Queueing Networks for a Healthcare System Deadlocking, Reinforcement Learning & Workforce Planning

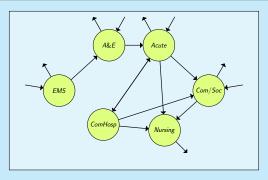
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EURO 2015 - Glasgow



Aneurin Bevan University Health Board





Upload Parameters

Run Analysis

Run Simulation

Nodes:

EMS - EDIT

A&E - EDIT
Acute - EDIT

Community & Social Care - EDIT

Community Hospital - EDIT

Nursing Homes - EDIT

View Results

COMMUNITY & SOCIAL CARE

Winter Workforce Requirements:

Summer Workforce Requirements: Skill 1: #### WTEs Skill 2: #### WTEs

Skill 1: ##### WTEs Skill 2: ##### WTEs Skill 3: ##### WTEs

Skill 4: ##### WTEs

Skill 4: ##### WTEs Skill 5: ##### WTEs

Skill 5: #### WTEs

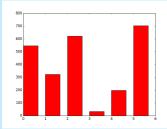
Spring Workforce Requirements:

Autumn Workforce Requirements:

Skill 1: ##### WTEs Skill 2: #### WTEs Skill 1: ##### WTEs Skill 2: ##### WTEs

Skill 3: #### WTEs Skill 4: #### WTEs Skill 5: #### WTEs Skill 3: ##### WTEs Skill 4: ##### WTEs

Skill 5: ##### WTEs



Performance Measures:

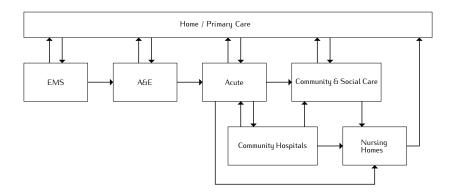
Winter Expected Occupancy: ####

Spring Exprected Occupancy: #####

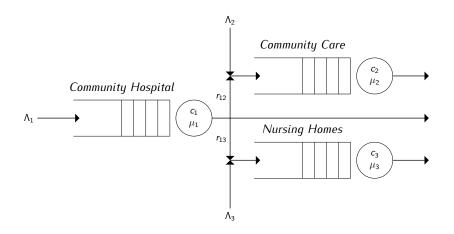
Summer Expected Occupancy: #####

Autumn Expected Occupancy: #####

Map of Healthcare System



Jackson Networks

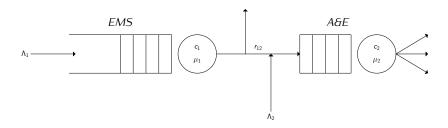


Jackson Networks

$$\lambda_i = \Lambda_i + \sum_j r_{ji} \lambda_j$$
 λ_2 Community Care

$$P(k_1, k_2, \ldots, k_M) = \prod_{i=1}^M P_i(k_i)$$

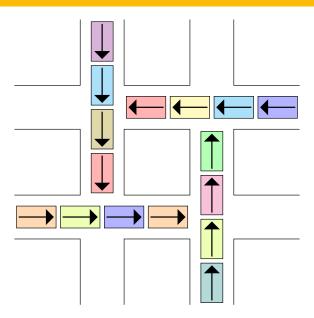
Restricted Networks

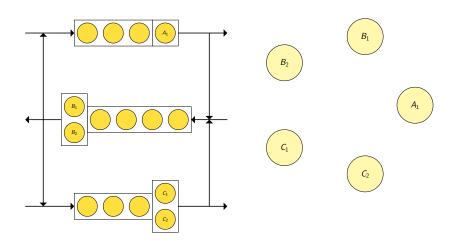


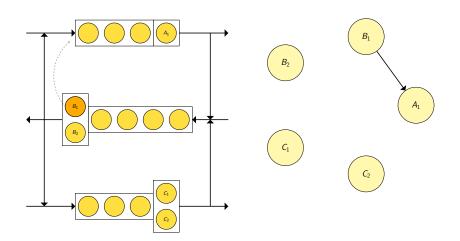
Restricted Networks

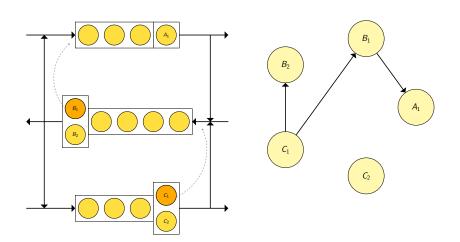
- Markov Chain Models
- Approximation Methods
- Simulation

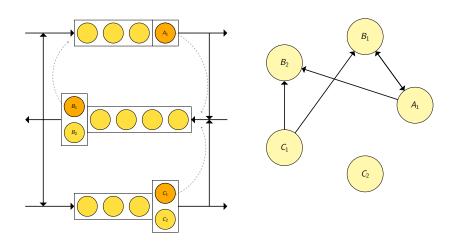
Deadlock

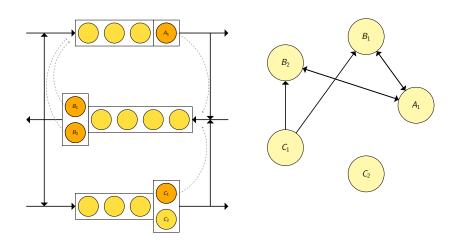


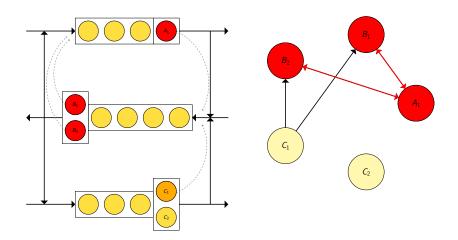




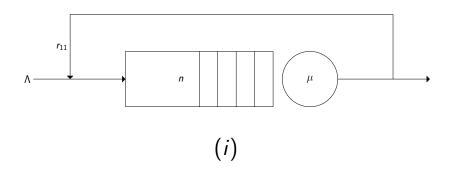








Markovian Model of Deadlock



$$S = \{i \in \mathbb{N} | 0 \le i \le n+1\} \cup \{-1\}$$

Define $\delta = i_2 - i_1$

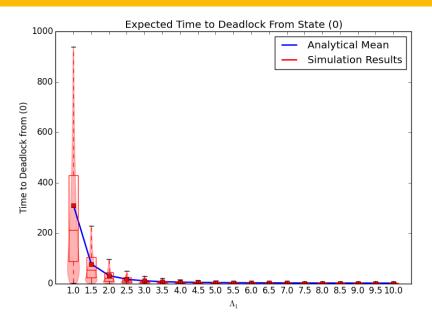
$$q_{i_1,i_2} = egin{cases} \Lambda & ext{if } i < n+1 \ 0 & ext{otherwise} \end{cases} & ext{if } \delta = 1 \ (1-r_{11})\mu & ext{if } \delta = -1 \ 0 & ext{otherwise} \end{cases}$$

$$q_{i,-1} = \begin{cases} r_{11}\mu & \text{if } i = n+1 \\ 0 & \text{otherwise} \end{cases}$$

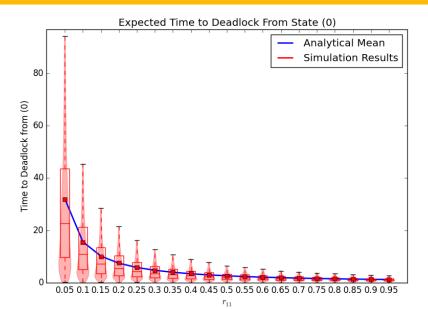
$$q_{-1,s} = 0$$



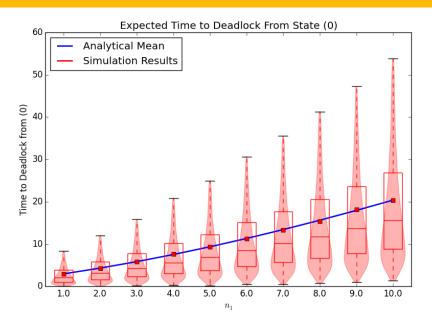
Times to Deadlock - Λ



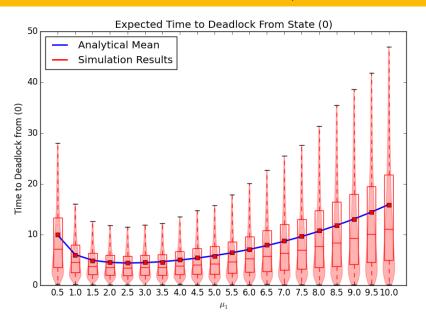
Times to Deadlock – r_{11}



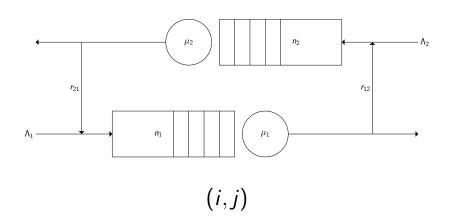
Times to Deadlock - n



Times to Deadlock - μ



Markovian Model of Deadlock



$$S = \{(i,j) \in \mathbb{N}^{(n_1+2 \times n_2+2)} | 0 \le i+j \le n_1+n_2+2 \} \cup \{(-1)\}$$
Define $\delta = (i_2,j_2) - (i_1,j_1)$

$$\begin{cases} \Lambda_1 & \text{if } i_1 \le n_1 \\ 0 & \text{otherwise} \end{cases} & \text{if } \delta = (1,0)$$

$$\Lambda_2 & \text{if } j_1 \le n_2 \\ 0 & \text{otherwise} \end{cases}$$

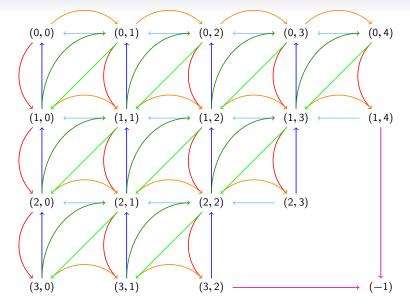
$$\begin{cases} \Lambda_2 & \text{if } j_1 \le n_2 \\ 0 & \text{otherwise} \end{cases}$$

$$\begin{cases} \delta = (0,1) \end{cases}$$

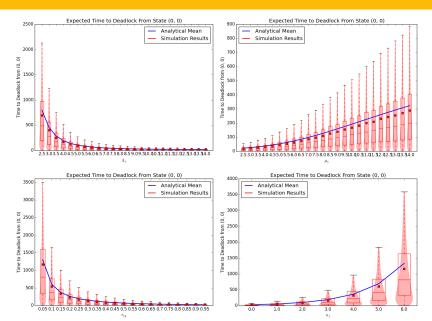
$$q_{(i_1,j_1),(i_2,j_2)} = \begin{cases} & \Lambda_1 & \text{if } i_1 \leq n_1 \\ & 0 & \text{otherwise} \\ & \Lambda_2 & \text{if } j_1 \leq n_2 \\ & 0 & \text{otherwise} \\ (1-r_{12})\mu_1 & \text{if } j_1 < n_2 + 2 \\ & 0 & \text{otherwise} \\ (1-r_{21})\mu_2 & \text{if } i_1 < n_1 + 2 \\ & 0 & \text{otherwise} \\ r_{12}\mu_1 & \text{if } j_1 < n_2 + 2 \\ & 0 & \text{otherwise} \\ r_{12}\mu_2 & \text{if } i_1 < n_1 + 2 \\ & 0 & \text{otherwise} \\ r_{21}\mu_2 & \text{if } i_1 < n_1 + 2 \\ & 0 & \text{otherwise} \\ \end{cases} & \text{if } \delta = (-1, 1) \\ & \epsilon_{11}\mu_2 & \text{if } i_1 < n_1 + 2 \\ & 0 & \text{otherwise} \\ & \epsilon_{21}\mu_2 & \text{if } i_1 < n_1 + 2 \\ & 0 & \text{otherwise} \\ \end{cases} & \text{if } \delta = (1, -1) \\ & \text{otherwise} \end{cases}$$

$$q_{(i_1,j_1),(-1)} = \begin{cases} r_{21}\mu_2 & \text{if } (i,j) = (n_1,n_2+2) \\ r_{12}\mu_1 & \text{if } (i,j) = (n_1+2,n_2) \\ 0 & \text{otherwise} \end{cases}$$

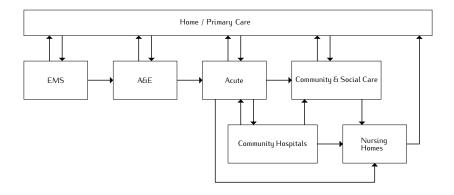
$$q_{-1,s} = 0$$



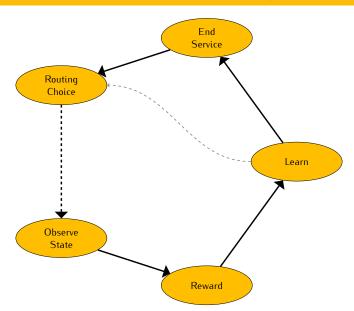
Times to Deadlock



Reinforcement Learning



Reinforcement Learning



Reinforcement Learning

Q-Learning

$$Q(s,a) \leftarrow Q(s,a) + \alpha[r + \gamma \max_{a'} Q(s',a') - Q(s,a)]$$

Diolch - Thank You

 $https://github.com/geraintpalmer/Presentations\\palmergi1@cardiff.ac.uk$