



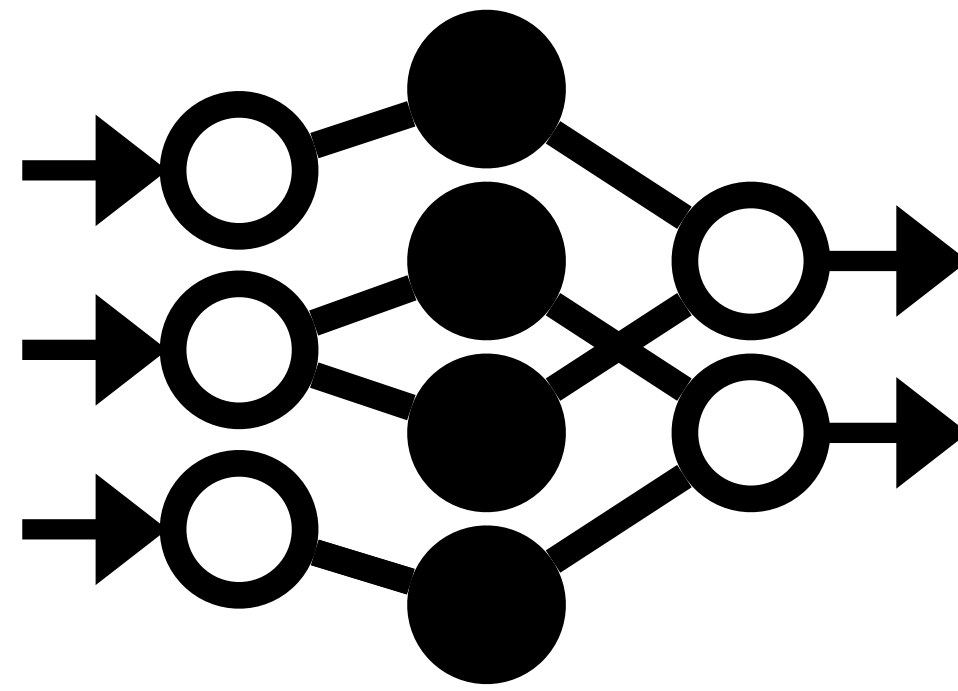
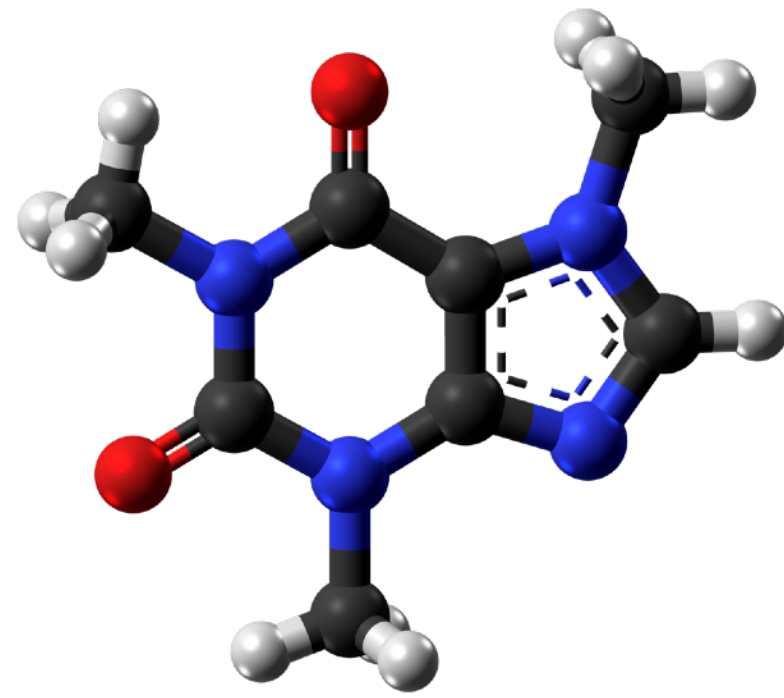
# DEEP SETS ARE VIABLE GRAPH LEARNERS

Gerrit Großmann

28.11.2023



# Predictions on Graphs

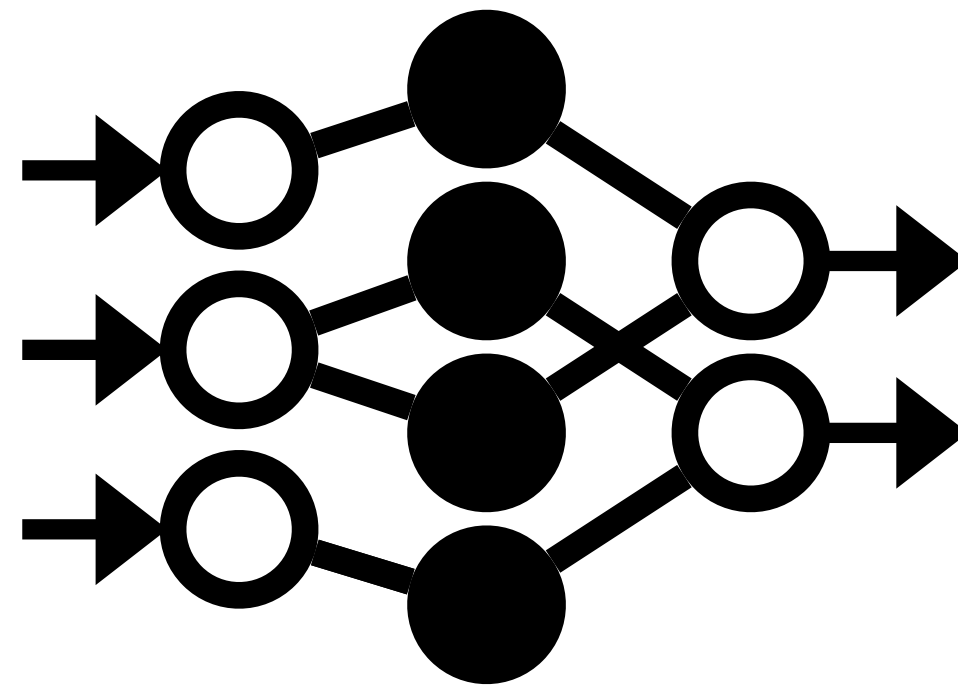
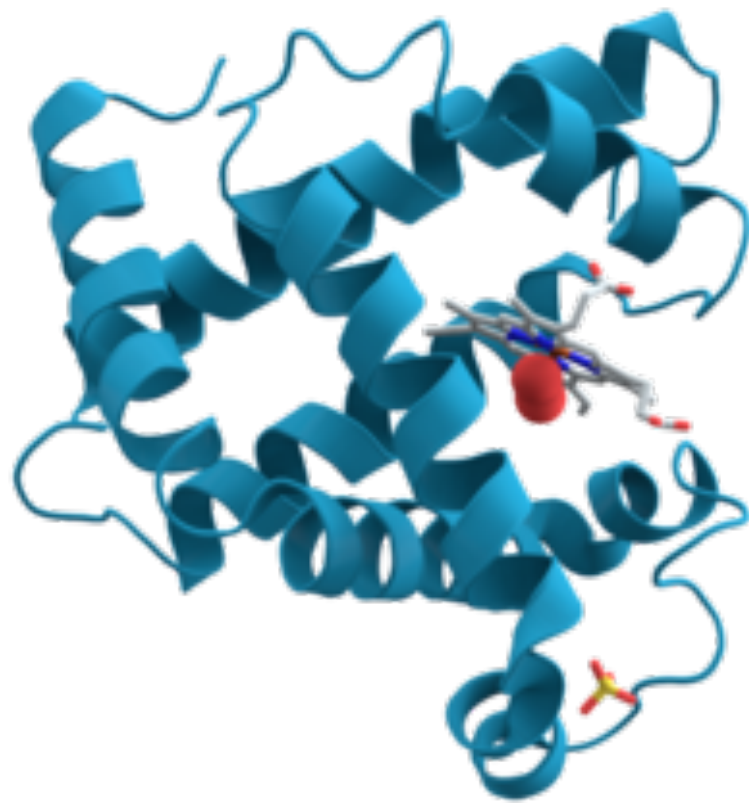


Toxic vs Non-Toxic

In many ways, graphs are the main modality  
of data we receive from nature.

- Petar Veličković

# Predictions on Graphs

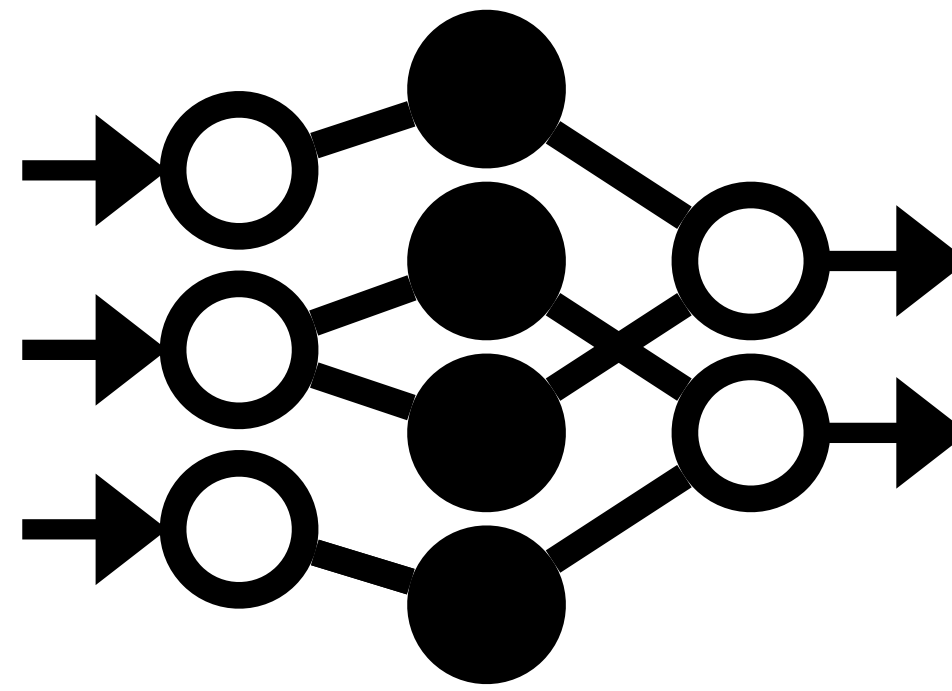
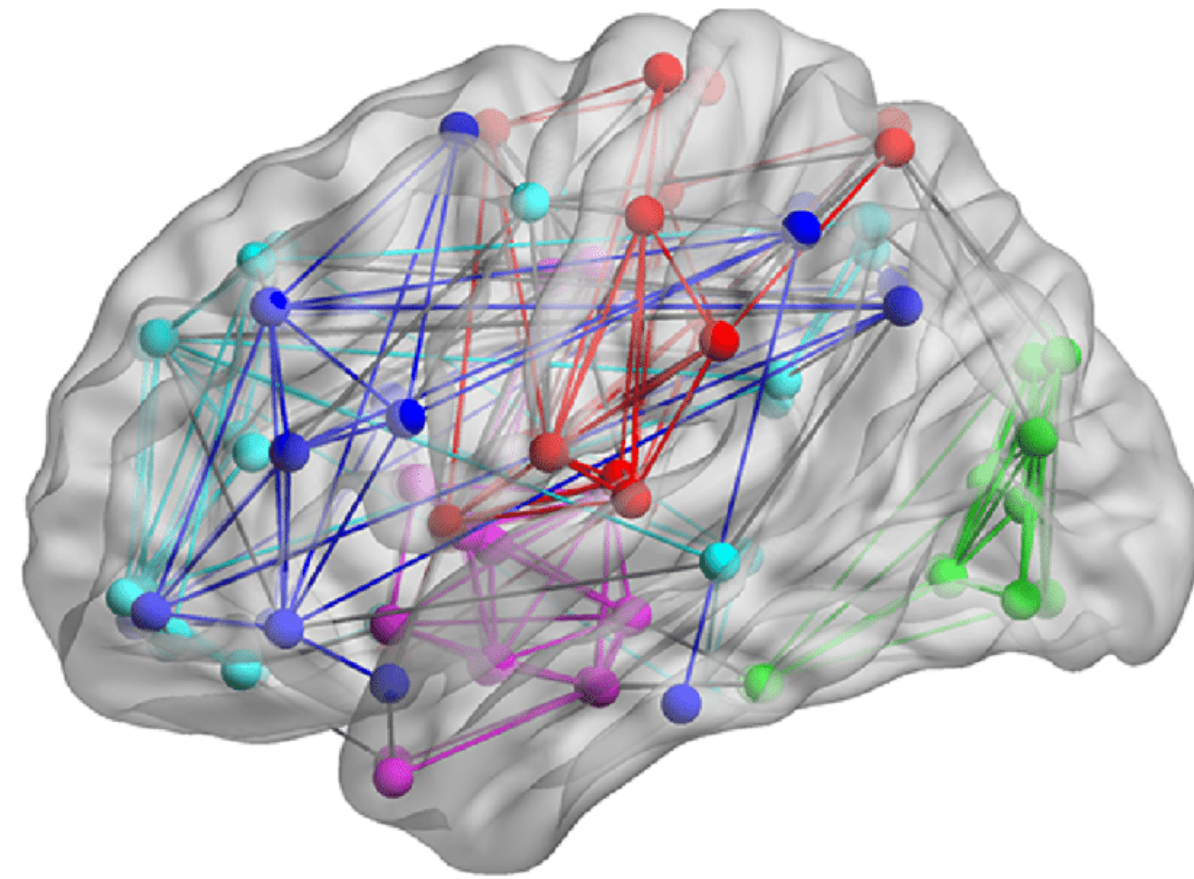


Kinase vs Phosphatase

In many ways, graphs are the main modality  
of data we receive from nature.

- Petar Veličković

# Predictions on Graphs



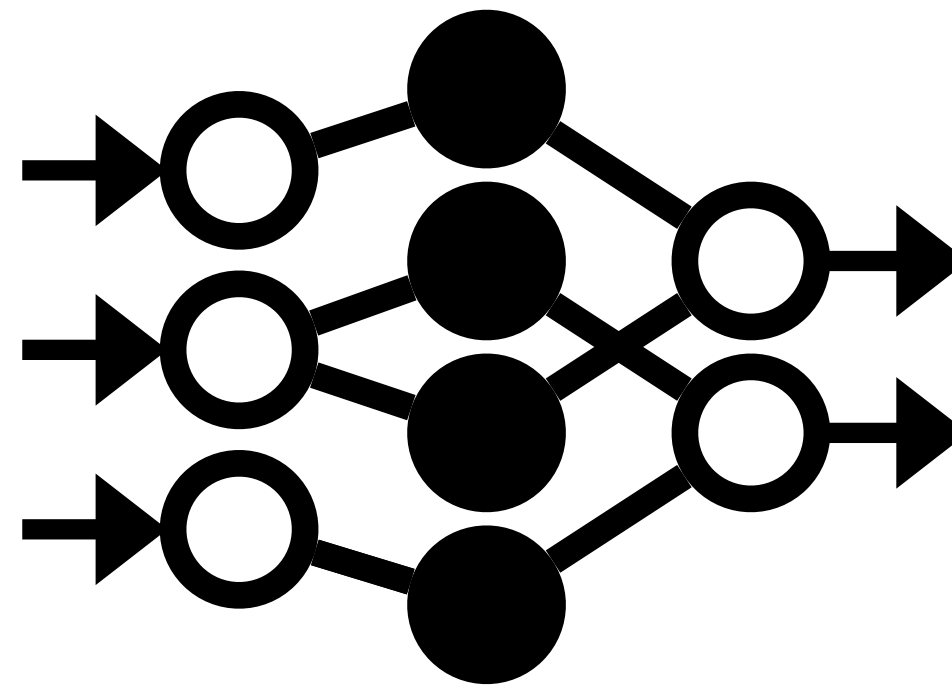
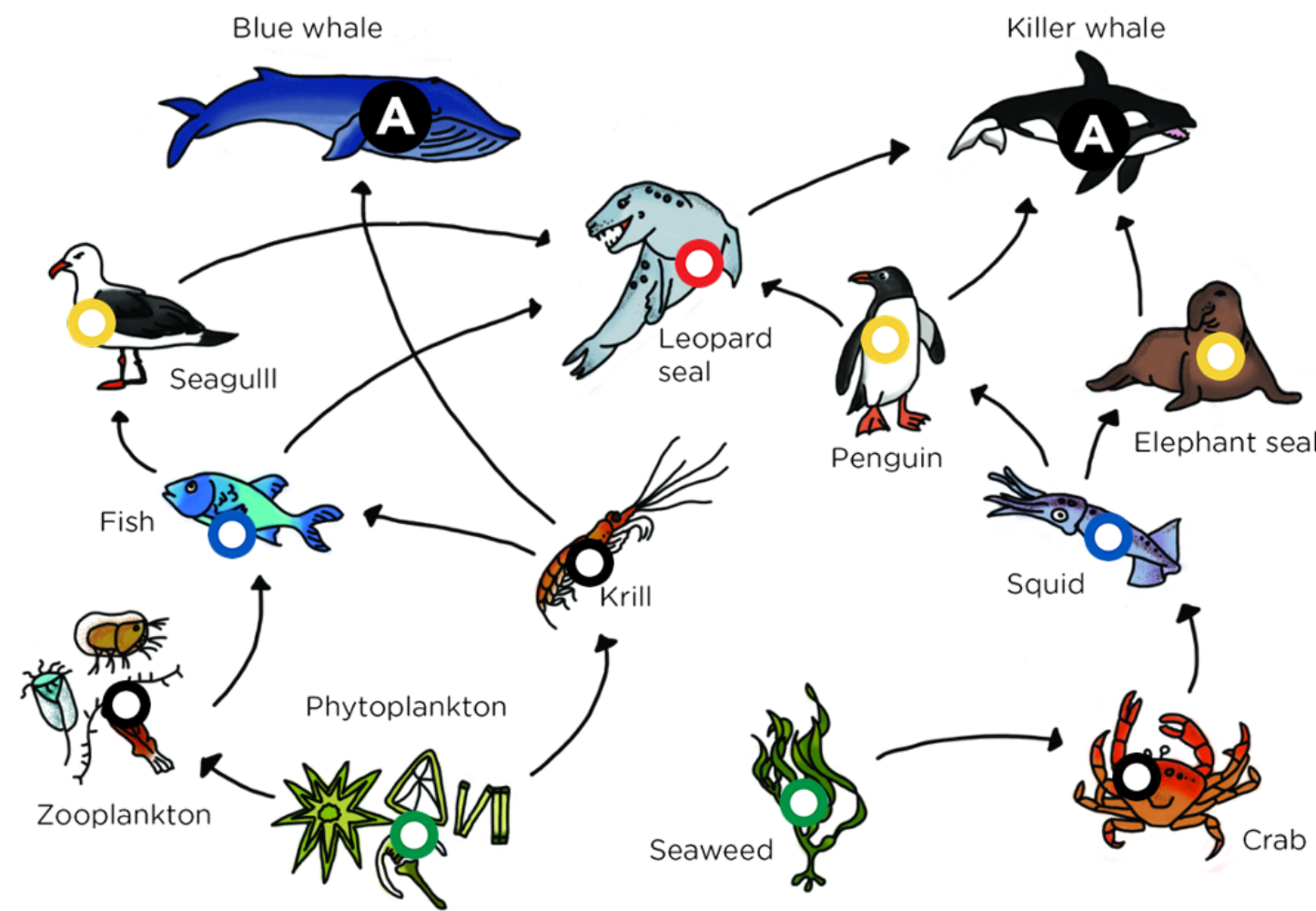
Attentive vs Distracted

In many ways, graphs are the main modality  
of data we receive from nature.

- Petar Veličković



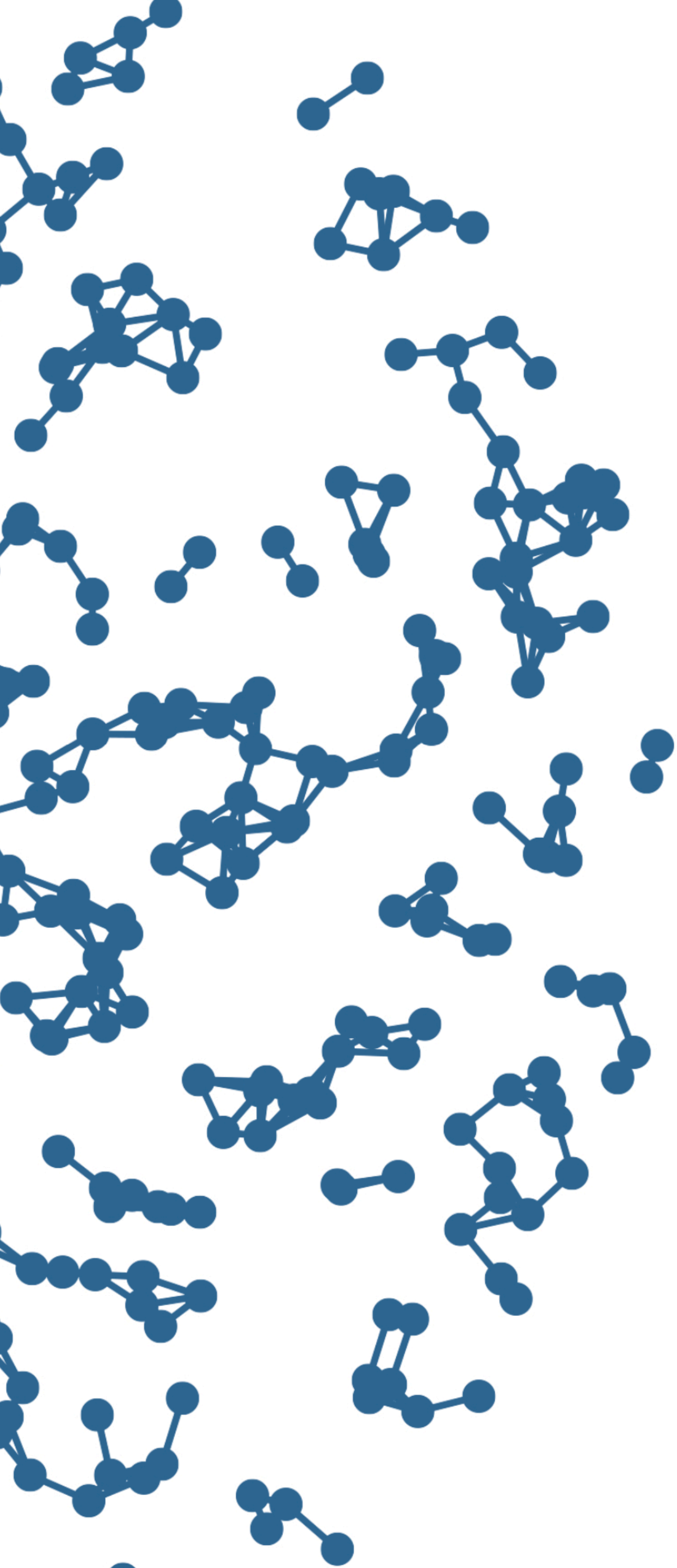
# Predictions on Graphs



Stable vs Endangered

In many ways, graphs are the main modality of data we receive from nature.

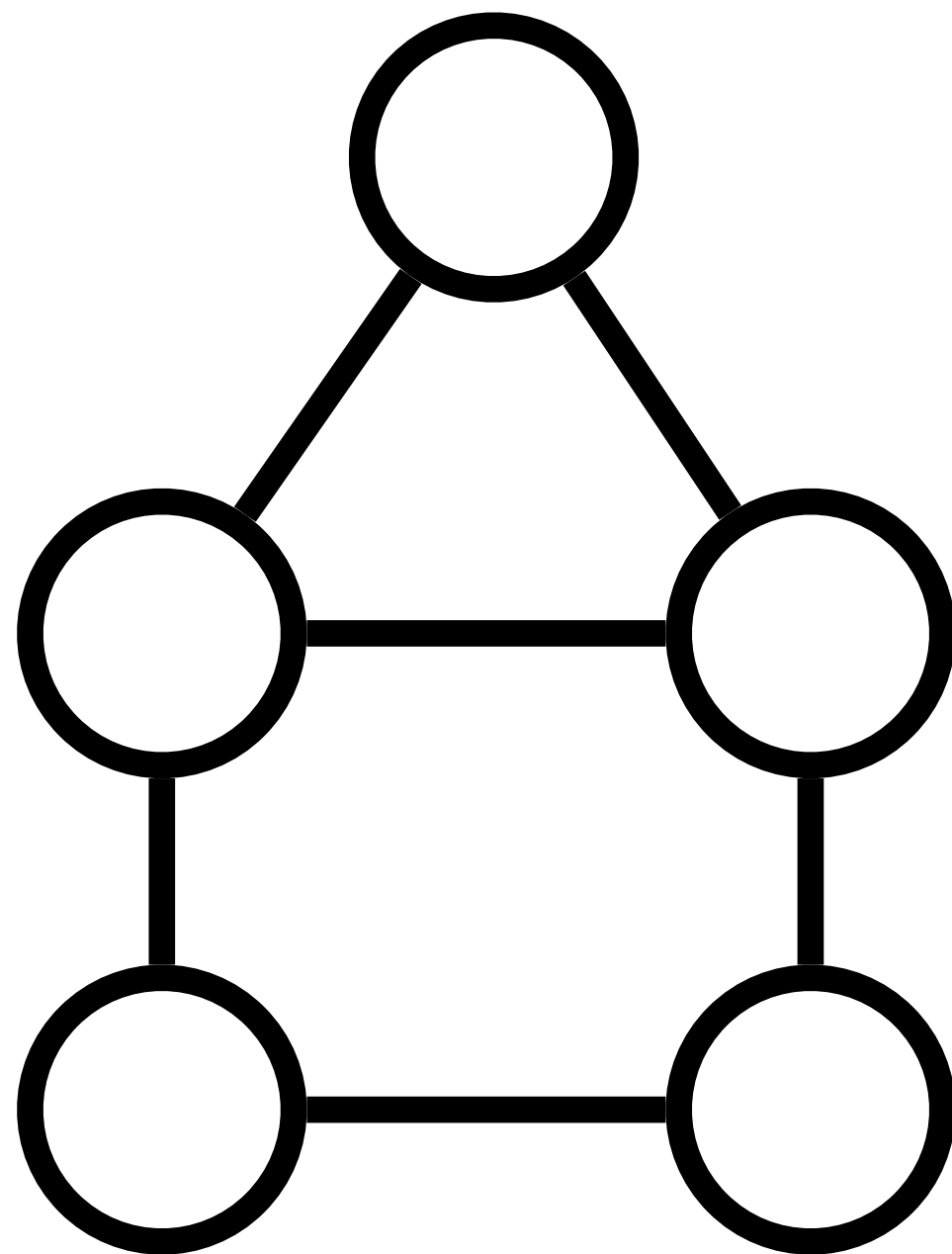
- Petar Veličković



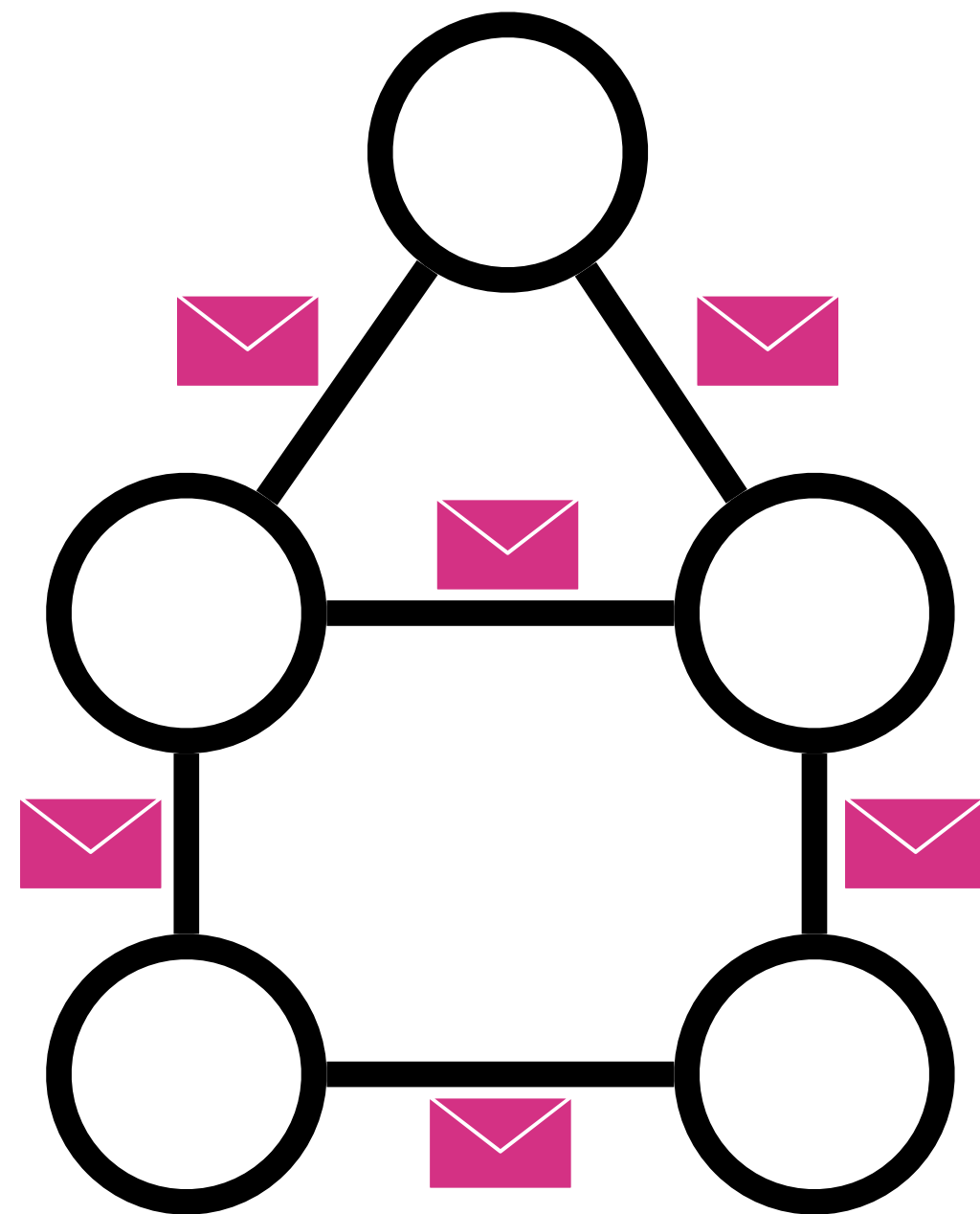
Part I

# MESSAGE PASSING

# Message Passing

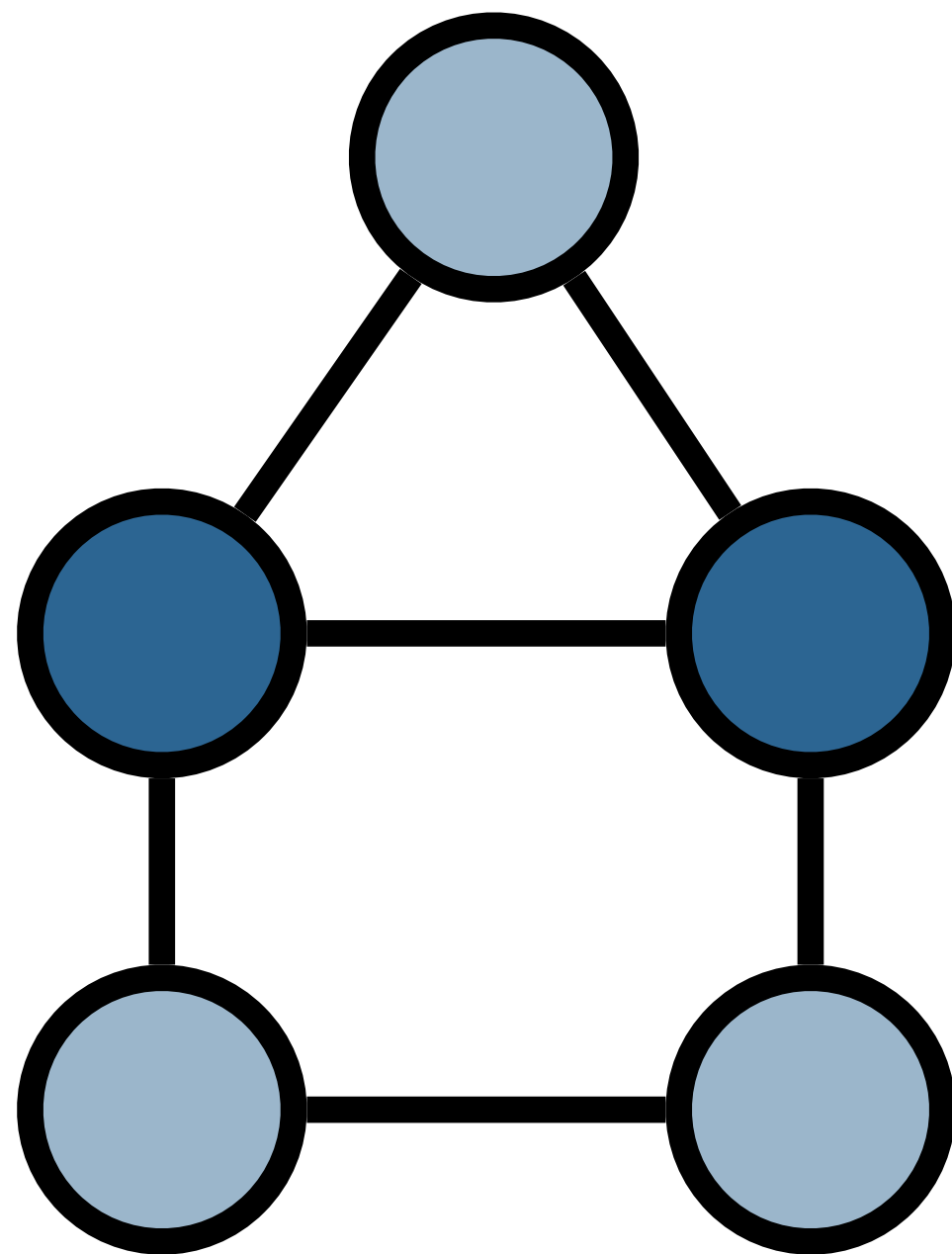


# Message Passing

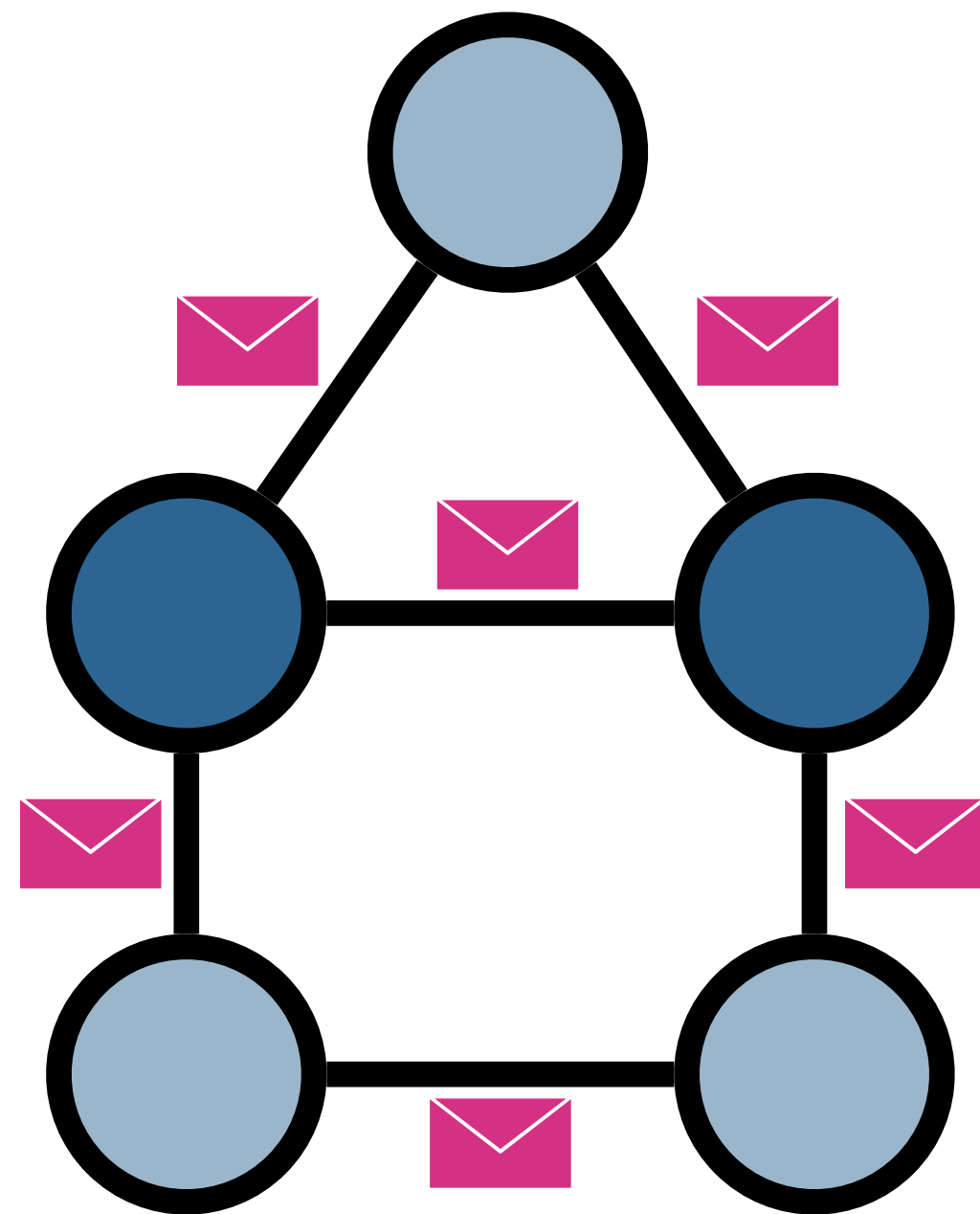




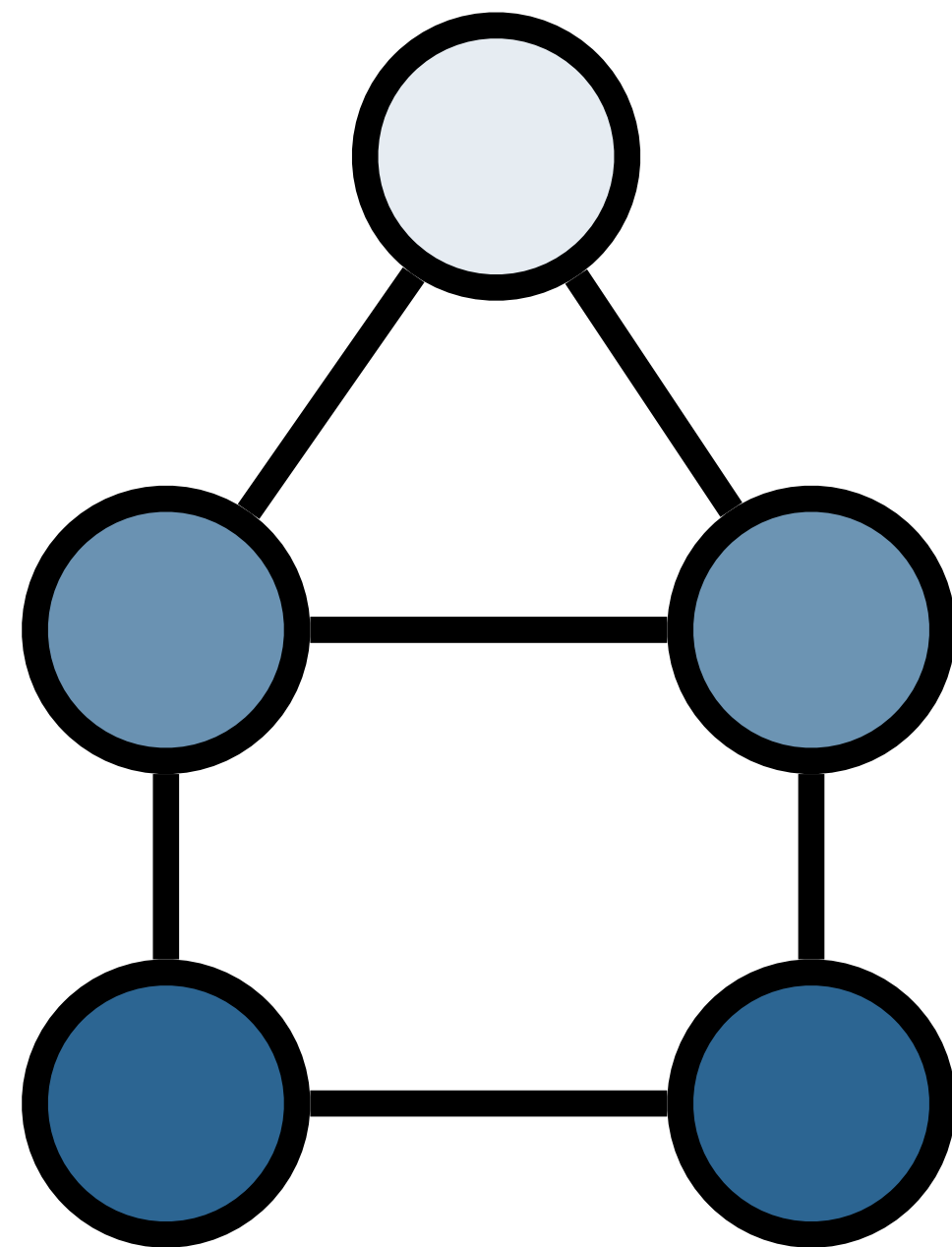
# Message Passing



# Message Passing



# Message Passing

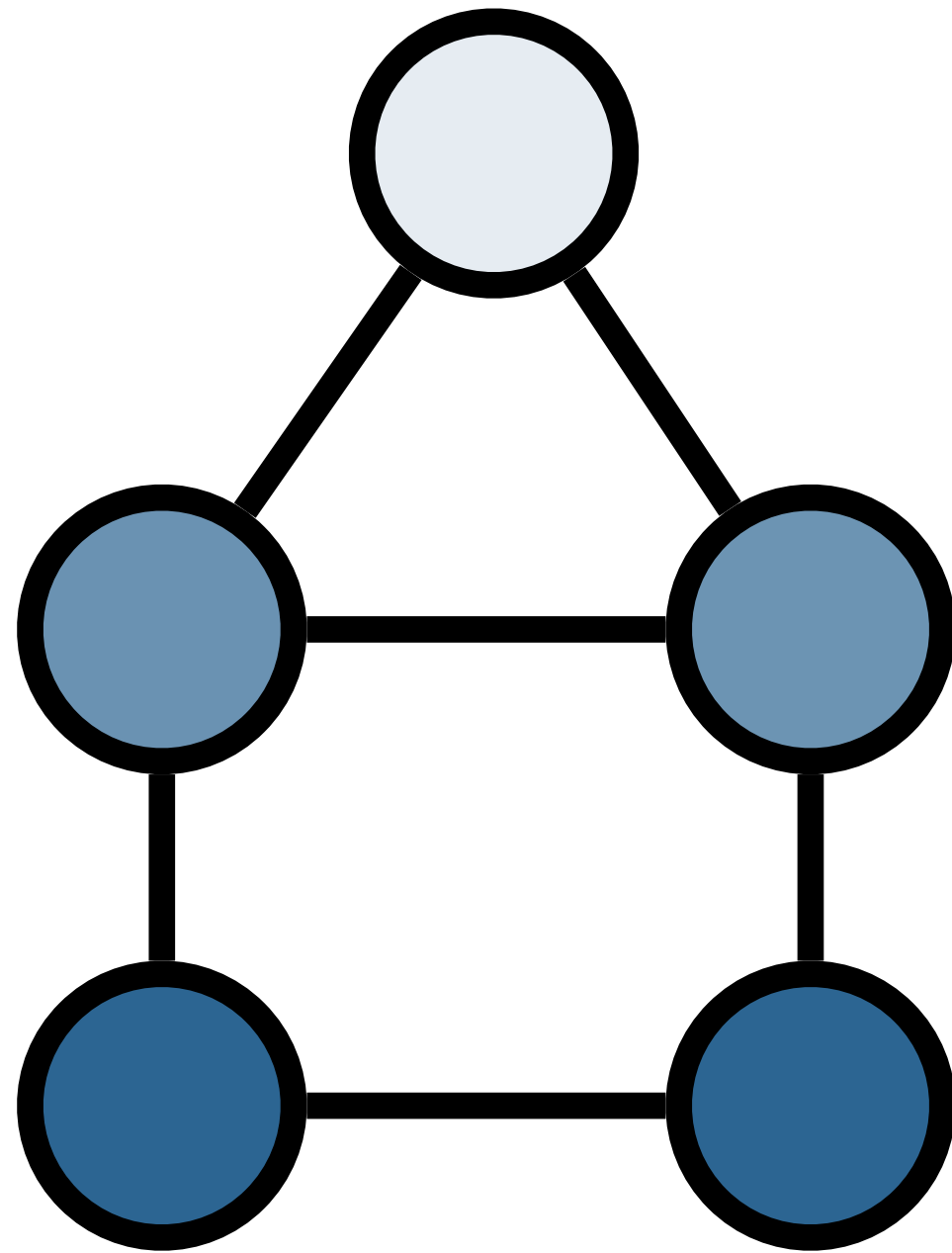


- Input graphs of arbitrary size.
- Isomorphic graphs are guaranteed to produce the same results.

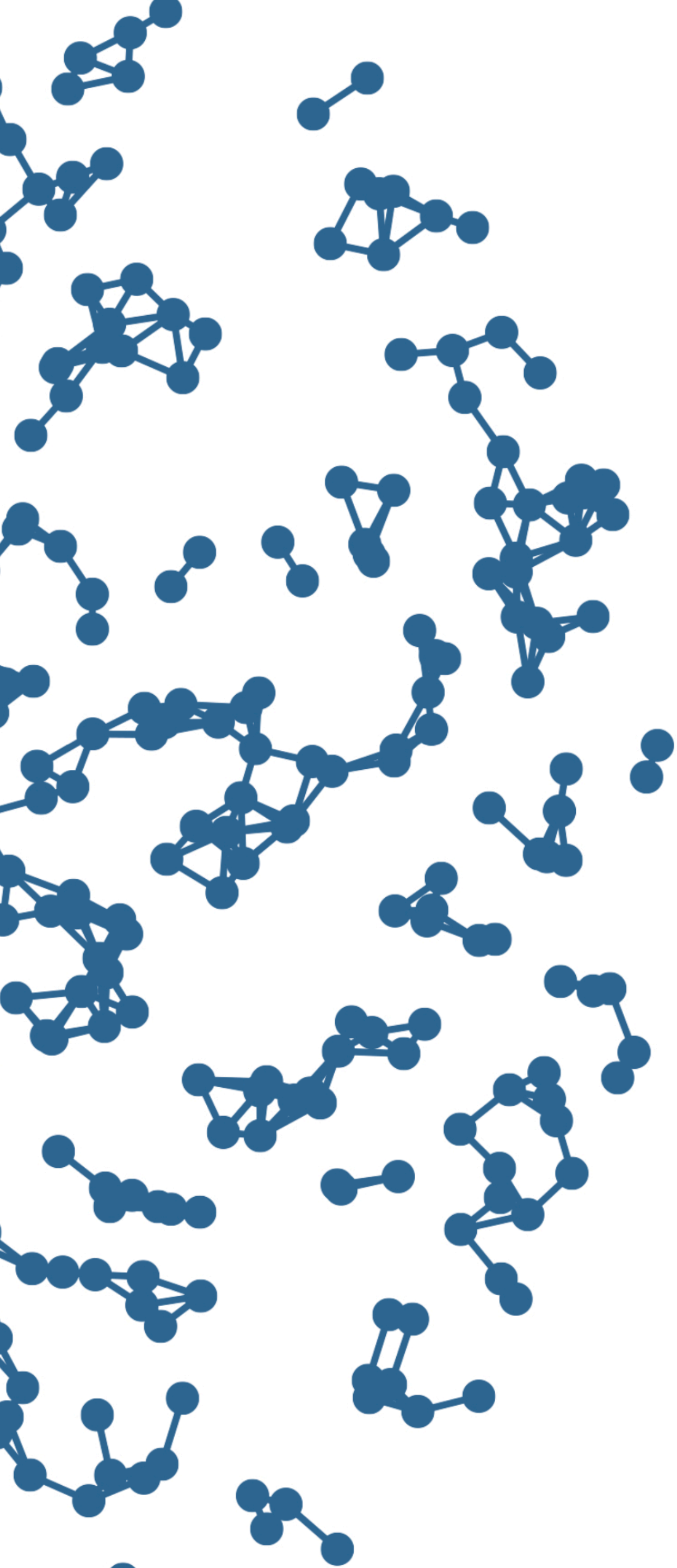


- Pair-wise relations expensive.
- Not very powerful (in their vanilla form)

# Message Passing



Do we really need *message passing* to capture the topology of a graph?



## Part II

# DEEP SETS

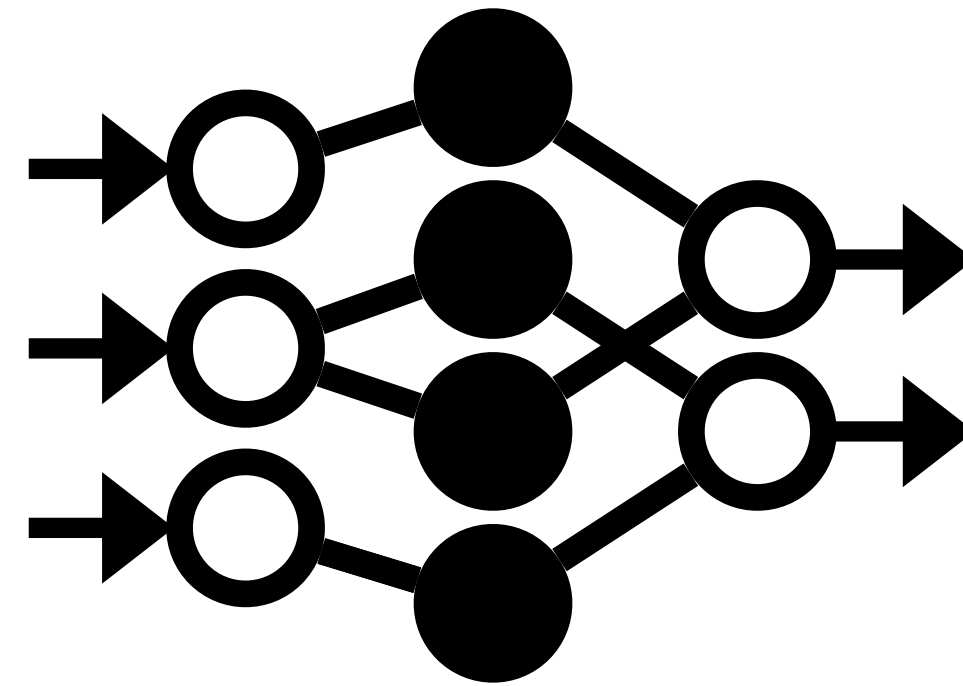


# Deep Sets



**Deep Sets** are neural networks that operate on (multi)sets.

$\{1, 2, 3, 4\}$



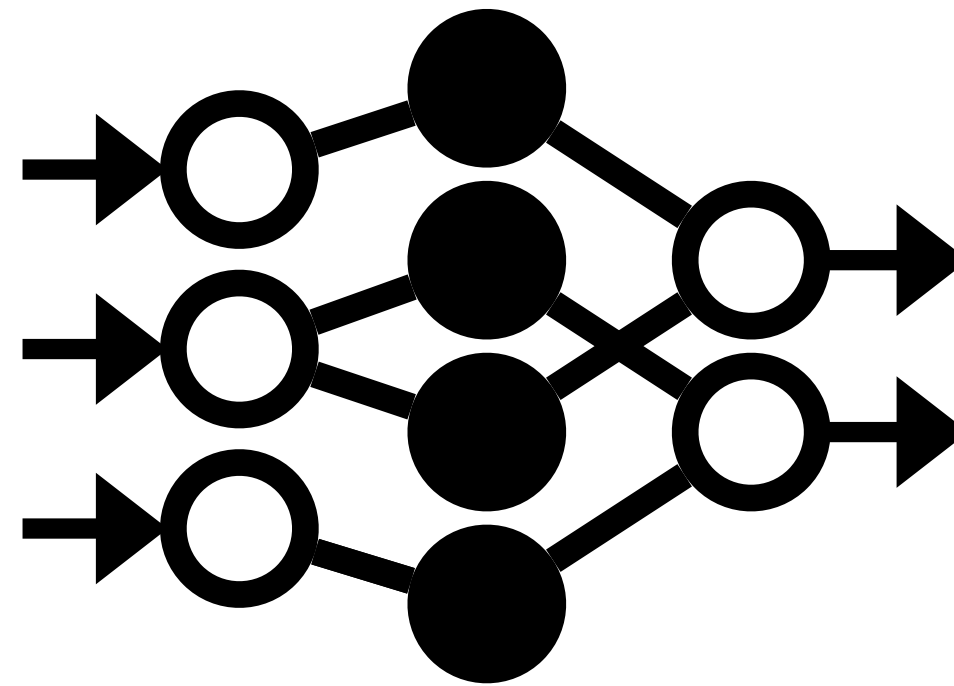
Contains the Number 5

# Deep Sets

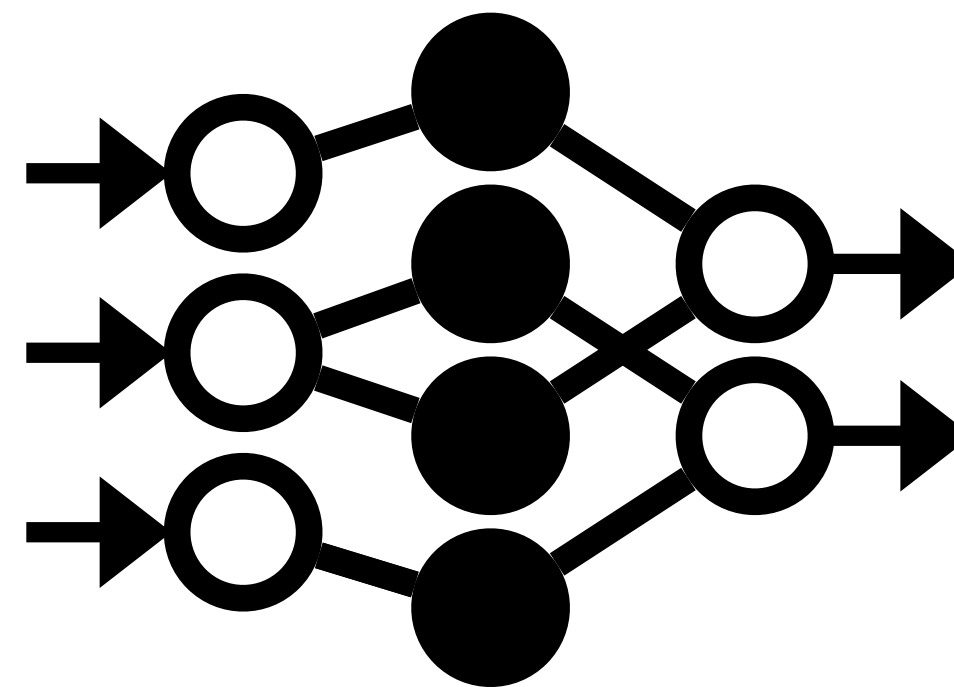


**Deep Sets** are neural networks that operate on (multi)sets.

[1,2,3,4]

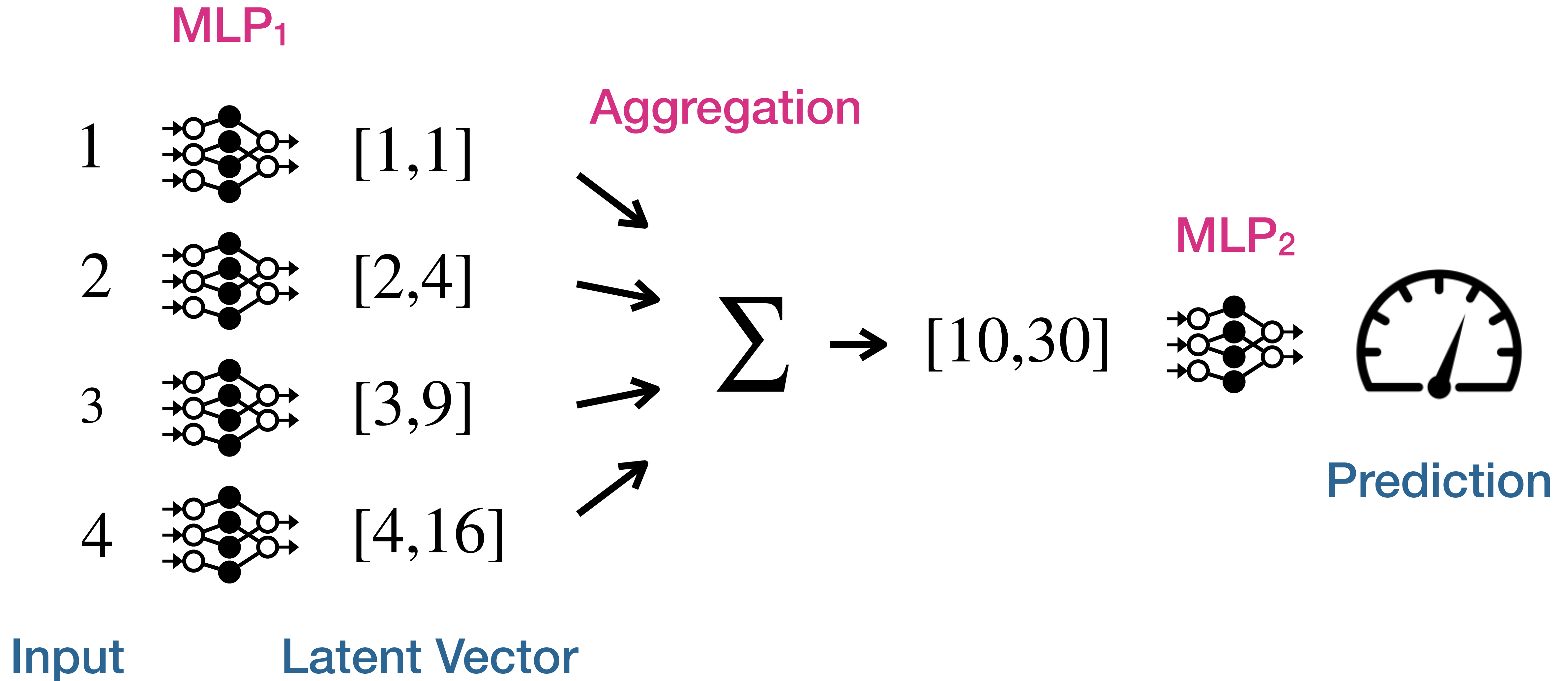


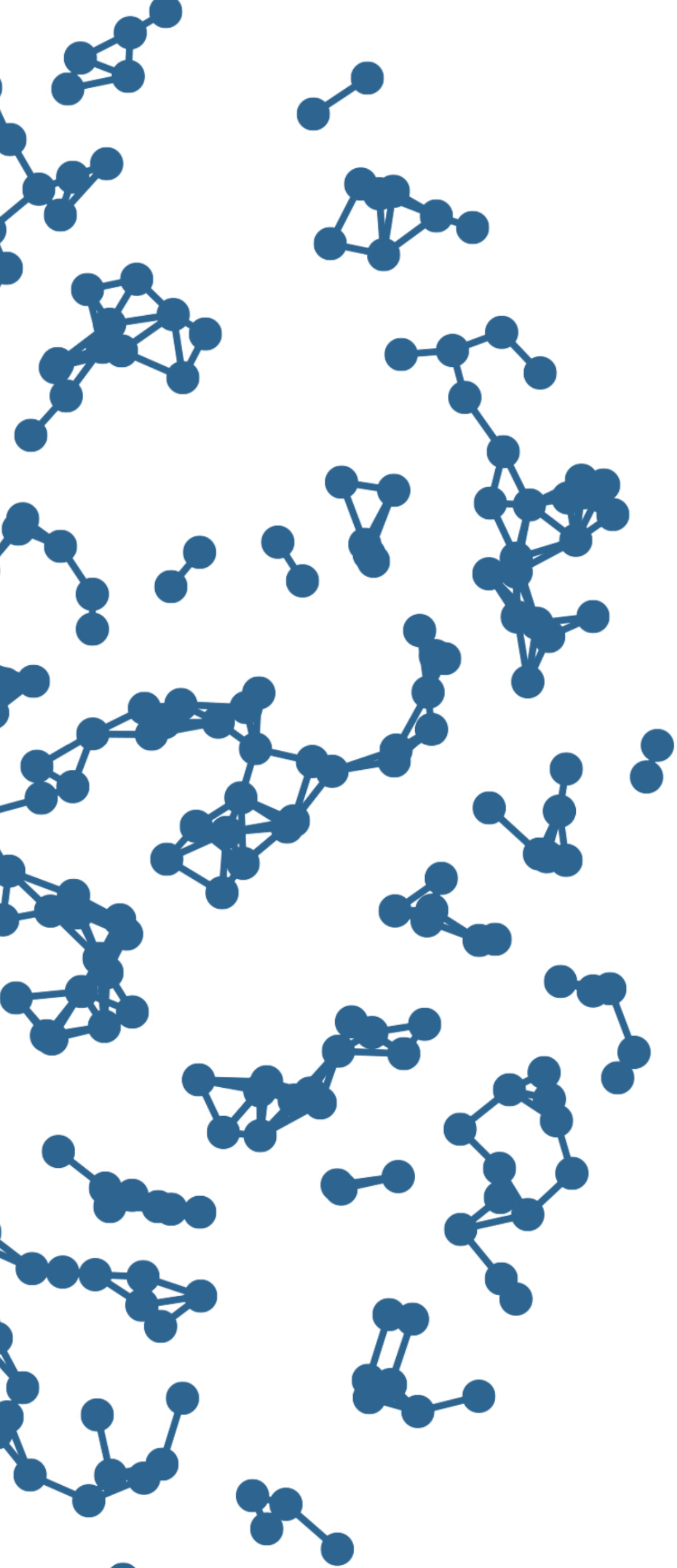
[4,3,1,2]



Guaranteed to  
produce the  
same results.

# Deep Sets

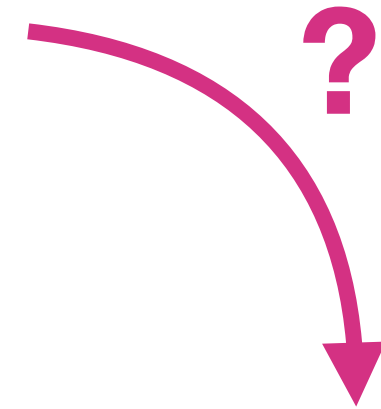
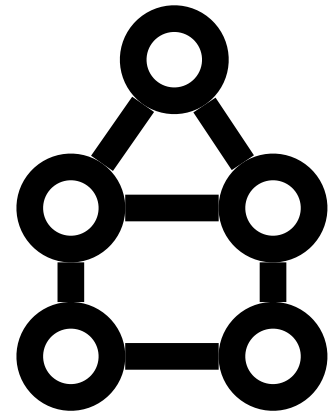




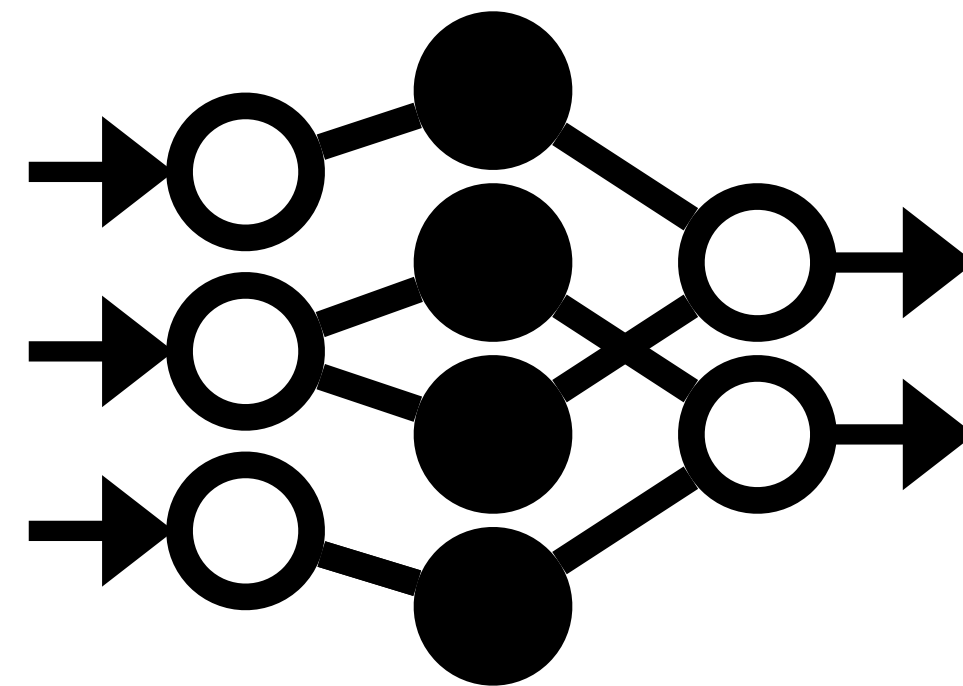
## Part III

# DEEP SETS ON GRAPHS

# Deep Sets on Graphs



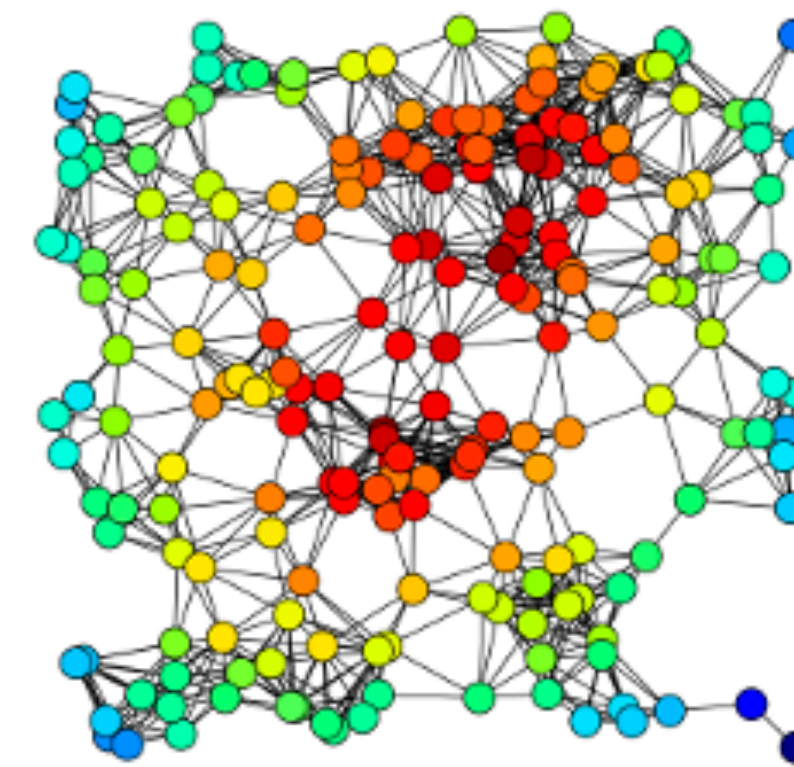
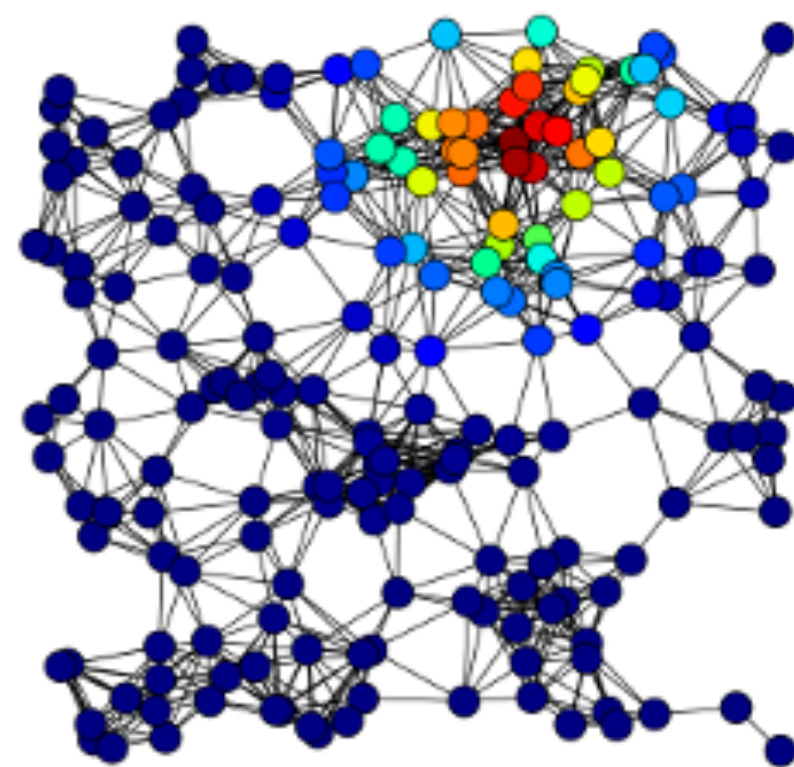
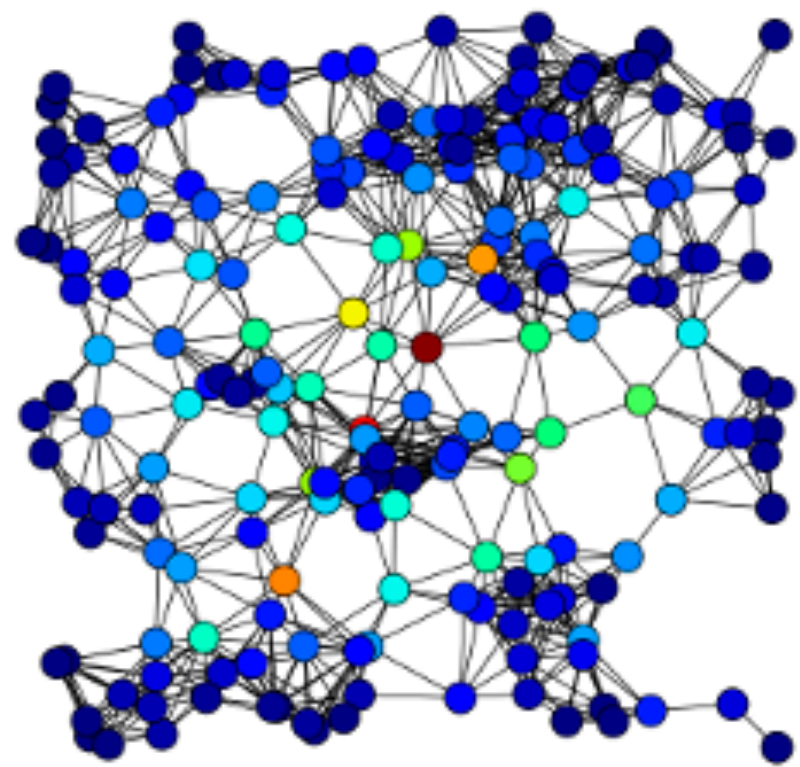
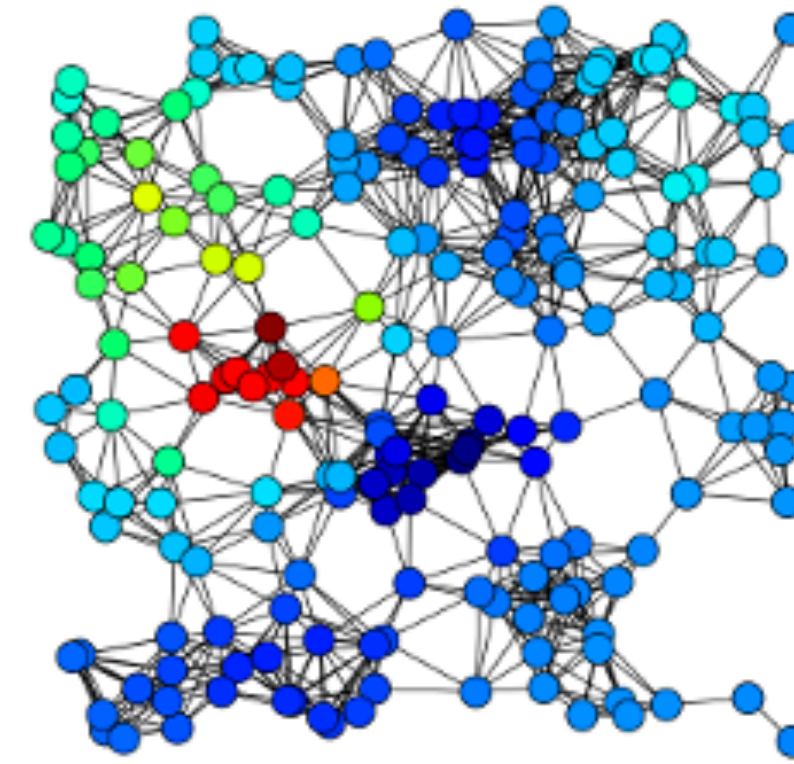
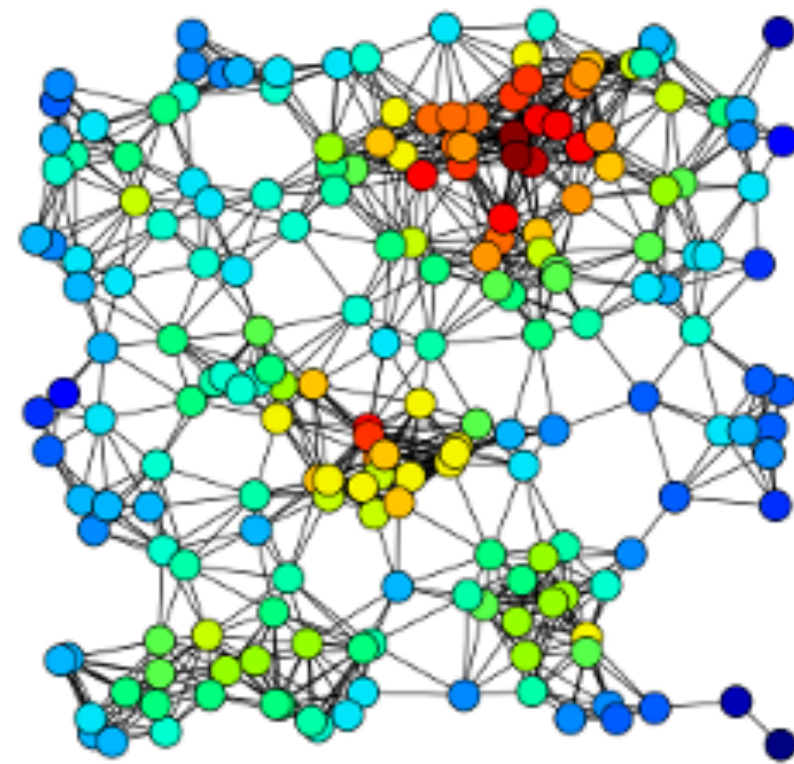
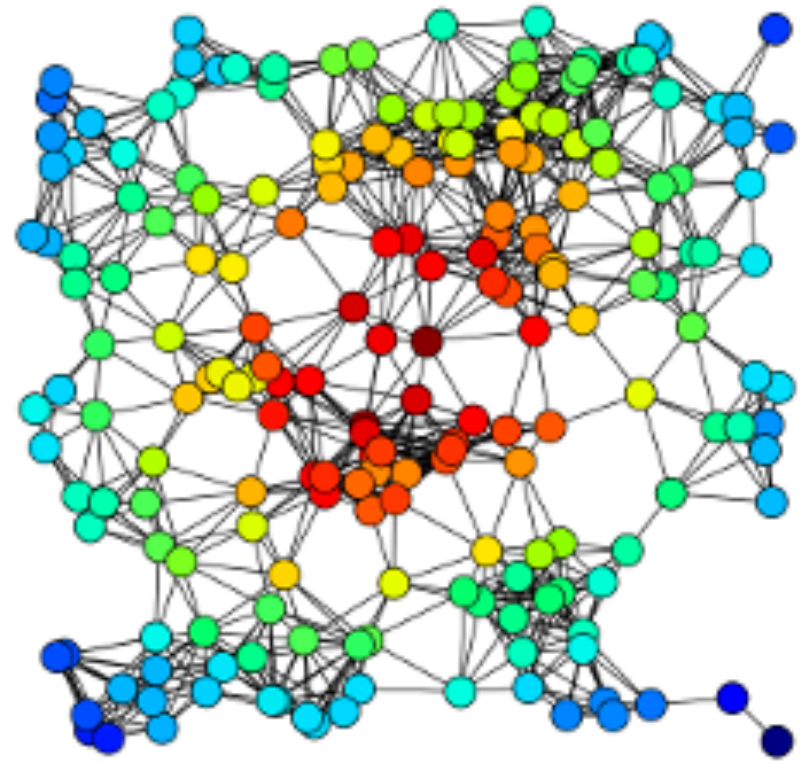
$\{1,2,3,4\}$



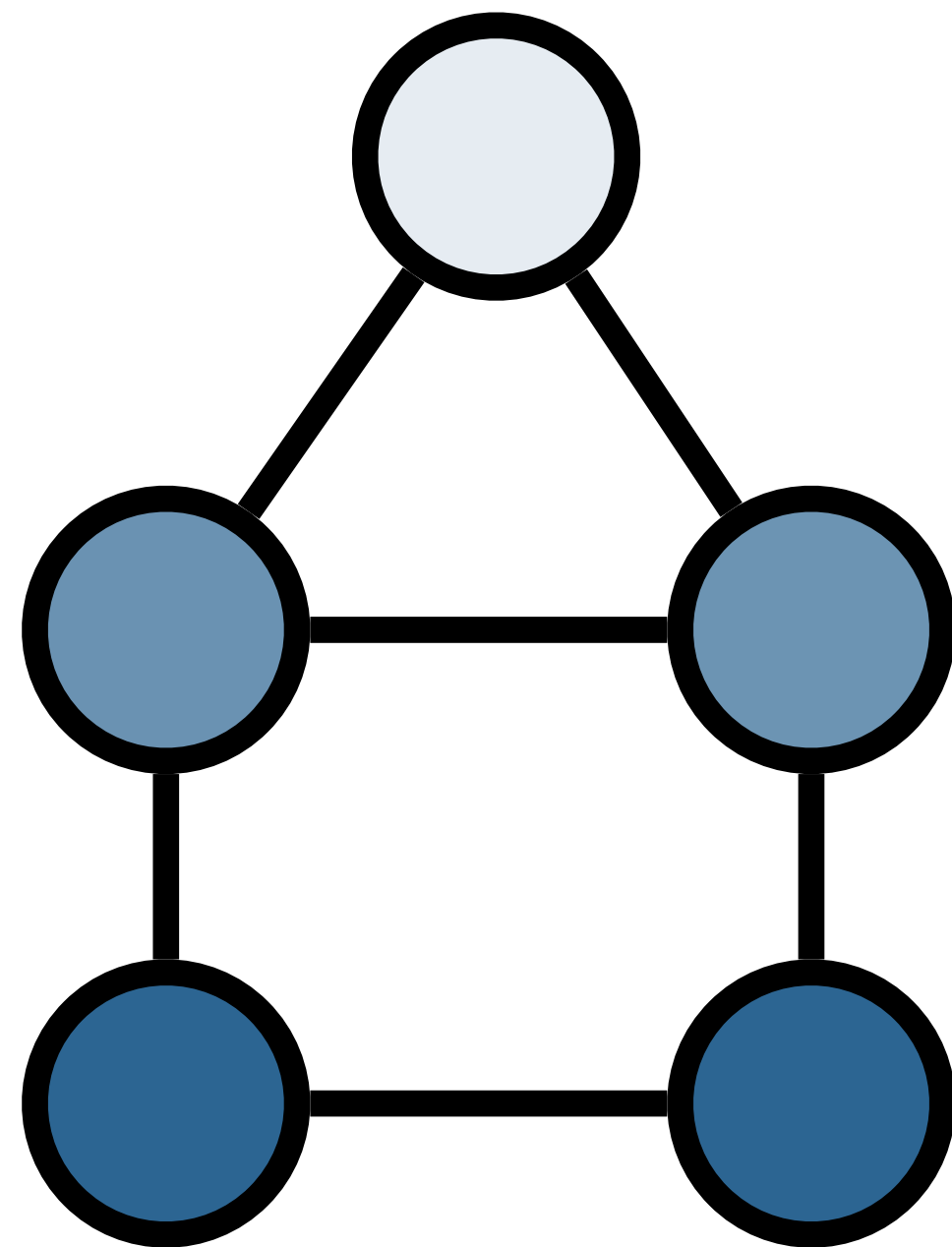
Contains the Number 5



# Centrality



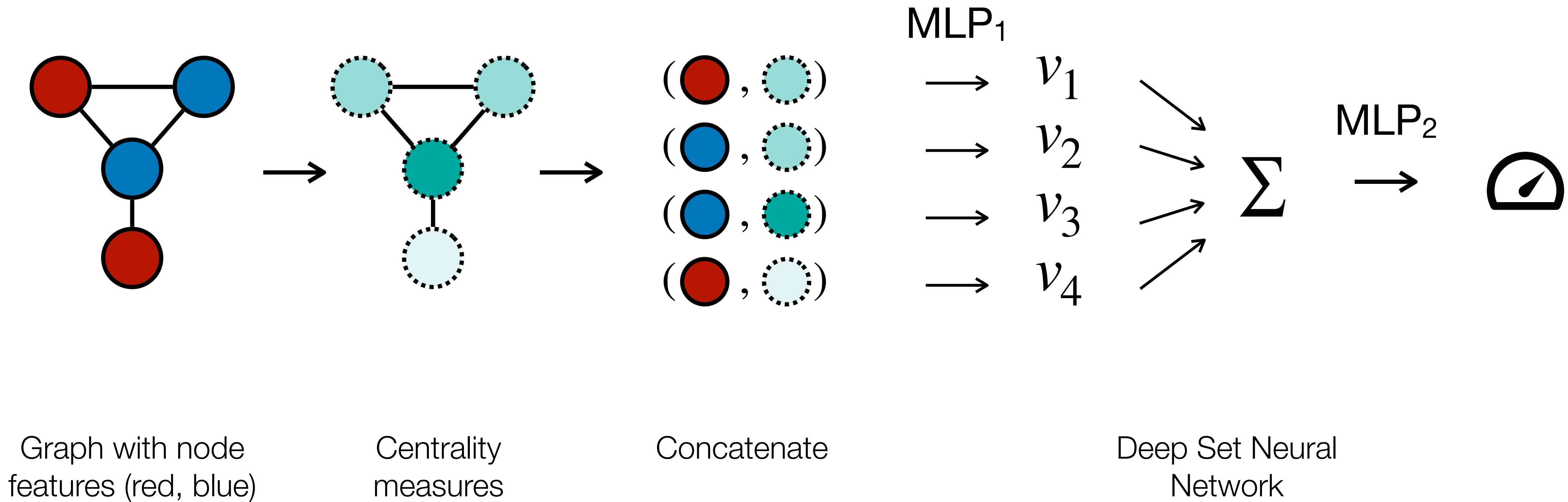
# Message Passing



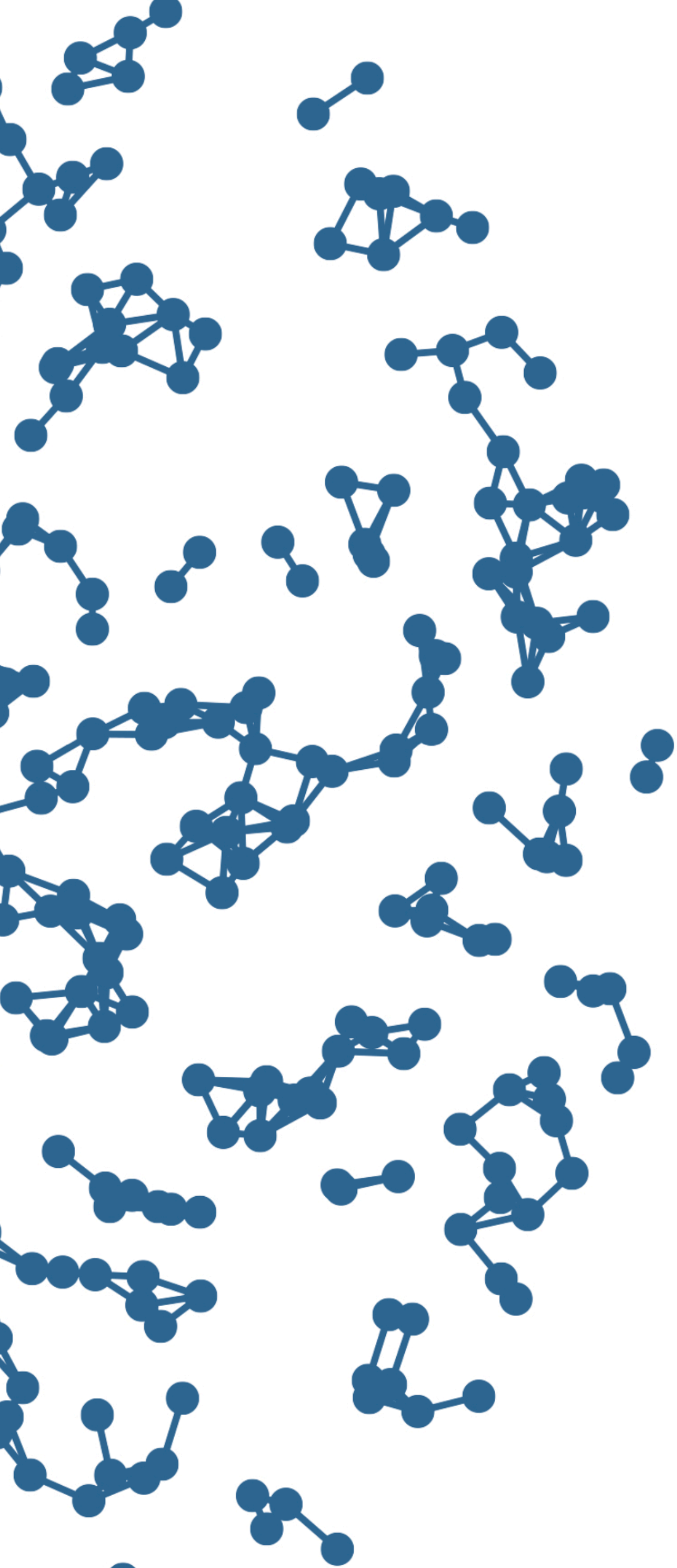
Do we really need *message passing* to capture the topology of a graph?

Maybe *centrality measures* are enough?

# Deep Sets







## Part IV

# EXPRESSIVENESS

# Expressiveness



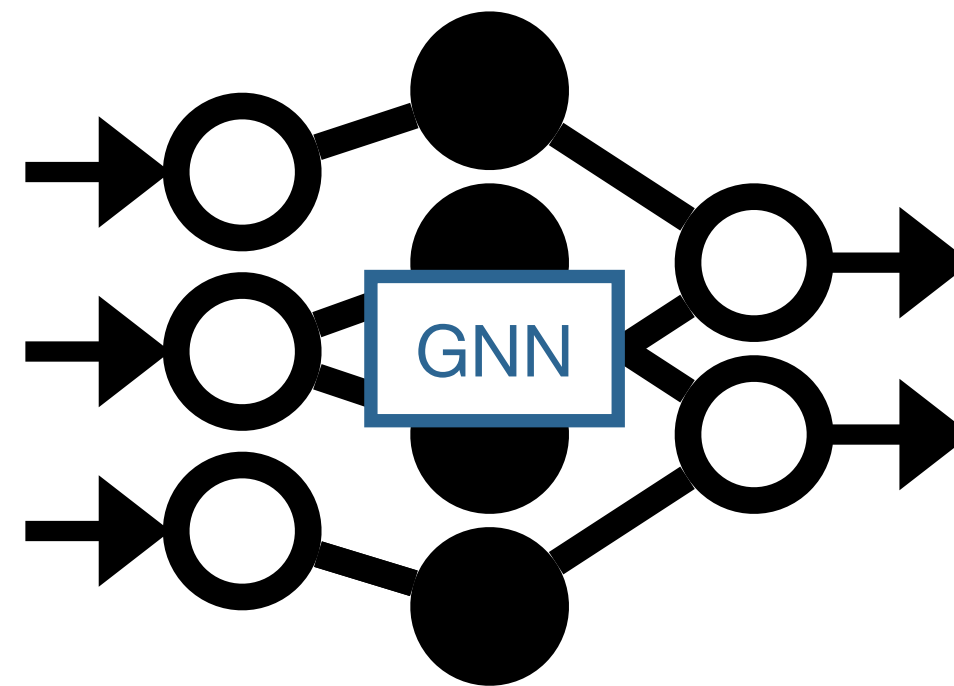
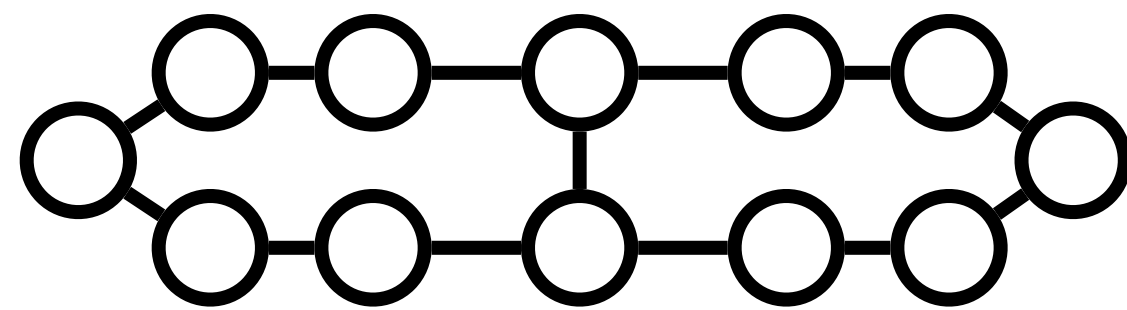
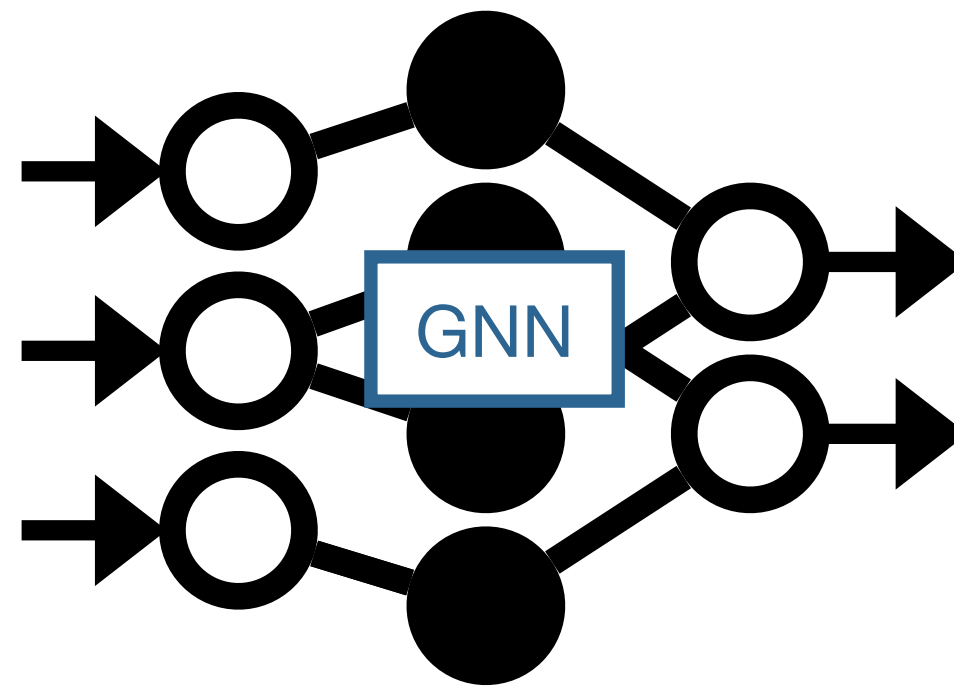
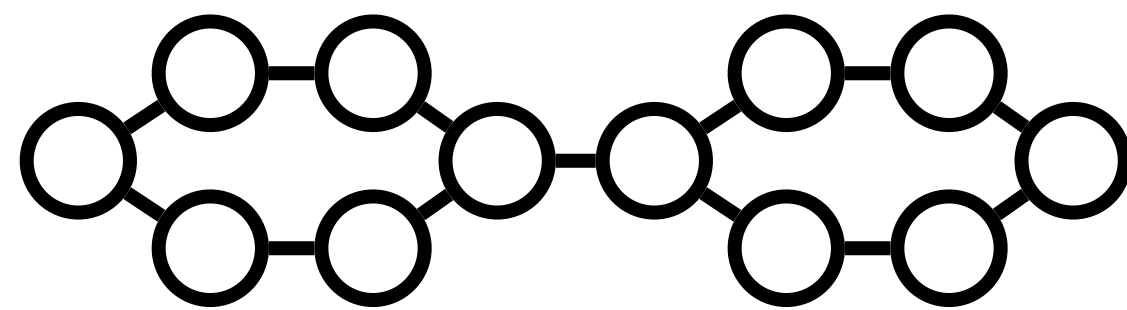
**Expressiveness** of GNNs is measured by their ability to distinguish non-isomorphic graphs



# Expressiveness



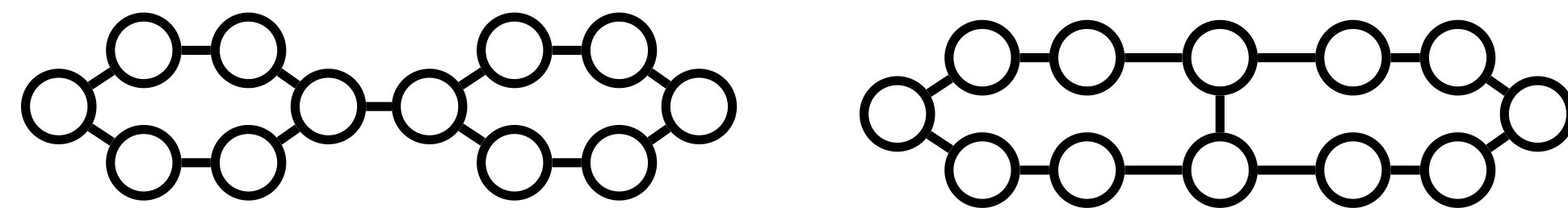
**Expressiveness** of GNNs is measured by their ability to distinguish non-isomorphic graphs



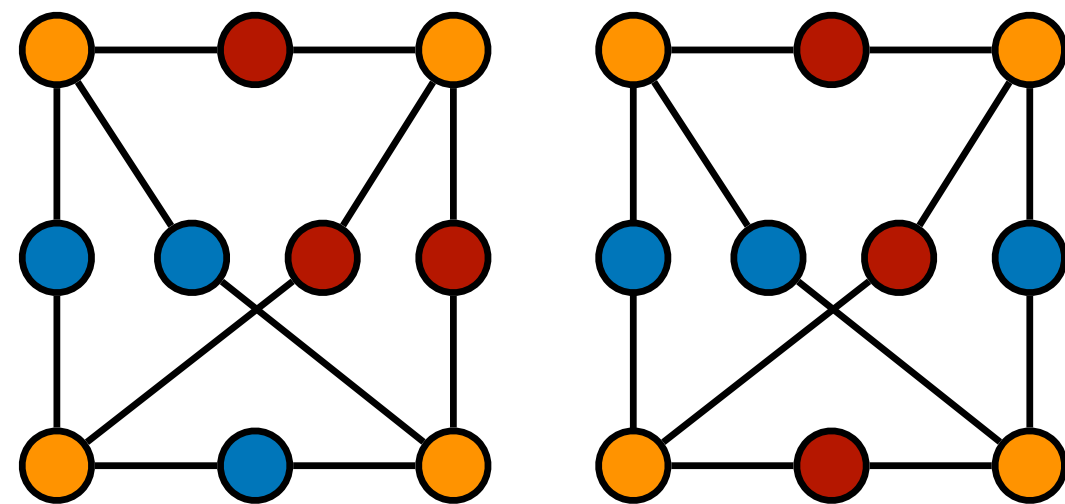
Guaranteed to  
produce the  
same results.

# Expressiveness

**Deep Sets** can distinguish graphs that GNNs cannot:

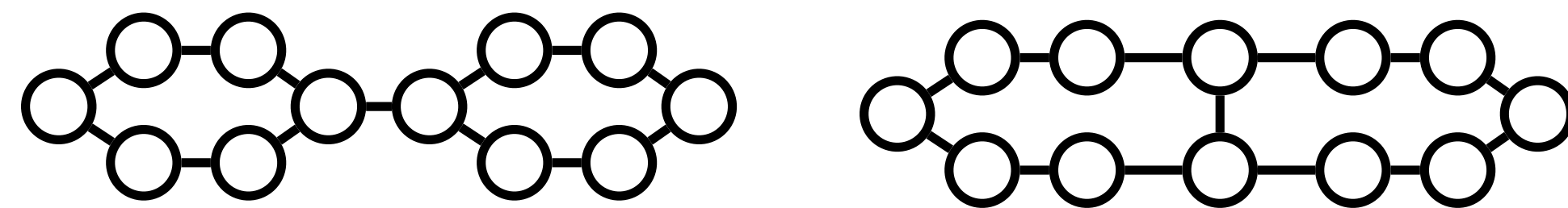


**GNNs** can distinguish graphs that Deep Sets cannot:

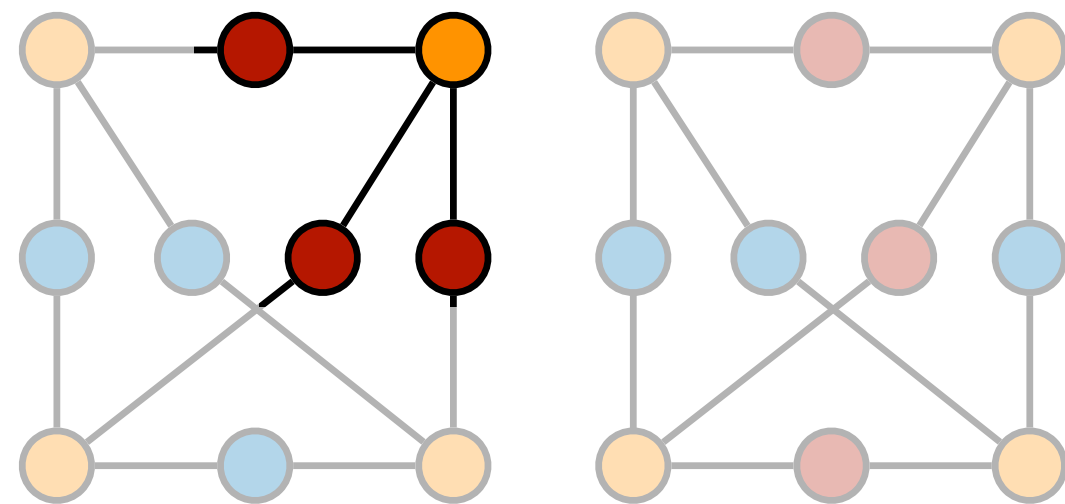


# Expressiveness

Deep Sets can distinguish graphs that GNNs cannot:



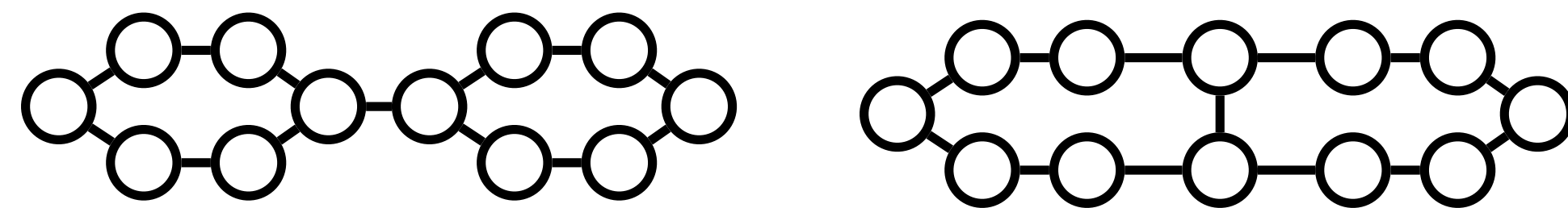
**GNNs can distinguish** graphs that Deep Sets cannot:



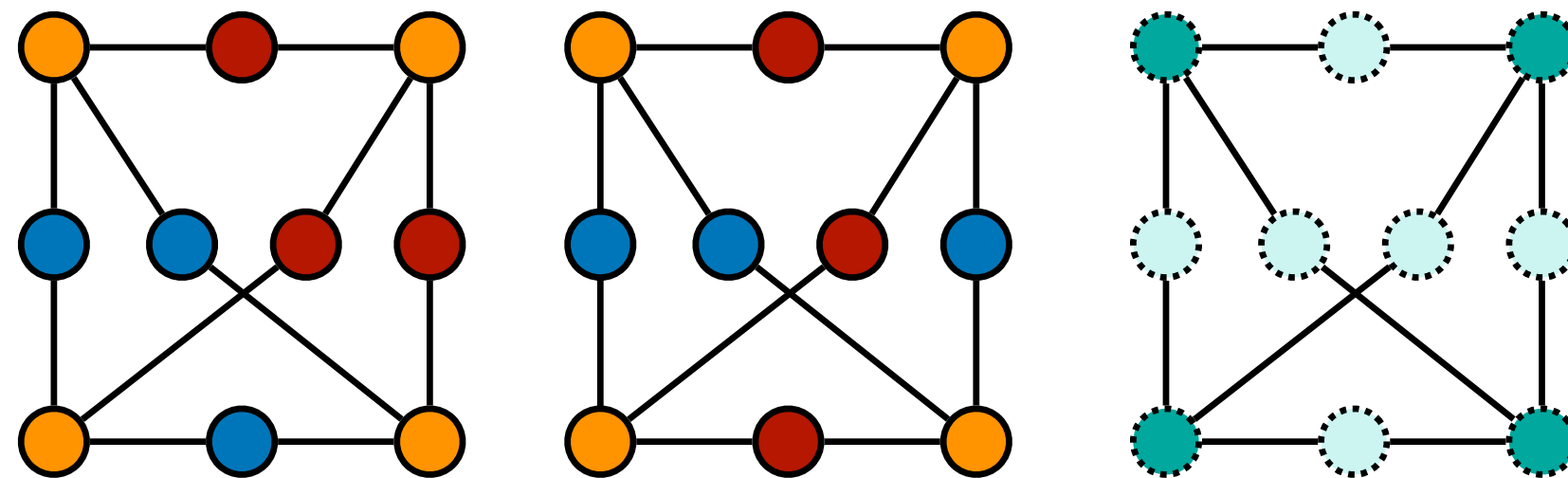
**Yellow** node with three **red** neighbors  
exists only in one of them.

# Expressiveness

Deep Sets can distinguish graphs that GNNs cannot:



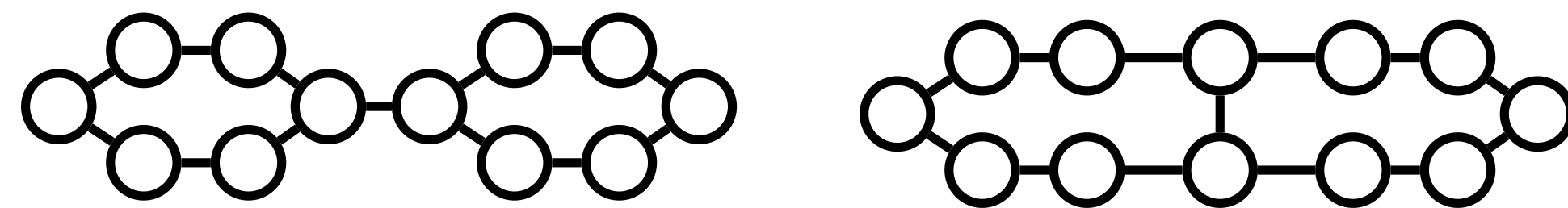
GNNs can distinguish graphs that **Deep Sets cannot**:



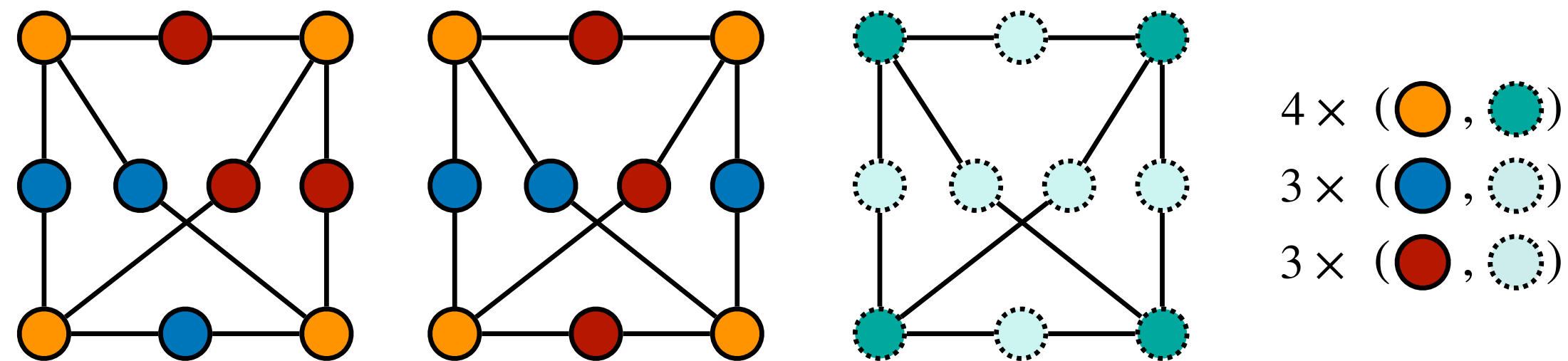
Same centralities  
for both graphs

# Expressiveness

Deep Sets can distinguish graphs that GNNs cannot:



GNNs can distinguish graphs that Deep Sets cannot:

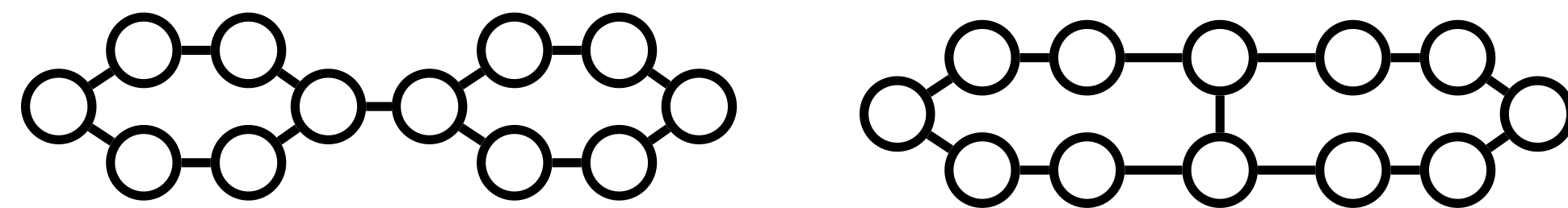


Same multiset  
for both graph

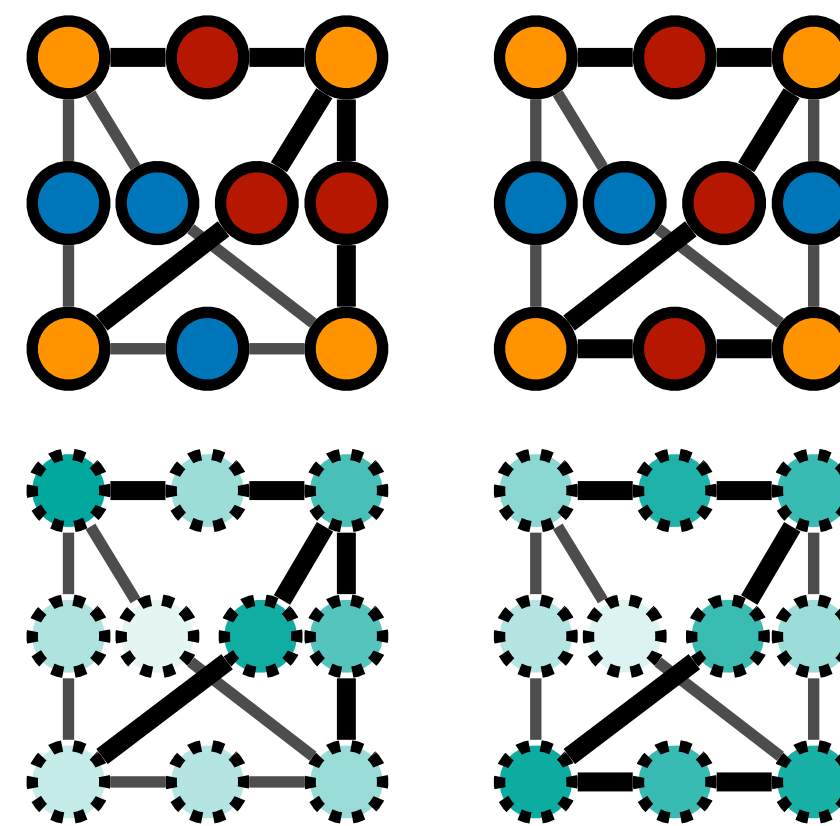


# Expressiveness

Deep Sets can distinguish graphs that GNNs cannot:



GNNs can distinguish graphs that Deep Sets cannot:

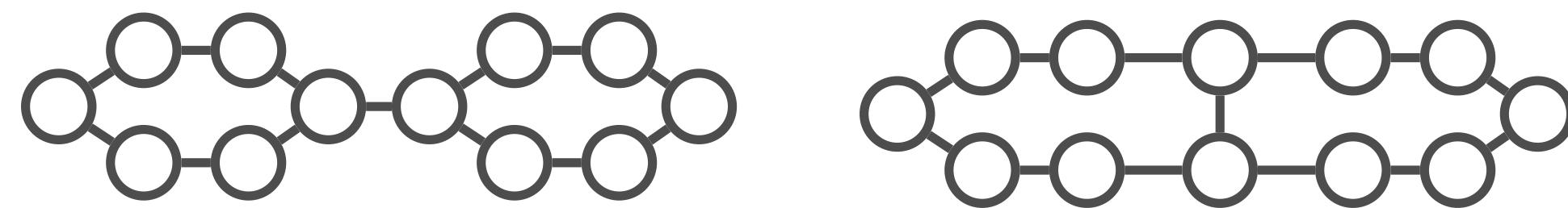


**Potential solution:**

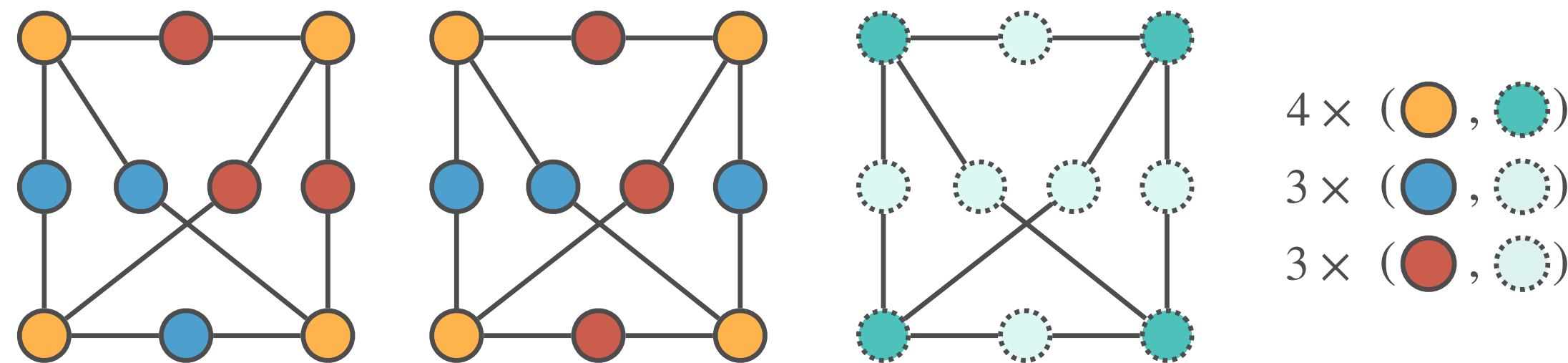
Make centrality aware of  
node-features

# Expressiveness

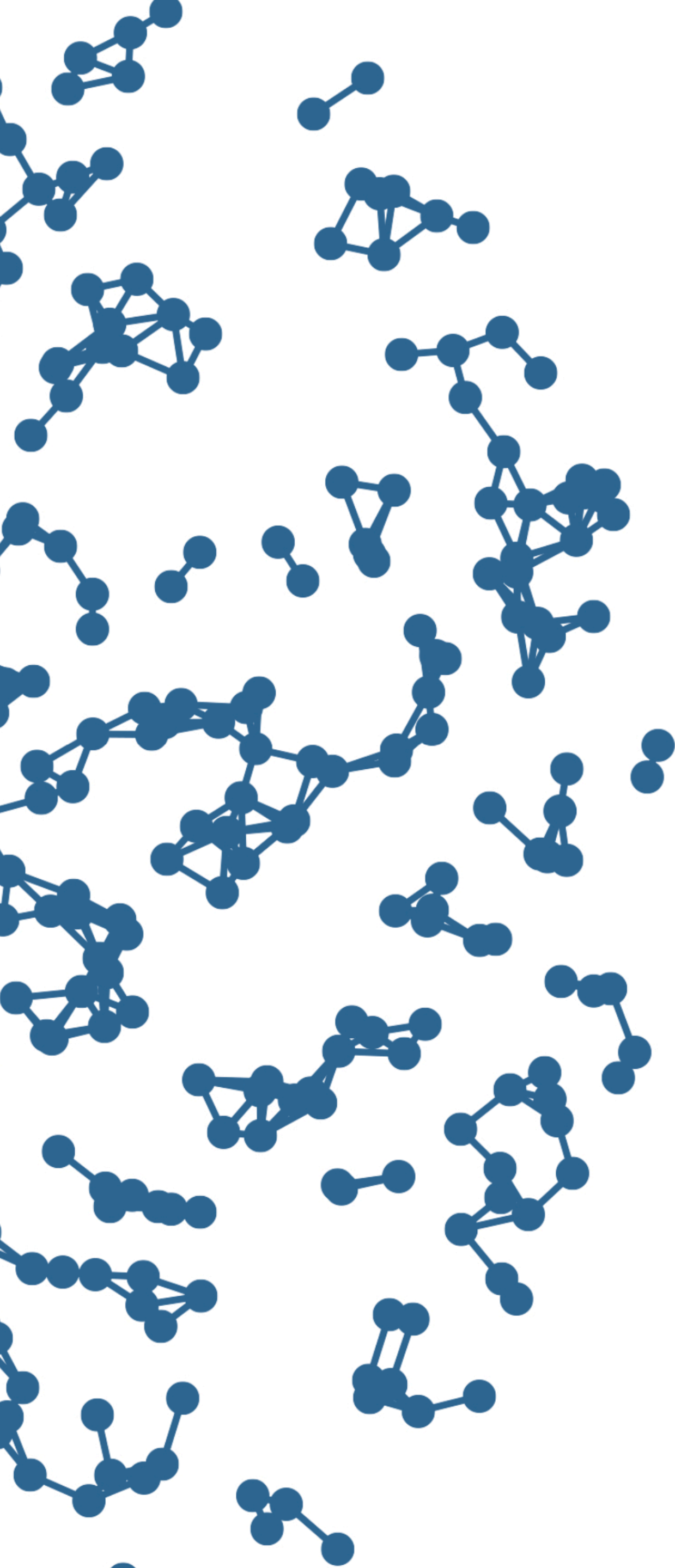
Deep Sets can distinguish graphs that GNNs cannot:



GNNs can distinguish graphs that Deep Sets cannot:



**Open Problem:** Exact position in the Weisfeiler-Lehman hierarchy



# Part V

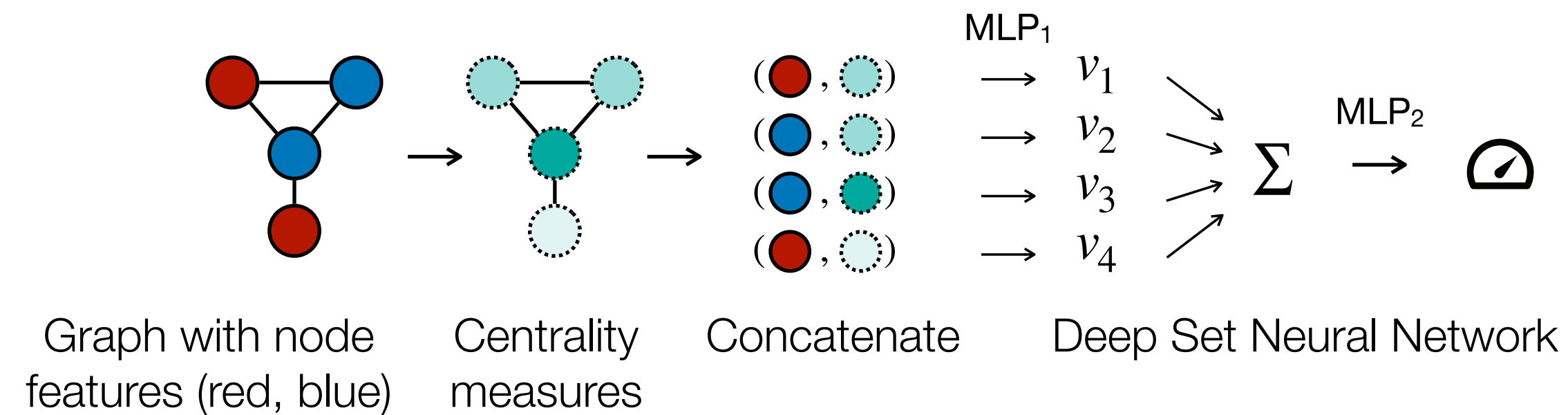
## RESULTS

# Results

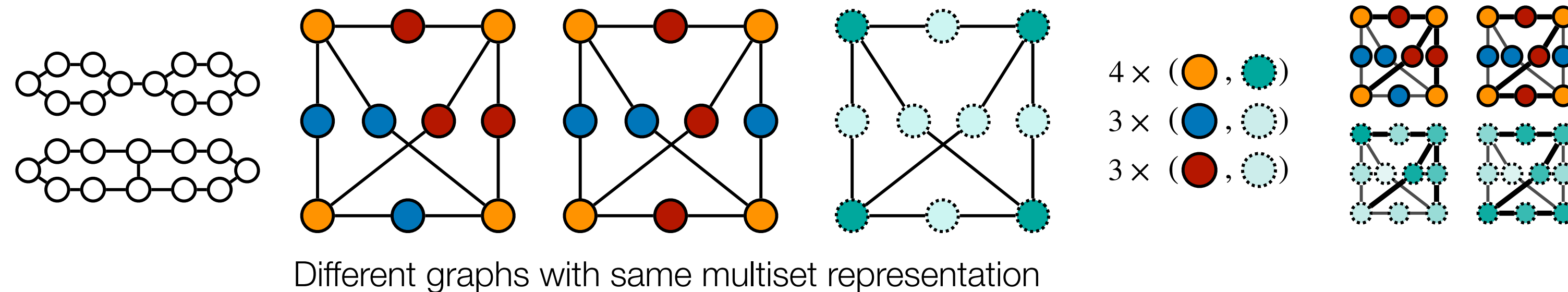
Dataset	DSNN	GCN	GIN	PNA	SOTA	$\bigcirc$ # $N$	$\bigcirc$ # $E$	# $G$
PROTEIN	$0.74 \pm 0.01$	$0.65 \pm 0.01$	$0.61 \pm 0.02$	$0.59 \pm 0.04$	0.85	39.1	145.6	1113
MUTAG	$0.80 \pm 0.06$	$0.55 \pm 0.06$	$0.79 \pm 0.04$	$0.52 \pm 0.00$	1.0	17.9	39.6	188
ENZYMES	$0.40 \pm 0.10$	$0.25 \pm 0.01$	$0.34 \pm 0.04$	$0.28 \pm 0.04$	0.78	32.6	124.2	600
IMBD-BINARY	$0.72 \pm 0.02$	$0.49 \pm 0.44$	$0.52 \pm 0.08$	$0.63 \pm 0.02$	0.96	19.8	193.1	1000

# Concluding Remarks

## Method:



## Expressiveness:



## Open Problems:

- Expressive power of centralities?
- Which centrality measures work best and why?
- Use set of edges instead?