

# **Introduction To Programming With MathRider And MathPiper**

**by Ted Kosan**

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# 1 Preface

## 2 1.1 Dedication

3 This book is dedicated to Steve Yegge and his blog entry "Math Every Day"  
4 (<http://steve.yegge.googlepages.com/math-every-day>).

## 5 1.2 Acknowledgments

6 The following people have provided feedback on this book (if I forgot to include  
7 your name on this list, please email me at ted.kosan at gmail.com):

8 Susan Addington

9 Matthew Moelter

10 Sherm Ostrowsky

## 11 1.3 Support Email List

12 The support email list for this book is called **mathrider-**  
13 **users@googlegroups.com** and you can subscribe to it at  
14 <http://groups.google.com/group/mathrider-users>.

## 15 1.4 Recommended Weekly Sequence When Teaching A Class With This 16 Book

- 17 • Week 1: Sections 1 - 6.
- 18 • Week 2: Sections 7 - 9.
- 19 • Week 3: Sections 10 - 13.
- 20 • Week 4: Sections 14 - 15.
- 21 • Week 5: Sections 16 - 19.



## 22 **2 Introduction**

23 MathRider is an open source mathematics computing environment for  
24 performing numeric and symbolic computations (the difference between numeric  
25 and symbolic computations are discussed in a later section). Mathematics  
26 computing environments are complex and it takes a significant amount of time  
27 and effort to become proficient at using one. The amount of power that these  
28 environments make available to a user, however, is well worth the effort needed  
29 to learn one. It will take a beginner a while to become an expert at using  
30 MathRider, but fortunately one does not need to be a MathRider expert in order  
31 to begin using it to solve problems.

### 32 **2.1 What Is A Mathematics Computing Environment?**

33 A Mathematics Computing Environment is a set of computer programs that 1)  
34 automatically execute a wide range of numeric and symbolic mathematics  
35 calculation algorithms and 2) provide a user interface which enables the user to  
36 access these calculation algorithms and manipulate the mathematical objects  
37 they create (An algorithm is a step-by-step sequence of instructions for solving a  
38 problem and we will be learning about algorithms later in the book).

39 Standard and graphing scientific calculator users interact with these devices  
40 using buttons and a small LCD display. In contrast to this, users interact with  
41 MathRider using a rich graphical user interface which is driven by a computer  
42 keyboard and mouse. Almost any personal computer can be used to run  
43 MathRider, including the latest subnotebook computers.

44 Calculation algorithms exist for many areas of mathematics and new algorithms  
45 are constantly being developed. Software that contains these kind of algorithms  
46 is commonly referred to as "Computer Algebra Systems (CAS)". A significant  
47 number of computer algebra systems have been created since the 1960s and the  
48 following list contains some of the more popular ones:

49 [http://en.wikipedia.org/wiki/Comparison\\_of\\_computer\\_algebra\\_systems](http://en.wikipedia.org/wiki/Comparison_of_computer_algebra_systems)

50 Some environments are highly specialized and some are general purpose. Some  
51 allow mathematics to be entered and displayed in traditional form (which is what  
52 is found in most math textbooks). Some are able to display traditional form  
53 mathematics but need to have it input as text and some are only able to have  
54 mathematics displayed and entered as text.

55 As an example of the difference between traditional mathematics form and text  
56 form, here is a formula which is displayed in traditional form:

$$a = x^2 + 4hx + \frac{3}{7}$$

57 and here is the same formula in text form:

58 
$$a = x^2 + 4h \cdot x + 3/7$$

59 Most computer algebra systems contain a mathematics-oriented programming  
60 language. This allows programs to be developed which have access to the  
61 mathematics algorithms which are included in the system. Some mathematics-  
62 oriented programming languages were created specifically for the system they  
63 work in while others were built on top of an existing programming language.

64 Some mathematics computing environments are proprietary and need to be  
65 purchased while others are open source and available for free. Both kinds of  
66 systems possess similar core capabilities, but they usually differ in other areas.

67 Proprietary systems tend to be more polished than open source systems and they  
68 often have graphical user interfaces that make inputting and manipulating  
69 mathematics in traditional form relatively easy. However, proprietary  
70 environments also have drawbacks. One drawback is that there is always a  
71 chance that the company that owns it may go out of business and this may make  
72 the environment unavailable for further use. Another drawback is that users are  
73 unable to enhance a proprietary environment because the environment's source  
74 code is not made available to users.

75 Some open source computer algebra systems do not have graphical user  
76 interfaces, but their user interfaces are adequate for most purposes and the  
77 environment's source code will always be available to whomever wants it. This  
78 means that people can use the environment for as long as they desire and they  
79 can also enhance it.

## 80 **2.2 What Is MathRider?**

81 MathRider is an open source Mathematics Computing Environment which has  
82 been designed to help people teach themselves the [STEM](#) disciplines (Science,  
83 Technology, Engineering, and Mathematics) in an efficient and holistic way. It  
84 inputs mathematics in textual form and displays it in either textual form or  
85 traditional form.

86 MathRider uses MathPiper as its default computer algebra system, BeanShell as  
87 its main scripting language, jEdit as its framework (hereafter referred to as the  
88 MathRider framework), and Java as its overall implementation language. One  
89 way to determine a person's MathRider expertise is by their knowledge of these  
90 components. (see Table 1)

Level	Knowledge
MathRider Developer	Knows Java, BeanShell, and the MathRider framework at an advanced level. Is able to develop MathRider plugins.
MathRider Customizer	Knows Java, BeanShell, and the MathRider framework at an intermediate level. Is able to develop MathRider macros.
MathRider Expert	Knows MathPiper at an advanced level and is skilled at using most aspects of the MathRider application.
MathRider Novice	Knows MathPiper at an intermediate level, but has only used MathRider for a short while.
MathRider Newbie	Does not know MathPiper but has been exposed to at least one programming language.
Programming Newbie	Does not know how a computer works and has never programmed before but knows how to use a word processor.

*Table 1: MathRider user experience levels.*

91 This book is for MathRider and Programming Newbies. This book will teach you  
 92 enough programming to begin solving problems with MathRider and the  
 93 language that is used is MathPiper. It will help you to become a MathRider  
 94 Novice, but you will need to learn MathPiper from books that are dedicated to it  
 95 before you can become a MathRider Expert.

96 The MathRider project website (<http://mathrider.org>) contains more information  
 97 about MathRider along with other MathRider resources.

## 98 **2.3 What Inspired The Creation Of Mathrider?**

99 Two of MathRider's main inspirations are Scott McNeally's concept of "No child  
 100 held back":

101 [http://weblogs.java.net/blog/turbogeek/archive/2004/09/no\\_child\\_held\\_b\\_1.html](http://weblogs.java.net/blog/turbogeek/archive/2004/09/no_child_held_b_1.html)

102 and Steve Yegge's thoughts on learning mathematics:

103 1) Math is a lot easier to pick up after you know how to program. In fact, if  
 104 you're a halfway decent programmer, you'll find it's almost a snap.

105 2) They teach math all wrong in school. Way, WAY wrong. If you teach  
 106 yourself math the right way, you'll learn faster, remember it longer, and it'll  
 107 be much more valuable to you as a programmer.

108 3) The right way to learn math is breadth-first, not depth-first. You need to  
 109 survey the space, learn the names of things, figure out what's what.

110 <http://steve-yegge.blogspot.com/2006/03/math-for-programmers.html>

111 MathRider is designed to help a person learn mathematics on their own with  
112 little or no assistance from a teacher. It makes learning mathematics easier by  
113 focusing on how to program first and it facilitates a breadth-first approach to  
114 learning mathematics.

## 115 **3 Downloading And Installing MathRider**

### 116 **3.1 *Installing Sun's Java Implementation***

117 MathRider is a Java-based application and therefore a current version of Sun's  
118 Java (at least Java 6) must be installed on your computer before MathRider can  
119 be run.

#### 120 **3.1.1 Installing Java On A Windows PC**

121 Many Windows PCs will already have a current version of Java installed. You can  
122 test to see if you have a current version of Java installed by visiting the following  
123 web site:

124 <http://java.com/>

125 This web page contains a link called "Do I have Java?" which will check your Java  
126 version and tell you how to update it if necessary.

#### 127 **3.1.2 Installing Java On A Macintosh**

128 Macintosh computers have Java pre-installed but you may need to upgrade to a  
129 current version of Java (at least Java 6) before running MathRider. If you need  
130 to update your version of Java, visit the following website:

131 <http://developer.apple.com/java.>

#### 132 **3.1.3 Installing Java On A Linux PC**

133 Locate the Java documentation for your Linux distribution and carefully follow  
134 the instructions provided for installing a Java 6 compatible version of Java on  
135 your system.

### 136 **3.2 *Downloading And Extracting***

137 One of the many benefits of learning MathRider is the programming-related  
138 knowledge one gains about how open source software is developed on the  
139 Internet. An important enabler of open source software development are  
140 websites, such as sourceforge.net (<http://sourceforge.net>) and java.net  
141 (<http://java.net>) which make software development tools available for free to  
142 open source developers.

143 MathRider is hosted at java.net and the URL for the project website is:

144 <http://mathrider.org>

MathRider can be obtained by selecting the **download** tab and choosing the correct download file for your computer. Place the download file on your hard drive where you want MathRider to be located. **For Windows users, it is recommended that MathRider be placed somewhere on c: drive.**

The MathRider download consists of a main directory (or folder) called **mathrider** which contains a number of directories and files. In order to make downloading quicker and sharing easier, the mathrider directory (and all of its contents) have been placed into a single compressed file called an **archive**. For **Windows** systems, the archive has a **.zip** extension and the archives for **Unix-based** systems have a **.tar.bz2** extension.

After an archive has been downloaded onto your computer, the directories and files it contains must be **extracted** from it. The process of extraction uncompresses copies of the directories and files that are in the archive and places them on the hard drive, usually in the same directory as the archive file. After the extraction process is complete, the archive file will still be present on your drive along with the extracted **mathrider** directory and its contents.

The **archive file** can be easily copied to a CD or USB drive if you would like to install MathRider on another computer or give it to a friend. **However, don't try to run MathRider from a USB drive because it will not work correctly.**

**(Note: If you already have a version of MathRider installed and you want to install a new version in the same directory that holds the old version, you must delete the old version first or move it to a separate directory.)**

### 3.2.1 Extracting The Archive File For Windows Users

Usually the easiest way for Windows users to extract the MathRider archive file is to navigate to the folder which contains the archive file (using the Windows GUI), **right click on the archive file (it should appear as a folder with a vertical zipper on it)**, and select **Extract All...** from the pop up menu.

After the extraction process is complete, a new folder called **mathrider** should be present in the same folder that contains the archive file. **(Note: be careful not to double click on the archive file by mistake when you are trying to open the mathrider folder. The Windows operating system will open the archive just like it opens folders and this can fool you into thinking you are opening the mathrider folder when you are not. You may want to move the archive file to another place on your hard drive after it has been extracted to avoid this potential confusion.)**

### 3.2.2 Extracting The Archive File For Unix Users

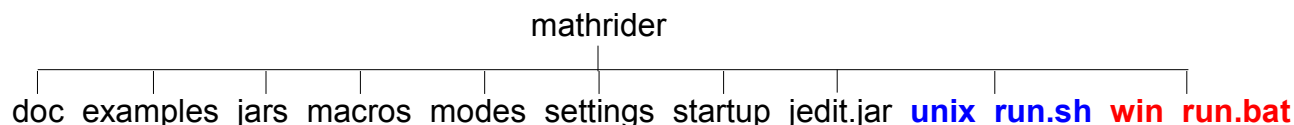
One way Unix users can extract the download file is to open a shell, change to the directory that contains the archive file, and extract it using the following command:

184     tar -xvjf <name of archive file>

185   If your desktop environment has GUI-based archive extraction tools, you can use  
186   these as an alternative.

### 187   **3.3 MathRider's Directory Structure & Execution Instructions**

188   The top level of MathRider's directory structure is shown in Illustration 1:



*Illustration 1: MathRider's Directory Structure*

189   The following is a brief description this top level directory structure:

190   **doc** - Contains MathRider's documentation files.

191   **examples** - Contains various example programs, some of which are pre-opened  
192   when MathRider is first executed.

193   **jars** - Holds plugins, code libraries, and support scripts.

194   **macros** - Contains various scripts that can be executed by the user.

195   **modes** - Contains files which tell MathRider how to do syntax highlighting for  
196   various file types.

197   **settings** - Contains the application's main settings files.

198   **startup** - Contains startup scripts that are executed each time MathRider  
199   launches.

200   **jedit.jar** - Holds the core jEdit application which MathRider builds upon.

201   **unix\_run.sh** - The script used to execute MathRider on Unix systems.

202   **win\_run.bat** - The batch file used to execute MathRider on Windows systems.

#### 203   **3.3.1 Executing MathRider On Windows Systems**

204   Open the **mathrider** folder **(not the archive file!)** and double click on the  
205   **win\_run** file.

### 206 **3.3.2 Executing MathRider On Unix Systems**

207 Open a shell, change to the **mathrider** folder, and execute the **unix\_run.sh**  
208 script by typing the following:

```
209     sh unix_run.sh
```

#### 210 **3.3.2.1 MacOS X**

211 Make a note of where you put the Mathrider application (for example  
212 **/Applications/mathrider**). Run Terminal (which is in /Applications/Utilities).  
213 Change to that directory (folder) by typing:

```
214     cd /Applications/mathrider
```

215 Run mathrider by typing:

```
216     sh unix_run.sh
```



## 217 4 The Graphical User Interface

218 MathRider is built on top of jEdit (<http://jedit.org>) so it has the "heart" of a  
219 programmer's text editor. Programmer's text editors are similar to standard text  
220 editors (like NotePad and WordPad) and word processors (like MS Word and  
221 OpenOffice) in a number of ways so getting started with MathRider should be  
222 relatively easy for anyone who has used a text editor or a word processor.  
223 However, programmer's text editors are more challenging to use than a standard  
224 text editor or a word processor because programmer's text editors have  
225 capabilities that are far more advanced than these two types of applications.

226 Most software is developed with a programmer's text editor (or environments  
227 which contain one) and so learning how to use a programmer's text editor is one  
228 of the many skills that MathRider provides which can be used in other areas.  
229 The MathRider series of books are designed so that these capabilities are  
230 revealed to the reader over time.

231 In the following sections, the main parts of MathRider's graphical user interface  
232 are briefly covered. Some of these parts are covered in more depth later in the  
233 book and some are covered in other books.

234 **As you read through the following sections, I encourage you to explore**  
235 **each part of MathRider that is being discussed using your own copy of**  
236 **MathRider.**

### 237 4.1 Buffers And Text Areas

238 In MathRider, open files are called **buffers** and they are viewed through one or  
239 more **text areas**. Each text area has a tab at its upper-left corner which displays  
240 the name of the buffer it is working on along with an indicator which shows  
241 whether the buffer has been saved or not. The user is able to select a text area  
242 by clicking its tab and double clicking on the tab will close the text area. Tabs  
243 can also be rearranged by dragging them to a new position with the mouse.

### 244 4.2 The Gutter

245 The gutter is the vertical gray area that is on the left side of the main window. It  
246 can contain line numbers, buffer manipulation controls, and context-dependent  
247 information about the text in the buffer.

### 248 4.3 Menus

249 The main menu bar is at the top of the application and it provides access to a  
250 significant portion of MathRider's capabilities. The commands (or **actions**) in  
251 these menus all exist separately from the menus themselves and they can be  
252 executed in alternate ways (such as keyboard shortcuts). The menu items (and

253 even the menus themselves) can all be customized, but the following sections  
254 describe the default configuration.

### 255 4.3.1 File

256 The File menu contains actions which are typically found in normal text editors  
257 and word processors. The actions to create new files, save files, and open  
258 existing files are all present along with variations on these actions.

259 Actions for opening recent files, configuring the page setup, and printing are  
260 also present.

### 261 4.3.2 Edit

262 The Edit menu also contains actions which are typically found in normal text  
263 editors and word processors (such as **Undo**, **Redo**, **Cut**, **Copy**, and **Paste**).  
264 However, there are also a number of more sophisticated actions available which  
265 are of use to programmers. For beginners, though, the typical actions will be  
266 sufficient for most editing needs.

### 267 4.3.3 Search

268 The actions in the Search menu are used heavily, even by beginners. A good way  
269 to get your mind around the search actions is to open the Search dialog window  
270 by selecting the **Find...** action (which is the first actions in the Search menu). A  
271 **Search And Replace** dialog window will then appear which contains access to  
272 most of the search actions.

273 At the top of this dialog window is a text area labeled **Search for** which allows  
274 the user to enter text they would like to find. Immediately below it is a text area  
275 labeled **Replace with** which is for entering optional text that can be used to  
276 replace text which is found during a search.

277 The column of radio buttons labeled **Search in** allows the user to search in a  
278 **Selection** of text (which is text which has been highlighted), the **Current**  
279 **Buffer** (which is the one that is currently active), **All buffers** (which means all  
280 opened files), or a whole **Directory** of files. The default is for a search to be  
281 conducted in the current buffer and this is the mode that is used most often.

282 The column of check boxes labeled **Settings** allows the user to either **Keep or**  
283 **hide the Search dialog window** after a search is performed, **Ignore the case**  
284 of searched text, use an advanced search technique called a **Regular**  
285 **expression** search (which is covered in another book), and to perform a  
286 **HyperSearch** (which collects multiple search results in a text area).

287 The **Find** button performs a normal find operation. **Replace & Find** will replace  
288 the previously found text with the contents of the **Replace with** text area and  
289 perform another find operation. **Replace All** will find all occurrences of the

290 contents of the **Search for** text area and replace them with the contents of the  
291 **Replace with** text area.

#### 292 **4.3.4 Markers, Folding, and View**

293 These are advanced menus and they are described in later sections.

#### 294 **4.3.5 Utilities**

295 The utilities menu contains a significant number of actions, some that are useful  
296 to beginners and others that are meant for experts. The two actions that are  
297 most useful to beginners are the **Buffer Options** actions and the **Global**  
298 **Options** actions. The **Buffer Options** actions allows the currently selected  
299 buffer to be customized and the **Global Options** actions brings up a rich dialog  
300 window that allows numerous aspects of the MathRider application to be  
301 configured.

302 Feel free to explore these two actions in order to learn more about what they do.

#### 303 **4.3.6 Macros**

304 This is an advanced menu and it is described in a later sections.

#### 305 **4.3.7 Plugins**

306 Plugins are component-like pieces of software that are designed to provide an  
307 application with extended capabilities and they are similar in concept to physical  
308 world components. The tabs on the right side of the application which are  
309 labeled "GeoGebra", "Jung", "MathPiper", "MathPiperDocs", etc. are all plugins  
310 and they can be **opened** and **closed** by clicking on their **tabs**. **Feel free to close**  
311 **any of these plugins which may be opened if you are not currently using**  
312 **them**. MathRider pPlugins are covered in more depth in a later section.

#### 313 **4.3.8 Help**

314 The most important action in the **Help** menu is the **MathRider Help** action.  
315 This action brings up a dialog window with contains documentation for the core  
316 MathRider application along with documentation for each installed plugin.

#### 317 **4.4 The Toolbar**

318 The **Toolbar** is located just beneath the menus near the top of the main window  
319 and it contains a number of icon-based buttons. These buttons allow the user to  
320 access the same actions which are accessible through the menus just by clicking  
321 on them. There is not room on the toolbar for all the actions in the menus to be

322 displayed, but the most common actions are present. The user also has the  
323 option of customizing the toolbar by using the **Utilities->Global Options->Tool**  
324 **Bar** dialog.

#### 325 **4.4.1 Undo And Redo**

326 The **Undo** button on the toolbar is able to undo any text was entered since the  
327 current session of MathRider was launched. This is very handy for undoing  
328 mistakes or getting back text which was deleted. The **Redo** button can be used  
329 if you have selected Undo too many times and you need to "undo" one ore more  
330 Undo operations.

## 331 **5 MathPiper: A Computer Algebra System For Beginners**

332 Computer algebra systems are extremely powerful and very useful for solving  
333 STEM-related problems. In fact, one of the reasons for creating MathRider was  
334 to provide a vehicle for delivering a computer algebra system to as many people  
335 as possible. If you like using a scientific calculator, you should love using a  
336 computer algebra system!

337 At this point you may be asking yourself "if computer algebra systems are so  
338 wonderful, why aren't more people using them?" One reason is that most  
339 computer algebra systems are complex and difficult to learn. Another reason is  
340 that proprietary systems are very expensive and therefore beyond the reach of  
341 most people. Luckily, there are some open source computer algebra systems  
342 that are powerful enough to keep most people engaged for years, and yet simple  
343 enough that even a beginner can start using them. MathPiper (which is based on  
344 a CAS called Yacas) is one of these simpler computer algebra systems and it is  
345 the computer algebra system which is included by default with MathRider.

346 A significant part of this book is devoted to learning MathPiper and a good way  
347 to start is by discussing the difference between numeric and symbolic  
348 computations.

### 349 **5.1 Numeric Vs. Symbolic Computations**

350 A Computer Algebra System (CAS) is software which is capable of performing  
351 both **numeric** and **symbolic** computations. **Numeric** computations are  
352 performed exclusively with numerals and these are the type of computations that  
353 are performed by typical hand-held calculators.

354 **Symbolic** computations (which also called algebraic computations) relate "...to  
355 the use of machines, such as computers, to manipulate mathematical equations  
356 and expressions in symbolic form, as opposed to manipulating the  
357 approximations of specific numerical quantities represented by those symbols."  
358 ([http://en.wikipedia.org/wiki/Symbolic\\_mathematics](http://en.wikipedia.org/wiki/Symbolic_mathematics)).

359 Since most people who read this document will probably be familiar with  
360 performing numeric calculations as done on a scientific calculator, the next  
361 section shows how to use MathPiper as a scientific calculator. The section after  
362 that then shows how to use MathPiper as a symbolic calculator. Both sections  
363 use the console interface to MathPiper. In MathRider, a console interface to any  
364 plugin or application is a text-only **shell** or **command line** interface to it. This  
365 means that you type on the keyboard to send information to the console and it  
366 prints text to send you information.

## 367 **5.2 Using The MathPiper Console As A Numeric (Scientific) Calculator**

368 Open the MathPiper plugin by selecting the **MathPiper** tab in the lower left part  
369 of the MathRider application. The MathPiper **console** interface is a text area  
370 which is inside this plugin. Feel free to increase or decrease the size of the  
371 console text area if you would like by dragging on the dotted lines which are at  
372 the top side and right side of the console window.

373 When the MathPiper console is first launched, it prints a welcome message and  
374 then provides **In>** as an input prompt:

```
375 MathPiper version ".76x".
```

```
376 In>
```

377 Click to the right of the prompt in order to place the cursor there then type **2+2**  
378 followed by **<shift><enter>** (or **<shift><return>** on a Macintosh):

```
379 In> 2+2
```

```
380 Result> 4
```

```
381 In>
```

382 When **<shift><enter>** was pressed, 2+2 was read into MathPiper for  
383 **evaluation** and **Result>** was printed followed by the result **4**. Another input  
384 prompt was then displayed so that further input could be entered. This **input,**  
385 **evaluation, output** process will continue as long as the console is running and  
386 it is sometimes called a **Read, Eval, Print Loop** or **REPL**. In further examples,  
387 the last **In>** prompt will not be shown to save space.

388 In addition to addition, MathPiper can also do subtraction, multiplication,  
389 exponents, and division:

```
390 In> 5-2
```

```
391 Result> 3
```

```
392 In> 3*4
```

```
393 Result> 12
```

```
394 In> 2^3
```

```
395 Result> 8
```

```
396 In> 12/6
```

```
397 Result> 2
```

398 Notice that the multiplication symbol is an asterisk (\*), the exponent symbol is a  
399 caret (^), and the division symbol is a forward slash (/). These symbols (along  
400 with addition (+), subtraction (-), and ones we will talk about later) are called

401 **operators** because they tell MathPiper to perform an operation such as addition  
402 or division.

403 MathPiper can also work with decimal numbers:

```
404 In> .5+1.2  
405 Result> 1.7
```

```
406 In> 3.7-2.6  
407 Result> 1.1
```

```
408 In> 2.2*3.9  
409 Result> 8.58
```

```
410 In> 2.2^3  
411 Result> 10.648
```

```
412 In> 9.5/3.2  
413 Result> 9.5/3.2
```

414 In the last example, MathPiper returned the fraction unevaluated. This  
415 sometimes happens due to MathPiper's symbolic nature, but a result in **numeric**  
416 **form** can be obtained by using the **N()** function:

```
417 In> N(9.5/3.2)  
418 Result> 2.96875
```

419 As can be seen here, when a result is given in numeric form, it means that it is  
420 given as a decimal number. The **N()** function is discussed in the next section.

## 421 5.2.1 Functions

422 **N()** is an example of a **function**. A function can be thought of as a "black box"  
423 which accepts input, processes the input, and returns a result. Each function  
424 has a name and in this case, the name of the function is **N** which stands for  
425 "**numeric**". To the right of a function's name there is always a set of  
426 parentheses and information that is sent to the function is placed inside of them.  
427 The purpose of the **N()** function is to make sure that the information that is sent  
428 to it is processed numerically instead of symbolically.

### 429 5.2.1.1 The Sqrt() Square Root Function

430 The following example show the **N()** function being used with the square root  
431 function **Sqrt()**:

```
432 In> Sqrt(9)  
433 Result: 3
```

```
434 In> Sqrt(8)
435 Result: Sqrt(8)
```

```
436 In> N(Sqrt(8))
437 Result: 2.828427125
```

438 Notice that Sqrt(9) returned 3 as expected but Sqrt(8) returned Sqrt(8). We  
439 needed to use the N() function to force the square root function to return a  
440 numeric result. The reason that Sqrt(8) does not appear to have done anything  
441 is because computer algebra systems like to work with expressions that are as  
442 exact as possible. In this case the **symbolic** value Sqrt(8) represents the number  
443 that is the square root of 8 more accurately than any decimal number can.

444 For example, the following four decimal numbers all represent  $\sqrt{8}$ , but none of  
445 them represent it more accurately than Sqrt(8) does:

```
446     2.828427125
```

```
447     2.82842712474619
```

```
448     2.82842712474619009760337744842
```

```
449     2.8284271247461900976033774484193961571393437507539
```

450 Whenever MathPiper returns a symbolic result and a numeric result is desired,  
451 simply use the N() function to obtain one. The ability to work with symbolic  
452 values are one of the things that make computer algebra systems so powerful  
453 and they are discussed in more depth in later sections.

#### 454 **5.2.1.2 The IsEven() Function**

455 Another often used function is **IsEven()**. The **IsEven()** function takes a number  
456 as input and returns **True** if the number is even and **False** if it is not even:

```
457 In> IsEven(4)
458 Result> True
```

```
459 In> IsEven(5)
460 Result> False
```

461 MathPiper has a large number of functions some of which are described in more  
462 depth in the MathPiper Documentation section and the MathPiper Programming  
463 Fundamentals section. **A complete list of MathPiper's functions is**  
464 **contained in the MathPiperDocs plugin and more of these functions will**  
465 **be discussed soon.**

#### 466 **5.2.2 Accessing Previous Input And Results**

467 The MathPiper console is like a mini text editor which means you can copy text



468 from it, paste text into it, and edit existing text. You can also reevaluate previous  
469 input by simply placing the cursor on the desired **In>** line and pressing  
470 **<shift><enter>** on it again.

471 The console also keeps a history of all input lines that have been evaluated. If  
472 the cursor is placed on any **In>** line, pressing **<ctrl><up arrow>** will display  
473 each previous line of input that has been entered.

474 Finally, MathPiper associates the most recent computation result with the  
475 percent (%) character. If you want to use the most recent result in a new  
476 calculation, access it with this character:

```
477 In> 5*8  
478 Result> 40
```

```
479 In> %  
480 Result> 40
```

```
481 In> %*2  
482 Result> 80
```

### 483 **5.3 Saving And Restoring A Console Session**

484 If you need to save the contents of a console session, you can copy and paste it  
485 into a MathRider buffer and then save the buffer. You can also copy a console  
486 session out of a previously saved buffer and paste it into the console for further  
487 processing. Section 7 **Using MathRider As A Programmer's Text Editor**  
488 discusses how to use the text editor that is built into MathRider.

#### 489 **5.3.1 Syntax Errors**

490 An expression's **syntax** is related to whether it is **typed** correctly or not. If input  
491 is sent to MathPiper which has one or more typing errors in it, MathPiper will  
492 return an error message which is meant to be helpful for locating the error. For  
493 example, if a backwards slash (\) is entered for division instead of a forward slash  
494 (/), MathPiper returns the following error message:

```
495 In> 12 \ 6  
  
496 Error parsing expression, near token \
```

497 The easiest way to fix this problem is to press the **up arrow** key to display the  
498 previously entered line in the console, change the \ to a /, and reevaluate the  
499 expression.

500 This section provided a short introduction to using MathPiper as a numeric  
501 calculator and the next section contains a short introduction to using MathPiper  
502 as a symbolic calculator.

## 503 **5.4 Using The MathPiper Console As A Symbolic Calculator**

504 MathPiper is good at numeric computation, but it is great at symbolic  
505 computation. If you have never used a system that can do symbolic computation,  
506 you are in for a treat!

507 As a first example, lets try adding fractions (which are also called **rational**  
508 **numbers**). Add  $\frac{1}{2} + \frac{1}{3}$  in the MathPiper console:

```
509 In> 1/2 + 1/3  
510 Result> 5/6
```

511 Instead of returning a numeric result like 0.83333333333333333333 (which is  
512 what a scientific calculator would return) MathPiper added these two rational  
513 numbers symbolically and returned  $\frac{5}{6}$ . If you want to work with this result  
514 further, remember that it has also been stored in the % symbol:

```
515 In> %  
516 Result> 5/6
```

517 Lets say that you would like to have MathPiper determine the numerator of this  
518 result. This can be done by using (or **calling**) the **Numerator()** function:

```
519 In> Numerator(%)  
520 Result> 5
```

521 Unfortunately, the % symbol cannot be used to have MathPiper determine the  
522 denominator of  $\frac{5}{6}$  because it only holds the result of the most recent  
523 calculation and  $\frac{5}{6}$  was calculated two steps back.

### 524 **5.4.1 Variables**

525 What would be nice is if MathPiper provided a way to store **results** (which are  
526 also called **values**) in symbols that we choose instead of ones that it chooses.  
527 Fortunately, this is exactly what it does! Symbols that can be associated with  
528 values are called **variables**. Variable names must start with an upper or lower  
529 case letter and be followed by zero or more upper case letters, lower case  
530 letters, or numbers. Examples of variable names include: 'a', 'b', 'x', 'y', 'answer',  
531 'totalAmount', and 'loop6'.

532 The process of associating a value with a variable is called **assigning** or **binding**  
533 the value to the variable and this consists of placing the name of a variable you

would like to create on the left side of an assignment operator (`:=`) and an expression on the right side of this operator. When the expression returns a value, the value is assigned (or bound to) to the variable.

Lets recalculate  $\frac{1}{2} + \frac{1}{3}$  but this time we will assign the result to the variable 'a':

```
In> a := 1/2 + 1/3
Result> 5/6
```

```
In> a
Result> 5/6
```

```
In> Numerator(a)
Result> 5
```

```
In> Denominator(a)
Result> 6
```

In this example, the assignment operator (`:=`) was used to assign the result (or **value**)  $\frac{5}{6}$  to the variable 'a'. **When 'a' was evaluated by itself, the value it was bound to (in this case  $\frac{5}{6}$ ) was returned.** This value will stay bound to the variable 'a' as long as MathPiper is running unless 'a' is cleared with the **Clear()** function or 'a' has another value assigned to it. This is why we were able to determine both the numerator and the denominator of the rational number assigned to 'a' using two functions in turn.

#### 5.4.1.1 Calculating With Unbound Variables

Here is an example which shows another value being assigned to 'a':

```
In> a := 9
Result> 9
```

```
In> a
Result> 9
```

and the following example shows 'a' being cleared (or **unbound**) with the **Clear()** function:

```
In> Clear(a)
Result> True
```

```
In> a
Result> a
```

565 Notice that the `Clear()` function returns **'True'** as a result after it is finished to  
566 indicate that the variable that was sent to it was successfully cleared (or  
567 **unbound**). Many functions either return **'True'** or **'False'** to indicate whether or  
568 not the operation they performed succeeded. Also notice that unbound variables  
569 return themselves when they are evaluated. In this case, 'a' returned 'a'.

570 **Unbound variables** may not appear to be very useful, but they provide the  
571 flexibility needed for computer algebra systems to perform symbolic calculations.  
572 In order to demonstrate this flexibility, let's first factor some numbers using the  
573 **Factor()** function:

```
574 In> Factor(8)
575 Result> 2^3
```

```
576 In> Factor(14)
577 Result> 2*7
```

```
578 In> Factor(2343)
579 Result> 3*11*71
```

580 Now let's factor an expression that contains the unbound variable 'x':

```
581 In> x
582 Result> x
```

```
583 In> IsBound(x)
584 Result> False
```

```
585 In> Factor(x^2 + 24*x + 80)
586 Result> (x+20)*(x+4)
```

```
587 In> Expand(%)
588 Result> x^2+24*x+80
```

589 Evaluating 'x' by itself shows that it does not have a value bound to it and this  
590 can also be determined by passing 'x' to the **IsBound()** function. `IsBound()`  
591 returns **'True'** if a variable is bound to a value and **'False'** if it is not.

592 What is more interesting, however, are the results returned by **Factor()** and  
593 **Expand()**. **Factor()** is able to determine when expressions with unbound  
594 variables are sent to it and it uses the rules of algebra to **manipulate** them into  
595 factored form. The **Expand()** function was then able to take the factored  
596 expression  $(x+20)(x+4)$  and manipulate it until it was expanded. One way to  
597 remember what the functions **Factor()** and **Expand()** do is to look at the second  
598 letters of their names. The 'a' in **Factor** can be thought of as **adding**  
599 parentheses to an expression and the 'x' in **Expand** can be thought of **xing** out  
600 or removing parentheses from an expression.

### 601 **5.4.1.2 Variable And Function Names Are Case Sensitive**

602 MathPiper variables are **case sensitive**. This means that MathPiper takes into  
603 account the **case** of each letter in a variable name when it is deciding if two or  
604 more variable names are the same variable or not. For example, the variable  
605 name **Box** and the variable name **box** are not the same variable because the first  
606 variable name starts with an upper case 'B' and the second variable name starts  
607 with a lower case 'b':

```
608 In> Box := 1
609 Result> 1
```

```
610 In> box := 2
611 Result> 2
```

```
612 In> Box
613 Result> 1
```

```
614 In> box
615 Result> 2
```

### 616 **5.4.1.3 Using More Than One Variable**

617 Programs are able to have more than 1 variable and here is a more sophisticated  
618 example which uses 3 variables:

```
619 a := 2
620 Result> 2
```

```
621 b := 3
622 Result> 3
```

```
623 a + b
624 Result> 5
```

```
625 answer := a + b
626 Result> 5
```

```
627 answer
628 Result> 5
```

629 The part of an expression that is on the **right side** of an assignment operator is  
630 always evaluated first and the result is then assigned to the variable that is on  
631 the **left side** of the operator.

632 Now that you have seen how to use the MathPiper console as both a **symbolic**

633 and a **numeric** calculator, our next step is to take a closer look at the functions  
634 which are included with MathPiper. As you will soon discover, MathPiper  
635 contains an amazing number of functions which deal with a wide range of  
636 mathematics.

## 637 **5.5 Exercises**

638 Use the MathPiper console which is at the bottom of the MathRider application  
639 to complete the following exercises.

### 640 **5.5.1 Exercise 1**

641 Perform the following calculation:

$$\frac{1}{4} + \frac{3}{8} - \frac{7}{16}$$

### 642 **5.5.2 Exercise 2**

643 a) Assign the variable **ans** to the result of the calculation  $\frac{1}{5} + \frac{7}{4} + \frac{15}{16}$  using  
644 the following line of code:

645 In> ans := 1/5 + 7/4 + 15/16

646 b) Use the Numerator() function to calculate the numerator of ans.

647 c) Use the Denominator() function to calculate the denominator of ans.

648 d) Use the N() function to calculate the numeric value of ans.

649 e) Use the Clear() function to unbind the variable ans and verify that ans  
650 is unbound by executing the following code and by using the IsBound()  
651 function:

652 In> ans

### 653 **5.5.3 Exercise 3**

654 Assign  $\frac{1}{4}$  to variable **x**,  $\frac{3}{8}$  to variable **y**, and  $\frac{7}{16}$  to variable **z** using the  
655 := operator. Then perform the following calculations:

656 a)

657 In> x

658 b)

659 In> y

```
660 c)
661 In> z

662 d)
663 In> x + y

664 d)
665 In> x + z

666 e)
667 In> x + y + z
```

## 6 The MathPiper Documentation Plugin

MathPiper has a significant amount of reference documentation written for it and this documentation has been placed into a plugin called **MathPiperDocs** in order to make it easier to navigate. The MathPiperDocs plugin is available in a tab called "MathPiperDocs" which is near the right side of the MathRider application. Click on this tab to open the plugin and click on it again to close it.

The left side of the MathPiperDocs window contains the names of all the functions that come with MathPiper and the right side of the window contains a mini-browser that can be used to navigate the documentation.

### 6.1 Function List

MathPiper's functions are divided into two main categories called **user** functions and **programmer functions**. In general, the **user functions** are used for solving problems in the MathPiper console or with short programs and the **programmer functions** are used for longer programs. However, users will often use some of the programmer functions and programmers will use the user functions as needed.

Both the user and programmer function names have been placed into a "tree" on the left side of the MathPiperDocs window to allow for easy navigation. The branches of the function tree can be opened and closed by clicking on the small "circle with a line attached to it" symbol which is to the left of each branch. Both the user and programmer branches have the functions they contain organized into categories and the **top category in each branch** lists all the functions in the branch in **alphabetical order** for quick access. Clicking on a function will bring up documentation about it in the browser window and selecting the **Collapse** button at the top of the plugin will collapse the tree.

**Don't be intimidated by the large number of categories and functions that are in the function tree!** Most MathRider beginners will not know what most of them mean, and some will not know what any of them mean. Part of the benefit MathRider provides is exposing the user to the existence of these categories and functions. The more you use MathRider, the more you will learn about these categories and functions and someday you may even get to the point where you understand all of them. This book is designed to show newbies how to begin using these functions using a gentle step-by-step approach.

### 6.2 Mini Web Browser Interface

MathPiper's reference documentation is in HTML (or web page) format and so the right side of the plugin contains a mini web browser that can be used to navigate through these pages. The browser's **home page** contains links to the main parts of the MathPiper documentation. As links are selected, the **Back** and



706 **Forward** buttons in the upper right corner of the plugin allow the user to move  
707 backward and forward through previously visited pages and the **Home** button  
708 navigates back to the home page.

709 The function names in the function tree all point to sections in the HTML  
710 documentation so the user can access function information either by navigating  
711 to it with the browser or jumping directly to it with the function tree.

## 712 **6.3 Exercises**

### 713 **6.3.1 Exercise 1**

714 Locate the `N()`, `IsEven()`, `IsOdd()`, `Clear()`, `IsBound()`, `Numerator()`,  
715 `Denominator()`, and `Factor()` functions in the **All Functions** section of the  
716 MathPiperDocs plugin and read the information that is available on them.

### 717 **6.3.2 Exercise 2**

718 Locate the `N()`, `IsEven()`, `IsOdd()`, `Clear()`, `IsBound()`, `Numerator()`,  
719 `Denominator()`, and `Factor()` functions in the **User Functions** section of the  
720 MathPiperDocs plugin and list which section each function is contained in.  
721 Don't include the **Alphabetical** or **Built In** subsections in your search.

## 722 **7 Using MathRider As A Programmer's Text Editor**

723 We have covered some of MathRider's mathematics capabilities and this section  
724 discusses some of its programming capabilities. As indicated in a previous  
725 section, MathRider is built on top of a programmer's text editor but what wasn't  
726 discussed was what an amazing and powerful tool a programmer's text editor is.

727 Computer programmers are among the most intelligent and productive people in  
728 the world and most of their work is done using a programmer's text editor (or  
729 something similar to one). Programmers have designed programmer's text  
730 editors to be super-tools which can help them maximize their personal  
731 productivity and these tools have all kinds of capabilities that most people would  
732 not even suspect they contained.

733 Even though this book only covers a small part of the editing capabilities that  
734 MathRider has, what is covered will enable the user to begin writing useful  
735 programs.

### 736 **7.1 Creating, Opening, Saving, And Closing Text Files**

737 A good way to begin learning how to use MathRider's text editing capabilities is  
738 by creating, opening, and saving text files. A text file can be created either by  
739 selecting **File->New** from the menu bar or by selecting the icon for this  
740 operation on the tool bar. When a new file is created, an empty text area is  
741 created for it along with a new tab named **Untitled**.

742 The file can be saved by selecting **File->Save** from the menu bar or by selecting  
743 the **Save** icon in the tool bar. The first time a file is saved, MathRider will ask  
744 the user what it should be named and it will also provide a file system navigation  
745 window to determine where it should be placed. After the file has been named  
746 and saved, its name will be shown in the tab that previously displayed **Untitled**.

747 A file can be closed by selecting **File->Close** from the menu bar and it can be  
748 opened by selecting **File->Open**.

### 749 **7.2 Editing Files**

750 If you know how to use a word processor, then it should be fairly easy for you to  
751 learn how to use MathRider as a text editor. Text can be selected by dragging  
752 the mouse pointer across it and it can be cut or copied by using actions in the  
753 **Edit** menu (or by using **<Ctrl>x** and **<Ctrl>c**). Pasting text can be done using  
754 the Edit menu actions or by pressing **<Ctrl>v**.

### 755 **7.3 File Modes**

756 Text file names are suppose to have a file extension which indicates what type of

757 file it is. For example, test.**txt** is a generic text file, test.**bat** is a Windows batch  
758 file, and test.**sh** is a Unix/Linux shell script (**unfortunately, Windows is usually**  
759 **configured to hide file extensions, but viewing a file's properties by right-clicking**  
760 **on it will show this information.**).

761 MathRider uses a file's extension type to set its text area into a customized  
762 **mode** which highlights various parts of its contents. For example, MathRider  
763 worksheet files have a **.mrw** extension and MathRider knows what colors to  
764 highlight the various parts of a .mrw file in.

## 765 ***7.4 Learning How To Type Properly Is An Excellent Investment Of Your*** 766 ***Time***

767 This is a good place in the document to mention that learning how to type  
768 properly is an investment that will pay back dividends throughout your whole  
769 life. Almost any work you do on a computer (including programming) will be  
770 done *much* faster and with less errors if you know how to type properly. Here is  
771 what Steve Yegge has to say about this subject:

772 "If you are a programmer, or an IT professional working with computers in *any*  
773 capacity, **you need to learn to type!** I don't know how to put it any more clearly  
774 than that."

775 A good way to learn how to program is to locate a free "learn how to type"  
776 program on the web and use it.

## 777 ***7.5 Exercises***

### 778 ***7.5.1 Exercise 1***

779 Create a text file called "**my\_text\_file.txt**" and place a few sentences in  
780 it. Save the text file somewhere on your hard drive then close it. Now,  
781 open the text file again using **File->Open** and verify that what you typed is  
782 still in the file.

## 783 8 MathRider Worksheet Files

784 While MathRider's ability to execute code inside a console provides a significant  
785 amount of power to the user, most of MathRider's power is derived from  
786 **worksheets**. MathRider worksheets are text files which have a **.mrw** extension  
787 and are able to execute multiple types of code in a single text area. The  
788 **worksheet\_demo\_1.mrw** file (which is preloaded in the MathRider environment  
789 when it is first launched) demonstrates how a worksheet is able to execute  
790 multiple types of code in what are called **code folds**.

### 791 8.1 Code Folds

792 Code folds are named sections inside a MathRider worksheet which contain  
793 source code that can be executed by placing the cursor inside of it and pressing  
794 **<shift><Enter>**. A fold always begins with a **start tag**, which starts with a  
795 percent symbol (%) followed by the **name of the fold type** (like this:  
796 **%<foldtype>**). The end of a fold is marked by an **end tag** which looks like  
797 **%/<foldtype>**. The only difference between a fold's start tag and its end tag is  
798 that the end tag has a slash (/) after the %.

799 For example, here is a MathPiper fold which will print the result of **2 + 3** to the  
800 MathPiper console (**Note: the semicolon ';' which is at the end of the line of**  
801 **code is required**):

```
802 %mathpiper  
803 2 + 3;  
804 %/mathpiper
```

805 The **output** generated by a fold (called the **parent fold**) is wrapped in a **new**  
806 **fold** (called a **child fold**) which is indented and placed just below the parent.  
807 This can be seen when the above fold is executed by pressing **<shift><enter>**  
808 inside of it:

```
809 %mathpiper  
810 2 + 3;  
811 %/mathpiper  
812     %output,preserve="false"  
813     Result: 5  
814 .    %/output
```

815 The most common type of output fold is **%output** and by default folds of type

816 %output have their **preserve property** set to **false**. This tells MathRider to  
817 overwrite the %output fold with a new version during the next execution of its  
818 parent. If preserve is set to **true**, the fold will not be overwritten and a new fold  
819 will be created instead.

820 There are other kinds of child folds, but in the rest of this document they will all  
821 be referred to in general as "output" folds.

## 822 8.1.1 The Description Attribute

823 Folds can also have what is called a "**description attribute**" placed after the  
824 start tag which describes what the fold contains. For example, the following  
825 %mathpiper fold has a description attribute which indicates that the fold adds  
826 two number together:

```
827 %mathpiper,title="Add two numbers together."
```

```
828 2 + 3;
```

```
829 %/mathpiper
```

830 The description attribute is added to the start tag of a fold by placing a comma  
831 after the fold's type name and then adding the text **title="<text>"** after the  
832 comma. (**Note: no spaces can be present before or after the comma (,) or**  
833 **the equals sign (=)** ).

## 834 8.2 Automatically Inserting Folds & Removing Unpreserved Folds

835 Typing the the top and bottom fold lines (for example:

```
836 %mathpiper
```

```
837 %/mathpiper
```

838 can be tedious and MathRider has a way to automatically insert them. Place the  
839 cursor at the beginning of a blank line in a .mrw worksheet file where you would  
840 like a fold inserted and then **press the right mouse button**.

841 A popup menu will be displayed and at the top of this menu are items which read  
842 "**Insert MathPiper Fold**", "**Insert Group Fold**", etc. If you select one of these  
843 menu items, an empty code fold of the proper type will automatically be inserted  
844 into the .mrw file at the position of the cursor.

845 This popup menu also has a menu item called "**Remove Unpreserved Folds**". If  
846 this menu item is selected, all folds which have a "**preserve="false"**" property  
847 will be removed.

## 848 **8.3 Exercises**

849 A MathRider worksheet file called "**newbies\_book\_examples\_1.mrw**" can be  
850 obtained from this website:

851 [https://mathrider.dev.java.net/source/browse/mathrider/trunk/src/doc/newbies\\_bo](https://mathrider.dev.java.net/source/browse/mathrider/trunk/src/doc/newbies_book/examples/proposed/misc/newbies_book_examples_1.mrw)  
852 [ok/examples/proposed/misc/newbies\\_book\\_examples\\_1.mrw](https://mathrider.dev.java.net/source/browse/mathrider/trunk/src/doc/newbies_book/examples/proposed/misc/newbies_book_examples_1.mrw)

853 It contains a number of %mathpiper folds which contain code examples from the  
854 previous sections of this book. Notice that all of the lines of code have a  
855 semicolon (;) placed after them. The reason this is needed is explained in a later  
856 section.

857 Download this worksheet file to your computer from the section on this website  
858 that contains the highest revision number and then open it in MathRider. Then,  
859 use the worksheet to do the following exercises.

### 860 **8.3.1 Exercise 1**

861 Execute folds 1-8 in the top section of the worksheet by placing the cursor  
862 inside of the fold and then pressing <shift><enter> on the keyboard.

### 863 **8.3.2 Exercise 2**

864 The code in folds 9 and 10 have errors in them. Fix the errors and then  
865 execute the folds again.

### 866 **8.3.3 Exercise 3**

867 Use the empty fold 11 to calculate the expression  $100 - 23$ ;

### 868 **8.3.4 Exercise 4**

869 Perform the following calculations by creating new folds at the bottom of  
870 the worksheet (using the right-click popup menu) and placing each  
871 calculation into its own fold:

872 a)  $2 * 7 + 3$

873 b)  $18 / 3$

874 c)  $234238342 + 2038408203$

875 d)  $324802984 * 2308098234$

876 e) Factor the result which was calculated in d).

## 877 9 MathPiper Programming Fundamentals

878 The MathPiper language consists of **expressions** and an expression consists of  
879 one or more **symbols** which represent **values**, **operators**, **variables**, and  
880 **functions**. In this section expressions are explained along with the values,  
881 operators, variables, and functions they consist of.

### 882 9.1 Values and Expressions

883 A **value** is a single symbol or a group of symbols which represent an idea. For  
884 example, the value:

885 3

886 represents the number three, the value:

887 0.5

888 represents the number one half, and the value:

889 "Mathematics is powerful!"

890 represents an English sentence.

891 Expressions can be created by using **values** and **operators** as building blocks.  
892 The following are examples of simple expressions which have been created this  
893 way:

894 3

895 2 + 3

896 5 + 6\*21/18 - 2^3

897 In MathPiper, **expressions** can be **evaluated** which means that they can be  
898 transformed into a **result value** by predefined rules. For example, when the  
899 expression 2 + 3 is evaluated, the result value that is produced is 5:

900 In> 2 + 3

901 Result> 5

### 902 9.2 Operators

903 In the above expressions, the characters +, -, \*, /, ^ are called **operators** and  
904 their purpose is to tell MathPiper what **operations** to perform on the **values** in  
905 an **expression**. For example, in the expression 2 + 3, the **addition** operator +  
906 tells MathPiper to add the integer 2 to the integer 3 and return the result.

907 The **subtraction** operator is -, the **multiplication** operator is \*, / is the  
908 **division** operator, % is the **remainder** operator (which is also used as the

909 "result of the last calculation" symbol), and ^ is the **exponent** operator.  
910 MathPiper has more operators in addition to these and some of them will be  
911 covered later.

912 The following examples show the -, \*, /, %, and ^ operators being used:

913 In> 5 - 2  
914 Result> 3

915 In> 3\*4  
916 Result> 12

917 In> 30/3  
918 Result> 10

919 In> 8%5  
920 Result> 3

921 In> 2^3  
922 Result> 8

923 The - character can also be used to indicate a negative number:

924 In> -3  
925 Result> -3

926 Subtracting a negative number results in a positive number (Note: there must be  
927 a space between the two negative signs):

928 In> - -3  
929 Result> 3

930 In MathPiper, **operators** are symbols (or groups of symbols) which are  
931 implemented with **functions**. One can either call the function that an operator  
932 represents directly or use the operator to call the function indirectly. However,  
933 using operators requires less typing and they often make a program easier to  
934 read.

### 935 **9.3 Operator Precedence**

936 When expressions contain more than one operator, MathPiper uses a set of rules  
937 called **operator precedence** to determine the order in which the operators are  
938 applied to the values in the expression. Operator precedence is also referred to  
939 as the **order of operations**. Operators with higher precedence are evaluated  
940 before operators with lower precedence. The following table shows a subset of  
941 MathPiper's operator precedence rules with higher precedence operators being  
942 placed higher in the table:



943     <sup>^</sup>     Exponents are evaluated right to left.  
 944     \*,%,/ Then multiplication, remainder, and division operations are evaluated  
 945     left to right.  
 946     +, - Finally, addition and subtraction are evaluated left to right.

947   Lets manually apply these precedence rules to the multi-operator expression we  
 948   used earlier. Here is the expression in source code form:

949                                 5 + 6\*21/18 - 2^3

950   And here it is in traditional form:

$$5 + 6 * \frac{21}{18} - 2^3$$

951   According to the precedence rules, this is the order in which MathPiper  
 952   evaluates the operations in this expression:

953   5 + 6\*21/18 - 2^3  
 954   5 + 6\*21/18 - 8  
 955   5 + 126/18 - 8  
 956   5 + 7 - 8  
 957   12 - 8  
 958   4

959   Starting with the first expression, MathPiper evaluates the <sup>^</sup> operator first which  
 960   results in the 8 in the expression below it. In the second expression, the \*  
 961   operator is executed next, and so on. The last expression shows that the final  
 962   result after all of the operators have been evaluated is 4.

#### 963   **9.4 Changing The Order Of Operations In An Expression**

964   The default order of operations for an expression can be changed by grouping  
 965   various parts of the expression within parentheses (). Parentheses force the  
 966   code that is placed inside of them to be evaluated before any other operators are  
 967   evaluated. For example, the expression 2 + 4\*5 evaluates to 22 using the  
 968   default precedence rules:

969   In> 2 + 4\*5  
 970   Result> 22

971   If parentheses are placed around 4 + 5, however, the addition operator is forced  
 972   to be evaluated before the multiplication operator and the result is 30:

```
973 In> (2 + 4)*5
974 Result> 30
```

975 Parentheses can also be nested and nested parentheses are evaluated from the  
976 most deeply nested parentheses outward:

```
977 In> ((2 + 4)*3)*5
978 Result> 90
```

979 (Note: precedence adjusting parentheses are different from the parentheses that  
980 are used to call functions.)

981 Since parentheses are evaluated before any other operators, they are placed at  
982 the top of the precedence table:

- 983     ()     Parentheses are evaluated from the inside out.
- 984     ^     Then exponents are evaluated right to left.
- 985     \*,%/,   Then multiplication, remainder, and division operations are evaluated  
986             left to right.
- 987     +, -   Finally, addition and subtraction are evaluated left to right.

## 988 9.5 Functions & Function Names

989 In programming, **functions** are named blocks of code that can be executed one  
990 or more times by being **called** from other parts of the same program or called  
991 from other programs. Functions **can have values passed to them** from the  
992 calling code and they **always return a value** back to the calling code when they  
993 are finished executing. An example of a function is the **IsEven()** function which  
994 was discussed in an previous section.

995 Functions are one way that MathPiper enables code to be reused. Most  
996 programming languages allow code to be reused in this way, although in other  
997 languages these named blocks of code are sometimes called **subroutines**,  
998 **procedures**, or **methods**.

999 The functions that come with MathPiper have names which consist of either a  
1000 single word (such as **Sum()**) or multiple words that have been put together to  
1001 form a compound word (such as **IsBound()**). All letters in the names of  
1002 functions which come with MathPiper are lower case except the beginning letter  
1003 in each word, which are upper case.

## 1004 **9.6 Functions That Produce Side Effects**

1005 Most functions are executed to obtain the **results** they produce but some  
1006 functions are executed in order to **have them perform work that is not in the**  
1007 **form of a result**. Functions that perform work that is not in the form of a result  
1008 are said to produce **side effects**. Side effects include many forms of work such  
1009 as sending information to the user, opening files, and changing values in the  
1010 computer's memory.

1011 When a function produces a side effect which sends information to the user, this  
1012 information has the words **Side Effects:** placed before it in the output instead of  
1013 the word **Result:**. The **Echo()** and **Write()** functions are examples of functions  
1014 that produce side effects and they are covered in the next section.

### 1015 **9.6.1 Printing Related Functions: Echo(), Write(), And Newline()**

1016 The printing related functions send text information to the user and this is  
1017 usually referred to as "printing" in this document. However, it may also be called  
1018 "echoing" and "writing".

#### 1019 **9.6.1.1 Echo()**

1020 The **Echo()** function takes one expression (or multiple expressions separated by  
1021 commas) evaluates each expression, and then prints the results as side effect  
1022 output. The following examples illustrate this:

```
1023 In> Echo(1)
1024 Result> True
1025 Side Effects>
1026 1
```

1027 In this example, the number 1 was passed to the Echo() function, the number  
1028 was evaluated (all numbers evaluate to themselves), and the result of the  
1029 evaluation was then printed as a side effect. Notice that Echo() **also returned a**  
1030 **result**. In MathPiper, all functions return a result, but functions whose main  
1031 purpose is to produce a side effect usually just return a result of **True** if the side  
1032 effect succeeded or **False** if it failed. In this case, Echo() returned a result of  
1033 **True** because it was able to successfully print a 1 as its side effect.

1034 The next example shows multiple expressions being sent to Echo() (notice that  
1035 the expressions are separated by commas):

```
1036 In> Echo(1,1+2,2*3)
1037 Result> True
1038 Side Effects>
1039 1 3 6
```

1040 The expressions were each evaluated and their results were returned (separated  
1041 by spaces) as side effect output. If it is desired that commas be printed between  
1042 the numbers in the output, simply place three commas between the expressions  
1043 that are passed to Echo():

```
1044 In> Echo(1,,,1+2,,,2*3)
1045 Result> True
1046 Side Effects>
1047 1 , 3 , 6
```

1048 Each time an Echo() function is executed, it always forces the display to drop  
1049 down to the next line after it is finished. This can be seen in the following  
1050 program which is similar to the previous one except it uses a separate Echo()  
1051 function to display each expression:

```
1052 %mathpiper
1053 Echo(1);
1054 Echo(1+2);
1055 Echo(2*3);
1056 %/mathpiper
1057 %output,preserve="false"
1058 Result: True
1059
1060 Side Effects:
1061 1
1062 3
1063 6
1064 . %/output
```

1065 Notice how the 1, the 3, and the 6 are each on their own line.

1066 Now that we have seen how Echo() works, lets use it to do something useful. If  
1067 more than one expression is evaluated in a %mathpiper fold, only the result from  
1068 the last expression that was evaluated (which is usually the bottommost  
1069 expression) is displayed:

```
1070 %mathpiper
1071 a := 1;
1072 b := 2;
1073 c := 3;
1074 %/mathpiper
```

```
1075 %output,preserve="false"
1076     Result: 3
1077 .    %/output
```

1078 In MathPiper, programs are executed one line at a time, starting at the topmost  
1079 line of code and working downwards from there. In this example, the line `a := 1;`  
1080 is executed first, then the line `b := 2;` is executed, and so on. Notice, however,  
1081 that even though we wanted to see what was in all three variables, only the  
1082 content of the last variable was displayed.

1083 The following example shows how `Echo()` can be used to display the contents of  
1084 all three variables:

```
1085 %mathpiper
1086 a := 1;
1087 Echo(a);
1088 b := 2;
1089 Echo(b);
1090 c := 3;
1091 Echo(c);
1092 %/mathpiper
1093 %output,preserve="false"
1094     Result: True
1095
1096     Side Effects:
1097     1
1098     2
1099     3
1100 .    %/output
```

### 1101 9.6.1.2 Echo Statements Are Useful For "Debugging" Programs

1102 The errors that are in a program are often called "bugs". This name came from  
1103 the days when computers were the size of large rooms and were made using  
1104 electromechanical parts. Periodically, bugs would crawl into the machines and  
1105 interfere with its moving mechanical parts and this would cause the machine to  
1106 malfunction. The bugs needed to be located and removed before the machine  
1107 would run properly again.

1108 Of course, even back then most program errors were produced by programmers  
1109 entering wrong programs or entering programs wrong, but they liked to say that  
1110 all of the errors were caused by bugs and not by themselves! The process of  
1111 fixing errors in a program became known as **debugging** and the names "bugs"

1112 and "debugging" are still used by programmers today.

1113 One of the standard ways to locate bugs in a program is to place **Echo()** function  
1114 calls in the code at strategic places which **print the contents of variables and**  
1115 **display messages**. These Echo() functions will enable you to see what your  
1116 program is doing while it is running. After you have found and fixed the bugs in  
1117 your program, you can remove the debugging Echo() function calls or comment  
1118 them out if you think they may be needed later.

### 1119 **9.6.1.3 Write()**

1120 The **Write()** function is similar to the Echo() function except it does not  
1121 automatically drop the display down to the next line after it finishes executing:

```
1122 %mathpiper
1123 Write(1);
1124 Write(1+2);
1125 Echo(2*3);
1126 %/mathpiper
1127     %output,preserve="false"
1128     Result: True
1129
1130     Side Effects:
1131     1 3 6
1132 .    %/output
```

1133 Write() and Echo() have other differences besides the one discussed here and  
1134 more information about them can be found in the documentation for these  
1135 functions.

### 1136 **9.6.1.4 NewLine()**

1137 The **NewLine()** function simply prints a blank line in the side effects output. It  
1138 is useful for placing vertical space between printed lines:

```
1139 %mathpiper
1140 a := 1;
1141 Echo(a);
1142 NewLine();
1143 b := 2;
1144 Echo(b);
```

```
1145 NewLine();
1146 c := 3;
1147 Echo(c);

1148 %/mathpiper

1149 %output,preserve="false"
1150 Result: True
1151
1152 Side Effects:
1153 1
1154 2
1155 3
1156 . %/output
```

## 1157 9.7 Expressions Are Separated By Semicolons

1158 As discussed earlier, all of the expressions that are inside of a **%mathpiper** fold  
1159 must have a semicolon (;) after them. However, the expressions executed in the  
1160 **MathPiper console** did not have a semicolon after them. MathPiper actually  
1161 requires that all expressions end with a semicolon, but one does not need to add  
1162 a semicolon to an expression which is typed into the MathPiper console **because**  
1163 **the console adds it automatically** when the expression is executed.

### 1164 9.7.1 Placing More Than One Expression On A Line In A Fold

1165 All the previous code examples have had each of their expressions on a separate  
1166 line, but multiple expressions can also be placed on a single line because the  
1167 semicolons tell MathPiper where one expression ends and the next one begins:

```
1168 %mathpiper

1169 a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c);

1170 %/mathpiper

1171 %output,preserve="false"
1172 Result: True
1173
1174 Side Effects:
1175 1
1176 2
1177 3
1178 . %/output
```

1179 The spaces that are in the code of this example are used to make the code more  
1180 readable. Any spaces that are present within any expressions or between them  
1181 are ignored by MathPiper and if we remove the spaces from the previous code,  
1182 the output remains the same:

```
1183 %mathpiper
1184 a:=1;Echo(a);b:=2;Echo(b);c:= 3;Echo(c);
1185 %/mathpiper
1186     %output,preserve="false"
1187     Result: True
1188
1189     Side Effects:
1190     1
1191     2
1192     3
1193 .    %/output
```

## 1194 9.7.2 Placing More Than One Expression On A Line In The Console Using 1195 A Code Block

1196 The MathPiper console is only able to execute one expression at a time so if the  
1197 previous code that executes three variable assignments and three Echo()  
1198 functions on a single line is evaluated in the console, only the expression **a := 1**  
1199 is executed:

```
1200 In> a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c);
1201 Result> 1
```

1202 Fortunately, this limitation can be overcome by placing the code into a **code**  
1203 **block**. A **code block** (which is also called a **compound expression**) consists of  
1204 one or more expressions which are separated by semicolons and placed within an  
1205 open bracket ([) and close bracket (]) pair. If a code block is evaluated in the  
1206 MathPiper console, each expression in the block will be executed from left to  
1207 right. The following example shows the previous code being executed within of a  
1208 code block inside the MathPiper console:

```
1209 In> [a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c);]
1210 Result> True
1211 Side Effects>
1212 1
1213 2
1214 3
```

1215 Notice that this time all of the expressions were executed and 1-3 was printed as



1216 a side effect. Code blocks always return the result of the last expression  
1217 executed as the result of the whole block. In this case, True was returned as the  
1218 result because the last Echo(c) function returned True. If we place another  
1219 expression after the Echo(c) function, however, the block will execute this new  
1220 expression last and its result will be the one returned by the block:

```
1221 In> [a := 1; Echo(a); b := 2; Echo(b); c := 3; Echo(c); 2 + 2]
1222 Result> 4
1223 Side Effects>
1224 1
1225 2
1226 3
```

1227 Finally, code blocks can have their contents placed on separate lines if desired:

```
1228 %mathpiper
1229 [
1230     a := 1;
1231
1232     Echo(a);
1233
1234     b := 2;
1235
1236     Echo(b);
1237
1238     c := 3;
1239
1240     Echo(c);
1241 ];
1242 %/mathpiper
1243
1244     %output,preserve="false"
1245     Result: True
1246
1247     Side Effects:
1248     1
1249     2
1250     3
1251 . %/output
```

1251 Code blocks are very powerful and we will be discussing them further in later  
1252 sections.

### 1253 9.7.2.1 Automatic Bracket, Parentheses, And Brace Match Indicating

1254 In programming, most open brackets '[' have a close bracket ']', most open  
1255 parentheses '(' have a close parentheses ')', and most open braces '{' have a  
1256 close brace '}'. It is often difficult to make sure that each "open" character has a

1257 matching "close" character and if any of these characters don't have a match,  
1258 then an error will be produced.

1259 Thankfully, most programming text editors have a character match indicating  
1260 tool that will help locate problems. To try this tool, paste the following code into  
1261 a .mrw file and following the directions that are present in its comments:

```
1262 %mathpiper
1263 /*
1264     Copy this code into a .mrw file. Then, place the cursor
1265     to the immediate right of any {, }, [, ], (, or ) character.
1266     You should notice that the match to this character is
1267     indicated by a rectangle being drawing around it.
1268 */
```

```
1269 list := {1,2,3};
1270 [
1271     Echo("Hello");
1272     Echo(list);
1273 ];
```

```
1274 %/mathpiper
```

## 1275 9.8 Strings

1276 A **string** is a **value** that is used to hold text-based information. The typical  
1277 expression that is used to create a string consists of **text which is enclosed**  
1278 **within double quotes**. Strings can be assigned to variables just like numbers  
1279 can and strings can also be displayed using the Echo() function. The following  
1280 program assigns a string value to the variable 'a' and then echos it to the user:

```
1281 %mathpiper
1282 a := "Hello, I am a string.";
1283 Echo(a);
1284 %/mathpiper
1285 %output,preserve="false"
1286 Result: True
1287
1288 Side Effects:
1289 Hello, I am a string.
1290 . %/output
```

## 1291 9.8.1 The MathPiper Console and MathPiper Folds Can Access The Same 1292 Variables

1293 A useful aspect of using MathPiper inside of MathRider is that variables that are  
1294 assigned inside of a **%mathpiper fold** are accessible inside of the **MathPiper**  
1295 **console** and variables that are assigned inside of the **MathPiper console** are  
1296 available inside of **%mathpiper folds**. For example, after the above fold is  
1297 executed, the string that has been bound to variable 'a' can be displayed in the  
1298 MathPiper console:

```
1299 In> a  
1300 Result> "Hello, I am a string."
```

## 1301 9.8.2 Using Strings To Make Echo's Output Easier To Read

1302 When the Echo() function is used to print the values of multiple variables, it is  
1303 often helpful to print some information next to each variable so that it is easier to  
1304 determine which value came from which Echo() function in the code. The  
1305 following program prints the name of the variable that each value came from  
1306 next to it in the side effects output:

```
1307 %mathpiper  
1308 a := 1;  
1309 Echo("Variable a: ", a);  
  
1310 b := 2;  
1311 Echo("Variable b: ", b);  
  
1312 c := 3;  
1313 Echo("Variable c: ", c);  
  
1314 %/mathpiper  
  
1315 %output,preserve="false"  
1316 Result: True  
1317  
1318 Side Effects:  
1319 Variable a: 1  
1320 Variable b: 2  
1321 Variable c: 3  
1322 . %/output
```

### 1323 9.8.2.1 Combining Strings With The : Operator

1324 If you need to combine two or more strings into one string, you can use the :  
1325 operator like this:

```
1326 In> "A" : "B" : "C"
1327 Result: "ABC"
```

```
1328 In> "Hello " : "there!"
1329 Result: "Hello there!"
```

### 1330 **9.8.2.2 WriteString()**

1331 The **WriteString()** function prints a string without shows the double quotes that  
1332 are around it.. For example, here is the Write() function being used to print the  
1333 string "Hello":

```
1334 In> Write("Hello")
1335 Result: True
1336 Side Effects:
1337 "Hello"
```

1338 Notice the double quotes? Here is how the WriteString() function prints "Hello":

```
1339 In> WriteString("Hello")
1340 Result: True
1341 Side Effects:
1342 Hello
```

### 1343 **9.8.2.3 NI()**

1344 The **NI()** (New Line) function is used with the : function to place newline  
1345 characters inside of strings:

```
1346 In> WriteString("A": NI() : "B")
1347 Result: True
1348 Side Effects:
1349 A
1350 B
```

### 1351 **9.8.2.4 Space()**

1352 The Space() function is used to add spaces to printed output:

```
1353 In> WriteString("A"); Space(10); WriteString("B")
1354 Result: True
1355 Side Effects:
1356 A          B
```

## 1357 **9.8.3 Accessing The Individual Letters In A String**

1358 Individual letters in a string (which are also called **characters**) can be accessed

1359 by placing the character's position number (also called an **index**) inside of  
1360 brackets **[]** after the variable it is bound to. A character's position is determined  
1361 by its distance from the left side of the string starting at 1. For example, in the  
1362 string "Hello", 'H' is at position 1, 'e' is at position 2, etc. The following code  
1363 shows individual characters in the above string being accessed:

```
1364 In> a := "Hello, I am a string."  
1365 Result> "Hello, I am a string."
```

```
1366 In> a[1]  
1367 Result> "H"
```

```
1368 In> a[2]  
1369 Result> "e"
```

```
1370 In> a[3]  
1371 Result> "l"
```

```
1372 In> a[4]  
1373 Result> "l"
```

```
1374 In> a[5]  
1375 Result> "o"
```

## 1376 9.9 Comments

1377 Source code can often be difficult to understand and therefore all programming  
1378 languages provide the ability for **comments** to be included in the code.  
1379 Comments are used to explain what the code near them is doing and they are  
1380 usually meant to be read by humans instead of being processed by a computer.  
1381 Therefore, comments are ignored by the computer when a program is executed.

1382 There are two ways that MathPiper allows comments to be added to source code.  
1383 The first way is by placing two forward slashes **//** to the left of any text that is  
1384 meant to serve as a comment. The text from the slashes to the end of the line  
1385 the slashes are on will be treated as a comment. Here is a program that contains  
1386 comments which use slashes:

```
1387 %mathpiper  
1388 //This is a comment.
```

```
1389 x := 2; //Set the variable x equal to 2.
```

```
1390 %/mathpiper
```

```
1391     %output,preserve="false"  
1392     Result: 2
```

```
1393 .    %/output
```

1394 When this program is executed, any text that starts with slashes is ignored.

1395 The second way to add comments to a MathPiper program is by enclosing the  
1396 comments inside of slash-asterisk/asterisk-slash symbols `/* */`. This option is  
1397 useful when a comment is too large to fit on one line. Any text between these  
1398 symbols is ignored by the computer. This program shows a longer comment  
1399 which has been placed between these symbols:

```
1400 %mathpiper
```

```
1401 /*  
1402  This is a longer comment and it uses  
1403  more than one line. The following  
1404  code assigns the number 3 to variable  
1405  x and then returns it as a result.  
1406 */
```

```
1407 x := 3;
```

```
1408 %/mathpiper
```

```
1409     %output,preserve="false"  
1410     Result: 3  
1411 .    %/output
```

## 1412 **9.10 Exercises**

1413 For the following exercises, create a new MathRider worksheet file called  
1414 **section\_9\_exercises\_<your first name>\_<your last name>.mrw**. (**Note:**  
1415 **there are no spaces in this file name**). For example, John Smith's worksheet  
1416 would be called:

1417 **section\_9\_exercises\_john\_smith.mrw**.

1418 After this worksheet has been created, place your answer for each exercise into  
1419 its own fold in this worksheet. Place a description attribute in the start tag of  
1420 each fold which indicates the exercise the fold contains the solution to. The folds  
1421 you create should look similar to this one:

```
1422 %mathpiper,title="Exercise 1"
```

```
1423 //Sample fold.
```

```
1424 %/mathpiper
```

**1425 9.10.1 Exercise 1**

1426 Change the precedence of the following expression using parentheses so that  
1427 it prints 20 instead of 14:

1428 `2 + 3 * 4`

**1429 9.10.2 Exercise 2**

1430 Place the following calculations into a fold and then use one Echo()  
1431 function per variable to print the results of the calculations. Put  
1432 strings in the Echo() functions which indicate which variable each  
1433 calculated value is bound to:

1434 `a := 1+2+3+4+5;`  
1435 `b := 1-2-3-4-5;`  
1436 `c := 1*2*3*4*5;`  
1437 `d := 1/2/3/4/5;`

**1438 9.10.3 Exercise 3**

1439 Place the following calculations into a fold and then use one Echo()  
1440 function to print the results of all the calculations on a single line  
1441 (Remember, the Echo() function can print multiple values if they are  
1442 separated by commas.):

1443 `Clear(x);`  
1444 `a := 2*2*2*2*2;`  
1445 `b := 2^5;`  
1446 `c := x^2 * x^3;`  
1447 `d := 2^2 * 2^3;`

**1448 9.10.4 Exercise 4**

1449 The following code assigns a string which contains all of the upper case  
1450 letters of the alphabet to the variable **upper**. Each of the three Echo()  
1451 functions prints an index number and the letter that is at that position in  
1452 the string. Place this code into a fold and then continue the Echo()  
1453 functions so that all 26 letters and their index numbers are printed

1454 `upper := "ABCDEFGHIJKLMNOPQRSTUVWXYZ";`

1455 `Echo(1,upper[1]);`  
1456 `Echo(2,upper[2]);`  
1457 `Echo(3,upper[3]);`

**1458 9.10.5 Exercise 5**

1459 Use Echo() functions to print an index number and the character at this  
1460 position for the following string (this is similar to what was done in  
1461 Exercise 4.):

```
1462 extra := "!.@#$%^&*() _+<>,?/{ }[]|\-=";
```

```
1463 Echo(1,extra[1]);
```

```
1464 Echo(2,extra[2]);
```

```
1465 Echo(3,extra[3]);
```

## 1466 9.10.6 Exercise 6

1467 The following program uses strings and index numbers to print a person's  
1468 name. Create a program which uses the three strings from this program to  
1469 print the names of three of your favorite movie actors.

```
1470 %mathpiper
```

```
1471 /*
```

```
1472     This program uses strings and index numbers to print
```

```
1473     a person's name.
```

```
1474 */
```

```
1475 upper := "ABCDEFGHJKLMNOPQRSTUVWXYZ";
```

```
1476 lower := "abcdefghijklmnopqrstuvwxyz";
```

```
1477 extra := "!.@#$%^&*() _+<>,?/{ }[]|\-=";
```

```
1478 //Print "Mary Smith."
```

```
1479 Echo(upper[13],lower[1],lower[18],lower[25],extra[12],upper[19],lower[13],l
```

```
1480 ower[9],lower[20],lower[8],extra[1]);
```

```
1481 %/mathpiper
```

```
1482     %output,preserve="false"
```

```
1483     Result: True
```

```
1484
```

```
1485     Side Effects:
```

```
1486     Mary Smith.
```

```
1487 . %/output
```



## 10 Rectangular Selection Mode And Text Area Splitting

### 10.1 Rectangular Selection Mode

One capability that MathRider has that a word processor may not have is the ability to select rectangular sections of text. To see how this works, do the following:

- 1) Type three or four lines of text into a text area.
- 2) Hold down the **<Alt>** key then slowly press the **backslash key** (\) a few times. The bottom of the MathRider window contains a text field which MathRider uses to communicate information to the user. As **<Alt>\** is repeatedly pressed, messages are displayed which read **Rectangular selection is on** and **Rectangular selection is off**.
- 3) Turn rectangular selection on and then select some text in order to see how this is different than normal selection mode. **When you are done experimenting, set rectangular selection mode to off.**

Most of the time normal selection mode is what you want to use but in certain situations rectangular selection mode is better.

### 10.2 Text area splitting

Sometimes it is useful to have two or more text areas open for a single document or multiple documents so that different parts of the documents can be edited at the same time. A situation where this would have been helpful was in the previous section where the output from an exercise in a MathRider worksheet contained a list of index numbers and letters which was useful for completing a later exercise.

MathRider has this ability and it is called **splitting**. If you look just to the right of the toolbar there is an icon which looks like a blank window, an icon to the right of it which looks like a window which was split horizontally, and an icon to the right of the horizontal one which is split vertically. If you let your mouse hover over these icons, a short description will be displayed for each of them. **(For now, ignore the icon which has a yellow sunburst on it. It is the New View icon and it is an advanced feature.)**

Select a text area and then experiment with splitting it by pressing the horizontal and vertical splitting buttons. Move around these split text areas with their scroll bars and when you want to unsplit the document, just press the **"Unsplit All"** icon.

## 1522 11 Working With Random Integers

1523 It is often useful to use random integers in a program. For example, a program  
1524 may need to simulate the rolling of dice in a game. In this section, a function for  
1525 obtaining nonnegative integers is discussed along with how to use it to simulate  
1526 the rolling of dice.

### 1527 11.1 Obtaining Nonnegative Random Integers With The RandomInteger() 1528 Function

1529 One way that a MathPiper program can generate random integers is with the  
1530 RandomInteger() function **(Note: the RandomInteger() function is not**  
1531 **currently listed in the MathPiperDocs plugin.)** The RandomInteger()  
1532 function takes an integer as a parameter and it returns a random integer  
1533 between 0 and the passed in integer. The following example shows random  
1534 integers between 0 and 4 **inclusive** being obtained from RandomInteger().  
1535 **Inclusive** here means that both 0 and 4 are included in the range of random  
1536 integers that may be returned. If the word **exclusive** was used instead, this  
1537 would mean that neither 0 nor 4 would be in the range.

```
1538 In> RandomInteger(5)
1539 Result> 3
1540 In> RandomInteger(5)
1541 Result> 4
1542 In> RandomInteger(5)
1543 Result> 3
1544 In> RandomInteger(5)
1545 Result> 1
1546 In> RandomInteger(5)
1547 Result> 2
1548 In> RandomInteger(5)
1549 Result> 4
1550 In> RandomInteger(5)
1551 Result> 1
1552 In> RandomInteger(5)
1553 Result> 1
1554 In> RandomInteger(5)
1555 Result> 0
1556 In> RandomInteger(5)
1557 Result> 1
```

1558 If generating integers between 1 and 5 inclusive is desired instead of integers  
1559 between 0 and 4, the number 1 can simply be added to the value which is  
1560 returned by RandomInteger():

```
1561 In> RandomInteger(5) + 1
```

```
1562 Result> 4
1563 In> RandomInteger(5) + 1
1564 Result> 5
1565 In> RandomInteger(5) + 1
1566 Result> 4
1567 In> RandomInteger(5) + 1
1568 Result> 2
1569 In> RandomInteger(5) + 1
1570 Result> 3
1571 In> RandomInteger(5) + 1
1572 Result> 5
1573 In> RandomInteger(5) + 1
1574 Result> 2
1575 In> RandomInteger(5) + 1
1576 Result> 2
1577 In> RandomInteger(5) + 1
1578 Result> 1
1579 In> RandomInteger(5) + 1
1580 Result> 2
```

1581 Random integers between 1 and 100 can be generated by passing 100 to  
1582 RandomInteger() and adding 1 to the result.:

```
1583 In> RandomInteger(100) + 1
1584 Result> 15
1585 In> RandomInteger(100) + 1
1586 Result> 14
1587 In> RandomInteger(100) + 1
1588 Result> 82
1589 In> RandomInteger(100) + 1
1590 Result> 93
1591 In> RandomInteger(100) + 1
1592 Result> 32
```

1593 A range of random integers that does not start with 0 or 1 can also be generated.  
1594 For example, random integers between 50 and 100 can be obtained by having  
1595 RandomInteger() generate a random integer between 0 and 49 and then adding  
1596 1 and 50 to the result:

```
1597 In> RandomInteger(50) + 1 + 50
1598 Result> 87
1599 In> RandomInteger(50) + 1 + 50
1600 Result> 100
1601 In> RandomInteger(50) + 1 + 50
1602 Result> 76
1603 In> RandomInteger(50) + 1 + 50
1604 Result> 60
1605 In> RandomInteger(50) + 1 + 50
1606 Result> 73
```

## 1607 **11.2 Simulating The Rolling Of Dice**

1608 The following example shows the simulated rolling of a single six sided die using  
1609 the RandomInteger() function:

```
1610 In> RandomInteger(6) + 1
1611 Result> 5
1612 In> RandomInteger(6) + 1
1613 Result> 6
1614 In> RandomInteger(6) + 1
1615 Result> 3
1616 In> RandomInteger(6) + 1
1617 Result> 2
1618 In> RandomInteger(6) + 1
1619 Result> 5
```

1620 Code that simulates the rolling of two 6 sided dice can be evaluated in the  
1621 MathPiper console by placing it within a **code block**. The following code  
1622 outputs the sum of the two simulated dice:

```
1623 In> [a := RandomInteger(6) + 1; b := RandomInteger(6) + 1; a + b;]
1624 Result> 6
1625 In> [a := RandomInteger(6) + 1; b := RandomInteger(6) + 1; a + b;]
1626 Result> 12
1627 In> [a := RandomInteger(6) + 1; b := RandomInteger(6) + 1; a + b;]
1628 Result> 6
1629 In> [a := RandomInteger(6) + 1; b := RandomInteger(6) + 1; a + b;]
1630 Result> 4
1631 In> [a := RandomInteger(6) + 1; b := RandomInteger(6) + 1; a + b;]
1632 Result> 3
1633 In> [a := RandomInteger(6) + 1; b := RandomInteger(6) + 1; a + b;]
1634 Result> 8
```

1635 Now that we have the ability to simulate the rolling of two 6 sided dice, it would  
1636 be interesting to determine if some sums of these dice occur more frequently  
1637 than other sums. What we would like to do is to roll these simulated dice  
1638 hundreds (or even thousands) of times and then analyze the sums that were  
1639 produced. We don't have the programming capability to easily do this yet, but  
1640 after we finish the section on while loops, we will.

## 12 Making Decisions

The simple programs that have been discussed up to this point show some of the power that software makes available to programmers. However, these programs are limited in their problem solving ability because they are unable to make decisions. This section shows how programs which have the ability to make decisions are able to solve a wider range of problems than programs that can't make decisions.

### 12.1 Conditional Operators

A program's decision making ability is based on a set of special operators which are called **conditional operators**. A **conditional operator** is an operator that is used to **compare two values**. Expressions that contain conditional operators return a **boolean value** and a **boolean value** is one that can only be **True** or **False**. In case you are curious about the strange name, boolean values come from the area of mathematics called **boolean logic**. This logic was created by a mathematician named **George Boole** and this is where the name boolean came from. Table 2 shows the conditional operators that MathPiper uses:

Operator	Description
<code>x = y</code>	Returns <b>True</b> if the two values are equal and <b>False</b> if they are not equal. Notice that <code>=</code> performs a comparison and not an assignment like <code>:=</code> does.
<code>x != y</code>	Returns <b>True</b> if the values are not equal and <b>False</b> if they are equal.
<code>x &lt; y</code>	Returns <b>True</b> if the left value is less than the right value and <b>False</b> if the left value is not less than the right value.
<code>x &lt;= y</code>	Returns <b>True</b> if the left value is less than or equal to the right value and <b>False</b> if the left value is not less than or equal to the right value.
<code>x &gt; y</code>	Returns <b>True</b> if the left value is greater than the right value and <b>False</b> if the left value is not greater than the right value.
<code>x &gt;= y</code>	Returns <b>True</b> if the left value is greater than or equal to the right value and <b>False</b> if the left value is not greater than or equal to the right value.

Table 2: Conditional Operators

This example shows some of these conditional operators being evaluated in the MathPiper console:

```
In> 1 < 2
Result> True
```

```
1661 In> 4 > 5
1662 Result> False
```

```
1663 In> 8 >= 8
1664 Result> True
```

```
1665 In> 5 <= 10
1666 Result> True
```

1667 The following examples show each of the conditional operators in Table 2 being  
1668 used to compare values that have been assigned to variables **x** and **y**:

```
1669 %mathpiper
```

```
1670 // Example 1.
1671 x := 2;
1672 y := 3;
```

```
1673 Echo(x, "=", y, ":", x = y);
1674 Echo(x, "!= ", y, ":", x != y);
1675 Echo(x, "< ", y, ":", x < y);
1676 Echo(x, "<= ", y, ":", x <= y);
1677 Echo(x, "> ", y, ":", x > y);
1678 Echo(x, ">= ", y, ":", x >= y);
```

```
1679 %/mathpiper
```

```
1680 %output,preserve="false"
1681 Result: True
1682
1683 Side Effects:
1684 2 = 3 :False
1685 2 != 3 :True
1686 2 < 3 :True
1687 2 <= 3 :True
1688 2 > 3 :False
1689 2 >= 3 :False
1690 . %/output
```

```
1691 %mathpiper
```

```
1692 // Example 2.
1693 x := 2;
1694 y := 2;
```

```
1695 Echo(x, "=", y, ":", x = y);
1696 Echo(x, "!= ", y, ":", x != y);
1697 Echo(x, "< ", y, ":", x < y);
1698 Echo(x, "<= ", y, ":", x <= y);
1699 Echo(x, "> ", y, ":", x > y);
```

```
1700     Echo(x, ">= ", y, ":", x >= y);
```

```
1701 %/mathpiper
```

```
1702     %output,preserve="false"
```

```
1703     Result: True
```

```
1704
```

```
1705     Side Effects:
```

```
1706     2 = 2 :True
```

```
1707     2 != 2 :False
```

```
1708     2 < 2 :False
```

```
1709     2 <= 2 :True
```

```
1710     2 > 2 :False
```

```
1711     2 >= 2 :True
```

```
1712 .    %/output
```

```
1713 %mathpiper
```

```
1714 // Example 3.
```

```
1715 x := 3;
```

```
1716 y := 2;
```

```
1717 Echo(x, "=", y, ":", x = y);
```

```
1718 Echo(x, "!= ", y, ":", x != y);
```

```
1719 Echo(x, "< ", y, ":", x < y);
```

```
1720 Echo(x, "<= ", y, ":", x <= y);
```

```
1721 Echo(x, "> ", y, ":", x > y);
```

```
1722 Echo(x, ">= ", y, ":", x >= y);
```

```
1723 %/mathpiper
```

```
1724     %output,preserve="false"
```

```
1725     Result: True
```

```
1726
```

```
1727     Side Effects:
```

```
1728     3 = 2 :False
```

```
1729     3 != 2 :True
```

```
1730     3 < 2 :False
```

```
1731     3 <= 2 :False
```

```
1732     3 > 2 :True
```

```
1733     3 >= 2 :True
```

```
1734 .    %/output
```

1735 Conditional operators are placed at a lower level of precedence than the other  
1736 operators we have covered to this point:

1737 ()     Parentheses are evaluated from the inside out.

1738 ^     Then exponents are evaluated right to left.

1739     \*,%,/ Then multiplication, remainder, and division operations are evaluated  
1740             left to right.

1741     +, - Then addition and subtraction are evaluated left to right.

1742     =,!=,<,<=,>,>= Finally, conditional operators are evaluated.

## 1743   **12.2 Predicate Expressions**

1744   Expressions which return either **True** or **False** are called "**predicate**"  
1745   expressions. By themselves, predicate expressions are not very useful and they  
1746   only become so when they are used with special decision making functions, like  
1747   the If() function (which is discussed in the next section).

## 1748   **12.3 Exercises**

### 1749   **12.3.1 Exercise 1**

1750   Open a MathPiper session and evaluate the following predicate expressions:

1751   In> 3 = 3

1752   In> 3 = 4

1753   In> 3 < 4

1754   In> 3 != 4

1755   In> -3 < 4

1756   In> 4 >= 4

1757   In> 1/2 < 1/4

1758   In> 15/23 < 122/189

1759   /\*In the following two expressions, notice that 1/2 is not considered to be  
1760   equal to .5 unless it is converted to a numerical value first.\*/

1761   In> 1/2 = .5

1762   In> N(1/2) = .5

### 1763   **12.3.2 Exercise 2**

1764   Come up with 10 predicate expressions of your own and evaluate them in the  
1765   MathPiper console.



## 1766 **12.4 Making Decisions With The If() Function & Predicate Expressions**

1767 All programming languages have the ability to make decisions and the most  
1768 commonly used function for making decisions in MathPiper is the **If()** function.

1769 There are two calling formats for the If() function:

```
If(predicate, then)  
If(predicate, then, else)
```

1770 The way the first form of the If() function works is that it evaluates the first  
1771 expression in its argument list (which is the "**predicate**" expression) and then  
1772 looks at the value that is returned. If this value is **True**, the "**then**" expression  
1773 that is listed second in the argument list is executed. If the predicate expression  
1774 evaluates to **False**, the "**then**" expression is not executed. (Note: any function  
1775 that accepts a predicate expression as a parameter can also accept the boolean  
1776 values True and False).

1777 The following program uses an **If()** function to determine if the value in variable  
1778 number is greater than 5. If number is greater than 5, the program will echo  
1779 "Greater" and then "End of program":

```
1780 %mathpiper  
1781 number := 6;  
1782 If(number > 5, Echo(number, "is greater than 5.));  
1783 Echo("End of program.");  
1784 %/mathpiper  
1785 %output,preserve="false"  
1786 Result: True  
1787  
1788 Side Effects:  
1789 6 is greater than 5.  
1790 End of program.  
1791 . %/output
```

1792 In this program, number has been set to 6 and therefore the expression number  
1793 > 5 is **True**. When the **If()** function evaluates the **predicate expression** and  
1794 determines it is **True**, it then executes the **first Echo()** function. The **second**  
1795 **Echo()** function at the bottom of the program prints "End of program"  
1796 regardless of what the If() function does. (**Note: semicolons cannot be placed**  
1797 **after expressions which are in function calls.**)

1798 Here is the same program except that **number** has been set to **4** instead of **6**:

```
1799 %mathpiper
1800 number := 4;
1801 If(number > 5, Echo(number, "is greater than 5.));
1802 Echo("End of program.");
1803 %/mathpiper
1804 %output,preserve="false"
1805 Result: True
1806
1807 Side Effects:
1808 End of program.
1809 . %/output
```

1810 This time the expression **number > 4** returns a value of **False** which causes the  
1811 **If()** function to not execute the "**then**" expression that was passed to it.

#### 1812 12.4.1 If() Functions Which Include An "Else" Parameter

1813 The second form of the If() function takes a third "**else**" expression which is  
1814 executed only if the predicate expression is **False**. This program is similar to the  
1815 previous one except an "**else**" expression has been added to it:

```
1816 %mathpiper
1817 x := 4;
1818 If(x > 5, Echo(x, "is greater than 5."), Echo(x, "is NOT greater than 5.));
1819 Echo("End of program.");
1820 %/mathpiper
1821 %output,preserve="false"
1822 Result: True
1823
1824 Side Effects:
1825 4 is NOT greater than 5.
1826 End of program.
1827 . %/output
```

## 1828 **12.5 Exercises**

### 1829 **12.5.1 Exercise 1**

1830 Write a program which uses the `RandomInteger()` function to simulate the  
1831 flipping of a coin (Hint: you can use 1 to represent a head and 0 to  
1832 represent a tail.). Use predicate expressions, the `If()` function, and the  
1833 `Echo()` function to print the string **"The coin came up heads."** or the string  
1834 **"The coin came up tails."**, depending on what the simulated coin flip came  
1835 up as when the code was executed.

## 1836 **12.6 The And(), Or(), & Not() Boolean Functions & Infix Notation**

### 1837 **12.6.1 And()**

1838 Sometimes a programmer needs to check if two or more expressions are all **True**  
1839 and one way to do this is with the **And()** function. The `And()` function has **two**  
1840 **calling formats** (or **notations**) and this is the first one:

```
And(expression1, expression2, expression3, ..., expressionN)
```

1841 This calling format is able to accept one or more predicate expressions as input.  
1842 If **all** of these expressions returns a value of **True**, the `And()` function will also  
1843 return a **True**. However, if **any** of the expressions return a **False**, then the `And()`  
1844 function will return a **False**. This can be seen in the following example:

```
1845 In> And(True, True)
1846 Result> True
```

```
1847 In> And(True, False)
1848 Result> False
```

```
1849 In> And(False, True)
1850 Result> False
```

```
1851 In> And(True, True, True, True)
1852 Result> True
```

```
1853 In> And(True, True, False, True)
1854 Result> False
```

1855 The second format (or notation) that can be used to call the `And()` function is  
1856 called **infix** notation:

```
expression1 And expression2
```

1857 With **infix** notation, an expression is placed on both sides of the And() function  
1858 name instead of being placed inside of parentheses that are next to it:

```
1859 In> True And True  
1860 Result> True
```

```
1861 In> True And False  
1862 Result> False
```

```
1863 In> False And True  
1864 Result> False
```

1865 Infix notation can only accept **two** expressions at a time, but it is often more  
1866 convenient to use than function calling notation. The following program also  
1867 demonstrates the infix version of the And() function being used:

```
1868 %mathpiper
```

```
1869 a := 7;  
1870 b := 9;
```

```
1871 Echo("1: ", a < 5 And b < 10);  
1872 Echo("2: ", a > 5 And b > 10);  
1873 Echo("3: ", a < 5 And b > 10);  
1874 Echo("4: ", a > 5 And b < 10);
```

```
1875 If(a > 5 And b < 10, Echo("These expressions are both true."));
```

```
1876 %/mathpiper
```

```
1877     %output,preserve="false"  
1878     Result: True  
1879  
1880     Side Effects:  
1881     1: False  
1882     2: False  
1883     3: False  
1884     4: True  
1885     These expressions are both true.  
1886 .    %/output
```

## 1887 12.6.2 Or()

1888 The Or() function is similar to the And() function in that it has both a function  
1889 calling format and an infix calling format and it only works with predicate  
1890 expressions. However, instead of requiring that all expressions be **True** in order  
1891 to return a **True**, Or() will return a **True** if **one or more expressions are True**.

1892 Here is the function calling format for Or():

```
Or(expression1, expression2, expression3, ..., expressionN)
```

1893 and this example shows Or() being used with function calling format:

1894 In> Or(True, False)

1895 Result> True

1896 In> Or(False, True)

1897 Result> True

1898 In> Or(False, False)

1899 Result> False

1900 In> Or(False, False, False, False)

1901 Result> False

1902 In> Or(False, True, False, False)

1903 Result> True

1904 The infix notation format for Or() is as follows:

```
expression1 Or expression2
```

1905 and this example shows infix notation being used:

1906 In> True Or False

1907 Result> True

1908 In> False Or True

1909 Result> True

1910 In> False Or False

1911 Result> False

1912 The following program also demonstrates the infix version of the Or() function  
1913 being used:

1914 %mathpiper

1915 a := 7;

1916 b := 9;

1917 Echo("1: ", a < 5 Or b < 10);

1918 Echo("2: ", a > 5 Or b > 10);

```
1919 Echo("3: ", a > 5 Or b < 10);
1920 Echo("4: ", a < 5 Or b > 10);

1921 If(a < 5 Or b < 10, Echo("At least one of these expressions is true.));

1922 %/mathpiper

1923     %output,preserve="false"
1924     Result: True
1925
1926     Side Effects:
1927     1: True
1928     2: True
1929     3: True
1930     4: False
1931     At least one of these expressions is true.
1932 .    %/output
```

### 1933 12.6.3 Not() & Prefix Notation

1934 The **Not()** function works with predicate expressions like the And() and Or()  
1935 functions do, except it can only accept **one** expression as input. The way Not()  
1936 works is that it changes a **True** value to a **False** value and a **False** value to a  
1937 **True** value. Here is the Not()'s function calling format:

```
Not(expression)
```

1938 and this example shows Not() being used with function calling format:

```
1939 In> Not(True)
1940 Result> False

1941 In> Not(False)
1942 Result> True
```

1943 Instead of providing an alternative infix calling format like And() and Or() do,  
1944 Not()'s second calling format uses **prefix** notation:

```
Not expression
```

1945 Prefix notation looks similar to function notation except no parentheses are used:

```
1946 In> Not True
1947 Result> False
```

```
1948 In> Not False
1949 Result> True
```

1950 Finally, here is a program that also uses the prefix version of Not():

```
1951 %mathpiper
1952 Echo("3 = 3 is ", 3 = 3);
1953 Echo("Not 3 = 3 is ", Not 3 = 3);
1954 %/mathpiper
1955     %output,preserve="false"
1956     Result: True
1957
1958     Side Effects:
1959     3 = 3 is True
1960     Not 3 = 3 is False
1961 .    %/output
```

## 1962 **12.7 Exercises**

### 1963 **12.7.1 Exercise 1**

1964 The following program simulates the rolling of two dice and prints a  
1965 message if **both** of the two dice come up less than or equal to 3. Create a  
1966 similar program which simulates the flipping of two coins and print the  
1967 message "Both coins came up heads." if both coins come up heads.

```
1968 %mathpiper
1969 /*
1970    This program simulates the rolling of two dice and prints a message if
1971    both of the two dice come up less than or equal to 3.
1972 */
1973
1973 dice1 := RandomInteger(6) + 1;
1974 dice2 := RandomInteger(6) + 1;
1975
1975 Echo("Dice1: ", dice1, " Dice2: ", dice2);
1976 NewLine();
1977
1977 If( dice1 <= 3 And dice2 <= 3, Echo("Both dice came up <= to 3.") );
1978 %/mathpiper
```

### 1979 **12.7.2 Exercise 2**

1980 The following program simulates the rolling of two dice and prints a

```
1981 message if either of the two dice come up less than or equal to 3. Create
1982 a similar program which simulates the flipping of two coins and print the
1983 message "At least one coin came up heads." if at least one coin comes up
1984 heads.

1985 %mathpiper
1986 /*
1987     This program simulates the rolling of two dice and prints a message if
1988     either of the two dice come up less than or equal to 3.
1989 */

1990 dice1 := RandomInteger(6) + 1;
1991 dice2 := RandomInteger(6) + 1;

1992 Echo("Dice1: ", dice1, "   Dice2: ", dice2);
1993 NewLine();

1994 If( dice1 <= 3 Or dice2 <= 3, Echo("At least one die came up <= 3.") );

1995 %/mathpiper
```



## 1996 **13 The While() Looping Function & Bodied Notation**

1997 Many kinds of machines, including computers, derive much of their power from  
1998 the principle of **repeated cycling**. **Repeated cycling** in a MathPiper program  
1999 means to execute one or more expressions over and over again and this process  
2000 is called "**looping**". MathPiper provides a number of ways to implement **loops**  
2001 in a program and these ways range from straight-forward to subtle.

2002 We will begin discussing looping in MathPiper by starting with the straight-  
2003 forward **While** function. The calling format for the **While** function is as follows:

```
2004 While(predicate)  
2005 [  
2006     body_expressions  
2007 ];
```

2008 The **While** function is similar to the **If** function except it will repeatedly execute  
2009 the expressions it contains as long as its "predicate" expression is **True**. As soon  
2010 as the predicate expression returns a **False**, the While() function skips the  
2011 expressions it contains and execution continues with the expression that  
2012 immediately follows the While() function (if there is one).

2013 The expressions which are contained in a While() function are called its "**body**"  
2014 and all functions which have body expressions are called "**bodied**" functions. If  
2015 a body contains more than one expression then these expressions need to be  
2016 placed within a **code block** (code blocks were discussed in an earlier section).  
2017 What a function's body is will become clearer after studying some example  
2018 programs.

### 2019 **13.1 Printing The Integers From 1 to 10**

2020 The following program uses a While() function to print the integers from 1 to 10:

```
2021 %mathpiper  
2022 // This program prints the integers from 1 to 10.  
  
2023 /*  
2024     Initialize the variable count to 1  
2025     outside of the While "loop".  
2026 */  
2027 count := 1;  
  
2028 While(count <= 10)  
2029 [  
2030     Echo(count);
```

```
2031
2032     count := count + 1;  //Increment count by 1.
2033 1;
2034 %/mathpiper
2035     %output,preserve="false"
2036     Result: True
2037
2038     Side Effects:
2039     1
2040     2
2041     3
2042     4
2043     5
2044     6
2045     7
2046     8
2047     9
2048     10
2049 .    %/output
```

2050 In this program, a single variable called **count** is created. It is used to tell the  
2051 Echo() function which integer to print and it is also used in the predicate  
2052 expression that determines if the While() function should continue to **loop** or not.

2053 When the program is executed, 1 is placed into **count** and then the While()  
2054 function is called. The predicate expression **count** <= 10 becomes **1** <= 10  
2055 and, since 1 is indeed less than or equal to 10, a value of **True** is returned by the  
2056 predicate expression.

2057 The While() function sees that the predicate expression returned a **True** and  
2058 therefore it executes all of the expressions inside of its **body** from top to bottom.

2059 The Echo() function prints the current contents of count (which is 1) and then the  
2060 expression count := count + 1 is executed.

2061 The expression **count := count + 1** is a standard expression form that is used in  
2062 many programming languages. Each time an expression in this form is  
2063 evaluated, it **increases the variable it contains by 1**. Another way to describe  
2064 the effect this expression has on **count** is to say that it **increments count by 1**.

2065 In this case **count** contains **1** and, after the expression is evaluated, **count**  
2066 contains **2**.

2067 After the last expression inside the body of the While() function is executed, the  
2068 While() function reevaluates its predicate expression to determine whether it  
2069 should continue looping or not. Since **count** is **2** at this point, the predicate  
2070 expression returns **True** and the code inside the body of the While() function is  
2071 executed again. This loop will be repeated until **count** is incremented to **11** and  
2072 the predicate expression returns **False**.

## 2073 **13.2 Printing The Integers From 1 to 100**

2074 The previous program can be adjusted in a number of ways to achieve different  
2075 results. For example, the following program prints the integers from 1 to 100 by  
2076 changing the **10** in the predicate expression to **100**. A Write() function is used in  
2077 this program so that its output is displayed on the same line until it encounters  
2078 the **wrap margin** in MathRider (which can be set in Utilities -> Buffer  
2079 Options...).

```
2080 %mathpiper
2081 // Print the integers from 1 to 100.
2082 count := 1;
2083 While(count <= 100)
2084 [
2085     Write(count,,);
2086     count := count + 1; //Increment count by 1.
2087 ];
2089 %/mathpiper
2090     %output,preserve="false"
2091     Result: True
2092
2093     Side Effects:
2094     1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,
2095     24,25,26,27,28,29,30,31,32,33,34,35,36,37,38,39,40,41,42,43,
2096     44,45,46,47,48,49,50,51,52,53,54,55,56,57,58,59,60,61,62,63,
2097     64,65,66,67,68,69,70,71,72,73,74,75,76,77,78,79,80,81,82,83,
2098     84,85,86,87,88,89,90,91,92,93,94,95,96,97,98,99,100
2099 . %/output
```

## 2100 **13.3 Printing The Odd Integers From 1 To 99**

2101 The following program prints the odd integers from 1 to 99 by changing the  
2102 **increment value** in the increment expression from **1** to **2**:

```
2103 %mathpiper
2104 //Print the odd integers from 1 to 99.
2105 x := 1;
2106 While(x <= 100)
2107 [
2108     Write(x,,);
```

```
2109     x := x + 2;    //Increment x by 2.
2110 ];
2111 %/mathpiper
2112     %output,preserve="false"
2113     Result: True
2114
2115     Side Effects:
2116     1,3,5,7,9,11,13,15,17,19,21,23,25,27,29,31,33,35,37,39,41,43,
2117     45,47,49,51,53,55,57,59,61,63,65,67,69,71,73,75,77,79,81,83,
2118     85,87,89,91,93,95,97,99
2119 .    %/output
```

### 2120 **13.4 Printing The Integers From 1 To 100 In Reverse Order**

2121 Finally, the following program prints the integers from 1 to 100 in reverse order:

```
2122 %mathpiper
2123 //Print the integers from 1 to 100 in reverse order.
2124 x := 100;
2125 While(x >= 1)
2126 [
2127     Write(x,,);
2128     x := x - 1;    //Decrement x by 1.
2129 ];
2130 %/mathpiper
2131     %output,preserve="false"
2132     Result: True
2133
2134     Side Effects:
2135     100,99,98,97,96,95,94,93,92,91,90,89,88,87,86,85,84,83,82,
2136     81,80,79,78,77,76,75,74,73,72,71,70,69,68,67,66,65,64,63,
2137     62,61,60,59,58,57,56,55,54,53,52,51,50,49,48,47,46,45,44,
2138     43,42,41,40,39,38,37,36,35,34,33,32,31,30,29,28,27,26,25,
2139     24,23,22,21,20,19,18,17,16,15,14,13,12,11,10,9,8,7,6,5,4,
2140     3,2,1
2141 .    %/output
```

2142 In order to achieve the reverse ordering, this program had to initialize **x** to **100**,  
2143 check to see if **x** was **greater than or equal to 1** ( $x \geq 1$ ), and **decrement** **x** by  
2144 **subtracting 1 from it** instead of adding 1 to it.

### 2145 **13.5 Expressions Inside Of Code Blocks Are Indented**

2146 In the programs in the previous sections which use while loops, notice that the  
2147 expressions which are inside of the While() function's code block are **indented**.  
2148 These expressions do not need to be indented to execute properly, but doing so  
2149 makes the program easier to read.

### 2150 **13.6 Long-Running Loops, Infinite Loops, & Interrupting Execution**

2151 It is easy to create a loop that will execute a **large number of times**, or even **an**  
2152 **infinite number of times**, either on purpose or by mistake. When you execute  
2153 a program that contains an **infinite loop**, it will run until you tell MathPiper to  
2154 **interrupt** its execution. This is done by opening the MathPiper console and then  
2155 pressing the "**Stop**" button which it contains. The Stop button is circular and it  
2156 has an X on it. (**Note: currently this button only works if MathPiper is**  
2157 **executed inside of a %mathpiper fold.**)

2158 Lets experiment with the **Stop** button by executing a program that contains an  
2159 infinite loop and then stopping it:

```
2160 %mathpiper
2161 //Infinite loop example program.
2162 x := 1;
2163 While(x < 10)
2164 [
2165     x := 3; //Oops, x is not being incremented!.
2166 ];
2167 %/mathpiper
2168     %output,preserve="false"
2169     Processing...
2170 . %/output
```

2171 Since the contents of x is never changed inside the loop, the expression **x < 10**  
2172 always evaluates to **True** which causes the loop to continue looping. Notice that  
2173 the %output fold contains the word "**Processing...**" to indicate that the program  
2174 is still running the code.

2175 Execute this program now and then interrupt it using the "**Stop**" button. When  
2176 the program is interrupted, the %output fold will display the message "**User**  
2177 **interrupted calculation**" to indicate that the program was interrupted. After a  
2178 program has been interrupted, the program can be edited and then rerun.

### 2179 **13.7 A Program That Simulates Rolling Two Dice 50 Times**

2180 The following program is larger than the previous programs that have been  
2181 discussed in this book, but it is also more interesting and more useful. It uses a  
2182 While() loop to simulate the rolling of two dice 50 times and it records how many  
2183 times each possible sum has been rolled so that this data can be printed. The  
2184 comments in the code explain what each part of the program does. (Remember, if  
2185 you copy this program to a MathRider worksheet, you can use **rectangular**  
2186 **selection mode** to easily remove the line numbers).

```
2187 %mathpiper
2188 /*
2189     This program simulates rolling two dice 50 times.
2190 */
2191
2192 /*
2193     These variables are used to record how many times
2194     a possible sum of two dice has been rolled. They are
2195     all initialized to 0 before the simulation begins.
2196 */
2197 numberOfTwosRolled := 0;
2198 numberOfThreesRolled := 0;
2199 numberOfFoursRolled := 0;
2200 numberOfFivesRolled := 0;
2201 numberOfSixesRolled := 0;
2202 numberOfSevensRolled := 0;
2203 numberOfEightsRolled := 0;
2204 numberOfNinesRolled := 0;
2205 numberOfTensRolled := 0;
2206 numberOfElevensRolled := 0;
2207 numberOfTwelvesRolled := 0;
2208
2209 //This variable keeps track of the number of the current roll.
2210 roll := 1;
2211
2212 Echo("These are the rolls:");
2213
2214 /*
2215     The simulation is performed inside of this while loop. The number of
2216     times the dice will be rolled can be changed by changing the number 50
2217     which is in the While function's predicate expression.
2218 */
2219 While(roll <= 50)
2220 [
2221     //Roll the dice.
2222     die1 := RandomInteger(6) + 1;
2223     die2 := RandomInteger(6) + 1;
```

```
2220
2221
2222 //Calculate the sum of the two dice.
2223 rollSum := die1 + die2;
2224
2225
2226 /*
2227 Print the sum that was rolled. Note: if a large number of rolls
2228 is going to be performed (say > 1000), it would be best to comment
2229 out this Write() function so that it does not put too much text
2230 into the output fold.
2231 */
2232 Write(rollSum,,);
2233
2234
2235 /*
2236 These If() functions determine which sum was rolled and then add
2237 1 to the variable which is keeping track of the number of times
2238 that sum was rolled.
2239 */
2240 If(rollSum = 2, numberOfTwosRolled := numberOfTwosRolled + 1);
2241 If(rollSum = 3, numberOfThreesRolled := numberOfThreesRolled + 1);
2242 If(rollSum = 4, numberOfFoursRolled := numberOfFoursRolled + 1);
2243 If(rollSum = 5, numberOfFivesRolled := numberOfFivesRolled + 1);
2244 If(rollSum = 6, numberOfSixesRolled := numberOfSixesRolled + 1);
2245 If(rollSum = 7, numberOfSevensRolled := numberOfSevensRolled + 1);
2246 If(rollSum = 8, numberOfEightsRolled := numberOfEightsRolled + 1);
2247 If(rollSum = 9, numberOfNinesRolled := numberOfNinesRolled + 1);
2248 If(rollSum = 10, numberOfTensRolled := numberOfTensRolled + 1);
2249 If(rollSum = 11, numberOfElevensRolled := numberOfElevensRolled+1);
2250 If(rollSum = 12, numberOfTwelvesRolled := numberOfTwelvesRolled+1);
2251
2252
2253 //Increment the roll variable to the next roll number.
2254 roll := roll + 1;
2255 ];

```

```
2256 //Print the contents of the sum count variables for visual analysis.
2257 NewLine();
2258 NewLine();
2259 Echo("Number of Twos rolled: ", numberOfTwosRolled);
2260 Echo("Number of Threes rolled: ", numberOfThreesRolled);
2261 Echo("Number of Fours rolled: ", numberOfFoursRolled);
2262 Echo("Number of Fives rolled: ", numberOfFivesRolled);
2263 Echo("Number of Sixes rolled: ", numberOfSixesRolled);
2264 Echo("Number of Sevens rolled: ", numberOfSevensRolled);
2265 Echo("Number of Eights rolled: ", numberOfEightsRolled);
2266 Echo("Number of Nines rolled: ", numberOfNinesRolled);
2267 Echo("Number of Tens rolled: ", numberOfTensRolled);
2268 Echo("Number of Elevens rolled: ", numberOfElevensRolled);
2269 Echo("Number of Twelves rolled: ", numberOfTwelvesRolled);
```

```
2270  %/mathpipec
2271      %output,preserve="false"
2272      Result: True
2273
2274      Side effects:
2275      These are the rolls:
2276      4,8,6,4,6,9,7,11,9,3,11,6,11,7,11,4,7,7,8,7,3,6,7,7,7,12,4,
2277      12,7,8,12,6,8,10,10,5,9,8,4,5,3,5,7,7,4,6,7,7,5,8,
2278
2279      Number of Twos rolled: 0
2280      Number of Threes rolled: 3
2281      Number of Fours rolled: 6
2282      Number of Fives rolled: 4
2283      Number of Sixes rolled: 6
2284      Number of Sevens rolled: 13
2285      Number of Eights rolled: 6
2286      Number of Nines rolled: 3
2287      Number of Tens rolled: 2
2288      Number of Elevens rolled: 4
2289      Number of Twelves rolled: 3
2290  .  %/output
```

## 2291 13.8 Exercises

### 2292 13.8.1 Exercise 1

2293 Create a program which uses a while loop to print the even integers from 2  
2294 to 50 inclusive.

### 2295 13.8.2 Exercise 2

2296 Create a program which prints all the multiples of 5 between 5 and 50  
2297 inclusive.

### 2298 13.8.3 Exercise 3

2299 Create a program which simulates the flipping of a coin 500 times. Print  
2300 the number of times the coin came up heads and the number of times it came  
2301 up tails after the loop is finished executing.



## 2302 14 Predicate Functions

2303 A **predicate function** is a function that either returns **True** or **False**. Most  
2304 predicate functions in MathPiper have names which begin with "**Is**". For  
2305 example, **IsEven()**, **IsOdd()**, **IsInteger()**, etc. The following examples show  
2306 some of the predicate functions that are in MathPiper:

```
2307 In> IsEven(4)
2308 Result> True
```

```
2309 In> IsEven(5)
2310 Result> False
```

```
2311 In> IsZero(0)
2312 Result> True
```

```
2313 In> IsZero(1)
2314 Result> False
```

```
2315 In> IsNegativeInteger(-1)
2316 Result> True
```

```
2317 In> IsNegativeInteger(1)
2318 Result> False
```

```
2319 In> IsPrime(7)
2320 Result> True
```

```
2321 In> IsPrime(100)
2322 Result> False
```

2323 There is also an **IsBound()** and an **IsUnbound()** function that can be used to  
2324 determine whether or not a value is bound to a given variable:

```
2325 In> a
2326 Result> a
```

```
2327 In> IsBound(a)
2328 Result> False
```

```
2329 In> a := 1
2330 Result> 1
```

```
2331 In> IsBound(a)
2332 Result> True
```

```
2333 In> Clear(a)
2334 Result> True
```

```
2335 In> a
2336 Result> a
```

```
2337 In> IsBound(a)
2338 Result> False
```

2339 The complete list of predicate functions is contained in the **User**  
2340 **Functions/Predicates** node in the MathPiperDocs plugin.

### 2341 **14.1 Finding Prime Numbers With A Loop**

2342 Predicate functions are very powerful when they are combined with loops  
2343 because they can be used to automatically make numerous checks. The  
2344 following program uses a while loop to pass the integers 1 through 20 (one at a  
2345 time) to the **IsPrime()** function in order to determine which integers are prime  
2346 and which integers are not prime:

```
2347 %mathpiper
2348 //Determine which numbers between 1 and 20 (inclusive) are prime.
2349 x := 1;
2350 While(x <= 20)
2351 [
2352     primeStatus := IsPrime(x);
2353     Echo(x, "is prime: ", primeStatus);
2354     x := x + 1;
2355 ];
2356
2357 %/mathpiper
2358
2359 %output,preserve="false"
2360 Result: True
2361
2362 Side Effects:
2363 1 is prime: False
2364 2 is prime: True
2365 3 is prime: True
2366 4 is prime: False
2367 5 is prime: True
2368 6 is prime: False
2369 7 is prime: True
2370 8 is prime: False
2371 9 is prime: False
2372 10 is prime: False
2373 11 is prime: True
2374 12 is prime: False
```

```
2375         13 is prime: True
2376         14 is prime: False
2377         15 is prime: False
2378         16 is prime: False
2379         17 is prime: True
2380         18 is prime: False
2381         19 is prime: True
2382         20 is prime: False
2383     .    %/output
```

2384 This program worked fairly well, but it is limited because it prints a line for each  
2385 prime number and also each non-prime number. This means that if large ranges  
2386 of integers were processed, enormous amounts of output would be produced.  
2387 The following program solves this problem by using an If() function to only print  
2388 a number if it is prime:

```
2389 %mathpiper

2390 //Print the prime numbers between 1 and 50 (inclusive).

2391 x := 1;

2392 While(x <= 50)
2393 [
2394     primeStatus := IsPrime(x);
2395
2396     If(primeStatus = True, Write(x,,) );
2397
2398     x := x + 1;
2399 ];

2400 %/mathpiper

2401     %output,preserve="false"
2402     Result: True
2403
2404     Side Effects:
2405     2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,
2406 .    %/output
```

2407 This program is able to process a much larger range of numbers than the  
2408 previous one without having its output fill up the text area. However, the  
2409 program itself can be shortened by moving the **IsPrime()** function **inside** of the  
2410 **If()** function instead of using the **primeStatus** variable to communicate with it:

```
2411 %mathpiper

2412 /*
```

```
2413     Print the prime numbers between 1 and 50 (inclusive).
2414     This is a shorter version which places the IsPrime() function
2415     inside of the If() function instead of using a variable.
2416 */
2417 x := 1;
2418 While(x <= 50)
2419 [
2420     If(IsPrime(x), Write(x,,) );
2421
2422     x := x + 1;
2423 ];
2424 %/mathpiper
2425     %output,preserve="false"
2426     Result: True
2427
2428     Side Effects:
2429     2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,
2430 .    %/output
```

## 2431 **14.2 Finding The Length Of A String With The Length() Function**

2432 Strings can contain zero or more characters and the **Length()** function can be  
2433 used to determine how many characters a string holds:

```
2434 In> s := "Red"
2435 Result> "Red"
2436 In> Length(s)
2437 Result> 3
```

2438 In this example, the string "Red" is assigned to the variable **s** and then **s** is  
2439 passed to the **Length()** function. The **Length()** function returned a **3** which  
2440 means the string contained **3 characters**.

2441 The following example shows that strings can also be passed to functions  
2442 directly:

```
2443 In> Length("Red")
2444 Result> 3
```

2445 An **empty string** is represented by **two double quote marks with no space in**  
2446 **between them**. The **length** of an empty string is **0**:

```
2447 In> Length("")
2448 Result> 0
```

### 2449 **14.3 Converting Numbers To Strings With The String() Function**

2450 Sometimes it is useful to convert a number to a string so that the individual  
2451 digits in the number can be analyzed or manipulated. The following example  
2452 shows a **number** being converted to a **string** with the **String()** function so that  
2453 its **leftmost** and **rightmost** digits can be placed into **variables**:

```
2454 In> number := 523
2455 Result> 523
```

```
2456 In> stringNumber := String(number)
2457 Result> "523"
```

```
2458 In> leftmostDigit := stringNumber[1]
2459 Result> "5"
```

```
2460 In> rightmostDigit := stringNumber[ Length(stringNumber) ]
2461 Result> "3"
```

2462 Notice that the Length() function is used here to determine which character in  
2463 **stringNumber** held the **rightmost** digit.

### 2464 **14.4 Finding Prime Numbers Which End With 7 (And Multi-line Function Calls)**

2466 Now that we have covered how to turn a number into a string, lets use this  
2467 ability inside a loop. The following program finds all the **prime numbers**  
2468 between **1** and **500** which have a **7 as their rightmost digit**. There are three  
2469 important things which are shown in this program:

2470 1) Function calls **can have their parameters placed on more than one**  
2471 **line** if the parameters are too long to fit on a **single line**. In this case, a long  
2472 code block is being placed inside of an If() function.

2473 2) Code blocks (which are considered to be compound expressions) **cannot**  
2474 **have a semicolon placed after them if they are in a function call**. If a  
2475 semicolon is placed after this code block, an error will be produced.

2476 3) If() functions can be placed inside of other If() functions in order to make  
2477 more complex decisions. This is referred to as **nesting** functions.

2478 When the program is executed, it finds 24 prime numbers which have 7 as their  
2479 rightmost digit:

```
2480 %mathpiper
2481 /*
2482     Find all the prime numbers between 1 and 500 which have a 7
2483     as their rightmost digit.
2484 */
2485 x := 1;
2486 While(x <= 500)
2487 [
2488     //Notice how function parameters can be put on more than one line.
2489     If(IsPrime(x),
2490         [
2491             stringVersionOfNumber := String(x);
2492             stringLength := Length(stringVersionOfNumber);
2493             //Notice that If() functions can be placed inside of other
2494             // If() functions.
2495             If(stringVersionOfNumber[stringLength] = "7", Write(x,,) );
2496         ] //Notice that semicolons cannot be placed after code blocks
2497         //which are in function calls.
2498     ); //This is the close parentheses for the outer If() function.
2499     x := x + 1;
2500 ];
2501
2502 %/mathpiper
2503
2504 %output,preserve="false"
2505 Result: True
2506
2507 Side Effects:
2508 7,17,37,47,67,97,107,127,137,157,167,197,227,257,277,307,317,
2509 337,347,367,397,457,467,487,
2510 . %/output
```

2514 It would be nice if we had the ability to store these numbers someplace so that  
2515 they could be processed further and this is discussed in the next section.

## 2516 14.5 Exercises

### 2517 14.5.1 Exercise 1

2518 Write a program which uses a loop to determine how many prime numbers there  
2519 are between 1 and 1000. You do not need to print the numbers themselves,  
2520 just how many there are.

**2521 14.5.2 Exercise 2**

2522 Write a program which uses a loop to print all of the prime numbers between  
2523 10 and 99 which contain the digit 3 in either their 1's place, or their  
2524 10's place, or both places.

## 2525 15 Lists: Values That Hold Sequences Of Expressions

2526 The **list** value type is designed to hold expressions in an **ordered collection** or  
2527 **sequence**. Lists are very flexible and they are one of the most heavily used  
2528 value types in MathPiper. Lists can **hold expressions of any type**, they can be  
2529 made to **grow and shrink as needed**, and they can be **nested**. Expressions in a  
2530 list can be **accessed by their position** in the list (similar to the way that  
2531 characters in a string are accessed) and they can also be **replaced by other**  
2532 **expressions**.

2533 One way to create a list is by placing zero or more expressions separated by  
2534 commas inside of a **pair of braces {}**. In the following example, a list is created  
2535 that contains various expressions and then it is assigned to the variable **x**:

```
2536 In> x := {7,42,"Hello",1/2,var}  
2537 Result> {7,42,"Hello",1/2,var}
```

```
2538 In> x  
2539 Result> {7,42,"Hello",1/2,var}
```

2540 The number of expressions in a list can be determined with the **Length()**  
2541 function:

```
2542 In> Length({7,42,"Hello",1/2,var})  
2543 Result> 5
```

2544 A single expression in a list can be accessed by placing a set of **brackets []** to  
2545 the right of the variable that is bound to the list and then putting the  
2546 expression's position number inside of the brackets (**Note: the first expression**  
2547 **in the list is at position 1 counting from the left end of the list**):

```
2548 In> x[1]  
2549 Result> 7
```

```
2550 In> x[2]  
2551 Result> 42
```

```
2552 In> x[3]  
2553 Result> "Hello"
```

```
2554 In> x[4]  
2555 Result> 1/2
```

```
2556 In> x[5]  
2557 Result> var
```

2558 The **1st** and **2nd** expressions in this list are **integers**, the **3rd** expression is a



2559 **string**, the **4th** expression is a **rational number** and the **5th** expression is an  
2560 **unbound variable**.

2561 Lists can also hold other lists as shown in the following example:

```
2562 In> x := {20, 30, {31, 32, 33}, 40}
```

```
2563 Result> {20,30,{31,32,33},40}
```

```
2564 In> x[1]
```

```
2565 Result> 20
```

```
2566 In> x[2]
```

```
2567 Result> 30
```

```
2568 In> x[3]
```

```
2569 Result> {31,32,33}
```

```
2570 In> x[4]
```

```
2571 Result> 40
```

```
2572
```

2573 The expression in the **3rd** position in the list is another **list** which contains the  
2574 integers **31**, **32**, and **33**.

2575 An expression in this second list can be accessed by two **two sets of brackets**:

```
2576 In> x[3][2]
```

```
2577 Result> 32
```

2578 The **3** inside of the first set of brackets accesses the **3rd** member of the **first** list  
2579 and the **2** inside of the second set of brackets accesses the **2nd** member of the  
2580 **second** list.

## 2581 **15.1 Append() & Nondestructive List Operations**

```
Append(list, expression)
```

2582 The **Append()** function adds an expression to the end of a list:

```
2583 In> testList := {21,22,23}
```

```
2584 Result> {21,22,23}
```

```
2585 In> Append(testList, 24)
```

```
2586 Result> {21,22,23,24}
```

2587 However, instead of changing the **original** list, **Append()** creates a **copy** of the  
2588 **original** list and appends the expression to the **copy**. This can be confirmed by  
2589 evaluating the variable **testList** after the **Append()** function has been called:

```
2590 In> testList
2591 Result> {21,22,23}
```

2592 Notice that the list that is bound to **testList** was not modified by the **Append()**  
2593 function. This is called a **nondestructive list operation** and **most MathPiper**  
2594 **functions that manipulate lists do so nondestructively**. To have the new list  
2595 bound to the variable that is being used, the following technique can be  
2596 employed:

```
2597 In> testList := {21,22,23}
2598 Result> {21,22,23}

2599 In> testList := Append(testList, 24)
2600 Result> {21,22,23,24}
```

```
2601 In> testList
2602 Result> {21,22,23,24}
```

2603 After this code has been executed, the new list has indeed been bound to  
2604 **testList** as desired.

2605 There are some functions, such as **DestructiveAppend()**, which **do** change the  
2606 original list and most of them begin with the word "Destructive". These are  
2607 called "destructive functions" and they are advanced functions which are not  
2608 covered in this book.

## 2609 **15.2 Using While Loops With Lists**

2610 Functions that loop can be used to **select each expression in a list in turn** so  
2611 that an operation can be performed on these expressions. The following  
2612 program uses a while loop to print each of the expressions in a list:

```
2613 %mathpiper
2614 //Print each number in the list.

2615 x := {55,93,40,21,7,24,15,14,82};
2616 y := 1;

2617 While(y <= Length(x))
2618 [
2619     Echo(y, "- ", x[y]);
2620     y := y + 1;
2621 ];

2622 %/mathpiper

2623 %output,preserve="false"
```

```
2624         Result: True
2625
2626         Side Effects:
2627         1 - 55
2628         2 - 93
2629         3 - 40
2630         4 - 21
2631         5 - 7
2632         6 - 24
2633         7 - 15
2634         8 - 14
2635         9 - 82
2636 .    %/output
```

2637 A **loop** can also be used to search through a list. The following program uses a  
2638 **While()** function and an **If()** function to search through a list to see if it contains  
2639 the number **53**. If 53 is found in the list, a message is printed:

```
2640 %mathpiper
2641 //Determine if 53 is in the list.
2642 testList := {18,26,32,42,53,43,54,6,97,41};
2643 index := 1;
2644 While(index <= Length(testList))
2645 [
2646     If(testList[index] = 53,
2647         Echo("53 was found in the list at position", index));
2648     index := index + 1;
2649 ];
2650
2651 %/mathpiper
2652 %output,preserve="false"
2653     Result: True
2654
2655     Side Effects:
2656     53 was found in the list at position 5
2657 .    %/output
```

2658 When this program was executed, it determined that **53** was present in the list at  
2659 position **5**.

### 2660 15.2.1 Using A While Loop And Append() To Place Values In A List

2661 In an earlier section it was mentioned that it would be nice if we could store a set  
2662 of values for later processing and this can be done with a **while loop** and the

2663 **Append()** function. The following program creates an empty list and assigned it  
2664 to the variable **primes**. The **while loop** and the **IsPrime()** function is then used  
2665 to locate the prime integers between 1 and 50 and the **Append()** function is used  
2666 to place them in the list. The last part of the program then prints some  
2667 information about the numbers that were placed into the list:

```
2668 %mathpiper
2669 //Place the prime numbers between 1 and 50 (inclusive) into a list.
2670 //Create an empty list.
2671 primes := {};
2672 x := 1;
2673 While(x <= 50)
2674 [
2675     /*
2676         If x is prime, append it to the end of the list and then assign
2677         the new list that is created to the variable 'primes'.
2678     */
2679     If(IsPrime(x), primes := Append(primes, x ) );
2680
2681     x := x + 1;
2682 ];
2683 //Print information about the primes that were found.
2684 Echo("Primes ", primes);
2685 Echo("The number of primes in the list = ", Length(primes) );
2686 Echo("The first number in the list = ", primes[1] );
2687 %/mathpiper
2688 %output,preserve="false"
2689 Result: True
2690
2691 Side Effects:
2692 Primes {2,3,5,7,11,13,17,19,23,29,31,37,41,43,47}
2693 The number of primes in the list = 15
2694 The first number in the list = 2
2695 . %/output
```

2696 The ability to place values into a list with a loop is very powerful and we will be  
2697 using this ability throughout the rest of the book.

## 2698 15.3 Exercises

### 2699 15.3.1 Exercise 1

2700 Create a program that uses a loop and an IsOdd() function to analyze the  
2701 following list and then print the number of odd numbers it contains.

2702 {73, 94, 80, 37, 56, 94, 40, 21, 7, 24, 15, 14, 82, 93, 32, 74, 22, 68, 65, 52, 85, 61, 46, 86, 25}

### 2703 15.3.2 Exercise 2

2704 Create a program that uses a loop and an IsNegativeNumber() function to  
2705 copy all of the negative numbers in the following list into a new list.  
2706 Use the variable **negativeNumbers** to hold the new list.

2707 {36, -29, -33, -6, 14, 7, -16, -3, -14, 37, -38, -8, -45, -21, -26, 6, 6, 38, -20, 33, 41, -  
2708 4, 24, 37, 40, 29}

### 2709 15.3.3 Exercise 3

2710 Create a program that uses a loop to analyze the following list and then  
2711 print the following information about it:

- 2712 1) The largest number in the list.  
2713 2) The smallest number in the list.  
2714 3) The sum of all the numbers in the list.

2715 {73, 94, 80, 37, 56, 94, 40, 21, 7, 24, 15, 14, 82, 93, 32, 74, 22, 68, 65, 52, 85, 61, 46, 86, 25}

## 2716 15.4 The ForEach() Looping Function

2717 The **ForEach()** function uses a **loop** to index through a list like the While()  
2718 function does, but it is more flexible and automatic. ForEach() also uses bodied  
2719 notation like the While() function and here is its calling format:

```
ForEach(variable, list) body
```

2720 **ForEach()** selects each expression in a list in turn, assigns it to the passed-in  
2721 "variable", and then executes the expressions that are inside of "body".  
2722 Therefore, body is **executed once for each expression in the list**.

## 2723 15.5 Print All The Values In A List Using A ForEach() function

2724 This example shows how ForEach() can be used to print all of the items in a list:

2725 `%mathpiper`

```
2726 //Print all values in a list.
2727 ForEach(value, {50,51,52,53,54,55,56,57,58,59})
2728 [
2729     Echo(value);
2730 ];
2731 %mathpiper
2732     %output,preserve="false"
2733     Result: True
2734
2735     Side Effects:
2736     50
2737     51
2738     52
2739     53
2740     54
2741     55
2742     56
2743     57
2744     58
2745     59
2746 .    %/output
```

## 2747 **15.6 Calculate The Sum Of The Numbers In A List Using ForEach()**

2748 In previous examples, counting code in the form **x := x + 1** was used to count  
2749 how many times a while loop was executed. The following program uses a  
2750 **ForEach()** function and a line of code similar to this counter to calculate the  
2751 **sum of the numbers in a list:**

```
2752 %mathpiper
2753 /*
2754     This program calculates the sum of the numbers
2755     in a list.
2756 */
2757 //This variable is used to accumulate the sum.
2758 sum := 0;
2759 ForEach(x, {1,2,3,4,5,6,7,8,9,10} )
2760 [
2761     /*
2762         Add the contents of x to the contents of sum
2763         and place the result back into sum.
2764     */
2765     sum := sum + x;
```

```
2766
2767     //Print the sum as it is being accumulated.
2768     Write(sum,,);
2769     l;

2770     NewLine(); NewLine();

2771     Echo("The sum of the numbers in the list = ", sum);

2772     %/mathpiper

2773     %output,preserve="false"
2774     Result: True
2775
2776     Side Effects:
2777     1,3,6,10,15,21,28,36,45,55,
2778
2779     The sum of the numbers in the list = 55
2780     . %/output
```

2781 In the above program, the integers **1** through **10** were manually placed into a list  
2782 by typing them individually. This method is limited because only a relatively  
2783 small number of integers can be placed into a list this way. The following section  
2784 discusses an operator which can be used to automatically place a large number  
2785 of integers into a list with very little typing.

## 2786 15.7 The .. Range Operator

```
first .. last
```

2787 A programmer often needs to create a list which contains **consecutive integers**  
2788 and the **.. "range"** operator can be used to do this. The **first** integer in the list is  
2789 placed before the **..** operator and the **last** integer in the list is placed after it  
2790 (**Note: there must be a space immediately to the left of the .. operator**  
2791 **and a space immediately to the right of it or an error will be generated.**).  
2792 Here are some examples:

```
2793 In> 1 .. 10
2794 Result> {1,2,3,4,5,6,7,8,9,10}

2795 In> 10 .. 1
2796 Result> {10,9,8,7,6,5,4,3,2,1}

2797 In> 1 .. 100
2798 Result> {1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,
2799         21,22,23,24,25,26,27,28,29,30,31,32,33,34,35,36,37,
2800         38,39,40,41,42,43,44,45,46,47,48,49,50,51,52,53,54,
2801         55,56,57,58,59,60,61,62,63,64,65,66,67,68,69,70,71,
```

```
2802         72,73,74,75,76,77,78,79,80,81,82,83,84,85,86,87,88,  
2803         89,90,91,92,93,94,95,96,97,98,99,100}
```

```
2804 In> -10 .. 10  
2805 Result> {-10,-9,-8,-7,-6,-5,-4,-3,-2,-1,0,1,2,3,4,5,6,7,8,9,10}
```

2806 As these examples show, the .. operator can generate lists of integers in  
2807 ascending order and descending order. It can also generate lists that are very  
2808 large and ones that contain negative integers.

2809 Remember, though, if one or both of the spaces around the .. are omitted, an  
2810 error is generated:

```
2811 In> 1..3  
2812 Result>  
2813 Error parsing expression, near token .3.
```

## 2814 **15.8 Using ForEach() With The Range Operator To Print The Prime** 2815 **Numbers Between 1 And 100**

2816 The following program shows how to use a **ForEach()** function instead of a  
2817 **While()** function to print the prime numbers between 1 and 100. Notice that  
2818 loops that are implemented with **ForEach()** often require less typing than  
2819 their **While()** based equivalents:

```
2820 %mathpiper  
2821 /*  
2822     This program prints the prime integers between 1 and 100 using  
2823     a ForEach() function instead of a While() function. Notice that  
2824     the ForEach() version requires less typing than the While()  
2825     version.  
2826 */  
2827 ForEach(x, 1 .. 100)  
2828 [  
2829     If(IsPrime(x), Write(x,,) );  
2830 ];  
2831 %/mathpiper  
2832 %output,preserve="false"  
2833 Result: True  
2834  
2835 Side Effects:  
2836 2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,53,59,61,67,71,  
2837 73,79,83,89,97,  
2838 . %/output
```



## 2839 15.8.1 Using ForEach() And The Range Operator To Place The Prime 2840 Numbers Between 1 And 50 Into A List

2841 A ForEach() function can also be used to place values in a list, just the the  
2842 While() function can:

```
2843 %mathpiper
2844 /*
2845     Place the prime numbers between 1 and 50 into
2846     a list using a ForEach() function.
2847 */
2848 //Create a new list.
2849 primes := {};
2850 ForEach(number, 1 .. 50)
2851 [
2852     /*
2853         If number is prime, append it to the end of the list and
2854         then assign the new list that is created to the variable
2855         'primes'.
2856     */
2857     If(IsPrime(number), primes := Append(primes, number) );
2858 ];
2859 //Print information about the primes that were found.
2860 Echo("Primes ", primes);
2861 Echo("The number of primes in the list = ", Length(primes) );
2862 Echo("The first number in the list = ", primes[1] );
2863 %/mathpiper
2864     %output,preserve="false"
2865     Result: True
2866
2867     Side Effects:
2868     Primes {2,3,5,7,11,13,17,19,23,29,31,37,41,43,47}
2869     The number of primes in the list = 15
2870     The first number in the list = 2
2871 .    %/output
```

2872 As can be seen from the above examples, the **ForEach()** function and the **range**  
2873 **operator** can do a significant amount of work with very little typing. You will  
2874 discover in the next section that MathPiper has functions which are even more  
2875 powerful than these two.

2876 **15.8.2 Exercises**2877 **15.8.3 Exercise 1**

2878 Create a program that uses a **ForEach()** function and an **IsOdd()** function to  
2879 analyze the following list and then print the number of odd numbers it  
2880 contains.

2881 {73, 94, 80, 37, 56, 94, 40, 21, 7, 24, 15, 14, 82, 93, 32, 74, 22, 68, 65, 52, 85, 61, 46, 86, 25}

2882 **15.8.4 Exercise 2**

2883 Create a program that uses a **ForEach()** function and an **IsNegativeNumber()**  
2884 function to copy all of the negative numbers in the following list into a  
2885 new list. Use the variable **negativeNumbers** to hold the new list.

2886 {36, -29, -33, -6, 14, 7, -16, -3, -14, 37, -38, -8, -45, -21, -26, 6, 6, 38, -20, 33, 41, -  
2887 4, 24, 37, 40, 29}

2888 **15.8.5 Exercise 3**

2889 Create a program that uses a **ForEach()** function to analyze the following  
2890 list and then print the following information about it:

- 2891 1) The largest number in the list.  
2892 2) The smallest number in the list.  
2893 3) The sum of all the numbers in the list.

2894 {73, 94, 80, 37, 56, 94, 40, 21, 7, 24, 15, 14, 82, 93, 32, 74, 22, 68, 65, 52, 85, 61, 46, 86, 25}

2895 **15.8.6 Exercise 4**

2896 Create a program that uses a **while loop** to make a list that contains **1000**  
2897 **random integers** between **1** and **100** inclusive. Then, use a **ForEach()**  
2898 function to determine how many integers in the list are **prime** and use an  
2899 **Echo()** function to print this total.

## 2900 **16 Functions & Operators Which Loop Internally**

2901 Looping is such a useful capability that MathPiper has many functions which  
2902 loop internally. Now that you have some experience with loops, you can use this  
2903 experience to help you imagine how these functions use loops to process the  
2904 information that is passed to them.

### 2905 **16.1 Functions & Operators Which Loop Internally To Process Lists**

2906 This section discusses a number of functions that use loops to process lists.

#### 2907 **16.1.1 TableForm()**

```
TableForm(list)
```

2908 The **TableForm()** function prints the contents of a list in the form of a table.  
2909 Each member in the list is printed on its own line and this sometimes makes the  
2910 contents of the list easier to read:

```
2911 In> testList := {2,4,6,8,10,12,14,16,18,20}  
2912 Result> {2,4,6,8,10,12,14,16,18,20}
```

```
2913 In> TableForm(testList)  
2914 Result> True  
2915 Side Effects>  
2916 2  
2917 4  
2918 6  
2919 8  
2920 10  
2921 12  
2922 14  
2923 16  
2924 18  
2925 20
```

#### 2926 **16.1.2 Contains()**

2927 The **Contains()** function searches a list to determine if it contains a given  
2928 expression. If it finds the expression, it returns **True** and if it doesn't find the  
2929 expression, it returns **False**. Here is the calling format for Contains():

```
Contains(list, expression)
```

2930 The following code shows Contains() being used to locate a number in a list:

```
2931 In> Contains({50,51,52,53,54,55,56,57,58,59}, 53)
2932 Result> True
```

```
2933 In> Contains({50,51,52,53,54,55,56,57,58,59}, 75)
2934 Result> False
```

2935 The **Not()** function can also be used with predicate functions like Contains() to  
2936 change their results to the opposite truth value:

```
2937 In> Not Contains({50,51,52,53,54,55,56,57,58,59}, 75)
2938 Result> True
```

### 2939 16.1.3 Find()

```
Find(list, expression)
```

2940 The **Find()** function searches a list for the first occurrence of a given expression.  
2941 If the expression is found, the **position of its first occurrence** is returned and  
2942 if it is not found, **-1** is returned:

```
2943 In> Find({23, 15, 67, 98, 64}, 15)
2944 Result> 2
```

```
2945 In> Find({23, 15, 67, 98, 64}, 8)
2946 Result> -1
```

### 2947 16.1.4 Count()

```
Count(list, expression)
```

2948 **Count()** determines the number of times a given expression occurs in a list:

```
2949 In> testList := {a,b,b,c,c,c,d,d,d,d,e,e,e,e,e}
2950 Result> {a,b,b,c,c,c,d,d,d,d,e,e,e,e,e}
```

```
2951 In> Count(testList, c)
2952 Result> 3
```

```
2953 In> Count(testList, e)
2954 Result> 5
```

```
2955 In> Count(testList, z)
2956 Result> 0
```

2957 **16.1.5 Select()**

```
Select(predicate function, list)
```

2958 **Select()** returns a list that contains all the expressions in a list which make a  
2959 given predicate function return **True**:

```
2960 In> Select("IsPositiveInteger", {46,87,59,-27,11,86,-21,-58,-86,-52})  
2961 Result> {46,87,59,11,86}
```

2962 In this example, notice that the **name** of the predicate function is passed to  
2963 Select() in **double quotes**. There are other ways to pass a predicate function to  
2964 Select() but these are covered in a later section.

2965 Here are some further examples which use the Select() function:

```
2966 In> Select("IsOdd", {16,14,82,92,33,74,99,67,65,52})  
2967 Result> {33,99,67,65}
```

```
2968 In> Select("IsEven", {16,14,82,92,33,74,99,67,65,52})  
2969 Result> {16,14,82,92,74,52}
```

```
2970 In> Select("IsPrime", 1 .. 75)  
2971 Result> {2,3,5,7,11,13,17,19,23,29,31,37,41,43,47,53,59,61,67,71,73}
```

2972 Notice how the third example uses the **..** operator to automatically generate a list  
2973 of consecutive integers from 1 to 75 for the Select() function to analyze.

2974 **16.1.6 The Nth() Function & The [] Operator**

```
Nth(list, index)
```

2975 The **Nth()** function simply returns the expression which is at a given position in  
2976 a list. This example shows the **third** expression in a list being obtained:

```
2977 In> testList := {a,b,c,d,e,f,g}  
2978 Result> {a,b,c,d,e,f,g}
```

```
2979 In> Nth(testList, 3)  
2980 Result> c
```

2981 As discussed earlier, the **[]** operator can also be used to obtain a single  
2982 expression from a list:

```
2983 In> testList[3]
2984 Result> c
```

2985 The **[]** operator can even obtain a single expression directly from a list without  
2986 needing to use a variable:

```
2987 In> {a,b,c,d,e,f,g}[3]
2988 Result> c
```

### 2989 **16.1.7 The : Prepend Operator**

```
expression : list
```

2990 The prepend operator is a colon **:** and it can be used to add an expression to the  
2991 beginning of a list:

```
2992 In> testList := {b,c,d}
2993 Result> {b,c,d}

2994 In> testList := a:testList
2995 Result> {a,b,c,d}
```

### 2996 **16.1.8 Concat()**

```
Concat(list1, list2, ...)
```

2997 The Concat() function is short for "concatenate" which means to join together  
2998 sequentially. It takes two or more lists and joins them together into a single  
2999 larger list:

```
3000 In> Concat({a,b,c}, {1,2,3}, {x,y,z})
3001 Result> {a,b,c,1,2,3,x,y,z}
```

### 3002 **16.1.9 Insert(), Delete(), & Replace()**

```
Insert(list, index, expression)
```

```
Delete(list, index)
```

```
Replace(list, index, expression)
```

3003 **Insert()** inserts an expression into a list at a given index, **Delete()** deletes an  
3004 expression from a list at a given index, and **Replace()** replaces an expression in  
3005 a list at a given index with another expression:

```
3006 In> testList := {a,b,c,d,e,f,g}
3007 Result> {a,b,c,d,e,f,g}

3008 In> testList := Insert(testList, 4, 123)
3009 Result> {a,b,c,123,d,e,f,g}

3010 In> testList := Delete(testList, 4)
3011 Result> {a,b,c,d,e,f,g}

3012 In> testList := Replace(testList, 4, xxx)
3013 Result> {a,b,c,xxx,e,f,g}
```

#### 3014 16.1.10 Take()

```
Take(list, amount)
Take(list, -amount)
Take(list, {begin_index,end_index})
```

3015 **Take()** obtains a sublist from the **beginning** of a list, the **end** of a list, or the  
3016 **middle** of a list. The expressions in the list that are not taken are discarded.

3017 A **positive** integer passed to Take() indicates how many expressions should be  
3018 taken from the **beginning** of a list:

```
3019 In> testList := {a,b,c,d,e,f,g}
3020 Result> {a,b,c,d,e,f,g}

3021 In> Take(testList, 3)
3022 Result> {a,b,c}
```

3023 A **negative** integer passed to Take() indicates how many expressions should be  
3024 taken from the **end** of a list:

```
3025 In> Take(testList, -3)
3026 Result> {e,f,g}
```

3027 Finally, if a **two member list** is passed to Take() it indicates the **range** of  
3028 expressions that should be taken from the **middle** of a list. The **first** value in the  
3029 passed-in list specifies the **beginning** index of the range and the **second** value  
3030 specifies its **end**:

```
3031 In> Take(testList, {3,5})
3032 Result> {c,d,e}
```

3033 **16.1.11 Drop()**

```
Drop(list, index)
Drop(list, -index)
Drop(list, {begin_index,end_index})
```

3034 **Drop()** does the opposite of Take() in that it **drops** expressions from the  
3035 **beginning** of a list, the **end** of a list, or the **middle** of a list and **returns a list**  
3036 **which contains the remaining expressions.**

3037 A **positive** integer passed to Drop() indicates how many expressions should be  
3038 dropped from the **beginning** of a list:

```
3039 In> testList := {a,b,c,d,e,f,g}
3040 Result> {a,b,c,d,e,f,g}
```

```
3041 In> Drop(testList, 3)
3042 Result> {d,e,f,g}
```

3043 A **negative** integer passed to Drop() indicates how many expressions should be  
3044 dropped from the **end** of a list:

```
3045 In> Drop(testList, -3)
3046 Result> {a,b,c,d}
```

3047 Finally, if a **two member list** is passed to Drop() it indicates the **range** of  
3048 expressions that should be dropped from the **middle** of a list. The **first** value in  
3049 the passed-in list specifies the **beginning** index of the range and the **second**  
3050 value specifies its **end**:

```
3051 In> Drop(testList, {3,5})
3052 Result> {a,b,f,g}
```

3053 **16.1.12 FillList()**

```
FillList(expression, length)
```

3054 The FillList() function simply creates a list which is of size "length" and fills it  
3055 with "length" copies of the given expression:

```
3056 In> FillList(a, 5)
3057 Result> {a,a,a,a,a}
```

```
3058 In> FillList(42,8)
3059 Result> {42,42,42,42,42,42,42,42}
```



3060 **16.1.13 RemoveDuplicates()**

```
RemoveDuplicates(list)
```

3061 **RemoveDuplicates()** removes any duplicate expressions that are contained in a  
3062 list:

```
3063 In> testList := {a,a,b,c,c,b,b,a,b,c,c}
```

```
3064 Result> {a,a,b,c,c,b,b,a,b,c,c}
```

```
3065 In> RemoveDuplicates(testList)
```

```
3066 Result> {a,b,c}
```

3067 **16.1.14 Reverse()**

```
Reverse(list)
```

3068 **Reverse()** reverses the order of the expressions in a list:

```
3069 In> testList := {a,b,c,d,e,f,g,h}
```

```
3070 Result> {a,b,c,d,e,f,g,h}
```

```
3071 In> Reverse(testList)
```

```
3072 Result> {h,g,f,e,d,c,b,a}
```

3073 **16.1.15 Partition()**

```
Partition(list, partition_size)
```

3074 The **Partition()** function breaks a list into sublists of size "partition\_size":

```
3075 In> testList := {a,b,c,d,e,f,g,h}
```

```
3076 Result> {a,b,c,d,e,f,g,h}
```

```
3077 In> Partition(testList, 2)
```

```
3078 Result> {{a,b},{c,d},{e,f},{g,h}}
```

3079 If the partition\_size does not divide the length of the list **evenly**, the remaining  
3080 elements are discarded:

```
3081 In> Partition(testList, 3)
```

```
3082 Result> {{h,b,c},{d,e,f}}
```

3083 The number of elements that Partition() will discard can be calculated by  
3084 dividing the length of a list by the partition size and obtaining the **remainder**:

```
3085 In> Length(testList) % 3  
3086 Result> 2
```

3087 Remember that % is the remainder operator. It divides two integers and returns  
3088 their remainder.

### 3089 16.1.16 Table()

```
Table(expression, variable, begin_value, end_value, step_amount)
```

3090 The Table() function creates a list of values by doing the following:

- 3091 1) Generating a sequence of values between a "begin\_value" and an  
3092 "end\_value" with each value being incremented by the "step\_amount".
- 3093 2) Placing each value in the sequence into the specified "variable", one value  
3094 at a time.
- 3095 3) Evaluating the defined "expression" (which contains the defined "variable")  
3096 for each value, one at a time.
- 3097 4) Placing the result of each "expression" evaluation into the result list.

3098 This example generates a list which contains the integers 1 through 10:

```
3099 In> Table(x, x, 1, 10, 1)  
3100 Result> {1,2,3,4,5,6,7,8,9,10}
```

3101 Notice that the expression in this example is simply the variable 'x' itself with no  
3102 other operations performed on it.

3103 The following example is similar to the previous one except that its expression  
3104 multiplies 'x' by 2:

```
3105 In> Table(x*2, x, 1, 10, 1)  
3106 Result> {2,4,6,8,10,12,14,16,18,20}
```

3107 Lists which contain decimal values can also be created by setting the  
3108 "step\_amount" to a decimal:

```
3109 In> Table(x, x, 0, 1, .1)  
3110 Result> {0,0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9,1}
```

3111 **16.1.17 HeapSort()**

```
HeapSort(list, compare)
```

3112 **HeapSort()** sorts the elements of **list** into the order indicated by **compare** with  
3113 **compare** typically being the **less than** operator "<" or the **greater than**  
3114 operator ">":

```
3115 In> HeapSort({4,7,23,53,-2,1}, "<");  
3116 Result: {-2,1,4,7,23,53}
```

```
3117 In> HeapSort({4,7,23,53,-2,1}, ">");  
3118 Result: {53,23,7,4,1,-2}
```

```
3119 In> HeapSort({1/2,3/5,7/8,5/16,3/32}, "<")  
3120 Result: {3/32,5/16,1/2,3/5,7/8}
```

```
3121 In> HeapSort({.5,3/5,.76,5/16,3/32}, "<")  
3122 Result: {3/32,5/16,.5,3/5,.76}
```

3123 **16.2 Functions That Work With Integers**

3124 This section discusses various functions which work with integers. Some of  
3125 these functions also work with non-integer values and their use with non-  
3126 integers is discussed in other sections.

3127 **16.2.1 RandomIntegerVector()**

```
RandomIntegerVector(length, lowest_possible, highest_possible)
```

3128 A vector is a list that does not contain other lists. **RandomIntegerVector()**  
3129 creates a list of size "length" that contains random integers that are no lower  
3130 than "lowest\_possible" and no higher than "highest possible". The following  
3131 example creates **10** random integers between **1** and **99** inclusive:

```
3132 In> RandomIntegerVector(10, 1, 99)  
3133 Result> {73,93,80,37,55,93,40,21,7,24}
```

3134 **16.2.2 Max() & Min()**

```
Max(value1, value2)  
Max(list)
```

3135 If two values are passed to **Max()**, it determines which one is larger:

```
3136 In> Max(10, 20)
```

3137 `Result> 20`

3138 If a list of values are passed to `Max()`, it finds the largest value in the list:

3139 `In> testList := RandomIntegerVector(10, 1, 99)`

3140 `Result> {73,93,80,37,55,93,40,21,7,24}`

3141 `In> Max(testList)`

3142 `Result> 93`

3143 The **Min()** function is the opposite of the `Max()` function.

```
Min(value1, value2)
```

```
Min(list)
```

3144 If two values are passed to `Min()`, it determines which one is smaller:

3145 `In> Min(10, 20)`

3146 `Result> 10`

3147 If a list of values are passed to `Min()`, it finds the smallest value in the list:

3148 `In> testList := RandomIntegerVector(10, 1, 99)`

3149 `Result> {73,93,80,37,55,93,40,21,7,24}`

3150 `In> Min(testList)`

3151 `Result> 7`

### 3152 **16.2.3 Div() & Mod()**

```
Div(dividend, divisor)
```

```
Mod(dividend, divisor)
```

3153 **Div()** stands for "divide" and determines the whole number of times a divisor  
3154 goes into a dividend:

3155 `In> Div(7, 3)`

3156 `Result> 2`

3157 **Mod()** stands for "modulo" and it determines the remainder that results when a  
3158 dividend is divided by a divisor:

3159 `In> Mod(7,3)`

3160 `Result> 1`

3161 The remainder/modulo operator **%** can also be used to calculate a remainder:

```
3162 In> 7 % 2
3163 Result> 1
```

#### 3164 **16.2.4 Gcd()**

```
Gcd(value1, value2)
Gcd(list)
```

3165 GCD stands for Greatest Common Divisor and the **Gcd()** function determines the  
3166 greatest common divisor of the values that are passed to it.

3167 If two integers are passed to Gcd(), it calculates their greatest common divisor:

```
3168 In> Gcd(21, 56)
3169 Result> 7
```

3170 If a list of integers are passed to Gcd(), it finds the greatest common divisor of all  
3171 the integers in the list:

```
3172 In> Gcd({9, 66, 123})
3173 Result> 3
```

#### 3174 **16.2.5 Lcm()**

```
Lcm(value1, value2)
Lcm(list)
```

3175 LCM stands for Least Common Multiple and the **Lcm()** function determines the  
3176 least common multiple of the values that are passed to it.

3177 If two integers are passed to Lcm(), it calculates their least common multiple:

```
3178 In> Lcm(14, 8)
3179 Result> 56
```

3180 If a list of integers are passed to Lcm(), it finds the least common multiple of all  
3181 the integers in the list:

```
3182 In> Lcm({3, 7, 9, 11})
3183 Result> 693
```

3184 **16.2.6 Sum()**

```
Sum(list)
```

3185 **Sum()** can find the sum of a list that is passed to it:

3186 In> testList := RandomIntegerVector(10,1,99)

3187 Result> {73,93,80,37,55,93,40,21,7,24}

3188 In> Sum(testList)

3189 Result> 523

3190 In> testList := 1 .. 10

3191 Result> {1,2,3,4,5,6,7,8,9,10}

3192 In> Sum(testList)

3193 Result> 55

3194 **16.2.7 Product()**

```
Product(list)
```

3195 This function has two calling formats, only one of which is discussed here.

3196 **Product(list)** multiplies all the expressions in a list together and returns their  
3197 product:

3198 In> Product({1,2,3})

3199 Result> 6

3200 **16.3 Exercises**3201 **16.3.1 Exercise 1**

3202 Create a program that uses **RandomIntegerVector()** to create a 100 member  
3203 list that contains random integers between 1 and 5 inclusive. Use **Count()**  
3204 to determine how many of each digit 1-5 are in the list and then print this  
3205 information. Hint: you can use the **HeapSort()** function to sort the  
3206 generated list to make it easier to check if your program is counting  
3207 correctly.

3208 **16.3.2 Exercise 2**

3209 Create a program that uses **RandomIntegerVector()** to create a 100 member  
3210 list that contains random integers between 1 and 50 inclusive and use  
3211 **Contains()** to determine if the number 25 is in the list. Print "25 was in  
3212 the list." if 25 was found in the list and "25 was not in the list." if it

3213 wasn't found.

### 3214 **16.3.3 Exercise 3**

3215 Create a program that uses **RandomIntegerVector()** to create a 100 member  
3216 list that contains random integers between 1 and 50 inclusive and use  
3217 **Find()** to determine if the number 10 is in the list. Print the position of  
3218 10 if it was found in the list and "10 was not in the list." if it wasn't  
3219 found.

### 3220 **16.3.4 Exercise 4**

3221 Create a program that uses **RandomIntegerVector()** to create a 100 member  
3222 list that contains random integers between 0 and 3 inclusive. Use **Select()**  
3223 with the **IsNonZeroInteger()** predicate function to obtain all of the nonzero  
3224 integers in this list.

### 3225 **16.3.5 Exercise 5**

3226 Create a program that uses **Table()** to obtain a list which contains the  
3227 squares of the integers between 1 and 10 inclusive.

## 3228 17 Nested Loops

3229 Now that you have seen how to solve problems with single loops, it is time to  
3230 discuss what can be done when a loop is placed inside of another loop. A loop  
3231 that is placed **inside** of another loop it is called a **nested loop** and this nesting  
3232 can be extended to numerous levels if needed. This means that loop 1 can have  
3233 loop 2 placed inside of it, loop 2 can have loop 3 placed inside of it, loop 3 can  
3234 have loop 4 placed inside of it, and so on.

3235 Nesting loops allows the programmer to accomplish an enormous amount of  
3236 work with very little typing.

### 3237 17.1 Generate All The Combinations That Can Be Entered Into A Two Digit 3238 Wheel Lock Using Two Nested Loops



3239 The following program generates all the combinations that can be entered into a  
3240 two digit wheel lock. It uses a nested loop to accomplish this with the "**inside**"  
3241 nested loop being used to generate **one's place** digits and the "**outside**" loop  
3242 being used to generate **ten's place** digits.

```
3243 %mathpiper
3244 /*
3245  Generate all the combinations can be entered into a two
3246  digit wheel lock.
3247 */
3248 combinations := {};
3249 ForEach(digit1, 0 .. 9) //This loop is called the "outside" loop.
```



```

3250 [
3251   ForEach(digit2, 0 .. 9)//This loop is called the "inside" loop.
3252   [
3253     combinations := Append(combinations, {digit1, digit2});
3254   ];
3255 ];

3256 Echo(TableForm(combinations));

3257 %/mathpiper

3258   %output,preserve="false"
3259   Result: True
3260
3261   Side Effects:
3262   {0,0}
3263   {0,1}
3264   {0,2}
3265   {0,3}
3266   {0,4}
3267   {0,5}
3268   {0,6}
3269   .
3270   . //The middle of the list has not been shown.
3271   .
3272   {9,3}
3273   {9,4}
3274   {9,5}
3275   {9,6}
3276   {9,7}
3277   {9,8}
3278   {9,9}
3279   True
3280 . %/output

```

3281 The relationship between the outside loop and the inside loop is interesting  
 3282 because each time the **outside loop cycles once**, the **inside loop cycles 10**  
 3283 **times**. Study this program carefully because nested loops can be used to solve a  
 3284 wide range of problems and therefore understanding how they work is  
 3285 important.

## 3286 17.2 Exercises

### 3287 17.2.1 Exercise 1

3288 Create a program that will generate all of the combinations that can be  
 3289 entered into a three digit wheel lock. (Hint: a triple nested loop can be  
 3290 used to accomplish this.)

## 3291 18 User Defined Functions

3292 In computer programming, a **function** is a named section of code that can be  
3293 **called** from other sections of code. **Values** can be sent to a function for  
3294 processing as part of the **call** and a function always returns a value as its result.  
3295 A function can also generate side effects when it is called and side effects have  
3296 been covered in earlier sections.

3297 The values that are sent to a function when it is called are called **arguments** or  
3298 **actual parameters** and a function can accept 0 or more of them. These  
3299 arguments are placed within parentheses.

3300 MathPiper has many predefined functions (some of which have been discussed in  
3301 previous sections) but users can create their own functions too. The following  
3302 program creates a function called **addNums()** which takes two numbers as  
3303 arguments, adds them together, and returns their sum back to the calling code  
3304 as a result:

```
3305 In> addNums(num1,num2) := num1 + num2
3306 Result> True
```

3307 This line of code defined a new function called **addNums** and specified that it  
3308 will accept two values when it is called. The **first** value will be placed into the  
3309 variable **num1** and the **second** value will be placed into the variable **num2**.

3310 Variables like num1 and num2 which are used in a function to accept values from  
3311 calling code are called **formal parameters**. **Formal parameter variables** are  
3312 used inside a function to process the **values/actual parameters/arguments**  
3313 that were placed into them by the calling code.

3314 The code on the **right side** of the **assignment operator** is **bound** to the  
3315 function name "**addNums**" and it is executed each time **addNums()** is called.  
3316 The following example shows the new **addNums()** function being called multiple  
3317 times with different values being passed to it:

```
3318 In> addNums(2,3)
3319 Result> 5
```

```
3320 In> addNums(4,5)
3321 Result> 9
```

```
3322 In> addNums(9,1)
3323 Result> 10
```

3324 Notice that, unlike the functions that come with MathPiper, we chose to have this  
3325 function's name start with a **lower case letter**. We could have had addNums()  
3326 begin with an upper case letter but it is a **convention** in MathPiper for **user**

3327 **defined function names to begin with a lower case letter to distinguish**  
3328 **them from the functions that come with MathPiper.**

3329 The values that are returned from user defined functions can also be assigned to  
3330 variables. The following example uses a %mathpiper fold to define a function  
3331 called **evenIntegers()** and then this function is used in the MathPiper console:

```
3332 %mathpiper
3333 evenIntegers(endInteger) :=
3334 [
3335     resultList := {};
3336
3337     x := 2;
3338     While(x <= endInteger)
3339     [
3340         resultList := Append(resultList, x);
3341
3342         x := x + 2;
3343     ];
3344     /*
3345     The result of the last expression which is executed in a function
3346     is the result that the function returns to the caller. In this case,
3347     resultList is purposely being executed last so that its contents are
3348     returned to the caller.
3349     */
3350     resultList;
3351 ];
3352 %/mathpiper
3353
3354 %output,preserve="false"
3355     Result: True
3356 . %/output
3357
3358 In> a := evenIntegers(10)
3359 Result> {2,4,6,8,10}
3360
3361 In> Length(a)
3362 Result> 5
```

3360 The function **evenIntegers()** returns a list which contains all the even integers  
3361 from 2 up through the value that was passed into it. The fold was first executed  
3362 in order to define the **evenIntegers()** function and make it ready for use. The  
3363 **evenIntegers()** function was then called from the MathPiper console and 10  
3364 was passed to it.

3365 After the function was finished executing, it returned a list of even integers as a

3366 result and this result was assigned to the variable 'a'. We then passed the list  
3367 that was assigned to 'a' to the **Length()** function in order to determine its size.

## 3368 **18.1 Global Variables, Local Variables, & Local()**

3369 The new **evenIntegers()** function seems to work well, but there is a problem.  
3370 The variables 'x' and **resultList** were defined inside the function as **global**  
3371 **variables** which means they are accessible from anywhere, including from  
3372 within other functions, within other folds (as shown here):

```
3373 %mathpiper
3374 Echo(x, ",", resultList);
3375 %/mathpiper
3376     %output,preserve="false"
3377     Result: True
3378
3379     Side Effects:
3380     12 , {2,4,6,8,10}
3381 .    %/output
```

3382 and from within the MathPiper console:

```
3383 In> x
3384 Result> 12
3385 In> resultList
3386 Result> {2,4,6,8,10}
```

3387 **Using global variables inside of functions is usually not a good idea**  
3388 because code in other functions and folds might already be using (or will use) the  
3389 same variable names. Global variables which have the same name are the same  
3390 variable. When one section of code changes the value of a given global variable,  
3391 the value is changed everywhere that variable is used and this will eventually  
3392 cause problems.

3393 In order to prevent errors being caused by global variables having the same  
3394 name, a function named **Local()** can be called inside of a function to define what  
3395 are called **local variables**. A **local variable** is only accessible inside the  
3396 function it has been defined in, even if it has the same name as a global variable.  
3397 The following example shows a second version of the **evenIntegers()** function  
3398 which uses **Local()** to make 'x' and **resultList** local variables:

```
3399 %mathpiper
3400 /*
3401  This version of evenIntegers() uses Local() to make
3402  x and resultList local variables
3403  */
3404 evenIntegers(endInteger) :=
3405 [
3406     Local(x,resultList);
3407     resultList := {};
3408
3409     x := 2;
3410
3411     While(x <= endInteger)
3412     [
3413         resultList := Append(resultList, x);
3414         x := x + 2;
3415     ];
3416
3417     /*
3418     The result of the last expression which is executed in a function
3419     is the result that the function returns to the caller. In this case,
3420     resultList is purposely being executed last so that its contents are
3421     returned to the caller.
3422     */
3423     resultList;
3424 ];
3425 %/mathpiper
3426     %output,preserve="false"
3427     Result: True
3428 . %/output
```

3429 We can verify that '**x**' and **resultList** are now local variables by first clearing  
3430 them, calling **evenIntegers()**, and then seeing what '**x**' and **resultList** contain:

```
3431 In> Clear(x, resultList)
3432 Result> True
3433 In> evenIntegers(10)
3434 Result> {2,4,6,8,10}
3435 In> x
3436 Result> x
3437 In> resultList
3438 Result> resultList
```

3439 **18.2 Exercises**3440 **18.2.1 Exercise 1**

3441 Create a function called **tenOddIntegers()** which returns a list which  
3442 contains 10 random odd integers between 1 and 99 inclusive.

3443 **18.2.2 Exercise 2**

3444 Create a function called **convertStringToList(string)** which takes a string  
3445 as a parameter and returns a list which contains all of the characters in  
3446 the string. Here is an example of how the function should work:

3447 In> convertStringToList("Hello friend!")

3448 Result> {"H","e","l","l","o"," ","f","r","i","e","n","d","!"}

3449 In> convertStringToList("Computer Algebra System")

3450 Result> {"C","o","m","p","u","t","e","r"," ","A","l","g","e","b","r","a","  
3451 ","S","y","s","t","e","m"}

## 3452 19 Miscellaneous topics

### 3453 19.1 Incrementing And Decrementing Variables With The ++ And -- 3454 Operators

3455 Up until this point we have been adding 1 to a variable with code in the form of **x**  
3456 **:= x + 1** and subtracting 1 from a variable with code in the form of **x := x - 1**.  
3457 Another name for **adding** 1 to a variable is **incrementing** it and **decrementing**  
3458 a variable means to **subtract** 1 from it. Now that you have had some experience  
3459 with these longer forms, it is time to show you shorter versions of them.

#### 3460 19.1.1 Incrementing Variables With The ++ Operator

3461 The number 1 can be added to a variable by simply placing the ++ operator after  
3462 it like this:

```
3463 In> x := 1  
3464 Result: 1
```

```
3465 In> x++;  
3466 Result: True
```

```
3467 In> x  
3468 Result: 2
```

3469 Here is a program that uses the ++ operator to increment a loop index variable:

```
3470 %mathpiper  
3471 count := 1;  
3472 While(count <= 10)  
3473 [  
3474     Echo(count);  
3475     count++; //The ++ operator increments the count variable.  
3476 ];  
3477  
3478 %/mathpiper  
3479 %output,preserve="false"  
3480 Result: True  
3481  
3482 Side Effects:  
3483 1  
3484 2
```

```
3485      3
3486      4
3487      5
3488      6
3489      7
3490      8
3491      9
3492     10
3493 .    %/output
```

## 3494 19.1.2 Decrementing Variables With The -- Operator

3495 The number 1 can be subtracted from a variable by simply placing the --  
3496 operator after it like this:

```
3497 In> x := 1
3498 Result: 1

3499 In> x--;
3500 Result: True

3501 In> x
3502 Result: 0
```

3503 Here is a program that uses the -- operator to decrement a loop index variable:

```
3504 %mathpiper

3505 count := 10;

3506 While(count >= 1)
3507 [
3508     Echo(count);
3509
3510     count--; //The -- operator decrements the count variable.
3511 ];

3512 %/mathpiper

3513 %output,preserve="false"
3514 Result: True
3515
3516 Side Effects:
3517 10
3518 9
3519 8
3520 7
3521 6
3522 5
```



```
3523         4
3524         3
3525         2
3526         1
3527     .    %/output
```