Introduction To Programming With MathRider And MathPiper

by Ted Kosan

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1 1 Preface

2 1.1 Dedication

- 3 This book is dedicated to Steve Yegge and his blog entry "Math Every Day"
- 4 (http://steve.yegge.googlepages.com/math-every-day).

5 1.2 Acknowledgments

- 6 The following people have provided feedback on this book (if I forgot to include
- 7 your name on this list, please email me at ted.kosan at gmail.com):
- 8 Susan Addington
- 9 Matthew Moelter
- 10 Sherm Ostrowsky

11 1.3 Support Email List

- 12 The support email list for this book is called **mathrider-**
- 13 **users@googlegroups.com** and you can subscribe to it at
- 14 <u>http://groups.google.com/group/mathrider-users</u>.

15 1.4 Recommended Weekly Sequence When Teaching A Class With This

16 **Book**

- 17 Week 1: Sections 1 6.
- 18 Week 2: Sections 7 9.
- 19 Week 3: Sections 10 13.
- 20 Week 4: Sections 14 15.
- 21 Week 5: Sections 16 19.

22 2 Introduction

32

- 23 MathRider is an open source mathematics computing environment for
- 24 performing numeric and symbolic computations (the difference between numeric
- 25 and symbolic computations are discussed in a later section). Mathematics
- 26 computing environments are complex and it takes a significant amount of time
- 27 and effort to become proficient at using one. The amount of power that these
- 28 environments make available to a user, however, is well worth the effort needed
- 29 to learn one. It will take a beginner a while to become an expert at using
- 30 MathRider, but fortunately one does not need to be a MathRider expert in order
- 31 to begin using it to solve problems.

2.1 What Is A Mathematics Computing Environment?

- 33 A Mathematics Computing Environment is a set of computer programs that 1)
- 34 automatically execute a wide range of numeric and symbolic mathematics
- 35 calculation algorithms and 2) provide a user interface which enables the user to
- 36 access these calculation algorithms and manipulate the mathematical objects
- 37 they create (An algorithm is a step-by-step sequence of instructions for solving a
- 38 problem and we will be learning about algorithms later in the book).
- 39 Standard and graphing scientific calculator users interact with these devices
- 40 using buttons and a small LCD display. In contrast to this, users interact with
- 41 MathRider using a rich graphical user interface which is driven by a computer
- 42 keyboard and mouse. Almost any personal computer can be used to run
- 43 MathRider, including the latest subnotebook computers.
- 44 Calculation algorithms exist for many areas of mathematics and new algorithms
- 45 are constantly being developed. Software that contains these kind of algorithms
- 46 is commonly referred to as "Computer Algebra Systems (CAS)". A significant
- 47 number of computer algebra systems have been created since the 1960s and the
- 48 following list contains some of the more popular ones:
- 49 http://en.wikipedia.org/wiki/Comparison of computer algebra systems
- 50 Some environments are highly specialized and some are general purpose. Some
- allow mathematics to be entered and displayed in traditional form (which is what
- 52 is found in most math textbooks). Some are able to display traditional form
- 53 mathematics but need to have it input as text and some are only able to have
- 54 mathematics displayed and entered as text.
- 55 As an example of the difference between traditional mathematics form and text
- 56 form, here is a formula which is displayed in traditional form:

$$a = x^2 + 4hx + \frac{3}{7}$$

57 and here is the same formula in text form:

 $a = x^2 + 4*h*x + 3/7$

- 59 Most computer algebra systems contain a mathematics-oriented programming
- 60 language. This allows programs to be developed which have access to the
- 61 mathematics algorithms which are included in the system. Some mathematics-
- oriented programming languages were created specifically for the system they
- 63 work in while others were built on top of an existing programming language.
- 64 Some mathematics computing environments are proprietary and need to be
- 65 purchased while others are open source and available for free. Both kinds of
- 66 systems possess similar core capabilities, but they usually differ in other areas.
- 67 Proprietary systems tend to be more polished than open source systems and they
- 68 often have graphical user interfaces that make inputting and manipulating
- 69 mathematics in traditional form relatively easy. However, proprietary
- 70 environments also have drawbacks. One drawback is that there is always a
- 71 chance that the company that owns it may go out of business and this may make
- 72 the environment unavailable for further use. Another drawback is that users are
- variable to enhance a proprietary environment because the environment's source
- 74 code is not made available to users.
- 75 Some open source computer algebra systems do not have graphical user
- 76 interfaces, but their user interfaces are adequate for most purposes and the
- 77 environment's source code will always be available to whomever wants it. This
- 78 means that people can use the environment for as long as they desire and they
- 79 can also enhance it.

80 2.2 What Is MathRider?

- 81 MathRider is an open source Mathematics Computing Environment which has
- 82 been designed to help people teach themselves the STEM disciplines (Science.
- 83 Technology, Engineering, and Mathematics) in an efficient and holistic way. It
- 84 inputs mathematics in textual form and displays it in either textual form or
- 85 traditional form.
- 86 MathRider uses MathPiper as its default computer algebra system, BeanShell as
- 87 its main scripting language, jEdit as its framework (hereafter referred to as the
- 88 MathRider framework), and Java as it overall implementation language. One
- 89 way to determine a person's MathRider expertise is by their knowledge of these
- 90 components. (see Table 1)

98

Level	Knowledge
MathRider Developer	Knows Java, BeanShell, and the MathRider framework at an advanced level. Is able to develop MathRider plugins.
MathRider Customizer	Knows Java, BeanShell, and the MathRider framework at an intermediate level. Is able to develop MathRider macros.
MathRider Expert	Knows MathPiper at an advanced level and is skilled at using most aspects of the MathRider application.
MathRider Novice	Knows MathPiper at an intermediate level, but has only used MathRider for a short while.
MathRider Newbie	Does not know MathPiper but has been exposed to at least one programming language.
Programming Newbie	Does not know how a computer works and has never programmed before but knows how to use a word processor.

Table 1: MathRider user experience levels.

- 91 This book is for MathRider and Programming Newbies. This book will teach you
- 92 enough programming to begin solving problems with MathRider and the
- 93 language that is used is MathPiper. It will help you to become a MathRider
- Novice, but you will need to learn MathPiper from books that are dedicated to it
- 95 before you can become a MathRider Expert.
- 96 The MathRider project website (http://mathrider.org) contains more information
- 97 about MathRider along with other MathRider resources.

2.3 What Inspired The Creation Of Mathrider?

- 99 Two of MathRider's main inspirations are Scott McNeally's concept of "No child 100 held back":
- 101 http://weblogs.java.net/blog/turbogeek/archive/2004/09/no-child-held-b-1.html
- and Steve Yegge's thoughts on learning mathematics:
- 1) Math is a lot easier to pick up after you know how to program. In fact, if you're a halfway decent programmer, you'll find it's almost a snap.
- 105 2) They teach math all wrong in school. Way, WAY wrong. If you teach yourself math the right way, you'll learn faster, remember it longer, and it'll be much more valuable to you as a programmer.
- 3) The right way to learn math is breadth-first, not depth-first. You need to survey the space, learn the names of things, figure out what's what.
- http://steve-yegge.blogspot.com/2006/03/math-for-programmers.html

- 111 MathRider is designed to help a person learn mathematics on their own with
- little or no assistance from a teacher. It makes learning mathematics easier by
- focusing on how to program first and it facilitates a breadth-first approach to
- 114 learning mathematics.

115 3 Downloading And Installing MathRider

116 3.1 Installing Sun's Java Implementation

- 117 MathRider is a Java-based application and therefore a current version of Sun's
- 118 Java (at least Java 6) must be installed on your computer before MathRider can
- 119 be run.

120 3.1.1 Installing Java On A Windows PC

- 121 Many Windows PCs will already have a current version of Java installed. You can
- test to see if you have a current version of Java installed by visiting the following
- 123 web site:
- 124 <u>http://java.com/</u>
- 125 This web page contains a link called "Do I have Java?" which will check your Java
- version and tell you how to update it if necessary.

127 **3.1.2 Installing Java On A Macintosh**

- Macintosh computers have Java pre-installed but you may need to upgrade to a
- 129 current version of Java (at least Java 6) before running MathRider. If you need
- 130 to update your version of Java, visit the following website:
- 131 http://developer.apple.com/java.

132 3.1.3 Installing Java On A Linux PC

- 133 Locate the Java documentation for your Linux distribution and carefully follow
- the instructions provided for installing a Java 6 compatible version of Java on
- 135 your system.

136 3.2 Downloading And Extracting

- One of the many benefits of learning MathRider is the programming-related
- 138 knowledge one gains about how open source software is developed on the
- 139 Internet. An important enabler of open source software development are
- 140 websites, such as sourceforge.net (http://sourceforge.net) and java.net
- 141 (http://java.net) which make software development tools available for free to
- 142 open source developers.
- 143 MathRider is hosted at java.net and the URL for the project website is:
- 144 <u>http://mathrider.org</u>

- 145 MathRider can be obtained by selecting the **download** tab and choosing the
- 146 correct download file for your computer. Place the download file on your hard
- drive where you want MathRider to be located. For Windows users, it is
- 148 recommended that MathRider be placed somewhere on c: drive.
- 149 The MathRider download consists of a main directory (or folder) called
- 150 **mathrider** which contains a number of directories and files. In order to make
- downloading quicker and sharing easier, the mathrider directory (and all of its
- 152 contents) have been placed into a single compressed file called an **archive**. For
- 153 Windows systems, the archive has a .zip extension and the archives for Unix-
- **based** systems have a .tar.bz2 extension.
- 155 After an archive has been downloaded onto your computer, the directories and
- 156 files it contains must be **extracted** from it. The process of extraction
- 157 uncompresses copies of the directories and files that are in the archive and
- places them on the hard drive, usually in the same directory as the archive file.
- 159 After the extraction process is complete, the archive file will still be present on
- 160 your drive along with the extracted **mathrider** directory and its contents.
- 161 The **archive file** can be easily copied to a CD or USB drive if you would like to
- install MathRider on another computer or give it to a friend. However, don't
- 163 try to run MathRider from a USB drive because it will not work correctly.
- 164 (Note: If you already have a version of MathRider installed and you want
- 165 to install a new version in the same directory that holds the old version,
- 166 you must delete the old version first or move it to a separate directory.)

3.2.1 Extracting The Archive File For Windows Users

- 168 Usually the easiest way for Windows users to extract the MathRider archive file
- 169 is to navigate to the folder which contains the archive file (using the Windows
- 170 GUI), right click on the archive file (it should appear as a folder with a
- vertical zipper on it), and select Extract All... from the pop up menu.
- 172 After the extraction process is complete, a new folder called **mathrider** should
- be present in the same folder that contains the archive file. (Note: be careful
- 174 not to double click on the archive file by mistake when you are trying to
- open the mathrider folder. The Windows operating system will open the
- 176 archive just like it opens folders and this can fool you into thinking you
- are opening the mathrider folder when you are not. You may want to
- 178 move the archive file to another place on your hard drive after it has
- 179 been extracted to avoid this potential confusion.)

3.2.2 Extracting The Archive File For Unix Users

- 181 One way Unix users can extract the download file is to open a shell, change to
- 182 the directory that contains the archive file, and extract it using the following
- 183 command:

180

- tar -xvjf <name of archive file>
- 185 If your desktop environment has GUI-based archive extraction tools, you can use
- 186 these as an alternative.

187 3.3 MathRider's Directory Structure & Execution Instructions

188 The top level of MathRider's directory structure is shown in Illustration 1:

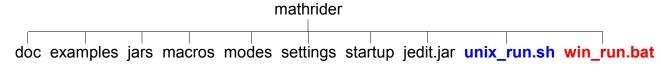


Illustration 1: MathRider's Directory Structure

- 189 The following is a brief description this top level directory structure:
- 190 **doc** Contains MathRider's documentation files.
- 191 **examples** Contains various example programs, some of which are pre-opened
- 192 when MathRider is first executed.
- 193 **jars** Holds plugins, code libraries, and support scripts.
- 194 **macros** Contains various scripts that can be executed by the user.
- 195 **modes** Contains files which tell MathRider how to do syntax highlighting for
- 196 various file types.
- 197 **settings** Contains the application's main settings files.
- 198 **startup** Contains startup scripts that are executed each time MathRider
- 199 launches.
- 200 **jedit.jar** Holds the core jEdit application which MathRider builds upon.
- 201 **unix_run.sh** The script used to execute MathRider on Unix systems.
- 202 **win_run.bat** The batch file used to execute MathRider on Windows systems.

203 3.3.1 Executing MathRider On Windows Systems

- 204 Open the mathrider folder (not the archive file!) and double click on the
- 205 **win run** file.

206 3.3.2 Executing MathRider On Unix Systems

- 207 Open a shell, change to the **mathrider** folder, and execute the **unix run.sh**
- 208 script by typing the following:
- sh unix run.sh
- 210 **3.3.2.1** MacOS X
- 211 Make a note of where you put the Mathrider application (for example
- 212 /Applications/mathrider). Run Terminal (which is in /Applications/Utilities).
- 213 Change to that directory (folder) by typing:
- 214 cd /Applications/mathrider
- 215 Run mathrider by typing:
- sh unix run.sh

4 The Graphical User Interface

- 218 MathRider is built on top of jEdit (http://jedit.org) so it has the "heart" of a
- 219 programmer's text editor. Programmer's text editors are similar to standard text
- 220 editors (like NotePad and WordPad) and word processors (like MS Word and
- OpenOffice) in a number of ways so getting started with MathRider should be
- 222 relatively easy for anyone who has used a text editor or a word processor.
- 223 However, programmer's text editors are more challenging to use than a standard
- 224 text editor or a word processor because programmer's text editors have
- capabilities that are far more advanced than these two types of applications.
- 226 Most software is developed with a programmer's text editor (or environments
- 227 which contain one) and so learning how to use a programmer's text editor is one
- of the many skills that MathRider provides which can be used in other areas.
- 229 The MathRider series of books are designed so that these capabilities are
- 230 revealed to the reader over time.
- 231 In the following sections, the main parts of MathRider's graphical user interface
- are briefly covered. Some of these parts are covered in more depth later in the
- 233 book and some are covered in other books.
- 234 As you read through the following sections, I encourage you to explore
- 235 each part of MathRider that is being discussed using your own copy of
- 236 **MathRider.**

237 4.1 Buffers And Text Areas

- 238 In MathRider, open files are called **buffers** and they are viewed through one or
- 239 more **text areas**. Each text area has a tab at its upper-left corner which displays
- 240 the name of the buffer it is working on along with an indicator which shows
- 241 whether the buffer has been saved or not. The user is able to select a text area
- 242 by clicking its tab and double clicking on the tab will close the text area. Tabs
- can also be rearranged by dragging them to a new position with the mouse.

244 **4.2** The Gutter

- 245 The gutter is the vertical gray area that is on the left side of the main window. It
- 246 can contain line numbers, buffer manipulation controls, and context-dependent
- 247 information about the text in the buffer.

4.3 Menus

248

- 249 The main menu bar is at the top of the application and it provides access to a
- 250 significant portion of MathRider's capabilities. The commands (or **actions**) in
- 251 these menus all exist separately from the menus themselves and they can be
- executed in alternate ways (such as keyboard shortcuts). The menu items (and

- even the menus themselves) can all be customized, but the following sections
- 254 describe the default configuration.

255 **4.3.1** File

- 256 The File menu contains actions which are typically found in normal text editors
- and word processors. The actions to create new files, save files, and open
- 258 existing files are all present along with variations on these actions.
- 259 Actions for opening recent files, configuring the page setup, and printing are
- also present.

261 **4.3.2** Edit

- 262 The Edit menu also contains actions which are typically found in normal text
- editors and word processors (such as **Undo**, **Redo**, **Cut**, **Copy**, and **Paste**).
- 264 However, there are also a number of more sophisticated actions available which
- are of use to programmers. For beginners, though, the typical actions will be
- 266 sufficient for most editing needs.

267 **4.3.3 Search**

- 268 The actions in the Search menu are used heavily, even by beginners. A good way
- 269 to get your mind around the search actions is to open the Search dialog window
- 270 by selecting the **Find...** action (which is the first actions in the Search menu). A
- 271 **Search And Replace** dialog window will then appear which contains access to
- 272 most of the search actions.
- 273 At the top of this dialog window is a text area labeled **Search for** which allows
- 274 the user to enter text they would like to find. Immediately below it is a text area
- 275 labeled **Replace with** which is for entering optional text that can be used to
- 276 replace text which is found during a search.
- 277 The column of radio buttons labeled **Search in** allows the user to search in a
- 278 **Selection** of text (which is text which has been highlighted), the **Current**
- 279 **Buffer** (which is the one that is currently active), **All buffers** (which means all
- opened files), or a whole **Directory** of files. The default is for a search to be
- 281 conducted in the current buffer and this is the mode that is used most often.
- 282 The column of check boxes labeled **Settings** allows the user to either **Keep or**
- 283 **hide the Search dialog window** after a search is performed, **Ignore the case**
- of searched text, use an advanced search technique called a **Regular**
- expression search (which is covered in another book), and to perform a
- 286 **HyperSearch** (which collects multiple search results in a text area).
- 287 The **Find** button performs a normal find operation. **Replace & Find** will replace
- 288 the previously found text with the contents of the **Replace with** text area and
- 289 perform another find operation. Replace All will find all occurrences of the

- 290 contents of the **Search for** text area and replace them with the contents of the
- 291 **Replace with** text area.

292 4.3.4 Markers, Folding, and View

293 These are advanced menus and they are described in later sections.

294 **4.3.5** Utilities

- 295 The utilities menu contains a significant number of actions, some that are useful
- 296 to beginners and others that are meant for experts. The two actions that are
- 297 most useful to beginners are the **Buffer Options** actions and the **Global**
- 298 **Options** actions. The **Buffer Options** actions allows the currently selected
- 299 buffer to be customized and the **Global Options** actions brings up a rich dialog
- 300 window that allows numerous aspects of the MathRider application to be
- 301 configured.
- Feel free to explore these two actions in order to learn more about what they do.

303 **4.3.6 Macros**

304 This is an advanced menu and it is described in a later sections.

305 **4.3.7 Plugins**

- 306 Plugins are component-like pieces of software that are designed to provide an
- 307 application with extended capabilities and they are similar in concept to physical
- 308 world components. The tabs on the right side of the application which are
- 309 labeled "GeoGebra", "Jung', "MathPiper", "MathPiperDocs", etc. are all plugins
- and they can be **opened** and **closed** by clicking on their **tabs**. **Feel free to close**
- 311 any of these plugins which may be opened if you are not currently using
- 312 **them.** MathRider pPlugins are covered in more depth in a later section.

313 **4.3.8 Help**

- The most important action in the **Help** menu is the **MathRider Help** action.
- 315 This action brings up a dialog window with contains documentation for the core
- 316 MathRider application along with documentation for each installed plugin.

317 **4.4 The Toolbar**

- 318 The **Toolbar** is located just beneath the menus near the top of the main window
- and it contains a number of icon-based buttons. These buttons allow the user to
- 320 access the same actions which are accessible through the menus just by clicking
- on them. There is not room on the toolbar for all the actions in the menus to be

- 322 displayed, but the most common actions are present. The user also has the
- option of customizing the toolbar by using the **Utilities->Global Options->Tool**
- 324 **Bar** dialog.

325 **4.4.1 Undo And Redo**

- 326 The **Undo** button on the toolbar is able to undo any text was entered since the
- 327 current session of MathRider was launched. This is very handy for undoing
- 328 mistakes or getting back text which was deleted. The **Redo** button can be used
- 329 if you have selected Undo too many times and you need to "undo" one ore more
- 330 Undo operations.

5 MathPiper: A Computer Algebra System For Beginners

- 332 Computer algebra systems are extremely powerful and very useful for solving
- 333 STEM-related problems. In fact, one of the reasons for creating MathRider was
- to provide a vehicle for delivering a computer algebra system to as many people
- as possible. If you like using a scientific calculator, you should love using a
- 336 computer algebra system!
- 337 At this point you may be asking yourself "if computer algebra systems are so
- 338 wonderful, why aren't more people using them?" One reason is that most
- 339 computer algebra systems are complex and difficult to learn. Another reason is
- that proprietary systems are very expensive and therefore beyond the reach of
- 341 most people. Luckily, there are some open source computer algebra systems
- that are powerful enough to keep most people engaged for years, and yet simple
- 343 enough that even a beginner can start using them. MathPiper (which is based on
- a CAS called Yacas) is one of these simpler computer algebra systems and it is
- 345 the computer algebra system which is included by default with MathRider.
- 346 A significant part of this book is devoted to learning MathPiper and a good way
- 347 to start is by discussing the difference between numeric and symbolic
- 348 computations.

349

5.1 Numeric Vs. Symbolic Computations

- 350 A Computer Algebra System (CAS) is software which is capable of performing
- 351 both **numeric** and **symbolic** computations. **Numeric** computations are
- performed exclusively with numerals and these are the type of computations that
- are performed by typical hand-held calculators.
- 354 **Symbolic** computations (which also called algebraic computations) relate "...to
- 355 the use of machines, such as computers, to manipulate mathematical equations
- and expressions in symbolic form, as opposed to manipulating the
- 357 approximations of specific numerical quantities represented by those symbols."
- 358 (http://en.wikipedia.org/wiki/Symbolic mathematics).
- 359 Since most people who read this document will probably be familiar with
- 360 performing numeric calculations as done on a scientific calculator, the next
- 361 section shows how to use MathPiper as a scientific calculator. The section after
- that then shows how to use MathPiper as a symbolic calculator. Both sections
- 363 use the console interface to MathPiper. In MathRider, a console interface to any
- 364 plugin or application is a text-only **shell** or **command line** interface to it. This
- means that you type on the keyboard to send information to the console and it
- 366 prints text to send you information.

367 5.2 Using The MathPiper Console As A Numeric (Scientific) Calculator

- 368 Open the MathPiper plugin by selecting the **MathPiper** tab in the lower left part
- of the MathRider application. The MathPiper **console** interface is a text area
- which is inside this plugin. Feel free to increase or decrease the size of the
- 371 console text area if you would like by dragging on the dotted lines which are at
- 372 the top side and right side of the console window.
- 373 When the MathPiper console is first launched, it prints a welcome message and
- 374 then provides **In>** as an input prompt:
- 375 MathPiper version ".76x".
- 376 In>
- 377 Click to the right of the prompt in order to place the cursor there then type **2+2**
- 378 followed by **<shift><enter>** (or **<shift><return>** on a Macintosh):
- 379 In> 2+2
- 380 Result> 4
- 381 In>
- When **<shift><enter>** was pressed, 2+2 was read into MathPiper for
- **evaluation** and **Result>** was printed followed by the result **4**. Another input
- prompt was then displayed so that further input could be entered. This **input**,
- 385 **evaluation, output** process will continue as long as the console is running and
- 386 it is sometimes called a **Read, Eval, Print Loop** or **REPL**. In further examples,
- the last **In>** prompt will not be shown to save space.
- 388 In addition to addition, MathPiper can also do subtraction, multiplication,
- 389 exponents, and division:
- 390 In> 5-2
- 391 Result> 3
- 392 In> 3*4
- 393 Result> 12
- 394 In> 2^3
- 395 Result> 8
- 396 In> 12/6
- 397 Result> 2
- 398 Notice that the multiplication symbol is an asterisk (*), the exponent symbol is a
- 399 caret (^), and the division symbol is a forward slash (/). These symbols (along
- 400 with addtion (+), subtraction (-), and ones we will talk about later) are called

- 401 **operators** because they tell MathPiper to perform an operation such as addition
- 402 or division.
- 403 MathPiper can also work with decimal numbers:

```
404
     In > .5 + 1.2
405
     Result> 1.7
406
    In> 3.7-2.6
407
    Result> 1.1
408
    In> 2.2*3.9
409
     Result> 8.58
410
    Tn > 2.2^3
411
     Result> 10.648
412
    In > 9.5/3.2
413
     Result> 9.5/3.2
```

- 414 In the last example, MathPiper returned the fraction unevaluated. This
- sometimes happens due to MathPiper's symbolic nature, but a result in **numeric**
- 416 **form** can be obtained by using the **N() function**:

```
417 In> N(9.5/3.2)
418 Result> 2.96875
```

- 419 As can be seen here, when a result is given in numeric form, it means that it is
- 420 given as a decimal number. The N() function is discussed in the next section.

421 **5.2.1 Functions**

- 422 **N()** is an example of a **function**. A function can be thought of as a "black box"
- 423 which accepts input, processes the input, and returns a result. Each function
- 424 has a name and in this case, the name of the function is **N** which stands for
- 425 **"numeric"**. To the right of a function's name there is always a set of
- 426 parentheses and information that is sent to the function is placed inside of them.
- 427 The purpose of the **N()** function is to make sure that the information that is sent
- 428 to it is processed numerically instead of symbolically.

429 5.2.1.1 The Sqrt() Square Root Function

- 430 The following example show the **N()** function being used with the square root
- 431 function **Sqrt()**:

```
432 In> Sqrt(9)
```

433 Result: 3

```
434 In> Sqrt(8)
435 Result: Sqrt(8)
436 In> N(Sqrt(8))
437 Result: 2.828427125
```

- Notice that Sqrt(9) returned 3 as expected but Sqrt(8) returned Sqrt(8). We
- 439 needed to use the N() function to force the square root function to return a
- 440 numeric result. The reason that Sqrt(8) does not appear to have done anything
- 441 is because computer algebra systems like to work with expressions that are as
- exact as possible. In this case the **symbolic** value Sqrt(8) represents the number
- that is the square root of 8 more accurately than any decimal number can.
- 444 For example, the following four decimal numbers all represent $\sqrt{8}$, but none of
- them represent it more accurately than Sgrt(8) does:
- 446 2.828427125
- 447 2.82842712474619
- 448 2.82842712474619009760337744842
- 2.8284271247461900976033774484193961571393437507539
- 450 Whenever MathPiper returns a symbolic result and a numeric result is desired,
- 451 simply use the N() function to obtain one. The ability to work with symbolic
- values are one of the things that make computer algebra systems so powerful
- and they are discussed in more depth in later sections.

454 **5.2.1.2** The IsEven() Function

- 455 Another often used function is **IsEven()**. The **IsEven()** function takes a number
- as input and returns **True** if the number is even and **False** if it is not even:

```
457 In> IsEven(4)
458 Result> True
459 In> IsEven(5)
460 Result> False
```

- 461 MathPiper has a large number of functions some of which are described in more
- depth in the MathPiper Documentation section and the MathPiper Programming
- 463 Fundamentals section. A complete list of MathPiper's functions is
- 464 contained in the MathPiperDocs plugin and more of these functions will
- 465 **be discussed soon.**

466

5.2.2 Accessing Previous Input And Results

The MathPiper console is like a mini text editor which means you can copy text

- 468 from it, paste text into it, and edit existing text. You can also reevaluate previous
- 469 input by simply placing the cursor on the desired **In>** line and pressing
- 470 **<shift><enter>** on it again.
- 471 The console also keeps a history of all input lines that have been evaluated. If
- 472 the cursor is placed on any **In>** line, pressing **<ctrl><up arrow>** will display
- 473 each previous line of input that has been entered.
- 474 Finally, MathPiper associates the most recent computation result with the
- percent (%) character. If you want to use the most recent result in a new
- 476 calculation, access it with this character:

```
477 In> 5*8

478 Result> 40

479 In> %

480 Result> 40

481 In> %*2

482 Result> 80
```

483 5.3 Saving And Restoring A Console Session

- 484 If you need to save the contents of a console session, you can copy and paste it
- into a MathRider buffer and then save the buffer. You can also copy a console
- 486 session out of a previously saved buffer and paste it into the console for further
- 487 processing. Section 7 **Using MathRider As A Programmer's Text Editor**
- 488 discusses how to use the text editor that is built into MathRider.

489 5.3.1 Syntax Errors

- 490 An expression's **syntax** is related to whether it is **typed** correctly or not. If input
- 491 is sent to MathPiper which has one or more typing errors in it, MathPiper will
- 492 return an error message which is meant to be helpful for locating the error. For
- 493 example, if a backwards slash (\) is entered for division instead of a forward slash
- 494 (/), MathPiper returns the following error message:

```
495 In> 12 \ 6
```

- 496 Error parsing expression, near token \setminus
- 497 The easiest way to fix this problem is to press the **up arrow** key to display the
- 498 previously entered line in the console, change the \ to a /, and reevaluate the
- 499 expression.
- 500 This section provided a short introduction to using MathPiper as a numeric
- 501 calculator and the next section contains a short introduction to using MathPiper
- 502 as a symbolic calculator.

503 5.4 Using The MathPiper Console As A Symbolic Calculator

- 504 MathPiper is good at numeric computation, but it is great at symbolic
- 505 computation. If you have never used a system that can do symbolic computation,
- 506 you are in for a treat!
- 507 As a first example, lets try adding fractions (which are also called rational
- 508 **numbers**). Add $\frac{1}{2} + \frac{1}{3}$ in the MathPiper console:
- 509 In> 1/2 + 1/3
- 510 Result> 5/6
- Instead of returning a numeric result like 0.8333333333333333333 (which is
- 512 what a scientific calculator would return) MathPiper added these two rational
- numbers symbolically and returned $\frac{5}{6}$. If you want to work with this result
- 514 further, remember that it has also been stored in the % symbol:
- 515 In> %
- 516 Result> 5/6
- 517 Lets say that you would like to have MathPiper determine the numerator of this
- result. This can be done by using (or **calling**) the **Numerator()** function:
- 519 In> Numerator(%)
- 520 Result> 5
- 521 Unfortunately, the % symbol cannot be used to have MathPiper determine the
- denominator of $\frac{5}{6}$ because it only holds the result of the most recent
- 523 calculation and $\frac{5}{6}$ was calculated two steps back.

524 **5.4.1 Variables**

- 525 What would be nice is if MathPiper provided a way to store **results** (which are
- also called **values**) in symbols that we choose instead of ones that it chooses.
- 527 Fortunately, this is exactly what it does! Symbols that can be associated with
- values are called **variables**. Variable names must start with an upper or lower
- 529 case letter and be followed by zero or more upper case letters, lower case
- letters, or numbers. Examples of variable names include: 'a', 'b', 'x', 'y', 'answer',
- 531 'totalAmount', and 'loop6'.
- 532 The process of associating a value with a variable is called **assigning** or **binding**
- 533 the value to the variable and this consists of placing the name of a variable you

- would like to create on the left side of an assignment operator (:=) and an
- expression on the right side of this operator. When the expression returns a
- value, the value is assigned (or bound to) to the variable.
- Lets recalculate $\frac{1}{2} + \frac{1}{3}$ but this time we will assign the result to the variable 'a':

```
538 In> a := 1/2 + 1/3
```

- 539 Result> 5/6
- 540 In> a
- 541 Result> 5/6
- 542 In> Numerator(a)
- 543 Result> 5
- 544 In> Denominator(a)
- 545 Result> 6
- In this example, the assignment operator (:=) was used to assign the result (or
- value) $\frac{5}{6}$ to the variable 'a'. When 'a' was evaluated by itself, the value it
- was bound to (in this case $\frac{5}{6}$) was returned. This value will stay bound to
- 549 the variable 'a' as long as MathPiper is running unless 'a' is cleared with the
- 550 **Clear()** function or 'a' has another value assigned to it. This is why we were able
- 551 to determine both the numerator and the denominator of the rational number
- assigned to 'a' using two functions in turn.

553 5.4.1.1 Calculating With Unbound Variables

- Here is an example which shows another value being assigned to 'a':
- 555 In> a := 9
- 556 Result> 9
- 557 In> a
- 558 Result> 9
- and the following example shows 'a' being cleared (or **unbound**) with the
- 560 **Clear()** function:
- 561 In> Clear(a)
- 562 Result> True
- 563 In> a
- 564 Result> a

- Notice that the Clear() function returns '**True**' as a result after it is finished to
- 566 indicate that the variable that was sent to it was successfully cleared (or
- **unbound**). Many functions either return '**True**' or '**False**' to indicate whether or
- 568 not the operation they performed succeeded. Also notice that unbound variables
- return themselves when they are evaluated. In this case, 'a' returned 'a'.
- 570 **Unbound variables** may not appear to be very useful, but they provide the
- 571 flexibility needed for computer algebra systems to perform symbolic calculations.
- 572 In order to demonstrate this flexibility, lets first factor some numbers using the
- 573 **Factor()** function:

```
574 In> Factor(8)
```

- 575 Result> 2^3
- 576 In> Factor (14)
- 577 Result> 2*7
- 578 In> Factor (2343)
- 579 Result> 3*11*71
- Now lets factor an expression that contains the unbound variable 'x':
- 581 In> x
- 582 Result> x
- 583 In> IsBound(x)
- 584 Result> False
- 585 In> Factor $(x^2 + 24x + 80)$
- 586 Result> (x+20)*(x+4)
- 587 In> Expand(%)
- 588 Result> $x^2+24*x+80$
- 589 Evaluating 'x' by itself shows that it does not have a value bound to it and this
- 590 can also be determined by passing 'x' to the **IsBound()** function. IsBound()
- returns '**True**' if a variable is bound to a value and '**False**' if it is not.
- 592 What is more interesting, however, are the results returned by **Factor()** and
- 593 **Expand()**. **Factor()** is able to determine when expressions with unbound
- variables are sent to it and it uses the rules of algebra to **manipulate** them into
- 595 factored form. The **Expand()** function was then able to take the factored
- 596 expression (x+20)(x+4) and manipulate it until it was expanded. One way to
- remember what the functions **Factor()** and **Expand()** do is to look at the second
- 598 letters of their names. The 'a' in Factor can be thought of as adding
- parentheses to an expression and the 'x' in **Expand** can be thought of **xing** out
- or removing parentheses from an expression.

601

5.4.1.2 Variable And Function Names Are Case Sensitive

- 602 MathPiper variables are **case sensitive**. This means that MathPiper takes into
- account the **case** of each letter in a variable name when it is deciding if two or
- more variable names are the same variable or not. For example, the variable
- name **Box** and the variable name **box** are not the same variable because the first
- one variable name starts with an upper case 'B' and the second variable name starts
- 607 with a lower case 'b':

```
608 In> Box := 1
609 Result> 1
610 In> box := 2
611 Result> 2
612 In> Box
613 Result> 1
614 In> box
615 Result> 2
```

616 **5.4.1.3 Using More Than One Variable**

Programs are able to have more than 1 variable and here is a more sophisticated

example which uses 3 variables:

```
a := 2
619
620 Result> 2
621
   b := 3
622 Result> 3
623 a + b
624
   Result> 5
625
    answer := a + b
626 Result> 5
627
    answer
628
    Result> 5
```

- 629 The part of an expression that is on the **right side** of an assignment operator is
- 630 always evaluated first and the result is then assigned to the variable that is on
- 631 the **left side** of the operator.
- Now that you have seen how to use the MathPiper console as both a **symbolic**

- and a **numeric** calculator, our next step is to take a closer look at the functions
- 634 which are included with MathPiper. As you will soon discover, MathPiper
- 635 contains an amazing number of functions which deal with a wide range of
- 636 mathematics.

637 5.5 Exercises

- Use the MathPiper console which is at the bottom of the MathRider application
- 639 to complete the following exercises.

640 **5.5.1 Exercise 1**

641 Perform the following calculation:

$$\frac{1}{4} + \frac{3}{8} - \frac{7}{16}$$

642 **5.5.2 Exercise 2**

- 643 a) Assign the variable **ans** to the result of the calculation $\frac{1}{5} + \frac{7}{4} + \frac{15}{16}$ using
- 644 the following line of code:
- 645 In> ans := 1/5 + 7/4 + 15/16
- 646 b) Use the Numerator() function to calculate the numerator of ans.
- 647 c) Use the Denominator() function to calculate the denominator of ans.
- 648 d) Use the N() function to calculate the numeric value of ans.
- 649 e) Use the Clear() function to unbind the variable ans and verify that ans
- 650 is unbound by executing the following code and by using the IsBound()
- 651 function:
- 652 In> ans

653 **5.5.3 Exercise 3**

- 654 Assign $\frac{1}{4}$ to variable **x**, $\frac{3}{8}$ to variable **y**, and $\frac{7}{16}$ to variable **z** using the
- 655 := operator. Then perform the following calculations:
- 656 a)
- 657 In> x
- 658 b)
- 659 In> y

```
660 c)
```

$$665$$
 In> x + z

$$667$$
 In> x + y + z

668 6 The MathPiper Documentation Plugin

- 669 MathPiper has a significant amount of reference documentation written for it
- and this documentation has been placed into a plugin called **MathPiperDocs** in
- order to make it easier to navigate. The MathPiperDocs plugin is available in a
- tab called "MathPiperDocs" which is near the right side of the MathRider
- 673 application. Click on this tab to open the plugin and click on it again to close it.
- 674 The left side of the MathPiperDocs window contains the names of all the
- 675 functions that come with MathPiper and the right side of the window contains a
- 676 mini-browser that can be used to navigate the documentation.

6.1 Function List

677

701

- 678 MathPiper's functions are divided into two main categories called **user** functions
- and **programmer functions**. In general, the **user functions** are used for
- 680 solving problems in the MathPiper console or with short programs and the
- 681 **programmer functions** are used for longer programs. However, users will
- often use some of the programmer functions and programmers will use the user
- 683 functions as needed.
- Both the user and programmer function names have been placed into a "tree" on
- the left side of the MathPiperDocs window to allow for easy navigation. The
- branches of the function tree can be opened and closed by clicking on the small
- 687 "circle with a line attached to it" symbol which is to the left of each branch. Both
- the user and programmer branches have the functions they contain organized
- into categories and the **top category in each branch** lists all the functions in
- 690 the branch in **alphabetical order** for guick access. Clicking on a function will
- 691 bring up documentation about it in the browser window and selecting the
- 692 **Collapse** button at the top of the plugin will collapse the tree.
- 693 Don't be intimidated by the large number of categories and functions
- 694 that are in the function tree! Most MathRider beginners will not know what
- 695 most of them mean, and some will not know what any of them mean. Part of the
- 696 benefit Mathrider provides is exposing the user to the existence of these
- 697 categories and functions. The more you use MathRider, the more you will learn
- about these categories and functions and someday you may even get to the point
- 699 where you understand all of them. This book is designed to show newbies how to
- begin using these functions using a gentle step-by-step approach.

6.2 Mini Web Browser Interface

- 702 MathPiper's reference documentation is in HTML (or web page) format and so
- 703 the right side of the plugin contains a mini web browser that can be used to
- 704 navigate through these pages. The browser's **home page** contains links to the
- 705 main parts of the MathPiper documentation. As links are selected, the **Back** and

- 706 **Forward** buttons in the upper right corner of the plugin allow the user to move
- 707 backward and forward through previously visited pages and the **Home** button
- 708 navigates back to the home page.
- 709 The function names in the function tree all point to sections in the HTML
- 710 documentation so the user can access function information either by navigating
- 711 to it with the browser or jumping directly to it with the function tree.

712 **6.3 Exercises**

713 **6.3.1 Exercise 1**

- 714 Locate the N(), IsEven(), IsOdd(), Clear(), IsBound(), Numerator(),
- 715 Denominator(), and Factor() functions in the All Functions section of the
- 716 MathPiperDocs plugin and read the information that is available on them.

717 **6.3.2 Exercise 2**

- 718 Locate the N(), IsEven(), IsOdd(), Clear(), IsBound(), Numerator(),
- 719 Denominator(), and Factor() functions in the User Functions section of the
- 720 MathPiperDocs plugin and list which section each function is contained in.
- 721 Don't include the **Alphabetical** or **Built In** subsections in your search.

722 7 Using MathRider As A Programmer's Text Editor

- 723 We have covered some of MathRider's mathematics capabilities and this section
- 724 discusses some of its programming capabilities. As indicated in a previous
- section, MathRider is built on top of a programmer's text editor but what wasn't
- discussed was what an amazing and powerful tool a programmer's text editor is.
- 727 Computer programmers are among the most intelligent and productive people in
- 728 the world and most of their work is done using a programmer's text editor (or
- 729 something similar to one). Programmers have designed programmer's text
- 730 editors to be super-tools which can help them maximize their personal
- 731 productivity and these tools have all kinds of capabilities that most people would
- 732 not even suspect they contained.
- 733 Even though this book only covers a small part of the editing capabilities that
- 734 MathRider has, what is covered will enable the user to begin writing useful
- 735 programs.

736

7.1 Creating, Opening, Saving, And Closing Text Files

- 737 A good way to begin learning how to use MathRider's text editing capabilities is
- 738 by creating, opening, and saving text files. A text file can be created either by
- 739 selecting **File->New** from the menu bar or by selecting the icon for this
- operation on the tool bar. When a new file is created, an empty text area is
- 741 created for it along with a new tab named **Untitled**.
- 742 The file can be saved by selecting **File->Save** from the menu bar or by selecting
- 743 the **Save** icon in the tool bar. The first time a file is saved, MathRider will ask
- the user what it should be named and it will also provide a file system navigation
- vindow to determine where it should be placed. After the file has been named
- and saved, its name will be shown in the tab that previously displayed **Untitled**.
- 747 A file can be closed by selecting **File->Close** from the menu bar and it can be
- opened by selecting **File->Open**.

749 7.2 Editing Files

- 750 If you know how to use a word processor, then it should be fairly easy for you to
- 751 learn how to use MathRider as a text editor. Text can be selected by dragging
- 752 the mouse pointer across it and it can be cut or copied by using actions in the
- 753 **Edit** menu (or by using **<Ctrl>x** and **<Ctrl>c**). Pasting text can be done using
- 754 the Edit menu actions or by pressing **<Ctrl>v**.

755 **7.3 File Modes**

756 Text file names are suppose to have a file extension which indicates what type of

- 757 file it is. For example, test.**txt** is a generic text file, test.**bat** is a Windows batch
- 758 file, and test.sh is a Unix/Linux shell script (unfortunately, Windows is usually
- 759 configured to hide file extensions, but viewing a file's properties by right-clicking
- on it will show this information.).
- 761 MathRider uses a file's extension type to set its text area into a customized
- 762 **mode** which highlights various parts of its contents. For example, MathRider
- 763 worksheet files have a .mrw extension and MathRider knows what colors to
- 764 highlight the various parts of a .mrw file in.

765 7.4 Learning How To Type Properly Is An Excellent Investment Of Your

- 766 **Time**
- 767 This is a good place in the document to mention that learning how to type
- 768 properly is an investment that will pay back dividends throughout your whole
- 769 life. Almost any work you do on a computer (including programming) will be
- 770 done *much* faster and with less errors if you know how to type properly. Here is
- 771 what Steve Yegge has to say about this subject:
- "If you are a programmer, or an IT professional working with computers in *any*
- 773 capacity, **you need to learn to type!** I don't know how to put it any more clearly
- 774 than that."
- 775 A good way to learn how to program is to locate a free "learn how to type"
- 776 program on the web and use it.

777 **7.5 Exercises**

778 **7.5.1 Exercise 1**

- 779 Create a text file called "my text file.txt" and place a few sentences in
- 780 it. Save the text file somewhere on your hard drive then close it. Now,
- 781 open the text file again using **File->Open** and verify that what you typed is
- 782 still in the file.

783

791

8 MathRider Worksheet Files

- 784 While MathRider's ability to execute code inside a console provides a significant
- amount of power to the user, most of MathRider's power is derived from
- 786 **worksheets**. MathRider worksheets are text files which have a **.mrw** extension
- and are able to execute multiple types of code in a single text area. The
- 788 worksheet demo 1.mrw file (which is preloaded in the MathRider environment
- 789 when it is first launched) demonstrates how a worksheet is able to execute
- 790 multiple types of code in what are called **code folds**.

8.1 Code Folds

- 792 Code folds are named sections inside a MathRider worksheet which contain
- 793 source code that can be executed by placing the cursor inside of it and pressing
- 794 **<shift><Enter>**. A fold always begins with a **start tag**, which starts with a
- 795 percent symbol (%) followed by the **name of the fold type** (like this:
- 796 **%<foldtype>**). The end of a fold is marked by an **end tag** which looks like
- 797 **%/<foldtype>**. The only difference between a fold's start tag and its end tag is
- 798 that the end tag has a slash (/) after the %.
- For example, here is a MathPiper fold which will print the result of 2 + 3 to the
- 800 MathPiper console (Note: the semicolon ';' which is at the end of the line of
- 801 **code is required**):
- 802 %mathpiper
- $803 \quad 2 + 3;$
- 804 %/mathpiper
- The **output** generated by a fold (called the **parent fold**) is wrapped in a **new**
- 806 **fold** (called a **child fold**) which is indented and placed just below the parent.
- 807 This can be seen when the above fold is executed by pressing **<shift><enter>**
- 808 inside of it:
- 809 %mathpiper
- $810 \quad 2 + 3;$
- 811 %/mathpiper
- 812 %output, preserve="false"
- 813 Result: 5
- 814 . %/output
- The most common type of output fold is **%output** and by default folds of type

- %output have their **preserve property** set to **false**. This tells MathRider to
- 817 overwrite the %output fold with a new version during the next execution of its
- parent. If preserve is set to **true**, the fold will not be overwritten and a new fold
- 819 will be created instead.
- 820 There are other kinds of child folds, but in the rest of this document they will all
- 821 be referred to in general as "output" folds.

822 8.1.1 The Description Attribute

- 823 Folds can also have what is called a "**description attribute**" placed after the
- 824 start tag which describes what the fold contains. For example, the following
- 825 %mathpiper fold has a description attribute which indicates that the fold adds
- 826 two number together:
- 827 %mathpiper, title="Add two numbers together."
- $828 \quad 2 + 3;$
- 829 %/mathpiper
- 830 The description attribute is added to the start tag of a fold by placing a comma
- after the fold's type name and then adding the text **title="<text>"** after the
- 832 comma. (Note: no spaces can be present before or after the comma (,) or
- 833 the equals sign (=)).

834 8.2 Automatically Inserting Folds & Removing Unpreserved Folds

- 835 Typing the top and bottom fold lines (for example:
- 836 %mathpiper
- 837 %/mathpiper
- 838 can be tedious and MathRider has a way to automatically insert them. Place the
- 839 cursor at the beginning of a blank line in a .mrw worksheet file where you would
- like a fold inserted and then **press the right mouse button**.
- 841 A popup menu will be displayed and at the top of this menu are items which read
- "Insert MathPiper Fold", "Insert Group Fold", etc. If you select one of these
- menu items, an empty code fold of the proper type will automatically be inserted
- 844 into the .mrw file at the position of the cursor.
- This popup menu also has a menu item called "Remove Unpreserved Folds". If
- this menu item is selected, all folds which have a "preserve="false"" property
- 847 will be removed.

848 **8.3 Exercises**

- 849 A MathRider worksheet file called "newbies_book_examples_1.mrw" can be
- 850 obtained from this website:
- 851 https://mathrider.dev.java.net/source/browse/mathrider/trunk/src/doc/newbies-bo
- 852 ok/examples/proposed/misc/newbies book examples 1.mrw
- 853 It contains a number of %mathpiper folds which contain code examples from the
- 854 previous sections of this book. Notice that all of the lines of code have a
- semicolon (;) placed after them. The reason this is needed is explained in a later
- 856 section.
- 857 Download this worksheet file to your computer from the section on this website
- 858 that contains the highest revision number and then open it in MathRider. Then,
- use the worksheet to do the following exercises.

860 **8.3.1 Exercise 1**

- 861 Execute folds 1-8 in the top section of the worksheet by placing the cursor
- 862 inside of the fold and then pressing $\langle \text{shift} \rangle \langle \text{enter} \rangle$ on the keyboard.

863 **8.3.2 Exercise 2**

- 864 The code in folds 9 and 10 have errors in them. Fix the errors and then
- 865 execute the folds again.

866 **8.3.3 Exercise 3**

867 Use the empty fold 11 to calculate the expression 100 - 23;

868 8.3.4 Exercise 4

- 869 Perform the following calculations by creating new folds at the bottom of
- 870 the worksheet (using the right-click popup menu) and placing each
- 871 calculation into its own fold:
- 872 a) 2*7 + 3
- 873 b) 18/3
- 874 c) 234238342 + 2038408203
- 875 d) 324802984 * 2308098234
- 876 e) Factor the result which was calculated in d).

9 MathPiper Programming Fundamentals

- 878 The MathPiper language consists of **expressions** and an expression consists of
- one or more **symbols** which represent **values**, **operators**, **variables**, and
- 880 **functions**. In this section expressions are explained along with the values,
- 881 operators, variables, and functions they consist of.

9.1 Values and Expressions

- 883 A **value** is a single symbol or a group of symbols which represent an idea. For
- 884 example, the value:
- 885 3

877

882

- 886 represents the number three, the value:
- 887 0.5
- 888 represents the number one half, and the value:
- "Mathematics is powerful!"
- 890 represents an English sentence.
- 891 Expressions can be created by using **values** and **operators** as building blocks.
- 892 The following are examples of simple expressions which have been created this
- 893 way:
- 894 3
- 895 2 + 3
- $5 + 6*21/18 2^3$
- 897 In MathPiper, **expressions** can be **evaluated** which means that they can be
- 898 transformed into a **result value** by predefined rules. For example, when the
- 899 expression 2 + 3 is evaluated, the result value that is produced is 5:
- 900 In> 2 + 3
- 901 Result> 5

902 **9.2 Operators**

- 903 In the above expressions, the characters +, -, *, /, $^{\circ}$ are called **operators** and
- 904 their purpose is to tell MathPiper what **operations** to perform on the **values** in
- an **expression**. For example, in the expression **2 + 3**, the **addition** operator **+**
- 906 tells MathPiper to add the integer 2 to the integer 3 and return the result.
- 907 The **subtraction** operator is **-**, the **multiplication** operator is *****, **/** is the
- 908 **division** operator, % is the **remainder** operator (which is also used as the

- "result of the last calculation" symbol), and ^ is the **exponent** operator.
- 910 MathPiper has more operators in addition to these and some of them will be
- 911 covered later.
- 912 The following examples show the -, *, /,%, and $^$ operators being used:
- 913 In> 5 2 914 Result> 3
- 915 In> 3*4
- 916 Result> 12
- 917 In> 30/3
- 918 Result> 10
- 919 In> 8%5
- 920 Result> 3
- 921 In> 2^3
- 922 Result> 8
- 923 The character can also be used to indicate a negative number:
- 924 In> -3
- 925 Result> -3
- 926 Subtracting a negative number results in a positive number (Note: there must be
- 927 a space between the two negative signs):
- 928 In> -3
- 929 Result> 3
- 930 In MathPiper, **operators** are symbols (or groups of symbols) which are
- 931 implemented with **functions**. One can either call the function that an operator
- 932 represents directly or use the operator to call the function indirectly. However,
- 933 using operators requires less typing and they often make a program easier to
- 934 read.

935

9.3 Operator Precedence

- 936 When expressions contain more than one operator, MathPiper uses a set of rules
- 937 called **operator precedence** to determine the order in which the operators are
- 938 applied to the values in the expression. Operator precedence is also referred to
- 939 as the **order of operations**. Operators with higher precedence are evaluated
- 940 before operators with lower precedence. The following table shows a subset of
- 941 MathPiper's operator precedence rules with higher precedence operators being
- 942 placed higher in the table:

- 943 ^ Exponents are evaluated right to left.
- *,%,/ Then multiplication, remainder, and division operations are evaluated left to right.
- 946 +, Finally, addition and subtraction are evaluated left to right.
- Lets manually apply these precedence rules to the multi-operator expression we used earlier. Here is the expression in source code form:

950 And here it is in traditional form:

$$5+6*\frac{21}{18}-2^3$$

- 951 According to the precedence rules, this is the order in which MathPiper
- 952 evaluates the operations in this expression:

```
953 5 + 6*21/18 - 2<sup>3</sup>

954 5 + 6*21/18 - 8

955 5 + 126/18 - 8

956 5 + 7 - 8

957 12 - 8

958 4
```

- 959 Starting with the first expression, MathPiper evaluates the ^ operator first which
- 960 results in the 8 in the expression below it. In the second expression, the *
- operator is executed next, and so on. The last expression shows that the final
- 962 result after all of the operators have been evaluated is 4.

9.4 Changing The Order Of Operations In An Expression

- The default order of operations for an expression can be changed by grouping
- various parts of the expression within parentheses (). Parentheses force the
- ode that is placed inside of them to be evaluated before any other operators are
- 967 evaluated. For example, the expression 2 + 4*5 evaluates to 22 using the
- 968 default precedence rules:

```
969 In> 2 + 4*5 970 Result> 22
```

963

- 971 If parentheses are placed around 4 + 5, however, the addition operator is forced
- 972 to be evaluated before the multiplication operator and the result is 30:

```
973 In> (2 + 4)*5 974 Result> 30
```

- Parentheses can also be nested and nested parentheses are evaluated from the
- 976 most deeply nested parentheses outward:

```
977 In> ((2 + 4)*3)*5
978 Result> 90
```

988

- 979 (Note: precedence adjusting parentheses are different from the parentheses that
- 980 are used to call functions.)
- 981 Since parentheses are evaluated before any other operators, they are placed at
- 982 the top of the precedence table:
- 983 () Parentheses are evaluated from the inside out.
- 7 Then exponents are evaluated right to left.
- *,%,/ Then multiplication, remainder, and division operations are evaluated left to right.
- 987 +, Finally, addition and subtraction are evaluated left to right.

9.5 Functions & Function Names

- 989 In programming, **functions** are named blocks of code that can be executed one
- 990 or more times by being **called** from other parts of the same program or called
- 991 from other programs. Functions can have values passed to them from the
- 992 calling code and they **always return a value** back to the calling code when they
- 993 are finished executing. An example of a function is the **IsEven()** function which
- 994 was discussed in an previous section.
- 995 Functions are one way that MathPiper enables code to be reused. Most
- 996 programming languages allow code to be reused in this way, although in other
- 997 languages these named blocks of code are sometimes called **subroutines**.
- 998 **procedures**, or **methods**.
- 999 The functions that come with MathPiper have names which consist of either a
- single word (such as **Sum()**) or multiple words that have been put together to
- 1001 form a compound word (such as **IsBound()**). All letters in the names of
- 1002 functions which come with MathPiper are lower case except the beginning letter
- in each word, which are upper case.

1004 9.6 Functions That Produce Side Effects

- 1005 Most functions are executed to obtain the **results** they produce but some
- 1006 functions are executed in order to have them perform work that is not in the
- 1007 **form of a result**. Functions that perform work that is not in the form of a result
- 1008 are said to produce **side effects**. Side effects include many forms of work such
- as sending information to the user, opening files, and changing values in the
- 1010 computer's memory.
- 1011 When a function produces a side effect which sends information to the user, this
- information has the words **Side Effects:** placed before it in the output instead of
- 1013 the word **Result:**. The **Echo()** and **Write()** functions are examples of functions
- that produce side effects and they are covered in the next section.

1015 9.6.1 Printing Related Functions: Echo(), Write(), And Newline()

- 1016 The printing related functions send text information to the user and this is
- 1017 usually referred to as "printing" in this document. However, it may also be called
- 1018 "echoing" and "writing".

1019 **9.6.1.1 Echo()**

- 1020 The **Echo()** function takes one expression (or multiple expressions separated by
- 1021 commas) evaluates each expression, and then prints the results as side effect
- 1022 output. The following examples illustrate this:
- 1023 In> Echo(1)
- 1024 Result> True
- 1025 Side Effects>
- 1026 1
- 1027 In this example, the number 1 was passed to the Echo() function, the number
- was evaluated (all numbers evaluate to themselves), and the result of the
- 1029 evaluation was then printed as a side effect. Notice that Echo() also returned a
- 1030 **result**. In MathPiper, all functions return a result, but functions whose main
- purpose is to produce a side effect usually just return a result of **True** if the side
- effect succeeded or **False** if it failed. In this case, Echo() returned a result of
- 1033 **True** because it was able to successfully print a 1 as its side effect.
- 1034 The next example shows multiple expressions being sent to Echo() (notice that
- 1035 the expressions are separated by commas):

```
1036 In> Echo (1, 1+2, 2*3)
```

- 1037 Result> True
- 1038 Side Effects>
- 1039 1 3 6

```
The expressions were each evaluated and their results were returned (separated
1040
      by spaces) as side effect output. If it is desired that commas be printed between
1041
      the numbers in the output, simply place three commas between the expressions
1042
1043
      that are passed to Echo():
1044
      In> Echo (1, 1, 1+2, 1, 2*3)
1045
      Result> True
1046
      Side Effects>
1047
      1,3,6
      Each time an Echo() function is executed, it always forces the display to drop
1048
      down to the next line after it is finished. This can be seen in the following
1049
      program which is similar to the previous one except it uses a separate Echo()
1050
      function to display each expression:
1051
1052
      %mathpiper
1053
      Echo (1);
1054
      Echo (1+2);
1055
      Echo (2*3);
1056
      %/mathpiper
1057
          %output, preserve="false"
1058
            Result: True
1059
1060
            Side Effects:
1061
             1
1062
             3
1063
             6
1064
          %/output
      Notice how the 1, the 3, and the 6 are each on their own line.
1065
1066
      Now that we have seen how Echo() works, lets use it to do something useful. If
      more than one expression is evaluated in a %mathpiper fold, only the result from
1067
      the last expression that was evaluated (which is usually the bottommost
1068
      expression) is displayed:
1069
1070
      %mathpiper
1071
      a := 1;
      b := 2;
1072
1073
      c := 3;
1074
      %/mathpiper
```

```
1075
          %output,preserve="false"
1076
            Result: 3
1077
          %/output
1078
      In MathPiper, programs are executed one line at a time, starting at the topmost
      line of code and working downwards from there. In this example, the line a := 1;
1079
      is executed first, then the line b := 2; is executed, and so on. Notice, however,
1080
      that even though we wanted to see what was in all three variables, only the
1081
1082
      content of the last variable was displayed.
1083
      The following example shows how Echo() can be used to display the contents of
1084
      all three variables:
1085
      %mathpiper
1086
      a := 1;
1087
      Echo(a);
1088
      b := 2;
1089
      Echo(b);
1090
      c := 3;
1091
      Echo(c);
1092
      %/mathpiper
1093
          %output,preserve="false"
1094
            Result: True
1095
1096
            Side Effects:
```

9.6.1.2 Echo Statements Are Useful For "Debugging" Programs

- 1102 The errors that are in a program are often called "bugs". This name came from
- the days when computers were the size of large rooms and were made using
- electromechanical parts. Periodically, bugs would crawl into the machines and
- interfere with its moving mechanical parts and this would cause the machine to
- 1106 malfunction. The bugs needed to be located and removed before the machine
- 1107 would run properly again.

1

2

3

%/output

1097

1098

1099

1100

1101

- 1108 Of course, even back then most program errors were produced by programmers
- entering wrong programs or entering programs wrong, but they liked to say that
- all of the errors were caused by bugs and not by themselves! The process of
- 1111 fixing errors in a program became known as **debugging** and the names "bugs"

- and "debugging" are still used by programmers today.
- One of the standard ways to locate bugs in a program is to place **Echo()** function
- calls in the code at strategic places which print the contents of variables and
- 1115 **display messages**. These Echo() functions will enable you to see what your
- program is doing while it is running. After you have found and fixed the bugs in
- 1117 your program, you can remove the debugging Echo() function calls or comment
- them out if you think they may be needed later.

1119 **9.6.1.3 Write()**

- 1120 The **Write()** function is similar to the Echo() function except it does not
- automatically drop the display down to the next line after it finishes executing:

```
1122
      %mathpiper
1123
      Write(1);
1124
      Write (1+2);
1125
      Echo (2*3);
1126
      %/mathpiper
1127
           %output,preserve="false"
1128
             Result: True
1129
1130
             Side Effects:
1131
             1 3 6
1132
          %/output
```

- 1133 Write() and Echo() have other differences besides the one discussed here and
- more information about them can be found in the documentation for these
- 1135 functions.

1136 **9.6.1.4 NewLine()**

- 1137 The **NewLine()** function simply prints a blank line in the side effects output. It
- is useful for placing vertical space between printed lines:

```
1139 %mathpiper

1140 a := 1;

1141 Echo(a);

1142 NewLine();

1143 b := 2;

1144 Echo(b);
```

```
1145
      NewLine();
1146
      c := 3;
1147
      Echo(C);
1148
      %/mathpiper
1149
           %output, preserve="false"
1150
             Result: True
1151
1152
             Side Effects:
1153
1154
             2
1155
             3
1156
          %/output
```

1157

9.7 Expressions Are Separated By Semicolons

- 1158 As discussed earlier, all of the expressions that are inside of a **%mathpiper** fold
- 1159 must have a semicolon (;) after them. However, the expressions executed in the
- 1160 **MathPiper console** did not have a semicolon after them. MathPiper actually
- requires that all expressions end with a semicolon, but one does not need to add
- a semicolon to an expression which is typed into the MathPiper console **because**
- the console adds it automatically when the expression is executed.

1164 9.7.1 Placing More Than One Expression On A Line In A Fold

- 1165 All the previous code examples have had each of their expressions on a separate
- line, but multiple expressions can also be placed on a single line because the
- semicolons tell MathPiper where one expression ends and the next one begins:

```
1168
      %mathpiper
1169
      a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c);
1170
      %/mathpiper
1171
          %output, preserve="false"
1172
            Result: True
1173
1174
            Side Effects:
1175
             1
1176
             2
1177
             3
1178
          %/output
```

- 1179 The spaces that are in the code of this example are used to make the code more
- 1180 readable. Any spaces that are present within any expressions or between them
- are ignored by MathPiper and if we remove the spaces from the previous code,
- 1182 the output remains the same:

```
1183
      %mathpiper
1184
      a:=1; Echo (a); b:=2; Echo (b); c:=3; Echo (c);
1185
      %/mathpiper
1186
           %output,preserve="false"
1187
             Result: True
1188
1189
             Side Effects:
1190
1191
             2
1192
             3
1193
          %/output
```

1194 9.7.2 Placing More Than One Expression On A Line In The Console Using

1195 A Code Block

- 1196 The MathPiper console is only able to execute one expression at a time so if the
- 1197 previous code that executes three variable assignments and three Echo()
- functions on a single line is evaluated in the console, only the expression $\mathbf{a} := \mathbf{1}$
- 1199 is executed:

```
1200 In> a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c); 1201 Result> 1
```

- 1202 Fortunately, this limitation can be overcome by placing the code into a **code**
- 1203 **block**. A **code block** (which is also called a **compound expression**) consists of
- one or more expressions which are separated by semicolons and placed within an
- open bracket ([) and close bracket (]) pair. If a code block is evaluated in the
- 1206 MathPiper console, each expression in the block will be executed from left to
- 1207 right. The following example shows the previous code being executed within of a
- 1208 code block inside the MathPiper console:

```
1209  In> [a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c);]
1210  Result> True
1211  Side Effects>
1212  1
1213  2
1214  3
```

Notice that this time all of the expressions were executed and 1-3 was printed as

- 1216 a side effect. Code blocks always return the result of the last expression
- 1217 executed as the result of the whole block. In this case, True was returned as the
- result because the last Echo(c) function returned True. If we place another
- 1219 expression after the Echo(c) function, however, the block will execute this new
- expression last and its result will be the one returned by the block:

```
1221 In> [a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c); 2 + 2]
1222 Result> 4
1223 Side Effects>
1224 1
1225 2
1226 3
```

1227 Finally, code blocks can have their contents placed on separate lines if desired:

```
1228
      %mathpiper
1229
      [
1230
           a := 1;
1231
1232
           Echo(a);
1233
1234
           b := 2;
1235
1236
           Echo(b);
1237
1238
           c := 3;
1239
1240
           Echo(c);
1241
      1;
1242
      %/mathpiper
1243
           %output, preserve="false"
1244
             Result: True
1245
1246
             Side Effects:
1247
1248
             2
1249
             3
1250
           %/output
```

- 1251 Code blocks are very powerful and we will be discussing them further in later
- 1252 sections.

1253

9.7.2.1 Automatic Bracket, Parentheses, And Brace Match Indicating

- 1254 In programming, most open brackets '[' have a close bracket ']', most open
- parentheses '(' have a close parentheses ')', and most open braces '{' have a
- 1256 close brace '}'. It is often difficult to make sure that each "open" character has a

- matching "close" character and if any of these characters don't have a match,
- then an error will be produced.
- 1259 Thankfully, most programming text editors have a character match indicating
- 1260 tool that will help locate problems. To try this tool, paste the following code into
- 1261 a .mrw file and following the directions that are present in its comments:

```
1262
      %mathpiper
1263
1264
          Copy this code into a .mrw file. Then, place the cursor
1265
          to the immediate right of any {, }, [, ], (, or ) character.
1266
          You should notice that the match to this character is
1267
          indicated by a rectangle being drawing around it.
1268
     */
1269
      list := \{1, 2, 3\};
1270
1271
          Echo("Hello");
1272
          Echo(list);
1273
      1;
1274
      %/mathpiper
```

1275 **9.8 Strings**

- 1276 A \mathbf{string} is a \mathbf{value} that is used to hold text-based information. The typical
- 1277 expression that is used to create a string consists of **text which is enclosed**
- 1278 **within double quotes**. Strings can be assigned to variables just like numbers
- 1279 can and strings can also be displayed using the Echo() function. The following
- 1280 program assigns a string value to the variable 'a' and then echos it to the user:

```
1281
      %mathpiper
1282
      a := "Hello, I am a string.";
1283
      Echo(a);
1284
      %/mathpiper
1285
          %output,preserve="false"
1286
            Result: True
1287
1288
            Side Effects:
1289
            Hello, I am a string.
1290
          %/output
```

1291 9.8.1 The MathPiper Console and MathPiper Folds Can Access The Same

1292 Variables

1301

- 1293 A useful aspect of using MathPiper inside of MathRider is that variables that are
- assigned inside of a **%mathpiper fold** are accessible inside of the **MathPiper**
- console and variables that are assigned inside of the **MathPiper console** are
- available inside of **%mathpiper folds**. For example, after the above fold is
- executed, the string that has been bound to variable 'a' can be displayed in the
- 1298 MathPiper console:

```
1299 In> a
1300 Result> "Hello, I am a string."
```

9.8.2 Using Strings To Make Echo's Output Easier To Read

- 1302 When the Echo() function is used to print the values of multiple variables, it is
- often helpful to print some information next to each variable so that it is easier to
- 1304 determine which value came from which Echo() function in the code. The
- 1305 following program prints the name of the variable that each value came from
- 1306 next to it in the side effects output:

```
1307
      %mathpiper
1308
     a := 1;
1309
     Echo("Variable a: ", a);
1310
     b := 2;
1311
     Echo("Variable b: ", b);
1312
     c := 3;
1313
     Echo("Variable c: ", c);
1314
      %/mathpiper
1315
          %output,preserve="false"
1316
            Result: True
1317
1318
            Side Effects:
1319
            Variable a: 1
1320
            Variable b: 2
1321
            Variable c: 3
1322
        %/output
```

1323 **9.8.2.1 Combining Strings With The: Operator**

- 1324 If you need to combine two or more strings into one string, you can use the:
- 1325 operator like this:

```
1326
     In> "A" : "B" : "C"
1327 Result: "ABC"
1328
     In> "Hello " : "there!"
1329
     Result: "Hello there!"
1330
     9.8.2.2 WriteString()
1331
     The WriteString() function prints a string without shows the double quotes that
1332
     are around it.. For example, here is the Write() function being used to print the
     string "Hello":
1333
1334
     In> Write("Hello")
1335
     Result: True
1336
     Side Effects:
1337
     "Hello"
     Notice the double quotes? Here is how the WriteString() function prints "Hello":
1338
1339
     In> WriteString("Hello")
1340
     Result: True
1341
     Side Effects:
1342
     Hello
     9.8.2.3 NI()
1343
     The NI() (New Line) function is used with the : function to place newline
1344
     characters inside of strings:
1345
     In> WriteString("A": Nl() : "B")
1346
1347
     Result: True
1348
     Side Effects:
1349
     Α
1350
     В
1351
     9.8.2.4 Space()
     The Space() function is used to add spaces to printed output:
1352
1353
     In> WriteString("A"); Space(10); WriteString("B")
1354
     Result: True
1355
     Side Effects:
1356
                 В
```

1357 9.8.3 Accessing The Individual Letters In A String

1358 Individual letters in a string (which are also called **characters**) can be accessed

- v.93a 08/17/09 Introduction To Programming 53/121 by placing the character's position number (also called an index) inside of 1359 brackets [] after the variable it is bound to. A character's position is determined 1360 1361 by its distance from the left side of the string starting at 1. For example, in the string "Hello", 'H' is at position 1, 'e' is at position 2, etc. The following code 1362 shows individual characters in the above string being accessed: 1363 1364 In> a := "Hello, I am a string." 1365 Result> "Hello, I am a string." 1366 In>a[1]1367 Result> "H" 1368 In>a[2]1369 Result> "e" 1370 In>a[3]1371 Result> "1" 1372 In>a[4]Result> "1" 1373 1374 In>a[5]1375 Result> "o" 9.9 Comments 1376 1377 Source code can often be difficult to understand and therefore all programming

- languages provide the ability for **comments** to be included in the code. 1378
- Comments are used to explain what the code near them is doing and they are 1379
- 1380 usually meant to be read by humans instead of being processed by a computer.
- Therefore, comments are ignored by the computer when a program is executed. 1381
- 1382 There are two ways that MathPiper allows comments to be added to source code.
- The first way is by placing two forward slashes // to the left of any text that is 1383
- meant to serve as a comment. The text from the slashes to the end of the line 1384
- 1385 the slashes are on will be treated as a comment. Here is a program that contains
- 1386 comments which use slashes:

```
1387
      %mathpiper
1388
      //This is a comment.
1389
     x := 2; //Set the variable x equal to 2.
1390
      %/mathpiper
1391
          %output, preserve="false"
1392
            Result: 2
```

```
1393 . %/output
```

- 1394 When this program is executed, any text that starts with slashes is ignored.
- 1395 The second way to add comments to a MathPiper program is by enclosing the
- 1396 comments inside of slash-asterisk/asterisk-slash symbols /* */. This option is
- useful when a comment is too large to fit on one line. Any text between these
- 1398 symbols is ignored by the computer. This program shows a longer comment
- 1399 which has been placed between these symbols:

```
1400
      %mathpiper
1401
1402
      This is a longer comment and it uses
1403
      more than one line. The following
1404
       code assigns the number 3 to variable
1405
       x and then returns it as a result.
1406
     * /
1407
     x := 3;
1408
     %/mathpiper
1409
          %output, preserve="false"
1410
            Result: 3
1411
          %/output
```

1412 **9.10 Exercises**

- 1413 For the following exercises, create a new MathRider worksheet file called
- 1414 section_9_exercises_<your first name>_<your last name>.mrw. (Note:
- there are no spaces in this file name). For example, John Smith's worksheet
- 1416 would be called:
- 1417 **section 9 exercises john smith.mrw**.
- 1418 After this worksheet has been created, place your answer for each exercise into
- 1419 its own fold in this worksheet. Place a description attribute in the start tag of
- each fold which indicates the exercise the fold contains the solution to. The folds
- 1421 you create should look similar to this one:

```
1422 %mathpiper,title="Exercise 1"
1423 //Sample fold.
1424 %/mathpiper
```

1425 **9.10.1 Exercise 1**

- 1426 Change the precedence of the following expression using parentheses so that
- 1427 it prints 20 instead of 14:
- 1428 2 + 3 * 4

1429 **9.10.2 Exercise 2**

- 1430 Place the following calculations into a fold and then use one Echo()
- 1431 function per variable to print the results of the calculations. Put
- 1432 strings in the Echo() functions which indicate which variable each
- 1433 calculated value is bound to:
- 1434 a := 1+2+3+4+5;
- 1435 b := 1-2-3-4-5;
- 1436 c := 1*2*3*4*5;
- 1437 d := 1/2/3/4/5;

1438 **9.10.3 Exercise 3**

- 1439 Place the following calculations into a fold and then use one Echo()
- 1440 function to print the results of all the calculations on a single line
- 1441 (Remember, the Echo() function can print multiple values if they are
- 1442 separated by commas.):
- 1443 Clear(x);
- 1444 a := 2*2*2*2*2;
- 1445 b := 2^5 ;
- 1446 c := $x^2 * x^3$;
- 1447 d := $2^2 * 2^3$;

1448 **9.10.4 Exercise 4**

- 1449 The following code assigns a string which contains all of the upper case
- 1450 letters of the alphabet to the variable upper. Each of the three Echo()
- 1451 functions prints an index number and the letter that is at that position in
- 1452 the string. Place this code into a fold and then continue the Echo()
- 1453 functions so that all 26 letters and their index numbers are printed
- 1454 upper := "ABCDEFGHIJKLMNOPQRSTUVWXYZ";
- 1455 Echo(1, upper[1]);
- 1456 Echo(2,upper[2]);
- 1457 Echo(3,upper[3]);

1458 **9.10.5 Exercise 5**

- 1459 Use Echo() functions to print an index number and the character at this
- 1460 position for the following string (this is similar to what was done in
- 1461 Exercise 4.):

1487

%/output

```
1462
     extra := ".!@#$%^&*() +<>,?/{}[]|\-=";
1463
     Echo(1,extra[1]);
1464
     Echo(2,extra[2]);
1465 Echo(3, extra[3]);
     9.10.6 Exercise 6
1466
1467
     The following program uses strings and index numbers to print a person's
1468
     name. Create a program which uses the three strings from this program to
1469
     print the names of three of your favorite movie actors.
1470
     %mathpiper
1471
1472
      This program uses strings and index numbers to print
1473
      a person's name.
1474
1475
     upper := "ABCDEFGHIJKLMNOPQRSTUVWXYZ";
1476
     lower := "abcdefghijklmnopqrstuvwxyz";
1477
     extra := ".!@#$%^&*() +<>,?/{}[]|\-=";
1478
     //Print "Mary Smith.".
1479
     Echo (upper[13], lower[1], lower[18], lower[25], extra[12], upper[19], lower[13], l
1480
     ower[9],lower[20],lower[8],extra[1]);
1481
     %/mathpiper
1482
          %output, preserve="false"
1483
           Result: True
1484
1485
           Side Effects:
1486
           Mary Smith.
```

10 Rectangular Selection Mode And Text Area Splitting

10.1 Rectangular Selection Mode

- One capability that MathRider has that a word processor may not have is the
- ability to select rectangular sections of text. To see how this works, do the
- 1492 following:

1488

1489

1504

- 1) Type three or four lines of text into a text area.
- 1494 2) Hold down the **<Alt>** kev then slowly press the **backslash kev** (\) a few
- times. The bottom of the MathRider window contains a text field which
- 1496 MathRider uses to communicate information to the user. As **<Alt>**\ is
- repeatedly pressed, messages are displayed which read **Rectangular**
- selection is on and Rectangular selection is off.
- 3) Turn rectangular selection on and then select some text in order to see
- how this is different than normal selection mode. When you are done
- experimenting, set rectangular selection mode to off.
- 1502 Most of the time normal selection mode is what you want to use but in certain
- 1503 situations rectangular selection mode is better.

10.2 Text area splitting

- 1505 Sometimes it is useful to have two or more text areas open for a single document
- or multiple documents so that different parts of the documents can be edited at
- 1507 the same time. A situation where this would have been helpful was in the
- 1508 previous section where the output from an exercise in a MathRider worksheet
- 1509 contained a list of index numbers and letters which was useful for completing a
- 1510 later exercise.
- 1511 MathRider has this ability and it is called **splitting**. If you look just to the right
- of the toolbar there is an icon which looks like a blank window, an icon to the
- right of it which looks like a window which was split horizontally, and an icon to
- 1514 the right of the horizontal one which is split vertically. If you let your mouse
- 1515 hover over these icons, a short description will be displayed for each of them.
- 1516 (For now, ignore the icon which has a yellow sunburst on it. It is the New
- 1517 View icon and it is an advanced feature.)
- 1518 Select a text area and then experiment with splitting it by pressing the horizontal
- and vertical splitting buttons. Move around these split text areas with their
- scroll bars and when you want to unsplit the document, just press the "**Unsplit**"
- 1521 **All**" icon.

1522 11 Working With Random Integers

- 1523 It is often useful to use random integers in a program. For example, a program
- may need to simulate the rolling of dice in a game. In this section, a function for
- obtaining nonnegative integers is discussed along with how to use it to simulate
- the rolling of dice.

1527

11.1 Obtaining Random Integers With The RandomInteger() Function

- One way that a MathPiper program can generate random integers is with the
- 1529 **RandomInteger()** function. The RandomInteger() function takes an integer as
- a parameter and it returns a random integer between 1 and the passed in
- integer. The following example shows random integers between 1 and 5
- 1532 **inclusive** being obtained from RandomInteger(). **Inclusive** here means that
- both 1 and 5 are included in the range of random integers that may be returned.
- 1534 If the word **exclusive** was used instead, this would mean that neither 1 nor 5
- 1535 would be in the range.

```
1536 In> RandomInteger(5)
```

- 1537 Result> 4
- 1538 In> RandomInteger (5)
- 1539 Result> 5
- 1540 In> RandomInteger(5)
- 1541 Result> 4
- 1542 In> RandomInteger (5)
- 1543 Result> 2
- 1544 In> RandomInteger (5)
- 1545 Result> 3
- 1546 In> RandomInteger(5)
- 1547 Result> 5
- 1548 In> RandomInteger (5)
- 1549 Result> 2
- 1550 In> RandomInteger (5)
- 1551 Result> 2
- 1552 In> RandomInteger (5)
- 1553 Result> 1
- 1554 In> RandomInteger (5)
- 1555 Result> 2
- 1556 Random integers between 1 and 100 can be generated by passing 100 to
- 1557 RandomInteger():

```
1558 In> RandomInteger (100)
```

- 1559 Result> 15
- 1560 In> RandomInteger(100)
- 1561 Result> 14

```
1562    In> RandomInteger(100)
1563    Result> 82
1564    In> RandomInteger(100)
1565    Result> 93
1566    In> RandomInteger(100)
1567    Result> 32
```

- 1568 A range of random integers that does not start with 1 can also be generated by
- using the **two argument** version of **RandomInteger()**. For example, random
- integers between 25 and 75 can be obtained by passing RandomInteger() the
- 1571 lowest integer in the range and the highest one:

```
1572
     In> RandomInteger(25, 75)
1573
     Result: 28
1574 In> RandomInteger (25, 75)
1575
    Result: 37
1576
    In> RandomInteger(25, 75)
1577
    Result: 58
1578
     In> RandomInteger(25, 75)
1579 Result: 50
1580
    In> RandomInteger(25, 75)
1581
     Result: 70
```

11.2 Simulating The Rolling Of Dice

- 1583 The following example shows the simulated rolling of a single six sided die using
- 1584 the RandomInteger() function:

```
1585
     In> RandomInteger(6)
1586
     Result> 5
1587
    In> RandomInteger(6)
1588 Result> 6
1589
    In> RandomInteger(6)
1590 Result> 3
1591
     In> RandomInteger(6)
1592
    Result> 2
1593
    In> RandomInteger(6)
1594
     Result> 5
```

1582

- 1595 Code that simulates the rolling of two 6 sided dice can be evaluated in the
- 1596 MathPiper console by placing it within a **code block**. The following code
- 1597 outputs the sum of the two simulated dice:

```
1598    In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
1599    Result> 6
1600    In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
1601    Result> 12
1602    In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
1603    Result> 6
```

```
1604    In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
1605    Result> 4
1606    In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
1607    Result> 3
1608    In> [a := RandomInteger(6); b := RandomInteger(6); a + b;]
1609    Result> 8
```

- Now that we have the ability to simulate the rolling of two 6 sided dice, it would
- 1611 be interesting to determine if some sums of these dice occur more frequently
- than other sums. What we would like to do is to roll these simulated dice
- 1613 hundreds (or even thousands) of times and then analyze the sums that were
- 1614 produced. We don't have the programming capability to easily do this yet, but
- after we finish the section on **while loops**, we will.

12 Making Decisions

- 1617 The simple programs that have been discussed up to this point show some of the
- 1618 power that software makes available to programmers. However, these programs
- are limited in their problem solving ability because they are unable to make
- decisions. This section shows how programs which have the ability to make
- decisions are able to solve a wider range of problems than programs that can't
- 1622 make decisions.

1616

1623

12.1 Conditional Operators

- 1624 A program's decision making ability is based on a set of special operators which
- are called **conditional operators**. A **conditional operator** is an operator that
- 1626 is used to **compare two values**. Expressions that contain conditional operators
- return a **boolean value** and a **boolean value** is one that can only be **True** or
- 1628 **False**. In case you are curious about the strange name, boolean values come
- 1629 from the area of mathematics called **boolean logic**. This logic was created by a
- 1630 mathematician named **George Boole** and this is where the name boolean came
- 1631 from. Table 2 shows the conditional operators that MathPiper uses:

Operator	Description
x = y	Returns True if the two values are equal and False if they are not equal. Notice that = performs a comparison and not an assignment like := does.
x != y	Returns True if the values are not equal and False if they are equal.
x < y	Returns True if the left value is less than the right value and False if the left value is not less than the right value.
x <= y	Returns True if the left value is less than or equal to the right value and False if the left value is not less than or equal to the right value.
x > y	Returns True if the left value is greater than the right value and False if the left value is not greater than the right value.
x >= y	Returns True if the left value is greater than or equal to the right value and False if the left value is not greater than or equal to the right value.

Table 2: Conditional Operators

- 1632 This example shows some of these conditional operators being evaluated in the
- 1633 MathPiper console:
- 1634 In> 1 < 2
- 1635 Result> True

```
1636
      In> 4 > 5
1637 Result> False
1638
     In> 8 >= 8
1639 Result> True
1640
     In> 5 <= 10
1641
     Result> True
1642
      The following examples show each of the conditional operators in Table 2 being
      used to compare values that have been assigned to variables \mathbf{x} and \mathbf{v}:
1643
1644
      %mathpiper
1645
      // Example 1.
1646
     x := 2;
1647
      y := 3;
      Echo(x, "= ", y, ":", x = y);
Echo(x, "!= ", y, ":", x != y);
1648
1649
     Echo (x, "< ", y, ":", x < y);
1650
1651
      Echo(x, "<= ", y, ":", x <= y);
      Echo(x, "> ", y, ":", x > y);
1652
1653
      Echo (x, ">= ", y, ":", x >= y);
1654
      %/mathpiper
1655
           %output, preserve="false"
1656
             Result: True
1657
1658
            Side Effects:
1659
             2 = 3:False
1660
            2 != 3 :True
            2 < 3 :True
1661
1662
           2 <= 3 :True
1663
            2 > 3 :False
1664
             2 >= 3 :False
1665 . %/output
1666
      %mathpiper
1667
          // Example 2.
1668
          x := 2;
1669
          y := 2;
1670
          Echo(x, "= ", y, ":", x = y);
1671
          Echo(x, "!= ", y, ":", x != y);
          Echo(x, "< ", y, ":", x < y);
Echo(x, "<= ", y, ":", x <= y);
1672
1673
          Echo(x, "> ", y, ":", x > y);
1674
```

```
Echo(x, ">= ", y, ":", x >= y);
1675
1676
      %/mathpiper
1677
          %output, preserve="false"
1678
            Result: True
1679
1680
            Side Effects:
1681
            2 = 2:True
1682
            2 != 2 :False
1683
            2 < 2 :False
            2 <= 2 :True
1684
1685
            2 > 2 :False
1686
            2 >= 2 :True
1687
     . %/output
1688
      %mathpiper
1689
      // Example 3.
1690
      x := 3;
1691
     y := 2;
1692
      Echo(x, "= ", y, ":", x = y);
Echo(x, "!= ", y, ":", x != y);
1693
      Echo(x, "< ", y, ":", x < y);
1694
      Echo (x, "<= ", y, ":", x <= y);
1695
      Echo(x, "> ", y, ":", x > y);
1696
      Echo (x, ">= ", y, ":", x \geq= y);
1697
1698
      %/mathpiper
1699
          %output, preserve="false"
1700
            Result: True
1701
1702
            Side Effects:
1703
            3 = 2:False
1704
            3 != 2 :True
1705
            3 < 2 :False
1706
            3 <= 2 :False
1707
            3 > 2 :True
1708
            3 >= 2 :True
1709
          %/output
```

- 1710 Conditional operators are placed at a lower level of precedence than the other 1711 operators we have covered to this point:
- 1712 () Parentheses are evaluated from the inside out.
- 1713 ^ Then exponents are evaluated right to left.

- *,%,/ Then multiplication, remainder, and division operations are evaluated left to right.
- 1716 +, Then addition and subtraction are evaluated left to right.
- =,!=,<,<=,>,>= Finally, conditional operators are evaluated.

1718 12.2 Predicate Expressions

- 1719 Expressions which return either **True** or **False** are called "**predicate**"
- 1720 expressions. By themselves, predicate expressions are not very useful and they
- only become so when they are used with special decision making functions, like
- the If() function (which is discussed in the next section).

1723 **12.3 Exercises**

1724 **12.3.1 Exercise 1**

- Open a MathPiper session and evaluate the following predicate expressions:
- 1726 In> 3 = 3
- 1727 In> 3 = 4
- 1728 In> 3 < 4
- 1729 In> 3 != 4
- 1730 In> -3 < 4
- 1731 In> 4 >= 4
- 1732 In> 1/2 < 1/4
- 1733 In> 15/23 < 122/189
- 1734 /*In the following two expressions, notice that 1/2 is not considered to be
- 1735 equal to .5 unless it is converted to a numerical value first.*/
- 1736 In> 1/2 = .5
- 1737 In> N(1/2) = .5

1738 **12.3.2 Exercise 2**

- 1739 Come up with 10 predicate expressions of your own and evaluate them in the
- 1740 MathPiper console.

1741 12.4 Making Decisions With The If() Function & Predicate Expressions

- 1742 All programming languages have the ability to make decisions and the most
- 1743 commonly used function for making decisions in MathPiper is the **If()** function.
- 1744 There are two calling formats for the If() function:

```
If(predicate, then)
If(predicate, then, else)
```

- 1745 The way the first form of the If() function works is that it evaluates the first
- expression in its argument list (which is the "**predicate**" expression) and then
- looks at the value that is returned. If this value is **True**, the "**then**" expression
- that is listed second in the argument list is executed. If the predicate expression
- evaluates to **False**, the "**then**" expression is not executed. (Note: any function
- that accepts a predicate expression as a parameter can also accept the boolean
- 1751 values True and False).
- 1752 The following program uses an **If()** function to determine if the value in variable
- number is greater than 5. If number is greater than 5, the program will echo
- 1754 "Greater" and then "End of program":

```
1755
      %mathpiper
1756
     number := 6;
1757
      If(number > 5, Echo(number, "is greater than 5."));
1758
     Echo("End of program.");
1759
     %/mathpiper
1760
          %output, preserve="false"
1761
            Result: True
1762
1763
            Side Effects:
1764
            6 is greater than 5.
1765
            End of program.
1766
          %/output
```

- 1767 In this program, number has been set to 6 and therefore the expression number
- 1768 > 5 is **True**. When the **If()** functions evaluates the **predicate expression** and
- determines it is **True**, it then executes the **first Echo()** function. The **second**
- 1770 **Echo()** function at the bottom of the program prints "End of program"
- 1771 regardless of what the If() function does. (**Note: semicolons cannot be placed**
- 1772 after expressions which are in function calls.)
- Here is the same program except that **number** has been set to **4** instead of **6**:

```
1774
      %mathpiper
1775
     number := 4;
1776
      If(number > 5, Echo(number, "is greater than 5."));
1777
     Echo("End of program.");
1778
      %/mathpiper
1779
          %output,preserve="false"
1780
            Result: True
1781
1782
            Side Effects:
1783
            End of program.
1784
          %/output
```

- This time the expression **number > 4** returns a value of **False** which causes the **If()** function to not execute the "**then**" expression that was passed to it.
- 1787 12.4.1 If() Functions Which Include An "Else" Parameter
- 1788 The second form of the If() function takes a third "else" expression which is
- 1789 executed only if the predicate expression is **False**. This program is similar to the
- 1790 previous one except an "else" expression has been added to it:

```
1791
      %mathpiper
1792
     x := 4;
1793
      If (x > 5, Echo(x, "is greater than 5."), Echo(x, "is NOT greater than 5."));
1794
     Echo("End of program.");
1795
      %/mathpiper
1796
          %output,preserve="false"
1797
            Result: True
1798
1799
            Side Effects:
1800
            4 is NOT greater than 5.
1801
            End of program.
1802
    . %/output
```

1803 **12.5 Exercises**

1804 **12.5.1 Exercise 1**

- 1805 Write a program which uses the RandomInteger() function to simulate the
- 1806 flipping of a coin (Hint: you can use 1 to represent a head and 0 to
- 1807 represent a tail.). Use predicate expressions, the If() function, and the
- 1808 Echo() function to print the string "The coin came up heads." or the string
- 1809 "The coin came up tails.", depending on what the simulated coin flip came
- 1810 up as when the code was executed.

1811 12.6 The And(), Or(), & Not() Boolean Functions & Infix Notation

1812 **12.6.1 And()**

- 1813 Sometimes a programmer needs to check if two or more expressions are all **True**
- and one way to do this is with the **And()** function. The And() function has **two**
- 1815 **calling formats** (or **notations**) and this is the first one:

```
And(expression1, expression2, expression3, ..., expressionN)
```

- 1816 This calling format is able to accept one or more predicate expressions as input.
- 1817 If **all** of these expressions returns a value of **True**, the And() function will also
- return a **True**. However, if **any** of the expressions return a **False**, then the And()
- 1819 function will return a **False**. This can be seen in the following example:
- 1820 In> And (True, True)
- 1821 Result> True
- 1822 In> And (True, False)
- 1823 Result> False
- 1824 In> And (False, True)
- 1825 Result> False
- 1826 In> And (True, True, True, True)
- 1827 Result> True
- 1828 In> And (True, True, False, True)
- 1829 Result> False
- 1830 The second format (or notation) that can be used to call the And() function is
- 1831 called **infix** notation:

```
1832
      With infix notation, an expression is placed on both sides of the And() function
      name instead of being placed inside of parentheses that are next to it:
1833
1834
      In> True And True
1835
     Result> True
1836
     In> True And False
1837
      Result> False
1838
     In> False And True
1839
      Result> False
1840
      Infix notation can only accept two expressions at a time, but it is often more
      convenient to use than function calling notation. The following program also
1841
1842
      demonstrates the infix version of the And() function being used:
1843
      %mathpiper
1844
      a := 7;
1845
     b := 9;
1846
      Echo("1: ", a < 5 And b < 10);
      Echo("2: ", a > 5 And b > 10);
1847
      Echo ("3: ", a < 5 And b > 10);
1848
      Echo ("4: ", a > 5 And b < 10);
1849
1850
      If(a > 5 And b < 10, Echo("These expressions are both true."));</pre>
1851
      %/mathpiper
1852
          %output, preserve="false"
1853
            Result: True
1854
1855
            Side Effects:
1856
            1: False
1857
            2: False
1858
            3: False
1859
1860
            These expressions are both true.
```

12.6.2 Or()

. %/output

1861

1862

The Or() function is similar to the And() function in that it has both a function calling format and an infix calling format and it only works with predicate expressions. However, instead of requiring that all expressions be **True** in order to return a **True**, Or() will return a **True** if **one or more expressions are True**. 1867 Here is the function calling format for Or():

```
Or(expression1, expression2, expression3, ..., expressionN)
```

and this example shows Or() being used with function calling format:

```
1869
     In> Or(True, False)
1870 Result> True
1871
    In> Or(False, True)
1872 Result> True
1873
    In> Or(False, False)
1874 Result> False
1875
     In> Or(False, False, False, False)
1876 Result> False
1877
     In> Or(False, True, False, False)
1878
    Result> True
```

1879 The infix notation format for Or() is as follows:

```
expression1 Or expression2
```

and this example shows infix notation being used:

```
1881 In> True Or False
1882 Result> True

1883 In> False Or True
1884 Result> True

1885 In> False Or False
1886 Result> False
```

1887 The following program also demonstrates the infix version of the Or() function

1888 being used:

```
1889 %mathpiper
1890 a := 7;
1891 b := 9;

1892 Echo("1: ", a < 5 or b < 10);
1893 Echo("2: ", a > 5 or b > 10);
```

```
1894
      Echo ("3: ", a > 5 Or b < 10);
1895
      Echo("4: ", a < 5 Or b > 10);
1896
      If (a < 5 Or b < 10, Echo("At least one of these expressions is true."));</pre>
1897
      %/mathpiper
1898
          %output, preserve="false"
1899
            Result: True
1900
1901
            Side Effects:
1902
            1: True
1903
            2: True
1904
            3: True
1905
            4: False
1906
            At least one of these expressions is true.
1907
          %/output
```

1908 **12.6.3 Not() & Prefix Notation**

- 1909 The **Not()** function works with predicate expressions like the And() and Or()
- 1910 functions do, except it can only accept **one** expression as input. The way Not()
- 1911 works is that it changes a **True** value to a **False** value and a **False** value to a
- 1912 **True** value. Here is the Not()'s function calling format:

```
Not(expression)
```

- 1913 and this example shows Not() being used with function calling format:
- 1914 In> Not(True)
 1915 Result> False

 1916 In> Not(False)
 1917 Result> True
- 1918 Instead of providing an alternative infix calling format like And() and Or() do,
- 1919 Not()'s second calling format uses **prefix** notation:

```
Not expression
```

- 1920 Prefix notation looks similar to function notation except no parentheses are used:
- 1921 In> Not True 1922 Result> False

```
1923
     In> Not False
1924
     Result> True
1925
     Finally, here is a program that also uses the prefix version of Not():
1926
     %mathpiper
1927
     Echo("3 = 3 is ", 3 = 3);
1928
     Echo ("Not 3 = 3 is ", Not 3 = 3);
1929
     %/mathpiper
1930
          %output, preserve="false"
1931
           Result: True
1932
1933
           Side Effects:
1934
           3 = 3 is True
1935
           Not 3 = 3 is False
1936 . %/output
1937 12.7 Exercises
     12.7.1 Exercise 1
1938
1939
     The following program simulates the rolling of two dice and prints a
1940
     message if both of the two dice come up less than or equal to 3. Create a
1941
     similar program which simulates the flipping of two coins and print the
1942
     message "Both coins came up heads." if both coins come up heads.
1943
      %mathpiper
1944
1945
      This program simulates the rolling of two dice and prints a message if
1946
      both of the two dice come up less than or equal to 3.
1947
1948
     dice1 := RandomInteger(6);
1949
     dice2 := RandomInteger(6);
1950
     Echo("Dice1: ", dice1, " Dice2: ", dice2);
1951
     NewLine();
1952
     If( dice1 <= 3 And dice2 <= 3, Echo("Both dice came up <= to 3.") );</pre>
1953
     %/mathpiper
```

1954 **12.7.2 Exercise 2**

1955 The following program simulates the rolling of two dice and prints a

```
1956
     message if either of the two dice come up less than or equal to 3. Create
1957
     a similar program which simulates the flipping of two coins and print the
     message "At least one coin came up heads." if at least one coin comes up
1958
1959
     heads.
1960
     %mathpiper
1961
1962
      This program simulates the rolling of two dice and prints a message if
1963
      either of the two dice come up less than or equal to 3.
1964
1965
     dice1 := RandomInteger(6);
1966
     dice2 := RandomInteger(6);
1967
     Echo("Dice1: ", dice1, " Dice2: ", dice2);
1968
     NewLine();
1969
     If( dice1 <= 3 Or dice2 <= 3, Echo("At least one die came up <= 3.") );</pre>
1970 %/mathpiper
```

13 The While() Looping Function & Bodied Notation

- 1972 Many kinds of machines, including computers, derive much of their power from
- 1973 the principle of **repeated cycling**. **Repeated cycling** in a MathPiper program
- means to execute one or more expressions over and over again and this process
- 1975 is called "**looping**". MathPiper provides a number of ways to implement **loops**
- in a program and these ways range from straight-forward to subtle.
- 1977 We will begin discussing looping in MathPiper by starting with the straight-
- 1978 forward **While** function. The calling format for the **While** function is as follows:

```
1979 While (predicate)
1980 [
1981 body_expressions
1982 ];
```

- 1983 The **While** function is similar to the **If** function except it will repeatedly execute
- 1984 the expressions it contains as long as its "predicate" expression is **True**. As soon
- 1985 as the predicate expression returns a **False**, the While() function skips the
- 1986 expressions it contains and execution continues with the expression that
- immediately follows the While() function (if there is one).
- 1988 The expressions which are contained in a While() function are called its "body"
- and all functions which have body expressions are called "**bodied**" functions. If
- 1990 a body contains more than one expression then these expressions need to be
- 1991 placed within a **code block** (code blocks were discussed in an earlier section).
- 1992 What a function's body is will become clearer after studying some example
- 1993 programs.

1994

13.1 Printing The Integers From 1 to 10

1995 The following program uses a While() function to print the integers from 1 to 10:

```
1996
      %mathpiper
1997
      // This program prints the integers from 1 to 10.
1998
1999
          Initialize the variable count to 1
2000
          outside of the While "loop".
2001
2002
      count := 1;
2003
      While (count <= 10)
2004
2005
          Echo (count);
```

```
2006
2007
           count := count + 1; //Increment count by 1.
2008
      ];
2009
      %/mathpiper
2010
           %output,preserve="false"
2011
             Result: True
2012
2013
             Side Effects:
2014
2015
             2
             3
2016
2017
             4
             5
2018
2019
             6
2020
             7
2021
             8
2022
             9
2023
             10
2024
          %/output
```

- In this program, a single variable called **count** is created. It is used to tell the
- 2026 Echo() function which integer to print and it is also used in the predicate
- 2027 expression that determines if the While() function should continue to **loop** or not.
- 2028 When the program is executed, 1 is placed into **count** and then the While()
- 2029 function is called. The predicate expression count <= 10 becomes 1 <= 10
- and, since 1 is indeed less than or equal to 10, a value of **True** is returned by the
- 2031 predicate expression.
- 2032 The While() function sees that the predicate expression returned a **True** and
- 2033 therefore it executes all of the expressions inside of its **body** from top to bottom.
- 2034 The Echo() function prints the current contents of count (which is 1) and then the
- 2035 expression count := count + 1 is executed.
- 2036 The expression **count** := **count** + **1** is a standard expression form that is used in
- 2037 many programming languages. Each time an expression in this form is
- 2038 evaluated, it **increases the variable it contains by 1**. Another way to describe
- 2039 the effect this expression has on **count** is to say that it **increments count** by **1**.
- 2040 In this case **count** contains **1** and, after the expression is evaluated, **count**
- 2041 contains **2**.
- 2042 After the last expression inside the body of the While() function is executed, the
- 2043 While() function reevaluates its predicate expression to determine whether it
- should continue looping or not. Since **count** is **2** at this point, the predicate
- 2045 expression returns **True** and the code inside the body of the While() function is
- 2046 executed again. This loop will be repeated until **count** is incremented to **11** and
- 2047 the predicate expression returns **False**.

2049

2075

The previous program can be adjusted in a number of ways to achieve different

13.2 Printing The Integers From 1 to 100

```
2050
      results. For example, the following program prints the integers from 1 to 100 by
      changing the 10 in the predicate expression to 100. A Write() function is used in
2051
      this program so that its output is displayed on the same line until it encounters
2052
      the wrap margin in MathRider (which can be set in Utilities -> Buffer
2053
2054
      Options...).
2055
      %mathpiper
2056
      // Print the integers from 1 to 100.
2057
      count := 1;
2058
      While (count <= 100)
2059
2060
          Write(count,,);
2061
2062
          count := count + 1; //Increment count by 1.
2063
      1;
2064
      %/mathpiper
2065
          %output, preserve="false"
2066
             Result: True
2067
2068
             Side Effects:
2069
             1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,
2070
             24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43,
2071
             44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63,
2072
             64,65,66,67,68,69,70,71,72,73,74,75,76,77,78,79,80,81,82,83,
2073
             84,85,86,87,88,89,90,91,92,93,94,95,96,97,98,99,100
          %/output
2074
```

13.3 Printing The Odd Integers From 1 To 99

The following program prints the odd integers from 1 to 99 by changing the increment value in the increment expression from 1 to 2:

```
2084
          x := x + 2; //Increment x by 2.
2085
      1;
2086
      %/mathpiper
2087
           %output, preserve="false"
2088
             Result: True
2089
2090
             Side Effects:
2091
             1,3,5,7,9,11,13,15,17,19,21,23,25,27,29,31,33,35,37,39,41,43,
2092
             45, 47, 49, 51, 53, 55, 57, 59, 61, 63, 65, 67, 69, 71, 73, 75, 77, 79, 81, 83,
2093
             85,87,89,91,93,95,97,99
2094
          %/output
```

2095 13.4 Printing The Integers From 1 To 100 In Reverse Order

2096 Finally, the following program prints the integers from 1 to 100 in reverse order:

```
2097
      %mathpiper
2098
      //Print the integers from 1 to 100 in reverse order.
2099
      x := 100;
2100
      While (x >= 1)
2101
      [
2102
          Write(x,,);
2103
          x := x - 1; //Decrement x by 1.
2104
      ];
2105
      %/mathpiper
2106
           %output, preserve="false"
2107
             Result: True
2108
2109
             Side Effects:
2110
              100,99,98,97,96,95,94,93,92,91,90,89,88,87,86,85,84,83,82,
2111
              81,80,79,78,77,76,75,74,73,72,71,70,69,68,67,66,65,64,63,
2112
              62,61,60,59,58,57,56,55,54,53,52,51,50,49,48,47,46,45,44,
2113
              43, 42, 41, 40, 39, 38, 37, 36, 35, 34, 33, 32, 31, 30, 29, 28, 27, 26, 25,
2114
              24, 23, 22, 21, 20, 19, 18, 17, 16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4,
2115
              3,2,1
2116
          %/output
```

In order to achieve the reverse ordering, this program had to initialize \mathbf{x} to $\mathbf{100}$,

2118 check to see if **x** was **greater than or equal to 1** ($x \ge 1$), and **decrement** x by

2119 **subtracting 1 from it** instead of adding 1 to it.

2135

2143

2144

2145

2120 13.5 Expressions Inside Of Code Blocks Are Indented

- 2121 In the programs in the previous sections which use while loops, notice that the
- 2122 expressions which are inside of the While() function's code block are **indented**.
- 2123 These expressions do not need to be indented to execute properly, but doing so
- 2124 makes the program easier to read.

13.6 Long-Running Loops, Infinite Loops, & Interrupting Execution

- 2126 It is easy to create a loop that will execute a large number of times, or even an
- 2127 **infinite number of times**, either on purpose or by mistake. When you execute
- 2128 a program that contains an **infinite loop**, it will run until you tell MathPiper to
- 2129 **interrupt** its execution. This is done by opening the MathPiper console and then
- 2130 pressing the "Stop" button which it contains. The Stop button is circular and it
- 2131 has an X on it. (Note: currently this button only works if MathPiper is
- 2132 **executed inside of a %mathpiper fold.**)
- 2133 Lets experiment with the **Stop** button by executing a program that contains an
- 2134 infinite loop and then stopping it:

%mathpiper

%output, preserve="false"

Processing...

- Since the contents of x is never changed inside the loop, the expression x < 10
- 2147 always evaluates to **True** which causes the loop to continue looping. Notice that
- 2148 the %output fold contains the word "**Processing...**" to indicate that the program
- 2149 is still running the code.

%/output

- 2150 Execute this program now and then interrupt it using the "Stop" button. When
- 2151 the program is interrupted, the %output fold will display the message "User
- 2152 **interrupted calculation**" to indicate that the program was interrupted. After a
- 2153 program has been interrupted, the program can be edited and then rerun.

2194

13.7 A Program That Simulates Rolling Two Dice 50 Times

```
The following program is larger than the previous programs that have been
2155
2156
     discussed in this book, but it is also more interesting and more useful. It uses a
     While() loop to simulate the rolling of two dice 50 times and it records how many
2157
     times each possible sum has been rolled so that this data can be printed. The
2158
     comments in the code explain what each part of the program does. (Remember, if
2159
     you copy this program to a MathRider worksheet, you can use rectangular
2160
     selection mode to easily remove the line numbers).
2161
2162
     %mathpiper
2163
2164
      This program simulates rolling two dice 50 times.
2165
2166
2167
       These variables are used to record how many times
2168
        a possible sum of two dice has been rolled. They are
2169
       all initialized to 0 before the simulation begins.
2170
2171
     numberOfTwosRolled := 0;
2172
     numberOfThreesRolled := 0;
2173
     numberOfFoursRolled := 0;
2174
     numberOfFivesRolled := 0;
2175
     numberOfSixesRolled := 0;
2176
     numberOfSevensRolled := 0;
2177
     numberOfEightsRolled := 0;
2178
     numberOfNinesRolled := 0;
2179
     numberOfTensRolled := 0;
2180
     numberOfElevensRolled := 0;
2181
     numberOfTwelvesRolled := 0;
2182
     //This variable keeps track of the number of the current roll.
2183
     roll := 1;
2184
     Echo("These are the rolls:");
2185
     /*
2186
      The simulation is performed inside of this while loop. The number of
2187
      times the dice will be rolled can be changed by changing the number 50
2188
      which is in the While function's predicate expression.
2189
2190
     While (roll <= 50)
2191
2192
          //Roll the dice.
2193
```

die1 := RandomInteger(6);

die2 := RandomInteger(6);

```
2195
2196
2197
         //Calculate the sum of the two dice.
2198
         rollSum := die1 + die2;
2199
2200
         /*
2201
2202
          Print the sum that was rolled. Note: if a large number of rolls
          is going to be performed (say > 1000), it would be best to comment
2203
2204
          out this Write() function so that it does not put too much text
2205
          into the output fold.
2206
2207
         Write(rollSum,,);
2208
2209
2210
2211
         These If() functions determine which sum was rolled and then add
2212
          1 to the variable which is keeping track of the number of times
2213
          that sum was rolled.
2214
         * /
2215
         If(rollSum = 2, numberOfTwosRolled := numberOfTwosRolled + 1);
2216
         If(rollSum = 3, numberOfThreesRolled := numberOfThreesRolled + 1);
2217
         If(rollSum = 4, numberOfFoursRolled := numberOfFoursRolled + 1);
2218
         If(rollSum = 5, numberOfFivesRolled := numberOfFivesRolled + 1);
2219
         If(rollSum = 6, numberOfSixesRolled := numberOfSixesRolled + 1);
2220
         If(rollSum = 7, numberOfSevensRolled := numberOfSevensRolled + 1);
2221
         If(rollSum = 8, numberOfEightsRolled := numberOfEightsRolled + 1);
2222
         If(rollSum = 9, numberOfNinesRolled := numberOfNinesRolled + 1);
2223
         If(rollSum = 10, numberOfTensRolled := numberOfTensRolled + 1);
2224
         If(rollSum = 11, numberOfElevensRolled := numberOfElevensRolled+1);
2225
         If(rollSum = 12, numberOfTwelvesRolled := numberOfTwelvesRolled+1);
2226
2227
2228
         //Increment the roll variable to the next roll number.
2229
         roll := roll + 1;
2230 ];
2231
     //Print the contents of the sum count variables for visual analysis.
2232 NewLine();
2233
     NewLine();
2234
     Echo("Number of Twos rolled: ", numberOfTwosRolled);
2235
     Echo("Number of Threes rolled: ", numberOfThreesRolled);
     Echo("Number of Fours rolled: ", numberOfFoursRolled);
2236
     Echo("Number of Fives rolled: ", numberOfFivesRolled);
2237
2238
     Echo ("Number of Sixes rolled: ", numberOfSixesRolled);
     Echo("Number of Sevens rolled: ", numberOfSevensRolled);
2239
     Echo("Number of Eights rolled: ", numberOfEightsRolled);
2240
2241
     Echo("Number of Nines rolled: ", numberOfNinesRolled);
2242
    Echo("Number of Tens rolled: ", numberOfTensRolled);
2243
     Echo("Number of Elevens rolled: ", numberOfElevensRolled);
2244
     Echo ("Number of Twelves rolled: ", numberOfTwelvesRolled);
```

```
2245
     %/mathpiper
2246
          %output,preserve="false"
2247
            Result: True
2248
2249
            Side effects:
2250
            These are the rolls:
2251
            4,8,6,4,6,9,7,11,9,3,11,6,11,7,11,4,7,7,8,7,3,6,7,7,7,12,4,
2252
            12,7,8,12,6,8,10,10,5,9,8,4,5,3,5,7,7,4,6,7,7,5,8,
2253
2254
            Number of Twos rolled: 0
2255
            Number of Threes rolled: 3
2256
            Number of Fours rolled: 6
2257
            Number of Fives rolled: 4
2258
            Number of Sixes rolled: 6
2259
            Number of Sevens rolled: 13
2260
            Number of Eights rolled: 6
2261
            Number of Nines rolled: 3
2262
            Number of Tens rolled: 2
2263
            Number of Elevens rolled: 4
2264
            Number of Twelves rolled: 3
2265 . %/output
```

2266 **13.8 Exercises**

2267 **13.8.1 Exercise 1**

2268 Create a program which uses a while loop to print the even integers from 2 2269 to 50 inclusive.

2270 **13.8.2 Exercise 2**

2271 Create a program which prints all the multiples of 5 between 5 and 50 2272 inclusive.

2273 **13.8.3 Exercise 3**

2274 Create a program which simulates the flipping of a coin 500 times. Print 2275 the number of times the coin came up heads and the number of times it came 2276 up tails after the loop is finished executing.

2277 14 Predicate Functions

- A **predicate function** is a function that either returns **True** or **False**. Most predicate functions in MathPiper have names which begin with "**Is**". For example, **IsEven()**, **IsOdd()**, **IsInteger()**, etc. The following examples show
- 2281 some of the predicate functions that are in MathPiper:

```
2282
     In> IsEven(4)
2283
     Result> True
2284
     In> IsEven(5)
2285
     Result> False
2286
     In> IsZero(0)
2287
    Result> True
2288
     In> IsZero(1)
2289 Result> False
2290
     In> IsNegativeInteger(-1)
2291
     Result> True
2292
     In> IsNegativeInteger(1)
2293
    Result> False
2294
     In> IsPrime(7)
2295
    Result> True
2296
    In> IsPrime(100)
```

Result> False

- There is also an **IsBound()** and an **IsUnbound()** function that can be used to
- 2299 determine whether or not a value is bound to a given variable:

```
2301
    Result> a
2302
     In> IsBound(a)
2303
     Result> False
2304
     In> a := 1
2305
     Result> 1
2306
     In> IsBound(a)
2307
     Result> True
2308
     In> Clear(a)
2309
     Result> True
```

In> a

2297

2300

```
2310 In> a
2311 Result> a
2312 In> IsBound(a)
2313 Result> False
2314 The complete b
```

- 2314 The complete list of predicate functions is contained in the **User**
- 2315 **Functions/Predicates** node in the MathPiperDocs plugin.

14.1 Finding Prime Numbers With A Loop

- 2317 Predicate functions are very powerful when they are combined with loops
- 2318 because they can be used to automatically make numerous checks. The
- 2319 following program uses a while loop to pass the integers 1 through 20 (one at a
- 2320 time) to the **IsPrime()** function in order to determine which integers are prime
- 2321 and which integers are not prime:

```
2322
     %mathpiper
2323
      //Determine which numbers between 1 and 20 (inclusive) are prime.
2324
     x := 1;
2325
     While (x \leq 20)
2326
2327
          primeStatus := IsPrime(x);
2328
2329
          Echo(x, "is prime: ", primeStatus);
2330
2331
          x := x + 1;
2332
     ];
2333
      %/mathpiper
2334
          %output, preserve="false"
2335
            Result: True
2336
2337
            Side Effects:
2338
            1 is prime: False
2339
            2 is prime: True
2340
            3 is prime: True
2341
            4 is prime: False
2342
            5 is prime: True
2343
            6 is prime: False
2344
            7 is prime: True
2345
            8 is prime: False
2346
            9 is prime: False
2347
            10 is prime: False
            11 is prime: True
2348
2349
            12 is prime: False
```

```
2350
            13 is prime: True
2351
            14 is prime: False
2352
            15 is prime: False
2353
            16 is prime: False
2354
            17 is prime: True
2355
            18 is prime: False
2356
            19 is prime: True
2357
            20 is prime: False
2358
          %/output
2359
     This program worked fairly well, but it is limited because it prints a line for each
      prime number and also each non-prime number. This means that if large ranges
2360
2361
      of integers were processed, enormous amounts of output would be produced.
      The following program solves this problem by using an If() function to only print
2362
2363
      a number if it is prime:
```

```
2364
      %mathpiper
2365
      //Print the prime numbers between 1 and 50 (inclusive).
2366
      x := 1;
2367
      While (x \leq 50)
2368
2369
          primeStatus := IsPrime(x);
2370
2371
          If(primeStatus = True, Write(x,,));
2372
2373
          x := x + 1;
2374
      1;
2375
      %/mathpiper
2376
          %output, preserve="false"
2377
            Result: True
2378
2379
            Side Effects:
2380
            2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,
2381
          %/output
```

This program is able to process a much larger range of numbers than the previous one without having its output fill up the text area. However, the program itself can be shortened by moving the **IsPrime()** function **inside** of the **If()** function instead of using the **primeStatus** variable to communicate with it:

```
2386 %mathpiper 2387 /*
```

2382

2383

23842385

```
2388
          Print the prime numbers between 1 and 50 (inclusive).
2389
          This is a shorter version which places the IsPrime() function
2390
          inside of the If() function instead of using a variable.
2391
2392
     x := 1;
2393
     While (x \leq 50)
2394
2395
          If (IsPrime(x), Write(x,,));
2396
2397
          x := x + 1;
2398
     ];
2399
      %/mathpiper
2400
          %output, preserve="false"
2401
            Result: True
2402
2403
            Side Effects:
2404
            2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,
2405
     . %/output
```

2406 14.2 Finding The Length Of A String With The Length() Function

Strings can contain zero or more characters and the **Length()** function can be used to determine how many characters a string holds:

```
2409    In> s := "Red"
2410    Result> "Red"

2411    In> Length(s)
2412    Result> 3
```

- 2413 In this example, the string "Red" is assigned to the variable $\bf s$ and then $\bf s$ is
- 2414 passed to the **Length()** function. The **Length()** function returned a **3** which
- 2415 means the string contained **3 characters**.
- 2416 The following example shows that strings can also be passed to functions
- 2417 directly:

```
2418 In> Length("Red")
2419 Result> 3
```

- 2420 An **empty string** is represented by **two double quote marks with no space in**
- 2421 **between them**. The **length** of an empty string is **0**:

```
2422 In> Length("")
2423 Result> 0
```

2424 14.3 Converting Numbers To Strings With The String() Function

- 2425 Sometimes it is useful to convert a number to a string so that the individual
- 2426 digits in the number can be analyzed or manipulated. The following example
- 2427 shows a **number** being converted to a **string** with the **String()** function so that
- 2428 its **leftmost** and **rightmost** digits can be placed into **variables**:

```
2429
     In> number := 523
2430
     Result> 523
2431
     In> stringNumber := String(number)
2432
     Result> "523"
2433
     In> leftmostDigit := stringNumber[1]
2434
     Result> "5"
2435
     In> rightmostDigit := stringNumber[ Length(stringNumber) ]
2436
     Result> "3"
```

- Notice that the Length() function is used here to determine which character in
- 2438 **stringNumber** held the **rightmost** digit.

2439 14.4 Finding Prime Numbers Which End With 7 (And Multi-line Function

2440 **Calls**)

- Now that we have covered how to turn a number into a string, lets use this
- 2442 ability inside a loop. The following program finds all the **prime numbers**
- between **1** and **500** which have a **7 as their rightmost digit**. There are three
- 2444 important things which are shown in this program:
- 2445 1) Function calls **can have their parameters placed on more than one**
- line if the parameters are too long to fit on a single line. In this case, a long
- 2447 code block is being placed inside of an If() function.
- 2448 2) Code blocks (which are considered to be compound expressions) **cannot**
- have a semicolon placed after them if they are in a function call. If a
- semicolon is placed after this code block, an error will be produced.
- 2451 3) If() functions can be placed inside of other If() functions in order to make
- 2452 more complex decisions. This is referred to as **nesting** functions.
- 2453 When the program is executed, it finds 24 prime numbers which have 7 as their
- 2454 rightmost digit:

```
2455
     %mathpiper
2456
     /*
2457
          Find all the prime numbers between 1 and 500 which have a 7
2458
          as their rightmost digit.
2459
     * /
2460
    x := 1;
2461
     While (x <= 500)
2462
2463
          //Notice how function parameters can be put on more than one line.
2464
          If (IsPrime (x),
2465
              [
2466
                  stringVersionOfNumber := String(x);
2467
2468
                  stringLength := Length(stringVersionOfNumber);
2469
2470
                  //Notice that If() functions can be placed inside of other
2471
                  // If() functions.
2472
                  If(stringVersionOfNumber[stringLength] = "7", Write(x,,));
2473
2474
              ] //Notice that semicolons cannot be placed after code blocks
2475
                //which are in function calls.
2476
2477
          ); //This is the close parentheses for the outer If() function.
2478
2479
          x := x + 1;
2480
     ];
2481
     %/mathpiper
          %output,preserve="false"
2482
2483
            Result: True
2484
2485
            Side Effects:
2486
            7,17,37,47,67,97,107,127,137,157,167,197,227,257,277,307,317,
2487
            337, 347, 367, 397, 457, 467, 487,
2488
          %/output
```

It would be nice if we had the ability to store these numbers someplace so that they could be processed further and this is discussed in the next section.

2491 **14.5 Exercises**

2492 **14.5.1 Exercise 1**

Write a program which uses a loop to determine how many prime numbers there are between 1 and 1000. You do not need to print the numbers themselves, just how many there are.

2496 **14.5.2 Exercise 2**

2497 Write a program which uses a loop to print all of the prime numbers between

2498 10 and 99 which contain the digit 3 in either their 1's place, or their

2499 10's place, or both places.

15 Lists: Values That Hold Sequences Of Expressions

- 2501 The **list** value type is designed to hold expressions in an **ordered collection** or
- 2502 **sequence**. Lists are very flexible and they are one of the most heavily used
- value types in MathPiper. Lists can **hold expressions of any type**, they can be
- 2504 made to **grow and shrink as needed**, and they can be **nested**. Expressions in a
- 2505 list can be accessed by their position in the list (similar to the way that
- characters in a string are accessed) and they can also be **replaced by other**
- 2507 **expressions**.

2500

- 2508 One way to create a list is by placing zero or more expressions separated by
- 2509 commas inside of a **pair of braces {}**. In the following example, a list is created
- 2510 that contains various expressions and then it is assigned to the variable \mathbf{x} :

```
2511 In> x := {7,42,"Hello",1/2,var}
2512 Result> {7,42,"Hello",1/2,var}
2513 In> x
```

Result> {7,42, "Hello", 1/2, var}

- 2515 The number of expressions in a list can be determined with the **Length()**
- 2516 function:

2514

```
2517 In> Length({7,42,"Hello",1/2,var})
2518 Result> 5
```

- 2519 A single expression in a list can be accessed by placing a set of **brackets** [] to
- 2520 the right of the variable that is bound to the list and then putting the
- expression's position number inside of the brackets (**Note: the first expression**
- 2522 in the list is at position 1 counting from the left end of the list):

```
2523
      In> x[1]
2524
      Result> 7
2525
      In> x[2]
2526
     Result> 42
2527
      In> x[3]
2528
      Result> "Hello"
2529
      In> x[4]
2530
     Result> 1/2
2531
      In> x[5]
2532
      Result> var
```

2533 The **1st** and **2nd** expressions in this list are **integers**, the **3rd** expression is a

- 2534 **string**, the **4th** expression is a **rational number** and the **5th** expression is an
- 2535 unbound variable.
- 2536 Lists can also hold other lists as shown in the following example:

```
2537
      In> x := \{20, 30, \{31, 32, 33\}, 40\}
2538
     Result> {20,30,{31,32,33},40}
2539
      In> x[1]
2540
    Result> 20
2541
     In> x[2]
2542
    Result> 30
2543
     In> x[3]
2544
     Result> {31,32,33}
2545
     In> x[4]
```

- 2548 The expression in the **3rd** position in the list is another **list** which contains the
- 2549 integers **31**, **32**, and **33**.

Result> 40

- 2550 An expression in this second list can be accessed by two **two sets of brackets**:
- 2551 In> x[3][2] 2552 Result> 32

2546

2547

- 2553 The **3** inside of the first set of brackets accesses the **3rd** member of the **first** list
- 2554 and the **2** inside of the second set of brackets accesses the **2nd** member of the
- 2555 **second** list.

2556 15.1 Append() & Nondestructive List Operations

```
Append(list, expression)
```

2557 The **Append()** function adds an expression to the end of a list:

```
2558 In> testList := {21,22,23}
2559 Result> {21,22,23}
2560 In> Append(testList, 24)
2561 Result> {21,22,23,24}
```

- 2562 However, instead of changing the **original** list, **Append()** creates a **copy** of the
- original list and appends the expression to the copy. This can be confirmed by
- evaluating the variable **testList** after the **Append()** function has been called:

2598

%/mathpiper

%output, preserve="false"

```
2565
      In> testList
2566
      Result> {21,22,23}
2567
      Notice that the list that is bound to testList was not modified by the Append()
      function. This is called a nondestructive list operation and most MathPiper
2568
      functions that manipulate lists do so nondestructively. To have the new list
2569
2570
      bound to the variable that is being used, the following technique can be
2571
      employed:
2572
      In> testList := \{21, 22, 23\}
2573
      Result> {21,22,23}
2574
      In> testList := Append(testList, 24)
2575
      Result> {21,22,23,24}
2576
      In> testList
2577
      Result> {21,22,23,24}
      After this code has been executed, the new list has indeed been bound to
2578
      testList as desired.
2579
      There are some functions, such as DestructiveAppend(), which do change the
2580
      original list and most of them begin with the word "Destructive". These are
2581
      called "destructive functions" and they are advanced functions which are not
2582
      covered in this book.
2583
      15.2 Using While Loops With Lists
2584
2585
      Functions that loop can be used to select each expression in a list in turn so
      that an operation can be performed on these expressions. The following
2586
      program uses a while loop to print each of the expressions in a list:
2587
2588
      %mathpiper
2589
      //Print each number in the list.
2590
      x := \{55, 93, 40, 21, 7, 24, 15, 14, 82\};
2591
      y := 1;
2592
      While (y <= Length (x))
2593
2594
          Echo(y, "- ", x[y]);
2595
          y := y + 1;
2596
      ];
```

```
2599
             Result: True
2600
2601
            Side Effects:
2602
            1 - 55
2603
            2 - 93
             3 - 40
2604
2605
             4 - 21
2606
            5 - 7
             6 - 24
2607
2608
            7 - 15
2609
            8 - 14
             9 - 82
2610
2611
          %/output
```

A **loop** can also be used to search through a list. The following program uses a 2612 While() function and an If() function to search through a list to see if it contains 2613 the number **53**. If 53 is found in the list, a message is printed: 2614

```
2615
      %mathpiper
2616
      //Determine if 53 is in the list.
2617
      testList := \{18, 26, 32, 42, 53, 43, 54, 6, 97, 41\};
2618
      index := 1;
2619
      While(index <= Length(testList))</pre>
2620
2621
          If (testList[index] = 53,
2622
              Echo("53 was found in the list at position", index));
2623
2624
          index := index + 1;
2625
      ];
2626
      %/mathpiper
2627
          %output,preserve="false"
2628
            Result: True
2629
2630
            Side Effects:
2631
            53 was found in the list at position 5
2632
          %/output
```

When this program was executed, it determined that 53 was present in the list at 2633 2634 position **5**.

15.2.1 Using A While Loop And Append() To Place Values In A List 2635

In an earlier section it was mentioned that it would be nice if we could store a set 2636 of values for later processing and this can be done with a **while loop** and the 2637

Append() function. The following program creates an empty list and assigned it to the variable **primes**. The **while loop** and the **IsPrime()** function is then used to locate the prime integers between 1 and 50 and the **Append()** function is used to place them in the list. The last part of the program then prints some information about the numbers that were placed into the list:

```
2643
      %mathpiper
2644
     //Place the prime numbers between 1 and 50 (inclusive) into a list.
2645
     //Create an empty list.
2646
     primes := {};
2647
     x := 1;
2648
     While (x \leq 50)
2649
      [
2650
          /*
2651
              If x is prime, append it to the end of the list and then assign
2652
              the new list that is created to the variable 'primes'.
2653
2654
          If(IsPrime(x), primes := Append(primes, x ) );
2655
2656
          x := x + 1;
2657
     ];
2658
     //Print information about the primes that were found.
2659
     Echo("Primes ", primes);
2660
     Echo("The number of primes in the list = ", Length(primes) );
2661
     Echo("The first number in the list = ", primes[1] );
2662
     %/mathpiper
2663
          %output, preserve="false"
2664
            Result: True
2665
2666
            Side Effects:
2667
            Primes {2,3,5,7,11,13,17,19,23,29,31,37,41,43,47}
2668
            The number of primes in the list = 15
2669
            The first number in the list = 2
          %/output
2670
```

The ability to place values into a list with a loop is very powerful and we will be using this ability throughout the rest of the book.

15.3 Exercises

2674 **15.3.1 Exercise 1**

- 2675 Create a program that uses a loop and an IsOdd() function to analyze the
- 2676 following list and then print the number of odd numbers it contains.
- 2677 {73,94,80,37,56,94,40,21,7,24,15,14,82,93,32,74,22,68,65,52,85,61,46,86,25}

2678 **15.3.2 Exercise 2**

- 2679 Create a program that uses a loop and an IsNegativeNumber() function to
- 2680 copy all of the negative numbers in the following list into a new list.
- 2681 Use the variable negativeNumbers to hold the new list.
- 2682 {36, -29, -33, -6, 14, 7, -16, -3, -14, 37, -38, -8, -45, -21, -26, 6, 6, 38, -20, 33, 41, -
- 2683 4,24,37,40,29}

2684 **15.3.3 Exercise 3**

- 2685 Create a program that uses a loop to analyze the following list and then
- 2686 print the following information about it:
- 2687 1) The largest number in the list.
- 2688 2) The smallest number in the list.
- 2689 3) The sum of all the numbers in the list.
- **2690** {73,94,80,37,56,94,40,21,7,24,15,14,82,93,32,74,22,68,65,52,85,61,46,86,25}

2691 15.4 The ForEach() Looping Function

- 2692 The **ForEach()** function uses a **loop** to index through a list like the While()
- 2693 function does, but it is more flexible and automatic. For Each() also uses bodied
- 2694 notation like the While() function and here is its calling format:

```
ForEach(variable, list) body
```

- 2695 **ForEach()** selects each expression in a list in turn, assigns it to the passed-in
- 2696 "variable", and then executes the expressions that are inside of "body".
- 2697 Therefore, body is **executed once for each expression in the list**.

2698 15.5 Print All The Values In A List Using A ForEach() function

- 2699 This example shows how ForEach() can be used to print all of the items in a list:
- 2700 %mathpiper

```
2701
      //Print all values in a list.
2702
      ForEach (value, {50,51,52,53,54,55,56,57,58,59})
2703
2704
          Echo (value);
2705
      ];
2706
      %/mathpiper
2707
          %output,preserve="false"
2708
            Result: True
2709
2710
            Side Effects:
2711
             50
2712
             51
2713
            52
2714
             53
2715
             54
2716
             55
2717
             56
2718
            57
2719
             58
2720
             59
2721
     . %/output
```

2722 15.6 Calculate The Sum Of The Numbers In A List Using ForEach()

- 2723 In previous examples, counting code in the form $\mathbf{x} := \mathbf{x} + \mathbf{1}$ was used to count
- 2724 how many times a while loop was executed. The following program uses a
- 2725 ForEach() function and a line of code similar to this counter to calculate the
- 2726 sum of the numbers in a list:

```
2727
      %mathpiper
2728
        This program calculates the sum of the numbers
2729
2730
       in a list.
2731
2732
      //This variable is used to accumulate the sum.
2733
      sum := 0;
2734
      ForEach (x, \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\})
2735
2736
2737
            Add the contents of x to the contents of sum
2738
            and place the result back into sum.
2739
2740
          sum := sum + x;
```

```
2741
2742
          //Print the sum as it is being accumulated.
2743
          Write(sum,,);
2744
      1;
2745
      NewLine(); NewLine();
2746
      Echo("The sum of the numbers in the list = ", sum);
2747
      %/mathpiper
2748
          %output,preserve="false"
2749
            Result: True
2750
2751
            Side Effects:
2752
            1, 3, 6, 10, 15, 21, 28, 36, 45, 55,
2753
2754
            The sum of the numbers in the list = 55
2755
          %/output
```

- 2756 In the above program, the integers **1** through **10** were manually placed into a list
- 2757 by typing them individually. This method is limited because only a relatively
- 2758 small number of integers can be placed into a list this way. The following section
- 2759 discusses an operator which can be used to automatically place a large number
- 2760 of integers into a list with very little typing.

2761 **15.7 The .. Range Operator**

```
first .. last
```

- 2762 A programmer often needs to create a list which contains consecutive integers
- 2763 and the .. "range" operator can be used to do this. The first integer in the list is
- 2764 placed before the .. operator and the **last** integer in the list is placed after it
- 2765 (Note: there must be a space immediately to the left of the .. operator
- 2766 and a space immediately to the right of it or an error will be generated.).
- 2767 Here are some examples:

```
2768
      In> 1 .. 10
2769
      Result> {1,2,3,4,5,6,7,8,9,10}
2770
      In> 10 .. 1
2771
      Result> {10,9,8,7,6,5,4,3,2,1}
2772
      In> 1 .. 100
2773
      Result> {1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,
2774
                21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37,
2775
                38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54,
2776
                55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71,
```

%/output

```
2777
               72,73,74,75,76,77,78,79,80,81,82,83,84,85,86,87,88,
2778
               89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100}
2779
      In > -10 .. 10
2780
     Result> \{-10, -9, -8, -7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}
2781
      As these examples show, the .. operator can generate lists of integers in
      ascending order and descending order. It can also generate lists that are very
2782
     large and ones that contain negative integers.
2783
2784
      Remember, though, if one or both of the spaces around the .. are omitted, an
2785
      error is generated:
2786
     In > 1..3
2787
      Result>
2788
     Error parsing expression, near token .3.
      15.8 Using ForEach() With The Range Operator To Print The Prime
2789
      Numbers Between 1 And 100
2790
2791
      The following program shows how to use a ForEach() function instead of a
      While() function to print the prime numbers between 1 and 100. Notice that
2792
2793
     loops that are implemented with ForEach() often require less typing than
     their While() based equivalents:
2794
2795
      %mathpiper
2796
2797
       This program prints the prime integers between 1 and 100 using
2798
        a ForEach() function instead of a While() function. Notice that
2799
        the ForEach() version requires less typing than the While()
2800
        version.
2801
      */
2802
      ForEach (x, 1 .. 100)
2803
2804
          If(IsPrime(x), Write(x,,));
2805
     1;
2806
     %/mathpiper
2807
          %output, preserve="false"
2808
            Result: True
2809
2810
            Side Effects:
2811
            2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,53,59,61,67,71,
2812
            73,79,83,89,97,
```

15.8.1 Using ForEach() And The Range Operator To Place The Prime 2814 2815

Numbers Between 1 And 50 Into A List

A ForEach() function can also be used to place values in a list, just the the 2816 2817 While() function can:

```
2818
     %mathpiper
2819
2820
      Place the prime numbers between 1 and 50 into
2821
       a list using a ForEach() function.
2822
2823
     //Create a new list.
2824
     primes := {};
2825
     ForEach (number, 1 .. 50)
2826
          /*
2827
2828
            If number is prime, append it to the end of the list and
2829
            then assign the new list that is created to the variable
2830
            'primes'.
2831
2832
          If(IsPrime(number), primes := Append(primes, number));
2833
     ];
2834
     //Print information about the primes that were found.
2835
     Echo("Primes ", primes);
2836
     Echo("The number of primes in the list = ", Length(primes) );
2837
     Echo("The first number in the list = ", primes[1] );
2838
     %/mathpiper
2839
          %output, preserve="false"
2840
            Result: True
2841
2842
            Side Effects:
2843
            Primes {2,3,5,7,11,13,17,19,23,29,31,37,41,43,47}
2844
            The number of primes in the list = 15
2845
            The first number in the list = 2
2846
         %/output
```

2847 As can be seen from the above examples, the **ForEach()** function and the **range operator** can do a significant amount of work with very little typing. You will 2848 2849 discover in the next section that MathPiper has functions which are even more powerful than these two. 2850

2851 **15.8.2 Exercises**

2852 **15.8.3 Exercise 1**

- 2853 Create a program that uses a ForEach() function and an IsOdd() function to
- 2854 analyze the following list and then print the number of odd numbers it
- 2855 contains.
- 2856 {73,94,80,37,56,94,40,21,7,24,15,14,82,93,32,74,22,68,65,52,85,61,46,86,25}

2857 **15.8.4 Exercise 2**

- 2858 Create a program that uses a ForEach() function and an IsNegativeNumber()
- 2859 function to copy all of the negative numbers in the following list into a
- 2860 new list. Use the variable **negativeNumbers** to hold the new list.
- 2861 {36, -29, -33, -6, 14, 7, -16, -3, -14, 37, -38, -8, -45, -21, -26, 6, 6, 38, -20, 33, 41, -
- 2862 4,24,37,40,29}

2863 **15.8.5 Exercise 3**

- 2864 Create a program that uses a ForEach() function to analyze the following
- 2865 list and then print the following information about it:
- 2866 1) The largest number in the list.
- 2867 2) The smallest number in the list.
- 2868 3) The sum of all the numbers in the list.
- **2869** {73,94,80,37,56,94,40,21,7,24,15,14,82,93,32,74,22,68,65,52,85,61,46,86,25}

2870 **15.8.6 Exercise 4**

- 2871 Create a program that uses a **while loop** to make a list that contains 1000
- 2872 random integers between 1 and 100 inclusive. Then, use a ForEach()
- 2873 function to determine how many integers in the list are prime and use an
- 2874 Echo() function to print this total.

2875 16 Functions & Operators Which Loop Internally

- 2876 Looping is such a useful capability that MathPiper has many functions which
- loop internally. Now that you have some experience with loops, you can use this
- 2878 experience to help you imagine how these functions use loops to process the
- 2879 information that is passed to them.

2880 16.1 Functions & Operators Which Loop Internally To Process Lists

2881 This section discusses a number of functions that use loops to process lists.

2882 **16.1.1 TableForm()**

```
TableForm(list)
```

- 2883 The **TableForm()** function prints the contents of a list in the form of a table.
- 2884 Each member in the list is printed on its own line and this sometimes makes the
- 2885 contents of the list easier to read:

```
2886
      In> testList := \{2,4,6,8,10,12,14,16,18,20\}
2887
      Result> {2,4,6,8,10,12,14,16,18,20}
2888
      In> TableForm(testList)
2889
      Result> True
2890
      Side Effects>
2891
      2
2892
      4
2893
      6
2894
      8
2895
      10
2896
      12
2897
      14
2898
      16
2899
      18
2900
      20
```

16.1.2 Contains()

2901

The **Contains()** function searches a list to determine if it contains a given expression. If it finds the expression, it returns **True** and if it doesn't find the expression, it returns **False**. Here is the calling format for Contains():

```
Contains(list, expression)
```

2905 The following code shows Contains() being used to locate a number in a list:

```
2906 In> Contains({50,51,52,53,54,55,56,57,58,59}, 53)
2907 Result> True

2908 In> Contains({50,51,52,53,54,55,56,57,58,59}, 75)
2909 Result> False
```

2910 The **Not()** function can also be used with predicate functions like Contains() to

2911 change their results to the opposite truth value:

```
2912 In> Not Contains({50,51,52,53,54,55,56,57,58,59}, 75)
2913 Result> True
```

2914 **16.1.3 Find()**

```
Find(list, expression)
```

- 2915 The **Find()** function searches a list for the first occurrence of a given expression.
- 2916 If the expression is found, the **position of its first occurrence** is returned and
- 2917 if it is not found, **-1** is returned:

```
2918 In> Find({23, 15, 67, 98, 64}, 15)
2919 Result> 2
2920 In> Find({23, 15, 67, 98, 64}, 8)
2921 Result> -1
```

2922 **16.1.4 Count()**

```
Count(list, expression)
```

2923 **Count()** determines the number of times a given expression occurs in a list:

```
2924
      In> testList := \{a,b,b,c,c,c,d,d,d,d,e,e,e,e,e\}
2925
     Result> {a,b,b,c,c,c,d,d,d,d,e,e,e,e,e,e}
2926
      In> Count(testList, c)
2927
     Result> 3
2928
      In> Count(testList, e)
2929
     Result> 5
2930
     In> Count(testList, z)
2931
     Result> 0
```

16.1.5 **Select()** 2932

```
Select(predicate function, list)
```

- **Select()** returns a list that contains all the expressions in a list which make a 2933
- given predicate function return **True**: 2934

```
2935
     In> Select("IsPositiveInteger", {46,87,59,-27,11,86,-21,-58,-86,-52})
2936
     Result> {46,87,59,11,86}
```

- 2937 In this example, notice that the **name** of the predicate function is passed to
- Select() in **double quotes**. There are other ways to pass a predicate function to 2938
- 2939 Select() but these are covered in a later section.
- 2940 Here are some further examples which use the Select() function:

```
2941
     In> Select("IsOdd", {16,14,82,92,33,74,99,67,65,52})
2942
     Result> {33,99,67,65}
2943
     In> Select("IsEven", {16,14,82,92,33,74,99,67,65,52})
2944
     Result> {16,14,82,92,74,52}
2945
     In> Select("IsPrime", 1 .. 75)
2946
     Result> {2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,53,59,61,67,71,73}
```

- Notice how the third example uses the .. operator to automatically generate a list 2947
- of consecutive integers from 1 to 75 for the Select() function to analyze. 2948

16.1.6 The Nth() Function & The [] Operator 2949

```
Nth(list, index)
```

- 2950 The **Nth()** function simply returns the expression which is at a given position in
- a list. This example shows the **third** expression in a list being obtained: 2951

```
2952
      In> testList := \{a,b,c,d,e,f,g\}
2953
     Result> {a,b,c,d,e,f,g}
2954
      In> Nth(testList, 3)
2955
     Result> c
```

- As discussed earlier, the [] operator can also be used to obtain a single 2956
- 2957 expression from a list:

```
2958 In> testList[3]
2959 Result> c
```

- 2960 The [] operator can even obtain a single expression directly from a list without
- 2961 needing to use a variable:
- 2962 In> {a,b,c,d,e,f,g}[3]
- 2963 Result> c

2964 **16.1.7 The : Prepend Operator**

```
expression : list
```

- 2965 The prepend operator is a colon: and it can be used to add an expression to the
- 2966 beginning of a list:

```
2967 In> testList := \{b,c,d\}
```

- 2968 Result> $\{b,c,d\}$
- 2969 In> testList := a:testList
- 2970 Result> $\{a,b,c,d\}$

2971 **16.1.8 Concat()**

```
Concat(list1, list2, ...)
```

- 2972 The Concat() function is short for "concatenate" which means to join together
- 2973 sequentially. It takes two or more lists and joins them together into a single
- 2974 larger list:

```
2975 In> Concat(\{a,b,c\}, \{1,2,3\}, \{x,y,z\})
```

2976 Result> $\{a,b,c,1,2,3,x,y,z\}$

2977 16.1.9 Insert(), Delete(), & Replace()

```
Insert(list, index, expression)
```

```
Delete(list, index)
```

```
Replace (list, index, expression)
```

```
Insert() inserts an expression into a list at a given index, Delete() deletes an expression from a list at a given index, and Replace() replaces an expression in a list at a given index with another expression:
```

```
2981
     In> testList := \{a,b,c,d,e,f,g\}
2982
     Result> {a,b,c,d,e,f,q}
2983
     In> testList := Insert(testList, 4, 123)
2984
     Result> {a,b,c,123,d,e,f,g}
2985
     In> testList := Delete(testList, 4)
2986
     Result> {a,b,c,d,e,f,q}
2987
     In> testList := Replace(testList, 4, xxx)
2988
     Result> {a,b,c,xxx,e,f,g}
```

2989 **16.1.10 Take()**

```
Take(list, amount)
Take(list, -amount)
Take(list, {begin_index,end_index})
```

- Take() obtains a sublist from the **beginning** of a list, the **end** of a list, or the middle of a list. The expressions in the list that are not taken are discarded.
- 2992 A **positive** integer passed to Take() indicates how many expressions should be
- 2993 taken from the **beginning** of a list:

```
2994    In> testList := {a,b,c,d,e,f,g}
2995    Result> {a,b,c,d,e,f,g}

2996    In> Take(testList, 3)
2997    Result> {a,b,c}
```

2998 A **negative** integer passed to Take() indicates how many expressions should be

```
2999 taken from the end of a list:
```

```
3000 In> Take(testList, -3) 3001 Result> \{e, f, g\}
```

- 3002 Finally, if a **two member list** is passed to Take() it indicates the **range** of
- 3003 expressions that should be taken from the **middle** of a list. The **first** value in the
- 3004 passed-in list specifies the **beginning** index of the range and the **second** value
- 3005 specifies its **end**:

```
3006 In> Take(testList, {3,5})
3007 Result> {c,d,e}
```

3008 **16.1.11 Drop()**

```
Drop(list, index)
Drop(list, -index)
Drop(list, {begin_index,end_index})
```

- 3009 **Drop()** does the opposite of Take() in that it **drops** expressions from the
- 3010 **beginning** of a list, the **end** of a list, or the **middle** of a list and **returns a list**
- 3011 which contains the remaining expressions.
- 3012 A **positive** integer passed to Drop() indicates how many expressions should be
- 3013 dropped from the **beginning** of a list:

```
3014    In> testList := {a,b,c,d,e,f,g}
3015    Result> {a,b,c,d,e,f,g}

3016    In> Drop(testList, 3)
3017    Result> {d,e,f,g}
```

- 3018 A **negative** integer passed to Drop() indicates how many expressions should be
- 3019 dropped from the **end** of a list:

```
3020 In> Drop(testList, -3)
3021 Result> {a,b,c,d}
```

- Finally, if a **two member list** is passed to Drop() it indicates the **range** of
- 3023 expressions that should be dropped from the **middle** of a list. The **first** value in
- 3024 the passed-in list specifies the **beginning** index of the range and the **second**
- 3025 value specifies its **end**:

```
3026 In> Drop(testList, {3,5})
3027 Result> {a,b,f,g}
```

3028 **16.1.12** FillList()

```
FillList(expression, length)
```

- 3029 The FillList() function simply creates a list which is of size "length" and fills it
- 3030 with "length" copies of the given expression:

```
3031 In> FillList(a, 5)
3032 Result> {a,a,a,a,a}

3033 In> FillList(42,8)
3034 Result> {42,42,42,42,42,42,42,42}
```

16.1.13 RemoveDuplicates() 3035

```
RemoveDuplicates(list)
```

RemoveDuplicates() removes any duplicate expressions that are contained in a 3036

```
3037
```

```
3038
     In> testList := {a,a,b,c,c,b,b,a,b,c,c}
3039
     Result> {a,a,b,c,c,b,b,a,b,c,c}
3040
```

In> RemoveDuplicates(testList)

3041 Result> {a,b,c}

3042 16.1.14 Reverse()

```
Reverse(list)
```

Reverse() reverses the order of the expressions in a list: 3043

```
3044
      In> testList := \{a,b,c,d,e,f,g,h\}
3045
     Result> {a,b,c,d,e,f,q,h}
3046
     In> Reverse(testList)
3047
     Result> {h,g,f,e,d,c,b,a}
```

16.1.15 **Partition()** 3048

```
Partition(list, partition size)
```

The **Partition()** function breaks a list into sublists of size "partition size": 3049

```
3050
     In> testList := \{a,b,c,d,e,f,g,h\}
3051
     Result> {a,b,c,d,e,f,g,h}
3052
     In> Partition(testList, 2)
3053
     Result> {{a,b},{c,d},{e,f},{g,h}}
```

If the partition size does not divide the length of the list **evenly**, the remaining 3054

elements are discarded: 3055

```
3056
     In> Partition(testList, 3)
3057
     Result> {{h,b,c},{d,e,f}}
```

- 3058 The number of elements that Partition() will discard can be calculated by
- 3059 dividing the length of a list by the partition size and obtaining the **remainder**:

```
3060 In> Length(testList) % 3 3061 Result> 2
```

- Remember that % is the remainder operator. It divides two integers and returns
- 3063 their remainder.

3064 **16.1.16 Table()**

```
Table(expression, variable, begin_value, end_value, step_amount)
```

- 3065 The Table() function creates a list of values by doing the following:
- 3066 1) Generating a sequence of values between a "begin_value" and an "end value" with each value being incremented by the "step amount".
- 3068 2) Placing each value in the sequence into the specified "variable", one value at a time.
- 3) Evaluating the defined "expression" (which contains the defined "variable") for each value, one at a time.
- 3072 4) Placing the result of each "expression" evaluation into the result list.
- 3073 This example generates a list which contains the integers 1 through 10:

```
3074 In> Table(x, x, 1, 10, 1)
3075 Result> \{1,2,3,4,5,6,7,8,9,10\}
```

- Notice that the expression in this example is simply the variable 'x' itself with no
- 3077 other operations performed on it.
- 3078 The following example is similar to the previous one except that its expression
- 3079 multiplies 'x' by 2:

```
3080 In> Table(x*2, x, 1, 10, 1)
3081 Result> {2,4,6,8,10,12,14,16,18,20}
```

- 3082 Lists which contain decimal values can also be created by setting the
- 3083 "step amount" to a decimal:

```
3084 In> Table(x, x, 0, 1, .1)
3085 Result> \{0,0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9,1\}
```

3086 **16.1.17 HeapSort()**

```
HeapSort(list, compare)
```

- 3087 **HeapSort()** sorts the elements of **list** into the order indicated by **compare** with
- 3088 compare typically being the **less than** operator "<" or the **greater than**
- 3089 operator ">":

```
3090
      In> HeapSort(\{4,7,23,53,-2,1\}, "<");
3091
      Result: \{-2, 1, 4, 7, 23, 53\}
3092
      In> HeapSort({4,7,23,53,-2,1}, ">");
      Result: \{53, 23, 7, 4, 1, -2\}
3093
3094
      In> HeapSort (\{1/2, 3/5, 7/8, 5/16, 3/32\}, "<")
3095
      Result: {3/32,5/16,1/2,3/5,7/8}
3096
      In> HeapSort (\{.5, 3/5, .76, 5/16, 3/32\}, "<")
3097
      Result: \{3/32, 5/16, .5, 3/5, .76\}
```

3098 16.2 Functions That Work With Integers

- 3099 This section discusses various functions which work with integers. Some of
- 3100 these functions also work with non-integer values and their use with non-
- 3101 integers is discussed in other sections.

3102 16.2.1 RandomIntegerVector()

```
RandomIntegerVector(length, lowest_possible, highest_possible)
```

- 3103 A vector is a list that does not contain other lists. **RandomIntegerVector()**
- 3104 creates a list of size "length" that contains random integers that are no lower
- 3105 than "lowest possible" and no higher than "highest possible". The following
- 3106 example creates **10** random integers between **1** and **99** inclusive:

```
3107 In> RandomIntegerVector(10, 1, 99)
3108 Result> {73,93,80,37,55,93,40,21,7,24}
```

3109 **16.2.2 Max() & Min()**

```
Max(value1, value2)
Max(list)
```

- 3110 If two values are passed to Max(), it determines which one is larger:
- 3111 In> Max(10, 20)

```
3112 Result> 20
```

3113 If a list of values are passed to Max(), it finds the largest value in the list:

```
3114    In> testList := RandomIntegerVector(10, 1, 99)
3115    Result> {73,93,80,37,55,93,40,21,7,24}

3116    In> Max(testList)
3117    Result> 93
```

3118 The **Min()** function is the opposite of the Max() function.

```
Min(value1, value2)
Min(list)
```

- 3119 If two values are passed to Min(), it determines which one is smaller:
- 3120 In> Min(10, 20)
- 3121 Result> 10
- 3122 If a list of values are passed to Min(), it finds the smallest value in the list:
- 3123 In> testList := RandomIntegerVector(10, 1, 99)
- 3124 Result> {73,93,80,37,55,93,40,21,7,24}
- 3125 In> Min(testList)
- 3126 Result> 7

3127 **16.2.3 Div() & Mod()**

```
Div(dividend, divisor)
Mod(dividend, divisor)
```

- 3128 **Div()** stands for "divide" and determines the whole number of times a divisor
- 3129 goes into a dividend:
- 3130 In> Div(7, 3)
- 3131 Result> 2
- 3132 **Mod()** stands for "modulo" and it determines the remainder that results when a
- 3133 dividend is divided by a divisor:
- 3134 In> Mod(7,3)
- 3135 Result> 1

3136 The remainder/modulo operator % can also be used to calculate a remainder:

```
3137 In> 7 % 2
3138 Result> 1
```

3139 **16.2.4 Gcd()**

```
Gcd(value1, value2)
Gcd(list)
```

- 3140 GCD stands for Greatest Common Divisor and the Gcd() function determines the
- 3141 greatest common divisor of the values that are passed to it.
- 3142 If two integers are passed to Gcd(), it calculates their greatest common divisor:

```
3143 In> Gcd(21, 56)
3144 Result> 7
```

- 3145 If a list of integers are passed to Gcd(), it finds the greatest common divisor of all
- 3146 the integers in the list:

```
3147 In> Gcd({9, 66, 123})
```

3148 Result> 3

3149 **16.2.5 Lcm()**

```
Lcm(value1, value2)
Lcm(list)
```

- 3150 LCM stands for Least Common Multiple and the Lcm() function determines the
- least common multiple of the values that are passed to it.
- 3152 If two integers are passed to Lcm(), it calculates their least common multiple:

```
3153 In> Lcm(14, 8)
3154 Result> 56
```

- 3155 If a list of integers are passed to Lcm(), it finds the least common multiple of all
- 3156 the integers in the list:

```
3157 In> Lcm({3,7,9,11})
```

3158 Result> 693

3159 **16.2.6 Sum()**

Sum(list)

- 3160 **Sum()** can find the sum of a list that is passed to it:
- 3161 In> testList := RandomIntegerVector(10,1,99)
- 3162 Result> {73,93,80,37,55,93,40,21,7,24}
- 3163 In> Sum(testList)
- 3164 Result> 523
- 3165 In> testList := 1 .. 10
- 3166 Result> {1,2,3,4,5,6,7,8,9,10}
- 3167 In> Sum(testList)
- 3168 Result> 55

3169 **16.2.7 Product()**

Product(list)

- 3170 This function has two calling formats, only one of which is discussed here.
- 3171 Product(list) multiplies all the expressions in a list together and returns their
- 3172 product:
- 3173 In> Product({1,2,3})
- 3174 Result> 6

3175 **16.3 Exercises**

3176 **16.3.1 Exercise 1**

- 3177 Create a program that uses RandomIntegerVector() to create a 100 member
- 3178 list that contains random integers between 1 and 5 inclusive. Use Count()
- 3179 to determine how many of each digit 1-5 are in the list and then print this
- 3180 information. Hint: you can use the HeapSort() function to sort the
- 3181 generated list to make it easier to check if your program is counting
- 3182 correctly.

3183 **16.3.2 Exercise 2**

- 3184 Create a program that uses RandomIntegerVector() to create a 100 member
- 3185 list that contains random integers between 1 and 50 inclusive and use
- 3186 Contains() to determine if the number 25 is in the list. Print "25 was in
- 3187 the list." if 25 was found in the list and "25 was not in the list." if it

3188 wasn't found.

3189 **16.3.3 Exercise 3**

- 3190 Create a program that uses RandomIntegerVector() to create a 100 member
- 3191 list that contains random integers between 1 and 50 inclusive and use
- 3192 Find() to determine if the number 10 is in the list. Print the position of
- 3193 10 if it was found in the list and "10 was not in the list." if it wasn't
- 3194 found.

3195 **16.3.4 Exercise 4**

- 3196 Create a program that uses RandomIntegerVector() to create a 100 member
- 3197 list that contains random integers between 0 and 3 inclusive. Use Select()
- 3198 with the IsNonZeroInteger() predicate function to obtain all of the nonzero
- 3199 integers in this list.

3200 **16.3.5 Exercise 5**

- 3201 Create a program that uses **Table()** to obtain a list which contains the
- 3202 squares of the integers between 1 and 10 inclusive.

3203

3213

17 Nested Loops

- Now that you have seen how to solve problems with single loops, it is time to
- 3205 discuss what can be done when a loop is placed inside of another loop. A loop
- 3206 that is placed **inside** of another loop it is called a **nested loop** and this nesting
- 3207 can be extended to numerous levels if needed. This means that loop 1 can have
- 3208 loop 2 placed inside of it, loop 2 can have loop 3 placed inside of it, loop 3 can
- 3209 have loop 4 placed inside of it, and so on.
- Nesting loops allows the programmer to accomplish an enormous amount of
- 3211 work with very little typing.

17.1 Generate All The Combinations That Can Be Entered Into A Two Digit

Wheel Lock Using Two Nested Loops



- 3214 The following program generates all the combinations that can be entered into a
- 3215 two digit wheel lock. It uses a nested loop to accomplish this with the "**inside**"
- nested loop being used to generate **one's place** digits and the "**outside**" loop
- 3217 being used to generate **ten's place** digits.

```
3218 %mathpiper
```

```
3219 /* Generate all the combinations can be entered into a two digit wheel lock.
```

3222 */

3223 combinations := {};

3224 ForEach (digit1, 0 .. 9) //This loop is called the "outside" loop.

3225

[

```
3226
          ForEach (digit2, 0 .. 9) // This loop is called the "inside" loop.
3227
3228
               combinations := Append(combinations, {digit1, digit2});
3229
          ];
3230
     ];
3231
      Echo (TableForm (combinations));
3232
      %/mathpiper
3233
          %output,preserve="false"
3234
            Result: True
3235
3236
            Side Effects:
3237
            {0,0}
3238
            {0,1}
3239
            {0,2}
3240
            {0,3}
3241
             {0,4}
3242
            {0,5}
3243
            {0,6}
3244
3245
               . //The middle of the list has not been shown.
3246
3247
             {9,3}
3248
            {9,4}
3249
            {9,5}
3250
            {9,6}
3251
            {9,7}
3252
            {9,8}
3253
            {9,9}
3254
            True
3255
          %/output
```

- 3256 The relationship between the outside loop and the inside loop is interesting
- because each time the **outside loop cycles once**, the **inside loop cycles 10**
- 3258 **times**. Study this program carefully because nested loops can be used to solve a
- 3259 wide range of problems and therefore understanding how they work is
- 3260 important.

3261

17.2 Exercises

3262 17.2.1 Exercise 1

3263 Create a program that will generate all of the combinations that can be 3264 entered into a three digit wheel lock. (Hint: a triple nested loop can be 3265 used to accomplish this.)

18 User Defined Functions

- 3267 In computer programming, a **function** is a named section of code that can be
- 3268 **called** from other sections of code. **Values** can be sent to a function for
- 3269 processing as part of the **call** and a function always returns a value as its result.
- 3270 A function can also generate side effects when it is called and side effects have
- 3271 been covered in earlier sections.
- 3272 The values that are sent to a function when it is called are called **arguments** or
- 3273 **actual parameters** and a function can accept 0 or more of them. These
- 3274 arguments are placed within parentheses.
- 3275 MathPiper has many predefined functions (some of which have been discussed in
- 3276 previous sections) but users can create their own functions too. The following
- program creates a function called **addNums()** which takes two numbers as
- 3278 arguments, adds them together, and returns their sum back to the calling code
- 3279 as a result:

3266

- 3280 In> addNums(num1, num2) := num1 + num2
- 3281 Result> True
- 3282 This line of code defined a new function called **addNums** and specified that it
- 3283 will accept two values when it is called. The **first** value will be placed into the
- variable **num1** and the **second** value will be placed into the variable **num2**.
- 3285 Variables like num1 and num2 which are used in a function to accept values from
- 3286 calling code are called **formal parameters**. **Formal parameter variables** are
- 3287 used inside a function to process the values/actual parameters/arguments
- 3288 that were placed into them by the calling code.
- 3289 The code on the **right side** of the **assignment operator** is **bound** to the
- 3290 function name "addNums" and it is executed each time addNums() is called.
- 3291 The following example shows the new **addNums()** function being called multiple
- 3292 times with different values being passed to it:
- 3293 In> addNums(2,3)
- 3294 Result> 5
- 3295 In> addNums (4,5)
- 3296 Result> 9
- 3297 In> addNums (9,1)
- 3298 Result> 10
- Notice that, unlike the functions that come with MathPiper, we chose to have this
- 3300 function's name start with a **lower case letter**. We could have had addNums()
- begin with an upper case letter but it is a **convention** in MathPiper for **user**

- defined function names to begin with a lower case letter to distinguish them from the functions that come with MathPiper.
- 3304 The values that are returned from user defined functions can also be assigned to
- variables. The following example uses a %mathpiper fold to define a function
- 3306 called **evenIntegers()** and then this function is used in the MathPiper console:

```
3307
      %mathpiper
3308
      evenIntegers (endInteger) :=
3309
3310
          resultList := {};
3311
          x := 2;
3312
3313
          While(x <= endInteger)</pre>
3314
3315
              resultList := Append(resultList, x);
3316
              x := x + 2;
3317
          1;
3318
          /*
3319
3320
           The result of the last expression which is executed in a function
           is the result that the function returns to the caller. In this case,
3321
3322
           resultList is purposely being executed last so that its contents are
3323
           returned to the caller.
3324
3325
          resultList;
3326
     ];
3327
      %/mathpiper
3328
          %output, preserve="false"
3329
            Result: True
3330
          %/output
3331
      In> a := evenIntegers(10)
3332
     Result> \{2, 4, 6, 8, 10\}
3333
      In> Length(a)
3334
     Result> 5
```

- 3335 The function **evenIntegers()** returns a list which contains all the even integers
- from 2 up through the value that was passed into it. The fold was first executed
- in order to define the **evenIntegers()** function and make it ready for use. The
- evenIntegers() function was then called from the MathPiper console and 10
- 3339 was passed to it.
- 3340 After the function was finished executing, it returned a list of even integers as a

- result and this result was assigned to the variable 'a'. We then passed the list
- that was assigned to 'a' to the **Length()** function in order to determine its size.

3343 18.1 Global Variables, Local Variables, & Local()

- 3344 The new **evenIntegers()** function seems to work well, but there is a problem.
- 3345 The variables 'x' and resultList were defined inside the function as global
- variables which means they are accessible from anywhere, including from
- 3347 within other functions, within other folds (as shown here):

```
3348
      %mathpiper
3349
      Echo(x, ",", resultList);
3350
      %/mathpiper
3351
          %output, preserve="false"
3352
            Result: True
3353
3354
            Side Effects:
3355
            12 , {2,4,6,8,10}
3356
          %/output
```

and from within the MathPiper console:

```
3358 In> x
3359 Result> 12
3360 In> resultList
3361 Result> {2,4,6,8,10}
```

3362 Using global variables inside of functions is usually not a good idea

- because code in other functions and folds might already be using (or will use) the
- 3364 same variable names. Global variables which have the same name are the same
- variable. When one section of code changes the value of a given global variable,
- 3366 the value is changed everywhere that variable is used and this will eventually
- 3367 cause problems.
- 3368 In order to prevent errors being caused by global variables having the same
- name, a function named **Local()** can be called inside of a function to define what
- are called **local variables**. A **local variable** is only accessible inside the
- function it has been defined in, even if it has the same name as a global variable.
- 3372 The following example shows a second version of the **evenIntegers()** function
- which uses **Local()** to make 'x' and **resultList** local variables:

3413 Result> resultList

```
3374
     %mathpiper
3375
     /*
3376
     This version of evenIntegers() uses Local() to make
3377
     x and resultList local variables
3378
     * /
3379
      evenIntegers (endInteger) :=
3380
3381
          Local(x, resultList);
3382
3383
          resultList := {};
3384
          x := 2;
3385
3386
          While(x <= endInteger)</pre>
3387
3388
              resultList := Append(resultList, x);
3389
              x := x + 2;
3390
          ];
3391
3392
          /*
3393
           The result of the last expression which is executed in a function
3394
           is the result that the function returns to the caller. In this case,
3395
           resultList is purposely being executed last so that its contents are
3396
           returned to the caller.
3397
          * /
3398
          resultList;
3399
    1;
3400
     %/mathpiper
3401
          %output, preserve="false"
3402
            Result: True
3403 . %/output
3404
     We can verify that 'x' and resultList are now local variables by first clearing
      them, calling evenIntegers(), and then seeing what 'x' and resultList contain:
3405
3406
     In> Clear(x, resultList)
3407
    Result> True
3408
     In> evenIntegers(10)
3409
     Result> \{2, 4, 6, 8, 10\}
3410
     In> x
3411
    Result> x
3412 In> resultList
```

3414 **18.2 Exercises**

3415 **18.2.1 Exercise 1**

- 3416 Create a function called tenOddIntegers() which returns a list which
- 3417 contains 10 random odd integers between 1 and 99 inclusive.

3418 **18.2.2 Exercise 2**

- 3419 Create a function called convertStringToList(string) which takes a string
- 3420 as a parameter and returns a list which contains all of the characters in
- 3421 the string. Here is an example of how the function should work:
- 3422 In> convertStringToList("Hello friend!")
- Result> {"H", "e", "l", "l", "o", " ", "f", "r", "i", "e", "n", "d", "!"} 3423
- 3424 In> convertStringToList("Computer Algebra System")
 3425 Result> {"C", "o", "m", "p", "u", "t", "e", "r", " ", "A", "l", "g", "e", "b", "r", "a", "
- 3426 ","S","y","s","t","e","m"}

19 Miscellaneous topics

3428 19.1 Incrementing And Decrementing Variables With The ++ And --

3429 **Operators**

3427

- 3430 Up until this point we have been adding 1 to a variable with code in the form of \mathbf{x}
- 3431 := $\mathbf{x} + \mathbf{1}$ and subtracting 1 from a variable with code in the form of $\mathbf{x} := \mathbf{x} \mathbf{1}$.
- 3432 Another name for **adding** 1 to a variable is **incrementing** it and **decrementing**
- 3433 a variable means to **subtract** 1 from it. Now that you have had some experience
- 3434 with these longer forms, it is time to show you shorter versions of them.

3435 19.1.1 Incrementing Variables With The ++ Operator

3436 The number 1 can be added to a variable by simply placing the ++ operator after

3437 it like this:

```
3438 In> x := 1

3439 Result: 1

3440 In> x++;

3441 Result: True

3442 In> x

3443 Result: 2
```

3444 Here is a program that uses the ++ operator to increment a loop index variable:

```
3445
      %mathpiper
3446
      count := 1;
3447
      While (count <= 10)</pre>
3448
3449
          Echo (count);
3450
3451
          count++; //The ++ operator increments the count variable.
3452
      ];
3453
      %/mathpiper
3454
          %output,preserve="false"
3455
             Result: True
3456
3457
             Side Effects:
3458
3459
             2
```

```
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```

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```

```
3460
             3
3461
3462
             5
3463
             6
3464
             7
3465
3466
             9
3467
             10
     . %/output
3468
```

19.1.2 Decrementing Variables With The -- Operator

The number 1 can be subtracted from a variable by simply placing the -operator after it like this:

```
3472 In> x := 1

3473 Result: 1

3474 In> x--;

3475 Result: True

3476 In> x

3477 Result: 0
```

3478 Here is a program that uses the -- operator to decrement a loop index variable:

```
3479
      %mathpiper
3480
      count := 10;
3481
      While(count >= 1)
3482
3483
          Echo (count);
3484
3485
          count--; //The -- operator decrements the count variable.
3486
      ];
3487
      %/mathpiper
3488
          %output,preserve="false"
3489
            Result: True
3490
3491
            Side Effects:
3492
            10
3493
            9
3494
            8
3495
            7
3496
            6
```

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3498		4
3499		3
3500		2
3501		1
3502	•	%/output