Responses to Reviewers

We would like to express our gratitude to the editor and reviewers for their useful suggestions and remarks on the manuscript.

The rest of this document will address specific concerns raised by the editor and reviewers.

Responses to Reviewer 5

• Reviewer 5 wrote:

"At the end of the Introduction, I would like to see a stronger and clearer statement of (what the authors see as) the main contributions of the paper. This should in essence answer the questions Why is this work important? Why does it merit publication in EJOR?"

• Reviewer 5 wrote:

"Now that (as it seems to me) Section 4 is the centrepiece of the work, the material here needs improvement. The proofs of Theorem 1 and Proposition 1 need some serious work to make them mathematically compelling."

• Reviewer 5 wrote:

"Reading the proof of Theorem 1, it is not at all clear to me that you have proved the statement in the result. For a start, the statement is if and only if and it is not at all clear to me that you have the implication going both ways. There is no mention of strongly connected components in the proof and yet that is a key property of a knot. I want to be able to see absolutely clearly that you can start from Suppose a deadlock state arises at t and from there infer that D(t) must contain a knot and then repeat with the implications reversed."

• Reviewer 5 wrote:

"So far as Proposition 1 is concerned, I assume that (starting from Theorem 1) the claim is that in the three examples of queueing networks listed the statements D(t) contains a knot and D(t) contains a weakly connected component without a sink node are equivalent (ie, are if and only if). Is that what you have proved? Please make it much clearer. As with Theorem 1, in the proofs the implications appear to go only one way, which is a concern. One further point, please explain the value of Proposition 1. Is it easier to check that D(t) has a weakly component without a sink node than that it contains a knot? Do you use Proposition 1 in any of your own analyses?"

• Reviewer 5 wrote:

"p.1 Abstract: These models are compared to results obtained I do not think this is quite what you mean;"

• Reviewer 5 wrote:

"p.1 Last four lines of the first para of Section 1. Please reword from These deadlocks can be real..... to achieve greater clarity;"

• Reviewer 5 wrote:

"p.2 Definition 1 and material following. Please aim for greater clarity here. If you relate Figure 1 to Definition 1, what exactly is the subset of customers in the latter which is relevant here? Is it just Asub1 and Bsub1?"

• Reviewer 5 wrote:

"p.3 bottom para to the end of Section 2. Please try to reword for clarity. This discussion could be clearer on the distinction between real-world deadlock and the model-based variety. It should also explain more clearly why the latter (which is the focus of the paper) matters;"

• Reviewer 5 wrote:

"pp4-6 The literature review is very long. If it is possible to lose some of the material toward the end of Section 3, that might help readability;"

• Reviewer 5 wrote:

"p.7 l.3 up In the definition of weakly connected does the either/or include both and? In other words, is a strongly connected vertex pair necessarily weakly connected?"

• Reviewer 5 wrote:

"p.10, l.2 up Should it not beto check whether any strongly connected component...."

• Reviewer 5 wrote:

"p.11, l.11 You claim In this section......expressions for their expected time to deadlock are found. What are you referring to here? I do not see any expressions unless you are claiming (5.1) meets this description."

• Reviewer 5 wrote:

"p.11, l.3up In (5.1) you give a formula for the expected number of time steps until absorption for a (discrete) Markov chain. Will you not need to uniformise your continuous chains to translate this easily into the expected time to deadlock? If so, should this be mentioned? How exactly did you compute the analytical mean times to deadlock in Figure 8 etc?"

• Reviewer 5 wrote:

"p.15, l.9the rate at which i are (is?) reduced for most states....Please explain. What does this mean?"

• Reviewer 5 wrote:

"p.15 Are Remarks 1 and 2 mathematical certainties or empirical observations? If the former, can they be proved rigorously?"

• Reviewer 5 wrote:

"p.16, l.3 I think possibilities should be probabilities here;"

• Reviewer 5 wrote:

"p.16, bottom In your description of state space S, the index applied to N should be 2 rather than the one given. The space S consists of pairs of integers. A similar comment applies

on p.19. Also please rewrite the material following the characterisation of S, some of which seems confusing and contradictory;"

• Reviewer 5 wrote:

"p.18 (and later). Having commented extensively on the analytical/simulation results given in Figure 8, you say very little about the Figures 11 and 14."