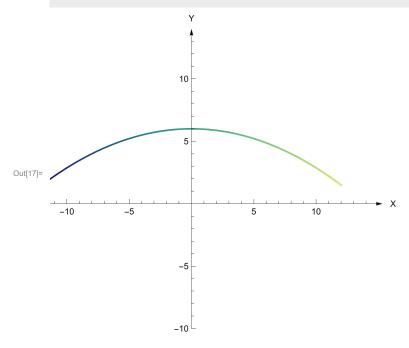
Case of two point incident on a parabola

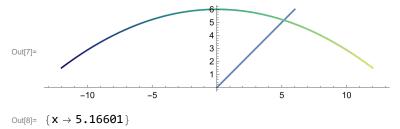
Equation Of Reflective Curve In Parametric and Cartesian Form

Plot of the equation



Incident ray of light at 45 degrees to x axis with source at origin

```
In[4]:= sourceparaeqn = {t, t};
sourcecarteqn = x;
sourceline = ParametricPlot[sourceparaeqn, {t, 0, 6}, PlotRange→All];
Show[sourceline, curve]
alincipt = N[Solve[sourcecarteqn=curvecarteqn, x]][2]
```

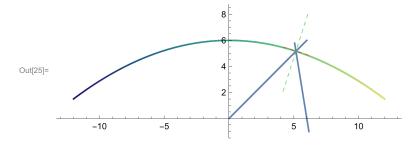


Tangent line at point of incident and reflected ray

altaneqn = Reduce[y-(curvecarteqn /. alincipt) == (D[curvecarteqn, x] /. alincipt) (x-({x} /.al alnoreqn = Reduce[y-(curvecarteqn /. alincipt) == (-1/(D[curvecarteqn, x] /. alincipt)) (x-({x} alnorplot = Plot[Last[List @@ alnoreqn], {x,({x} /.alincipt)[1]-1,({x} /.alincipt)[1]+1}, Pl altanplot = Plot[Last[List @@ altaneqn], {x,({x} /.alincipt)[1]-1,({x} /.alincipt)[1]+1}, Pl alrefangle = Reduce[(1-(-1/(D[curvecarteqn, x] /. alincipt)))/(1+1*(-1/(D[curvecarteqn, x] / alrefeqn = Reduce[y-(curvecarteqn /. alincipt) == Last[List @@ alrefangle](x-({x} /.alincipt)[1]+1}] alrefplot = Plot[Last[List @@ alrefeqn], {x,({x} /.alincipt)[1]-0.1,({x} /.alincipt)[1]+1}] Show[sourceline, curve, altanplot,alnorplot,alrefplot]

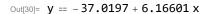
```
Out[18]= y == 6.83399 - 0.322876 x
Out[19]= y == -10.834 + 3.09717 x
```

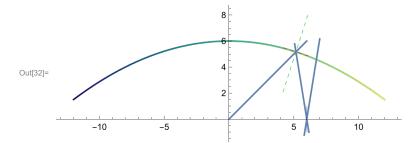
Out[22]= m == -6.16601



Now, on 2nd reflection on the axis

```
a2incipt = Last[List @@ Reduce[Last[List @@ a1refeqn]==0,x]];
a2noreqn = {a2incipt, y};
a2norplot = ParametricPlot[a2noreqn,{x, -1, 1}, {y, -1, 1}];
a2refangle = (Tan[π]-Last[List @@ a1refangle])/(1+Tan[π]*Last[List @@ a1refangle]);
a2refeqn = Reduce[y-0==a2refangle(x-a2incipt),y]
a2refplot = Plot[Last[List @@ a2refeqn], {x,a2incipt - 0.2,a2incipt+1}];
Show[sourceline, curve, a1tanplot,a1norplot,a1refplot,a2norplot, a2refplot]
```



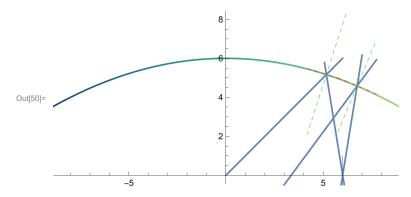


Now on 3rd Reflection

a3incipt = N[Solve[Last[List @@ a2refeqn] == curvecarteqn, x]] [2] In[42]:= a3taneqn = Reduce[y-(curvecarteqn /. a3incipt) == (D[curvecarteqn, x] /. a3incipt) (x-({x} /.a3 a3noreqn = Reduce[y-(curvecarteqn /. a3incipt) = $(-1/(D[curvecarteqn, x] /. a3incipt))(x-({x})$ a3norplot = Plot[Last[List @@ a3noreqn], $\{x,(\{x\} /.a3incipt)[1]-1,(\{x\} /.a3incipt)[1]]+1\}$, Pl $a3 tanplot = Plot[Last[List @@ a3 taneqn], {x,({x} /.a3 incipt) [1]-1,({x} /.a3 incipt) [1]+1}, Plast[List @@ a3 taneqn], {x,({x} /.a3 incipt) [1]-1,({x} /.a3 incipt) [1]+1}, Plast[List @@ a3 taneqn], {x,({x} /.a3 incipt) [1]-1,({x} /.a3 incipt$ a3refangle = Reduce[(a2refangle-(-1/(D[curvecarteqn, x] /. a3incipt))))/(1+a2refangle*(-1/(D[a3refeqn = Reduce[y-(curvecarteqn /. a3incipt) == Last[List @@ a3refangle](x-({x} /.a3incipt)[a3refplot = Plot[Last[List @@ a3refeqn], {x,({x} /.a3incipt)[1]-4,({x} /.a3incipt)[1]+1}]; Show[sourceline, curve, a1tanplot,a1norplot,a1refplot,a2norplot, a2refplot, a3tanplot,a3norplo

 $\text{Out[42]= } \left\{ \, x \, \rightarrow 6.74625 \, \right\}$ Out[43]= y == 7.42225 - 0.421641 xOut[44]= y == -11.4222 + 2.37169 x

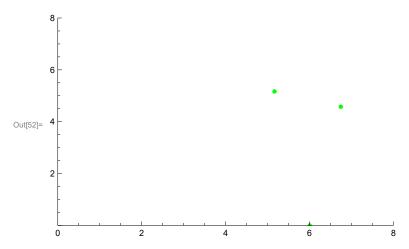
Out[47] = m == 1.3508



Plot of points of intersection

interpts = $\{x/.a1incipt, (curvecarteqn /. a1incipt)\}, \{a2incipt, 0\}, \{x /.a3incipt, (curvecarteqn /. a1incipt)\}$ In[51]:= ptplot = ListPlot[interpts, PlotRange→{{0, 8},,{0, 8}},PlotStyle→{Green}]

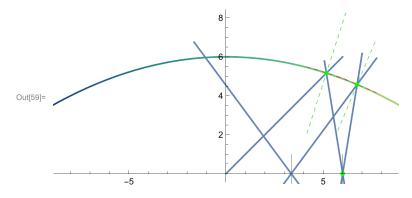
 $Out[51] = \{ \{5.16601, 5.16601\}, \{6.00383, 0\}, \{6.74625, 4.57775\}, \{a4incipt, 0\} \}$



Now 4th reflection

```
a4incipt = Last[List @@ Reduce[Last[List @@ a3refeqn]==0,x]];
a4noreqn = {a4incipt, y};
a4norplot = ParametricPlot[a4noreqn,{x, -1, 1}, {y, -1, 1}];
a4refangle = (Tan[π]-Last[List @@ a3refangle])/(1+Tan[π]*Last[List @@ a3refangle]);
a4refeqn = Reduce[y-0==a4refangle(x-a4incipt),y]
a4refplot = Plot[Last[List @@ a4refeqn], {x,a4incipt - 5,a4incipt+1}];
Show[sourceline, curve, a1tanplot,a1norplot,a1refplot,a2norplot, a2refplot, a3tanplot,a3norplo
```





Now on 5th Reflection

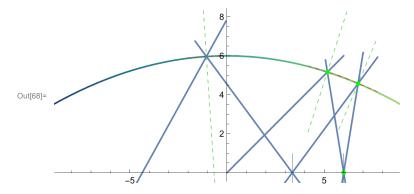
a5incipt = N[Solve[Last[List @@ a4refeqn] == curvecarteqn, x] [1]
a5taneqn = Reduce[y-(curvecarteqn /. a5incipt) == (D[curvecarteqn, x] /. a5incipt) (x-({x} /.a5 a5noreqn = Reduce[y-(curvecarteqn /. a5incipt) == (-1/(D[curvecarteqn, x] /. a5incipt)) (x-({x} a5norplot = Plot[Last[List @@ a5noreqn], {x,({x} /.a5incipt) [1]-1,({x} /.a5incipt) [1]+1}, Pl a5tanplot = Plot[Last[List @@ a5taneqn], {x,({x} /.a5incipt) [1]-1,({x} /.a5incipt) [1]+1}, Pl a5refangle = Reduce[(a4refangle-(-1/(D[curvecarteqn, x] /. a5incipt)))/(1+a4refangle*(-1/(D[a5refeqn = Reduce[y-(curvecarteqn /. a5incipt) == Last[List @@ a5refangle](x-({x} /.a5incipt) [1]+1});
show[sourceline, curve, a1tanplot,a1norplot,a1refplot,a2norplot, a2refplot, a3tanplot,a3norplo

```
Out[60]= \{x \rightarrow -1.05854\}

Out[61]= y == 6.03502 + 0.0661585 \times

Out[62]= y == -10.035 - 15.1152 \times

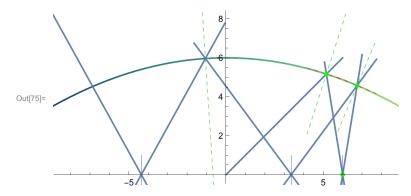
Out[65]= m == 1.80834
```



Now 6th reflection

```
a6incipt = Last[List @@ Reduce[Last[List @@ a5refeqn]==0,x]];
In[69]:=
       a6noreqn = {a6incipt, y};
       a6norplot = ParametricPlot[a6noreqn,\{x, -1, 1\}, \{y, -1, 1\}];
       a6refangle = (Tan[\pi]-Last[List @@ a5refangle])/(1+Tan[\pi]*Last[List @@ a5refangle]);
       a6refeqn = Reduce[y-0==a6refangle(x-a6incipt),y]
       a6refplot = Plot[Last[List @@ a6refeqn], {x,a6incipt - 5,a6incipt+1}];
       Show[sourceline, curve, a1tanplot,a1norplot,a1refplot,a2norplot, a2refplot, a3tanplot,a3norplo
```

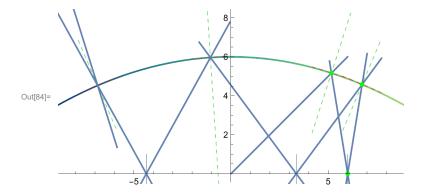
Out[73]= y == -7.87917 - 1.80834 x



Now on 7th Reflection

a7incipt = N[Solve[Last[List @@ a6refeqn]==curvecarteqn, x]][1] In[76]:= a7taneqn = Reduce[y-(curvecarteqn /. a7incipt) == (D[curvecarteqn, x] /. a7incipt)(x-({x} /.a7 $a7moreqn = Reduce[y-(curvecarteqn /. a7incipt) = (-1/(D[curvecarteqn, x] /. a7incipt))(x-({x}))$ $a7 norplot = Plot[Last[List @@ a7 noreqn], {x,({x} /.a7 incipt) [1]]-1,({x} /.a7 incipt) [1]]+1}, Plot[Last[List @@ a7 noreqn], {x,({x} /.a7 incipt) [1]]+1}, Plot[Last[List @@ a7 noreqn], {x,({x} /.a7 incipt) [1]]+1}]+1])$ $a7tanplot = Plot[Last[List @@ a7taneqn], {x,({x} /.a7incipt) [1] -1,({x} /.a7incipt) [1] +1}, Pl$ a7refangle = Reduce[(a6refangle-(-1/(D[curvecarteqn, x] /. a7incipt)))/(1+a6refangle*(-1/(D[a7refeqn = Reduce[y-(curvecarteqn /. a7incipt) == Last[List @@ a7refangle](x-({x} /.a7incipt)[a7refplot = Plot[Last[List @@ a7refeqn], {x,({x} /.a7incipt) [1]-4,({x} /.a7incipt) [1]+1}]; Show[sourceline, curve, a1tanplot,a1norplot,a1refplot,a2norplot, a2refplot, a3tanplot,a3norplo

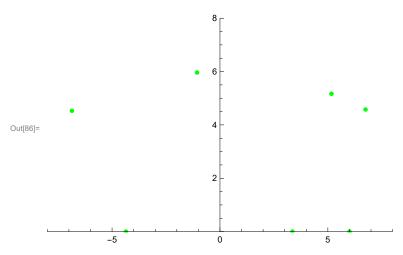
```
Out[76]= \{x \rightarrow -6.86151\}
Out[77]= y == 7.47126 + 0.428844 x
Out[78]= y == -11.4713 - 2.33185 x
Out[81]= m == -3.17522
```



Plot of points of intersection

interpts = $\{\{x/.alincipt, (curvecarteqn /. alincipt)\}, \{a2incipt, 0\}, \{x /.a3incipt, (curvecarteqn)\}\}$ In[85]:= $ptplot = ListPlot[interpts, PlotRange \rightarrow \{\{-8, 8\}, \{0, 8\}\}, PlotStyle \rightarrow \{Green\}]$

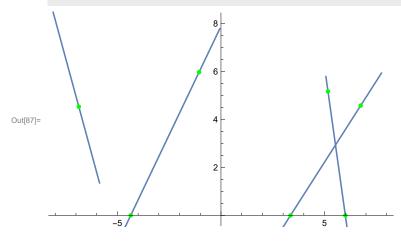
 $\texttt{Out[85]=} \ \{ \{ \textbf{5.16601}, \, \textbf{5.16601} \}, \, \{ \textbf{6.00383}, \, \textbf{0} \}, \, \{ \textbf{6.74625}, \, \textbf{4.57775} \}, \\$ $\{3.35734, 0\}, \{-1.05854, 5.96498\}, \{-4.35714, 0\}, \{-6.86151, 4.52874\}\}$



Plot of reflected rays

In[87]:=

 $Show[a1refplot,a3refplot,a5refplot,a7refplot,ptplot,PlotRange \rightarrow \{\{-8,\ 8\},\{0,\ 8\}\},\ AxesOrigin \rightarrow \{\{-8,\ 8$



Now we have to consider the incident points on the plane mirrors as source if they produce any further reflection. Each point source will lead to a different orthotomic curve. (If the light rays from the sources were parallel we have a relation among them in this case.)

Plotting orthotomic points for each incident point on curve with the respective source

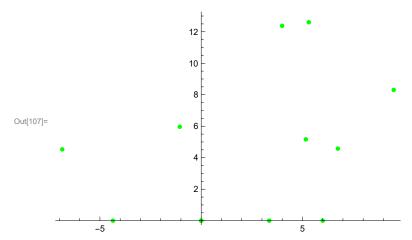
```
a = 0.322876; b=1; c=-6.83399;
In[88]:=
         source = \{0, 0\}
         x = (b(b*source[1]-a*source[2])-a*c)/(a^2+b^2); y=(a(-b*source[1]+a*source[2])-b*c)/(a^2+b^2);
         points = {Last[List @@ Reduce[source[1]]-x=x-m, m]],Last[List @@ Reduce[source[2]]-y=y-m, m]]
         AppendTo[interpts, points]
         ptplot = ListPlot[interpts, PlotRange→Full,PlotStyle→{Green}]
Out[89]= \{0, 0\}
Out[91]= \{3.99644, 12.3776\}
\texttt{Out} \texttt{[92]=} \ \{ \{ \texttt{5.16601}, \, \texttt{5.16601} \}, \, \{ \texttt{6.00383}, \, \texttt{0} \}, \, \{ \texttt{6.74625}, \, \texttt{4.57775} \}, \, \{ \texttt{3.35734}, \, \texttt{0} \}, \\
         \{-1.05854, 5.96498\}, \{-4.35714, 0\}, \{-6.86151, 4.52874\}, \{3.99644, 12.3776\}\}
                                      10
                                       8
Out[93]=
            -6
         a = 0.4216405353733948; b=1; c=-7.422245928559704;
In[94]:=
         source = {6.003831069285709`,0}
         x = (b(b*source[1]-a*source[2])-a*c)/(a^2+b^2); y=(a(-b*source[1]+a*source[2])-b*c)/(a^2+b^2);
         points2 = {Last[List @@ Reduce[source[1]-x==x-m, m]],Last[List @@ Reduce[source[2]-y==y-m, m]
         AppendTo[interpts, points2];
         AppendTo[interpts, {0, 0}];
         ptplot = ListPlot[interpts, PlotRange→Full,PlotStyle→{Green}]
Out[95]= \{6.00383, 0\}
Out[97]= \{9.50559, 8.30509\}
                                12
                                10
Out[100]=
```

-5

```
a = 0.4216405353733948; b=1; c=-7.422245928559704;
In[101]:=
         source = {0,0}
          x = (b(b*source[1]-a*source[2])-a*c)/(a^2+b^2); y=(a(-b*source[1]+a*source[2])-b*c)/(a^2+b^2); 
         points 3 = \{Last[List @@ Reduce[source[1]] - x == x - m, \ m]], Last[List @@ Reduce[source[2]] - y == y - m, \ m]\}
         AppendTo[interpts, points3];
         AppendTo[interpts, {0, 0}];
         ptplot = ListPlot[interpts, PlotRange \rightarrow Full, PlotStyle \rightarrow \{Green\}]
```

Out[102]= $\{0, 0\}$

Out[104]= $\{5.31427, 12.6038\}$



```
a = -0.0661585; b=1; c=-6.03502;
In[108]:=
                          source = \{0,0\}
                          x = (b(b*source[1] - a*source[2]) - a*c)/(a^2+b^2); y = (a(-b*source[1] + a*source[2]) - b*c)/(a^2+b^2);
                          points3 = {Last[List @@ Reduce[source[1]-x==x-m, m]],Last[List @@ Reduce[source[2]-y==y-m, m]
                          AppendTo[interpts, points3];
                          AppendTo[interpts, {0, 0}];
                          a = -0.0661585; b=1; c=-6.03502;
                          source = {6.003831069285709`,0}
                          x = (b(b*source[1]-a*source[2])-a*c)/(a^2+b^2); y=(a(-b*source[1]+a*source[2])-b*c)/(a^2+b^2);
                          points3 = {Last[List @@ Reduce[source[[1]]-x=:x-m, m]],Last[List @@ Reduce[source[[2]]-y==y-m, m]
                          AppendTo[interpts, points3]
                          a = -0.428844; b=1; c=-7.47126;
                          source = \{0,0\}
                          x = (b(b*source[1]-a*source[2])-a*c)/(a^2+b^2); y=(a(-b*source[1]+a*source[2])-b*c)/(a^2+b^2);
                          points3 = {Last[List @@ Reduce[source[1]-x=x-m, m]],Last[List @@ Reduce[source[2]-y=y-m, m]
                          AppendTo[interpts, points3];
                          AppendTo[interpts, {0, 0}];
                          a = -0.428844; b=1; c=-7.47126;
                          source = {6.003831069285709`,0}
                          x = (b(b*source[1]-a*source[2])-a*c)/(a^2+b^2); y=(a(-b*source[1]+a*source[2])-b*c)/(a^2+b^2);
                          points3 = {Last[List @@ Reduce[source[[1]]-x==x-m, m]],Last[List @@ Reduce[source[[2]]-y==y-m, m]
                          AppendTo[interpts, points3]
                         ptplot = ListPlot[interpts, PlotRange→Full,PlotStyle→{Green}]
 Out[109]= \{0, 0\}
 Out[111]= \{-0.795056, 12.0174\}
 Out[115]= \{6.00383, 0\}
 Out[117]= \{5.15645, 12.8084\}
 \texttt{Out[118]} = \{\{5.16601, 5.16601\}, \{6.00383, 0\}, \{6.74625, 4.57775\}, \{3.35734, 0\}, \{-1.05854, 5.96498\}, \{0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0685, 0.0
                          \{-4.35714, 0\}, \{-6.86151, 4.52874\}, \{3.99644, 12.3776\}, \{9.50559, 8.30509\}, \{0, 0\},
                          \{5.31427, 12.6038\}, \{0, 0\}, \{-0.795056, 12.0174\}, \{0, 0\}, \{5.15645, 12.8084\}\}
 Out[120]= \{0, 0\}
 Out[122]= \{-5.41259, 12.6214\}
 Out[126]= \{6.00383, 0\}
 Out[128]= \{-1.27402, 16.9709\}
 \texttt{Out[129]=} \ \{ \{ 5.16601, 5.16601 \}, \{ 6.00383, 0 \}, \{ 6.74625, 4.57775 \}, \{ 3.35734, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \}, \{ 6.00383, 0 \},
                          \{-1.05854, 5.96498\}, \{-4.35714, 0\}, \{-6.86151, 4.52874\}, \{3.99644, 12.3776\},
                          \{9.50559, 8.30509\}, \{0, 0\}, \{5.31427, 12.6038\}, \{0, 0\}, \{-0.795056, 12.0174\},
                          \{0, 0\}, \{5.15645, 12.8084\}, \{-5.41259, 12.6214\}, \{0, 0\}, \{-1.27402, 16.9709\}\}
```

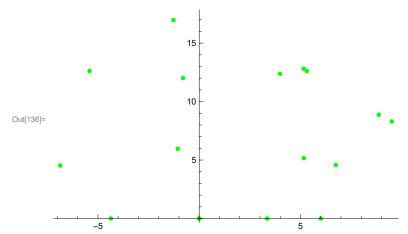
```
15
                                            10
Out[130]=
                    -5
                                                                        5
```

```
a = 0.322876; b=1; c=-6.83399;
In[131]:=
        source = {6.003831069285709`,0}
        x = (b(b*source[1]-a*source[2])-a*c)/(a^2+b^2); y=(a(-b*source[1]+a*source[2])-b*c)/(a^2+b^2);
        points = {Last[List @@ Reduce[source[1]-x=x-m, m]],Last[List @@ Reduce[source[2]-y=y-m, m]]
        AppendTo[interpts, points]
        ptplot = ListPlot[interpts, PlotRange→Full,PlotStyle→{Green}]
```

Out[132]= $\{6.00383, 0\}$

Out[134]= $\{8.86666, 8.86665\}$

 $\texttt{Out[135]=} \ \{ \{5.16601, \, 5.16601\}, \, \{6.00383, \, 0\}, \, \{6.74625, \, 4.57775\}, \, \{3.35734, \, 0\}, \, \{-1.05854, \, 5.96498\}, \, \{-1.05854, \, 5.964$ $\{-4.35714, 0\}, \{-6.86151, 4.52874\}, \{3.99644, 12.3776\}, \{9.50559, 8.30509\}, \{0, 0\},$ $\{5.31427, 12.6038\}, \{0, 0\}, \{-0.795056, 12.0174\}, \{0, 0\}, \{5.15645, 12.8084\},$ $\{-5.41259,\ 12.6214\},\ \{0,\ 0\},\ \{-1.27402,\ 16.9709\},\ \{8.86666,\ 8.86665\}\}$



```
cata = ResourceFunction["CatacausticCurvePlot"][curveparaeqn, {0,0},{t, 0.2, 1,.5}, Axes→True
In[137]:=
        orthoorigin = ResourceFunction["Orthotomic"][curveparaeqn, t]
        orthodiff = ResourceFunction["Orthotomic"][curveparaeqn, {6.003831069285709,0},t]
        orthoplot = ParametricPlot[orthoorigin , {t, -2, 12}];
        orthoplot2 = ParametricPlot[orthodiff , \{t, -2,12\}, ColorFunction \rightarrow "Rainbow"];\\
        Show[orthoplot,orthoplot2, sourceline, curve, a1tanplot,a1norplot,a1refplot,a2norplot, a2refpl
```

