reason that Sqrt(8) does not appear to have done anything
- 449 is because computer algebra systems like to work with expressions that are as
- exact as possible. In this case the **symbolic** value Sqrt(8) represents the number
- 451 that is the square root of 8 more accurately than any decimal number can.
- 452 For example, the following four decimal numbers all represent $\sqrt{8}$, but none of
- 453 them represent it more accurately than Sgrt(8) does:
- 454 2.828427125
- 455 2.82842712474619
- 456 2.82842712474619009760337744842
- 457 2.8284271247461900976033774484193961571393437507539
- 458 Whenever MathPiper returns a symbolic result and a numeric result is desired,
- 459 simply use the N() function to obtain one. The ability to work with symbolic
- values are one of the things that make computer algebra systems so powerful
- and they are discussed in more depth in later sections.

462 **5.2.1.2 The IsEven() Function**

- 463 Another often used function is **IsEven()**. The **IsEven()** function takes a number
- as input and returns **True** if the number is even and **False** if it is not even:

```
465 In> IsEven(4)
466 Result> True
467 In> IsEven(5)
```

- 468 Result> False
- 469 MathPiper has a large number of functions some of which are described in more
- 470 depth in the MathPiper Documentation section and the MathPiper Programming
- 471 Fundamentals section. A complete list of MathPiper's functions is
- 472 contained in the MathPiperDocs plugin and more of these functions will
- 473 **be discussed soon.**

474 5.2.2 Accessing Previous Input And Results

- 475 The MathPiper console is like a mini text editor which means you can copy text
- 476 from it, paste text into it, and edit existing text. You can also reevaluate previous
- 477 input by simply placing the cursor on the desired **In>** line and pressing
- 478 **<shift><enter>** on it again.
- 479 The console also keeps a history of all input lines that have been evaluated. If
- 480 the cursor is placed on any **In>** line, pressing **<ctrl><up arrow>** will display
- 481 each previous line of input that has been entered.
- 482 Finally, MathPiper associates the most recent computation result with the
- 483 percent (%) character. If you want to use the most recent result in a new
- 484 calculation, access it with this character:

```
485 In> 5*8

486 Result> 40

487 In> %

488 Result> 40

489 In> %*2

490 Result> 80
```

491 5.3 Saving And Restoring A Console Session

- 492 If you need to save the contents of a console session, you can copy and paste it
- 493 into a MathRider buffer and then save the buffer. You can also copy a console
- 494 session out of a previously saved buffer and paste it into the console for further
- 495 processing. Section 7 **Using MathRider As A Programmer's Text Editor**
- 496 discusses how to use the text editor that is built into MathRider.

497 5.3.1 Syntax Errors

- 498 An expression's **syntax** is related to whether it is **typed** correctly or not. If input
- 499 is sent to MathPiper which has one or more typing errors in it, MathPiper will
- return an error message which is meant to be helpful for locating the error. For
- 501 example, if a backwards slash (\) is entered for division instead of a forward slash
- 502 (/), MathPiper returns the following error message:

```
503 In> 12 \setminus 6
```

- 504 Error parsing expression, near token \
- 505 The easiest way to fix this problem is to press the **up arrow** key to display the
- 506 previously entered line in the console, change the \ to a /, and reevaluate the
- 507 expression.

- 508 This section provided a short introduction to using MathPiper as a numeric
- 509 calculator and the next section contains a short introduction to using MathPiper
- 510 as a symbolic calculator.

511 5.4 Using The MathPiper Console As A Symbolic Calculator

- 512 MathPiper is good at numeric computation, but it is great at symbolic
- 513 computation. If you have never used a system that can do symbolic computation,
- 514 you are in for a treat!
- 515 As a first example, lets try adding fractions (which are also called **rational**
- 516 **numbers**). Add $\frac{1}{2} + \frac{1}{3}$ in the MathPiper console:
- 517 In> 1/2 + 1/3
- 518 Result> 5/6
- 520 what a scientific calculator would return) MathPiper added these two rational
- numbers symbolically and returned $\frac{5}{6}$. If you want to work with this result
- 522 further, remember that it has also been stored in the % symbol:
- 523 In> %
- 524 Result> 5/6
- 525 Lets say that you would like to have MathPiper determine the numerator of this
- result. This can be done by using (or **calling**) the **Numerator()** function:
- 527 In> Numerator(%)
- 528 Result> 5

532

- 529 Unfortunately, the % symbol cannot be used to have MathPiper determine the
- 530 denominator of $\frac{5}{6}$ because it only holds the result of the most recent
- 531 calculation and $\frac{5}{6}$ was calculated two steps back.

5.4.1 Variables

- 533 What would be nice is if MathPiper provided a way to store **results** (which are
- also called **values**) in symbols that we choose instead of ones that it chooses.
- 535 Fortunately, this is exactly what it does! Symbols that can be associated with
- values are called **variables**. Variable names must start with an upper or lower
- case letter and be followed by zero or more upper case letters, lower case
- letters, or numbers. Examples of variable names include: 'a', 'b', 'x', 'y', 'answer',

- 539 'totalAmount', and 'loop6'.
- 540 The process of associating a value with a variable is called **assigning** or **binding**
- 541 the value to the variable and this consists of placing the name of a **variable** you
- would like to create on the **left** side of an assignment operator (:=) and an
- 543 **expression** on the **right** side of this operator. When the expression returns a
- value, the value is assigned (or bound to) to the variable.
- Lets recalculate $\frac{1}{2} + \frac{1}{3}$ but this time we will assign the result to the variable 'a':

```
546 In> a := 1/2 + 1/3
```

- 547 Result> 5/6
- 548 In> a
- 549 Result> 5/6
- 550 In> Numerator(a)
- 551 Result> 5
- 552 In> Denominator(a)
- 553 Result> 6
- In this example, the assignment operator (:=) was used to assign the result (or
- value) $\frac{5}{6}$ to the variable 'a'. When 'a' was evaluated by itself, the value it
- was bound to (in this case $\frac{5}{6}$) was returned. This value will stay bound to
- 557 the variable 'a' as long as MathPiper is running unless 'a' is cleared with the
- 558 **Clear()** function or 'a' has another value assigned to it. This is why we were able
- 559 to determine both the numerator and the denominator of the rational number
- assigned to 'a' using two functions in turn. (Note: there can be no spaces
- 561 **between the : and the =)**

562 5.4.1.1 Calculating With Unbound Variables

563 Here is an example which shows another value being assigned to 'a':

```
564 In> a := 9
```

- 565 Result> 9
- 566 In> a
- 567 Result> 9
- and the following example shows 'a' being cleared (or **unbound**) with the
- 569 **Clear()** function:
- 570 In> Clear(a)

```
571
     Result> True
572
     In> a
573
     Result> a
     Notice that the Clear() function returns 'True' as a result after it is finished to
574
     indicate that the variable that was sent to it was successfully cleared (or
575
     unbound). Many functions either return 'True' or 'False' to indicate whether or
576
     not the operation they performed succeeded. Also notice that unbound variables
577
578
     return themselves when they are evaluated. In this case, 'a' returned 'a'.
     Unbound variables may not appear to be very useful, but they provide the
579
     flexibility needed for computer algebra systems to perform symbolic calculations.
580
581
     In order to demonstrate this flexibility, lets first factor some numbers using the
582
     Factor() function:
583
     In> Factor(8)
584
     Result> 2^3
585
     In> Factor(14)
586
    Result> 2*7
587
     In> Factor(2343)
588
     Result> 3*11*71
     Now lets factor an expression that contains the unbound variable 'x':
589
590
     In> x
591
     Result> x
592
     In> IsBound(x)
593
     Result> False
594
     In> Factor (x^2 + 24*x + 80)
595
    Result> (x+20)*(x+4)
596
     In> Expand(%)
597
     Result> x^2+24*x+80
     Evaluating 'x' by itself shows that it does not have a value bound to it and this
598
599
     can also be determined by passing 'x' to the IsBound() function. IsBound()
     returns 'True' if a variable is bound to a value and 'False' if it is not.
600
     What is more interesting, however, are the results returned by Factor() and
601
     Expand(). Factor() is able to determine when expressions with unbound
602
603
     variables are sent to it and it uses the rules of algebra to manipulate them into
     factored form. The Expand() function was then able to take the factored
604
     expression (x+20)(x+4) and manipulate it until it was expanded. One way to
605
     remember what the functions Factor() and Expand() do is to look at the second
606
```

- letters of their names. The 'a' in Factor can be thought of as adding
- parentheses to an expression and the 'x' in **Expand** can be thought of **xing** out
- or removing parentheses from an expression.

610 5.4.1.2 Variable And Function Names Are Case Sensitive

- MathPiper variables are **case sensitive**. This means that MathPiper takes into
- account the **case** of each letter in a variable name when it is deciding if two or
- 613 more variable names are the same variable or not. For example, the variable
- name **Box** and the variable name **box** are not the same variable because the first
- variable name starts with an upper case 'B' and the second variable name starts
- 616 with a lower case 'b':

```
617 In> Box := 1
618 Result> 1
619 In> box := 2
620 Result> 2
621 In> Box
622 Result> 1
623 In> box
624 Result> 2
```

625 **5.4.1.3** Using More Than One Variable

Programs are able to have more than 1 variable and here is a more sophisticated example which uses 3 variables:

```
628 a := 2
629 Result> 2
630 b := 3
631 Result> 3
632 a + b
633 Result> 5
634 answer := a + b
635 Result> 5
636 answer
637 Result> 5
```

- 638 The part of an expression that is on the **right side** of an assignment operator is
- 639 always evaluated first and the result is then assigned to the variable that is on

- 640 the **left side** of the operator.
- Now that you have seen how to use the MathPiper console as both a **symbolic**
- and a **numeric** calculator, our next step is to take a closer look at the functions
- 643 which are included with MathPiper. As you will soon discover, MathPiper
- 644 contains an amazing number of functions which deal with a wide range of
- 645 mathematics.

646 **5.5 Exercises**

- Use the MathPiper console which is at the bottom of the MathRider application
- 648 to complete the following exercises.

649 **5.5.1 Exercise 1**

- 650 Carefully read all of section 5. Evaluate each one of the examples in
- 651 section 5 in the MathPiper console and verify that the results match the
- 652 ones in the book.

653 **5.5.2 Exercise 2**

- 654 Answer each one of the following questions:
- 655 a) What is the purpose of the N() function?
- 656 b) What is a variable?
- 657 c) Are the variables 'x' and 'X' the same variable?
- 658 d) What is the difference between a bound variable and an unbound variable?
- 659 e) How can you tell if a variable is bound or not?
- 660 f) How can a variable be bound to a value?
- 661 g) How can a variable be unbound from a value?
- 662 h) What does the % character do?

663 **5.5.3 Exercise 3**

664 Perform the following calculation:

$$\frac{1}{4} + \frac{3}{8} - \frac{7}{16}$$

665 **5.5.4 Exercise 4**

- 666 a) Assign the variable **answer** to the result of the calculation $\frac{1}{5} + \frac{7}{4} + \frac{15}{16}$
- 667 using the following line of code:
- 668 In> answer := 1/5 + 7/4 + 15/16
- 669 b) Use the Numerator() function to calculate the numerator of answer.
- 670 c) Use the Denominator() function to calculate the denominator of **answer**.
- 671 d) Use the N() function to calculate the numeric value of answer.
- 672 e) Use the Clear() function to unbind the variable answer and verify that
- 673 answer is unbound by executing the following code and by using the
- 674 IsBound() function:
- 675 In> answer

676 **5.5.5 Exercise 5**

- 677 Assign $\frac{1}{4}$ to variable **x**, $\frac{3}{8}$ to variable **y**, and $\frac{7}{16}$ to variable **z** using the
- 678 := operator. Then perform the following calculations:
- 679 a)
- 680 In> x
- 681 b)
- 682 In> y
- 683 c)
- 684 In> z
- 685 d)
- 686 In> x + y
- 687 e)
- 688 In> x + z
- 689 f)
- 690 In> x + y + z

691 6 The MathPiper Documentation Plugin

- 692 MathPiper has a significant amount of reference documentation written for it
- and this documentation has been placed into a plugin called **MathPiperDocs** in
- order to make it easier to navigate. The MathPiperDocs plugin is available in a
- 695 tab called "MathPiperDocs" which is near the right side of the MathRider
- 696 application. Click on this tab to open the plugin and click on it again to close it.
- 697 The left side of the MathPiperDocs window contains the names of all the
- 698 functions that come with MathPiper and the right side of the window contains a
- 699 mini-browser that can be used to navigate the documentation.

6.1 Function List

700

- 701 MathPiper's functions are divided into two main categories called **user** functions
- and **programmer functions**. In general, the **user functions** are used for
- 703 solving problems in the MathPiper console or with short programs and the
- 704 **programmer functions** are used for longer programs. However, users will
- often use some of the programmer functions and programmers will use the user
- 706 functions as needed.
- 707 Both the user and programmer function names have been placed into a "tree" on
- 708 the left side of the MathPiperDocs window to allow for easy navigation. The
- 709 branches of the function tree can be opened and closed by clicking on the small
- 710 "circle with a line attached to it" symbol which is to the left of each branch. Both
- 711 the user and programmer branches have the functions they contain organized
- 712 into categories and the **top category in each branch** lists all the functions in
- 713 the branch in **alphabetical order** for guick access. Clicking on a function will
- 714 bring up documentation about it in the browser window and selecting the
- 715 **Collapse** button at the top of the plugin will collapse the tree.
- 716 Don't be intimidated by the large number of categories and functions
- 717 **that are in the function tree!** Most MathRider beginners will not know what
- 718 most of them mean, and some will not know what any of them mean. Part of the
- 719 benefit Mathrider provides is exposing the user to the existence of these
- 720 categories and functions. The more you use MathRider, the more you will learn
- about these categories and functions and someday you may even get to the point
- 722 where you understand all of them. This book is designed to show newbies how to
- begin using these functions using a gentle step-by-step approach.

724 6.2 Mini Web Browser Interface

- 725 MathPiper's reference documentation is in HTML (or web page) format and so
- 726 the right side of the plugin contains a mini web browser that can be used to
- 727 navigate through these pages. The browser's **home page** contains links to the
- main parts of the MathPiper documentation. As links are selected, the **Back** and

- 729 **Forward** buttons in the upper right corner of the plugin allow the user to move
- 730 backward and forward through previously visited pages and the **Home** button
- 731 navigates back to the home page.
- 732 The function names in the function tree all point to sections in the HTML
- 733 documentation so the user can access function information either by navigating
- to it with the browser or jumping directly to it with the function tree.

735 **6.3 Exercises**

736 **6.3.1 Exercise 1**

- 737 Carefully read all of section 6. Locate the N(), IsEven(), IsOdd(),
- 738 Clear(), IsBound(), Numerator(), Denominator(), and Factor() functions in
- 739 the All Functions section of the MathPiperDocs plugin and read the
- 740 information that is available on them. List the one line descriptions
- 741 which are at the top of the documentation for each of these functions.

742 **6.3.2 Exercise 2**

- 743 Locate the N(), IsEven(), IsOdd(), Clear(), IsBound(), Numerator(),
- 744 Denominator(), and Factor() functions in the User Functions section of the
- 745 MathPiperDocs plugin and list which category each function is contained in.
- 746 Don't include the Alphabetical or Built In categories in your search. For
- 747 example, the N() function is in the Numbers (Operations) category.

748 7 Using MathRider As A Programmer's Text Editor

- 749 We have covered some of MathRider's mathematics capabilities and this section
- 750 discusses some of its programming capabilities. As indicated in a previous
- 751 section, MathRider is built on top of a programmer's text editor but what wasn't
- discussed was what an amazing and powerful tool a programmer's text editor is.
- 753 Computer programmers are among the most intelligent and productive people in
- 754 the world and most of their work is done using a programmer's text editor (or
- 755 something similar to one). Programmers have designed programmer's text
- 756 editors to be super-tools which can help them maximize their personal
- 757 productivity and these tools have all kinds of capabilities that most people would
- 758 not even suspect they contained.
- 759 Even though this book only covers a small part of the editing capabilities that
- 760 MathRider has, what is covered will enable the user to begin writing useful
- 761 programs.

762

7.1 Creating, Opening, Saving, And Closing Text Files

- 763 A good way to begin learning how to use MathRider's text editing capabilities is
- by creating, opening, and saving text files. A text file can be created either by
- 765 selecting **File->New** from the menu bar or by selecting the icon for this
- operation on the tool bar. When a new file is created, an empty text area is
- 767 created for it along with a new tab named **Untitled**.
- 768 The file can be saved by selecting **File->Save** from the menu bar or by selecting
- 769 the **Save** icon in the tool bar. The first time a file is saved, MathRider will ask
- the user what it should be named and it will also provide a file system navigation
- 771 window to determine where it should be placed. After the file has been named
- and saved, its name will be shown in the tab that previously displayed **Untitled**.
- 773 A file can be closed by selecting **File->Close** from the menu bar and it can be
- opened by selecting **File->Open**.

775 **7.2 Editing Files**

- 776 If you know how to use a word processor, then it should be fairly easy for you to
- 777 learn how to use MathRider as a text editor. Text can be selected by dragging
- 778 the mouse pointer across it and it can be cut or copied by using actions in the
- 779 **Edit** menu (or by using **<Ctrl>x** and **<Ctrl>c**). Pasting text can be done using
- 780 the Edit menu actions or by pressing **<Ctrl>v**.

781 7.3 *File Modes*

782 Text file names are suppose to have a file extension which indicates what type of

- 783 file it is. For example, test.**txt** is a generic text file, test.**bat** is a Windows batch
- 784 file, and test.sh is a Unix/Linux shell script (unfortunately, Windows is usually
- 785 configured to hide file extensions, but viewing a file's properties by right-clicking
- 786 on it will show this information.).
- 787 MathRider uses a file's extension type to set its text area into a customized
- 788 **mode** which highlights various parts of its contents. For example, MathRider
- 789 worksheet files have a .mrw extension and MathRider knows what colors to
- 790 highlight the various parts of a .mrw file in.

791 7.4 Learning How To Type Properly Is An Excellent Investment Of Your

- 792 **Time**
- 793 This is a good place in the document to mention that learning how to type
- 794 properly is an investment that will pay back dividends throughout your whole
- 795 life. Almost any work you do on a computer (including programming) will be
- 796 done *much* faster and with less errors if you know how to type properly. Here is
- 797 what Steve Yegge has to say about this subject:
- 798 "If you are a programmer, or an IT professional working with computers in *any*
- 799 capacity, **you need to learn to type!** I don't know how to put it any more clearly
- 800 than that."
- 801 A good way to learn how to type is to locate a free "learn how to type" program
- 802 on the web and use it.

803 **7.5 Exercises**

804 **7.5.1 Exercise 1**

- 805 Carefully read all of section 7. Create a text file called
- 806 "my text file.txt" and place a few sentences in it. Save the text file
- 807 somewhere on your hard drive then close it. Now, open the text file again
- 808 using **File->Open** and verify that what you typed is still in the file.

8 MathRider Worksheet Files

- 810 While MathRider's ability to execute code inside a console provides a significant
- amount of power to the user, most of MathRider's power is derived from
- worksheets. MathRider worksheets are text files which have a .mrw extension
- and are able to execute multiple types of code in a single text area. The
- 814 worksheet demo 1.mrw file (which is preloaded in the MathRider environment
- when it is first launched) demonstrates how a worksheet is able to execute
- 816 multiple types of code in what are called **code folds**.

817 **8.1 Code Folds**

- 818 Code folds are named sections inside a MathRider worksheet which contain
- source code that can be executed by placing the cursor inside of it and pressing
- 820 **<shift><Enter>**. A fold always begins with a **start tag**, which starts with a
- 821 percent symbol (%) followed by the **name of the fold type** (like this:
- 822 **%<foldtype>**). The end of a fold is marked by an **end tag** which looks like
- 823 %/<foldtype>. The only difference between a fold's start tag and its end tag is
- 824 that the end tag has a slash (/) after the %.
- 825 For example, here is a MathPiper fold which will print the result of 2 + 3 to the
- 826 MathPiper console (Note: the semicolon ';' which is at the end of the line of
- 827 **code is required**):
- 828 %mathpiper
- $829 \quad 2 + 3;$
- 830 %/mathpiper
- The **output** generated by a fold (called the **parent fold**) is wrapped in a **new**
- fold (called a child fold) which is indented and placed just below the parent.
- 833 This can be seen when the above fold is executed by pressing **<shift><enter>**
- 834 inside of it:
- 835 %mathpiper
- $836 \quad 2 + 3;$
- 837 %/mathpiper
- %output, preserve="false"
- 839 Result: 5
- 840 . %/output
- The most common type of output fold is **%output** and by default folds of type

- 842 %output have their **preserve property** set to **false**. This tells MathRider to
- 843 overwrite the %output fold with a new version during the next execution of its
- parent. If preserve is set to **true**, the fold will not be overwritten and a new fold
- will be created instead.
- 846 There are other kinds of child folds, but in the rest of this document they will all
- 847 be referred to in general as "output" folds.

848 **8.1.1 The title Attribute**

- 849 Folds can also have what is called a "**title attribute**" placed after the start tag
- which describes what the fold contains. For example, the following %mathpiper
- 851 fold has a title attribute which indicates that the fold adds two number together:
- 852 %mathpiper,title="Add two numbers together."
- $853 \quad 2 + 3;$
- 854 %/mathpiper
- 855 The title attribute is added to the start tag of a fold by placing a comma after the
- 856 fold's type name and then adding the text **title="<text>"** after the comma.
- 857 (Note: no spaces can be present before or after the comma (,) or the
- 858 **equals sign (=)**).

859 8.2 Automatically Inserting Folds & Removing Unpreserved Folds

- 860 Typing the top and bottom fold lines (for example:
- 861 %mathpiper
- 862 %/mathpiper
- 863 can be tedious and MathRider has a way to automatically insert them. Place the
- 864 cursor at the beginning of a blank line in a .mrw worksheet file where you would
- like a fold inserted and then **press the right mouse button**.
- 866 A popup menu will be displayed and at the top of this menu are items which read
- 867 "Insert MathPiper Fold", "Insert Group Fold", etc. If you select one of these
- 868 menu items, an empty code fold of the proper type will automatically be inserted
- 869 into the .mrw file at the position of the cursor.
- 870 This popup menu also has a menu item called "**Remove Unpreserved Folds**". If
- 871 this menu item is selected, all folds which have a "preserve="false"" property
- will be removed.

8.3 Placing Text Outside Of A Fold

874 Text can also be placed outside of a fold like the following example shows:

```
875
    Text can be placed above folds like this.
876
    text text text text
877
    text text text text
878
    %mathpiper, title="Fold 1"
879
    2 + 3;
880
    %/mathpiper
881
    Text can be placed between folds like this.
882
    text text text text
883
    text text text text
884
    %mathpiper, title="Fold 2"
885
    3 + 4;
886
    %/mathpiper
887
    Text can be placed between folds like this.
888
    text text text text
889
    text text text text
    Placing text outside a fold is useful for describing what is being done in certain
890
    folds and it is also good for saving work that has been done in the MathPiper
891
    console.
892
```

8.4 Exercises

- 894 A MathRider worksheet file called "newbies_book_examples_1.mrw" can be
- 895 obtained from this website:
- 896 https://mathrider.dev.java.net/source/browse/mathrider/trunk/src/doc/newbies-bo
- 897 <u>ok/examples/proposed/misc/newbies book examples 1.mrw</u>
- 898 It contains a number of %mathpiper folds which contain code examples from the
- 899 previous sections of this book. Notice that all of the lines of code have a
- 900 semicolon (;) placed after them. The reason this is needed is explained in a later
- 901 section.

- 902 Download this worksheet file to your computer from the section on this website
- 903 that contains the highest revision number and then open it in MathRider. Then,
- 904 use the worksheet to do the following exercises.

905 **8.4.1 Exercise 1**

- 906 Carefully read all of section 8. Execute folds 1-8 in the top section of
- 907 the worksheet by placing the cursor inside of the fold and then pressing
- 908 <shift><enter> on the keyboard.

909 **8.4.2 Exercise 2**

- 910 The code in folds 9 and 10 have errors in them. Fix the errors and then
- 911 execute the folds again.

912 **8.4.3 Exercise 3**

913 Use the empty fold 11 to calculate the expression 100 - 23;

914 **8.4.4 Exercise 4**

- 915 Perform the following calculations by creating new folds at the bottom of
- 916 the worksheet (using the right-click popup menu) and placing each
- 917 calculation into its own fold:
- 918 a) 2*7 + 3
- 919 b) 18/3
- 920 c) 234238342 + 2038408203
- 921 d) 324802984 * 2308098234
- 922 e) Factor the result which was calculated in d).

9 MathPiper Programming Fundamentals

- 924 The MathPiper language consists of **expressions** and an expression consists of
- one or more **symbols** which represent **values**, **operators**, **variables**, and
- 926 **functions**. In this section expressions are explained along with the values,
- 927 operators, variables, and functions they consist of.

9.1 Values and Expressions

- 929 A **value** is a single symbol or a group of symbols which represent an idea. For
- 930 example, the value:
- 931 3

923

928

- 932 represents the number three, the value:
- 933 0.5
- 934 represents the number one half, and the value:
- "Mathematics is powerful!"
- 936 represents an English sentence.
- 937 Expressions can be created by using **values** and **operators** as building blocks.
- 938 The following are examples of simple expressions which have been created this
- 939 way:
- 940 3
- 941 2 + 3
- $5 + 6*21/18 2^3$
- In MathPiper, **expressions** can be **evaluated** which means that they can be
- 944 transformed into a **result value** by predefined rules. For example, when the
- expression 2 + 3 is evaluated, the result value that is produced is 5:
- 946 In> 2 + 3
- 947 Result> 5

948 **9.2 Operators**

- In the above expressions, the characters +, -, *, /, $^{\circ}$ are called **operators** and
- 950 their purpose is to tell MathPiper what **operations** to perform on the **values** in
- an **expression**. For example, in the expression **2 + 3**, the **addition** operator **+**
- 952 tells MathPiper to add the integer **2** to the integer **3** and return the result.
- 953 The **subtraction** operator is **-**, the **multiplication** operator is *****, **/** is the
- 954 **division** operator, % is the **remainder** operator (which is also used as the

- "result of the last calculation" symbol), and ^ is the **exponent** operator.
- 956 MathPiper has more operators in addition to these and some of them will be
- 957 covered later.
- 958 The following examples show the -, *, /,%, and $^$ operators being used:

```
959
     In>5-2
960
    Result> 3
961
    In> 3*4
962
    Result> 12
963
    In> 30/3
964
    Result> 10
965
    In> 8%5
966
    Result> 3
967
    In> 2^3
968
    Result> 8
```

- 969 The character can also be used to indicate a negative number:
- 970 In> -3 971 Result> -3
- 972 Subtracting a negative number results in a positive number (Note: there must be
- 973 a space between the two negative signs):
- 974 In> -3 975 Result> 3
- 976 In MathPiper, **operators** are symbols (or groups of symbols) which are
- 977 implemented with **functions**. One can either call the function that an operator
- 978 represents directly or use the operator to call the function indirectly. However,
- 979 using operators requires less typing and they often make a program easier to
- 980 read.

9.3 Operator Precedence

- 982 When expressions contain more than one operator, MathPiper uses a set of rules
- 983 called **operator precedence** to determine the order in which the operators are
- applied to the values in the expression. Operator precedence is also referred to
- 985 as the **order of operations**. Operators with higher precedence are evaluated
- 986 before operators with lower precedence. The following table shows a subset of
- 987 MathPiper's operator precedence rules with higher precedence operators being
- 988 placed higher in the table:

- 989 ^ Exponents are evaluated right to left.
- *,%,/ Then multiplication, remainder, and division operations are evaluated left to right.
- 992 +, Finally, addition and subtraction are evaluated left to right.
- Lets manually apply these precedence rules to the multi-operator expression we used earlier. Here is the expression in source code form:

996 And here it is in traditional form:

$$5+6*\frac{21}{18}-2^3$$

- 997 According to the precedence rules, this is the order in which MathPiper
- 998 evaluates the operations in this expression:

```
999 5 + 6*21/18 - 2<sup>3</sup>

1000 5 + 6*21/18 - 8

1001 5 + 126/18 - 8

1002 5 + 7 - 8

1003 12 - 8

1004 4
```

- 1005 Starting with the first expression, MathPiper evaluates the ^ operator first which
- 1006 results in the 8 in the expression below it. In the second expression, the *
- operator is executed next, and so on. The last expression shows that the final
- result after all of the operators have been evaluated is **4**.

9.4 Changing The Order Of Operations In An Expression

- 1010 The default order of operations for an expression can be changed by grouping
- various parts of the expression within parentheses (). Parentheses force the
- 1012 code that is placed inside of them to be evaluated before any other operators are
- 1013 evaluated. For example, the expression 2 + 4*5 evaluates to 22 using the
- 1014 default precedence rules:

```
1015 In> 2 + 4*5 1016 Result> 22
```

- 1017 If parentheses are placed around 2 + 4, however, the addition operator is forced
- 1018 to be evaluated before the multiplication operator and the result is 30:

```
1019 In> (2 + 4)*5 1020 Result> 30
```

- 1021 Parentheses can also be nested and nested parentheses are evaluated from the
- 1022 most deeply nested parentheses outward:
- 1023 In> ((2 + 4)*3)*5
- 1024 Result> 90

- 1025 (Note: precedence adjusting parentheses are different from the parentheses that
- 1026 are used to call functions.)
- 1027 Since parentheses are evaluated before any other operators, they are placed at
- 1028 the top of the precedence table:
- 1029 () Parentheses are evaluated from the inside out.
- 1030 ^ Then exponents are evaluated right to left.
- *,%,/ Then multiplication, remainder, and division operations are evaluated left to right.
- +, Finally, addition and subtraction are evaluated left to right.

9.5 Functions & Function Names

- 1035 In programming, **functions** are named blocks of code that can be executed one
- or more times by being **called** from other parts of the same program or called
- 1037 from other programs. Functions can have values passed to them from the
- calling code and they **always return a value** back to the calling code when they
- are finished executing. An example of a function is the **IsEven()** function which
- 1040 was discussed in an previous section.
- 1041 Functions are one way that MathPiper enables code to be reused. Most
- programming languages allow code to be reused in this way, although in other
- languages these named blocks of code are sometimes called **subroutines**.
- 1044 **procedures**, or **methods**.
- 1045 The functions that come with MathPiper have names which consist of either a
- single word (such as **Sum()**) or multiple words that have been put together to
- 1047 form a compound word (such as **IsBound()**). All letters in the names of
- 1048 functions which come with MathPiper are lower case except the beginning letter
- 1049 in each word, which are upper case.

1050 9.6 Functions That Produce Side Effects

- 1051 Most functions are executed to obtain the **results** they produce but some
- 1052 functions are executed in order to have them perform work that is not in the
- 1053 **form of a result**. Functions that perform work that is not in the form of a result
- are said to produce **side effects**. Side effects include many forms of work such
- as sending information to the user, opening files, and changing values in the
- 1056 computer's memory.
- 1057 When a function produces a side effect which sends information to the user, this
- information has the words **Side Effects:** placed before it in the output instead of
- the word **Result:**. The **Echo()** and **Write()** functions are examples of functions
- that produce side effects and they are covered in the next section.

1061 9.6.1 Printing Related Functions: Echo(), Write(), And Newline()

- 1062 The printing related functions send text information to the user and this is
- 1063 usually referred to as "printing" in this document. However, it may also be called
- 1064 "echoing" and "writing".

1065 **9.6.1.1 Echo()**

- 1066 The **Echo()** function takes one expression (or multiple expressions separated by
- 1067 commas) evaluates each expression, and then prints the results as side effect
- 1068 output. The following examples illustrate this:
- 1069 In> Echo(1)
- 1070 Result> True
- 1071 Side Effects>
- 1072 1
- 1073 In this example, the number 1 was passed to the Echo() function, the number
- 1074 was evaluated (all numbers evaluate to themselves), and the result of the
- 1075 evaluation was then printed as a side effect. Notice that Echo() also returned a
- 1076 **result**. In MathPiper, all functions return a result, but functions whose main
- purpose is to produce a side effect usually just return a result of **True** if the side
- 1078 effect succeeded or False if it failed. In this case, Echo() returned a result of
- 1079 **True** because it was able to successfully print a 1 as its side effect.
- 1080 The next example shows multiple expressions being sent to Echo() (notice that
- 1081 the expressions are separated by commas):

```
1082 In> Echo (1, 1+2, 2*3)
```

- 1083 Result> True
- 1084 Side Effects>
- 1085 1 3 6

```
The expressions were each evaluated and their results were returned (separated
1086
      by spaces) as side effect output. If it is desired that commas be printed between
1087
      the numbers in the output, simply place three commas between the expressions
1088
1089
      that are passed to Echo():
1090
      In> Echo (1, 1, 1+2, 1, 2*3)
1091
      Result> True
1092
      Side Effects>
1093
      1,3,6
1094
      Each time an Echo() function is executed, it always forces the display to drop
      down to the next line after it is finished. This can be seen in the following
1095
      program which is similar to the previous one except it uses a separate Echo()
1096
1097
      function to display each expression:
1098
      %mathpiper
1099
      Echo (1);
1100
      Echo (1+2);
1101
      Echo (2*3);
1102
      %/mathpiper
1103
          %output, preserve="false"
1104
            Result: True
1105
1106
            Side Effects:
1107
             1
1108
             3
1109
             6
1110
          %/output
      Notice how the 1, the 3, and the 6 are each on their own line.
1111
1112
      Now that we have seen how Echo() works, lets use it to do something useful. If
1113
      more than one expression is evaluated in a %mathpiper fold, only the result from
      the last expression that was evaluated (which is usually the bottommost
1114
      expression) is displayed:
1115
1116
      %mathpiper
1117
      a := 1;
      b := 2;
1118
1119
      c := 3;
1120
      %/mathpiper
```

```
1121 %output,preserve="false"
1122 Result: 3
1123 . %/output
```

- In MathPiper, programs are executed one line at a time, starting at the topmost
- line of code and working downwards from there. In this example, the line a := 1;
- is executed first, then the line b := 2; is executed, and so on. Notice, however,
- that even though we wanted to see what was in all three variables, only the
- 1128 content of the last variable was displayed.
- 1129 The following example shows how Echo() can be used to display the contents of
- 1130 all three variables:

```
1131
      %mathpiper
1132
      a := 1;
1133
      Echo(a);
1134
      b := 2;
1135
      Echo(b);
1136
      c := 3;
1137
      Echo(C);
1138
      %/mathpiper
1139
          %output,preserve="false"
1140
             Result: True
1141
1142
             Side Effects:
1143
             1
1144
             2
1145
             3
1146
          %/output
```

1147 9.6.1.2 Echo Functions Are Useful For "Debugging" Programs

- 1148 The errors that are in a program are often called "bugs". This name came from
- the days when computers were the size of large rooms and were made using
- electromechanical parts. Periodically, bugs would crawl into the machines and
- interfere with its moving mechanical parts and this would cause the machine to
- malfunction. The bugs needed to be located and removed before the machine
- 1153 would run properly again.
- Of course, even back then most program errors were produced by programmers
- entering wrong programs or entering programs wrong, but they liked to say that
- all of the errors were caused by bugs and not by themselves! The process of
- fixing errors in a program became known as **debugging** and the names "bugs"

- and "debugging" are still used by programmers today.
- One of the standard ways to locate bugs in a program is to place **Echo()** function
- calls in the code at strategic places which print the contents of variables and
- 1161 **display messages**. These Echo() functions will enable you to see what your
- program is doing while it is running. After you have found and fixed the bugs in
- 1163 your program, you can remove the debugging Echo() function calls or comment
- them out if you think they may be needed later.

1165 **9.6.1.3 Write()**

- 1166 The **Write()** function is similar to the Echo() function except it does not
- automatically drop the display down to the next line after it finishes executing:

```
1168
      %mathpiper
1169
      Write(1,,);
1170
      Write (1+2,,);
1171
      Echo (2*3);
1172
      %/mathpiper
1173
           %output, preserve="false"
1174
             Result: True
1175
1176
             Side Effects:
1177
             1,3,6
          %/output
1178
```

- 1179 Write() and Echo() have other differences besides the one discussed here and
- more information about them can be found in the documentation for these
- 1181 functions.

1182 **9.6.1.4 NewLine()**

- 1183 The **NewLine()** function simply prints a blank line in the side effects output. It
- is useful for placing vertical space between printed lines:

```
1185 %mathpiper

1186 a := 1;

1187 Echo(a);

1188 NewLine();

1189 b := 2;

1190 Echo(b);
```

```
1191
      NewLine();
1192
      c := 3;
1193
      Echo(C);
1194
      %/mathpiper
1195
           %output, preserve="false"
1196
             Result: True
1197
1198
             Side Effects:
1199
1200
             2
1201
             3
1202
          %/output
```

9.7 Expressions Are Separated By Semicolons

- 1204 As discussed earlier, all of the expressions that are inside of a **%mathpiper** fold
- 1205 must have a semicolon (;) after them. However, the expressions executed in the
- 1206 **MathPiper console** did not have a semicolon after them. MathPiper actually
- 1207 requires that all expressions end with a semicolon, but one does not need to add
- 1208 a semicolon to an expression which is typed into the MathPiper console **because**
- 1209 **the console adds it automatically** when the expression is executed.

1210 9.7.1 Placing More Than One Expression On A Line In A Fold

- 1211 All the previous code examples have had each of their expressions on a separate
- line, but multiple expressions can also be placed on a single line because the
- semicolons tell MathPiper where one expression ends and the next one begins:

```
1214
      %mathpiper
1215
      a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c);
1216
      %/mathpiper
1217
          %output, preserve="false"
1218
            Result: True
1219
1220
            Side Effects:
1221
            1
1222
            2
1223
            3
1224
          %/output
```

- 1225 The spaces that are in the code of this example are used to make the code more
- 1226 readable. Any spaces that are present within any expressions or between them
- are ignored by MathPiper and if we remove the spaces from the previous code,
- 1228 the output remains the same:

```
1229
      %mathpiper
1230
      a:=1; Echo (a); b:=2; Echo (b); c:=3; Echo (c);
1231
      %/mathpiper
1232
           %output,preserve="false"
1233
             Result: True
1234
1235
             Side Effects:
1236
1237
             2
1238
             3
1239
          %/output
```

1240 9.7.2 Placing Multiple Expressions In A Code Block

- 1241 A **code block** (which is also called a **compound expression**) consists of one or
- more expressions which are separated by semicolons and placed within an open
- bracket ([) and close bracket (]) pair. When a code block is evaluated, each
- 1244 expression in the block will be executed from left to right. The following
- 1245 example shows expressions being executed within of a code block inside the
- 1246 MathPiper console:

```
1247 In> [a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c);]
1248 Result> True
1249 Side Effects>
1250 1
1251 2
1252 3
```

- Notice that all of the expressions were executed and 1-3 was printed as a side
- effect. Code blocks always return the result of the last expression executed
- as the result of the whole block. In this case, **True** was returned as the result
- because the last **Echo(c)** function returned **True**. If we place **another**
- expression after the Echo(c) function, however, the block will execute this
- new expression last and its result will be the one returned by the block:

```
1259  In> [a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c); 2 + 2;]
1260  Result> 4
1261  Side Effects>
1262  1
```

```
1263 2
1264 3
```

1265 Finally, code blocks can have their contents placed on separate lines if desired:

```
1266
      %mathpiper
1267
      [
1268
          a := 1;
1269
1270
          Echo(a);
1271
1272
          b := 2;
1273
1274
          Echo(b);
1275
1276
          c := 3;
1277
1278
          Echo(c);
1279
      ];
1280
      %/mathpiper
1281
           %output, preserve="false"
1282
             Result: True
1283
1284
             Side Effects:
1285
             1
1286
             2
1287
             3
1288
     . %/output
```

- 1289 Code blocks are very powerful and we will be discussing them further in later 1290 sections.
- 1291 9.7.2.1 Automatic Bracket, Parentheses, And Brace Match Indicating
- 1292 In programming, most open brackets '[' have a close bracket ']', most open
- parentheses '(' have a close parentheses ')', and most open braces '{' have a
- 1294 close brace '}'. It is often difficult to make sure that each "open" character has a
- matching "close" character and if any of these characters don't have a match,
- then an error will be produced.
- 1297 Thankfully, most programming text editors have a character match indicating
- 1298 tool that will help locate problems. To try this tool, paste the following code into
- 1299 a .mrw file and following the directions that are present in its comments:

```
1300 %mathpiper
```

1301 /*

```
1302
          Copy this code into a .mrw file. Then, place the cursor
1303
          to the immediate right of any {, }, [, ], (, or ) character.
1304
          You should notice that the match to this character is
1305
          indicated by a rectangle being drawing around it.
1306
      * /
1307
     list := \{1, 2, 3\};
1308
      Γ
1309
          Echo("Hello");
1310
          Echo(list);
1311
     1;
1312
      %/mathpiper
```

1313 **9.8 Strings**

A **string** is a **value** that is used to hold text-based information. The typical expression that is used to create a string consists of **text which is enclosed**within double quotes. Strings can be assigned to variables just like numbers can and strings can also be displayed using the Echo() function. The following program assigns a string value to the variable 'a' and then echos it to the user:

```
1319
      %mathpiper
1320
     a := "Hello, I am a string.";
1321
     Echo(a);
1322
      %/mathpiper
1323
          %output, preserve="false"
1324
            Result: True
1325
1326
            Side Effects:
1327
            Hello, I am a string.
1328
     . %/output
```

1329 9.8.1 The MathPiper Console and MathPiper Folds Can Access The Same 1330 Variables

- 1331 A useful aspect of using MathPiper inside of MathRider is that variables that are
- assigned inside of a **%mathpiper fold** are accessible inside of the **MathPiper**
- 1333 console and variables that are assigned inside of the MathPiper console are
- available inside of **%mathpiper folds**. For example, after the above fold is
- executed, the string that has been bound to variable 'a' can be displayed in the
- 1336 MathPiper console:

```
1337 In> a
1338 Result> "Hello, I am a string."
```

1339 9.8.2 Using Strings To Make Echo's Output Easier To Read

- 1340 When the Echo() function is used to print the values of multiple variables, it is
- often helpful to print some information next to each variable so that it is easier to
- 1342 determine which value came from which Echo() function in the code. The
- 1343 following program prints the name of the variable that each value came from
- 1344 next to it in the side effects output:

```
1345
     %mathpiper
1346
     a := 1;
1347
     Echo("Variable a: ", a);
1348
     b := 2;
1349
     Echo("Variable b: ", b);
1350 c := 3;
1351
    Echo("Variable c: ", c);
1352
    %/mathpiper
1353
          %output, preserve="false"
1354
           Result: True
1355
1356
           Side Effects:
1357
           Variable a: 1
1358
           Variable b: 2
1359
           Variable c: 3
1360
    . %/output
```

1361 **9.8.2.1 Combining Strings With The : Operator**

- 1362 If you need to combine two or more strings into one string, you can use the:
- 1363 operator like this:

```
1364 In> "A" : "B" : "C"
1365 Result: "ABC"
1366 In> "Hello " : "there!"
1367 Result: "Hello there!"
```

1368 **9.8.2.2 WriteString()**

1369 The **WriteString()** function prints a string without showing the double quotes

```
that are around it.. For example, here is the Write() function being used to print
1370
1371
     the string "Hello":
1372
     In> Write("Hello")
1373
     Result: True
1374
     Side Effects:
1375
     "Hello"
     Notice the double quotes? Here is how the WriteString() function prints "Hello":
1376
1377
     In> WriteString("Hello")
1378
     Result: True
1379
     Side Effects:
1380
     Hello
1381
     9.8.2.3 NI()
     The NI() (New Line) function is used with the : function to place newline
1382
     characters inside of strings:
1383
1384
     In> WriteString("A": N1() : "B")
1385
     Result: True
1386
     Side Effects:
1387
1388
     В
     9.8.2.4 Space()
1389
     The Space() function is used to add spaces to printed output:
1390
1391
     In> WriteString("A"); Space(5); WriteString("B")
1392
     Result: True
1393
     Side Effects:
1394
     A
           В
1395
     In> WriteString("A"); Space(10); WriteString("B")
1396
     Result: True
1397
     Side Effects:
1398
     A B
1399
     In> WriteString("A"); Space(20); WriteString("B")
1400
     Result: True
1401
      Side Effects:
1402
     Α
                            В
```

1403 9.8.3 Accessing The Individual Letters In A String

- 1404 Individual letters in a string (which are also called **characters**) can be accessed
- by placing the character's position number (also called an **index**) inside of

brackets [] after the variable it is bound to. A character's position is determined 1406 by its distance from the left side of the string starting at 1. For example, in the 1407 string "Hello", 'H' is at position 1, 'e' is at position 2, etc. The following code 1408 shows individual characters in the above string being accessed: 1409 1410 In> a := "Hello, I am a string." 1411 Result> "Hello, I am a string." 1412 In>a[1]1413 Result> "H" 1414 In>a[2]1415 Result> "e" 1416 In>a[3]1417 Result> "1" 1418 In>a[4]1419 Result> "1" 1420 In> a[5] 1421 Result> "o" 9.8.3.1 Indexing Before The Beginning Of A String Or Past The End Of A String 1422 Lets see what happens if an index is used that is less than 1 or greater than the 1423 1424 length of a given string. First, we will bind the string "Hello" to the variable 'a': 1425 In> a := "Hello" 1426 Result: "Hello" Then, we'll index the character at position **1** and then the character at position **0**: 1427 1428 In>a[1]1429 Result: "H" 1430 In> a[0] 1431 Result: 1432 Exception: In function "StringMidGet" : 1433 bad argument number 1(counting from 1) : 1434 The offending argument aindex evaluated to 0 1435 Notice that using an index of **0** resulted in an error. Next, lets access the character at position 5 (which is the 'o'), then the character 1436

at position **6** and finally the character at position **7**:

1438 In> a[5]

```
1439 Result: "o"

1440 In> a[6]
1441 Result: """

1442 In> a[7]
1443 Result:
1444 Exception: String index out of range: 8
```

- 1445 The 'o' at position **5** was returned correctly, but accessing position **6** returned a
- double quote character (") and accessing position 7 resulted in an error. What
- 1447 you can see in this section is that errors are usually produced if an index is not
- set to the position of an actual character in a string.

1449 **9.9 Comments**

- 1450 Source code can often be difficult to understand and therefore all programming
- languages provide the ability for **comments** to be included in the code.
- 1452 Comments are used to explain what the code near them is doing and they are
- usually meant to be read by humans instead of being processed by a computer.
- 1454 Therefore, comments are ignored by the computer when a program is executed.
- 1455 There are two ways that MathPiper allows comments to be added to source code.
- 1456 The first way is by placing two forward slashes // to the left of any text that is
- meant to serve as a comment. The text from the slashes to the end of the line
- the slashes are on will be treated as a comment. Here is a program that contains
- 1459 comments which use slashes:

- 1467 When this program is executed, any text that starts with slashes is ignored.
- 1468 The second way to add comments to a MathPiper program is by enclosing the
- 1469 comments inside of slash-asterisk/asterisk-slash symbols /* */. This option is
- 1470 useful when a comment is too large to fit on one line. Any text between these
- 1471 symbols is ignored by the computer. This program shows a longer comment
- 1472 which has been placed between these symbols:

```
1473
      %mathpiper
1474
1475
      This is a longer comment and it uses
1476
      more than one line. The following
1477
      code assigns the number 3 to variable
1478
       x and then returns it as a result.
1479
      * /
1480
     x := 3;
1481
     %/mathpiper
1482
          %output, preserve="false"
1483
            Result: 3
1484
          %/output
```

9.10 How To Tell If MathPiper Has Crashed And What To Do If It Has

- 1486 Sometimes code will be evaluated which has one or more unusual errors in it and
- 1487 the errors will cause MathPiper to "crash". Unfortunately, beginners are more
- 1488 likely to crash MathPiper than more experienced programmers are because a
- beginner's program is more likely to have errors in it. When MathPiper crashes,
- 1490 no harm is done but it will not work correctly after that. The only way to
- 1491 recover from a MathPiper crash is to exit MathRider and then relaunch
- 1492 it. All the information in your buffers will be saved and preserved but the
- 1493 **contents of the console will not be**. Be sure to copy the contents of the
- 1494 console into a buffer and then save it before restarting.
- 1495 The main way to tell if MathRider has crashed is that it will indicate that **there**
- 1496 **are errors in lines of code that are actually fine**. If you are receiving an
- error in code that looks okay to you, simply restarting MathRider may fix the
- 1498 problem. If you restart MathRider and the error is still present, this usually
- 1499 means that there really is an error in the code.

9.11 Exercises

1485

- 1501 For the following exercises, create a new MathRider worksheet file called
- 1502 book 1 section 9 exercises <your first name> <your last name>.mrw.
- 1503 (Note: there are no spaces in this file name). For example, John Smith's
- 1504 worksheet would be called:
- 1505 book 1 section 9 exercises john smith.mrw.
- 1506 After this worksheet has been created, place your answer for each exercise that
- 1507 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 1508 start tag of each fold which indicates the exercise the fold contains the solution
- 1509 to. The folds you create should look similar to this one:

- 1510 %mathpiper, title="Exercise 1" 1511 //Sample fold. 1512 %/mathpiper If an exercise uses the MathPiper console instead of a fold, copy the work you 1513 did in the console into the worksheet so it can be saved. 1514 1515 **9.11.1 Exercise 1** 1516 Carefully read all of section 9. Evaluate each one of the examples in 1517 section 9 in the MathPiper worksheet you created or in the MathPiper 1518 console and verify that the results match the ones in the book. Copy all 1519 of the console examples you evaluated into your worksheet so they will be 1520 saved but do not put them in a fold. 9.11.2 Exercise 2 1521 1522 Change the precedence of the following expression using parentheses so that 1523 it prints 20 instead of 14: 1524 2 + 3 * 4 1525 **9.11.3 Exercise 3** 1526 Place the following calculations into a fold and then use one Echo() 1527 function per variable to print the results of the calculations. Put 1528 strings in the Echo() functions which indicate which variable each 1529 calculated value is bound to: 1530 a := 1+2+3+4+5; 1531 b := 1-2-3-4-5;1532 c := 1*2*3*4*5; 1533 d := 1/2/3/4/5; 1534 **9.11.4 Exercise 4** 1535 Place the following calculations into a fold and then use one Echo() 1536 function to print the results of all the calculations on a single line 1537 (Remember, the Echo() function can print multiple values if they are 1538 separated by commas.): 1539 Clear(x);
- 1539 Clear(x); 1540 a := 2*2*2*2*2; 1541 b := 2^5; 1542 c := x^2 * x^3; 1543 d := 2^2 * 2^3;

```
1544 9.11.5 Exercise 5
1545
     The following code assigns a string which contains all of the upper case
1546
     letters of the alphabet to the variable upper. Each of the three Echo()
1547
     functions prints an index number and the letter that is at that position in
1548
     the string. Place this code into a fold and then continue the Echo()
1549
     functions so that all 26 letters and their index numbers are printed
1550 upper := "ABCDEFGHIJKLMNOPQRSTUVWXYZ";
1551
    Echo(1, upper[1]);
1552 Echo(2,upper[2]);
1553 Echo(3,upper[3]);
1554 9.11.6 Exercise 6
1555
     Use Echo() functions to print an index number and the character at this
1556
     position for the following string (this is similar to what was done in the
1557
     previous exercise.):
1558 extra := ".!@#$%^&*() _+<>,?/{}[]|-=;";
1559
     Echo(1, extra[1]);
1560 Echo(2,extra[2]);
1561 Echo(3, extra[3]);
1562 9.11.7 Exercise 7
1563
     The following program uses strings and index numbers to print a person's
1564
     name. Create a program which uses the three strings from this program to
1565
     print the names of three of your favorite musical bands.
1566
     %mathpiper
1567
1568
       This program uses strings and index numbers to print
1569
      a person's name.
1570
1571
     upper := "ABCDEFGHIJKLMNOPQRSTUVWXYZ";
1572
     lower := "abcdefghijklmnopgrstuvwxyz";
1573
     extra := ".!@#$%^&*() +<>,?/{}[]|\-=";
1574
     //Print "Mary Smith.".
1575
     Echo (upper[13], lower[1], lower[18], lower[25], extra[12], upper[19], lower[13], l
1576
    ower[9],lower[20],lower[8],extra[1]);
1577 %/mathpiper
1578
          %output,preserve="false"
```

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1579 Result: True 1580 1581 1582 1581 Side Effects: 1582 Mary Smith. 1583 . %/output

10 Rectangular Selection Mode And Text Area Splitting

10.1 Rectangular Selection Mode

- One capability that MathRider has that a word processor may not have is the
- ability to select rectangular sections of text. To see how this works, do the
- 1588 following:

1584

1585

- 1) Type three or four lines of text into a text area.
- 1590 2) Hold down the **<Alt>** kev then slowly press the **backslash kev** (\) a few
- times. The bottom of the MathRider window contains a text field which
- 1592 MathRider uses to communicate information to the user. As **<Alt>**\ is
- repeatedly pressed, messages are displayed which read **Rectangular**
- selection is on and Rectangular selection is off.
- 1595 3) Turn rectangular selection on and then select some text in order to see
- how this is different than normal selection mode. When you are done
- experimenting, set rectangular selection mode to off.
- 1598 Most of the time normal selection mode is what you want to use but in certain
- 1599 situations rectangular selection mode is better.

1600 10.2 Text area splitting

- 1601 Sometimes it is useful to have two or more text areas open for a single document
- or multiple documents so that different parts of the documents can be edited at
- 1603 the same time. A situation where this would have been helpful was in the
- 1604 previous section where the output from an exercise in a MathRider worksheet
- 1605 contained a list of index numbers and letters which was useful for completing a
- 1606 later exercise.
- 1607 MathRider has this ability and it is called **splitting**. If you look just to the right
- of the toolbar there is an icon which looks like a blank window, an icon to the
- right of it which looks like a window which was split horizontally, and an icon to
- 1610 the right of the horizontal one which is split vertically. If you let your mouse
- 1611 hover over these icons, a short description will be displayed for each of them.
- 1612 Select a text area and then experiment with splitting it by pressing the horizontal
- and vertical splitting buttons. Move around these split text areas with their
- scroll bars and when you want to unsplit the document, just press the "**Unsplit**"
- 1615 **All**" icon.

1616

10.3 Exercises

- 1617 For the following exercises, create a new MathRider worksheet file called
- 1618 book_1_section_10_exercises_<your first name>_<your last name>.mrw.

- 1619 (Note: there are no spaces in this file name). For example, John Smith's
- 1620 worksheet would be called:
- 1621 book_1_section_10_exercises_john_smith.mrw.
- 1622 For the following exercises, simply type your answers anywhere in the
- 1623 worksheet.
- 1624 **10.3.1 Exercise 1**
- 1625 Carefully read all of section 10 then answer the following questions:
- 1626 a) Give two examples where rectangular selection mode may be more useful
- 1627 than regular selection mode.
- 1628 b) How can windows that have been split be unsplit?

11 Working With Random Integers

- 1630 It is often useful to use random integers in a program. For example, a program
- may need to simulate the rolling of dice in a game. In this section, a function for
- obtaining nonnegative integers is discussed along with how to use it to simulate
- the rolling of dice.

1629

1634

11.1 Obtaining Random Integers With The RandomInteger() Function

- One way that a MathPiper program can generate random integers is with the
- 1636 **RandomInteger()** function. The RandomInteger() function takes an integer as
- a parameter and it returns a random integer between 1 and the passed in
- integer. The following example shows random integers between 1 and 5
- 1639 **inclusive** being obtained from RandomInteger(). **Inclusive** here means that
- both 1 and 5 are included in the range of random integers that may be returned.
- 1641 If the word **exclusive** was used instead, this would mean that neither 1 nor 5
- 1642 would be in the range.

```
1643
     In> RandomInteger(5)
1644
     Result> 4
1645
     In> RandomInteger(5)
1646
     Result> 5
1647
     In> RandomInteger(5)
1648
     Result> 4
1649
     In> RandomInteger(5)
1650
     Result> 2
1651
     In> RandomInteger(5)
1652
     Result> 3
1653
     In> RandomInteger(5)
1654
     Result> 5
1655
     In> RandomInteger(5)
1656
     Result> 2
1657
     In> RandomInteger(5)
1658
     Result> 2
1659
     In> RandomInteger(5)
1660
     Result> 1
1661
      In> RandomInteger(5)
```

- 1663 Random integers between 1 and 100 can be generated by passing 100 to
- 1664 RandomInteger():

Result> 2

```
1669    In> RandomInteger(100)
1670    Result> 82
1671    In> RandomInteger(100)
1672    Result> 93
1673    In> RandomInteger(100)
1674    Result> 32
```

- 1675 A range of random integers that does not start with 1 can also be generated by
- using the **two argument** version of **RandomInteger()**. For example, random
- integers between 25 and 75 can be obtained by passing RandomInteger() the
- lowest integer in the range and the highest one:

```
1679
     In> RandomInteger(25, 75)
1680
     Result: 28
1681 In> RandomInteger(25, 75)
1682 Result: 37
1683
    In> RandomInteger(25, 75)
1684
    Result: 58
1685
     In> RandomInteger(25, 75)
1686
    Result: 50
1687
     In> RandomInteger(25, 75)
1688
     Result: 70
```

11.2 Simulating The Rolling Of Dice

The following example shows the simulated rolling of a single six sided die using the RandomInteger() function:

```
1692
     In> RandomInteger(6)
1693
     Result> 5
1694 In> RandomInteger(6)
1695 Result> 6
1696 In> RandomInteger(6)
1697
    Result> 3
1698
     In> RandomInteger(6)
1699
    Result> 2
1700
    In> RandomInteger(6)
1701
     Result> 5
```

- 1702 Code that simulates the rolling of two 6 sided dice can be evaluated in the
- 1703 MathPiper console by placing it within a **code block**. The following code
- 1704 outputs the sum of the two simulated dice:

```
1705    In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
1706    Result> 6
1707    In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
1708    Result> 12
1709    In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
1710    Result> 6
```

- 1711 In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
 1712 Result> 4
 1713 In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
 1714 Result> 3
 1715 In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
 1716 Result> 8
- 1717 Now that we have the ability to simulate the rolling of two 6 sided dice, it would
- 1718 be interesting to determine if some sums of these dice occur more frequently
- 1719 than other sums. What we would like to do is to roll these simulated dice
- 1720 hundreds (or even thousands) of times and then analyze the sums that were
- 1721 produced. We don't have the programming capability to easily do this yet, but
- after we finish the section on **While loops**, we will.
- 1723 **11.3 Exercises**
- 1724 For the following exercises, create a new MathRider worksheet file called
- 1725 book 1 section 11 exercises <your first name> <your last name>.mrw.
- 1726 (Note: there are no spaces in this file name). For example, John Smith's
- 1727 worksheet would be called:
- 1728 book_1_section_11_exercises_john_smith.mrw.
- 1729 After this worksheet has been created, place your answer for each exercise that
- 1730 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 1731 start tag of each fold which indicates the exercise the fold contains the solution
- to. The folds you create should look similar to this one:
- 1733 %mathpiper, title="Exercise 1"
- 1734 //Sample fold.
- 1735 %/mathpiper
- 1736 If an exercise uses the MathPiper console instead of a fold, copy the work you
- did in the console into the worksheet so it can be saved but do not put it in a fold.
- 1738 11.3.1 Exercise 1
- 1739 Carefully read all of section 11. Evaluate each one of the examples in
- 1740 section 11 in the MathPiper worksheet you created or in the MathPiper
- 1741 console and verify that the results match the ones in the book. Copy all
- 1742 of the console examples you evaluated into your worksheet so they will be
- 1743 saved but do not put them in a fold.

1744 12 Making Decisions

- 1745 The simple programs that have been discussed up to this point show some of the
- 1746 power that software makes available to programmers. However, these programs
- are limited in their problem solving ability because they are unable to make
- decisions. This section shows how programs which have the ability to make
- decisions are able to solve a wider range of problems than programs that can't
- 1750 make decisions.

1751

12.1 Conditional Operators

- 1752 A program's decision making ability is based on a set of special operators which
- are called **conditional operators**. A **conditional operator** is an operator that
- 1754 is used to **compare two values**. Expressions that contain conditional operators
- return a **boolean value** and a **boolean value** is one that can only be **True** or
- 1756 **False**. In case you are curious about the strange name, boolean values come
- 1757 from the area of mathematics called **boolean logic**. This logic was created by a
- mathematician named **George Boole** and this is where the name boolean came
- 1759 from. Table 2 shows the conditional operators that MathPiper uses:

Operator	Description
x = y	Returns True if the two values are equal and False if they are not equal. Notice that = performs a comparison and not an assignment like := does.
x != y	Returns True if the values are not equal and False if they are equal.
x < y	Returns True if the left value is less than the right value and False if the left value is not less than the right value.
x <= y	Returns True if the left value is less than or equal to the right value and False if the left value is not less than or equal to the right value.
x > y	Returns True if the left value is greater than the right value and False if the left value is not greater than the right value.
x >= y	Returns True if the left value is greater than or equal to the right value and False if the left value is not greater than or equal to the right value.

Table 2: Conditional Operators

- 1760 This example shows some of these conditional operators being evaluated in the
- 1761 MathPiper console:
- 1762 In> 1 < 2
- 1763 Result> True

```
1764
      In> 4 > 5
1765
     Result> False
1766
     In> 8 >= 8
1767 Result> True
1768
     In> 5 <= 10
1769
      Result> True
      The following examples show each of the conditional operators in Table 2 being
1770
1771
      used to compare values that have been assigned to variables \mathbf{x} and \mathbf{v}:
1772
      %mathpiper
1773
      // Example 1.
1774
      x := 2;
1775
      y := 3;
      Echo(x, "= ", y, ":", x = y);
Echo(x, "!= ", y, ":", x != y);
1776
1777
      Echo(x, "< ", y, ":", x < y);
1778
1779
      Echo(x, "<= ", y, ":", x <= y);
      Echo(x, "> ", y, ":", x > y);
1780
1781
      Echo (x, ">= ", y, ":", x >= y);
1782
      %/mathpiper
1783
           %output, preserve="false"
1784
             Result: True
1785
1786
            Side Effects:
1787
             2 = 3:False
1788
            2 != 3 :True
1789
            2 < 3 :True
1790
           2 <= 3 :True
1791
             2 > 3 :False
1792
             2 >= 3 :False
1793 . %/output
1794
      %mathpiper
1795
          // Example 2.
1796
          x := 2;
1797
          y := 2;
1798
          Echo(x, "= ", y, ":", x = y);
1799
          Echo(x, "!= ", y, ":", x != y);
          Echo(x, "< ", y, ":", x < y);
Echo(x, "<= ", y, ":", x <= y);
1800
1801
          Echo(x, "> ", y, ":", x > y);
1802
```

```
Echo(x, ">= ", y, ":", x >= y);
1803
1804
      %/mathpiper
1805
          %output, preserve="false"
1806
            Result: True
1807
1808
            Side Effects:
1809
            2 = 2:True
1810
            2 != 2 :False
1811
            2 < 2 :False
1812
            2 <= 2 :True
1813
            2 > 2 :False
1814
            2 >= 2 :True
1815 . %/output
1816
      %mathpiper
1817
      // Example 3.
1818
      x := 3;
1819
     y := 2;
1820
     Echo(x, "= ", y, ":", x = y);
Echo(x, "!= ", y, ":", x != y);
1821
     Echo(x, "< ", y, ":", x < y);
1822
     Echo (x, "<= ", y, ":", x <= y);
1823
     Echo(x, "> ", y, ":", x > y);
1824
     Echo (x, ">= ", y, ":", x \geq= y);
1825
1826
      %/mathpiper
1827
          %output, preserve="false"
1828
            Result: True
1829
1830
            Side Effects:
1831
            3 = 2:False
            3 != 2 :True
1832
1833
            3 < 2 :False
1834
            3 <= 2 :False
1835
            3 > 2 :True
1836
            3 >= 2 :True
1837
    . %/output
```

- 1838 Conditional operators are placed at a lower level of precedence than the other operators we have covered to this point:
- 1840 () Parentheses are evaluated from the inside out.
- 1841 ^ Then exponents are evaluated right to left.

- *,%,/ Then multiplication, remainder, and division operations are evaluated left to right.
- 1844 +, Then addition and subtraction are evaluated left to right.
- =,!=,<,<=,>,>= Finally, conditional operators are evaluated.

1846 12.2 Predicate Expressions

- 1847 Expressions which return either **True** or **False** are called "**predicate**"
- 1848 expressions. By themselves, predicate expressions are not very useful and they
- only become so when they are used with special decision making functions, like
- the If() function (which is discussed in the next section).

1851 **12.3 Exercises**

- 1852 For the following exercises, create a new MathRider worksheet file called
- 1853 book 1 section 12a exercises <your first name> <your last name>.mrw.
- 1854 (Note: there are no spaces in this file name). For example, John Smith's
- 1855 worksheet would be called:
- 1856 book_1_section_12a_exercises_john_smith.mrw.
- 1857 After this worksheet has been created, place your answer for each exercise that
- 1858 requires a fold into its own fold in this worksheet. Place a title attribute in the
- start tag of each fold which indicates the exercise the fold contains the solution
- 1860 to. The folds you create should look similar to this one:
- 1861 %mathpiper, title="Exercise 1"
- 1862 //Sample fold.
- 1863 %/mathpiper
- 1864 If an exercise uses the MathPiper console instead of a fold, copy the work you
- did in the console into the worksheet so it can be saved but do not put it in a fold.

1866 **12.3.1 Exercise 1**

- 1867 Carefully read all of section 12 up to this point. Evaluate each one of
- 1868 the examples in the sections you read in the MathPiper worksheet you
- 1869 created or in the MathPiper console and verify that the results match the
- 1870 ones in the book. Copy all of the console examples you evaluated into your
- 1871 worksheet so they will be saved but do not put them in a fold.

1872 **12.3.2 Exercise 2**

1873 Open a MathPiper session and evaluate the following predicate expressions:

```
1874
     In> 3 = 3
1875
     In> 3 = 4
1876
    In> 3 < 4
    In> 3 != 4
1877
1878
     In > -3 < 4
1879 In> 4 >= 4
1880
     In> 1/2 < 1/4
1881
     In> 15/23 < 122/189
1882
     /*In the following two expressions, notice that 1/2 is not considered to be
1883
     equal to .5 unless it is converted to a numerical value first.*/
1884
     In > 1/2 = .5
1885
     In > N(1/2) = .5
```

1886 **12.3.3 Exercise 3**

- 1887 Come up with 10 predicate expressions of your own and evaluate them in the
- 1888 MathPiper console.

1889 12.4 Making Decisions With The If() Function & Predicate Expressions

- 1890 All programming languages have the ability to make decisions and the most
- 1891 commonly used function for making decisions in MathPiper is the **If()** function.
- 1892 There are two calling formats for the If() function:

```
If(predicate, then)
If(predicate, then, else)
```

- 1893 The way the first form of the If() function works is that it evaluates the first
- 1894 expression in its argument list (which is the "**predicate**" expression) and then
- looks at the value that is returned. If this value is **True**, the "**then**" expression
- that is listed second in the argument list is executed. If the predicate expression
- evaluates to **False**, the "**then**" expression is not executed. (Note: any function

1932

End of program.

%/output

```
1898
      that accepts a predicate expression as a parameter can also accept the boolean
1899
     values True and False).
     The following program uses an If() function to determine if the value in variable
1900
      number is greater than 5. If number is greater than 5, the program will echo
1901
      "Greater" and then "End of program":
1902
1903
      %mathpiper
1904
     number := 6;
1905
      If (number > 5, Echo (number, "is greater than 5."));
1906
     Echo("End of program.");
1907
      %/mathpiper
1908
          %output,preserve="false"
1909
            Result: True
1910
1911
            Side Effects:
1912
            6 is greater than 5.
1913
            End of program.
1914 .
         %/output
1915
      In this program, number has been set to 6 and therefore the expression number
      > 5 is True. When the If() functions evaluates the predicate expression and
1916
      determines it is True, it then executes the first Echo() function. The second
1917
1918
      Echo() function at the bottom of the program prints "End of program"
      regardless of what the If() function does. (Note: semicolons cannot be placed
1919
      after expressions which are in function calls.)
1920
1921
      Here is the same program except that number has been set to 4 instead of 6:
1922
     %mathpiper
1923
     number := 4;
1924
      If(number > 5, Echo(number, "is greater than 5."));
1925
     Echo("End of program.");
1926
      %/mathpiper
1927
          %output, preserve="false"
1928
            Result: True
1929
1930
            Side Effects:
```

- 1933 This time the expression **number > 4** returns a value of **False** which causes the
- 1934 **If()** function to not execute the "**then**" expression that was passed to it.

1935 12.4.1 If() Functions Which Include An "Else" Parameter

- 1936 The second form of the If() function takes a third "else" expression which is
- 1937 executed only if the predicate expression is **False**. This program is similar to the
- 1938 previous one except an "else" expression has been added to it:

```
1939
      %mathpiper
1940
     x := 4;
1941
     If (x > 5, Echo(x, "is greater than 5."), Echo(x, "is NOT greater than 5."));
1942
     Echo("End of program.");
1943
      %/mathpiper
1944
          %output, preserve="false"
1945
            Result: True
1946
1947
            Side Effects:
1948
            4 is NOT greater than 5.
1949
            End of program.
1950
     . %/output
```

1951 **12.5 Exercises**

- 1952 For the following exercises, create a new MathRider worksheet file called
- 1953 book 1 section 12b exercises <your first name> <your last name>.mrw.
- 1954 (Note: there are no spaces in this file name). For example, John Smith's
- 1955 worksheet would be called:
- 1956 book 1 section 12b exercises john smith.mrw.
- 1957 After this worksheet has been created, place your answer for each exercise that
- 1958 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 1959 start tag of each fold which indicates the exercise the fold contains the solution
- 1960 to. The folds you create should look similar to this one:

```
1961 %mathpiper,title="Exercise 1"
1962 //Sample fold.
1963 %/mathpiper
```

1964 If an exercise uses the MathPiper console instead of a fold, copy the work you

did in the console into the worksheet so it can be saved but do not put it in a fold. 1965

12.5.1 Exercise 1 1966

- 1967 Carefully read all of section 12 starting at the end of the previous
- 1968 exercises and up to this point. Evaluate each one of the examples in the
- 1969 sections you read in the MathPiper worksheet you created or in the
- 1970 MathPiper console and verify that the results match the ones in the book.
- 1971 Copy all of the console examples you evaluated into your worksheet so they
- 1972 will be saved but do not put them in a fold.

12.5.2 Exercise 2 1973

- 1974 Write a program which uses the RandomInteger() function to simulate the
- 1975 flipping of a coin (Hint: you can use 1 to represent a head and 2 to
- 1976 represent a tail.). Use predicate expressions, the If() function, and the
- 1977 Echo() function to print the string "The coin came up heads." or the string
- 1978 "The coin came up tails.", depending on what the simulated coin flip came
- 1979 up as when the code was executed.

12.6 The And(), Or(), & Not() Boolean Functions & Infix Notation 1980

12.6.1 And() 1981

1989

- 1982 Sometimes a programmer needs to check if two or more expressions are all **True**
- and one way to do this is with the **And()** function. The And() function has **two** 1983
- **calling formats** (or **notations**) and this is the first one: 1984

```
And (expression1, expression2, expression3, ..., expressionN)
```

- 1985 This calling format is able to accept one or more predicate expressions as input.
- If **all** of these expressions returns a value of **True**, the And() function will also 1986
- return a **True**. However, if **any** of the expressions return a **False**, then the And() 1987
- 1988 function will return a **False**. This can be seen in the following example:

```
In> And(True, True)
1990
     Result> True
1991
     In> And(True, False)
1992
     Result> False
1993
     In> And(False, True)
1994
     Result> False
1995
```

In> And(True, True, True, True) 1996 Result> True

```
1997 In> And (True, True, False, True)
1998 Result> False
```

The second format (or notation) that can be used to call the And() function is called **infix** notation:

```
expression1 And expression2
```

With **infix** notation, an expression is placed on both sides of the And() function name instead of being placed inside of parentheses that are next to it:

```
2003
     In> True And True
2004
     Result> True
2005
     In> True And False
2006
     Result> False
2007
     In> False And True
2008
     Result> False
2009
     In> True And True And True And True
2010
     Result: True
```

- 2011 Infix notation can only accept **two** expressions at a time, but it is often more
- 2012 convenient to use than function calling notation. The following program also
- 2013 demonstrates the infix version of the And() function being used:

```
2014
      %mathpiper
2015
      a := 7;
2016
      b := 9;
2017
      Echo("1: ", a < 5 And b < 10);
Echo("2: ", a > 5 And b > 10);
2018
2019
      Echo ("3: ", a < 5 And b > 10);
2020
      Echo ("4: ", a > 5 And b < 10);
2021
      If(a > 5 And b < 10, Echo("These expressions are both true."));</pre>
2022
      %/mathpiper
2023
           %output, preserve="false"
2024
             Result: True
2025
2026
             Side Effects:
2027
             1: False
2028
             2: False
2029
             3: False
```

```
2030
            4: True
2031
            These expressions are both true.
2032
          %/output
     12.6.2 Or()
2033
      The Or() function is similar to the And() function in that it has both a function
2034
2035
     calling format and an infix calling format and it only works with predicate
      expressions. However, instead of requiring that all expressions be True in order
2036
      to return a True, Or() will return a True if one or more expressions are True.
2037
      Here is the function calling format for Or():
2038
      Or(expression1, expression2, expression3, ..., expressionN)
      and this example shows Or() being used with function calling format:
2039
2040
     In> Or(True, False)
2041
     Result> True
2042
     In> Or(False, True)
2043
     Result> True
2044
     In> Or(False, False)
2045 Result> False
2046
     In> Or(False, False, False, False)
2047
     Result> False
2048
     In> Or(False, True, False, False)
2049
     Result> True
     The infix notation format for Or() is as follows:
2050
      expression1 Or expression2
      and this example shows infix notation being used:
2051
2052
     In> True Or False
2053
     Result> True
```

```
2053 Result> True

2054 In> False Or True

2055 Result> True

2056 In> False Or False
```

```
2057
      Result> False
      The following program also demonstrates the infix version of the Or() function
2058
2059
      being used:
2060
      %mathpiper
2061
      a := 7;
2062
      b := 9;
2063
      Echo("1: ", a < 5 Or b < 10);
2064
      Echo ("2: ", a > 5 Or b > 10);
2065
      Echo("3: ", a > 5 Or b < 10);
      Echo ("4: ", a < 5 Or b > 10);
2066
2067
      If(a < 5 Or b < 10, Echo("At least one of these expressions is true."));</pre>
2068
      %/mathpiper
2069
          %output,preserve="false"
2070
            Result: True
2071
2072
            Side Effects:
2073
            1: True
2074
            2: True
2075
            3: True
2076
            4: False
```

2079 **12.6.3 Not() & Prefix Notation**

%/output

- 2080 The **Not()** function works with predicate expressions like the And() and Or()
- 2081 functions do, except it can only accept **one** expression as input. The way Not()
- 2082 works is that it changes a **True** value to a **False** value and a **False** value to a
- 2083 **True** value. Here is the Not()'s function calling format:

At least one of these expressions is true.

```
Not(expression)
```

2084 and this example shows Not() being used with function calling format:

```
2085 In> Not(True)
2086 Result> False
2087 In> Not(False)
2088 Result> True
```

2077

In> Not True

2092

2089 Instead of providing an alternative infix calling format like And() and Or() do,

2090 Not()'s second calling format uses **prefix** notation:

```
Not expression
```

2091 Prefix notation looks similar to function notation except no parentheses are used:

```
2093
      Result> False
2094
      In> Not False
2095
      Result> True
2096
      Finally, here is a program that also uses the prefix version of Not():
2097
      %mathpiper
2098
      Echo ("3 = 3 is ", 3 = 3);
2099
      Echo ("Not 3 = 3 is ", Not 3 = 3);
2100
      %/mathpiper
```

- 2108 **12.7 Exercises**
- 2109 For the following exercises, create a new MathRider worksheet file called
- 2110 book 1 section 12c exercises <vour first name> <vour last name>.mrw.
- 2111 (Note: there are no spaces in this file name). For example, John Smith's
- 2112 worksheet would be called:
- 2113 book 1 section 12c exercises john smith.mrw.
- 2114 After this worksheet has been created, place your answer for each exercise that
- 2115 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 2116 start tag of each fold which indicates the exercise the fold contains the solution
- 2117 to. The folds you create should look similar to this one:
- 2118 %mathpiper, title="Exercise 1"

```
2119 //Sample fold.
```

2120 %/mathpiper

- 2121 If an exercise uses the MathPiper console instead of a fold, copy the work you
- 2122 did in the console into the worksheet so it can be saved but do not put it in a fold.

2123 **12.7.1 Exercise 1**

- 2124 Carefully read all of section 12 starting at the end of the previous
- 2125 exercises and up to this point. Evaluate each one of the examples in the
- 2126 sections you read in the MathPiper worksheet you created or in the
- 2127 MathPiper console and verify that the results match the ones in the book.
- 2128 Copy all of the console examples you evaluated into your worksheet so they
- 2129 will be saved but do not put them in a fold.

2130 **12.7.2 Exercise 2**

- 2131 The following program simulates the rolling of two dice and prints a
- 2132 message if both of the two dice come up less than or equal to 3. Create a
- 2133 similar program which simulates the flipping of two coins and print the
- 2134 message "Both coins came up heads." if both coins come up heads.

```
2135 %mathpiper
```

2136 /*

2137 This program simulates the rolling of two dice and prints a message if

2138 both of the two dice come up less than or equal to 3.

2139 */

```
2140 die1 := RandomInteger(6);
```

2141 die2 := RandomInteger(6);

2142 Echo("Die1: ", die1, " Die2: ", die2);

2143 NewLine();

2144 If (die1 <= 3 And die2 <= 3, Echo("Both dice came up <= to 3."));

2145 %/mathpiper

2146 **12.7.3 Exercise 3**

- 2147 The following program simulates the rolling of two dice and prints a
- 2148 message if either of the two dice come up less than or equal to 3. Create
- 2149 a similar program which simulates the flipping of two coins and print the
- 2150 message "At least one coin came up heads." if at least one coin comes up
- 2151 heads.
- 2152 %mathpiper
- 2153 /*
- This program simulates the rolling of two dice and prints a message if
- either of the two dice come up less than or equal to 3.

```
2156 */
2157
     die1 := RandomInteger(6);
2158
     die2 := RandomInteger(6);
2159
     Echo("Diel: ", diel, " Die2: ", die2);
2160
     NewLine();
2161 If( die1 <= 3 Or die2 <= 3, Echo("At least one die came up <= 3.") );
2162 %/mathpiper
```

13 The While() Looping Function & Bodied Notation

- 2164 Many kinds of machines, including computers, derive much of their power from
- 2165 the principle of **repeated cycling**. **Repeated cycling** in a MathPiper program
- 2166 means to execute one or more expressions over and over again and this process
- 2167 is called "looping". MathPiper provides a number of ways to implement loops
- 2168 in a program and these ways range from straight-forward to subtle.
- 2169 We will begin discussing looping in MathPiper by starting with the straight-
- 2170 forward **While** function. The calling format for the **While** function is as follows:

```
2171 While (predicate)
2172 [
2173 body_expressions
2174 ];
```

- 2175 The **While** function is similar to the **If** function except it will repeatedly execute
- 2176 the expressions it contains as long as its "predicate" expression is **True**. As soon
- 2177 as the predicate expression returns a **False**, the While() function skips the
- 2178 expressions it contains and execution continues with the expression that
- 2179 immediately follows the While() function (if there is one).
- 2180 The expressions which are contained in a While() function are called its "**body**"
- and all functions which have body expressions are called "bodied" functions. If
- 2182 a body contains more than one expression then these expressions need to be
- 2183 placed within a **code block** (code blocks were discussed in an earlier section).
- 2184 What a function's body is will become clearer after studying some example
- 2185 programs.

2186

13.1 Printing The Integers From 1 to 10

2187 The following program uses a While() function to print the integers from 1 to 10:

```
2188
      %mathpiper
2189
      // This program prints the integers from 1 to 10.
2190
2191
          Initialize the variable count to 1
2192
          outside of the While "loop".
2193
2194
      count := 1;
2195
      While (count <= 10)
2196
2197
          Echo (count);
```

```
2198
2199
           count := count + 1; //Increment count by 1.
2200
      ];
2201
      %/mathpiper
2202
           %output,preserve="false"
2203
             Result: True
2204
2205
             Side Effects:
2206
             1
             2
2207
2208
             3
2209
             4
             5
2210
             6
2211
2212
             7
2213
             8
2214
             9
2215
             10
2216
          %/output
```

- 2217 In this program, a single variable called **count** is created. It is used to tell the
- 2218 Echo() function which integer to print and it is also used in the predicate
- 2219 expression that determines if the While() function should continue to **loop** or not.
- 2220 When the program is executed, **1** is placed into **count** and then the While()
- 2221 function is called. Notice that **count** is bound to the value 1 **above the While**
- loop. Setting a variable to an initial value is called **initializing** the variable and
- in this case, count needs to be initialized before it is used in the While() function.
- The predicate expression count ≤ 10 becomes $1 \leq 10$ and, since 1 is indeed
- less than or equal to 10, a value of **True** is returned by the predicate expression.
- 2226 The While() function sees that the predicate expression returned a **True** and
- therefore it executes all of the expressions inside of its **body** from top to bottom.
- 2228 The Echo() function prints the current contents of count (which is 1) and then the
- 2229 expression count := count + 1 is executed.
- 2230 The expression **count** := **count** + **1** is a standard expression form that is used in
- 2231 many programming languages. Each time an expression in this form is
- 2232 evaluated, it **increases the variable it contains by 1**. Another way to describe
- 2233 the effect this expression has on **count** is to say that it **increments count** by **1**.
- 2234 In this case **count** contains **1** and, after the expression is evaluated, **count**
- 2235 contains **2**.
- 2236 After the last expression inside the body of the While() function is executed, the
- 2237 While() function reevaluates its predicate expression to determine whether it
- 2238 should continue looping or not. Since **count** is **2** at this point, the predicate
- expression returns **True** and the code inside the body of the While() function is

- executed again. This loop will be repeated until **count** is incremented to **11** and
- 2241 the predicate expression returns **False**.

2242 13.2 Printing The Integers From 1 to 100

- 2243 The previous program can be adjusted in a number of ways to achieve different
- results. For example, the following program prints the integers from 1 to 100 by
- 2245 changing the **10** in the predicate expression to **100**. A Write() function is used in
- 2246 this program so that its output is displayed on the same line until it encounters
- 2247 the **wrap margin** in MathRider (which can be set in Utilities -> Buffer
- 2248 Options...).

```
2249
      %mathpiper
2250
      // Print the integers from 1 to 100.
2251
      count := 1;
2252
      While (count <= 100)
2253
2254
          Write(count,,);
2255
2256
          count := count + 1; //Increment count by 1.
2257
      ];
2258
      %/mathpiper
2259
           %output,preserve="false"
2260
             Result: True
2261
2262
             Side Effects:
2263
             1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,
2264
             24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43,
2265
             44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63,
2266
             64,65,66,67,68,69,70,71,72,73,74,75,76,77,78,79,80,81,82,83,
2267
             84,85,86,87,88,89,90,91,92,93,94,95,96,97,98,99,100
2268
          %/output
```

2269 (Note: In MathRider, the above numbers will all be on a single line.)

13.3 Printing The Odd Integers From 1 To 99

- 2271 The following program prints the odd integers from 1 to 99 by changing the
- increment value in the increment expression from 1 to 2:
- 2273 %mathpiper

2270

2274 //Print the odd integers from 1 to 99.

```
2275
     x := 1;
2276
      While (x \leq 100)
2277
2278
          Write(x,,);
2279
          x := x + 2; //Increment x by 2.
2280
      ];
2281
      %/mathpiper
2282
          %output, preserve="false"
2283
             Result: True
2284
2285
             Side Effects:
2286
             1,3,5,7,9,11,13,15,17,19,21,23,25,27,29,31,33,35,37,39,41,43,
2287
             45, 47, 49, 51, 53, 55, 57, 59, 61, 63, 65, 67, 69, 71, 73, 75, 77, 79, 81, 83,
2288
             85,87,89,91,93,95,97,99
2289
     . %/output
```

13.4 Printing The Integers From 1 To 100 In Reverse Order

2291 Finally, the following program prints the integers from 1 to 100 in reverse order:

```
2292
      %mathpiper
2293
      //Print the integers from 1 to 100 in reverse order.
2294
      x := 100;
2295
      While (x >= 1)
2296
2297
          Write(x,,);
2298
          x := x - 1; //Decrement x by 1.
2299
      ];
2300
      %/mathpiper
2301
          %output,preserve="false"
2302
            Result: True
2303
2304
            Side Effects:
2305
             100,99,98,97,96,95,94,93,92,91,90,89,88,87,86,85,84,83,82,
2306
             81,80,79,78,77,76,75,74,73,72,71,70,69,68,67,66,65,64,63,
2307
             62,61,60,59,58,57,56,55,54,53,52,51,50,49,48,47,46,45,44,
2308
             43,42,41,40,39,38,37,36,35,34,33,32,31,30,29,28,27,26,25,
2309
             24, 23, 22, 21, 20, 19, 18, 17, 16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4,
2310
             3,2,1
2311
          %/output
```

- In order to achieve the reverse ordering, this program had to initialize \mathbf{x} to $\mathbf{100}$,
- check to see if x was greater than or equal to 1 ($x \ge 1$), and decrement x by
- 2314 **subtracting 1 from it** instead of adding 1 to it.

13.5 Expressions Inside Of Code Blocks Are Indented

- 2316 In the programs in the previous sections which use While loops, notice that the
- 2317 expressions which are inside of the While() function's code block are **indented**.
- 2318 These expressions do not need to be indented to execute properly, but doing so
- 2319 makes the program easier to read.

13.6 Long-Running Loops, Infinite Loops, & Interrupting Execution

- 2321 It is easy to create a loop that will execute a large number of times, or even an
- 2322 **infinite number of times**, either on purpose or by mistake. When you execute
- 2323 a program that contains an **infinite loop**, it will run until you tell MathPiper to
- 2324 **interrupt** its execution. This is done by opening the MathPiper **console** and
- then pressing the "Halt Calculation" button which in the upper left corner of
- 2326 the console.

2315

- 2327 Lets experiment with the **Halt Calculation** button by executing a program that
- 2328 contains an infinite loop and then stopping it:

```
2329
      %mathpiper
2330
      //Infinite loop example program.
2331
      x := 1;
2332
     While (x < 10)
2333
2334
          x := 3; //Oops, x is not being incremented!.
2335
      ];
2336
     %/mathpiper
2337
          %output, preserve="false"
2338
            Processing...
2339
     . %/output
```

- Since the contents of x is never changed inside the loop, the expression x < 10
- 2341 always evaluates to **True** which causes the loop to continue looping. Notice that
- 2342 the %output fold contains the word "**Processing...**" to indicate that the program
- 2343 is still running the code.
- 2344 Execute this program now and then interrupt it using the **Halt Calculation**
- button. When the program is interrupted, the %output fold will display the
- 2346 message "User interrupted calculation" to indicate that the program was

2347 interrupted. After a program has been interrupted, the program can be edited

2348 and then rerun.

2349

13.7 A Program That Simulates Rolling Two Dice 50 Times

The following program is larger than the previous programs that have been discussed in this book, but it is also more interesting and more useful. It uses a

2352 While() loop to simulate the rolling of two dice 50 times and it records how many

2353 times each possible sum has been rolled so that this data can be printed. The

comments in the code explain what each part of the program does. (Remember, if

2355 you copy this program to a MathRider worksheet, you can use rectangular

2356 **selection mode** to easily remove the line numbers).

```
2357
      %mathpiper
2358
2359
      This program simulates rolling two dice 50 times.
2360
2361
2362
        These variables are used to record how many times
2363
        a possible sum of two dice has been rolled. They are
2364
        all initialized to 0 before the simulation begins.
2365
2366
     numberOfTwosRolled := 0;
2367
     numberOfThreesRolled := 0;
2368
     numberOfFoursRolled := 0;
2369
     numberOfFivesRolled := 0;
2370
     numberOfSixesRolled := 0;
2371
     numberOfSevensRolled := 0;
2372
     numberOfEightsRolled := 0;
2373
     numberOfNinesRolled := 0;
2374
     numberOfTensRolled := 0;
2375
     numberOfElevensRolled := 0;
2376
     numberOfTwelvesRolled := 0;
2377
      //This variable keeps track of the number of the current roll.
2378
     roll := 1;
2379
     Echo("These are the rolls:");
2380
2381
      The simulation is performed inside of this While loop. The number of
2382
      times the dice will be rolled can be changed by changing the number 50
2383
      which is in the While function's predicate expression.
2384
2385
      While (roll <= 50)
```

```
2386
     [
2387
          //Roll the dice.
2388
          die1 := RandomInteger(6);
2389
          die2 := RandomInteger(6);
2390
2391
2392
          //Calculate the sum of the two dice.
2393
          rollSum := die1 + die2;
2394
2395
2396
2397
          Print the sum that was rolled. Note: if a large number of rolls
2398
           is going to be performed (say > 1000), it would be best to comment
2399
           out this Write() function so that it does not put too much text
2400
           into the output fold.
2401
          * /
2402
          Write(rollSum,,);
2403
2404
2405
          /*
2406
           These If() functions determine which sum was rolled and then add
2407
           1 to the variable which is keeping track of the number of times
2408
           that sum was rolled.
2409
2410
          If(rollSum = 2, numberOfTwosRolled := numberOfTwosRolled + 1);
2411
          If(rollSum = 3, numberOfThreesRolled := numberOfThreesRolled + 1);
2412
          If(rollSum = 4, numberOfFoursRolled := numberOfFoursRolled + 1);
2413
          If(rollSum = 5, numberOfFivesRolled := numberOfFivesRolled + 1);
2414
          If(rollSum = 6, numberOfSixesRolled := numberOfSixesRolled + 1);
2415
          If(rollSum = 7, numberOfSevensRolled := numberOfSevensRolled + 1);
2416
          If(rollSum = 8, numberOfEightsRolled := numberOfEightsRolled + 1);
2417
          If(rollSum = 9, numberOfNinesRolled := numberOfNinesRolled + 1);
2418
          If(rollSum = 10, numberOfTensRolled := numberOfTensRolled + 1);
2419
          If(rollSum = 11, numberOfElevensRolled := numberOfElevensRolled+1);
2420
          If(rollSum = 12, numberOfTwelvesRolled := numberOfTwelvesRolled+1);
2421
2422
2423
          //Increment the roll variable to the next roll number.
2424
          roll := roll + 1;
2425 ];
2426
      //Print the contents of the sum count variables for visual analysis.
2427
      NewLine();
2428 NewLine();
2429
     Echo("Number of Twos rolled: ", numberOfTwosRolled);
     Echo("Number of Threes rolled: ", numberOfThreesRolled);
Echo("Number of Fours rolled: ", numberOfFoursRolled);
2430
2431
     Echo("Number of Fives rolled: ", numberOfFivesRolled);
2432
     Echo("Number of Sixes rolled: ", numberOfSixesRolled);
Echo("Number of Sevens rolled: ", numberOfSevensRolled);
2433
2434
2435
      Echo("Number of Eights rolled: ", numberOfEightsRolled);
```

```
2436
     Echo("Number of Nines rolled: ", numberOfNinesRolled);
2437
     Echo("Number of Tens rolled: ", numberOfTensRolled);
2438
     Echo("Number of Elevens rolled: ", numberOfElevensRolled);
2439
     Echo ("Number of Twelves rolled: ", numberOfTwelvesRolled);
2440
     %/mathpiper
2441
          %output, preserve="false"
2442
            Result: True
2443
2444
            Side effects:
2445
            These are the rolls:
2446
            4,8,6,4,6,9,7,11,9,3,11,6,11,7,11,4,7,7,8,7,3,6,7,7,7,12,4,
2447
            12,7,8,12,6,8,10,10,5,9,8,4,5,3,5,7,7,4,6,7,7,5,8,
2448
2449
            Number of Twos rolled: 0
2450
            Number of Threes rolled: 3
2451
            Number of Fours rolled: 6
2452
            Number of Fives rolled: 4
2453
            Number of Sixes rolled: 6
2454
            Number of Sevens rolled: 13
2455
            Number of Eights rolled: 6
2456
            Number of Nines rolled: 3
2457
            Number of Tens rolled: 2
2458
            Number of Elevens rolled: 4
2459
            Number of Twelves rolled: 3
2460
          %/output
```

2461 **13.8 Exercises**

- 2462 For the following exercises, create a new MathRider worksheet file called
- 2463 book 1 section 13 exercises <your first name> <your last name>.mrw.
- 2464 (Note: there are no spaces in this file name). For example, John Smith's
- 2465 worksheet would be called:

2466 book_1_section_13_exercises_john_smith.mrw.

- 2467 After this worksheet has been created, place your answer for each exercise that
- 2468 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 2469 start tag of each fold which indicates the exercise the fold contains the solution
- 2470 to. The folds you create should look similar to this one:

```
2471 %mathpiper,title="Exercise 1"
```

- 2472 //Sample fold.
- 2473 %/mathpiper

- 2474 If an exercise uses the MathPiper console instead of a fold, copy the work you
- 2475 did in the console into the worksheet so it can be saved but do not put it in a fold.

2476 **13.8.1 Exercise 1**

- 2477 Carefully read all of section 13 up to this point. Evaluate each one of
- 2478 the examples in the sections you read in the MathPiper worksheet you
- 2479 created or in the MathPiper console and verify that the results match the
- 2480 ones in the book. Copy all of the console examples you evaluated into your
- 2481 worksheet so they will be saved but do not put them in a fold.

2482 **13.8.2 Exercise 2**

- 2483 Create a program which uses a While loop to print the even integers from 2
- 2484 to 50 inclusive.

2485 **13.8.3 Exercise 3**

- 2486 Create a program which prints all the multiples of 5 between 5 and 50
- 2487 inclusive.

2488 **13.8.4 Exercise 4**

- 2489 Create a program which simulates the flipping of a single coin 500 times.
- 2490 Print the number of times the coin came up heads and the number of times it
- 2491 came up tails after the loop is finished executing.

2503

14 Predicate Functions

```
A predicate function is a function that either returns True or False. Most
2493
     predicate functions in MathPiper have names which begin with "Is". For
2494
     example, IsEven(), IsOdd(), IsInteger(), etc. The following examples show
2495
     some of the predicate functions that are in MathPiper:
2496
2497
      In> IsEven(4)
2498
     Result> True
2499
     In> IsEven(5)
2500
     Result> False
2501
     In> IsZero(0)
2502
    Result> True
```

2505

In> IsZero(1) 2504 Result> False

- In> IsNegativeInteger(-1) 2506 Result> True
- 2507 In> IsNegativeInteger(1)
- 2508 Result> False
- 2509 In> IsPrime(7)
- 2510 Result> True
- 2511 In> IsPrime(100)
- 2512 Result> False
- There is also an **IsBound()** predicate function that can be used to determine 2513
- whether or not a value is bound to a given variable: 2514

```
2515
     In> a
2516 Result> a
2517
     In> IsBound(a)
2518
    Result> False
2519
     In> a := 1
2520
     Result> 1
2521
     In> IsBound(a)
2522
    Result> True
```

2523 In> Clear(a)

Result> True

```
2525 In> a
2526 Result> a
2527 In> IsBound(a)
2528 Result> False
```

- 2529 The complete list of predicate functions is contained in the **User**
- 2530 **Functions/Predicates** node in the MathPiperDocs plugin.

14.1 Finding Prime Numbers With A Loop

- 2532 Predicate functions are very powerful when they are combined with loops
- 2533 because they can be used to automatically make numerous checks. The
- 2534 following program uses a While loop to pass the integers 1 through 20 (one at a
- 2535 time) to the **IsPrime()** function in order to determine which integers are prime
- 2536 and which integers are not prime:

```
2537
      %mathpiper
2538
      //Determine which numbers between 1 and 20 (inclusive) are prime.
2539
     x := 1;
2540
     While (x \leq= 20)
2541
2542
          primeStatus := IsPrime(x);
2543
2544
          Echo(x, "is prime: ", primeStatus);
2545
2546
          x := x + 1;
2547
     ];
2548
      %/mathpiper
2549
          %output, preserve="false"
2550
            Result: True
2551
2552
            Side Effects:
2553
            1 is prime: False
2554
            2 is prime: True
2555
            3 is prime: True
2556
            4 is prime: False
2557
            5 is prime: True
2558
            6 is prime: False
2559
            7 is prime: True
2560
            8 is prime: False
2561
            9 is prime: False
2562
            10 is prime: False
2563
            11 is prime: True
2564
            12 is prime: False
```

```
2565
            13 is prime: True
2566
            14 is prime: False
2567
            15 is prime: False
2568
            16 is prime: False
2569
            17 is prime: True
2570
            18 is prime: False
2571
            19 is prime: True
2572
            20 is prime: False
2573
          %/output
      This program worked fairly well, but it is limited because it prints a line for each
2574
2575
      prime number and also each non-prime number. This means that if large ranges
2576
      of integers were processed, enormous amounts of output would be produced.
      The following program solves this problem by using an If() function to only print
2577
2578
      a number if it is prime:
2579
      %mathpiper
2580
      //Print the prime numbers between 1 and 50 (inclusive).
2581
      x := 1;
2582
      While (x \leq 50)
2583
2584
          primeStatus := IsPrime(x);
2585
2586
          If(primeStatus = True, Write(x,,));
2587
2588
          x := x + 1;
2589
      1;
2590
      %/mathpiper
2591
          %output, preserve="false"
2592
            Result: True
2593
2594
            Side Effects:
2595
            2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,
2596
          %/output
      This program is able to process a much larger range of numbers than the
2597
      previous one without having its output fill up the text area. However, the
2598
2599
      program itself can be shortened by moving the IsPrime() function inside of the
      If() function instead of using the primeStatus variable to communicate with it:
2600
```

2601 %mathpiper

/*

```
2603
          Print the prime numbers between 1 and 50 (inclusive).
2604
          This is a shorter version which places the IsPrime() function
2605
          inside of the If() function instead of using a variable.
2606
2607
     x := 1;
2608
     While (x \leq 50)
2609
2610
          If (IsPrime(x), Write(x,,));
2611
2612
          x := x + 1;
2613
     ];
2614
     %/mathpiper
2615
          %output, preserve="false"
2616
            Result: True
2617
2618
            Side Effects:
2619
            2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,
2620
    . %/output
```

2621 14.2 Finding The Length Of A String With The Length() Function

Strings can contain zero or more characters and the **Length()** function can be used to determine how many characters a string holds:

```
2624 In> s := "Red"
2625 Result> "Red"
2626 In> Length(s)
2627 Result> 3
```

- 2628 In this example, the string "Red" is assigned to the variable $\bf s$ and then $\bf s$ is
- passed to the **Length()** function. The **Length()** function returned a **3** which
- 2630 means the string contained **3 characters**.
- 2631 The following example shows that strings can also be passed to functions
- 2632 directly:

```
2633 In> Length("Red")
2634 Result> 3
```

- 2635 An **empty string** is represented by **two double quote marks with no space in**
- 2636 **between them**. The **length** of an empty string is **0**:

```
2637 In> Length("")
2638 Result> 0
```

2639 14.3 Converting Numbers To Strings With The String() Function

- 2640 Sometimes it is useful to convert a number to a string so that the individual
- 2641 digits in the number can be analyzed or manipulated. The following example
- shows a **number** being converted to a **string** with the **String()** function so that
- 2643 its **leftmost** and **rightmost** digits can be placed into **variables**:

```
2644
     In> number := 523
2645
     Result> 523
2646
     In> stringNumber := String(number)
2647
     Result> "523"
2648
     In> leftmostDigit := stringNumber[1]
2649
     Result> "5"
2650
     In> rightmostDigit := stringNumber[ Length(stringNumber) ]
2651
     Result> "3"
```

- Notice that the Length() function is used here to determine which character in
- 2653 **stringNumber** held the **rightmost** digit. Also, keep in mind that when numbers
- are in string form, operations such as +, -, *, and / cannot be performed on
- 2655 them.

2656 14.4 Finding Prime Numbers Which End With 7 (And Multi-line Function

- 2657 **Calls**)
- Now that we have covered how to turn a number into a string, lets use this
- 2659 ability inside a loop. The following program finds all the **prime numbers**
- between 1 and 500 which have a 7 as their rightmost digit. There are three
- 2661 important things which are shown in this program:
- 1) Function calls **can have their parameters placed on more than one**line if the parameters are too long to fit on a **single line**. In this case, a long code block is being placed inside of an If() function.
- 2665 2) Code blocks (which are considered to be compound expressions) **cannot**2666 **have a semicolon placed after them if they are in a function call**. If a
 2667 semicolon is placed after this code block, an error will be produced.
- 3) If() functions can be placed inside of other If() functions in order to make more complex decisions. This is referred to as **nesting** functions.
- 2670 When the program is executed, it finds 24 prime numbers which have 7 as their

2671 rightmost digit:

```
2672
     %mathpiper
2673
2674
          Find all the prime numbers between 1 and 500 which have a 7
2675
          as their rightmost digit.
     */
2676
2677
     x := 1;
2678
     While (x <= 500)
2679
          //Notice how function parameters can be put on more than one line.
2680
2681
          If (IsPrime(x),
2682
              Γ
2683
                  stringVersionOfNumber := String(x);
2684
2685
                  stringLength := Length(stringVersionOfNumber);
2686
2687
                  //Notice that If() functions can be placed inside of other
2688
                  // If() functions.
2689
                  If(stringVersionOfNumber[stringLength] = "7", Write(x,,) );
2690
2691
              ] //Notice that semicolons cannot be placed after code blocks
2692
                //which are in function calls.
2693
2694
          ); //This is the close parentheses for the outer If() function.
2695
2696
          x := x + 1;
2697
     1;
2698
      %/mathpiper
2699
          %output, preserve="false"
2700
            Result: True
2701
2702
            Side Effects:
2703
            7,17,37,47,67,97,107,127,137,157,167,197,227,257,277,307,317,
2704
            337, 347, 367, 397, 457, 467, 487,
2705
          %/output
```

It would be nice if we had the ability to store these numbers someplace so that they could be processed further and this is discussed in the next section.

14.5 Exercises

- 2709 For the following exercises, create a new MathRider worksheet file called
- 2710 book_1_section_14_exercises_<your first name>_<your last name>.mrw.
- 2711 (Note: there are no spaces in this file name). For example, John Smith's

- 2712 worksheet would be called:
- 2713 book_1_section_14_exercises_john_smith.mrw.
- 2714 After this worksheet has been created, place your answer for each exercise that
- 2715 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 2716 start tag of each fold which indicates the exercise the fold contains the solution
- 2717 to. The folds you create should look similar to this one:
- 2718 %mathpiper,title="Exercise 1"
- 2719 //Sample fold.
- 2720 %/mathpiper
- 2721 If an exercise uses the MathPiper console instead of a fold, copy the work you
- 2722 did in the console into the worksheet so it can be saved but do not put it in a fold.
- 2723 **14.5.1 Exercise 1**
- 2724 Write a program which uses a While loop to determine how many prime numbers
- 2725 there are between 1 and 1000. You do not need to print the numbers
- 2726 themselves, just how many there are.
- 2727 14.5.2 Exercise 2
- 2728 Write a program which uses a While loop to print all of the prime numbers
- 2729 between 10 and 99 which contain the digit 3 in either their 1's place or
- 2730 their 10's place.

15 Lists: Values That Hold Sequences Of Expressions

- 2732 The **list** value type is designed to hold expressions in an **ordered collection** or
- 2733 **sequence**. Lists are very flexible and they are one of the most heavily used
- value types in MathPiper. Lists can **hold expressions of any type**, they can be
- 2735 made to **grow and shrink as needed**, and they can be **nested**. Expressions in a
- 2736 list can be accessed by their position in the list (similar to the way that
- 2737 characters in a string are accessed) and they can also be **replaced by other**
- 2738 **expressions**.

2731

- 2739 One way to create a list is by placing zero or more expressions separated by
- 2740 commas inside of a **pair of braces {}**. In the following example, a list is created
- 2741 that contains various expressions and then it is assigned to the variable \mathbf{x} :

```
2742    In> exampleList := {7,42,"Hello",1/2,var}
2743    Result> {7,42,"Hello",1/2,var}
2744    In> exampleList
```

- 2745 Result> {7,42,"Hello",1/2,var}
- 2746 The number of expressions in a list can be determined with the **Length()**
- 2747 function:

```
2748 In> Length({7,42,"Hello",1/2,var})
2749 Result> 5
```

- 2750 A single expression in a list can be accessed by placing a set of **brackets** [] to
- 2751 the right of the variable that is bound to the list and then putting the
- 2752 expression's position number inside of the brackets (**Note: the first expression**
- 2753 in the list is at position 1 counting from the left end of the list):

```
2754
     In> exampleList[1]
2755
     Result> 7
2756
     In> exampleList[2]
2757
     Result> 42
2758
     In> exampleList[3]
2759
     Result> "Hello"
2760
     In> exampleList[4]
2761
     Result> 1/2
2762
     In> exampleList[5]
```

Result> var

2763

2764 The **1st** and **2nd** expressions in this list are **integers**, the **3rd** expression is a

- string, the 4th expression is a rational number and the 5th expression is an
- 2766 **unbound variable**.
- 2767 Lists can also hold other lists as shown in the following example:

```
2768  In> exampleList := {20, 30, {31, 32, 33}, 40}
2769  Result> {20,30,{31,32,33},40}

2770  In> exampleList[1]
2771  Result> 20

2772  In> exampleList[2]
2773  Result> 30
```

- 2774 In> exampleList[3]
- 2775 Result> {31,32,33}
- 2776 In> exampleList[4]
- 2777 Result> 40
- 2778
- 2779 The expression in the **3rd** position in the list is another **list** which contains the
- 2780 integers **31**, **32**, and **33**.
- 2781 An expression in this second list can be accessed by two **two sets of brackets**:
- 2782 In> exampleList[3][2] 2783 Result> 32
- 2784 The **3** inside of the first set of brackets accesses the **3rd** member of the **first** list
- 2785 and the **2** inside of the second set of brackets accesses the **2nd** member of the
- 2786 **second** list.

2787 15.1 Append() & Nondestructive List Operations

```
Append(list, expression)
```

2788 The **Append()** function adds an expression to the end of a list:

```
2789    In> testList := {21,22,23}
2790    Result> {21,22,23}

2791    In> Append(testList, 24)
2792    Result> {21,22,23,24}
```

- 2793 However, instead of changing the **original** list, **Append()** creates a **copy** of the
- original list and appends the expression to the copy. This can be confirmed by
- evaluating the variable **testList** after the **Append()** function has been called:

%/mathpiper

```
2796
     In> testList
2797
      Result> {21,22,23}
2798
      Notice that the list that is bound to testList was not modified by the Append()
      function. This is called a nondestructive list operation and most MathPiper
2799
      functions that manipulate lists do so nondestructively. To have the new list
2800
2801
      bound to the variable that is being used, the following technique can be
      employed:
2802
2803
      In> testList := \{21, 22, 23\}
2804
      Result> {21,22,23}
2805
      In> testList := Append(testList, 24)
2806
      Result> {21,22,23,24}
2807
      In> testList
2808
      Result> {21,22,23,24}
      After this code has been executed, the new list has indeed been bound to
2809
      testList as desired.
2810
      There are some functions, such as DestructiveAppend(), which do change the
2811
      original list and most of them begin with the word "Destructive". These are
2812
      called "destructive functions" and they are advanced functions which are not
2813
      covered in this book.
2814
      15.2 Using While Loops With Lists
2815
2816
      Functions that loop can be used to select each expression in a list in turn so
      that an operation can be performed on these expressions. The following
2817
      program uses a While loop to print each of the expressions in a list:
2818
2819
      %mathpiper
2820
      //Print each number in the list.
2821
      testList := \{55, 93, 40, 21, 7, 24, 15, 14, 82\};
2822
      index := 1;
2823
      While(index <= Length(testList))</pre>
2824
2825
          Echo(index, "- ", testList[index]);
2826
          index := index + 1;
2827
      ];
```

```
2829
          %output, preserve="false"
2830
            Result: True
2831
2832
            Side Effects:
2833
            1 - 55
            2 - 93
2834
2835
            3 - 40
2836
             4 - 21
2837
            5 - 7
2838
            6 - 24
            7 - 15
2839
2840
            8 - 14
2841
            9 - 82
2842
          %/output
```

A **loop** can also be used to search through a list. The following program uses a **While()** function and an **If()** function to search through a list to see if it contains the number **53**. If 53 is found in the list, a message is printed:

```
2846
      %mathpiper
2847
      //Determine if 53 is in the list.
2848
      testList := \{18, 26, 32, 42, 53, 43, 54, 6, 97, 41\};
2849
      index := 1;
2850
      While(index <= Length(testList))</pre>
2851
2852
          If(testList[index] = 53,
2853
              Echo("53 was found in the list at position", index));
2854
2855
          index := index + 1;
2856
     ];
2857
      %/mathpiper
2858
          %output, preserve="false"
2859
            Result: True
2860
2861
            Side Effects:
2862
            53 was found in the list at position 5
2863
          %/output
```

When this program was executed, it determined that **53** was present in the list at position **5**.

%mathpiper

2866

2874

15.2.1 Using A While Loop And Append() To Place Values Into A List

In an earlier section it was mentioned that it would be nice if we could store a set of values for later processing and this can be done with a **While loop** and the **Append()** function. The following program creates an empty list and assigned it to the variable **primes**. The **While loop** and the **IsPrime()** function is then used to locate the prime integers between 1 and 50 and the **Append()** function is used to place them in the list. The last part of the program then prints some information about the numbers that were placed into the list:

```
2875
     //Place the prime numbers between 1 and 50 (inclusive) into a list.
2876
     //Create an empty list.
2877
     primesList := {};
2878
     index := 1;
2879
     While (index <= 50)
2880
2881
          /*
2882
              If x is prime, append it to the end of the list and then assign
2883
              the new list that is created to the variable 'primes'.
          * /
2884
2885
          If(IsPrime(index), primesList := Append(primesList, index ) );
2886
2887
          index := index + 1;
2888
     ];
2889
     //Print information about the primes that were found.
2890
     Echo("Primes ", primesList);
2891
     Echo ("The number of primes in the list = ", Length (primesList) );
     Echo("The first number in the list = ", primesList[1] );
2892
2893
      %/mathpiper
2894
          %output,preserve="false"
2895
            Result: True
2896
2897
            Side Effects:
2898
            Primes {2,3,5,7,11,13,17,19,23,29,31,37,41,43,47}
2899
            The number of primes in the list = 15
2900
            The first number in the list = 2
2901
          %/output
```

The ability to place values into a list with a loop is very powerful and we will be using this ability throughout the rest of the book.

2904 **15.3 Exercises**

- 2905 For the following exercises, create a new MathRider worksheet file called
- 2906 book_1_section_15a_exercises_<your first name>_<your last name>.mrw.
- 2907 (Note: there are no spaces in this file name). For example, John Smith's
- 2908 worksheet would be called:
- 2909 book_1_section_15a_exercises_john_smith.mrw.
- 2910 After this worksheet has been created, place your answer for each exercise that
- 2911 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 2912 start tag of each fold which indicates the exercise the fold contains the solution
- 2913 to. The folds you create should look similar to this one:
- 2914 %mathpiper, title="Exercise 1"
- 2915 //Sample fold.
- 2916 %/mathpiper
- 2917 If an exercise uses the MathPiper console instead of a fold, copy the work you
- 2918 did in the console into the worksheet so it can be saved but do not put it in a fold.

2919 **15.3.1 Exercise 1**

- 2920 Create a program that uses a While loop and an IsOdd() predicate function
- 2921 to analyze the following list and then print the number of odd numbers it
- 2922 contains.
- 2923 {73,94,80,37,56,94,40,21,7,24,15,14,82,93,32,74,22,68,65,52,85,61,46,86,25}

2924 **15.3.2 Exercise 2**

- 2925 Create a program that uses a While loop and an IsNegativeNumber() function
- 2926 to copy all of the negative numbers in the following list into a new list.
- 2927 Use the variable negativeNumbersList to hold the new list. Print the
- 2928 contents of the list after it has been created.
- 2929 {36, -29, -33, -6, 14, 7, -16, -3, -14, 37, -38, -8, -45, -21, -26, 6, 6, 38, -20, 33, 41, -
- 2930 4,24,37,40,29}

2931 **15.3.3 Exercise 3**

- 2932 Create one program that uses a single While loop to analyze the following
- 2933 list and then print the following information about it:
- 2934 1) The largest number in the list.
- 2935 2) The smallest number in the list.
- 2936 3) The sum of all the numbers in the list.

{73,12,80,37,56,94,40,21,7,24,15,14,82,93,32,74,22,68,65,52,85,61,46,86,25}

```
2938
     Hint: the following program finds the largest number in a list and it can
2939
     be used as a starting point for solving this exercise.
2940
     %mathpiper
2941
2942
      The variable that keeps track of the largest number encountered so
2943
      far needs to be initialized to the lowest possible value it may
2944
      hold. Whv?
2945
      * /
2946
     largest := 0;
2947
     numbersList := \{4,6,7,9,2,1,3\};
2948
     index := 1;
2949
     While(index <= Length(numbersList) )</pre>
2950
2951
          Echo("Largest: ", largest);
2952
2953
          If (numbersList[index] > largest, largest := numbersList[index]);
2954
2955
          index := index + 1;
2956
     ];
2957
     Echo ("The largest number in the list is: ", largest);
2958
     %/mathpiper
```

2959 15.4 The ForEach() Looping Function

- 2960 The **ForEach()** function uses a **loop** to index through a list like the While()
- 2961 function does, but it is more flexible and automatic. ForEach() also uses bodied
- 2962 notation like the While() function and here is its calling format:

```
ForEach(variable, list) body
```

- 2963 **ForEach()** selects each expression in a list in turn, assigns it to the passed-in
- 2964 "variable", and then executes the expressions that are inside of "body".
- 2965 Therefore, body is **executed once for each expression in the list**.

2966 15.5 Print All The Values In A List Using A ForEach() function

2967 This example shows how ForEach() can be used to print all of the items in a list:

```
2968
      %mathpiper
2969
      //Print all values in a list.
2970
      ForEach (value, {50,51,52,53,54,55,56,57,58,59})
2971
2972
          Echo (value);
2973
      ];
2974
      %/mathpiper
2975
          %output,preserve="false"
2976
             Result: True
2977
2978
             Side Effects:
2979
             50
2980
             51
2981
             52
2982
             53
2983
             54
2984
             55
2985
             56
2986
             57
2987
             58
2988
             59
2989 .
          %/output
```

2990 15.6 Calculate The Sum Of The Numbers In A List Using ForEach()

In previous examples, counting code in the form $\mathbf{x} := \mathbf{x} + \mathbf{1}$ was used to count how many times a While loop was executed. The following program uses a ForEach() function and a line of code similar to this counter to calculate the

sum of the numbers in a list:

```
2995
      %mathpiper
2996
2997
      This program calculates the sum of the numbers
2998
        in a list.
2999
      * /
3000
      //This variable is used to accumulate the sum.
3001
      sum := 0;
3002
      ForEach (number, {1,2,3,4,5,6,7,8,9,10})
3003
3004
3005
            Add the contents of x to the contents of sum
```

```
3006
            and place the result back into sum.
3007
3008
          sum := sum + number;
3009
3010
          //Print the sum as it is being accumulated.
3011
          Write(sum,,);
3012
     ];
3013
     NewLine(); NewLine();
3014
     Echo("The sum of the numbers in the list = ", sum);
3015
      %/mathpiper
3016
          %output, preserve="false"
3017
            Result: True
3018
3019
            Side Effects:
3020
            1,3,6,10,15,21,28,36,45,55,
3021
3022
            The sum of the numbers in the list = 55
3023
          %/output
```

- In the above program, the integers **1** through **10** were manually placed into a list
- 3025 by typing them individually. This method is limited because only a relatively
- 3026 small number of integers can be placed into a list this way. The following section
- 3027 discusses an operator which can be used to automatically place a large number
- 3028 of integers into a list with very little typing.

15.7 The .. Range Operator

```
first .. last
```

- 3030 A programmer often needs to create a list which contains consecutive integers
- and the .. "range" operator can be used to do this. The first integer in the list is
- 3032 placed before the .. operator and the **last** integer in the list is placed after it
- 3033 (Note: there must be a space immediately to the left of the .. operator
- and a space immediately to the right of it or an error will be generated.).
- 3035 Here are some examples:

```
3036 In> 1 .. 10

3037 Result> {1,2,3,4,5,6,7,8,9,10}

3038 In> 10 .. 1

3039 Result> {10,9,8,7,6,5,4,3,2,1}

3040 In> 1 .. 100

3041 Result> {1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,
```

3080

73,79,83,89,97,

```
3042
               21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37,
3043
               38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54,
3044
               55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71,
3045
               72,73,74,75,76,77,78,79,80,81,82,83,84,85,86,87,88,
               89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100}
3046
3047
      In > -10 .. 10
3048
      Result> \{-10, -9, -8, -7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}
3049
      As these examples show, the .. operator can generate lists of integers in
      ascending order and descending order. It can also generate lists that are very
3050
3051
      large and ones that contain negative integers.
      Remember, though, if one or both of the spaces around the .. are omitted, an
3052
3053
      error is generated:
3054
      In>1..3
3055
      Result>
3056
      Error parsing expression, near token .3.
      15.8 Using ForEach() With The Range Operator To Print The Prime
3057
      Numbers Between 1 And 100
3058
      The following program shows how to use a ForEach() function instead of a
3059
      While() function to print the prime numbers between 1 and 100. Notice that
3060
3061
      loops that are implemented with ForEach() often require less typing than
      their While() based equivalents:
3062
3063
      %mathpiper
3064
3065
        This program prints the prime integers between 1 and 100 using
3066
        a ForEach() function instead of a While() function. Notice that
3067
        the ForEach() version requires less typing than the While()
3068
        version.
      */
3069
3070
      ForEach (number, 1 .. 100)
3071
3072
          If (IsPrime (number), Write (number,,) );
3073
      ];
3074
      %/mathpiper
3075
          %output,preserve="false"
3076
            Result: True
3077
3078
            Side Effects:
```

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71,

3081 . %/output

15.8.1 Using ForEach() And The Range Operator To Place The Prime Numbers Between 1 And 50 Into A List

A ForEach() function can also be used to place values in a list, just the While() function can:

```
3086
     %mathpiper
3087
3088
      Place the prime numbers between 1 and 50 into
3089
       a list using a ForEach() function.
3090
3091
     //Create a new list.
3092
     primesList := {};
3093
     ForEach (number, 1 .. 50)
3094
3095
          /*
3096
            If number is prime, append it to the end of the list and
3097
            then assign the new list that is created to the variable
3098
            'primes'.
3099
3100
          If(IsPrime(number), primesList := Append(primesList, number));
3101
     ];
3102
     //Print information about the primes that were found.
3103
     Echo("Primes ", primesList);
3104
     Echo("The number of primes in the list = ", Length(primesList) );
3105
     Echo("The first number in the list = ", primesList[1] );
3106
     %/mathpiper
3107
          %output,preserve="false"
3108
            Result: True
3109
3110
            Side Effects:
3111
            Primes {2,3,5,7,11,13,17,19,23,29,31,37,41,43,47}
3112
            The number of primes in the list = 15
3113
            The first number in the list = 2
3114
         %/output
```

As can be seen from the above examples, the **ForEach()** function and the **range** operator can do a significant amount of work with very little typing. You will

discover in the next section that MathPiper has functions which are even more

3118 powerful than these two.

3119 **15.8.2 Exercises**

- 3120 For the following exercises, create a new MathRider worksheet file called
- 3121 book_1_section_15b_exercises_<your first name>_<your last name>.mrw.
- 3122 (Note: there are no spaces in this file name). For example, John Smith's
- 3123 worksheet would be called:
- 3124 book_1_section_15b_exercises_john_smith.mrw.
- 3125 After this worksheet has been created, place your answer for each exercise that
- 3126 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 3127 start tag of each fold which indicates the exercise the fold contains the solution
- 3128 to. The folds you create should look similar to this one:
- 3129 %mathpiper, title="Exercise 1"
- 3130 //Sample fold.
- 3131 %/mathpiper
- 3132 If an exercise uses the MathPiper console instead of a fold, copy the work you
- 3133 did in the console into the worksheet so it can be saved but do not put it in a fold.

3134 **15.8.3 Exercise 1**

- 3135 Create a program that uses a ForEach() function and an IsOdd() predicate
- 3136 function to analyze the following list and then print the number of odd
- 3137 numbers it contains.
- 3138 {73,94,80,37,56,94,40,21,7,24,15,14,82,93,32,74,22,68,65,52,85,61,46,86,25}

3139 **15.8.4 Exercise 2**

- 3140 Create a program that uses a ForEach() function and an IsNegativeNumber()
- 3141 function to copy all of the negative numbers in the following list into a
- 3142 new list. Use the variable negativeNumbersList to hold the new list.
- 3143 Print the contents of the list after it has been created.
- 3145 4,24,37,40,29}

3146 **15.8.5 Exercise 3**

- 3147 Create one program that uses a single ForEach() function to analyze the
- 3148 following list and then print the following information about it:
- 3149 1) The largest number in the list.
- 3150 2) The smallest number in the list.
- 3151 3) The sum of all the numbers in the list.

- 3152 {73,94,80,37,56,94,40,21,7,24,15,14,82,93,32,74,22,68,65,52,85,61,46,86,25}
- 3153 **15.8.6 Exercise 4**
- 3154 Create one program that does the following: 1) uses a While loop to make a
- 3155 list that contains 1000 random integers between 1 and 100 inclusive. 2)
- 3156 uses a ForEach() function to determine how many integers in the list are
- 3157 **prime** and use an **Echo()** function to print this total.

3158 16 Functions & Operators Which Loop Internally

- Looping is such a useful capability that MathPiper has many functions which
- 3160 loop internally. Now that you have some experience with loops, you can use this
- 3161 experience to help you imagine how these functions use loops to process the
- 3162 information that is passed to them.

3163 16.1 Functions & Operators Which Loop Internally To Process Lists

3164 This section discusses a number of functions that use loops to process lists.

3165 **16.1.1 TableForm()**

```
TableForm(list)
```

- The **TableForm()** function prints the contents of a list in the form of a table.
- 3167 Each member in the list is printed on its own line and this sometimes makes the
- 3168 contents of the list easier to read:

```
3169
      In> testList := \{2,4,6,8,10,12,14,16,18,20\}
3170
      Result> {2,4,6,8,10,12,14,16,18,20}
3171
      In> TableForm(testList)
3172
      Result> True
3173
      Side Effects>
3174
      2
3175
      4
3176
      6
3177
      8
3178
      10
3179
      12
3180
      14
3181
      16
3182
      18
3183
      20
```

3184 **16.1.2 Contains()**

The **Contains()** function searches a list to determine if it contains a given expression. If it finds the expression, it returns **True** and if it doesn't find the

3187 expression, it returns **False**. Here is the calling format for Contains():

```
Contains(list, expression)
```

3188 The following code shows Contains() being used to locate a number in a list:

3193 The **Not()** function can also be used with predicate functions like Contains() to

3194 change their results to the opposite truth value:

```
3195 In> Not Contains(\{50, 51, 52, 53, 54, 55, 56, 57, 58, 59\}, 75)
3196 Result> True
```

3197 **16.1.3 Find()**

```
Find(list, expression)
```

- 3198 The **Find()** function searches a list for the first occurrence of a given expression.
- 3199 If the expression is found, the **position of its first occurrence** is returned and
- 3200 if it is not found, **-1** is returned:

```
3201 In> Find({23, 15, 67, 98, 64}, 15)
3202 Result> 2

3203 In> Find({23, 15, 67, 98, 64}, 8)
3204 Result> -1
```

3205 **16.1.4 Count()**

```
Count(list, expression)
```

3206 **Count()** determines the number of times a given expression occurs in a list:

```
3207
      In> testList := \{a,b,b,c,c,c,d,d,d,d,e,e,e,e,e\}
3208
     Result> {a,b,b,c,c,c,d,d,d,d,e,e,e,e,e,e}
3209
      In> Count(testList, c)
3210
     Result> 3
3211
      In> Count(testList, e)
3212
     Result> 5
3213
     In> Count(testList, z)
3214
     Result> 0
```

3215 **16.1.5 Select()**

```
Select(predicate function, list)
```

- 3216 **Select()** returns a list that contains all the expressions in a list which make a
- 3217 given predicate function return **True**:

```
3218 In> Select("IsPositiveInteger", {46,87,59,-27,11,86,-21,-58,-86,-52})
```

- 3219 Result> {46,87,59,11,86}
- 3220 In this example, notice that the **name** of the predicate function is passed to
- 3221 Select() in **double quotes**. There are other ways to pass a predicate function to
- 3222 Select() but these are covered in a later section.
- 3223 Here are some further examples which use the Select() function:

```
3224 In> Select("IsOdd", {16,14,82,92,33,74,99,67,65,52})
```

- 3225 Result> {33,99,67,65}
- 3226 In> Select("IsEven", {16,14,82,92,33,74,99,67,65,52})
- 3227 Result> {16,14,82,92,74,52}
- 3228 In> Select("IsPrime", 1 .. 75)
- 3229 Result> {2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,53,59,61,67,71,73}
- 3230 Notice how the third example uses the .. operator to automatically generate a list
- of consecutive integers from 1 to 75 for the Select() function to analyze.

3232 **16.1.6 The Nth() Function & The [] Operator**

```
Nth(list, index)
```

- 3233 The **Nth()** function simply returns the expression which is at a given position in
- 3234 a list. This example shows the **third** expression in a list being obtained:

```
3235 In> testList := \{a,b,c,d,e,f,g\}
```

- 3236 Result> {a,b,c,d,e,f,g}
- 3237 In> Nth(testList, 3)
- 3238 Result> c
- 3239 As discussed earlier, the [] operator can also be used to obtain a single
- 3240 expression from a list:

```
3241
      In> testList[3]
3242
      Result> c
3243
3244
```

The [] operator can even obtain a single expression directly from a list without

needing to use a variable:

```
3245
      In> \{a,b,c,d,e,f,g\} [3]
3246
      Result> c
```

16.1.7 The : Prepend Operator 3247

```
expression : list
```

The prepend operator is a colon: and it can be used to add an expression to the 3248

3249 beginning of a list:

```
3250
     In> testList := {b,c,d}
3251
    Result> {b,c,d}
3252
     In> testList := a:testList
3253
     Result> {a,b,c,d}
```

16.1.8 Concat() 3254

```
Concat(list1, list2, ...)
```

- The Concat() function is short for "concatenate" which means to join together 3255
- 3256 sequentially. It takes two or more lists and joins them together into a single
- 3257 larger list:

```
3258
      In> Concat(\{a,b,c\}, \{1,2,3\}, \{x,y,z\})
3259
      Result> \{a,b,c,1,2,3,x,y,z\}
```

16.1.9 Insert(), Delete(), & Replace() 3260

```
Insert(list, index, expression)
```

```
Delete(list, index)
```

```
Replace(list, index, expression)
```

- 3261 **Insert()** inserts an expression into a list at a given index, **Delete()** deletes an
- 3262 expression from a list at a given index, and **Replace()** replaces an expression in
- 3263 a list at a given index with another expression:

```
3264
     In> testList := \{a,b,c,d,e,f,g\}
3265
     Result> {a,b,c,d,e,f,q}
3266
     In> testList := Insert(testList, 4, 123)
3267
     Result> {a,b,c,123,d,e,f,g}
3268
     In> testList := Delete(testList, 4)
3269
     Result> {a,b,c,d,e,f,q}
3270
     In> testList := Replace(testList, 4, xxx)
3271
     Result> {a,b,c,xxx,e,f,g}
```

3272 **16.1.10 Take()**

```
Take(list, amount)
Take(list, -amount)
Take(list, {begin_index,end_index})
```

- 3273 **Take()** obtains a sublist from the **beginning** of a list, the **end** of a list, or the
- 3274 **middle** of a list. The expressions in the list that are not taken are discarded.
- 3275 A **positive** integer passed to Take() indicates how many expressions should be
- 3276 taken from the **beginning** of a list:

```
3277    In> testList := {a,b,c,d,e,f,g}
3278    Result> {a,b,c,d,e,f,g}

3279    In> Take(testList, 3)
3280    Result> {a,b,c}
```

- 3281 A **negative** integer passed to Take() indicates how many expressions should be
- 3282 taken from the **end** of a list:

```
3283 In> Take(testList, -3)
3284 Result> {e,f,g}
```

- Finally, if a **two member list** is passed to Take() it indicates the **range** of
- 3286 expressions that should be taken from the **middle** of a list. The **first** value in the
- 3287 passed-in list specifies the **beginning** index of the range and the **second** value
- 3288 specifies its **end**:

```
3289 In> Take(testList, {3,5})
3290 Result> {c,d,e}
```

3291 **16.1.11 Drop()**

```
Drop(list, index)
Drop(list, -index)
Drop(list, {begin_index,end_index})
```

- 3292 **Drop()** does the opposite of Take() in that it **drops** expressions from the
- 3293 **beginning** of a list, the **end** of a list, or the **middle** of a list and **returns a list**
- 3294 which contains the remaining expressions.
- 3295 A **positive** integer passed to Drop() indicates how many expressions should be
- 3296 dropped from the **beginning** of a list:

```
3297    In> testList := {a,b,c,d,e,f,g}
3298    Result> {a,b,c,d,e,f,g}

3299    In> Drop(testList, 3)
3300    Result> {d,e,f,g}
```

- 3301 A **negative** integer passed to Drop() indicates how many expressions should be
- 3302 dropped from the **end** of a list:

```
3303 In> Drop(testList, -3)
3304 Result> {a,b,c,d}
```

- Finally, if a **two member list** is passed to Drop() it indicates the **range** of
- 3306 expressions that should be dropped from the **middle** of a list. The **first** value in
- 3307 the passed-in list specifies the **beginning** index of the range and the **second**
- 3308 value specifies its **end**:

```
3309 In> Drop(testList, {3,5})
3310 Result> {a,b,f,g}
```

3311 **16.1.12 FillList()**

```
FillList(expression, length)
```

- 3312 The FillList() function simply creates a list which is of size "length" and fills it
- 3313 with "length" copies of the given expression:

```
3314 In> FillList(a, 5)
3315 Result> {a,a,a,a,a}

3316 In> FillList(42,8)
3317 Result> {42,42,42,42,42,42,42,42}
```

3318 16.1.13 RemoveDuplicates()

RemoveDuplicates(list)

- 3319 **RemoveDuplicates()** removes any duplicate expressions that are contained in a
- 3320 list:

```
3321 In> testList := \{a,a,b,c,c,b,b,a,b,c,c\}
```

- 3322 Result> {a,a,b,c,c,b,b,a,b,c,c}
- 3323 In> RemoveDuplicates(testList)
- 3324 Result> {a,b,c}

3325 **16.1.14 Reverse()**

Reverse(list)

- 3326 **Reverse()** reverses the order of the expressions in a list:
- 3327 In> testList := $\{a,b,c,d,e,f,g,h\}$
- 3328 Result> $\{a,b,c,d,e,f,g,h\}$
- 3329 In> Reverse (testList)
- 3330 Result> $\{h,g,f,e,d,c,b,a\}$

3331 **16.1.15 Partition()**

Partition(list, partition_size)

- 3332 The **Partition()** function breaks a list into sublists of size "partition size":
- 3333 In> testList := $\{a,b,c,d,e,f,g,h\}$
- 3334 Result> $\{a,b,c,d,e,f,g,h\}$
- 3335 In> Partition(testList, 2)
- 3336 Result> {{a,b},{c,d},{e,f},{g,h}}
- 3337 If the partition size does not divide the length of the list **evenly**, the remaining
- 3338 elements are discarded:
- 3339 In> Partition(testList, 3)
- 3340 Result> $\{\{a,b,c\},\{d,e,f\}\}$

- 3341 The number of elements that Partition() will discard can be calculated by
- dividing the length of a list by the partition size and obtaining the **remainder**:
- 3343 In> Length(testList) % 3
- 3344 Result> 2
- Remember that % is the remainder operator. It divides two integers and returns
- 3346 their remainder.

3347 **16.1.16 Table()**

```
Table(expression, variable, begin_value, end_value, step_amount)
```

- 3348 The Table() function creates a list of values by doing the following:
- 1) Generating a sequence of values between a "begin_value" and an
 "end value" with each value being incremented by the "step amount".
- 2) Placing each value in the sequence into the specified "variable", one value at a time.
- 3) Evaluating the defined "expression" (which contains the defined "variable") for each value, one at a time.
- 3355 4) Placing the result of each "expression" evaluation into the result list.
- 3356 This example generates a list which contains the integers 1 through 10:

```
3357 In> Table(x, x, 1, 10, 1)
3358 Result> {1,2,3,4,5,6,7,8,9,10}
```

- Notice that the expression in this example is simply the variable 'x' itself with no
- 3360 other operations performed on it.
- 3361 The following example is similar to the previous one except that its expression
- 3362 multiplies 'x' by 2:

```
3363 In> Table(x*2, x, 1, 10, 1)
3364 Result> {2,4,6,8,10,12,14,16,18,20}
```

- 3365 Lists which contain decimal values can also be created by setting the
- 3366 "step amount" to a decimal:

```
3367 In> Table(x, x, 0, 1, .1)
3368 Result> \{0,0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9,1\}
```

3369 **16.1.17 HeapSort()**

```
HeapSort(list, compare)
```

- 3370 **HeapSort()** sorts the elements of **list** into the order indicated by **compare** with
- 3371 compare typically being the **less than** operator "<" or the **greater than**
- 3372 operator ">":

```
3373 In> HeapSort({4,7,23,53,-2,1}, "<");
```

- 3374 Result: {-2,1,4,7,23,53}
- 3375 In> HeapSort({4,7,23,53,-2,1}, ">");
- 3376 Result: {53,23,7,4,1,-2}
- 3377 In> HeapSort({1/2,3/5,7/8,5/16,3/32}, "<")
- 3378 Result: {3/32,5/16,1/2,3/5,7/8}
- 3379 In> HeapSort({.5,3/5,.76,5/16,3/32}, "<")
- 3380 Result: {3/32,5/16,.5,3/5,.76}

3381 **16.2 Functions That Work With Integers**

- 3382 This section discusses various functions which work with integers. Some of
- 3383 these functions also work with non-integer values and their use with non-
- 3384 integers is discussed in other sections.

3385 16.2.1 RandomIntegerVector()

```
RandomIntegerVector(length, lowest_possible, highest_possible)
```

- 3386 A vector is a list that does not contain other lists. **RandomIntegerVector()**
- 3387 creates a list of size "length" that contains random integers that are no lower
- 3388 than "lowest possible" and no higher than "highest possible". The following
- 3389 example creates **10** random integers between **1** and **99** inclusive:

```
3390 In> RandomIntegerVector(10, 1, 99)
```

3391 Result> {73,93,80,37,55,93,40,21,7,24}

3392 **16.2.2 Max() & Min()**

```
Max(value1, value2)
Max(list)
```

- 3393 If two values are passed to Max(), it determines which one is larger:
- 3394 In> Max(10, 20)

```
3395 Result> 20
```

3396 If a list of values are passed to Max(), it finds the largest value in the list:

```
3397    In> testList := RandomIntegerVector(10, 1, 99)
3398    Result> {73,93,80,37,55,93,40,21,7,24}

3399    In> Max(testList)
3400    Result> 93
```

3401 The **Min()** function is the opposite of the Max() function.

```
Min(value1, value2)
Min(list)
```

3402 If two values are passed to Min(), it determines which one is smaller:

```
3403 In> Min(10, 20)
3404 Result> 10
```

3405 If a list of values are passed to Min(), it finds the smallest value in the list:

```
3406    In> testList := RandomIntegerVector(10, 1, 99)
3407    Result> {73,93,80,37,55,93,40,21,7,24}

3408    In> Min(testList)
3409    Result> 7
```

3410 **16.2.3 Div() & Mod()**

```
Div(dividend, divisor)
Mod(dividend, divisor)
```

- 3411 **Div()** stands for "divide" and determines the whole number of times a divisor
- 3412 goes into a dividend:

```
3413 In> Div(7, 3)
3414 Result> 2
```

3415 **Mod()** stands for "modulo" and it determines the remainder that results when a

3416 dividend is divided by a divisor:

```
3417 In> Mod(7,3)
3418 Result> 1
```

3419 The remainder/modulo operator % can also be used to calculate a remainder:

```
3420 In> 7 % 2
3421 Result> 1
```

3422 **16.2.4 Gcd()**

```
Gcd(value1, value2)
Gcd(list)
```

- 3423 GCD stands for Greatest Common Divisor and the Gcd() function determines the
- 3424 greatest common divisor of the values that are passed to it.
- 3425 If two integers are passed to Gcd(), it calculates their greatest common divisor:

```
3426 In> Gcd(21, 56)
3427 Result> 7
```

- 3428 If a list of integers are passed to Gcd(), it finds the greatest common divisor of all
- 3429 the integers in the list:

```
3430 In> Gcd({9, 66, 123})
3431 Result> 3
```

3432 **16.2.5** Lcm()

```
Lcm(value1, value2)
Lcm(list)
```

- 3433 LCM stands for Least Common Multiple and the Lcm() function determines the
- least common multiple of the values that are passed to it.
- 3435 If two integers are passed to Lcm(), it calculates their least common multiple:

```
3436 In> Lcm(14, 8)
3437 Result> 56
```

- 3438 If a list of integers are passed to Lcm(), it finds the least common multiple of all
- 3439 the integers in the list:

```
3440 In> Lcm({3,7,9,11})
3441 Result> 693
```

3442 **16.2.6 Sum()**

```
Sum(list)
```

- 3443 **Sum()** can find the sum of a list that is passed to it:
- 3444 In> testList := RandomIntegerVector(10,1,99)
- 3445 Result> {73,93,80,37,55,93,40,21,7,24}
- 3446 In> Sum(testList)
- 3447 Result> 523
- 3448 In> testList := 1 .. 10
- 3449 Result> {1,2,3,4,5,6,7,8,9,10}
- 3450 In> Sum(testList)
- 3451 Result> 55

3452 **16.2.7 Product()**

Product(list)

- 3453 This function has two calling formats, only one of which is discussed here.
- 3454 Product(list) multiplies all the expressions in a list together and returns their
- 3455 product:
- 3456 In> Product({1,2,3})
- 3457 Result> 6

3458 **16.3 Exercises**

- 3459 For the following exercises, create a new MathRider worksheet file called
- 3460 book_1_section_16_exercises_<your first name> <your last name>.mrw.
- 3461 (Note: there are no spaces in this file name). For example, John Smith's
- 3462 worksheet would be called:
- 3463 book 1 section 16 exercises john smith.mrw.
- 3464 After this worksheet has been created, place your answer for each exercise that
- requires a fold into its own fold in this worksheet. Place a title attribute in the
- 3466 start tag of each fold which indicates the exercise the fold contains the solution
- to. The folds you create should look similar to this one:
- 3468 %mathpiper, title="Exercise 1"
- 3469 //Sample fold.

- 3470 %/mathpiper
- 3471 If an exercise uses the MathPiper console instead of a fold, copy the work you
- 3472 did in the console into the worksheet so it can be saved but do not put it in a fold.

3473 **16.3.1 Exercise 1**

- 3474 Create a program that uses RandomIntegerVector() to create a 100 member
- 3475 list that contains random integers between 1 and 5 inclusive. Use one
- 3476 Count() call in a loop to determine how many of each digit 1-5 are in the
- 3477 list and then print this information. Hint: you can use the HeapSort()
- 3478 function to sort the generated list to make it easier to check if your
- 3479 program is counting correctly.

3480 **16.3.2 Exercise 2**

- 3481 Create a program that uses RandomIntegerVector() to create a 100 member
- 3482 list that contains random integers between 1 and 50 inclusive and use
- 3483 Contains() to determine if the number 25 is in the list. Print "25 was in
- 3484 the list." if 25 was found in the list and "25 was not in the list." if it
- 3485 wasn't found.

3486 **16.3.3 Exercise 3**

- 3487 Create a program that uses RandomIntegerVector() to create a 100 member
- 3488 list that contains random integers between 1 and 50 inclusive and use
- 3489 Find() to determine if the number 10 is in the list. Print the position of
- 3490 10 if it was found in the list and "10 was not in the list." if it wasn't
- 3491 found.

3492 **16.3.4 Exercise 4**

- 3493 Create a program that uses RandomIntegerVector() to create a 100 member
- 3494 list that contains random integers between 0 and 3 inclusive. Use Select()
- 3495 with the IsNonZeroInteger() predicate function to obtain all of the nonzero
- 3496 integers in this list.

3497 **16.3.5 Exercise 5**

- 3498 Create a program that uses **Table()** to obtain a list which contains the
- 3499 squares of the integers between 1 and 10 inclusive.

17 Nested Loops

- Now that you have seen how to solve problems with single loops, it is time to
- 3502 discuss what can be done when a loop is placed inside of another loop. A loop
- 3503 that is placed **inside** of another loop it is called a **nested loop** and this nesting
- 3504 can be extended to numerous levels if needed. This means that loop 1 can have
- loop 2 placed inside of it, loop 2 can have loop 3 placed inside of it, loop 3 can
- 3506 have loop 4 placed inside of it, and so on.
- Nesting loops allows the programmer to accomplish an enormous amount of
- 3508 work with very little typing.

17.1 Generate All The Combinations That Can Be Entered Into A Two Digit Wheel Lock Using A Nested Loop



- 3511 The following program generates all the combinations that can be entered into a
- 3512 two digit wheel lock. It uses a nested loop to accomplish this with the "inside"
- nested loop being used to generate **one's place** digits and the "**outside**" loop
- 3514 being used to generate **ten's place** digits.

```
3515 %mathpiper
3516 /*
3517    Generate all the combinations can be entered into a two
3518    digit wheel lock.
3519 */
3520 combinationsList := {};
3521 ForEach(digit1, 0 .. 9) //This loop is called the "outside" loop.
```

```
3522
      [
3523
          ForEach (digit2, 0 .. 9) //This loop is called the "inside" loop.
3524
3525
               combinationsList := Append(combinationsList, {digit1, digit2});
3526
          ];
3527
      ];
      Echo (TableForm (combinationsList));
3528
3529
      %/mathpiper
3530
          %output, preserve="false"
3531
            Result: True
3532
3533
            Side Effects:
3534
            {0,0}
3535
            {0,1}
3536
            {0,2}
3537
            {0,3}
3538
             \{0,4\}
3539
            {0,5}
3540
            {0,6}
3541
3542
               . //The middle of the list has not been shown.
3543
3544
            {9,3}
3545
            {9,4}
3546
            {9,5}
3547
            {9,6}
3548
            {9,7}
3549
            {9,8}
3550
            {9,9}
3551
            True
3552 .
          %/output
```

- 3553 The relationship between the outside loop and the inside loop is interesting
- because each time the **outside loop cycles once**, the **inside loop cycles 10**
- 3555 **times**. Study this program carefully because nested loops can be used to solve a
- 3556 wide range of problems and therefore understanding how they work is
- 3557 important.

3558 **17.2 Exercises**

- 3559 For the following exercises, create a new MathRider worksheet file called
- 3560 book 1 section 17 exercises <your first name> <your last name>.mrw.
- 3561 (Note: there are no spaces in this file name). For example, John Smith's
- 3562 worksheet would be called:
- 3563 book 1 section 17 exercises john smith.mrw.

- 3564 After this worksheet has been created, place your answer for each exercise that
- 3565 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 3566 start tag of each fold which indicates the exercise the fold contains the solution
- 3567 to. The folds you create should look similar to this one:
- 3568 %mathpiper, title="Exercise 1"
- 3569 //Sample fold.
- 3570 %/mathpiper
- 3571 If an exercise uses the MathPiper console instead of a fold, copy the work you
- 3572 did in the console into the worksheet so it can be saved but do not put it in a fold.
- 3573 **17.2.1 Exercise 1**
- 3574 Create a program that will generate all of the combinations that can be
- 3575 entered into a three digit wheel lock. (Hint: a triple nested loop can be
- 3576 used to accomplish this.)

18 User Defined Functions

- 3578 In computer programming, a **function** is a named section of code that can be
- 3579 **called** from other sections of code. **Values** can be sent to a function for
- processing as part of the **call** and a function always returns a value as its result.
- 3581 A function can also generate side effects when it is called and side effects have
- 3582 been covered in earlier sections.
- 3583 The values that are sent to a function when it is called are called **arguments** or
- actual parameters and a function can accept 0 or more of them. These
- 3585 arguments are placed within parentheses.
- 3586 MathPiper has many predefined functions (some of which have been discussed in
- 3587 previous sections) but users can create their own functions too. The following
- program creates a function called **addNums()** which takes two numbers as
- arguments, adds them together, and returns their sum back to the calling code
- 3590 as a result:

3577

- 3591 In> addNums(num1, num2) := num1 + num2
- 3592 Result> True
- 3593 This line of code defined a new function called **addNums** and specified that it
- will accept two values when it is called. The **first** value will be placed into the
- variable **num1** and the **second** value will be placed into the variable **num2**.
- 3596 Variables like num1 and num2 which are used in a function to accept values from
- 3597 calling code are called **formal parameters**. **Formal parameter variables** are
- 3598 used inside a function to process the values/actual parameters/arguments
- 3599 that were placed into them by the calling code.
- 3600 The code on the **right side** of the **assignment operator** is **bound** to the
- 3601 function name "addNums" and it is executed each time addNums() is called.
- 3602 The following example shows the new **addNums()** function being called multiple
- 3603 times with different values being passed to it:
- 3604 In> addNums(2,3)
- 3605 Result> 5
- 3606 In> addNums (4,5)
- 3607 Result> 9
- 3608 In> addNums(9,1)
- 3609 Result> 10
- 3610 Notice that, unlike the functions that come with MathPiper, we chose to have this
- 3611 function's name start with a **lower case letter**. We could have had addNums()
- begin with an upper case letter but it is a **convention** in MathPiper for **user**

defined function names to begin with a lower case letter to distinguish
 them from the functions that come with MathPiper.

The values that are returned from user defined functions can also be assigned to variables. The following example uses a %mathpiper fold to define a function called **evenIntegers()** and then this function is used in the MathPiper console to assign a list of even integers to the variable "a":

```
3619
      %mathpiper
3620
     evenIntegers (endInteger) :=
3621
      [
3622
          resultList := {};
3623
          x := 2;
3624
3625
          While(x <= endInteger)</pre>
3626
3627
              resultList := Append(resultList, x);
3628
              x := x + 2;
3629
          ];
3630
3631
3632
           The result of the last expression which is executed in a function
3633
           is the result that the function returns to the caller. In this case,
3634
           resultList is purposely being executed last so that its contents are
           returned to the caller.
3635
3636
          */
3637
          resultList;
3638
     ];
3639
      %/mathpiper
3640
          %output,preserve="false"
3641
            Result: True
3642
     . %/output
3643
     In> a := evenIntegers(10)
3644
     Result> {2,4,6,8,10}
3645
      In> Length(a)
3646
     Result> 5
```

The function **evenIntegers()** returns a list which contains all the even integers from 2 up through the value that was passed into it. The fold was first executed in order to define the **evenIntegers()** function and make it ready for use. The **evenIntegers()** function was then called from the MathPiper console and 10 was passed to it.

- After the function was finished executing, it returned a list of even integers as a 3652
- result and this result was assigned to the variable 'a'. We then passed the list 3653
- that was assigned to 'a' to the **Length()** function in order to determine its size. 3654

18.1 Global Variables, Local Variables, & Local()

- The new evenIntegers() function seems to work well, but there is a problem. 3656
- 3657 The variables 'x' and resultList were defined inside the function as global
- **variables** which means they are accessible from anywhere, including from 3658
- 3659 within other functions, within other folds (as shown here):

```
3660
      %mathpiper
      Echo(x, ",", resultList);
3661
3662
      %/mathpiper
3663
          %output, preserve="false"
3664
            Result: True
3665
3666
             Side Effects:
3667
             12 , {2,4,6,8,10}
3668
          %/output
```

3669 and from within the MathPiper console:

```
3670
      In> x
3671
      Result> 12
3672
      In> resultList
3673
      Result> \{2, 4, 6, 8, 10\}
```

Using global variables inside of functions is usually not a good idea 3674

- because code in other functions and folds might already be using (or will use) the 3675
- same variable names. Global variables which have the same name are the same 3676
- variable. When one section of code changes the value of a given global variable, 3677
- the value is changed everywhere that variable is used and this will eventually 3678
- 3679 cause problems.
- In order to prevent errors being caused by global variables having the same 3680
- name, a function named Local() can be called inside of a function to define what 3681
- are called **local variables**. A **local variable** is only accessible inside the 3682
- function it has been defined in, even if it has the same name as a global variable. 3683
- The following example shows a second version of the **evenIntegers()** function 3684
- which uses **Local()** to make 'x' and **resultList** local variables: 3685

```
3686
     %mathpiper
3687
3688
     This version of evenIntegers() uses Local() to make
3689
      x and resultList local variables
3690
3691
      evenIntegers (endInteger) :=
3692
3693
          Local(x, resultList);
3694
3695
          resultList := {};
3696
          x := 2;
3697
3698
          While(x <= endInteger)</pre>
3699
3700
              resultList := Append(resultList, x);
3701
              x := x + 2;
3702
          ];
3703
3704
3705
           The result of the last expression which is executed in a function
3706
           is the result that the function returns to the caller. In this case,
3707
           resultList is purposely being executed last so that its contents are
3708
           returned to the caller.
3709
3710
          resultList;
3711
    1;
3712
      %/mathpiper
3713
          %output, preserve="false"
3714
            Result: True
3715
          %/output
     We can verify that 'x' and resultList are now local variables by first clearing
3716
      them, calling evenIntegers(), and then seeing what 'x' and resultList contain:
3717
3718
     In> Clear(x, resultList)
3719
     Result> True
3720
     In> evenIntegers(10)
3721
     Result> \{2,4,6,8,10\}
3722
     In> x
3723 Result> x
3724 In> resultList
```

- 3725 Result> resultList
- 3726 **18.2 Exercises**
- 3727 For the following exercises, create a new MathRider worksheet file called
- 3728 book 1 section 18 exercises <your first name> <your last name>.mrw.
- 3729 (Note: there are no spaces in this file name). For example, John Smith's
- 3730 worksheet would be called:
- 3731 **book_1_section_18_exercises_john_smith.mrw**.
- 3732 After this worksheet has been created, place your answer for each exercise that
- 3733 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 3734 start tag of each fold which indicates the exercise the fold contains the solution
- 3735 to. The folds you create should look similar to this one:
- 3736 %mathpiper, title="Exercise 1"
- 3737 //Sample fold.
- 3738 %/mathpiper
- 3739 If an exercise uses the MathPiper console instead of a fold, copy the work you
- 3740 did in the console into the worksheet so it can be saved but do not put it in a fold.
- 3741 **18.2.1 Exercise 1**
- 3742 Create a function called tenOddIntegers() which returns a list which
- 3743 contains 10 random odd integers between 1 and 99 inclusive.
- 3744 **18.2.2 Exercise 2**
- 3745 Create a function called convertStringToList(string) which takes a string
- 3746 as a parameter and returns a list which contains all of the characters in
- 3747 the string. Here is an example of how the function should work:
- 3748 In> convertStringToList("Hello friend!")
- 3749 Result> {"H", "e", "l", "l", "o", " ", "f", "r", "i", "e", "n", "d", "!"}
- 3750 In> convertStringToList("Computer Algebra System")
- 3751 Result> {"C", "o", "m", "p", "u", "t", "e", "r", " ", "A", "l", "g", "e", "b", "r", "a", "
- 3752 ","s","y","s","t","e","m"}

19 Miscellaneous topics

3754 19.1 Incrementing And Decrementing Variables With The ++ And --

3755 **Operators**

3753

3761

- 3756 Up until this point we have been adding 1 to a variable with code in the form of \mathbf{x}
- 3757 := $\mathbf{x} + \mathbf{1}$ and subtracting 1 from a variable with code in the form of $\mathbf{x} := \mathbf{x} \mathbf{1}$.
- 3758 Another name for **adding** 1 to a variable is **incrementing** it and **decrementing**
- 3759 a variable means to **subtract** 1 from it. Now that you have had some experience
- with these longer forms, it is time to show you shorter versions of them.

19.1.1 Incrementing Variables With The ++ Operator

3762 The number 1 can be added to a variable by simply placing the ++ operator after

3763 it like this:

```
3764 In> x := 1

3765 Result: 1

3766 In> x++;

3767 Result: True

3768 In> x

3769 Result: 2
```

3770 Here is a program that uses the ++ operator to increment a loop index variable:

```
3771
      %mathpiper
3772
      index := 1;
3773
      While(index <= 10)</pre>
3774
3775
          Echo (index);
3776
3777
          index++; //The ++ operator increments the index variable.
3778
      ];
3779
      %/mathpiper
3780
          %output,preserve="false"
3781
             Result: True
3782
3783
             Side Effects:
3784
3785
             2
```

```
3786
             3
3787
3788
             5
3789
             6
3790
             7
3791
3792
             9
3793
             10
3794
     . %/output
```

19.1.2 Decrementing Variables With The -- Operator

The number 1 can be subtracted from a variable by simply placing the -operator after it like this:

```
3798 In> x := 1

3799 Result: 1

3800 In> x--;

3801 Result: True

3802 In> x

3803 Result: 0
```

3804 Here is a program that uses the -- operator to decrement a loop index variable:

```
3805
      %mathpiper
3806
      index := 10;
3807
      While (index >= 1)
3808
3809
          Echo(index);
3810
3811
          index--; //The -- operator decrements the index variable.
3812
      ];
3813
      %/mathpiper
3814
          %output,preserve="false"
3815
            Result: True
3816
3817
            Side Effects:
3818
             10
3819
             9
3820
            8
3821
            7
3822
             6
3823
             5
```

```
3824 4
3825 3
3826 2
3827 1
3828 %/output
```

19.1.3 The Break() Function

3830 The **Break()** function is used to end a loop early and here is its calling format:

```
Break()
```

The following program has a While loop which is configured to loop 10 times.
However, when the loop counter variable **index** reaches 5, the Break() function is called and this causes the loop to end early:

```
3834
      %mathpiper
3835
3836
      index := 1;
3837
3838
      While (index <= 10)
3839
3840
          Echo(index);
3841
3842
           If (index = 5, Break());
3843
3844
           index++;
3845
      ];
3846
3847
      %/mathpiper
3848
           %output,preserve="false"
3849
             Result: True
3850
3851
             Side Effects:
3852
             1
3853
             2
3854
             3
3855
             4
3856
             5
3857
           %/output
```

When a Break() function is used to end a loop, it is called "**breaking out**" of the loop. Notice that only the numbers 1-5 are printed in this program.

19.1.4 The Continue() Function

The **Continue()** function is similar to the Break() function, except that instead of ending the loop, it simply causes it to **skip the remainder of the loop for the** current loop iteration. Here is the Continue() function's calling format:

```
Continue()
```

The following program uses a While loop which is configured to print the integers from 0 to 8. However, the Continue() function is used to skip the execution of the Echo() function when the loop indexing variable **index** is equal to 5:

```
3868
      %mathpiper
3869
3870
      index := 0;
3871
3872
      While (index < 8)
3873
3874
           index++;
3875
           If(index = 5, Continue());
3876
3877
3878
           Echo (index);
3879
      ];
3880
      %/mathpiper
3881
           %output, preserve="false"
3882
             Result: True
3883
3884
             Side Effects:
3885
3886
             2
             3
3887
3888
             4
3889
             6
3890
             7
3891
3892
           %/output
```

Notice that the number 5 is not printed when this program is executed.

19.1.5 The Repeat() Function

3894

3895 The Repeat() function is a looping function which is similar to While() and

ForEach(), but it is simpler than these two. Here are the two calling formats for Repeat():

```
Repeat(count) body
Repeat() body
```

The first version of Repeat() simply takes an integer argument which indicates how many times it should loop. The following program shows how to use Repeat() to print 4 copies of the word "Hello":

```
3901
      %mathpiper
3902
3903
      Repeat (4)
3904
3905
          Echo("Hello");
3906
      ];
3907
3908
      %/mathpiper
3909
           %output, preserve="false"
3910
             Result: 4
3911
3912
             Side Effects:
3913
             Hello
3914
             Hello
3915
             Hello
3916
             Hello
3917
          %/output
```

The second version of Repeat() does not take any arguments and it is designed to run as an **infinite loop**. The Break() function is then used to make the Repeat() function stop looping. The following program would print the loop indexing variable **index** forever, but the Break() function is used to stop the loop after **3** iterations:

```
3933
          index := index + 1;
3934
      1;
3935
3936
      Echo("Loop count: ", loopCount);
3937
3938
      %/mathpiper
3939
          %output, preserve="false"
3940
            Result: True
3941
3942
            Side Effects:
3943
3944
             2
3945
             3
3946
            Loop count: 2
3947
          %/output
```

Notice that Repeat() returns the number of times it actually looped as a result and that this information is assigned to the variable **loopCount**.

19.1.6 The EchoTime() Function

3950

- 3951 Computers are extremely fast, but they still take time to execute programs.
- 3952 Sometimes it is important to determine how long it takes to evaluate a given
- 3953 expression in order to do things like determine if a section of code need to run
- 3954 quicker than it currently is or determine if one piece of code is slower than
- 3955 another. The EchoTime() function is a bodied function which is used to time
- 3956 **how long a section of code takes to run** and here is its calling format:

```
EchoTime()expression
```

The following examples use EchoTime() to determine how long it takes to add the numbers 2 and 3 together and how long it takes to factor 1234567:

```
3959
      In> EchoTime() 2 + 3
3960
     Result: 5
3961
     Side Effects:
3962
     0.000080946 seconds taken.
3963
     In> EchoTime() Factor(1234567)
3964
     Result: 127*9721
3965
     Side Effects:
3966
     0.395028773 seconds taken.
```

3967 In the following program, a ForEach loop is used to have the Factor() function

factor all the numbers in a list. The EchoTime() function is used to determine how long it takes to do all the factoring:

```
3970
     %mathpiper
3971
3972
     EchoTime() ForEach(number, {100,54,65,67,344,98,454})
3973
3974
          Echo(number, " - ", Factor(number));
3975
      ];
3976
3977
     %/mathpiper
3978
          %output,preserve="false"
3979
            Result: True
3980
3981
            Side Effects:
3982
            100 - 2^2*5^2
3983
            54 - 2*3^3
3984
            65 - 5*13
3985
            67 - 67
3986
            344 - 2^3*43
3987
            98 - 2*7^2
3988
            454 - 2*227
3989
            0.262678978 seconds taken.
3990
     . %/output
```

Finally, the following program show how to time a code block which prints the numbers from 1 to 100:

```
3993
      %mathpiper
3994
3995
      EchoTime()
3996
3997
           index := 1;
3998
3999
           While(index <= 100)</pre>
4000
4001
               Write(index,,);
4002
4003
               If (index % 10 = 0, NewLine());
4004
4005
               index++;
4006
           ];
4007
4008
          NewLine();
4009
      ];
4010
      %/mathpiper
```

```
4011
           %output,preserve="false"
4012
              Result: True
4013
4014
              Side Effects:
4015
              1,2,3,4,5,6,7,8,9,10,
4016
              11, 12, 13, 14, 15, 16, 17, 18, 19, 20,
4017
              21, 22, 23, 24, 25, 26, 27, 28, 29, 30,
4018
              31, 32, 33, 34, 35, 36, 37, 38, 39, 40,
              41, 42, 43, 44, 45, 46, 47, 48, 49, 50,
4019
4020
              51, 52, 53, 54, 55, 56, 57, 58, 59, 60,
4021
              61,62,63,64,65,66,67,68,69,70,
4022
              71,72,73,74,75,76,77,78,79,80,
4023
              81,82,83,84,85,86,87,88,89,90,
4024
              91, 92, 93, 94, 95, 96, 97, 98, 99, 100,
4025
4026
              0.055418423 seconds taken.
4027
           %/output
```

4028 **19.2 Exercises**

- 4029 For the following exercises, create a new MathRider worksheet file called
- 4030 book_1_section_19_exercises_<your first name>_<your last name>.mrw.
- 4031 (Note: there are no spaces in this file name). For example, John Smith's
- 4032 worksheet would be called:
- 4033 **book_1_section_19_exercises_john_smith.mrw**.
- 4034 After this worksheet has been created, place your answer for each exercise that
- 4035 requires a fold into its own fold in this worksheet. Place a title attribute in the
- 4036 start tag of each fold which indicates the exercise the fold contains the solution
- 4037 to. The folds you create should look similar to this one:
- 4038 %mathpiper,title="Exercise 1"
- 4039 //Sample fold.
- 4040 %/mathpiper
- 4041 If an exercise uses the MathPiper console instead of a fold, copy the work you
- did in the console into the worksheet so it can be saved but do not put it in a fold.

4043 **19.2.1 Exercise 1**

- 4044 Create a program which uses a While loop to display the numbers from 1 to 4045 50. Use the ++ operator to increment the loop index variable.
- 4046 19.2.2 Exercise 2
- 4047 Create a program which uses a While loop to display the numbers from 1 to

- 4048 50 in reverse order. Use the -- operator to decrement the loop index
- 4049 variable.

4050 19.2.3 Exercise 3

- 4051 Create a program which uses a Continue() function to cause a While loop
- 4052 which is configured to print the numbers from 1 to 100 to skip printing the
- 4053 number 72.

4054 19.2.4 Exercise 4

- 4055 Create a program which uses the version of the Repeat() function which
- 4056 takes an integer as an argument and the : string concatenation operator to
- 4057 print the following:
- 4058 Hello
- 4059 HelloHello
- 4060 HelloHelloHello
- 4061 HelloHelloHello
- 4062 HelloHelloHelloHello
- 4063 Hint:
- 4064 In> string := "Hi"
- 4065 Result: "Hi"
- 4066 In> string := string : "Hi"
- 4067 Result: "HiHi"

4068 **19.2.5 Exercise 5**

- 4069 In the last example in the EchoTime() section, what operator is being used
- 4070 to format the output into lines of 10 numbers and how is this operator
- 4071 doing this?