

If \mathbf{P}_{refl} is a negative identity matrix and \mathbf{P}_{refl2} is the identity matrix scaled by r_{refl2} as suggested in the main write-up, then $\mathbf{G} = -r_{refl2}\mathbf{N}^2$ and

$$\mathbf{G} = \mathbf{N}_2^2 = -r_{refl2} \begin{bmatrix} 1 & ik_0 h_2 n_2^2 \\ ik_0 h_2 \cos^2 \theta_2 & 1 \end{bmatrix}^2 = \begin{bmatrix} p_2 & -p_2 \\ 1 & 1 \end{bmatrix} (-r_{refl2}) \begin{bmatrix} 1 + ik_0 h_2 n_2 \cos \theta_2 & 0 \\ 0 & 1 - ik_0 h_2 n_2 \cos \theta_2 \end{bmatrix}^2 \begin{bmatrix} \frac{1}{2p_2} & \frac{1}{2} \\ \frac{-1}{2p_2} & \frac{1}{2} \end{bmatrix}$$

This is convenient because $\mathbf{G}^L = \mathbf{S}(-r_{refl2})^L \mathbf{\Lambda}^L \mathbf{S}^{-1}$ meaning that for any power the diagonal in the middle is just made of two binomial expansions of the form $(1 \pm ia)^{2L}$ for $a = k_0 h_2 n_2 \cos \theta_2$. This means the full model would be (in various configurations):

$$\frac{1}{r_{refl2}} \mathbf{S} \left(\sum_{K=1}^L (-r_{refl2})^K \mathbf{\Lambda}^K \right) \mathbf{S}^{-1} \begin{bmatrix} A_1 + R_1 \\ p_1(A_1 - R_1) \end{bmatrix} + \begin{bmatrix} R_1 \\ p_1 R_1 \end{bmatrix} = \begin{bmatrix} R_{tot} \\ p_1 R_{tot} \end{bmatrix}$$

or

$$\frac{1}{r_{refl2}} \begin{bmatrix} p_2 & -p_2 \\ 1 & 1 \end{bmatrix} \left(\sum_{K=1}^L (-r_{refl2})^K \begin{bmatrix} (1 + ia)^{2K} & 0 \\ 0 & (1 - ia)^{2K} \end{bmatrix} \right) \begin{bmatrix} \frac{A_1}{2} \left(\frac{1}{p_2} + p_1 \right) + \frac{R_1}{2} \left(\frac{1}{p_2} - p_1 \right) \\ \frac{A_1}{2} \left(p_1 - \frac{1}{p_2} \right) - \frac{R_1}{2} \left(p_1 + \frac{1}{p_2} \right) \end{bmatrix} + \begin{bmatrix} R_1 \\ p_1 R_1 \end{bmatrix} = \begin{bmatrix} R_{tot} \\ p_1 R_{tot} \end{bmatrix}$$

or

$$\frac{1}{r_{refl2}} \begin{bmatrix} p_2 & -p_2 \\ 1 & 1 \end{bmatrix} \left(\sum_{K=1}^L (-r_{refl2})^K \begin{bmatrix} (1 + ia)^{2K} \left(\frac{A_1}{2} \left(\frac{1}{p_2} + p_1 \right) + \frac{R_1}{2} \left(\frac{1}{p_2} - p_1 \right) \right) \\ (1 - ia)^{2K} \left(\frac{A_1}{2} \left(p_1 - \frac{1}{p_2} \right) - \frac{R_1}{2} \left(p_1 + \frac{1}{p_2} \right) \right) \end{bmatrix} \right) + \begin{bmatrix} R_1 \\ p_1 R_1 \end{bmatrix} = \begin{bmatrix} R_{tot} \\ p_1 R_{tot} \end{bmatrix}$$

Some other useful equations:

$$p_2 = n_2 \cos \theta_2$$

$$\cos \theta_2 = \sqrt{1 - \frac{n_1^2 \sin^2 \theta_1}{n_2^2}}$$

$$R_1 = A_1 \frac{p_1 - p_2}{p_1 + p_2} = A_1 r_1$$

$$a = k_0 h_2 n_2 \cos \theta_2$$

$$n_2 \approx \sqrt{\varepsilon_2}$$

$$r_{refl2} = \frac{p_2 - p_1}{p_1 + p_2}$$