

PHYS 615 – HW 5

Types of homework questions

- RQ (Reading questions): prompt you to go back to the text and read and think about the text more carefully and explain in your own words. While not directly tested in quizzes, can help you think more deeply about quiz questions.
- BF (Building foundations): gives you an opportunity to build and practice foundational skills that you have, presumably, seen before.
- TQQ (typical quiz questions): Similar questions (though perhaps longer or shorter) will be asked on quizzes. But the difficulty level and skills tested will be similar.
- Design (D): These are questions in which you are given a desired outcome and asked to figure out how to make it happen. These will often also be TQQ's, but always starting with desired motion/behavior as the given.
- COMP (Computing): computing questions often related to TQQ but will never be asked on a quiz (since debugging can take so long). You will need to do at least four computing questions over the semester
- FC (free choice): allows you to decide where to put your time. Any of the following are possible: work through a section of the text or a lecture in detail; redo a problem from before; do an unassigned problem in the text; extend a computing project; try a problem using a different analytical approach (e.g. forces instead of conservation of energy).
- ACT (in-class activity): These questions are repeats of questions (or similar to) that occurred in a previous in-class activity.
- **Standard Reading Questions:** How does the reading connect with what you already know? What was something new? Ask an "I wonder" question OR give an example applying the idea in the reading.

Please remember to say something about the "Check/Learn" part at the end of solving a problem!

Note that while this homework does not have designated "RQ" questions, in particular the activity-based questions can certainly benefit from reading the corresponding sections in the text.

Full credit will be given at 75% of the total points possible, so you can choose a subset of problems (you can do more / all, but the score is capped at 75%)

1. TQQ / ACT (25 points) Hand in Activity 3.1 (except the challenge problem. You could use the challenge problem as your free choice problem.)
2. TQQ / ACT (20 points) Hand in Activity 3.2.
3. TQQ / ACT (15 points) Hand in Activity 3.3.
4. TQQ (10 points)

A uniform thin sheet of metal is cut into the shape of a semicircle of radius R and lies in the x - y plane with its center at the origin and diameter along the x axis. Find the position of the CM using polar coordinates. [In this case, Taylor's Eq. (3.9) becomes a two-dimensional integral of the form $\int \vec{r} \sigma dA$, where σ denotes the surface mass density (mass / area) and dA is the element of area $dA = r dr d\phi$.]

5. TQQ (10 points)

- (a) A vector \vec{a} of magnitude $a = |\vec{a}|$ lies along the x direction. A second vector, \vec{b} of magnitude b is rotated counterclockwise from the x axis by an angle of ϕ . As we (hopefully) know, the direction of the cross product $\vec{a} \times \vec{b}$ is given by the right-hand rule, and the magnitude is $ab \sin \theta$, where θ is the angle between the two vectors.

Write down $\vec{a} \times \vec{b}$ using the above formula in vector components notation (ie., using components and unit vectors $\hat{x}, \hat{y}, \hat{z}$).

Write down \vec{a} and \vec{b} individually in vector component notation.

Use the "determinant rule" to calculate the cross product. Does it match what you wrote down before? Does that meet your expectations? (See bottom of <https://betterexplained.com/articles/cross-product/> for calculating the cross product with the determinant, though it's probably what you usually use in any case.)

- (b) If the vectors \vec{a} and \vec{b} form two of the sides of a triangle, show that $\frac{1}{2}|\vec{a} \times \vec{b}|$ is equal to the area of that triangle.

6. RQ / TQQ (10 points)

A particle moves under the influence of a central force directed toward a fixed origin O .

- (a) Explain why the particle's angular momentum about O is constant.
- (b) Give in detail the argument that the particle's orbit must lie in a single plane containing O .

7. FC (10 points) (free choice): allows you to decide where to put your time. Any of the following are possible: work through a section of the text or a lecture in detail; polish up a group work assignment from class; redo a problem from before; do an unassigned problem in the text; extend a computing project; try a problem using a different analytical approach (e.g. forces instead of conservation of energy).