

# Journal of Statistical Software

MMMMMM YYYY, Volume VV, Issue II.

doi: 10.18637/jss.v000.i00

## The chords R Package- A Principled Approach to Respondent Driven Sampling

Jonathan D. Rosenblatt

Ben Gurion University

Yakir Berchenko

Gertner Institute for Epidemiology and Health Policy Research Simon D. Frost Cambridge University

#### Abstract

The abstract of the article.

Keywords: RDS, estimation, counting-process, R.

#### 1. Introduction

As the name suggests, Respondent Driven Sampling (RDS) is a framework for sampling by chain-referral. RDS is a bundle of a sampling mechanism and analysis methods, most common in the study of marginalized populations which do not lend themselves to simple sampling (Heckathorn 1997, 2002).

In RDS seeds are selected – usually by convenience – from the target population, and given coupons. They use these coupons to recruit others, who themselves become recruiters. Recruits are given an incentive, usually money, for taking part in the survey, and also for recruiting others. This process continues in recruitment waves until the survey is stopped, usually when a target sample size is reached.

With the above sampling mechanism, highly connected individuals will be overrepresented in the sample. If the attribute of interest is correlated with an individual's degree, as is often the case (e.g. HIV), naïveestimates will be biased towards the state of the highly connected subgroups. An unbiased Horowitz-Thompson-type estimator (Horvitz and Thompson 1952) would require the knowledge of frequency of each degree. Clearly, the frequency of each degree will also be biased towards higher degrees, and thus cannot be recovered from the knowledge of individuals' degrees alone. The common remedy to this matter is the inverse-degree weighting heuristic (??).

In Berchenko, Rosenblatt, and Frost (2013) we proposed a generative model for RDS. The model is based on the idea that RDS spreads like an epidemic, and we can thus borrow epidemiological generative models. In particular SIR [TODO: add citation], for likelihood based inference. Having assumed a generative process, we can now estimate degree frequencies, introduce covariates, check the goodness of fit, and discuss the model's assumptions.

The details of the assumed generative model can be found in Berchenko et al. (2013), but the essentials are now detailed for completeness.

Denote  $N_k$  the unknown population frequency of degree k, i.e., the number of individuals with k "friends". Denote  $N := \sum_k N_k$ , the total population size. Denote by  $x_t$  the degree of the respondent recruited at time t. Our task is to estimate  $\hat{N}_1, \hat{N}_2, \ldots$ , based on a sample of  $x_{t_1}, \ldots, x_{t_\tau}$ . Denote  $\lambda_{k,t}$ , the probability of recruiting an individual with degree k in the time interval  $[t, t + \Delta]$ . We assume the following generative multivariate counting model:

$$\lambda_{k,t} = \beta_k \frac{n_t}{N} (N_k - n_{k,t}) \Delta t + o(\Delta t), \tag{1}$$

where  $\beta_k$  is some base recruitment rate,  $n_t$  is the number of recruiting individuals at time t, and  $n_{k,t} := \sum_{s \leq t} I_{\{x_s = k\}}$  the number of recruited individuals of degree k. It thus follows that  $\frac{I_t}{N}$  is the recruiting population proportion, and  $(N_k - n_{k,t})$  the recruitment "potential" of degree k. In these terms, our model implies that the recruitment probability, in short enough time periods, is proportional to the recruiting team (a.k.a. the "snowball") and the recruiting potential. For more on this model, and relations to other existing models, see Berchenko *et al.* (2013).

Equipped with this generative model, we may state the estimation of  $N_1, N_2, \ldots$  as a likelihood maximization problem. Moreover, we show in Berchenko *et al.* (2013) that the maximum likelihood estimator (MLE) of  $N_1, N_2, \ldots$  is separable for the various k, and independent of  $\beta_k$ . This fact is used by Berchenko *et al.* (2013) for proof of the asymptotic properties of  $\hat{N}_1, \hat{N}_2, \ldots$ , and in the **chords** package to accelerate the estimation task.

MLEs for  $N_1, N_2, \ldots$  in model (1) have an interesting finite sample property: They tend to return  $\hat{N}_k = \infty$  with non null probabilities. This clearly calls for some regularization. The Bayesian framework, a celebrated regularization device, will not work in this problem. Informally speaking, this is because any shrinkage of  $\infty$  is still  $\infty$ . In our package, we have implemented several regularization devices. Some very crude heuristics, and some less so. In particular, we generalized the ideas of Musa and Iannino (1991) and Osborne and Severini (2000) to our multivariate case. The former proposing a jacknife-type resampling scheme, and the latter an integrated likelihood approach.

The usage of the package, the MLE estimator, and the small-sample modifications, is demonstrated in the next section.

#### 2. Work Flow

We start by demonstrating the workflow on some data supplied with the package. The data consists of [TODO: describe data]. For more details, see Salganik, Fazito, Bertoni, Abdo, Mello, and Bastos (2011).

first input first line first input second line

output of first input

second input

#### 3. Some Technicalities

### 4. Conclusion

#### 5. Future Work

#### References

- Berchenko Y, Rosenblatt J, Frost SDW (2013). "Modeling and Analysing Respondent Driven Sampling as a Counting Process." arXiv:1304.3505. 1304.3505.
- Heckathorn D (1997). "Respondent-driven sampling: a new approach to the study of hidden populations." *Social Problems*, **44**(2), 174–199.
- Heckathorn D (2002). "Respondent-driven sampling II: deriving valid population estimates from chain-referral samples of hidden populations." Social Problems, 49(1), 11–34.
- Horvitz DG, Thompson DJ (1952). "A generalization of sampling without replacement from a finite universe." *Journal of the American Statistical Association*, **47**(260), 663–685.
- Musa JD, Iannino A (1991). "Estimating the Total Number of Software Failures Using an Exponential Model." SIGSOFT Softw. Eng. Notes, 16(3), 80–84. ISSN 0163-5948. doi: 10.1145/127099.127123.
- Osborne JA, Severini TA (2000). "Inference for Exponential Order Statistic Models Based on an Integrated Likelihood Function." *Journal of the American Statistical Association*, **95**(452), 1220–1228. ISSN 0162-1459. doi:10.1080/01621459.2000.10474322.
- Salganik MJ, Fazito D, Bertoni N, Abdo AH, Mello MB, Bastos FI (2011). "Assessing Network Scale-up Estimates for Groups Most at Risk of HIV/AIDS: Evidence From a Multiple-Method Study of Heavy Drug Users in Curitiba, Brazil." *American Journal of Epidemiology*, 174(10), 1190–1196. doi:10.1093/aje/kwr246.

#### Affiliation:

Jonathan D. Rosenblatt
Department of Industrial Engineering and Management
Faculty of Engineering
Ben Gurion University of the Negev
P.O. 653, Beer Sheva, 8410501
E-mail: johnros@bgu.ac.il

URL: http://www.john-ros.com/

Journal of Statistical Software
published by the Foundation for Open Access Statistics
MMMMMM YYYY, Volume VV, Issue II
doi:10.18637/jss.v000.i00

http://www.jstatsoft.org/

http://www.foastat.org/

Submitted: yyyy-mm-dd

Accepted: yyyy-mm-dd