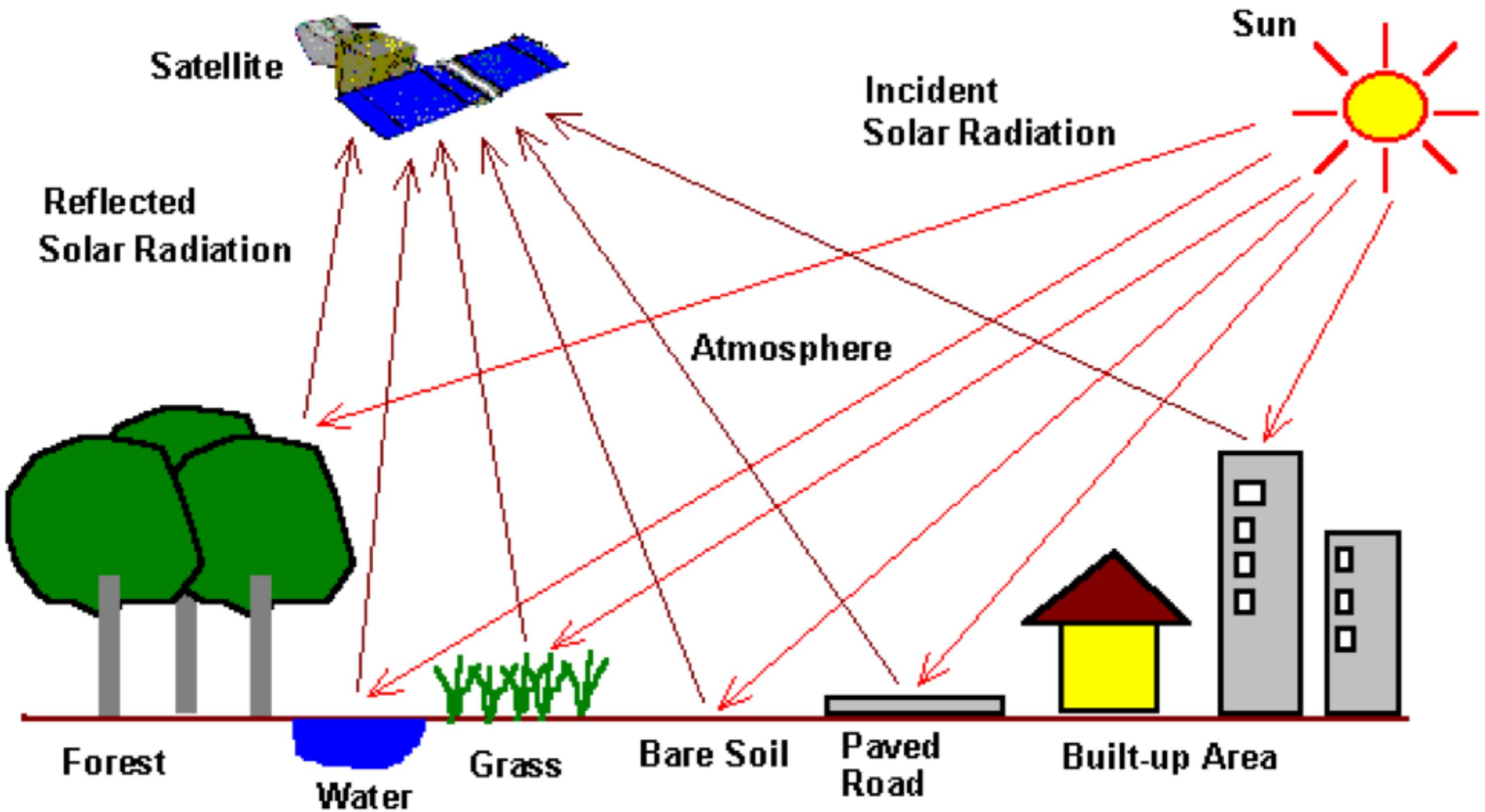


Mid-term review

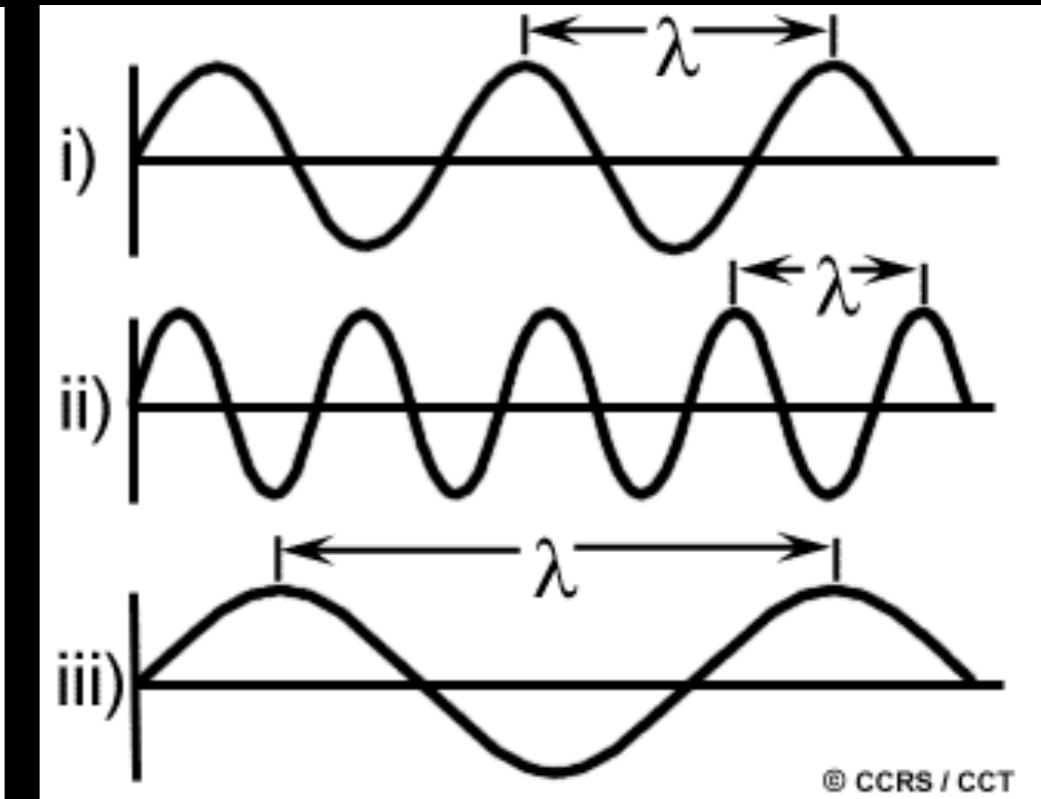
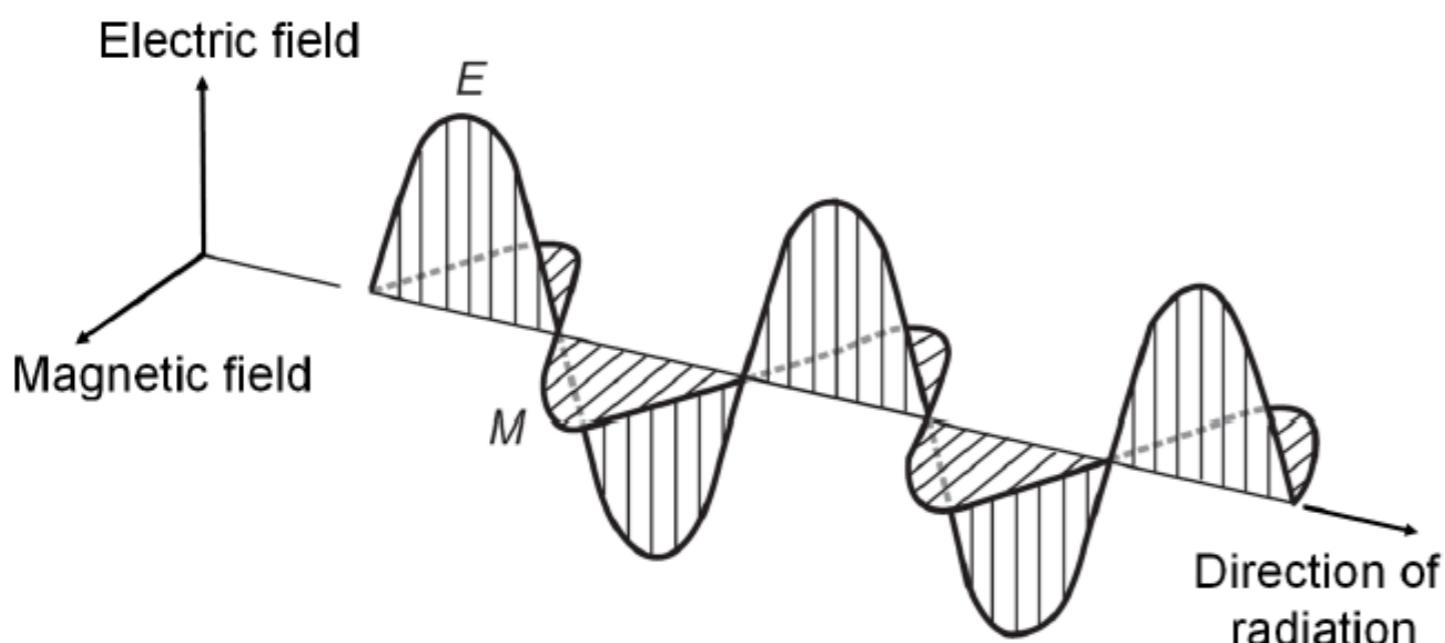
Xi Yang

Department of Environmental Sciences
University of Virginia
xiyang@virginia.edu
390 Clark Hall

The Big Picture



Electromagnetic wave



- **Wavelength (λ):** the distance between successive crests of a wave
- Frequency (v) = c/λ .
- $Q = hc/\lambda = hv$. Q is in joule, h is Planck's constant.

Basic concepts

- Radiant Energy (Q , unit: joule): the total energy radiated toward a surface.
- Radiant Flux ($\Phi = \delta Q / \delta t$, unit: joule/s=watt): the energy per unit of time
- Irradiance ($E = \delta \Phi / \delta A$, unit: w/m^2): the radiant flux arriving on a surface per unit area
- Exitance or Emittance (M , w/m^2): the radiant flux *leaving* a surface
- Radiance (L , unit: $\text{w m}^{-2} \text{ sr}^{-1}$): the total energy exiting in a certain direction per unit area per solid angle of measurement.
- Spectral Irradiance ($E = \delta \Phi / \delta A / \delta \lambda$, unit: $\text{w/m}^2/\text{nm}$): the radiant flux arriving on a surface per unit area per unit wavelength.
- Spectral Radiance (L , unit: $\text{w m}^{-2} \text{ sr}^{-1} \text{ nm}^{-1}$): the total energy exiting in a certain direction per unit area per solid angle of measurement per unit wavelength.

EMR wavelengths

- **Visible** (400 nm-700nm). Red: 620-700 nm; Green: 500-578 nm; Blue: 446-500 nm.
- **Infrared** (0.7 um-100um). NIR: 0.7 - 1.4 um; SWIR: 1.4-3 um (and beyond); TIR: 8 -14 um;
- **Microwave** (1 mm - 1 m).
- Solar spectrum: what is its wavelength range?

EM laws

- Planck's law of radiation: the spectral distribution of the emittance of a blackbody is a function of its temperature and wavelength.

$$M(\lambda) = \frac{c_1}{\lambda^5 (e^{(c_2/\lambda T)} - 1)} = f(\lambda, T)$$

$c_1 = 3.741 \times 10^8 \text{ W m}^{-2} \text{ um}^{-1};$
 $c_2 = 1.438 \times 10^4 \text{ um K}$

- Stefan-Boltzmann law:

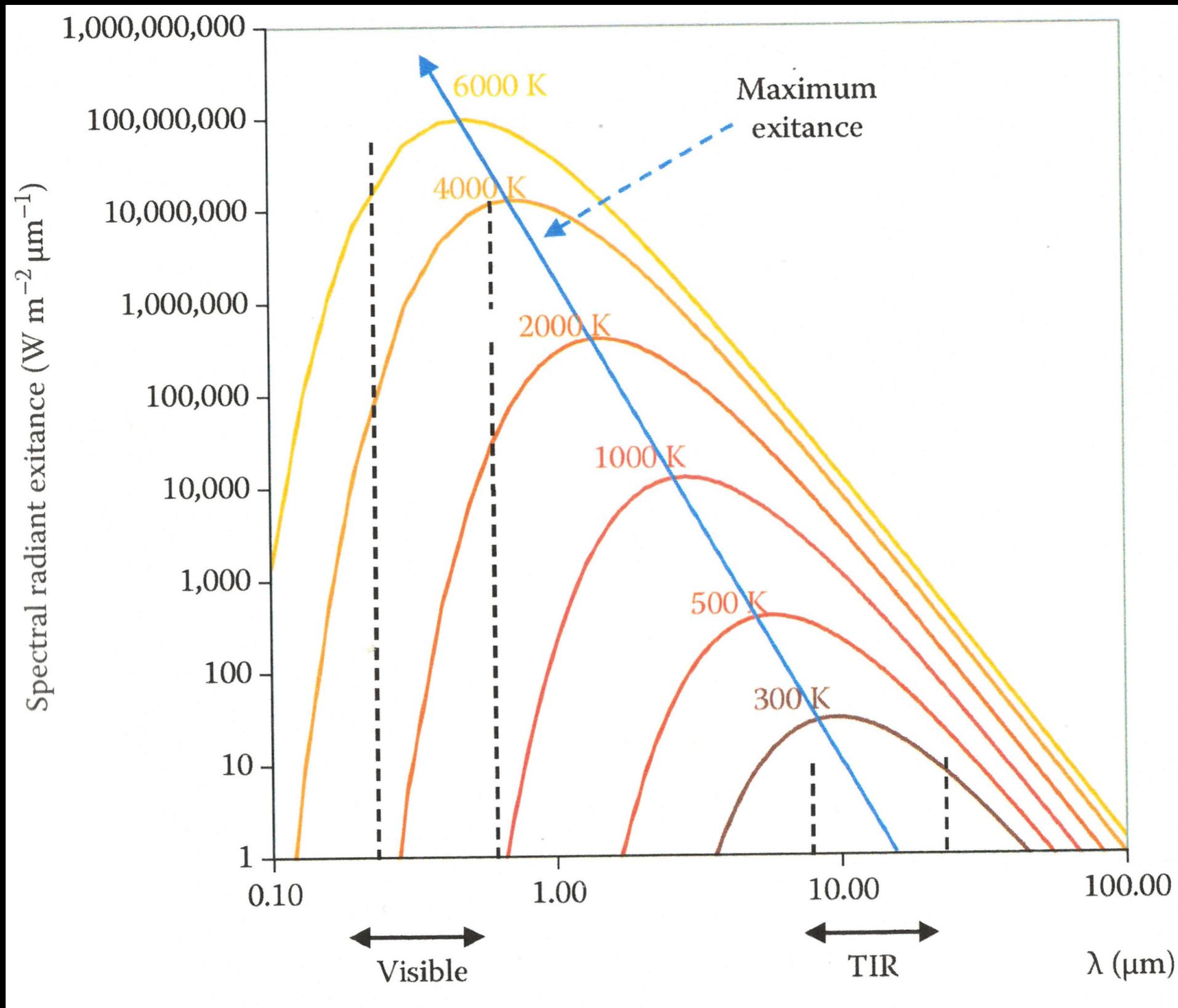
$$M = \sigma T^4 \quad \sigma = 5.6697 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

- An application of Kirchhoff's law:

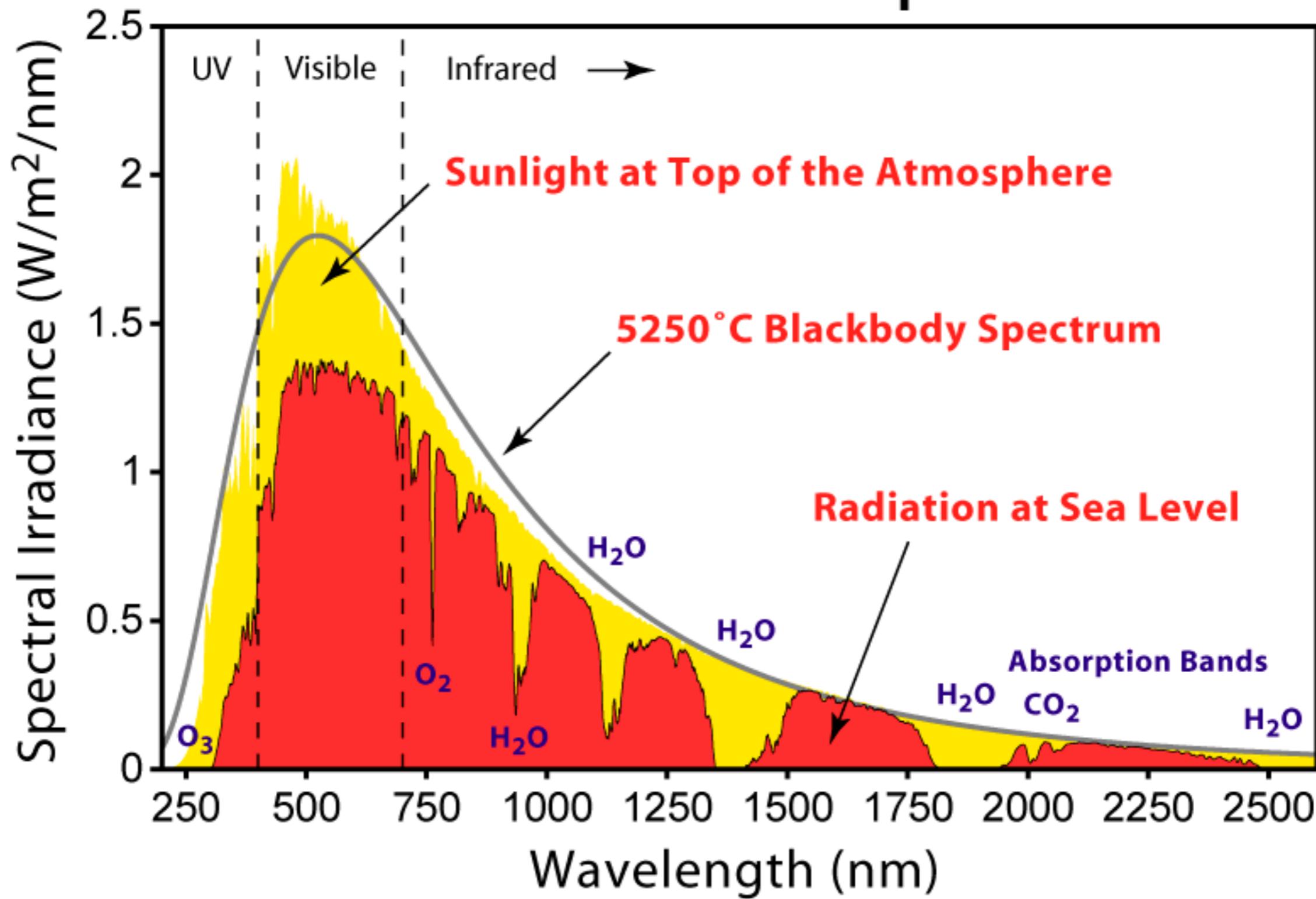
$$M = \epsilon \sigma T^4 \quad \epsilon = 0.1$$
$$\sigma = 5.6697 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$$

- Wien's Displacement Law: $\lambda_{\max} = \frac{2898}{T}$

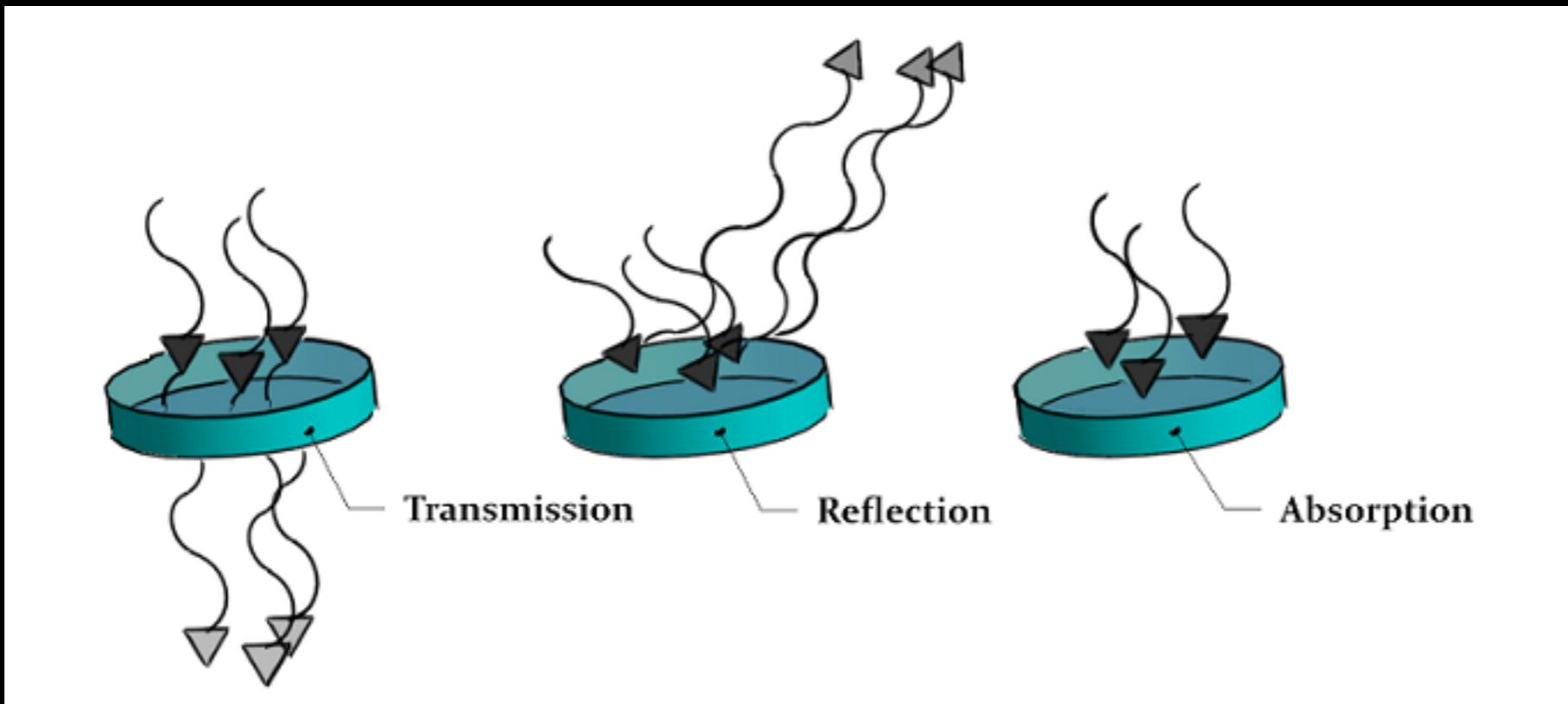
EM laws



Solar Radiation Spectrum



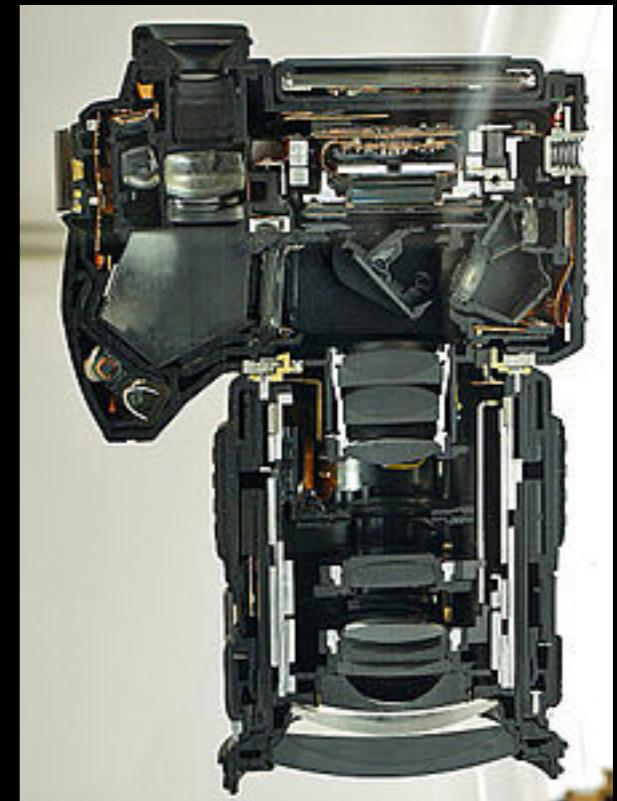
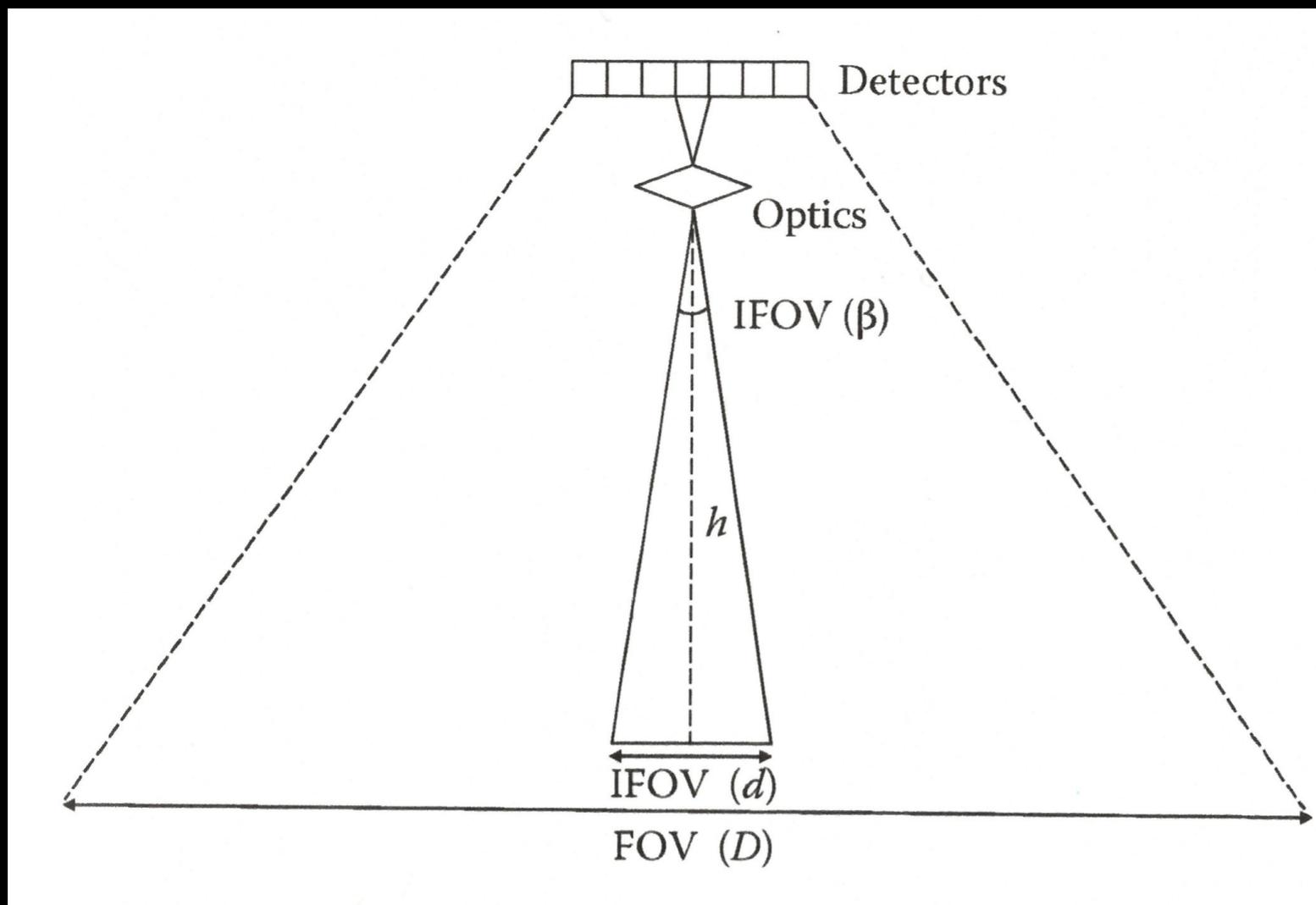
Reflectance



Incoming radiation = Transmission + Reflection + Absorption

$$I = Transmittance + Reflectance + Absorbance$$

Spatial resolution



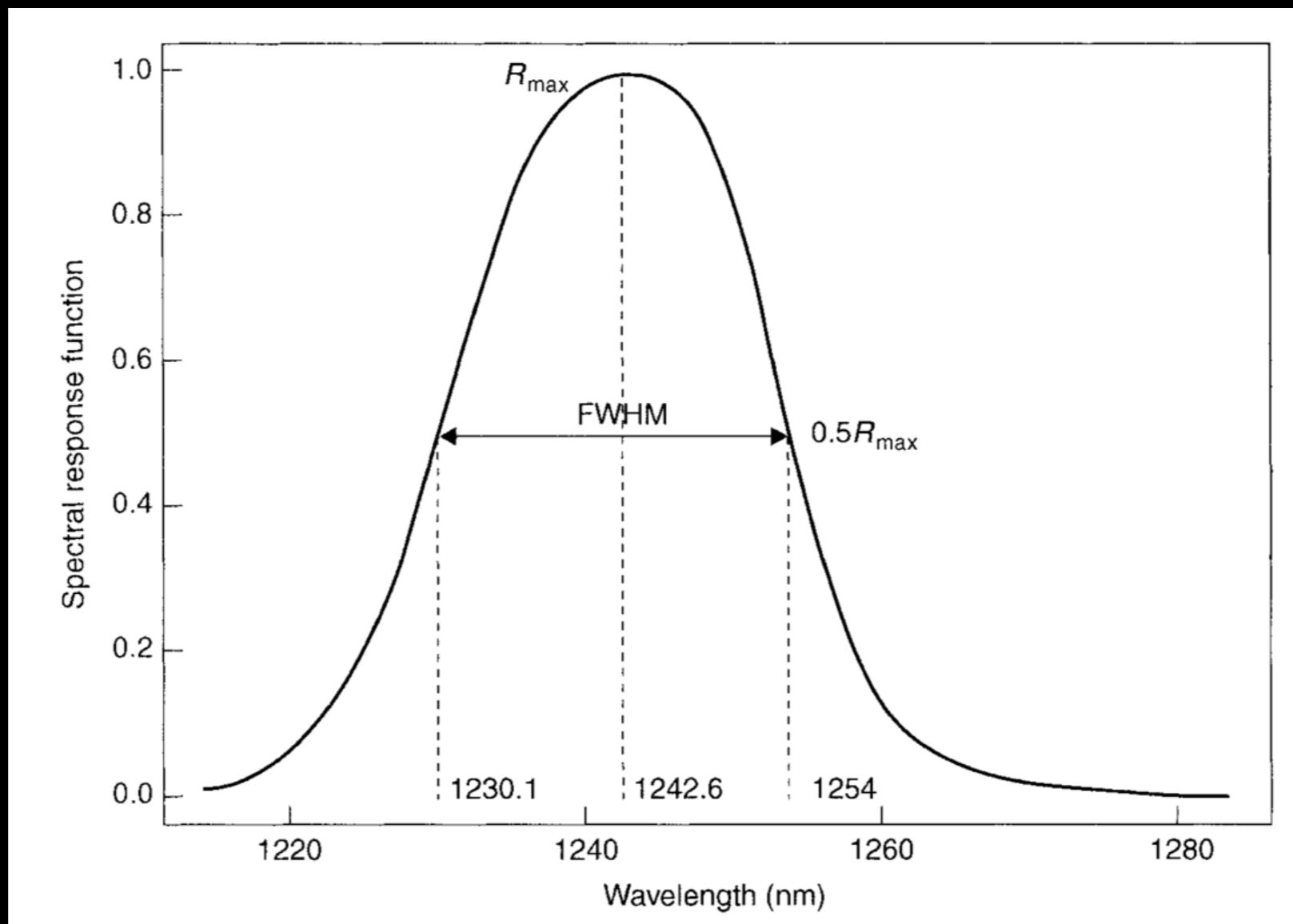
- Field-of-View (FOV)
- Instant Field of View (IFOV) - radian/meter
- Spatial resolution: pixel size small/large (high/low; fine/coarse)

Three resolutions (II) - temporal resolution

- Temporal resolution is observing frequency.
- The temporal resolution of a satellite product depends on the satellite orbit:
 - Geostationary - low inclination, high altitude
 - Polar-orbiting - high inclination, low altitude
 - Sun-synchronous (one type of polar-orbiting)
 - Non-sun-synchronous - medium inclination, low altitude

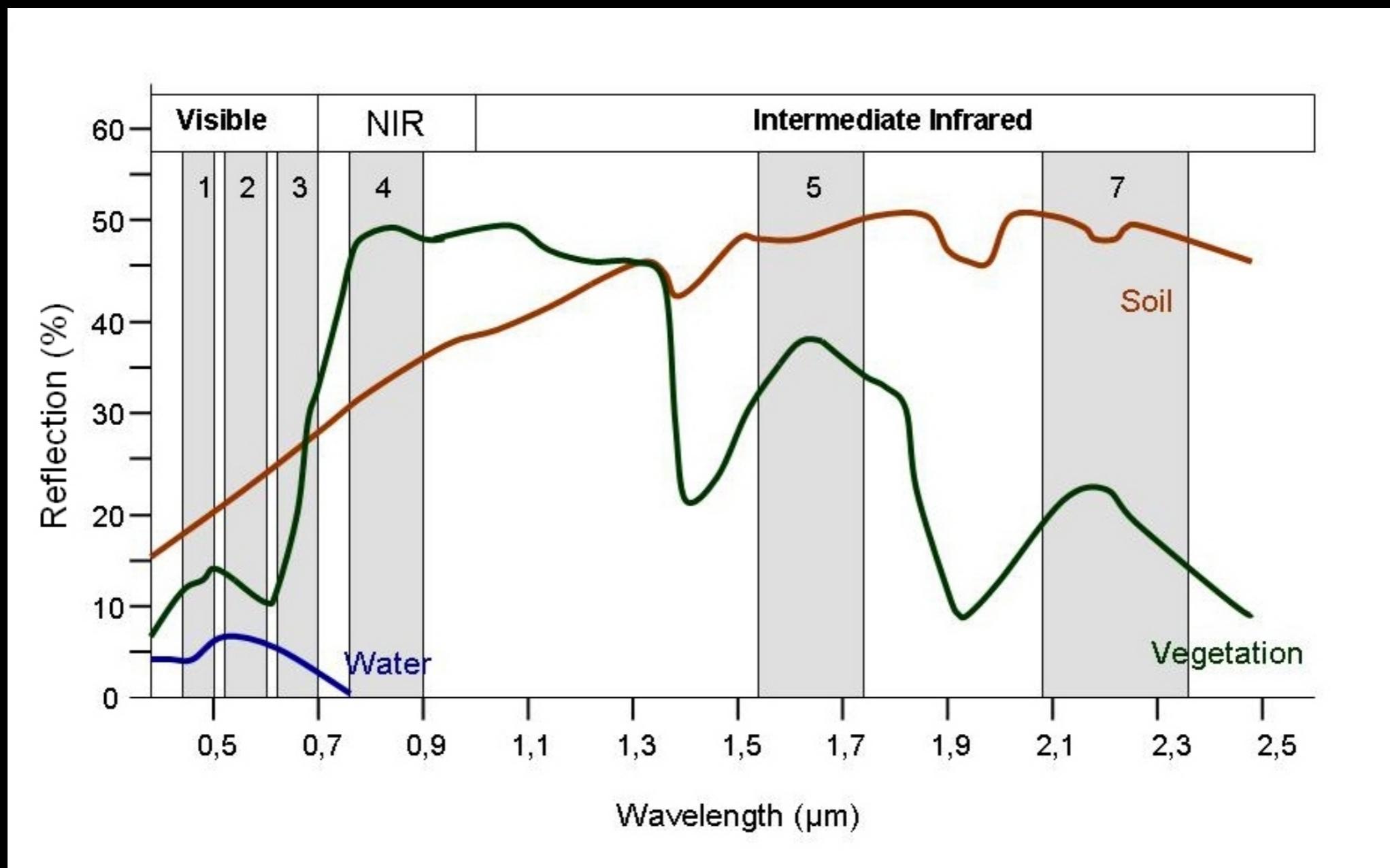
Three resolutions (III) - spectral resolution

- Spectral resolution refers to the ability to differentiate two lines in the spectrum. It is often described as the Full-Width-at-Half-Maximum (FWHM).



Spectral Bands

- A band refers to a spectral region on the EMR. Satellites are designed to collect spectral radiance of specific wavelengths.



Spatial resolution of TM, ETM+, and OLI

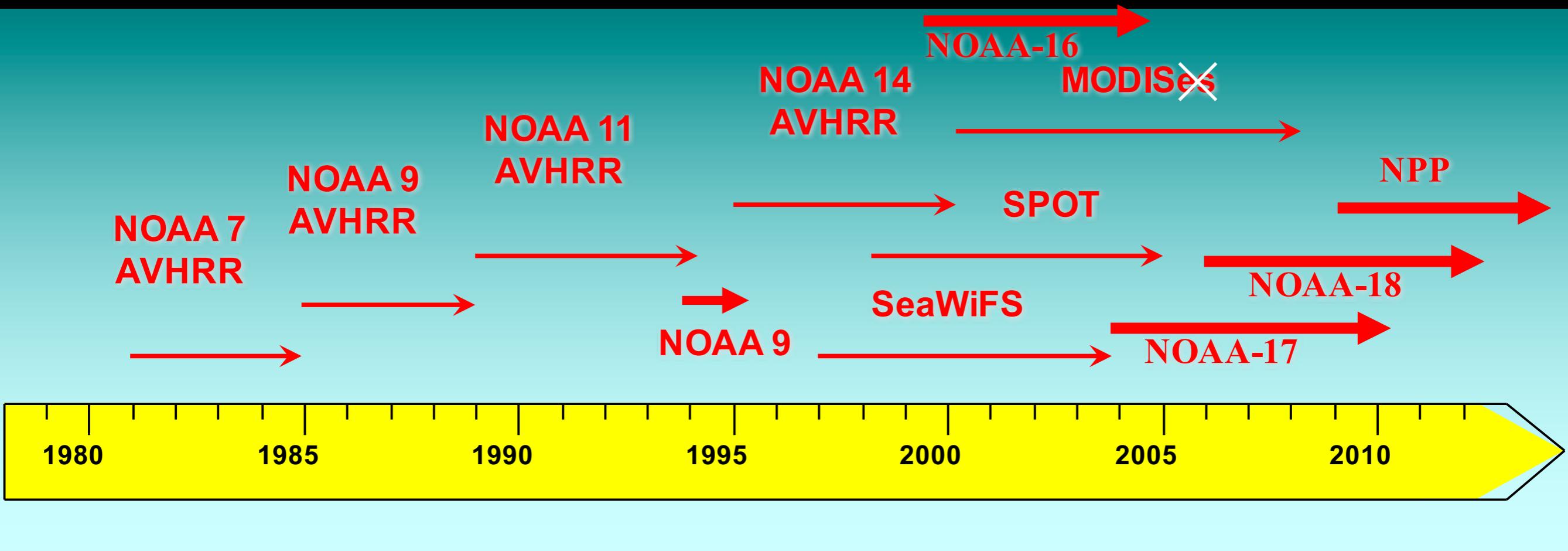
Satellite	Sensor	Swath	Bits	VNIR	SWIR	TIR
L8	OLI	185km	12	30m 30m 15m	30m 30m	30m 30m
	TIRS					100m 100m
Landsat 7	ETM+	185km	8	30m 30m 30m 15m	30m 30m	60m
Landsat 4 & 5	MSS	185km	8	82m 82m 82m	82m	
	TM	185km	8	30m 30m 30m	30m 30m 30m	120m
Landsat 1-2	RBV	183km		80m 80m 80m		
Landsat 3	RBV	183km		40m		
Landsat 1-3	MSS	183km	8	79m 79m 79m 79m		240m (L3 Only)

- VNIR + SWIR: 80m -> 30m;
- TIR: 240m -> 120m -> 60m -> 100m;
- Panchromatic: 15m



NOAA/AVHRR & MODIS

New Era for Global Monitoring



- AVHRR: Advanced Very High Resolution Radiometer
- MODIS: MODerate resolution Imaging Spectrometer

Radiometric calibration (II) - Radiance

$$L_\lambda = \left(\frac{\text{LMAX}_\lambda - \text{LMIN}_\lambda}{Q_{\text{cal max}}} \right) Q_{\text{cal}} + \text{LMIN}_\lambda$$

Spectral Radiances, LMIN_λ and LMAX_λ in $\text{W}/(\text{m}^2 \cdot \text{sr} \cdot \mu\text{m})$									
Processing Date	From March 1, 1984				After May 5, 2003				
	To May 4, 2003								
Band	LMIN_λ	LMAX_λ	G_{rescale}	B_{rescale}	LMIN_λ	LMAX_λ	G_{rescale}	B_{rescale}	
1	-1.52	152.10	0.602431	-1.52	-1.52	193.0	0.762824	-1.52	
2	-2.84	296.81	1.175100	-2.84	-2.84	365.0	1.442510	-2.84	
3	-1.17	204.30	0.805765	-1.17	-1.17	264.0	1.039880	-1.17	
4	-1.51	206.20	0.814549	-1.51	-1.51	221.0	0.872588	-1.51	
5	-0.37	27.19	0.108078	-0.37	-0.37	30.2	0.119882	-0.37	
6	1.2378	15.303	0.055158	1.2378	1.2378	15.303	0.055158	1.2378	
7	-0.15	14.38	0.056980	-0.15	-0.15	16.5	0.065294	-0.15	

Three types of scattering in the atmosphere

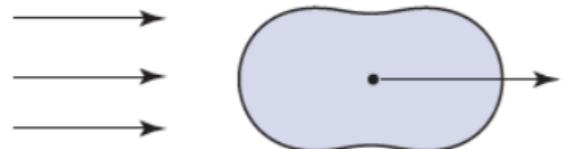
- Rayleigh Scattering
- Mie Scattering
- Non-selective Scattering

Rayleigh and Mie scattering

$$x = \frac{2\pi r}{\lambda}$$

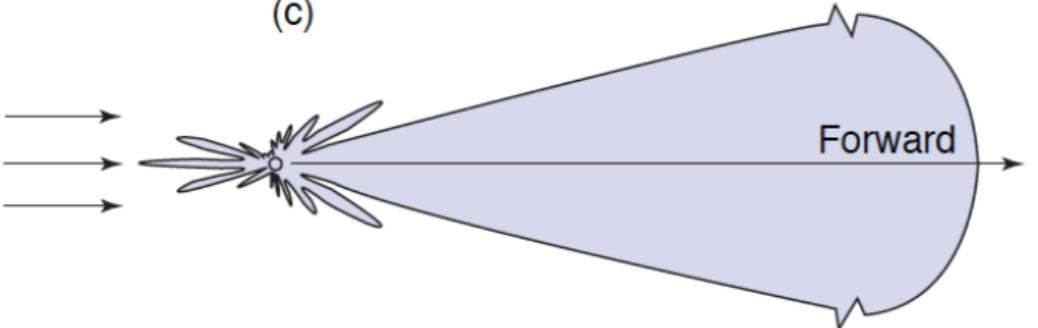
Rayleigh scattering

Incident Beam

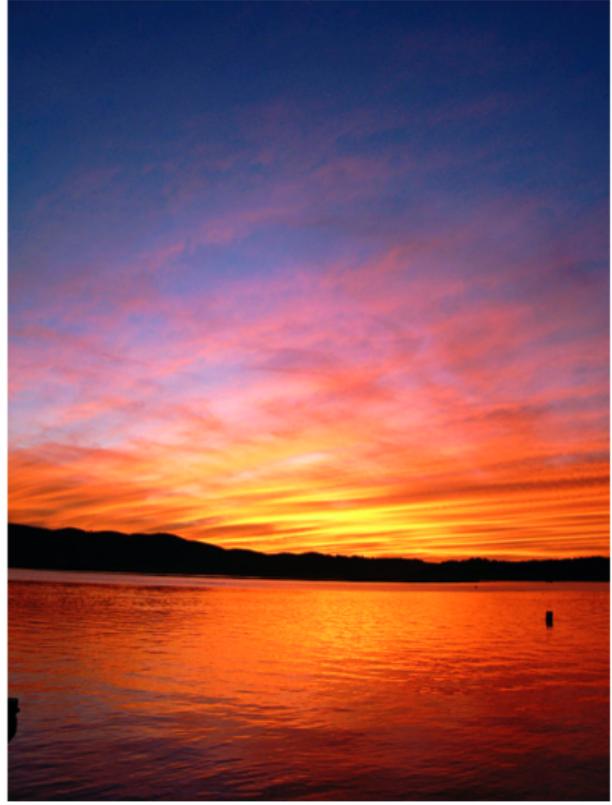

$$K_\lambda \propto \lambda^{-4}$$

Mie scattering

(c)



Forward



Beer-lambert law

$$I_{\lambda z_0} = I_{\lambda \infty} e^{-\sec \theta \int_{z_0}^{\infty} k_{\lambda} \rho r dz} = I_{\lambda \infty} e^{-\tau_A \sec \theta}$$

$$\tau_{\lambda} = \int_{z_0}^{\infty} k_{\lambda} \rho r dz$$

Radiative Transfer in the Atmosphere

Case I: No atmosphere

$$L_{sat} = \frac{\rho E_o \cos \theta_s}{\pi}$$

L_{sat} : radiance at sensor
 E_o : TOA solar irradiance
 ρ : surface reflectance
 θ : solar zenith angle

Case 2: Atmosphere attenuation

$$L_{sat} = \frac{\rho T_\phi [T_\theta E_o \cos \theta_s + E_D]}{\pi} + L_{path}$$

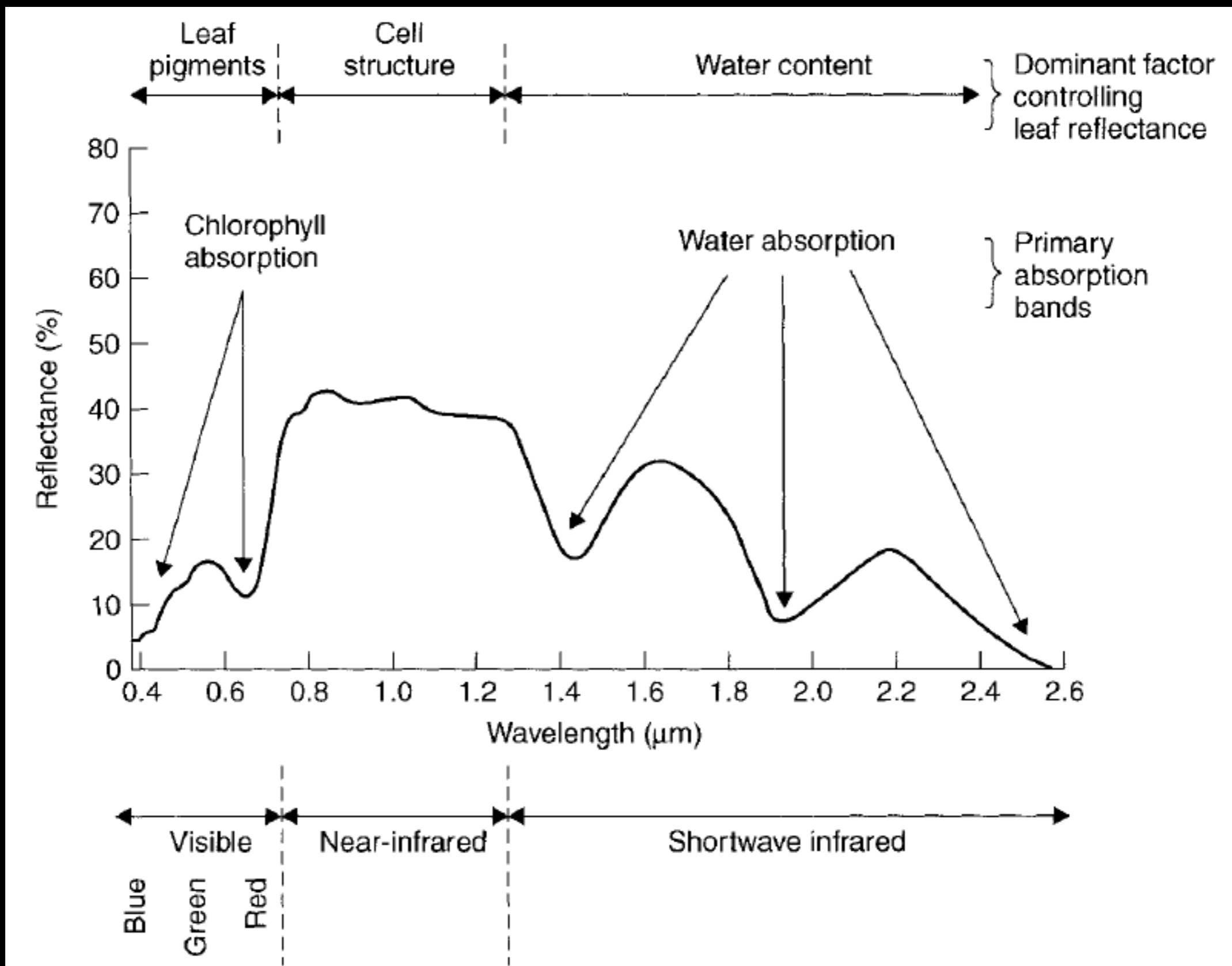
T_θ : Transmission of the atmosphere from TOA to the surface

T_ϕ : Transmission of the atmosphere from the surface to TOA

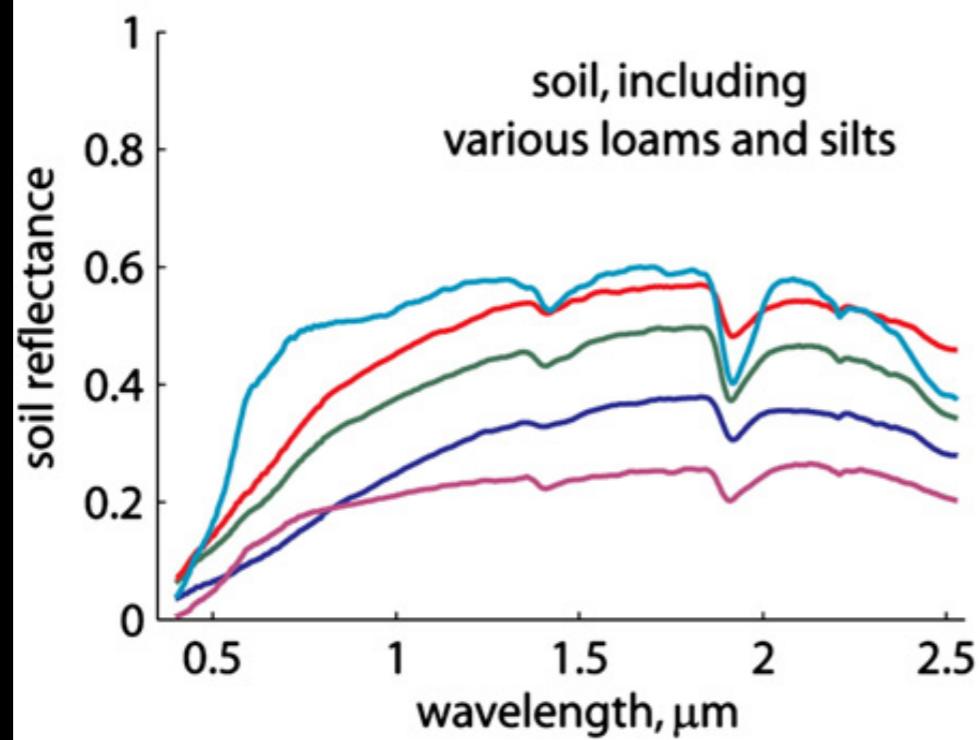
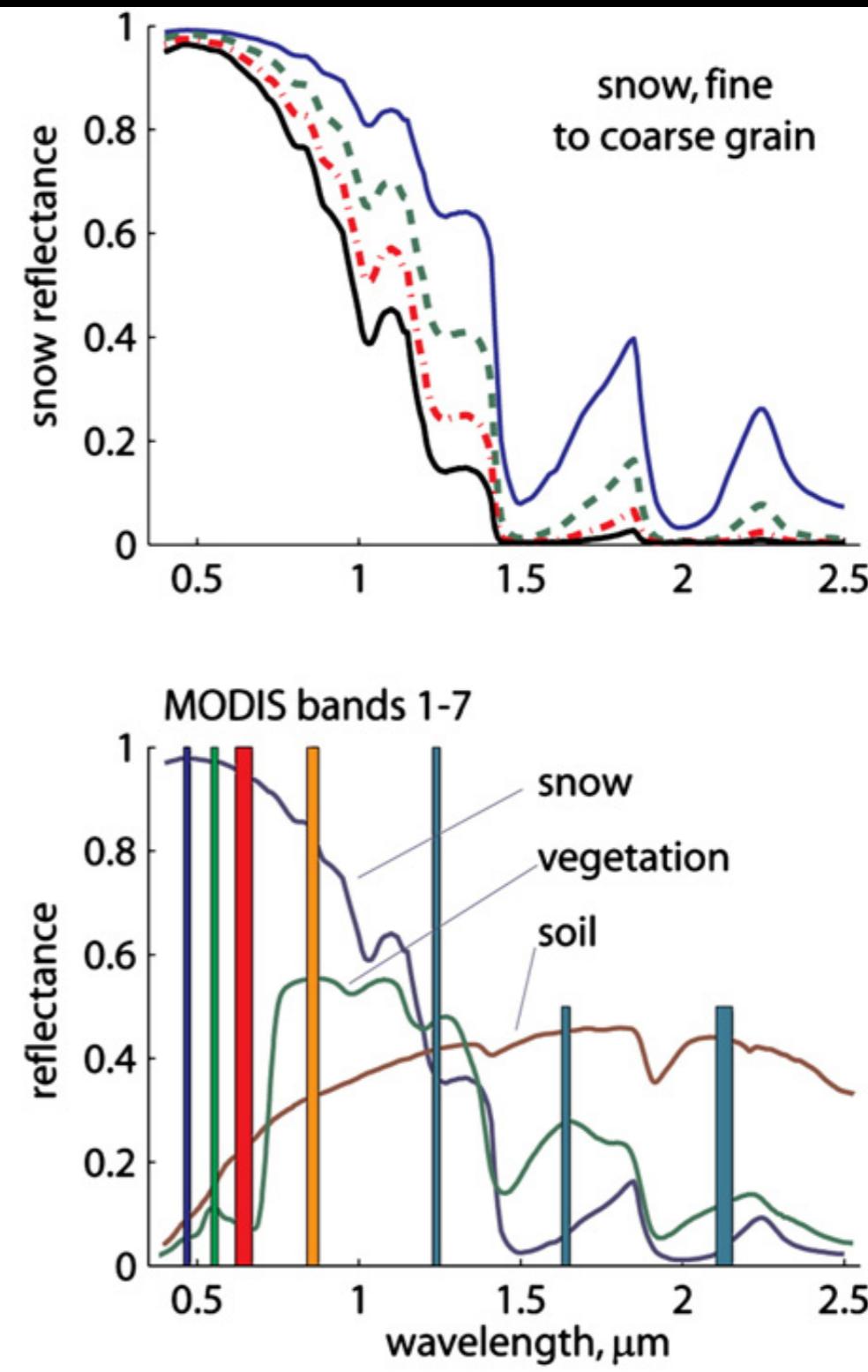
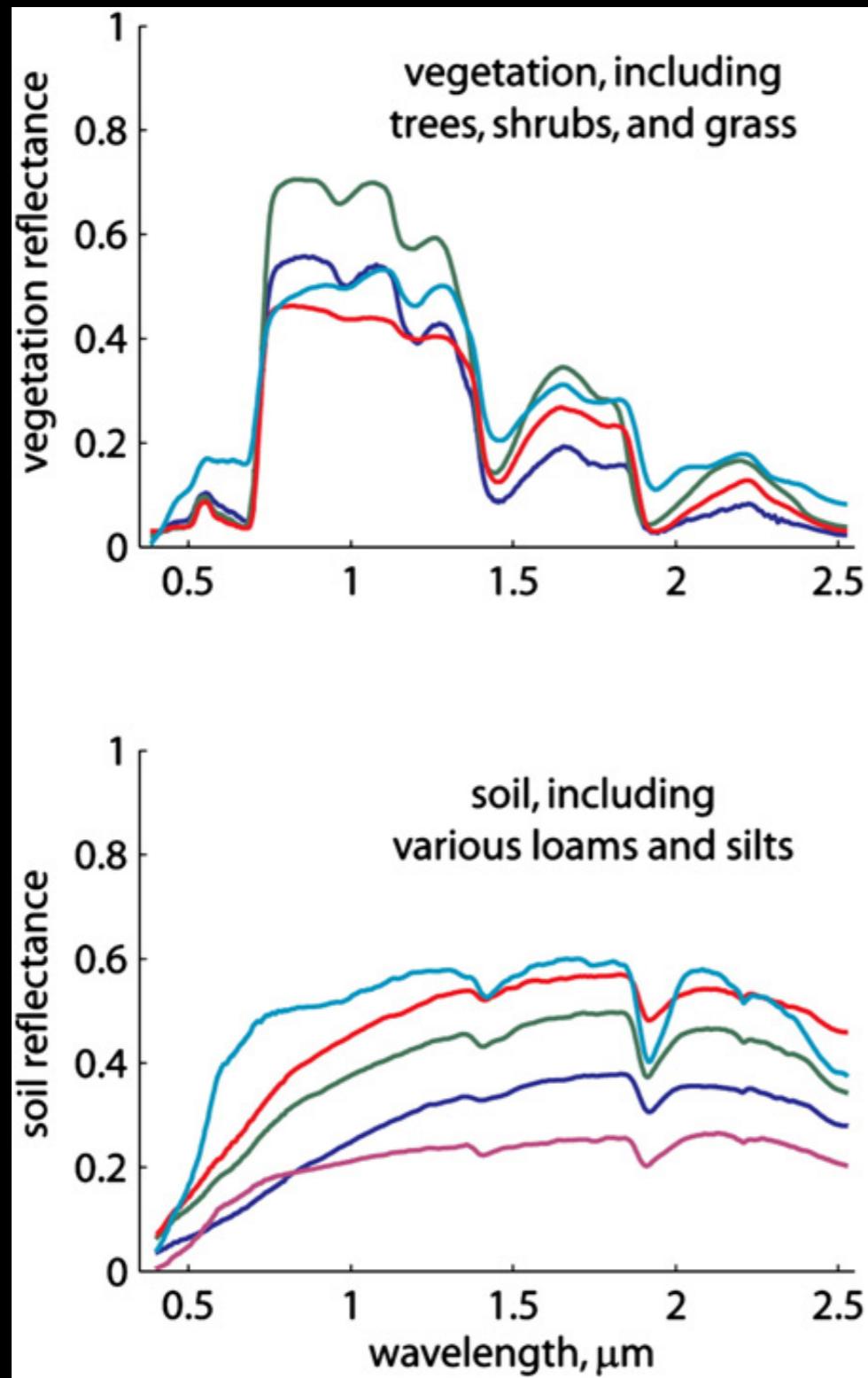
E_D : Downwelling scattered irradiance

L_{path} : Path irradiance

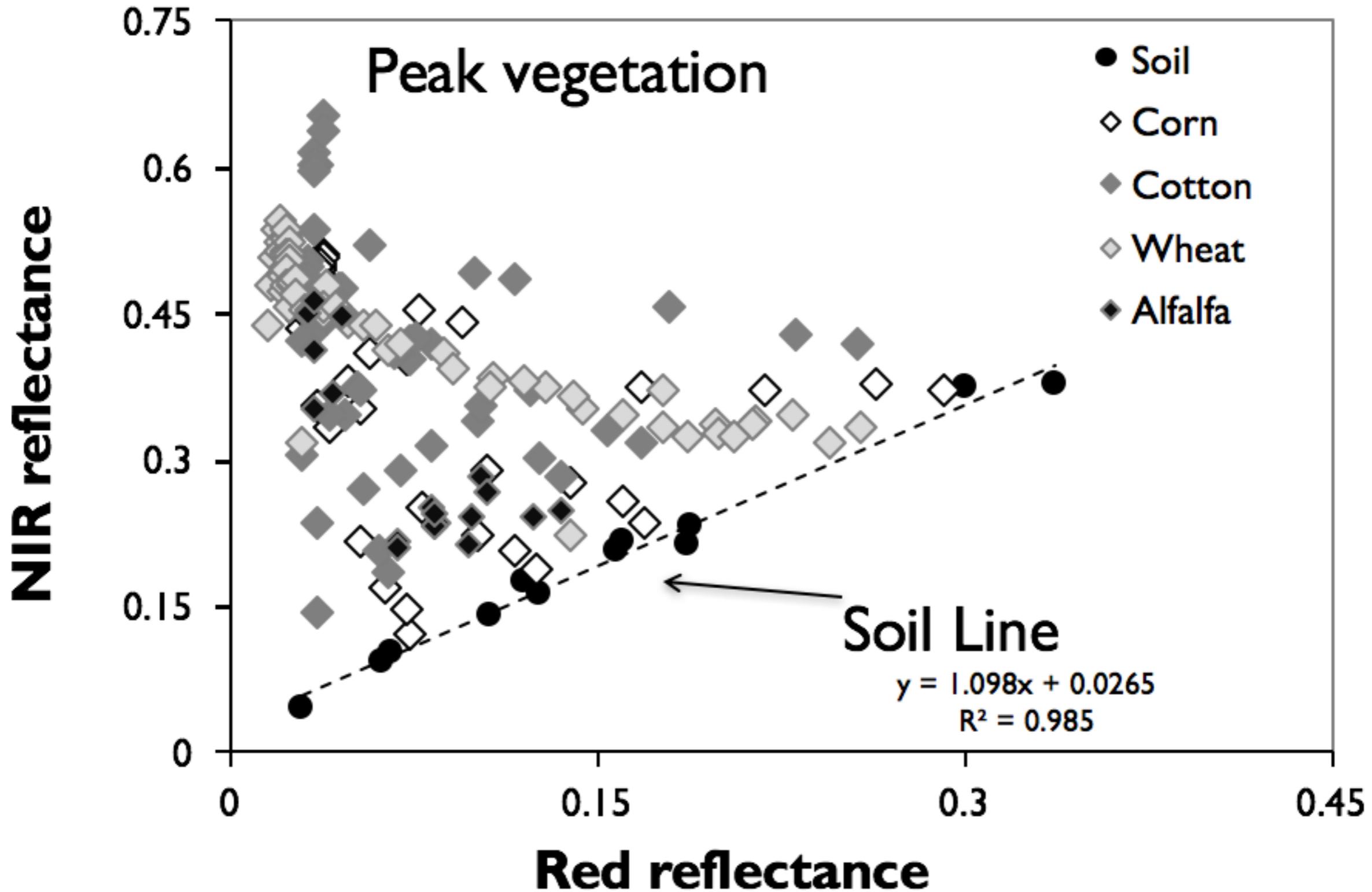
Leaf spectra



Identify spectra



Soil line



Vegetation indices

- Simple Ratio (SR): $SR = NIR/R;$
- Normalized Difference Vegetation Index (NDVI): $NDVI = (NIR-R)/(NIR+R);$
- Enhanced Vegetation Index:

$$EVI = 2.5 \frac{NIR - R}{NIR + 6R - 7.5B + 1}$$

Spectral Mixture Analysis

- Basic assumption: the reflectance of a pixel is a linear combination of the endmember spectra times their relative cover fraction.
- Two parts to the algorithm:

$$\sum_{i=1}^N F_i = F_1 + F_2 + \dots + F_N = 1$$

Sum to 100%: endmembers must collectively “explain” the pixel

$$\rho_\lambda = F_1 \rho_{\lambda,1} + F_2 \rho_{\lambda,2} + \dots + F_N \rho_{\lambda,N} + E_\lambda$$

Best-fit fractions (and error) are calculated for each DN value for each band of each pixel

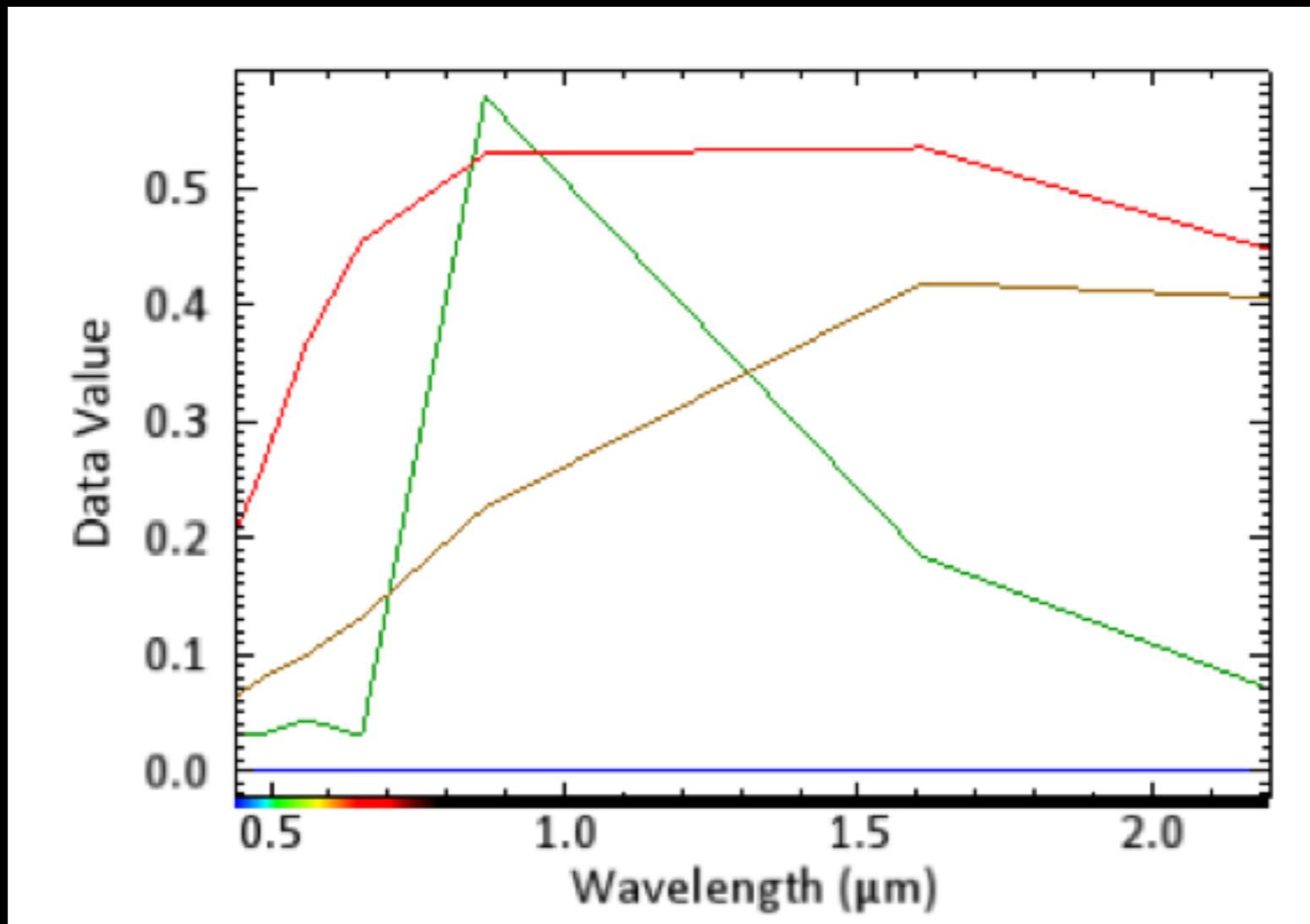
F_i =fraction of endmember i in pixel (usually $0 \leq F_i \leq 1$)

ρ_λ =the pixel reflectance for band λ

$\rho_{\lambda,i}$ =the reflectance for band λ of endmember i

E_λ =error term for band λ

Choosing Endmembers



- Represents a major land cover in the image
- Spectrally distinct

Land cover classification

Supervised classification assumes knowledge of some parts of the study area (“training fields”) is acquired by external sources or fieldwork.

The accuracy of supervised classification depends on the quality of these “training fields”.

Unsupervised classification identifies spectral classes in the image by finding clusters of pixels with similar pixel values.

Classification accuracy

- Ground truth: from geolocated field observations; aerial survey; other data sources.
- Two types of errors:
 - Omission Error (“false negative”, OE): the number of unassigned pixels / total number of pixels in that category.
 - Commission Errors (“false positive”, CE): pixels that are included in a given category when they are not in fact part of that category.
- Two types of accuracies:
 - Producer Accuracy (PA): $1 - OE$
 - User Accuracy (UA): $1 - CE$.

Confusion Matrix

Classification	Reference									User's Accuracy	Commission Error
	1	2	4	5	6	7	9	A	B		
1	927	49	63		42		5	87		1173	79
2		35									
4			6								
5											
6				11							
7											
9							99				
A								70			
B											
Total				1148							
Producer's Accuracy					80.7						
Omission Error						19.3					

$$OE_i = \frac{X_{+i} - X_{ii}}{X_{+i}}$$

$$PA_i = \frac{X_{ii}}{X_{+i}}$$

$$CE_i = \frac{X_{i+} - X_{ii}}{X_{i+}}$$

$$UA_{u,j} = \frac{X_{ii}}{X_{i+}}$$

Overall Accuracy (OA):

$$\widehat{OA} = \frac{\sum_{i=1,n} X_{ii}}{\sum_{i=1,n} \sum_{j=1,n} X_{ij}}$$