

## TUTORIAL 1 · [COMPUTATION AND LOGIC]



### OBJECTIVES

In this tutorial you will:

- meet your tutorial group colleagues, and discuss and work with them;
- learn how to submit your tutorial solutions for marking;
- learn more about *Venn diagrams*, *decision trees*, and *encodings*.



### TASKS

Exercises 1–6 are mandatory. Exercise 7 is optional.



**DEADLINE** Saturday, 26th of September, 4PM UK time

## **Good Scholarly Practice**

*Please remember the good scholarly practice requirements of the University regarding work for credit.*

*You can find guidance at the School page*

*<http://web.inf.ed.ac.uk/infweb/admin/policies/academic-misconduct>.*

*This also has links to the relevant University pages. Please do not publish solutions to these exercises on the internet or elsewhere, to avoid others copying your solutions.*



## **I. We're all different. And that's a good thing!**

In the first part of the tutorial, we'll explore and celebrate diversity.


*You'll start getting to know your colleagues by focusing on qualities which make you uniquely you. You'll use Venn diagrams and decision trees to help you visualize and reason about differences between the members of your group.*


# EXERCISE 1

MANDATORY |  BEFORE TUTORIAL SESSION

There are 6 students in your tutorial group. During the tutorial session, you will meet your colleagues. You'll work together for the entire semester, so it's important you get to know each other.


## **Before the session:**


 Think of 3 questions for your colleagues to help you get to know them. The questions should help you identify each student in your group, should admit only true/false answers, and should be sensible – you don't want to be intrusive. The questions shouldn't be too particular either: don't ask for their name.

 Write down your questions: you can either type them and save them in a file, or write them on a piece of paper and then scan or take a picture of the paper.

 Upload the file in the tutorial assignment for week 1 on [Learn](#).


### **At the beginning of the session:**

 Talk to your group colleagues and your tutor. Introduce yourselves: What's your name? Where are you from? Are you already on campus?


 Write down two lists for your group:


- For list A, each of you should name something you are excited about at the start of the academic year.
- For list B, each of you should name something you are an expert at.


Try to think of distinct answers for each of the lists.


 Your tutor has prepared a list of three things about them. But only two of them are true. Each one of you should try to guess which item is false. Then put together your answers and decide on one of them. Did you guess it right?


## EXERCISE 3

MANDATORY |  DURING TUTORIAL SESSION

 Check on Learn the feedback you received for Exercise 1. Ask your tutor for explanations if something's not clear.

 Each of you should read the questions you submitted. Write down all the answers to your questions, including your own. Then draw the corresponding Venn diagram.

 Using the diagram, check if for each of the 3 questions you submitted there exist at least 2 students who replied *true* and at least 2 students who replied *false*. In other words, check if none of your 3 questions singles out (identifies) a student.

 Let your colleagues know if your 3 questions verify the constraint above. If so, you're a winner! Your questions can be used by your group to solve Exercises 4 and 5. If none of you submitted 3 questions that satisfy the constraint, choose together 3 suitable questions to use next.

## EXERCISE 4

MANDATORY | 🕒 DURING TUTORIAL SESSION

📖 A **query** is an expression obtained from binary questions and the connectives *and* (intersection), *or* (union), and *not* (complement).

👥 Check together if there exists a student in your group who can be uniquely identified by a query formed using the 3 questions your group has selected in the previous exercise. If there is one, then how many more students can be uniquely identified by a query?




✎ Change the 3 questions such that each of you 6 can be uniquely identified. Be sure not to break the constraint in Exercise 3.

✎ Draw the decision tree corresponding to your new questions and query, as in **Lecture 1.b**. Using the decision tree, define an encoding for all students. What's your code number?

🧠 How many questions would you need to ask in order to identify all the students in your group (to visit all the leaves of your tree)?

## EXERCISE 5

MANDATORY |  DURING TUTORIAL SESSION

-  Can we obtain the same result as in the previous exercise (identify just as many students with a query) by using just 2 base (binary) questions?
-  What is the minimum number of base questions we need in order to identify each of the 6 students with a query?
-  What about the minimum number of base questions for identifying each of the 450 students in your year?






## II. We have things in common.

Being different is useful when trying to solve complex problems together: every one of us can contribute with things we're experts at. However, it's easy to check that it's often simpler to find things that unite us than things that differentiate us. Let's do the maths!


*In the second part of the tutorial, we'll consider the duals of the questions in the first part to reason about things we have in common and how we are alike.*


## EXERCISE 6


MANDATORY |  DURING TUTORIAL SESSION


 Go back to the questions you submitted for Exercise 1.

Check if each question separates at least 1 student from the group: we don't want the questions to be too general or too inclusive.

 Choose with your group 3 questions that satisfy the constraint above and use them to solve the next tasks. Draw the associated Venn diagram.

 Using the diagram, check if any 2 students are united by one of the questions (they give the same answer to the question). What about by a query?

 Change the 3 questions such that any 2 students are united by a query.

 What is the minimum number of base questions we need such that any 2 students are united by a question? What about by a query? What if we have 450 students instead of 6?

## EXERCISE 7

OPTIONAL |  DURING TUTORIAL SESSION



### What are the odds?

How difficult is it to choose suitable questions for discriminating between or grouping elements of a set?

Obviously, the number of questions is infinite, limited only by one's vocabulary [kudos, mr. Wittgenstein!]. This makes them difficult to analyse. But for the purpose of this tutorial, we can simplify the matter greatly. That is because we are not so much interested in the textual formulation of a question (the words used) as we are in the answers it receives from each of you 6.





So suppose we make no distinction between questions that receive the same answers. For example, if your group comprises students A, B, C, D, E, F, and questions Q1 and Q2 are both answered *true* by A, B, C and *false* by D, E, F, we will consider Q1 and Q2 to be **effectively the same**.





## Individual

-  How many effectively different questions can each of you ask?
-  What is the probability of you asking one of those questions?

## Team power

Now consider triples of questions.

-  How many triples are there? Note that a question in a triple may be effectively the same as another question in that triple.
-  What is the probability of your group to propose one of these triples?
-  Can you compute the number of triples that satisfy the constraint in Exercise 3 (none of the questions individually identifies a student)?
-  What is the probability of proposing one of those triples?

-  Now think of queries that we can form from triples of questions. Each triple may generate several queries. Can we know exactly how many? Is there a minimum number of such queries? How about a maximum?
-  How many triples can generate a query that identifies a student?
-  What is the probability of identifying a student with a query?
-  Can you think of a similar set of tasks to compute the probability of having any 2 students in your group united by 3 questions that satisfy the constraint in Exercise 6?

By comparing these two last probabilities you will see that there is generally a much greater chance of being alike than different.