

Problem 1 Gerald Susanteo

Best case = fully sorted array since our last HW, $3N^2+4N+1$ is what we would expect
But since the while loop only runs N times as the array is fully sorted meaning we can disregard it.

```
Insertion-Sort(A,n) 1
  for(i-1) to n      N+1
    key=A[i]         N
    j=i-1            N
    while j>=0 and A[j]>key  N
      A[j+1]=A[j]    N
      j=j-1          N
    A[j+1]= key      N
```

=> $N+1+N+N+N+N+N+N+1$

=> $7N+2$

Since the while loop may not loop itself, the best case scenario will be Because the while loop $O(g(n))=7*N$ Hence, **$O(n)$** is the best case

Average Case = Considering the array is scrambled but the elements are only one off from sorted

```
Insertion-Sort(A,n) 1
                    - //nothing
  for(i-1) to n      N+1
    key=A[i]         N
    j=i-1            N
    while j>=0 and A[j]>key  N(N+1)
      A[j+1]=A[j]    N*N
      j=j-1          N*N
    A[j+1]= key      N
```

=> $N+1+N+N+N^2+N+N^2+N^2+N$

=> $3N^2+4N+1$

Since to run the while loop which in this case is inside the for loop so the costs is $\Omega(g(n))$ is $\Omega(n^2)$

Hence the worse case is similar to the average case = $\Theta(g(n))$ would also be $\Theta(n^2)$

Problem 2

The best case = when the number of rows and columns in both a and b are 1

MATRIX_MULTIPLY(A, B): 1

```

if columns(A) ≠ rows(B): 1
    raise ValueError("Matrix multiplication is not defined.") 1

```

```

rows_A ← number of rows in A 1
cols_A ← number of columns in A 1
cols_B ← number of columns in B 1
result ← matrix of size rows_A x cols_B filled with zeros 1

```

```

for i from 1 to rows_A do: 1
    for j from 1 to cols_B do: 1
        sum ← 0 1
        for k from 1 to cols_A do: 1
            sum ← sum + A[i][k] * B[k][j] 1
        result[i][j] ← sum return result 1

```

=> 1+1+1+1+1+1+1+1+1+1+1+1+1+1

=> 13

Hence the base case is $O(1)$ since the code only run once

Average case = Since the highest order is n^2 the time constraint is also $\Omega(n^2)$

```

MATRIX_MULTIPLY(A, B): 1
if columns(A) ≠ rows(B): 1
    raise ValueError("Matrix multiplication is not defined.") 1
rows_A ← number of rows in A 1
cols_A ← number of columns in A 1
cols_B ← number of columns in B 1
result ← matrix of size rows_A x cols_B filled with zeros 1
for i from 1 to rows_A do: N+1
    for j from 1 to cols_B do: N(N+1)
        sum ← 0 N*N
        for k from 1 to cols_A do: N(N+1)
            sum ← sum + A[i][k] * B[k][j] N*N
        result[i][j] ← sum return result N

```

=> 7+N+1+N^2+N+N^2+N^2+N+N^2+N

=> $3n^2+4N+8$

Since the highest order is n^2 the time constraint is also $\Omega(n^2)$

For the worst case we will get the same as average case where $\Theta(g(n))$ would also be $\Theta(n^2)$