APPENDIX B: USING BROUWER-MEAN ELEMENTS FROM TBUS PART IV

The Brouwer-mean elements in part IV of the APT predict bulletin (TBUS) can be used in a stand-alone Brouwer-Lyddane orbit prediction package to determine orbit position information at any time (t- t_0) where t_0 represents the time of the Brouwer mean elements in part IV and t represents the user request time. The Brouwer-Lyddane algorithm is an analytical solution of satellite motion for a simplified disturbing potential field limited to zonal harmonic coefficients for J_2 through J_5 . Lyddane modified Brouwer's formulation to obtain algorithms applicable for zero eccentricity and zero inclination.

The Brouwer-Lyddane orbit prediction package contains seven subroutines and one block data subprogram which can be called from a user supplied driver to obtain orbit information in the form desired by the user.

The first subroutine to be called is BROLYD. This subroutine takes as input the Brouwer mean or osculating elements at time t_0 , and outputs the osculating Keplerian and Brouwer mean elements at the time $(t-t_0)$ given in common block BLCNST. The calling sequence for subroutine BROLYD is described below.

If users require output in the form of inertial position and velocity vectors then a second subroutine CELEM can be called. This subroutine takes as input the osculating Keplerian elements for BROLYD and outputs the inertial position and velocity vectors. The calling sequences for subroutine CELEM is also described below.

A third subroutine, BFIXED, transforms the position and velocity vectors from CELEM to earth fixed coordinates. The user must supply the Greenwich hour angle to this subroutine.

Subroutine XYZPLH converts the position vector in the earth fixed coordinates to geodetic latitude, east longitude, and height.

Three other subroutines are included in this prediction package. These are DKEPLR, MA3331, and DATAN0. DKEPLR is a subroutine to solve Kepler's equation. MA3331 computes the product of a 3X3 matrix and a 3X1 matrix. DATAN0 computes a value for the arc-tangent between 0 and 2π .

A block data subprogram for the common block BLCNST includes several constants needed by the stand-alone orbit prediction package. These constants are described below and are presently used in NESDIS's polar navigation system.

CALLING SEQUENCE FOR SUBROUTINE BROLYD:

CALL BROLYD (OSCELE, DPELE, IPERT, IPASS, IDMEAN, ORBEL)

ARGUMENTS:

OSCELE - OUTPUT OSCULATING ELEMENTS AT TIME TTO

OSCELE (1) = SEMI-MAJOR AXIS

OSCELE (2) = ECCENTRICITY

OSCELE (3) = INCLINATION

OSCELE (4) = NODE

OSCELE (5) = ARGUMENT OF PERIGEE

OSCELE (6) = MEAN ANOMALY

DPELE - INPUT IS OSCULATING ELEMENTS AT EPOCH IF IDMEAN = 0 INPUT IS BROUWER MEAN AT EPOCH IF IDMEAN \square 0 OUTPUT ELEMENTS ARE BROUWER MEAN AT TIME TTO

DPELE(1) = SEMI-MAJOR AXIS

DPELE (2) = ECCENTRICITY

DPELE (3) = INCLINATION

DPELE (4) = NODE

DPELE (5) = ARGUMENT OF PERIGEE

DPELE (6) = MEAN ANOMALY

IDMEAN - DETERMINES WHICH ELEMENTS ARE INPUT IN DPELE

- = 0, OSCULATING
- □ 0, BROUWER MEAN

IPASS =1, COMPUTE CONSTANTS NEEDED IN COMPUTATION OF OSCULATING ELEMENTS

=2, UPDATE OSCULATING ELEMENT TO OBSERVATION TIME WITHOUT UPDATING CONSTANTS

IPERT =0, NO PERTURBATIONS DUE TO OBLATENESS COMPUTED

- =1, SECULAR TERMS COMPUTED
- =2, SECULAR + LONG PERIODIC + SHORT PERIODIC TERMS

ORBEL - OUTPUT AUXILIARY ORBITAL ELEMENTS

CALLING SEQUENCE FOR SUBROUTINE CELEM:

CALL CELEM (ORBEL, GMC, PV, VV)

ARGUMENTS:

ORBEL - INPUT OSCULATING ELEMENTS

ORBEL(1) = SEMI-MAJOR AXIS

ORBEL (2) = ECCENTRICITY

ORBEL (3) = INCLINATION

ORBEL(4) = NODE

ORBEL (5) = ARGUMENT OF PERIGEE

ORBEL(6) = MEAN ANOMALY

GMC - INPUT GRAVITATIONAL CONSTANT

PV - OUTPUT CARTESIAN POSITION VECTOR

PV(1) = X

PV(2) = Y

PV(3) = Z

VV - OUTPUT CARTESIAN VELOCITY VECTOR

VV(1) = XDOT

VV(2) = YDOT

VV(3) = ZDOT

COMMON BLOCK BLCNST

COMMON/BLCNST/TTO, R, AE, GM, BJ2, BJ3, BJ4, BJ5, FLTINV, XKE, ESQ

VARIABLES USED IN COMMON/BLCNST/:

TTO - INPUT REQUEST TIME IN SECONDS FROM EPOCH

R - OUTPUT MAGNITUDE OF SATELLITE RADIUS VECTOR

- AE INPUT MEAN EQUATORIAL RADIUS OF THE EARTH (KM)
- GM INPUT GRAVITATIONAL CONSTANT OF THE EARTH (KM³/SEC²)
- BJ2 INPUT C_{2,0} ZONAL HARMONIC COEFFICIENT
- BJ3 INPUT C_{3,0} ZONAL HARMONIC COEFFICIENT
- BJ4 INPUT C_{4,0} ZONAL HARMONIC COEFFICIENT
- BJ5 INPUT C_{5,0} ZONAL HARMONIC COEFFICIENT
- FLTINV INPUT INVERSE FLATTENING COEFFICIENT (1/F)
- XKE GRAVITATIONAL CONSTANT (EARTH RADII)^{3/2}/MIN)
- ESQ THE SQUARE OF THE MAJOR ECCENTRICITY CALCULATED FROM $e^2\!\!=\!\!(2f\text{-}f^2)$

00000010 00000020 NAME AMMSMA 00000030 TYPE - SUBROUTINE LANGUAGE - FORTRAN 00000040 VERSIONS - 1.0 DATE - 07/01/81 PROGRAMMER - T.LIU 00000050 00000060 FUNCTIONS: 00000070 TO CALCULATE THE AVERAGE MEAN MOTION AND THE SEMIMAJOR 08000000 AXIES. 00000090 INPUT PARAMETERS: 00000100 COMMON/DATA2/..... 00000110 OUTPUT PARAMETERS: 00000120 DMEAN - AVERAGE MEAN MOTION 00000130 BMELMT(1) - SEMIMAJOR AXIES 00000140 00000150 SUBROUTINES CALLED: NONE SUBROUTINE AMMSMA (DMEAN, BMELMT) 00000210 REAL*8 IMPLICIT (A-H,O-Z)00000220 COMMON/DATA2/ DESIGI, EPTIME, DMMDT, D2MDT, 00000230 DRAGT, IETYPE, NELSET, DINCL, RASC, ECC, ARGP, DMEANA, 1 00000240 DMMOT, IREVNO, ISATNO 00000250 REAL*8 BMELMT(6) 00000260 COMMON/BLCNST/ TTO, R, AE, GM, BJ2, BJ3, BJ4, BJ5, FLTINV, XKE, ESQ 00000261 TOTHRD, RE, DEGRAD/0.66666667, 1., 0.01745329252D0/ DATA 00000270 TWOPI/6.2831853/ DATA 00000290 DATA XMNPDA/1440./

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```
00000295
      XJ2=-BJ2
00000299
      CK2=.5*XJ2*RE**2
00000300
      TEMP=TWOPI/XMNPDA/XMNPDA
00000320
      DMEN=DMMOT*TEMP*XMNPDA
00000350
      RINCL=DINCL*DEGRAD
00000400
      A1=(XKE/DMEN)**TOTHRD
00000500
      COSIO=DCOS(RINCL)
00000600
      THETA2=COSIO*COSIO
00000700
      X3THM1=3.*THETA2-1.
00000800
      EOSQ=ECC*ECC
00000900
      BETAO2=1.-EOSQ
00001000
      BETAO=DSQRT(BETAO2)
00001100
      DEL1=1.5*CK2*X3THM1/(A1*A1*BETAO*BETAO2)
00001200
      AO=A1*(1.-DEL1*(.5*TOTHRD+DEL1*(1.+134./81.*DEL1)))
00001300
      DELO=1.5*CK2*X3THM1/(AO*AO*BETAO*BETAO2)
00001400
      DMEAN=DMEN/(1.+DELO)
00001500
      DSEMI=AO/(1.-DELO)
00001600
      BMELMT(1)=DSEMI*AE
00001650
      RETURN
00001700
      END
```

00001800

```
SUBROUTINE BFIXED (KEY, GHA, PV, VV, POSOUT, VELOUT, B)
     IMPLICIT REAL*8 (A-H, O-Z)
C
     NAME - BFIXED
C
C
     LANGUAGE- FORTHXP TYPE- SUBROUTINE
C
C
     VERSION- 1.0 DATE- 10/14/77
                                           PROGRAMMER- SACHS, A.
C
C
     PURPOSE -TRANSFORM THE POSITION AND VELOCITY FROM TOD TO
C
     PSUEDO BODY FIXED.
С
C
     INPUT PARAMETERS - KEY= 3 FOR RETURN OF BODY FIXED POSITION
С
     ONLY, GHA= GREENWICH HOUR ANGLE IN RADIANS, PV= POSITION VECTOR,
С
     VV= VELOCITY VECTOR (KM/SEC).
C
С
     OUTPUT PARAMETERS - POSOUT =POSITION VECTOR, VELOUT =VELOCITY
C
     VECTOR, B = ROTATION MATRIX.
С
C
     SUBROUTINES CALLED - MA3331
C
C
     COMMENT- B MATRIX COMPUTATION IS FROM SUBROUTINE EVAL OF GTDS.
C
DIMENSION B(3,3), BDOT(3,3), PV(3), VV(3), VELOUT(3), VOUT(3)
     DIMENSION POSOUT(3)
     DATA OMEGAE, BDOT/7.29211585494D-5, 9*0.D0/
C COMPUTE MATRIX TO ROTATE POSITION FROM TOD TO PSUEDO BODY FIXED.
C SPIN FACTOR IS ZERO.
     XP=0.0D0
     YP=0.0D0
     B(1,1) = DCOS(GHA)
     B(1,2) = DSIN(GHA)
     B(1,3) = XP
     B(2,1) = -B(1,2)
     B(2,2) = B(1,1)
     B(2,3) = -YP
     B(3,1) = -XP*B(1,1)-YP*B(1,2)
     B(3,2) = -XP*B(1,2)+YP*B(1,1)
     B(3,3) = 1.0D0
C ROTATE THE INPUT POSITION VECTOR.
     CALL MA3331 (B, PV. POSOUT)
     IF (KEY.EQ.3) GO TO 30
C COMPUTE MATRIX TO ROTATE VELOCITY FROM TOD TO PSUEDO BODY FIXED.
     BDOT(1,1) = -B(1,2)
     BDOT(1,2) = B(1,1)
     BDOT(2,1) = -B(1,1)
     BDOT(2,2) = -B(1,2)
C ROTATE THE INPUT VELOCITY VECTOR.
     CALL MA3331(B, VV, VOUT)
C ROTATE THE INPUT POSITION VECTOR.
     CALL MA3331(BDOT, PV, VELOUT)
```

```
C OBTAIN THE BODY FIXED VELOCITY.

DO 20 I=1,3

20 VELOUT(I) = VELOUT(I)*OMEGAE + VOUT(I)

30 CONTINUE

RETURN

END
```

```
BLOCK DATA
    IMPLICIT REAL*8 (A-H,O-Z)
C
    NAME- BLCNST
С
С
    LANGUAGE- FORTHXP
                       TYPE- PROGRAM
С
С
    THIS COMMON BLOCK WAS UPDATED MARCH 28, 1984 TO INCLUDE XKE
С
    AND ESQ BY E. HARROD S/SP12
С
    THIS BLOCK DATA IS COMPILED WITH THE ROUTINE PSCEAR, ANY
С
    PROGRAM USING PSCEAR DOES NOT NEED TO RECOMPILE THIS BLOCK
С
    DATA
COMMON/BLCNST/ TTO,R,AE,GM,BJ2,BJ3,BJ4,BJ5,FLTINV,XKE,ESQ
    DATA TTO,R,GM,AE,BJ2,BJ3,BJ4,BJ5,FLTINV,XKE,ESQ/2*0.D0,
    1 398600.8D0,6378.135D0,-0.10826158D-02,0.25388100D-05,
    2 0.16559700D-05,0.21848266D-06,298.25D0,0.743669161D-01,
    3 0.6994317778266721D-02/
    END
```

```
SUBROUTINE BROLYD(OSCELE, DPELE, IPERT, IPASS, IDMEAN, ORBEL)
C*
     REF. "BROUWER-LYDDANE ORBIT GENERATOR ROUTINE"
C*
               (X-553-70-223)
C*
         BY E.A. GALBREATH 1970
C*-----*
C*
    MODIFIED 7/31/74 VIONA BROWN AND R.A. GORDON TO INTERFACE *
C*
IMPLICIT REAL*8(A-H,O-Z)
     REAL*8 PI2/6.283185307179586D0/
     DIMENSION OSCELE(6), DPELE(6), ORBEL(5)
     COMMON /BLCNST/ TTO,R,AE,GM,BJ2,BJ3,BJ4,BJ5,FLTINV,XKE,ESQ
     DATA BMU, RE/1.0D0, 1.0D0/, BKSUBC/0.01D0/
     EK = DSQRT(GM/AE**3)
     DELT = EK*TTO
     GO TO (10,111), IPASS
C
C EPOCH ELEMENTS AT EPOCH TIME
  10 ADP = DPELE(1)/AE
    EDP = DPELE(2)
    BIDP = DPELE(3)
    HDP = DPELE(4)
     GDP = DPELE(5)
    BLDP = DPELE(6)
    A0 = ADP
     E0 = EDP
     BIO = BIDP
    H0 = HDP
     G0 = GDP
     BL0 = BLDP
     IFLG = 0
C
C COMPUTE MEAN MOTION
     ANU=DSQRT(BMU/A0**3)
C
C COMPUTE FRACTIONS
     F3D8=3.0D0/8.0D0
     F1D2=1.0D0/2.0D0
     F3D2=3.0D0/2.0D0
     F1D4=1.0D0/4.0D0
     F5D4=5.0D0/4.0D0
     F1D8=1.0D0/8.0D0
     F5D12=5.0D0/12.0D0
     F1D16=1.0D0/16.0D0
     F15D16=15.0D0/16.0D0
     F5D24=5.0D0/24.0D0
     F3D32=3.0D0/32.0D0
    F15D32=15.0D0/32.0D0
     F5D64=5.0D0/64.0D0
```

```
F35384=35.0D0/384.0D0
      F35576=35.ODO/576.0D0
      F35D52=35.0D0/1152.0D0
     F1D3=1.0D0/3.0D0
     F5D16=5.0D0/16.0D0
     BK2 = -F1D2*(BJ2*RE*RE)
     BK3 = BJ3*RE**3
     BK4 = F3D8*(BJ4*RE**4)
     BK5=BJ5*RE**5
      GO TO 153
  111 IF(IPERT.EQ.0)GO TO 7
      IF(IDMEAN.NE.0)GO TO 202
      ADP = DPELE(1)/AE
      EDP = DPELE(2)
     BIDP = DPELE(3)
     HDP = DPELE(4)
     GDP = DPELE(5)
      BLDP = DPELE(6)
  153 EDP2=EDP*EDP
     CN2=1.0-EDP2
      CN=DSQRT(CN2)
      GM2=BK2/ADP**2
      GMP2=GM2/(CN2*CN2)
      GM4=BK4/ADP**4
      GMP4=GM4/CN**8
     THETA=DCOS(BIDP)
     THETA2=THETA*THETA
      THETA4=THETA2*THETA2
  202 IF(IDMEAN.EQ.0)GO TO 155
      IF(IPASS.EQ.2) GO TO 150
C COMPUTE LDOT, GDOT, HDOT
  157 BLDOT=CN*ANU*(GMP2*(F3D2*(3.0*THETA2-1)+GMP2*F3D32*(THETA2
     1*(-96.0*CN+30.0-90.0*CN2)+(16.0*CN+25.0*CN2-15.0)+THETA4
     2*(144.0*CN+25.0*CN2+105.0)))+EDP2*GMP4*F15D16*(3.0+35.0*THETA4
     3-30.0*THETA2))
     GDOT=ANU*(F5D16*GMP4*((THETA2*(126.0*CN2-270.0)+THETA4*(385.0
     1-189.0*CN2))-9.0*CN2+21.0)+GMP2*(F3D32*GMP2*(THETA4*(45.0*CN2
     2+360.0*CN+385.0)+THETA2*(90.0-192.0*CN-126.0*CN2)+(24.0*CN
     3+25.0*CN2-35))+F3D2*(5*THETA2-1)))
     HDOT=ANU*(GMP4*F5D4*THETA*(3.0-7.0*THETA2)*(5.0-3.0*CN2)+GMP2
     1*(GMP2*F3D8*(THETA*(12.0*CN+9.0*CN2-5.0)-THETA*THETA2*(5.0*CN2
     2+36.0*CN+35.0))-3*THETA))
  155 IF(IFLG.EQ.1)GO TO 19
  COMPUTE ISUBC TO TEST CRITICAL INCLINATION
      BISUBC=((1.0-5.0*THETA2)**(-2))*((25.0*THETA4*THETA)*(GMP2*EDP2))
      IFLG=1
 FIRST CHECK FOR CRITICAL INCLINATION
С
```

С

 \overline{C} С

C

C

C

```
IF(BISUBC.GT.BKSUBC)GO TO 158
     ASSIGN 163 TO ID8
      GO TO 159
C
C IS THERE CRITICAL INCLINATION?
С
  19 IF(BISUBC.GT.BKSUBC)GO TO 150
  159 IF(IPERT.EQ.1)GO TO 150
     GM3=BK3/ADP**3
      GMP3=GM3/(CN2*CN2*CN2)
      GM5=BK5/ADP**5
      GMP5=GM5/CN**10
     G3DG2=GMP3/GMP2
      G4DG2=GMP4/GMP2
     G5DG2=GMP5/GMP2
C
C COMPUTE A1-A8
      A1=(F1D8*GMP2*CN2)*(1.0-11.0*THETA2-((40.0*THETA4)/(1.0-5.0*THETA2)))
     A2=(F5D12*G4DG2*CN2)*(1.0-((8.0*THETA4)/(1.0-5.0*THETA2))-3.0*THETA2)
      A3=G5DG2*((3.0*EDP2)+4.0)
     A4=G5DG2*(1.0-(24.0*THETA4)/(1.0-5.0*THETA2)-9.0*THETA2)
     A5=(G5DG2*(3.0*EDP2+4.0))*(1.0-(24.0*THETA4)/(1.0-5.0*THETA2)-
9.0*THETA2)
      A6=G3DG2*F1D4
     SINI=DSIN(BIDP)
     A10=CN2*SINI
     A7=A6*A10
     A8P=G5DG2*EDP*(1.0-(16.0*THETA4)/(1.0-5.0*THETA2)-5.0*THETA2)
     A8=A8P*EDP
С
C
   COMPUTE B13-B15
С
     B13=EDP*(A1-A2)
     B14=A7+F5D64*A5*A10
      B15=A8*A10*F35384
C
С
   COMPUTE A11-A27
C
     A11=2.0+EDP2
     A12=3.0*EDP2+2.0
     A13=THETA2*A12
      A14=(5.0*EDP2+2.0)*(THETA4/(1.0-5.0*THETA2))
     A17=THETA4/((1.0-5.0*THETA2)*(1.0-5.0*THETA2))
     A15=(EDP2*THETA4*THETA2)/((1.0-5.0*THETA2)*(1.0-5.0*THETA2))
     A16=THETA2/(1.0-5.0*THETA2)
     A18=EDP*SINI
     A19=A18/(1.0+CN)
     A21=EDP*THETA
     A22=EDP2*THETA
     SINI2=DSIN(BIDP/2.0)
     COSI2=DCOS(BIDP/2.0)
      TANI2=DTAN(BIDP/2.0)
```

```
A26=16.0*A16+40.0*A17+3.0
                      A27=A22*F1D8*(11.0+200.0*A17+80.0*A16)
C COMPUTE B1-B12
С
                      B1=CN*(A1-A2)-((A11-400.0*A15-40.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A13)*F1D16+(11.0+200.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A14-11.0*A
                   1*A17+80.0*A16)*A22*F1D8)*GMP2+((-80.0*A15-8.0*A14-3.0*A13+A11)
                   2*F5D24+F5D12*A26*A22)*G4DG2
                      B2=A6*A19*(2.0+CN-EDP2)+F5D64*A5*A19*CN2-F15D32*A4*A18*CN*CN2
1+(F5D64*A5+A6)*A21*TANI2+(9.0*EDP2+26.0)*F5D64*A4*A18+F15D32*A3*
2A21*A26*SINI*(1.0-THETA)
                      B3=((80.0*A17+5.0+32.0*A16)*A22*SINI*(THETA-1.0)*F35576 *G5DG2*EDP)
                   1-((A22*TANI2+(2.0*EDP2+3.0*(1.0-CN2*CN))*SINI)*F35D52*A8P)
                      B4=CN*EDP*(A1-A2)
                      B5=((9.0*EDP2+4.0)*A10*A4*F5D64+A7)*CN
                      B6=F35384*A8*CN2*CN*SINI
                      B7 = ((CN2*A18)/(1.0-5.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2)+(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2)+(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2)+(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2)+(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2)+(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*(F1D8*GMP2*(1.0-15.0*THETA2))*
                   1-7.0*THETA2)*G4DG2*(-F5D12))
                     B8=F5D64*(A3*CN2*(1.0-9.0*THETA2-(24.0*THETA4/(1.0-5.0*THETA2))))
                  1+A6*CN2
                      B9=A8*F35384*CN2
                      B10=SINI*(A22*A26*G4DG2*F5D12-A27*GMP2)
                      B11=A21*(A5*F5D64+A6+A3*A26*F15D32*SINI*SINI)
                     B12=-((80.0*A17+32.0*A16+5.0)*(A22*EDP*SINI*SINI*F35576*G5DG2)+(A8
                  1*A21*F35D52))
        150 IF (IPERT.EQ.0)GO TO 7
                       IF (IDMEAN.EQ.0)GO TO 4
C
C COMPUTE SECULAR TERMS
C "MEAN" MEAN ANOMALY
С
                      BLDP = ANU*DELT + BLDOT*DELT+BL0
                      BLDP = DMOD(BLDP, PI2)
                       IF(BLDP.LT.0.0D0)BLDP = BLDP + PI2
C MEAN ARGUMENT OF PERIGEE
C
                      GDP = GDOT*DELT + GO
                      GDP = DMOD(GDP, PI2)
                       IF(GDP.LT.0.0D0)GDP = GDP + PI2
С
C MEAN LONGITUDE OF ASCENDING NODE
C
                      HDP = HDOT*DELT + HO
                      HDP = DMOD(HDP, PI2)
                      IF(HDP.LT.0.0D0)HDP = HDP + PI2
               4 DO 33 NN=1,6
           33 OSCELE(NN) = DPELE(NN)
                     A = ADP
                      E = EDP
                      BI = BIDP
                      H = HDP
                      G = GDP
```

```
BL = BLDP
С
C COMPUTE TRUE ANOMALY (DOUBLE PRIMED)
              EADP = DKEPLR(BLDP, EDP)
              SINDE = DSIN(EADP)
              COSDE = DCOS(EADP)
              SINFD = CN*SINDE
              COSFD = COSDE - EDP
              FDP = DATANO(SINFD, COSFD)
              IF(IPERT.EQ.1)GO TO 7
              DADR=(1.0-EDP*COSDE)**(-1)
              SINFD=SINFD*DADR
              COSFD=COSFD*DADR
              CS2GFD=DCOS(2.0*GDP+2.0*FDP)
              DADR2=DADR*DADR
              DADR3=DADR2*DADR
              COSFD2=COSFD*COSFD
C COMPUTE A (SEMI-MAJOR AXIS)
C
              A = ADP*(1.0+GM2*((3.0*THETA2-1.0)*(EDP2/(CN2*CN2*CN2)))*(CN+(1.0/(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(CN+(1.0))*(C
            1+CN)))+((3.0*THETA2-1.0)/(CN2*CN2*CN2))*(EDP*COSFD)*(3.0+3.0*EDP
            2*COSFD+EDP2*COSFD2)+3.0*(1.0-THETA2)*DADR3*CS2GFD))
              SN2GFD=DSIN(2.0*GDP+2.0*FDP)
              SNF2GD=DSIN(2.0*GDP+FDP)
              CSF2GD=DCOS(2.0*GDP+FDP)
              SN2GD=DSIN(2.0*GDP)
              CS2GD=DCOS(2.0*GDP)
              SN3GD=DSIN(3.0*GDP)
              CS3GD=DCOS(3.0*GDP)
              SN3FGD=DSIN(3.0*FDP+2.0*GDP)
              CS3FGD=DCOS(3.0*FDP+2.0*GDP)
              SINGD=DSIN(GDP)
              COSGD=DCOS (GDP)
              GO TO ID8, (163,164)
     163 DLT1E=B14*SINGD+B13*CS2GD-B15*SN3GD
C
C COMPUTE (L+G+H) PRIMED
              BLGHP=HDP+GDP+BLDP+B3*CS3GD+B1*SN2GD+B2*COSGD
              BLGHP=DMOD(BLGHP, PI2)
              IF(BLGHP.LT.0.0D0)BLGHP=BLGHP+PI2
              EDPDL=B4*SN2GD-B5*COSGD+B6*CS3GD-F1D4*CN2*CN*GMP2*(2.0*(3.0*THETA2
            1-1.0)*(DADR2*CN2+DADR+1.0)*SINFD+3.0*(1.0-THETA2)*((-DADR2*CN2
            2-DADR+1.0)*SNF2GD+(DADR2*CN2+DADR+F1D3)*SN3FGD))
              DLTI=F1D2*THETA*GMP2*SINI*(EDP*CS3FGD+3.0*(EDP*CSF2GD+CS2GFD))
            1-(A21/CN2)*(B8*SINGD+B7*CS2GD-B9*SN3GD)
              SINDH=(1.0/COSI2)*(F1D2*(B12*CS3GD+B11*COSGD+B10*SN2GD-(F1D2*GMP2
            1*THETA*SINI*(6.0*(EDP*SINFD-BLDP+FDP)-(3.0*(SN2GFD+EDP*SNF2GD)+EDP
            2*SN3FGD)))))
C
C COMPUTE (L+G+H)
```

```
С
  164 BLGH=BLGHP+((1.0/(CN+1.0))*F1D4*EDP*GMP2*CN2*(3.0*(1.0-THETA2)*
     1(SN3FGD*(F1D3+DADR2*CN2+DADR)+SNF2GD*(1.0-(DADR2*CN2+DADR)))+2.0*
     2SINFD*(3.0*THETA2-1.0)*(DADR2*CN2+DADR+1.0)))+GMP2*F3D2*((-2.0*
     3THETA-1.0+5.0*THETA2)*(EDP*SINFD+FDP-BLDP))+(3.0+2.0*THETA-5.0*
     4THETA2)*(GMP2*F1D4*(EDP*SN3FGD+3.0*(SN2GFD+EDP*SNF2GD)))
     BLGH=DMOD(BLGH, PI2)
     IF(BLGH.LT.0.0D0)BLGH=BLGH+PI2
     DLTE=DLT1E+(F1D2*CN2*((3.0*(1.0/(CN2*CN2*CN2))*GM2*(1.0-THETA2)
     1*CS2GFD*(3.0*EDP*COSFD2+3.0*COSFD+EDP2*COSFD*COSFD2+EDP))-(GMP2
     2*(1.0-THETA2)*(3.0*CSF2GD+CS3FGD))+(3.0*THETA2-1.0)*GM2*(1.0/
     3(CN2*CN2*CN2))*(EDP*CN+(EDP/(1.0+CN))+3.0*EDP*COSFD2+3.0*COSFD+
     4EDP2*COSFD*COSFD2)))
      EDPDL2=EDPDL*EDPDL
      EDPDE2=(EDP+DLTE)*(EDP+DLTE)
C
C COMPUTE E (ECCENTRICITY)
      E=DSQRT(EDPDL2+EDPDE2)
      SINDH2=SINDH*SINDH
      SQUAR=(DLTI*COSI2*F1D2+SINI2)*(DLTI*COSI2*F1D2+SINI2)
      SQRI=DSQRT(SINDH2+SQUAR)
C COMPUTE BI (INCLINATION)
     BI=DARSIN(SQRI)
     BI=2.0*BI
      BI=DMOD(BI,PI2)
      IF(BI.LT.0.0D0)BI=BI+PI2
С
C CHECK FOR E (ECCENTRICITY)=0
      IF(E.NE.0.0) GO TO 168
      BL=0.0
C
C CHECK FOR BI (INCLINATION)=0
  145 IF(BI.NE.0.0) GO TO 169
     H=0.0
C COMPUTE G (ARGUMENT OF PERIGEE)
  146 G=BLGH-BL-H
      G=DMOD(G,PI2)
      IF(G.LT.0.0D0)G=G+PI2
C
C COMPUTE TRUE ANOMALY
      EA = DKEPLR(BL, E)
      ARG1 = DSIN(EA) * DSQRT(1.0-E**2)
     ARG2 = DCOS(EA) - E
      IF = DATANO(ARG1,ARG2)
      OSCELE(1) = A*AE
```

```
OSCELE(2) = E
      OSCELE(3) = BI
      OSCELE(4) = H
      OSCELE(5) = G
      OSCELE(6) = BL
    7 CONTINUE
      DPELE(1) = ADP*AE
      DPELE(2) = EDP
      DPELE(3) = BIDP
      DPELE(4) = HDP
      DPELE(5) = GDP
      DPELE(6) = BLDP
      IF(IPERT.EQ.0)BL = DMOD(ANU*DELT,PI2)
      ORBEL(1) = EADP
      ORBEL(2) = GDP + FDP
      ORBEL(3) = GDP
      ORBEL(4) = EK*(ANU + BLDOT)
      ORBEL(5) = FDP
      R = A*AE*(1.0D0 - E*DCOS(EA))
      GO TO 45
C MODIFICATIONS FOR CRITICAL INCLINATION
С
  158 DLT1E=0.0
      BLGHP=0.0
      EDPDL=0.0
      DLTI=0.0
      SINDH=0.0
      ASSIGN 164 TO ID8
     GO TO 150
  168 SINLDP=DSIN(BLDP)
      COSLDP=DCOS(BLDP)
      SINHDP=DSIN(HDP)
      COSHDP=DCOS (HDP)
С
C COMPUTE L (MEAN ANOMALY)
C
       ARG1=EDPDL*COSLDP+(EDP+DLTE)*SINLDP
       ARG2=(EDP+DLTE)*COSLDP-(EDPDL*SINLDP)
       BL=DATAN2(ARG1,ARG2)
       BL=DMOD(BL,PI2)
       IF(BL.LT.0.0D0)BL=BL+PI2
       GO TO 145
C COMPUTE H (LONGITUDE OF ASCENDING NODE)
   169 ARG1=SINDH*COSHDP+SINHDP*(F1D2*DLTI*COSI2+SINI2)
       ARG2=COSHDP*(F1D2*DLTI*COSI2+SINI2)-(SINDH*SINHDP)
       H=DATAN2(ARG1,ARG2)
       H=DMOD(H,PI2)
       IF(H.LT.0.0D0)H=H+PI2
       GO TO 146
    45 CONTINUE
       RETURN
```

```
SUBROUTINE CELEM (ORBEL, GMC, PV, VV)
      ORIGINAL VERSION...1/22/71...CHARLES K. CAPPS
C
С
      PURPOSE:
C
                  THIS ROUTINE CONVERTS CLASSICAL OSCULATING ORBITAL ELEMENTS
            T \cap
С
            CARTESIAN ELEMENTS.
С
      CALLING SEQUENCE:
            CALL CELEM(ORBEL, GMC, PV, VV)
С
С
      INPUT THROUGH ARGUMENT LIST:
C
                  ORBEL(1) = SEMI-MAJOR AXIS, A (OSCULATING ELEMENTS)
С
                  ORBEL(2) = ECCENTRICITY, E
С
                  ORBEL(3) = INCLINATION, I
С
                  ORBEL(4) = LONGITUDE OF ASCENDING NODE, CAP OMEGA
С
                  ORBEL(5) = ARGUMENT OF PERIFOCUS, OMEGA
С
                  ORBEL(6) = MEAN ANOMALY, M
C
                  GMC = GRAVITATIONAL CONSTANT
С
      OUTPUT THROUGH ARGUMENT LIST:
С
                  PV = CARTESIAN POSITION VECTOR
С
                  VV = CARTESIAN VELOCITY VECTOR
C
      METHOD:
                  USES MILES STANDISH ITERATIVE SCHEME FOR SOLUTION TO
C
            KEPLERS EQN.
C
      REFERENCES:
С
                  GTDS TASK SPEC FOR CELEM, C.E. VELEZ, 13 JANUARY 1971
С
                  DODS SYSTEM DESCRIPTION, SUBROUTINE KEPLR1
                  P. EXCOBAL- "METHODS OF ORBIT DETERMINATION"
C
C
                  X-552-67-421, "COMPARISON OF ITERATIVE TECHNIQUES FOR THE
            SOLUTION OF
            KEPLERS EQUATION", I.COLE AND R.BORCHERS
C
С
            PROGRAMMER:
C
                  CHARLES K. CAPPS, CODE 553.2, GSFC
C
        IMPLICIT REAL*8(A-H,O-Z)
        DATA MAX /10/
        DIMENSION PV(3), VV(3), ORBEL(6)
        DATA TOL /+0.5D-16/
        ITER = 0
C
        FIND IF THIS IS ELLIPTIC OR HYPERBOLIC ORBIT
        IF (ORBEL (1).LE.0.0D0.AND.ORBEL(2).GT.1.0D0) GO TO 50
C
        ELLIPTIC ORBIT TAKES THIS ROUTE.
        FIRST FIND ECCENTRIC ANOMALY VIA NEWTONS (MILES STANDISH VERSION)
        E1 = ORBEL(6)
  10
        F = E1 - (ORBEL(2) * DSIN(E1)) - ORBEL (6)
        D = 1.0D0 - (ORBEL (2) * DCOS (E1 - 0.5D0 *F))
        E2 = E1 - (F / D)
        IF (DABS (E1-E2)-TOL)40,40,20
  20
        ITER = ITER + 1
        E1 = E2
        IF(ITER - MAX) 10,10,30
        SET UP ERROR CODE TO RETURN FROM SUBROUTINE
  30
        NERR = 13
       ECCENTRIC ANOMALY CONVERGED, NOW GET XO, YO, R
  40
       COSE = DCOS(E2)
```

```
SINE = DSIN (E2)

TEMP = 1.0D0 - ORBEL(2) * ORBEL (2)

XO = ORBEL(1) * (COSE - ORBEL(2))

YO = ORBEL(1) * (DSQRT(TEMP)* SINE)

R = ORBEL(1) * (1.0D0 - ORBEL (2) * COSE)

XOD = (-DSQRT(GMC* ORBEL(1))* SINE)/R

YOD = (DSQRT(GMC*ORBEL(1))* (TEMP))*COSE) /R

GO TO 100

C HYPERBOLIC ORBITS TAKE THIS ROUTE

50 E1 = ORBEL(6) /2.0D0

60 F = ORBEL(2) * DSINH(E1) - E1 - ORBEL(6)

D = ORBEL(2) * DCOSH(E1 - 0.5D0 * F ) - 1.0D0
```

```
E2=E1-(F/D)
        IF (DABS (E1-E2)-TOL)90,90,70
     70 ITER = ITER + 1
       E1 = E2
       IF (ITER - MAX) 60,60,80
C
       SET UP ERROR CODE FOR NON-CONVERGENCE PRIOR TO EXIT.
    80 \text{ NERR} = 14
С
       ECCENTRIC ANOMALY COMPUTED, NOW GET XO, YO, R
    90 COSE = DCOSH (E2)
       SINE = DSINH(E2)
       TEMP = ORBEL(2) * ORBEL(2) - 1.0D0
       XO = ORBEL(1)*(COSE-ORBEL(2))
       YO = -ORBEL (1)*DSQRT (TEMP) * SINE
       R = ORBEL (1)*(1.0D0 - ORBEL(2) * COSE)
       XOD = (-DSQRT(-GMC*ORBEL(1))*SINE)/R
       YOD = (DSQRT(-GMC*ORBEL(1)*TEMP)*COSE)/R
   100 COSO = DCOS(ORBEL(5))
       SINO = DSIN (ORBEL(5))
       COSOM = DCOS (ORBEL(4))
       SINOM = DSIN (ORBEL(4))
       COSI = DCOS(ORBEL(3))
       SINI = DSIN (ORBEL(3))
       B11 = COSO * COSOM - SINO * SINOM * COSI
       B21 = COSO * SINOM + SINO * COSOM * COSI
       B31 = SINO * SINI
       B12 = -SINO * COSOM - COSO * SINOM * COSI
       B22 = -SINO * SINOM + COSO * COSOM * COSI
       B32 = COSO * SINI
C
       NOW MULTIPLY 3 X 2 MATRIX BY 2 X 1 VECTORS FOR POSITION, VELOCITY.
       PV(1) = B11 * XO + B12 * YO
       PV(2) = B21 * XO + B22 * YO
       PV(3) = B31 * XO + B32 * YO
       VV(1) = B11*XOD + B12 * YOD
       VV(2) = B21 * XOD + B22 * YOD
       VV(3) = B31 * XOD + B32 * YOD
   999 RETURN
       END
      DOUBLE PRECISION FUNCTION DATANO(ARG1, ARG2)
C
                  VERSION OF 03/10/71
C
С
                  FORTRAN IV FUNCTION SUBROUTINE FOR THE IBM-360
C
C
                  PURPOSE
C
                              COMPUTE A VALUE FOR THE ARCTAN BETWEEN 0 AND 2
C
                  TANGENT IS DEFINED BY THE TWO INPUT ARGUMENTS AS ARG1/ARG2
С
С
                  CALLING SEQUENCE
С
                              NONE
С
                  INPUT
С
                              ARG1 - FIST ARGUMENT OF THE ARC TANGENT
С
                              ARG2 - SECOND ARGUMENT OF THE ARC TANGENT
С
```

```
С
                 OUTPUT
С
                             A DOUBLE PRECISION ARC TANGENT (+ VALUE BETWEEN
                 0 AND 2PI)
С
С
                 METHOD
С
С
                             USES FORTRAN MATH SUBROUTINE DATAN2 WHICH
                 RETURNS A VALUE
С
                 BETWEEN -PI AND PI, GIVEN TWO ARGUMENTS
C
С
                 REQUIRED SUBROUTINES
С
                             1- FUNCTION SUBROUTINE DATAN2
С
С
                 PROGRAMMER
С
                             R. E. GILLIAN - COMPUTING AND SOFTWARE
C
C******START PROGRAM****************************
C
С
                 COMPUTE ARCTAN BETWEEN -PI AND PI
C
      IMPLICIT REAL*8 (A-H,P-Z)
  50 DATAN0=DATAN2(ARG1,ARG2)
С
C
                 IF ARCTAN IS NEGATIVE, ADD 2PI TO THE RESULT
 100 IF(DATANO.GE.O) GO TO 999
     DATAN0 = DATAN0 + 6.283185307179586D0
     ARG = DATANO
  999 RETURN
     END
     FUNCTION DKEPLR(M,E)
     IMPLICIT REAL*8(A-H,O-Z)
     REAL*8 M,PI2/6.283185307179586D0/,TOL/0.5D-15/
C
C SUBROUTINE TO SOLVE KEPLER'S EQUATION
C KEPLER'S EQUATION RELATES GEOMETRY OR POSITION IN ORBIT PLANE TO TIME.
C
C M - MEAN ANOMALY (0<M<2PI)
C E - ECCENTRICITY
C EA - ECCENTRIC ANOMALY
     EA = 0
     IF(M)1,2,1
   1 EA=M + E*DSIN(M)
     DO 22 I=1,12
     OLDEA=EA
     FE=EA-E*DSIN(EA)-M
     EA=EA-FE/(1-E*DCOS(EA-0.5D0*FE))
C TEST FOR CONVERGENCE
     DELEA=DABS (EA-OLDEA)
     IF(DELEA.LE.TOL)GO TO 2
   22 CONTINUE
    2 EA=DMOD(EA,PI2)
```

```
DKEPLR=EA
     RETURN
     END
     SUBROUTINE MA3331(/A/,/B/,/C/)
С
С
     PURPOSE
С
         TO COMPUTE THE PRODUCT OF A 3X3 MATRIX AND A 3X1 MATRIX
С
С
     VERSION OF JULY 23, 1971
С
C
     METHOD
С
         WRITE THE EXPLICIT CODE FOR THE MULTIPLICATION OF A 3X3 MATRIX AND
С
     A 3X1 MATRIX AND RETURN THE RESULT IN THE 'C' MATRIX
С
С
     CALLING SEQUENCE
C
         CALL MAT31(A,B,C)
С
              = INPUT 3X3 MATRIX
С
         В
              = INPUT 3X1 MATRIX
С
              = OUTPUT 3X3 MATRIX
C
С
     PROGRAMMER
С
         N.R. BURTON COMPUTER SCIENCES CORPORATION
С
     ********START PROGRAM*********************
С
     IMPLICIT
                    REAL*8(A-H,O-Z)
     DIMENSION A(9), B(3), C(3)
     C(1)=A(1)*B(1)+A(4)*B(2)+A(7)*B(3)
     C(2)=A(2)*B(1)+A(5)*B(2)+A(8)*B(3)
     C(3)=A(3)*B(1)+A(6)*B(2)+A(9)*B(3)
     RETURN
     END
```

```
SUBROUTINE XYZPLH(EQS, XSTA, YSTA, ZSTA, RLAT, RLON, AE, HE, IERR)
C
С
                 FORTRAN IV SUBROUTINE FOR THE IBM-360, 3/20/74 VERSION
С
                 PURPOSE
С
                             TO CONVERT STATION COORDINATES FROM THE EARTH-
                 FIXED CARTESIAN
C
                 COORDINATES TO GEODETIC LATITUDE, EAST LONGITUDE, AND
SPHEROID C
                       HEIGHT
С
                 CALLING SEQUENCE
C
                 XYZPLH(EQS, XSTA, YSTA, ZSTA, RLAT, RLON, HE, IERR, AE)
С
С
                             EQS - ECCENTRICITY OF THE BODY SQUARED
С
                             AE - SEMI-MAJOR AXIS
С
                             XSTA - EARTH-FIXED CARTESIAN COORDINATE X
С
                             YSTA - EARTH-FIXED CARTESIAN COORDINATE Y
C
                             ZSTA - EARTH-FIXED CARTESIAN COORDINATE Z
C
                 OUTPUT
С
                             RLAT - GEODETIC LATITUDE
C
                             RLON - EAST LONGITUDE
C
                             HE - SPHEROID HEIGHT
                             IERR - ERROR FLAG
C
C
                                0=HEIGHT CONVERGED
С
                                1=HEIGHT DID NOT CONVERGE
С
                                2=LONGITUDE IS UNDEFINED
С
                 REQUIRED SUBPROGRAMS
C
                             DATAN0
С
                 PROGRAMMER
                            R.E. GILLIAN, COMPUTING AND SOFTWARE
IMPLICIT REAL*8(A-H,P-Z)
     IERR=0
     T=EQS*ZSTA
     XYSQ=XSTA**2+YSTA**2
     IF (DABS(ZSTA).GE.1.0D-15) GO TO 5
     HE = DSQRT(XYSQ) - AE
     RLAT = 0.0 D0
     GO TO 21
    5 DO 10 J = 1, 25
      ZT = ZSTA + T
     H1=DSQRT(XYSQ+ZT**2)
     SINPHI=ZT/H1
     ESQSP=EQS*SINPHI
     H2=AE/DSQRT(1.0D0-ESQSP*SINPHI)
     T1=H2*ESQSP
     IF(DABS((T1-T)/T1).LT..1D-14) GO TO 20
   10 T=T1
     IERR=1
     GO TO 30
   20 HE=H1-H2
     RLAT=DARSIN(SINPHI)
   21 IF(XSTA.EQ.0.0D0) GO TO 40
     GO TO 25
```

- 40 IF(YSTA.EQ.0.0D0) IERR=IERR+2 IF(IERR.GT.0) GO TO 30 IF(YSTA.LT.0.0D0) GO TO 50 RLON=3.14159265358793/2.0D0 GO TO 30
- 50 RLON=3.14159265358793*1.5D0 GO TO 30
- 25 RLON=DATANO(YSTA,XSTA)
- 30 CONTINUE RETURN End