### LXe scintillation model

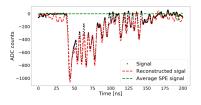
January 23, 2020

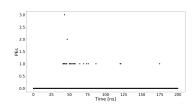
## Objective

We want to use the data collected by the Cs and Co runs to estimate the parameters for the scintillation model. In the following we show that there is a  $\delta(t)$  component in the model with high statistical significance and propose how to go on to claim a discovery.

## Signal Reconstruction

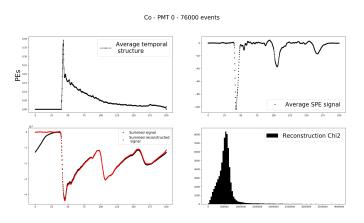
To study the temporal structure of the photon emission a processing algorithm uses a template of the average SPE signal to reconstruct the temporal PE pattern in each event for each PMT separately. The output of this process is the number of PEs created in the PMT in each digitization point.



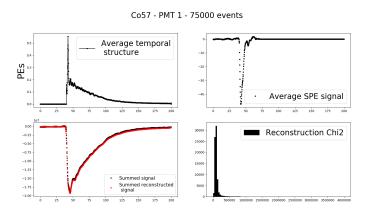




#### Reconstruction results



#### Reconstruction results



#### Reconstruction results

25

Average temporal structure

Average temporal structure

Average SPE signal

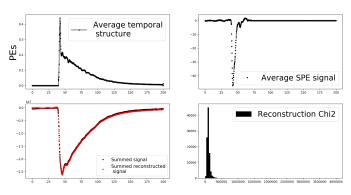
Summed signal Summed reconstructed signal

Summed reconstructed

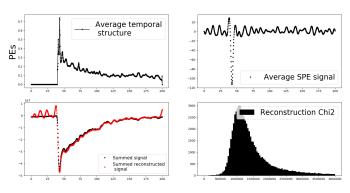
Reconstruction Chi2

500000 1000000 1500000 2000000 2500000 3000000 3500000 4000000

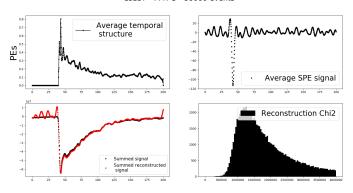
Cs137 - PMT 1 - 96000 events



Co57 - PMT 3 - 71000 events

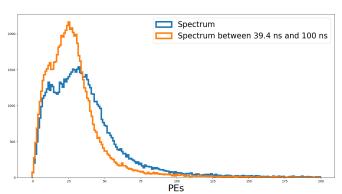


Cs137 - PMT 3 - 86000 events

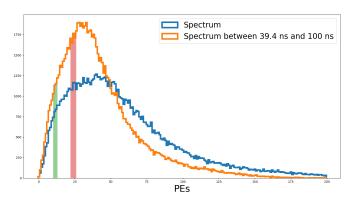


## 1 PMT Spectrum

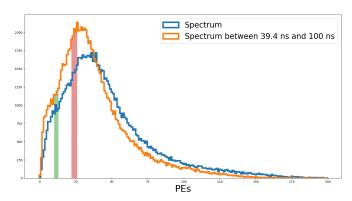
Co57 - PMT 0 - 76000 events



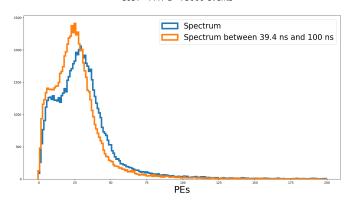
Cs137 - PMT 0 - 97000 events



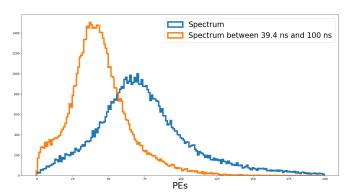
Cs137 - PMT 1 - 96000 events



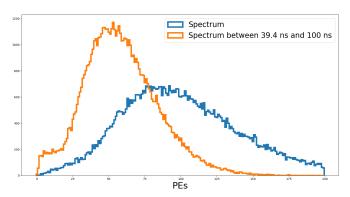
Co57 - PMT 1 - 75000 events



Co57 - PMT 3 - 71000 events

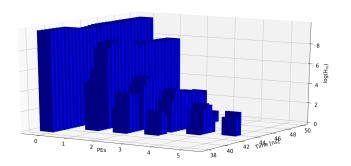


Cs137 - PMT 3 - 86000 events



### PE Histogram

The basis for analysis is a 2D histogram (for each PMT and each source)  $H_{ni}$  which holds the number of events in which n PEs were resolved at time i,



The average temporal structure which shown in the Reconstruction result slide is the average on each column.



### Model for $H_{ni}$

The number of photons emitted at time i,

$$n_i^{ph} \sim \text{Poisson}(Y_i N),$$
 (1)

where N is the average number of photon emitted in the events, and  $Y_i$  is the scintillation model (the probability to emit a photon at time i).

The number of PEs created in the PMT at time i,

$$n_i^{pe} \sim \text{Binom}(Q, \text{Poisson}(Y_i N)),$$
 (2)

where Q is the photon detection efficiency (quantum efficiency, collection efficiency and double PE probability).

Each PMT has its temporal uncertainty combined with the code's temporal uncertainty. The number of PEs that need to be resolved at time i,

$$\tilde{n}_i \sim \sum_j m_j^i, \tag{3}$$

where  $m_j^i$  is a random variable that represents the number of PEs that were created at time j but resolved at time i.

$$m_j^i \sim n_j^{pe} \text{Norm}(i - j - T | \sigma_t)$$
 (4)

where  $\sigma_t$  is the temporal resolution of the PMT and the code and T is the average delay of the PMT.

Since  $\tilde{n}_i$  is a sum of independent random variables its distribution can be approximated by a distribution with mean and variance  $\langle \tilde{n}_i \rangle = \sum_j \langle m \rangle_j^i$ ,  $\text{Var}_i = \sum_j \text{Var}_j^i$ , where,

$$\langle m \rangle_j^i = \text{Var}_j = Q N_0 Y_j \text{Norm}(i - j - T | \sigma_t)$$
 (5)

Poisson has an equal mean and variance, xo

$$\tilde{n_i} \sim \text{Poisson}\left(QN\sum_j Y_j \text{Norm}(i-j-T|\sigma_t)\right)$$
 (6)

#### Scintillation model

 $Y_j$  is the probability to emit a photon at time  $t_j \Delta t$ .

$$Y_{j} = \Delta t F \delta(t_{j} - T) + \Delta t \frac{1 - F}{\tau_{s}} e^{-t_{j}/\tau_{s}}$$

$$\langle \tilde{n}_{i} \rangle = \frac{QN\Delta t}{\sqrt{2\pi}\sigma_{t}} \int_{0}^{\infty} Y(\tilde{t}) e^{-(\tilde{t} - t_{i} - T)^{2}/2\sigma_{t}^{2}} =$$

$$NQ\Delta t \left[ \frac{e^{-(t_{i} - T)^{2}/2\sigma_{t}^{2}}}{\sqrt{2\pi}\sigma_{t}} + \frac{K}{\tau} e^{-t/\tau} \left( 1 - \operatorname{erf} \left( \frac{\sigma}{\sqrt{2}\tau} - \frac{t - T}{\sqrt{2}\sigma} \right) \right) \right]$$
(8)

Where K is a normalization constant,

$$K = \left[1 - \operatorname{erf}\left(\frac{\sigma}{\sqrt{2}\tau} + \frac{T}{\sqrt{2}\sigma}\right) + e^{-\sigma^2/2\tau^2 - T/\tau} \left(1 + \operatorname{erf}\left(\frac{T}{\sqrt{2}\sigma}\right)\right)\right]^{-1}$$

#### SPE resolution

Finally, the code has its resolution for SPEs (its accuracy to resolve the correct number of PEs from the signal at a given time). The probability to resolve n PEs given  $\tilde{n}$  is the correct number,

$$n_i \sim P_n(\tilde{n}|\sigma_{pe}) = \sum_m \text{Norm}(m-1|\sigma_{pe}) P_{n-m}(\tilde{n}-1|\sigma_{pe})$$
 (10)

## Expectation for $H_{ni}$

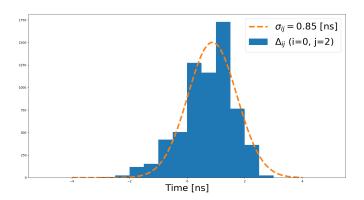
The expected number of events in which n PEs were resolved at time i is,

$$h_{ni} = N_{ev} \sum_{m} P_n(m|\sigma_{pe}) Poisson(m|\langle \tilde{n}_i \rangle)$$
 (11)

This is a model with 7 parameters:  $N, Q, F, \tau_s, T, \sigma_t, \sigma_{PE}$ . Some of them can be constrained by calibration data.

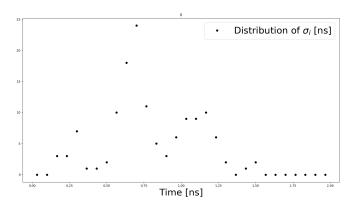
#### Calibration $\sigma_t$

We can calibrate  $\sigma_t$  for each PMT by the pulser data. Consider PMT<sub>i</sub> that we want to calibrate and a any PMT<sub>j</sub>. For each pulser event in which both PMTs saw SPE we measure  $\Delta_{ij}$ , the time difference between the two signals.  $\Delta_{ij} \sim \text{Norm}(T_{ij}, \sigma_{ij})$ .



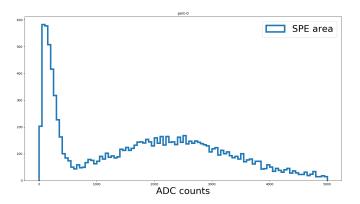
$$\sigma_i = \sqrt{\frac{1}{2}(\sigma_{ij}^2 + \sigma_{ik}^2 - \sigma_{jk}^2)}$$
 for any  $j \neq k$ .

So a pair of PMTs (k, j) is used to estimate the  $\sigma_i$ . Each PMT<sub>i</sub> has  $\frac{1}{2}\binom{19}{2}$  estimates for  $\sigma_i$  and their mean is  $\sigma_t$  for that PMT.



### Calibration of $\sigma_{PE}$

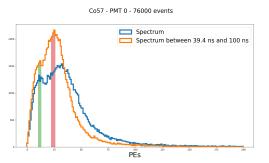
This is just the width of the SPE are distribution.



### Constrain on NQ

We choose the data to fit our model to from a narrow PE bands from the spectrum which can be estimated that origin of the events in these bands is from the same energy and their variation is due to statistical fluctuation and no physical. Thus we expect that

$$N_{PE} \sim \text{Poisson}(\sum_{39.4ns}^{100ns} \langle h_{ni} \rangle_n)$$
 (12)



#### Fit

To find the parameters which give  $h_{ni}$  as close to  $H_{ni}$  we maximize

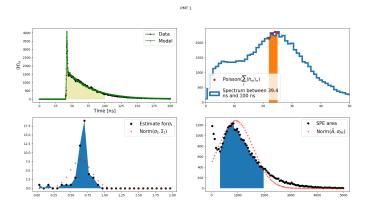
$$L(\text{data}, \text{model}(\theta)) = \sum_{\text{dataset}} \sum_{j \in J} \text{Poisson}(\text{data}_j | \text{model}_j) / \text{len}(J)$$
(13)

Where  $\theta$  are the parameters J is some subrange of the dataset, and

- ▶ Dataset  $H_{ni}$ , model  $h_{ni}$ .
- ▶ Dataset distribution of estimates for  $\sigma_t$ , model Norm $(\sigma_t, \Sigma_t)$ .
- ▶ Dataset distribution of SPE areas, model Norm $(\bar{A}, \bar{A} \cdot \sigma_{PE})$ .
- ▶ Dataset PE spectrum, model Poisson $(\sum_{39.4ns}^{100ns} \langle h_{ni} \rangle_n)$ .

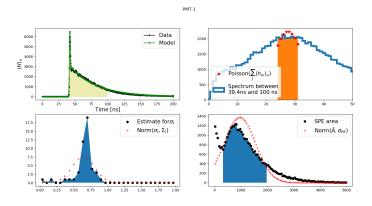
This adds two dummy parameters,  $\Sigma_t$  is the standard deviation of the estimates of  $\sigma_t$  and  $\bar{A}$  is the mean SPE area.

# Results (<sup>57</sup>Co peak 2)



NQ	F	$\sigma_t[ns]$	$\sigma_t[ns]$	$\sigma_{PE}$
33	0.1	34	0.6	0.7

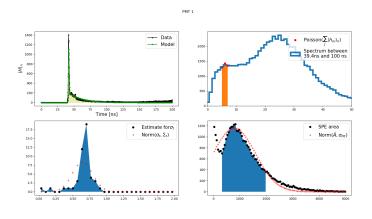
# Results ( $^{137}$ Cs)



NQ	F	$\sigma_t[ns]$	$\sigma_t[ns]$	$\sigma_{PE}$
39	0.09	38	0.6	0.6

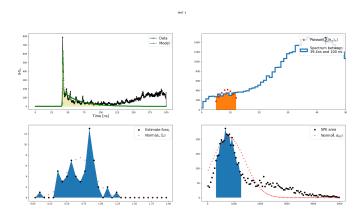
# Results (<sup>57</sup>Co peak 1)

Notice that for this peak F is much greater and  $\tau_s$  is much smaller.



NQ	F	$\sigma_t[ns]$	$\sigma_t[ns]$	$\sigma_{PE}$
7	0.4	18	0.6	1

# Results ( ${}^{57}$ Co peak 1 - strange result)



#### Parameter estimation

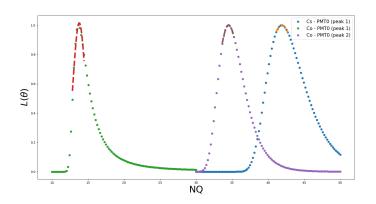
 $\hat{\theta}$  are the parameters that maximize L so for any parameter  $\theta_i$ ,

$$\partial_{\theta_i} L = 0 \quad \rightarrow \quad L(\hat{\theta} + \Delta \theta) = L_{max} \left(1 + \frac{\partial_{\theta_i}^2 L}{2L_{max}} \Delta \theta^2\right) \quad \rightarrow \quad (14)$$

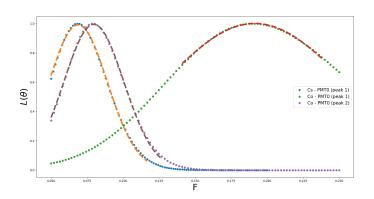
$$L(\hat{\theta} + \Delta \theta) \approx L_{max} e^{-\Delta \theta^2 / 2\sigma_{\theta}^2}$$

For each parameter L was maximized while holding the parameter fixed (for a range of parameters, for PMT individually)

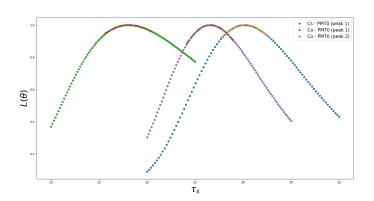
# NQ



Source	$\hat{NQ}$	$\sigma_{NQ}$
Cs	42	2.5
Co (peak 1)	14	0.8
Co (peak 2)	34	1.7



Source	$\hat{F}$	$\sigma_F$	significance $[\sigma]$
Cs	0.07	0.02	3
Co (peak 1)	0.2	0.06	3
Co (peak 2)	0.08	0.02	4



Source	$\hat{ au_s}[ns]$	$\sigma_{\tau_s}[ns]$
Cs	40	6
Co (peak 1)	28	8
Co (peak 2)	37	5

## How to go on

- ▶ Preform this analysis for all PMTs individually for both sources and both orientations (source to the lab / to the door).
- ▶ Study the low energy component in the Co spectrum and if it has a different scintillation regime (NR?).
- ▶ Maximize L with the constrain that  $N, F, \tau_s$  is the same for all PMTs (but different between sources). This will brake the degeneracy of NQ.
- ▶ Maximize L with only  $N, \tau_s$  fixed for all PMTs. This will show the anisotropy in the fast component.
- ▶ Maximize L with  $N, \tau_s$  fixed and constrain a 90 deg between the symmetry axis of the anisotropy of F in the two orientations.
- ightharpoonup Maximize L with the above with the constrain that F is isotropic in the BG data.