6502 Programming

by Ted Kosan

Part of The Professor And Pat series (professorandpat.org)

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1 Pat Returns From A Visit

- 2 It had been almost a week since Pat had last stopped by. I was just
- 3 beginning to wonder if Pat had decided that learning how to program a
- 4 computer was too much effort when I heard a knock at my door. I opened
- 5 the door and there stood Pat, wearing a big frown.
- 6 "Come in Pat." I said in a cheerful voice. "What are you so 'happy' about?"
- 7 "My family spent all last week visiting friends and I wasn't able to work with
- 8 assembly language at all!" said Pat. "And when I told people that I was
- 9 learning how a computer worked, they didn't seem to understand what I
- 10 was talking about when I tried to explain it to them. I felt like I was alone in
- 11 a strange way during this trip, even though I was surrounded by people. Do
- 12 you kind of know what I mean, professor?"
- 13 I smiled and nodded my head. "Oh yes, I know what you mean, Pat. Most
- 14 people that study technical subjects have this problem and the more you
- 15 learn, the worse it gets."
- 16 After a few moments of thought I added "You could always stop learning
- 17 about computers and perhaps devote your time to learning something more
- 18 common, like a sport. This should give you plenty to talk about the next
- 19 time you go visiting."
- 20 "No way!" said Pat with determination. "I'm never going to give up learning
- 21 about computers! Ever since I started learning about computers, it feels
- 22 like I've entered a whole new world which is full of wonder and unexpected
- possibilities. I haven't told you this before, but sometimes I get little pangs
- $\,$ 24 $\,$ of fear about losing the knowledge of computers I have gained, like I
- 25 learned it all in a dream and when I wake up, the knowledge will be gone. I
- 26 wouldn't trade my knowledge of computers for anything in the world, not
- 27 even for a cure for the loneliness I felt."
- 28 "As a technologist, you will indeed need to live with a certain amount of
- 29 loneliness," I said "but only in certain situations like your visit.
- 30 Fortunately, there are millions of people in the world who are deep
- 31 technologists. They are very easy to communicate with through the
- 32 Internet and they will understand exactly what you are talking about. Over
- 33 time, you will find that the relationships you form with people on the
- 34 Internet who have the same interests as you do will more than make up for
- 35 the loneliness you experience in other areas of your life."

- 36 "Thanks, professor!" Pat said with a smile. "That lifted my spirits a bit."
- 37 I smiled too as Pat's face brightened.
- 38 "Do you know what would make me feel even better, though?" asked Pat.
- 39 "What?" I asked.
- 40 "If you told me more about how programming worked." replied Pat. "When
- 41 I watch you create a program, you make it look so easy and I seem to
- 42 understand most of what you are doing. By the time I get home, though, my
- 43 understanding gets fuzzy and I become confused. Thats why I want to talk
- 44 more about programming and how to do it properly.
- 45 I understand how most of the instructions we have been using work, but I
- 46 don't guite get how to arrange the instructions into sequences that can
- 47 solve problems. It seems to me that a lot of programming exists at a level
- 48 that is above the instructions themselves, but I just can't see it yet."

49 Algorithms

- 50 "You are correct about a significant part of programming existing at a level
- 51 that is above the level of the instructions, Pat." I said. "A computer
- 52 programmer certainly needs to know at least one programming language,
- 53 but when a programmer solves a problem, they do it at a level that is higher
- 54 in abstraction than even the more abstract computer languages.
- 55 After the problem is solved, then the solution is encoded into a
- 56 programming language. It is almost as if a programmer is actually two
- 57 people. The first person is the **problem solver** and the second person is
- 58 the **coder**. The reason that programming may seem confusing to you is
- 59 that, when you have watched me program you have only seen the coding
- 60 phase and not the problem solving phase which I have been doing in my
- 61 head.
- 62 I have been doing the problem solving phase in my head because the
- 63 programs we have developed up to this point have been simple. With more
- 64 complex programs, however, the problem solving phase and the coding
- 65 phase are more distinct. The solution to a problem is usually recorded and
- 66 then passed from the **problem solver** to the **coder** in the form of a
- 67 document."

- 68 "Are you saying that the problem solver can solve a programming problem
- 69 without even turning on the computer?" asked Pat.
- 70 "Yes." I replied "The first thing that a problem solver will do with a problem
- 71 is to **analyze** it. This is an extremely important step because if a problem is
- 72 not analyzed, then it can not be properly solved."
- 73 "What does analyze mean?" asked Pat.
- 74 "To **analyze** something means to break it down into its component parts
- 75 and then these parts are studied to determine how they work." I replied. "A
- 76 well known saying is 'divide and conquer' and when a difficult problem is
- analyzed, it is broken down into smaller problems which are each simpler to
- 78 solve than the overall problem. The **problem solver** then develops an
- 79 **algorithm** to solve each of the simpler problems and, when these
- 80 algorithms are combined, they form the solution to the overall problem."
- 81 "An algo-what?" asked Pat.
- 82 "An al-gor-rhythm." I said. "An **algorithm** is a sequence of instructions
- 83 which describe how to accomplish a given task. These instructions can be
- 84 expressed in various ways including writing them in natural languages (like
- 85 English), drawing diagrams of them, and encoding them in a programming
- 86 language.
- 87 The concept of an algorithm came from the various procedures that
- 88 mathematicians developed for solving mathematical problems, like
- 89 calculating the sum of 2 numbers or calculating their product.
- 90 Algorithms can also be used to solve more general problems. An example
- 91 would be the set of instructions that could be followed by a person who
- 92 needs to solve the garage sizing problem we discussed earlier." I then
- 93 wrote the following algorithm on the whiteboard:
- 94 1) Measure the length and width of each item that will be placed into the
- 95 garage using metric units and record these measurements.
- 96 2) Divide the measurements from step 1 by 100 then cut out pieces of paper
- 97 that match these dimensions to serve as models of the original items.
- 98 3) Cut out a piece of paper which is 1.5 times as long as the model of the
- 99 largest car and 3 times wider than it to serve as a model of the garage floor.

- 100 4) Locate where the garage doors will be placed on the model of the garage
- 101 floor, mark the locations with a pencil, and place the models of both cars on
- 102 top of the model of the garage floor, just within the perimeter of the paper
- 103 and between the two pencil marks.
- 104 5) Place the models of the items on top of the model of the garage floor in
- 105 the empty space that is not being occupied by the models of the cars.
- 106 6) Move the models of the items into various positions within this empty
- 107 space to determine how well all the items will fit within this size garage.
- 108 7) If the fit is acceptable, go to step 10.
- 109 8) If there is not enough room in the garage, increase the length dimension,
- 110 the width dimension (or both dimensions) of the garage floor model by 10%,
- 111 create a new garage floor model, and go to step 4.
- 112 9) If there is too much room in the garage, decrease the length dimension,
- 113 the width dimension (or both dimensions) of the garage model by 10%, create
- a new garage floor model, and go to step 4.
- 115 10) Measure the length and width dimensions of the garage floor model,
- 116 multiply these dimensions by 100, and then build the garage using these
- 117 larger dimensions.
- 118 "That's a lot of steps!" said Pat.
- "Yes," I said "an algorithm needs to be detailed enough so that it leads to
- 120 the desired solution if it is followed exactly. This often results in an
- 121 algorithm having a significant number of steps. After the steps have been
- developed and recorded in a document, however, they can be followed over
- and over again by people who need to solve the given problem."
- 124 "This algorithm for the garage sizing problem is written in English
- 125 sentences." said Pat. "Are algorithms usually written using sentences
- before being encoded into programs, or can they be encoded into a
- 127 programming language right from the start?"
- 128 "An algorithm is usually not expressed in a programming language while it
- 129 is being developed and this is why a computer does not need to be turned
- 130 on during algorithm development. After the algorithm is complete and
- 131 recorded in a document, it is then encoded into a programming language as
- 132 a separate step."
- 133 "What happens if the program that the algorithm was encoded into doesn't

- 134 run correctly when it is executed?" asked Pat.
- 135 "Assuming that the **syntax** of the program is correct," I replied "the
- problem will usually be 1) an incorrect algorithm that was encoded
- 137 correctly, 2) a correct algorithm that was encoded incorrectly, or 3) an
- 138 incorrect algorithm that was encoded incorrectly. The programmer needs
- 139 to study both the algorithm and the way it was encoded into a program in
- order to find the cause of the problem.
- 141 When either syntax errors or algorithm errors are present in a program, the
- program is said to have 'bugs' and the process of locating the bugs and
- 143 fixing them is known as **debugging** the program."
- "Bugs can't get inside of computer chips so why are program errors called
- 145 bugs!?" asked Pat.
- 146 I smiled and said "Bugs can not crawl inside of today's computer chips, but
- 147 the early computers used larger electrical components that bugs could
- 148 crawl into." I then found the following information on the Internet which
- 149 explained where the concept of a computer bug came from:
- 150 Date: 23 Aug 1981 05:38:25-PDT
- 151 From: ARPAVAX.sjk at Berkeley
- 152 Subject: origin of bug
- 153 Ever wondered about the origins of the term "bugs" as applied to computer
- 154 technology? U.S. Navy Capt. Grace Murray Hopper has firsthand explanation.
- 155 The 74-year-old captain, who is still on active duty, was a pioneer in
- 156 computer technology during World War II. At the C.W. Post Center of
- 157 Long Island University, Hopper told a group of Long Island public school
- administrators that the first computer "bug" was a real bug -- a moth.
- 159 At Harvard one August night in 1945, Hopper and her associates were working
- on the "granddaddy" of modern computers, the Mark I. "Things were going
- 161 badly; there was something wrong in one of the circuits of the long
- 162 glass-enclosed computer," she said. "Finally, someone located the
- 163 trouble spot and, using ordinary tweezers, removed the problem, a two-inch
- 164 moth. From then on, when anything went wrong with a computer, we said it
- 165 had bugs in it." Hopper said that when the veracity of her story was
- 166 questioned recently, "I referred them to my 1945 log book, now in the
- 167 collection of Naval Surface Weapons Center, and they found the remains of
- 168 that moth taped to the page in question."



169 "That's hilarious!" said Pat.

170 **Computation**

- 171 After a few moments of thought Pat said "I understand how a person can
- perform the steps in an algorithm, Professor, but I am having a hard time
- 173 understanding how a computer can perform these steps when its CPU is
- 174 only capable of executing simple machine language instructions."
- 175 "In order to understand how a CPU is able to perform the steps in an
- algorithm, one must first understand what **computation** (which is also
- 177 known as **calculation**) is." I said. "Lets search for some good definitions of
- 178 each of these words on the Internet and read what they have to say." I then
- 179 performed the search and selected the following 2 definitions for
- 180 **computation**:
- 181 1) The manipulation of numbers or symbols according to fixed rules. Usually
- 182 applied to the operations of an automatic electronic computer, but by
- 183 extension to some processes performed by minds or brains.
- 184 (www.informatics.susx.ac.uk/books/computers-and-thought/gloss/node1.html)
- 185 2) A computation can be seen as a purely physical phenomenon occurring inside
- 186 a closed physical system called a computer. Examples of such physical systems
- 187 include digital computers, quantum computers, DNA computers, molecular
- 188 computers, analog computers or wetware computers.

- 189 (www.informatics.susx.ac.uk/books/computers-and-thought/gloss/node1.html)
- 190 I had Pat read the definitions for computation out loud then I said "The 2
- definitions for **computation** I selected indicate that it is the 'manipulation
- 192 **of numbers or symbols according to fixed rules**' and that it 'can be
- 193 seen as a purely physical phenomenon occurring inside a closed
- 194 **physical system called a computer**.' Both definitions indicate that the
- machines we normally think of as computers are just **one type of**
- 196 **computer** and that other types of closed physical systems can also act as
- 197 computers. These other types of computers include DNA computers,
- 198 molecular computers, analog computers, and wetware computers (or
- 199 brains)."
- 200 "Are you saying that brains manipulate symbols using rules, just like normal
- 201 computers do?" asked Pat.
- 202 "Yes." I replied.
- 203 "How can brains manipulate symbols?" asked Pat. "Do they implement the
- 204 Von Neumann architecture?"
- 205 "No," I replied "brains do not implement the Von Neumann architecture,
- 206 but they do manipulate symbols using rules just like normal computers do.
- 207 Read aloud the 2 definitions for **calculation** I selected and lets see if these
- 208 definitions shed any light on the kind of rules that normal computers,
- 209 brains, and other types of computers use." Pat then read the following
- 210 definitions:
- 211 1) A calculation is a deliberate process for transforming one or more inputs
- 212 into one or more results. (en.wikipedia.org/wiki/Calculation)
- 213 2) Calculation: the procedure of calculating; determining something by
- 214 mathematical or logical methods (wordnet.princeton.edu/perl/webwn)
- 215 "These definitions for calculation," I said "indicate that it 'is a deliberate
- 216 process for transforming one or more inputs into one or more
- 217 **results**' and that this is done 'by mathematical or logical methods'. We
- 218 do not yet completely understand what mathematical and logical methods
- 219 brains use to perform calculations, but rapid progress is being made in this
- 220 area."
- 221 "What is logic?" asked Pat.

- 222 "The concept of logic is used in a number of different contexts. I will find a
- 223 definition for **logic** on the Internet which fits our context." I then located
- 224 the following definition and had Pat read it aloud:
- 225 The logic of a system is the whole structure of rules that must be used for
- 226 any reasoning within that system. Most of mathematics is based upon a well-
- 227 understood structure of rules and is considered to be highly logical. It is
- 228 always necessary to state, or otherwise have it understood, what rules are
- 229 being used before any logic can be applied. (ddi.cs.uni-
- 230 potsdam.de/Lehre/TuringLectures/MathNotions.htm)
- 231 "**Reasoning**," I said "is the process of using predefined rules to move from
- 232 one point in a system to another point in the system. For example, when a
- 233 person adds 2 numbers together on a piece of paper, they must follow the
- rules of the addition algorithm in order to obtain a correct sum. The
- addition algorithm's rules are its logic and, when someone applies these
- 236 rules during a calculation, they are **reasoning** with the rules.
- 237 Lets now apply these concepts to your question about how a computer can
- 238 perform the steps of an algorithm when its CPU is only capable of executing
- 239 simple machine language instructions. When a person develops an
- 240 algorithm, the steps in the algorithm are usually stated as high-level tasks
- 241 which do not contain all of the smaller steps that are necessary to perform
- 242 each task.
- 243 For example, a person might write a step that states 'Drive from New York
- 244 to San Francisco.' This large step can be broken down into smaller steps
- that contain instructions such as 'turn left at the intersection, go west for 10
- 246 kilometers, etc.' If all of the smaller steps in a larger step are completed,
- 247 then the larger step is completed too.
- 248 A human that needs to perform this large driving step would usually be able
- 249 to figure out what smaller steps need to be performed in order accomplish
- 250 it. As we learned earlier, however, computers are very stupid and before
- any algorithm can be executed on a computer, the algorithm's steps must be
- 252 broken down into smaller steps, and these smaller steps must be broken
- 253 down into even small steps, until the steps are simple enough to be
- 254 performed by the instruction set of a CPU."
- 255 "How many smaller steps does a larger step usually need to be broken down
- into before it can be implemented in machine language?" asked Pat.

- 257 "Sometimes only a few smaller steps are needed to implement a larger step,
- 258 but sometimes hundreds or even thousands of smaller steps are required.
- 259 Hundreds or thousands of smaller steps will translate into hundreds or
- 260 thousands of machine language instructions."
- 261 "That's a lot of steps and instructions!" said Pat. "It almost seems like its
- 262 too much work to convert an algorithm into thousands of little steps and
- 263 then into maybe thousands of assembly language instructions needed to run
- 264 it on a computer."
- 265 "You are right, Pat." I said "If assembly language was the only language
- that computers could be programmed in, then most algorithms would be too
- 267 large to be placed into a computer. It was for the purpose of solving this
- 268 problem that high-level languages were created.
- 269 With assembly language, a human needs to manually convert an algorithm
- 270 into assembly language instructions before a computer can execute the
- algorithm. An algorithm that is encoded into a high-level language,
- 272 however, does not need to be broken down into as many smaller steps as
- 273 would be needed with assembly language. The hard work of breaking down
- an algorithm that has been encoded into a high-level language is
- automatically done by either a **compiler** or an **interpreter**. This is why
- 276 most of the time, programmers use a high-level language to develop in
- 277 instead of assembly language."
- 278 "If high-level languages are so much easier to encode algorithms into than
- assembly language," said Pat "why are we studying assembly language?"
- 280 I smiled, looked at Pat, and said "For many years, I taught beginning
- 281 programming to students using the normal method of starting them with a
- 282 high-level language without covering assembly language at all. A beginning
- 283 programmer is definitely able to start writing programs quicker in a high-
- level language than they could with assembly language and I (along with
- 285 many others) thought that guicker in this case meant better.
- Over time, however, I noticed that most of these students were not able to
- 287 program very well. I eventually figured out that the main reason that most
- 288 of them could not program very well was that they did not understand how
- 289 a computer actually worked because much of this understanding is at the
- 290 assembly language level.
- 291 Even though most programmers do not program in assembly language,

- 292 somehow, having a solid understanding of how a computer works at its
- 293 lowest levels, and having had the experience of manually encoding
- algorithms into assembly language, wires a programmer's brain in a way
- that enables them to be much better high-level language programmers than
- 296 they otherwise would be.
- 297 I love assembly language, but even I prefer to program in a high-level
- 298 language whenever possible. The reason I am teaching assembly language
- 299 to you as your first computer language is because I want to give you the
- 300 foundation you will need to become an excellent high-level language
- 301 programmer."

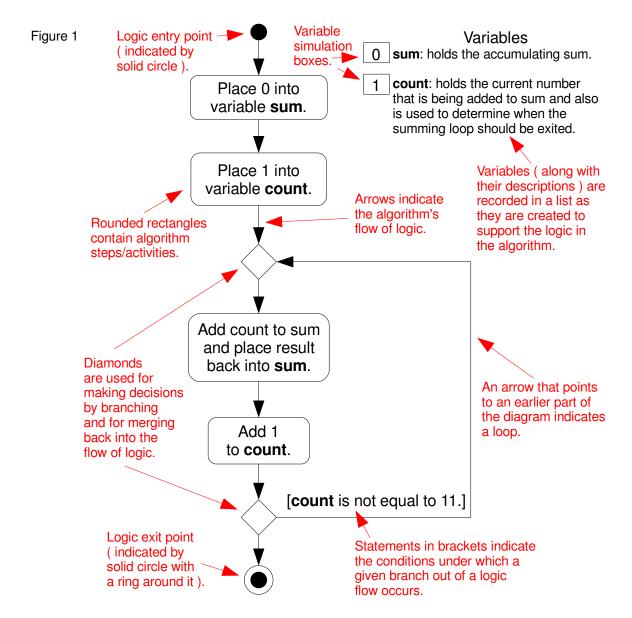
302 UML Activity Diagrams

- 303 Pat said "I think I'm beginning to understand now how a programmer
- 304 becomes a **problem solver** when they develop an algorithm and then
- 305 becomes a **coder** when they encode the algorithm into a programming
- 306 language. I would like to talk some more about how the problem solver
- 307 develops an algorithm, though.
- 308 Earlier you said that an algorithm can be recorded in a natural language
- 309 like English but it can also be recorded using a diagram. Can you show me
- 310 how recording an algorithm into a diagram would work?"
- 311 "Yes." I replied. "You may be surprised to learn, however, that a whole
- 312 diagram-based language has been created which allows all aspects of a
- 313 program to be designed by 'problem solvers', including the algorithms that
- 314 a program uses. This language is call \mathbf{UML} which stands for $\mathbf{Unified}$
- 315 **Modeling Language**. Later on, when we begin studying high-level
- 316 languages, we will cover UML in more depth. For now, though, I will show
- 317 you how one of UML's diagrams, called an Activity diagram, works.
- 318 The purpose of an **Activity diagram** is to show the sequence of steps (or
- 319 activities) that are part of some piece of logic and this makes them well
- 320 suited for recording algorithms. I will now show you how activity diagrams
- work by using them to develop algorithms which solve various problems. I
- 322 will also encode each diagram into a 6502 assembly language program so
- 323 you can see how the encoding process is done."

324 Calculating The Sum Of The Numbers Between 1 And 10

- 325 Before I began solving the first problem, I took some sheets of paper from
- 326 the printer and created 2 funny-looking hats with them using a scissors and

- tape. I wrote 'Problem Solver' on the first hat and 'Coder' on the second hat
- 328 and Pat started laughing when I put on the 'Problem Solver' hat.
- 329 "The first thing that needs to be done with a problem before it can be
- 330 analyzed and solved," I said "is to describe it clearly and accurately." I then
- 331 wrote the following problem description on the whiteboard:
- 332 **Description**: In this problem, the sum of the numbers between 1 and 10
- 333 inclusive needs to be determined.
- "Inclusive here means that the numbers 1 and 10 will be included in the
- 335 sum." I said. "Since this is a fairly simple problem that is similar to one I
- 336 solved earlier with a program, we will not need to spend too much time
- 337 analyzing it." I then developed an algorithm for solving the problem by
- 338 drawing an Activity diagram on the whiteboard. (see Fig. 1)



339 As I was developing the Activity diagram, I created variables as needed and 340 recorded their names in a list along with their descriptions. I would also 341 periodically start at the entry point and walk through the logic to make sure it was correct (I did this out loud so Pat could follow along too). I placed 342 simulation boxes next to each variable so that I could record and update 343 344 how the logic was changing the variable's values. During a walk-through, I 345 would often find errors which I would then fix by moving flow arrows and 346 adjusting the text that was inside the activity rectangles.

347 Eventually, I reached a point where I could not find any more errors in the

logic and then I said to Pat "It looks like the algorithm is complete now and I can stop being the **problem solver** and pass the algorithm over to the **coder** so it can be encoded into assembly language." I then took off the 'Problem Solver' hat and put on the 'Coder' hat and Pat started laughing again. I brought up MathRider and encoded the Activity diagram into the following 6502 assembly language program:

```
354
                      000001 | : Program Name: sum10.
                      000002 |;
355
356
                      000003 |; Version: 1.03
                      000004 |;
357
358
                      000005 |; Description: In this program, the sum of the
                             ; numbers between 1 and 10 inclusive will be
359
                      000006
360
                      000007
                             |; determined.
                      800000
361
                             **********************
362
                      000009
363
                      000010
                             |;Program entry point.
364
     0200
                      000011
                                    org 0200h
365
                      000012
                      000013 |; Place 0 into variable sum.
366
367
     0200 A9 00
                      000014
                                    lda #0d
368
     0202 8D 1F 02
                      000015
                                    sta sum
369
                      000016
370
                      000017
                             |;Place 1 into variable count.
371
     0205 A9 01
                      000018
                                    lda #1d
372
     0207 8D 20 02
                      000019
                                    sta count
373
                      000020
374
                      000021
                             |;Top of summing loop.
375
     020A
                      000022
                             |LoopTop *
376
                      000023
377
                      000024
                             ; Add count to sum and place result back into sum.
378
     020A AD 1F 02
                      000025
                                    lda sum
379
     020D 18
                      000026
                                    clc
                                    adc count
380
     020E 6D 20 02
                      000027
381
     0211 8D 1F 02
                      000028
                                    sta sum
382
                      000029
383
                      000030 |; Add 1 to count.
384
     0214 EE 20 02
                      000031
                                    inc count
385
                      000032
386
                      000033 |; If count is not equal to 11 yet then branch back
387
                      000034
                             |; to LoopTop.
388
     0217 AD 20 02
                                    lda count
                      000035
389
     021A C9 0B
                      000036
                                    cmp #11d
390
     021C D0 EC
                      000037
                                    bne looptop
391
                      000038
392
                      000039
                             |;Exit program.
     021E 00
393
                      000040
                                    brk
394
                      000041
                      000042 | ; **********************
395
```

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408 It did not take me very long to develop the program and when I was finished

16/34

- 409 I took off the Coder hat.
- 410 Pat said "That was fast. In fact, it took you much longer to develop the

end

- 411 algorithm than it did to code the program. Is that normal?"
- 412 "Yes," I replied "most of the work that is involved in developing a program
- 413 happens in the **problem solving** stage. After the program's logic has been
- 414 developed and recorded in a document like an Activity diagram, coding this
- 415 logic is usually a straight-forward task.

000053

000054

- 416 I now want you to study both the Activity diagram and the program and
- 417 then tell me if you notice anything interesting about the comments in the
- 418 program.

406

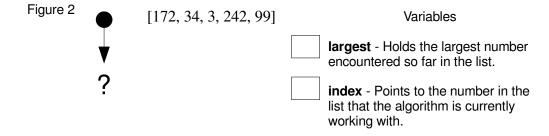
407

- 419 Pat studied both the diagram and the program for a while then said "Hey,
- 420 the comments in the program are taken directly from the diagram!"
- 421 "Indeed they are." I said. "You wanted to see how the steps in an algorithm
- were encoded into assembly language and you can see in this example that
- 423 the encoding process consists of taking each step in the algorithm and
- 424 creating a group of assembly language instructions that perform that step.
- 425 All the assembly language instructions in a given group are the small steps
- 426 that need to be performed in order to perform the larger step they are a
- 427 part of.
- 428 The task of translating a step in the algorithm to a group of assembly
- 429 language instructions that represent that step in a program is so direct that
- 430 the text that describes the step in the algorithm can sometimes be used
- 431 unchanged to describe what its analogous group of instructions does."

432 Finding The Largest Number In A List Of 100 Numbers

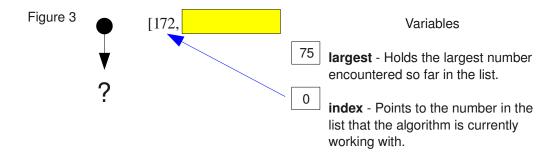
- 433 "Here is the next problem we are going to solve," I said. I then wrote this
- 434 problem description on the whiteboard:
- 435 Description: Find the largest number in a list of 100 numbers.
- 436 "This problem is more sophisticated than the previous problem and so we
- 437 will need to spend more time analyzing it." I said. "One of the strategies for
- 438 solving any problem is to try to solve a simpler problem that is similar
- 439 **to the original problem**. In this case, I propose that we try to solve the
- problem for a list of 5 numbers first, then use the knowledge we gained to
- 441 solve the larger problem."
- 442 "Okay." Said Pat.
- 443 "What should the **range** be for the numbers in the list?" I asked.
- 444 "Range?" asked Pat.
- 445 "Range in this case means the numbers in the list can be no lower than a
- 446 certain number and no higher than some other number. Therefore, you
- 447 have a range of numbers between a lower limit number and an upper limit
- 448 number to choose from." I said.
- 449 "Will the lower limit number and the upper limit number both be inclusive?"
- 450 asked Pat?
- 451 "Yes they will." I replied. "Also, when a person is developing an algorithm
- 452 that will be encoded into a programming language, they must **always be**
- 453 mindful of how many bits will be needed to represent the numbers in
- 454 **the algorithm**. In this case, I recommend that we use **bytes** to represent
- 455 the numbers in the list and that the numbers be non-negative. With these
- 456 assumptions, what is the range of the numbers that can be in the list?"
- 457 "0 to 255." said Pat.
- 458 "Very good." I said. "Whenever assumptions are applied to an algorithm,
- 459 these should be recorded near the problem's description." I then added the
- 460 following assumption section to the whiteboard:
- 461 Assumptions: The numbers in the list will be no lower than 0 and no higher
- 462 than 255.

- "Now, give me a list of 5 numbers that meet these requirements." I said. 463
- 464 Pat thought for a moment then said "172, 34, 3, 242, 99."
- 465 I wrote these numbers on the whiteboard.
- 466 "What variables do you think our algorithm is going to need?" I asked.
- 467 Pat said "I think we are going to need a variable to hold the **largest**
- number. Hmmm, I am not sure what other variables we will need, though." 468
- 469 "How should we keep track of where we are in the list?" I asked.
- 470 "Oh yes, we will also need an **indexing** variable." said Pat.
- "Lets start with these variables, then, and begin developing the program's 471
- 472 logic." I said. Then I put the information on the whiteboard (see Fig. 2)



- "What should the algorithm do first, Pat?" I asked. 473
- 474 Pat studied the information I had placed on the whiteboard then said "I
- 475 think the first thing the algorithm should do is to set the variables to their
- 476 initial values."
- 477 "I agree." I said. "Setting variables to their initial values is referred to as
- **initializing** the variables and they can be initialized either by algorithm 478
- 479 steps or by just placing the initial values into the variable's simulation
- boxes. If the initial values are placed into the simulation boxes, these 480
- variables will be initialized when the variables are defined in the program. 481
- 482 For example, in the 6502 assembly language we have been using, largest
- 483 **dbt** 5d would initialize the variable largest to 5 decimal. Since we
- initialized the variables using logic in the last problem, we will initialize 484
- them when they are defined in this problem." 485

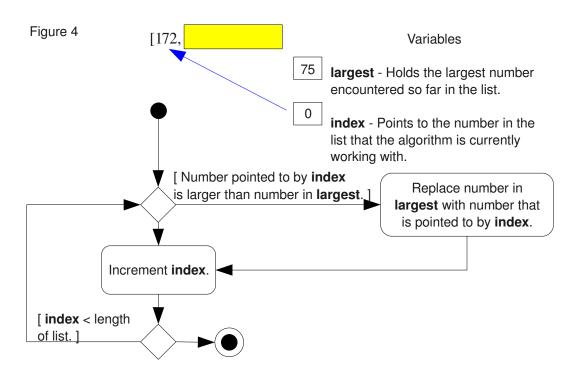
- 486 "Okay." said Pat.
- 487 "What should we initialize these variables to?" I asked.
- 488 "The variable **index** should be initialized to 0 but I'm not sure what **largest**
- 489 should be initialized to." said Pat after thinking about the question for some
- 490 time.
- 491 "If you are not sure, just come up with a number for now and we will
- 492 change it if we find a better number later.
- 493 "Set it to 75." said Pat. I then set **largest** to 75 and **index** to 0.
- 494 "Now pretend that you are a computer and describe how you would
- 495 determine the largest number in this list." I said. "Keep in mind that the
- 496 computer is not able to 'see' the whole list at one time like a human can.
- The computer is only able to see one number in the list at any given time so
- 498 which number would you start with?"
- 499 "I would probably start with the first number in the list." answered Pat.
- 500 "Which number is the first number in the list and what offset is it at?" I
- 501 asked.
- 502 "172 is the first number and it is at offset 0." replied Pat.
- 503 I then covered the other numbers in the list with a yellow piece of paper
- and drew an arrow from **index's** simulation box to the number 172. (see
- 505 Fig. 3)



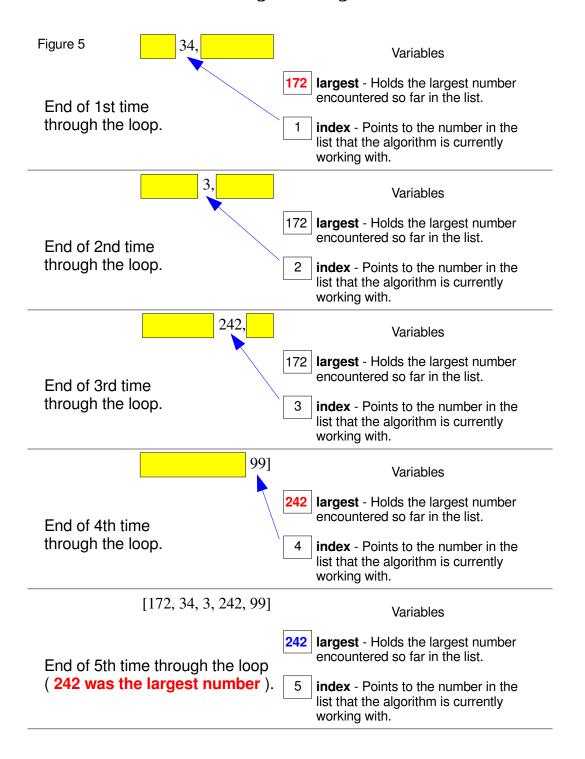
Then I said "What logic do you think should be performed in the algorithm, 507 Pat?"

"How about something like 'If the number referenced by index is greater than the number that is in largest, then replace the number in largest with the number that is referenced by index. Increment index to point to each number in the list in turn so that the logic can determine if it is the largest so far.'" said Pat.

513 "That sounds pretty good!" I said. "Now lets place this logic into the 514 Activity diagram. Whenever you encounter 'if' and 'then' inside sentences 515 that describe logic, these words indicate that a **decision** is being made. In 516 this case, we will place a **diamond** immediately after the **entry point** 517 symbol in the Activity diagram and then attach an activity rectangle that 518 contains the 'number compare and replace logic' to it. The words 'in turn' 519 indicate that a loop will be needed in the algorithm." I then added this logic to the Activity diagram. (see Fig. 4) 520



- When the Activity diagram was finished I said "Our next step is to pretend
- 522 we are a computer and perform a 'dry run' of the logic in the algorithm."
- 523 "A dry run?" asked Pat "What does that mean?"
- 524 "In the context of computer programming," I replied "it means to mentally
- execute a program, or a program's algorithms, without using a computer. A
- 526 programmer should always dry run their algorithms and programs to make
- 527 sure they are correct."
- 528 "Why are dry runs 'dry'?" asked Pat.
- 529 I laughed and said "My understanding is that the term 'dry run' comes from
- 530 the firefighter service. When a firetruck is sent out on a rehearsal or test
- 531 run, water is not usually used and therefore the run is dry. The term dry
- 532 run is often used to mean any kind of a rehearsal or test that is performed
- 533 before doing it for real."
- Pat and I then did a dry run of the algorithm using the list of numbers that
- 535 Pat came up with which were 172, 34, 3, 242, and 99. (see Fig. 5)



- 536 "It worked!" cried Pat. "The algorithm figured out that the largest number
- 537 in the list is 242!"
- 538 "Yes it did, but we can not celebrate just yet." I said.
- 539 "Why not?" asked Pat.
- 540 "Dry run the algorithm again, but this time use this list of numbers."
- 541 I wrote the following list on the whiteboard:
- 542 {2, 9, 3, 5, 7}
- Pat performed another dry run of the algorithm with the second list then
- 544 said "Hey, it didn't work this time! The algorithm says that the largest
- 545 number in the list is 75 even though the largest number is actually 9."
- 546 "What do you think the problem is?" I asked.
- 547 Pat studied the algorithm for a while then said "Oh, I see the problem. I
- 548 had told you to initialize the variable **largest** to 75, but 75 is larger than all
- of the numbers in the second list. Since none of the numbers in the list is
- 550 larger than 75, the 75 never gets replaced."
- 551 "Is there a number we can initialize **largest** to so that the algorithm will
- work correctly with any list that conforms to our stated assumptions?" I
- 553 asked.
- Pat thought about this question for a while then said "I think we will need to
- 555 initialize **largest** with the lowest number in the range of numbers that are
- allowed to be in the list. Since 0 is the lowest number in the range we
- 557 selected, this is what we should initialize largest to."
- 558 "Very Good!" I said. "These are the type of errors that performing dry runs
- of algorithms and programs are meant to find. I think our algorithm is
- 560 correct now and it should also be able to handle the 100 number list from
- 561 the original problem. I will now encode the algorithm into a program." I
- brought up an editor and encoded the logic that was in the Activity diagram
- into the following program:

```
564 000001 |; Program Name: largest. 565 000002 |;
```

```
566
                     000003 |; Version: 1.01.
567
                     000004 |;
                     000005 |; Description: Find the largest number in a list
568
569
                     000006 |; of 100 numbers.
570
                     000007
571
                     000008 |; Assumptions: The numbers in the list will be no
                            |; lower than 0 and no higher than 255.
572
573
                     000010
                     000011
574
                     575
                     000013 |; Program entry point.
576
     0200
                     000014 |
577
                                   org 0200h
578
                     000015
579
                     000016 |; This program will use the X register to point
580
                     000017
                            |; to the current number in the list
581
                     000018 |; instead of a variable called 'index'.
                     000019 |;
582
583
                     000020 |; Initialize register X to refer to offset 0 into
                     000021 |; the list of numbers starting at 'list'.
584
585
     0200 A2 00
                     000022 |
                                   ldx #0d
586
                     000023
587
                     000024 |; Compare the number that X is referring to in the
588
                     000025 |; list to the number that is in 'largest'. If the
                     000026 |; number being pointed to is larger than the contents
589
                     000027 |; of the variable 'largest', then fall through to
590
591
                     000028 |; the code that will replace the contents of 'largest'
592
                     000029 |; with the new number.
593
                     000030 | LoopTop *
     0202
                                   lda list,x
     0202 BD 14 02
594
                     000031
                     000032 |
595
     0205 CD 13 02
                                   cmp largest
     0208 90 03
596
                     000033 I
                                   bcc NotLarger
597
                     000034
                            |IsLarger *
598
     020A
                     000035
599
                     000036
600
                     000037
                            |;Replace the number in 'largest' with the current
601
                     000038 |; number from the list.
                     000039
602
     020A 8D 13 02
                                   sta largest
603
                     000040
604
     020D
                     000041 |NotLarger *
605
                     000042
                     000043 |; Increment the X register so that it references the
606
                     000044 |; next number in the list.
607
608
     020D E8
                     000045
                                   inx
609
                     000046
                     000047 |; Check to see if the end of the list has been reached.
610
                     000048 |; If it has, then exit the program. If it has not,
611
612
                     000049 |; then branch back to the top of the loop.
613
     020E
                     000050 | CheckListEnd *
     020E E0 64
                     000051
614
                                   cpx #100d
615
     0210 D0 F0
                                   bne LoopTop
                     000052 |
```

```
616
                      000053 I
                      000054 |; Exit the program.
617
     0212 00
                      000055
618
                                    brk
619
                      000056
620
                      000057
                      000058 | ; ***********************
621
622
                      000059 |; Variables area.
623
                      000060 |;
624
                      000061 |; In this program, the variables area is being placed
                      000062 |; below the code because the variables take up
625
                      000063 |; a significant amount of memory. This makes
626
                      000064 |; it more difficult to determine where the variables
627
                      000065 |; area ends so that the start of the code area
628
629
                      000066 |; can be determined.
630
                      000067
631
                      890000
632
                      000069 |; Holds the largest number
633
                      000070 |; encountered so far in the list.
                      000071 |; ( Notice that variables can
634
635
                      000072 |; be initialized here instead of
636
                      000073 |; in the code as an option ).
637
     0213 00
                      000074 |largest dbt 0d
638
                      000075
639
                      000076
640
                      000077 |; This list contains 100 numbers ranging from 0
641
                      000078 |; to 255.
642
     0214 3B
                      000079 |list dbt 59d,61d,37d,128d,71d,150d,195d,130d,69d,84d
643
     0215 3D
     0216 25
644
645
     0217 80
     0218 47
646
647
     0219 96
     021A C3
648
649
     021B 82
650
     021C 45
651
     021D 54
                      000080 |
     021E AB
                                  dbt 171d,227d,99d,214d,233d,136d,80d,253d,242d
652
     021F E3
653
654
     0220 63
     0221 D6
655
     0222 E9
656
657
     0223 88
     0224 50
658
659
     0225 FD
     0226 F2
660
     0227 70
                      000081 | dbt 112d,221d,151d,101d,117d,76d,226d,174d,205d
661
662
     0228 DD
     0229 97
663
     022A 65
664
     022B 75
665
```

	v2.08	65	02 Programming	26/34
666 667 668 669 670 671 672 673 674	022C 4C 022D E2 022E AE 022F CD 0230 54 0231 4E 0232 8B 0233 59 0234 C3 0235 F3	000082	dbt 84d,78d,139d,89d,195d,243d,69	9d,128d,217d,215d
676 677 678 679 680 681 682 683 684 685	0236 45 0237 80 0238 D9 0239 D7 023A 39 023B 64 023C E3 023D E2 023E E9 023F EE	000083	dbt 57d,100d,227d,226d,233d,238d	I,229d,228d,135d
686 687 688 689 690 691 692 693	0240 E5 0241 E4 0242 87 0243 8C 0244 62 0245 D3 0246 F5 0247 78	000084	dbt 140d,98d,211d,245d,120d,206d	l,198d,47d,191d
694 695 696 697 698 699 700 701 702	0248 CE 0249 C6 024A 2F 024B BF 024C EF 024D 1B 024E EC 024F 0C 0250 F2	000085	dbt 239d,27d,236d,12d,242d,148d,	98d,11d,38d,189d
703 704 705 706 707 708 709 710 711 712 713 714 715	0251 94 0252 62 0253 0B 0254 26 0255 BD 0256 EE 0257 E1 0258 8E 0259 D6 025A D6 025B 15 025C 4B 025D 11	000086	dbt 238d,225d,142d,214d,214d,21d	l,75d,17d,190d

The Professor And Pat series (professorandpat.org)

	v2.08	6502 Programming		27/34
716 717 718 719 720	025E BE 025F B2 0260 7B 0261 7D 0262 7B	000087	dbt 178d,123d,125d,123	d,10d,166d,123d,135d,220d
721 722 723 724 725	0263 0A 0264 A6 0265 7B 0266 87 0267 DC			
726 727 728 729 730 731	0268 C1 0269 2E 026A F8 026B DE 026C 3F 026D CE	000088	dbt 193d,46d,248d,222d	,63d,206d,197d,101d,144d
732 733 734 735	026E C5 026F 65 0270 90 0271 C9	000089	dbt 201d,233d,12d,241d	.85d.180d.29d
736 737 738 739 740 741	0272 E9 0273 0C 0274 F1 0275 55 0276 B4 0277 1D	,		, , , , , , , , , , , , , , , , , , , ,
742 743		000090 000091	end	

744 Exercises

- 745 These exercises use the programs that are included below them.
- a) Load the copy, scan, alpha, and sumlist programs into the emulator and
- 747 verify that they work correctly. You may need to trace them to
- 748 **understand how they work**. Type at least one of these in by hand instead
- 749 of using copy and paste.
- 750 b) Create activity diagrams for copy, scan, alpha, and sumlist. Use any
- 751 drawing program that will work (http://openoffice.org is free and it's
- 752 drawing application works well for drawing diagrams.)

753 Copy The Contents Of list1 To list2

```
754
     %uasm65
755
     ;Program Name: copy.
756
757
     :Version: 1.01.
758
759
     ;Description: Copy the contents of list1 to list2.
760
761
     ;Assumptions: The numbers in the list will be no
     ; lower than 0 and no higher than 255.
762
     ************
763
764
     ;Program entry point.
765
           org 0200h
     ;The X register will be used to point to each number in both list1 and list2.
766
767
           ldx #0d
768
     ;Copy the 10 bytes from list1 to list2.
769
     LoopTop
770
          lda list1,x
          sta list2,x
771
772
           inx
773
           cpx #10d
774
          bne LoopTop
775
     ;Exit the program.
```

```
776
           brk
      *************
777
778
     ; Variables area.
779
     ;This list contains 10 bytes.
     list1 dbt 41h,42h,43h,44h,45h,46h,47h,48h,49h,4ah
780
     ;This byte is placed here to make it easier to see the contents of list1
781
     ;and list2 when they are dumped in the monitor.
782
           dbt 0d
783
     ;Set aside 10 memory locations and initialize each one to 0d.
784
785
     list2 dbt 10d(0d)
786
           end
787
     %/uasm65
     Scan string1 And Determine How Many Capital And Lower Case A's
788
     It Contains
789
790
     %uasm65
791
     ;Program Name: scan.
792
793
     ; Version: 1.01.
794
795
     ;Description: Scan list1 and determine how many capital A's and lower case
796
     : a's it contains.
797
798
     ;Assumptions: The numbers in the list will be no
799
      ; lower than 0 and no higher than 255.
     800
     ;Program entry point.
801
           org 0200h
802
803
     ;The X register will be used to point to each ASCII character in string1
804
           ldx #0d
805
     LoopTop *
806
           lda string1,x
     ;If we have reached the 0 that has been placed at the end of the string, then
807
808
     ; exit the program.
```

```
809
           cmp #0d
           beg EndOfList
810
811
     CheckLowerCase *
812
     ;If the current character is a lower case 'a', then increment LowerCaseCount.
813
           cmp #'a'
814
           bne CheckUpperCase
           inc LowerCaseCount
815
           imp NextCharacter
816
817
     CheckUpperCase *
818
     ;If the current character is an upper case 'a', then increment UpperCaseCount.
           cmp #'A'
819
820
           bne NextCharacter
821
           inc UpperCaseCount
822
     NextCharacter *
823
           inx
824
           jmp LoopTop
     EndOfList *
825
826
     ;Exit the program.
827
           brk
     828
829
     ; Variables area.
830
     LowerCaseCount dbt 0d
831
     UpperCaseCount dbt 0d
     ;This list contains a string of ASCII characters.
832
     string1 dbt "A bird in the hand is worth two in the bush. Early to bed and "
833
834
             dbt "early to rise makes a person healthy, wealthy, and wise."
            dbt 0d
835
836
           end
     %/uasm65
837
```

- 838 Place Capital A's In The First 10 Bytes Of alphaList, Capital B's In
- 839 The Second 10 Bytes Of alphaList, And So On Until alphaList Is
- 840 Filled With Letters
- 841 %uasm65

```
;Program Name: alpha.uasm.
842
843
     ; Version: 1.02.
844
845
846
     ;Description: Place capital A's in the first 10 bytes of alphaList, capital
847
     ; in the second 10 bytes of alphalist and so on until alphaList is filled
848
     ; with letters.
849
850
     ;Assumptions: The numbers in the list will be no
851
     ; lower than 0 and no higher than 255.
852
     ************
853
854
     ;Program entry point.
855
           org 0200h
856
     ;The X register will be used as a pointer.
           ldx #0d
857
           lda #10d
858
859
           sta rowCount
860
           sta columnCount
     ;Initialize the 'A' register to be a capital 'A'.
861
           lda #65d
862
     LoopTop *
863
864
     ;Place character in list at offset X.
           sta alphalist,x
865
     ;Point X to the next character position in the list.
866
867
           inx
     ; If we have not placed 10 characters in this row yet, then loop.
868
869
           dec columnCount
           bne LoopTop
870
     ;Reset the column counter.
871
           ldy #10d
872
873
           sty columnCount
874
     ;Increase to the next letter in the alphabet.
           clc
875
           adc #1d
876
     ; If we have not filled 10 rows yet then loop.
877
           dec rowCount
878
           bne LoopTop
879
```

```
088
     EndOfList *
881
     ;Exit the program.
882
           brk
      *************
883
884
     :Variables area.
885
     rowCount
                 dbt 0d
886
     columnCount dbt 0d
887
     alphalist dbt 100d(?)
888
           end
     %/uasm65
889
890
     Calculate The Sum Of The 100 Bytes That Are In numbersList
891
     %uasm65
892
     ;Program Name: sumlist.uasm.
893
     :Version: 1.01.
894
895
896
     ;Description: Calculate the sum of the numbers that are in numberlist.
897
898
     ;Assumptions: The numbers in the list will be no
899
      ; lower than 0 and no higher than 255.
900
      ***********
901
     ;Program entry point.
902
           org 0200h
     ;The X register will be used as a pointer.
903
           ldx #0d
904
      ;Initialize the 16 bit wide variable "sum" to 0. Note: 8 bits is called a
905
     ; "byte" and 16 bits is called a "word". sum+0d accesses the high byte of sum
906
      ; and sum+1d accesses the low byte of sum.
907
           lda #0d
908
909
           sta sum+0d
910
           sta sum+1d
911
     LoopTop
912
     ;Obtain the next number from the list.
913
           lda numberList,x
```

```
914
     ;Add the number to the low byte of sum and then place the result back into
     ; the low byte of sum.
915
916
           clc
917
           adc sum+1d
918
           sta sum+1d
     ;If the carry flag was set during the addition, this means that the addition
919
     ; resulted in a value that was greater than 255 and the high byte of sum needs
920
     ; to be incremented by 1. If the result was 255 or less, the carry would not
921
922
     ; be set and we can branch around the increment of the high byte of sum.
923
           bcc NoCarry
924
     Carry *
925
           inc sum+0d
926
     NoCarry *
927
     ; Point to the next number in the list and loop back if we have not reached
928
     : the end of the list.
929
           inx
           cpx #100d
930
931
           bne LoopTop
932
     ;Exit the program.
933
           brk
     934
935
     ; Variables area.
936
     ;DWD stands for Define Word and it creates a variable that is 16 bits wide.
937
     ; Sum needs to be 16 bits wide because the sum of the numbers in numberList
     ; will be greater than 255 (which is the largest number that can be held in
938
939
     ; an 8 bit byte).
           dwd?
940
     sum
941
     ;This list contains 100 numbers ranging from 0 to 255.
     numberList *
942
943
           dbt 59d,61d,37d,128d,71d,150d,195d,130d,69d,84d
           dbt 171d,227d,99d,214d,233d,136d,80d,253d,242d
944
945
           dbt 112d,221d,151d,101d,117d,76d,226d,174d,205d
           dbt 84d,78d,139d,89d,195d,243d,69d,128d,217d,215d
946
           dbt 57d,100d,227d,226d,233d,238d,229d,228d,135d
947
           dbt 140d,98d,211d,245d,120d,206d,198d,47d,191d
948
949
           dbt 239d,27d,236d,12d,242d,148d,98d,11d,38d,189d
           dbt 238d, 225d, 142d, 214d, 214d, 21d, 75d, 17d, 190d
950
           dbt 178d, 123d, 125d, 123d, 10d, 166d, 123d, 135d, 220d
951
952
           dbt 193d,46d,248d,222d,63d,206d,197d,101d,144d
           dbt 201d,233d,12d,241d,85d,180d,29d
953
954
           end
```

955 %/uasm65