

# CS3223 Database Systems

## Implementation

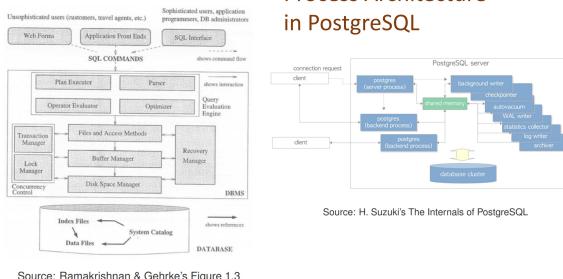
AY23/24 Sem 2, github.com/gerteck

### Introduction

#### Course Details

- Prerequisite Knowledge: CS2040S, CS2102, CS2106 background (helpful).
- Reference Textbook: Raghu & Johannes Database M. Systems, 2002. Encouraged to read ahead based on schedule before the lecture.
- Course covers data structures, algorithms, different components making up database systems.

#### Architecture of DBMS



Source: Ramakrishnan & Gehrke's Figure 1.3

- OLTP:** Online Transaction Processing is a type of data processing that consists of executing a number of transactions occurring concurrently—online banking, shopping, order entry, or sending text messages, for example.
- OLAP:** Online Analytical Processing.
- Focusing on centralized database running on a single server.

## 1. Data Storage

**References:** R&G Chapt 8. (Storage & Indexing Overview), Chapt 9. (Storing Data: Disks and Files).

#### A DBMS stores

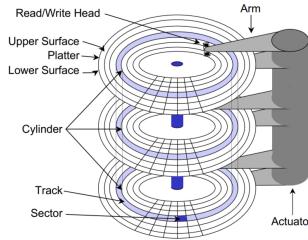
- Relations (Actual tables)
- System catalog (aka data dictionary) storing metadata about relations. (Relation schemas, structure of relations, constraints, triggers. View definitions, Indexes - derived info to speed up access to relations, Statistical information about relations for use by query optimizer.)
- Log files: Information maintained for data recovery.

#### DBMS Storage

**Memory Hierarchy:** Primary (registers, RAM), secondary (HDD, SSD), tertiary memory with capacity / cost / access speed / volatility tradeoffs.

- DBMS stores data on non-volatile disk for persistence.
- DBMS processes data in main memory (RAM).
- Disk access operations (I/O). Read: transfer data from disk to RAM. Write: transfer data from RAM to disk.
- Make use of index to speed up access, so that don't have to retrieve all the data when you run a query. Retrieve index and read only the block that contains specified data. Minimize I/O cost.

### Magnetic Hard-Disk Drive HDD



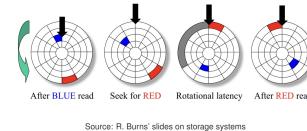
Source: R. Burns' slides on storage systems

- Cylinder, Track, Sector: Units of the HDD storage system. To read from different tracks, need to move the mechanical HDD arm.

#### Disk Access Time:

- command processing time: interpreting access command by disk controller.
- seek time: moving arms to position disk head on track.
- rotational delay: waiting for block to rotate under head.
- transfer time: actually moving data to/from disk surface.
- access time:** = seek time + rotational delay + transfer time. (CPT considered negligible).

#### Disk Access Time Components



- Seek time
  - avg. seek time: 5-6 ms
- Rotational delay (or rotational latency)
  - Depends on rotation speed - measured in rotations per minute (RPM)
    - Average rotational delay = time for  $\frac{1}{2}$  revolution
    - Example: For 10000 RPM, avg. rotational delay =  $0.5 \times (60 / 10000) = 3$  ms
- Transfer time
  - n = number of requested sectors on same track
    - transfer time =  $n \times \text{time for one revolution}$
    - avg. transfer time: 100-200  $\mu$ s
  - Sequential vs random I/O

#### Concept of Sequential vs random I/O.

- Sequential:** Both sector on same track.
- Random:** Sectors on different track, require seeking (moving arm).
- Given a set of data, we hope to store the data contiguously, on the same track. (Minimize incurring random I/O). If data is too large, store on same track, but different surface (aka same cylinder).
- Complexity hidden to OS by disk controller. Shown as a sequence of memory locations.

#### Solid-State Drive: SSD

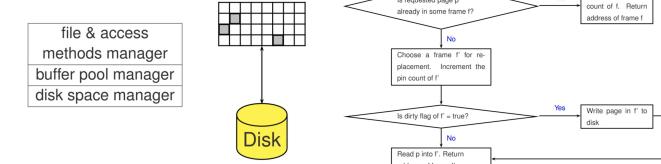
- Build with NAND flash memory without any mechanical moving parts. Lower power consumption.
- Random I/O:** 100x faster than HDD. (no moving parts)
- Sequential I/O:** slightly faster than HDD ( 2x )
- Disadvantages:** update to a page requires erasure of multiple pages ( 5ms ) before overwriting page. Limited number of times a page can be erased (  $10^5 - 10^6$  )

#### Storage Manager Components

- Data is stored, retrieved in units called **disk blocks (or pages)**.
  - Each block = sequence of one or more contiguous sectors.
- Files & access methods layer (aka file layer)** - deals with organization and retrieval of data.
- Buffer Manager** - controls reading/writing of disk pages.

- Disk Space Manager** - keeps track of pages used by file layer.

Storage Manager   Buffer Manager   BM: Handling request for page p Components



#### Buffer Manager

- Buffer pool:** Main memory allocated for DBMS.
- Buffer pool is partitioned into block-sized pages called **frames**.
- Clients of buffer pool can request for disk page to be fetched into buffer pool, release a disk page in buffer pool.
- A page in the buffer is **dirty** if it has been modified & not updated on disk.
- Two variables** maintained for each frame in buffer pool:
  - pin count:** number of clients using page (initialized 0)
  - dirty flag:** whether page is dirty (initialized false)
- Free list: Keeps track of frames that are free / empty.
- Pin count:**
  - Incrementing pin count is **pinning** the requested page in its frame.
  - Decrementing is **unpinning** the page.

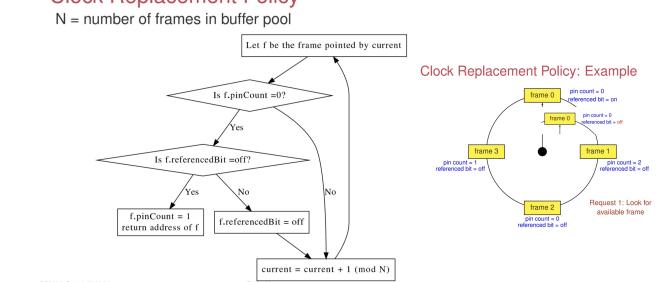
- Unpinning a page, dirty flag should be updated to true if page is dirty.
- A page in buffer can be replaced only when pin count is 0.
- Before replacing buffer page, needs to be written back to disk if its dirty flag is true.

- Buffer manager coordinates with transaction manager to ensure data correctness and recoverability.

#### Replacement Policies

- Replacement policy: Deciding which unpinned page to replace. (some examples:)
- Random, FIFO, Most Recently Used (MRU), Least Recently Used (LRU): (Use queue of pointers to frames with pin count = 0), most common, makes use of temporal locality.
- Clock:** cheaper popular variant of LRU
  - current** variable: points to some buffer frame.
  - Each frame has a **referenced bit**, turns on when its pin count turns 0.
  - Replace a page that has referenced bit off & pin count = 0.

#### Clock Replacement Policy



## Files

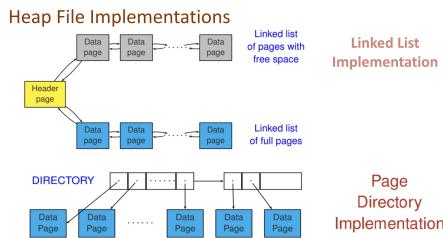
### File Abstraction

- Each relation is a file of records.
- Each record has a unique record identifier called RID / TID.
- Common file operations: create/delete file, insert record, delete/get record with given RID, scan all records.

**File Organization:** Method of arranging data records in a file that is stored on disk.

- **Heap file:** Unordered file
- **Sorted file:** Records order on some search key.
- **Hashed file:** Records located in blocks via a hash function.

### Heap File Implementations



- **Linked list implementation:** Two linked lists, one with pages with free space, other of completely full pages.
- **Page Directory Implementation:** Two leveled implementation. Each big block is a disk block with some metadata. Each disk block has a number of data pages.

### Page Formats:

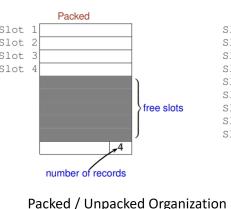
Records are organized within a page and referenced with the RID.

- **RID = (page id, slot number)**
- For **Fixed-Length Records**, Organization can be:

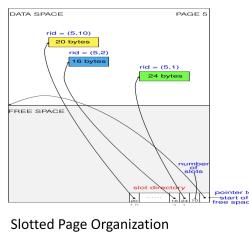
- **Packed Organization:** Store records in contiguous slots.
- For packed organization, memory organization is tough and costly when record in slot is deleted, need to move up a record. But as RID serves as a reference, but need to propagate change in RID.
- **Unpacked Organization:** Uses bit array to maintain free slots.
- For unpacked organization, more bookkeeping needed (use bitmap, 1 & 0 to check if occupied) to store records.

- For **Variable-Length Records**: We could assume some maximum size, then use packed organization. But wasteful. Instead, we can use **Slotted Page Organization**.

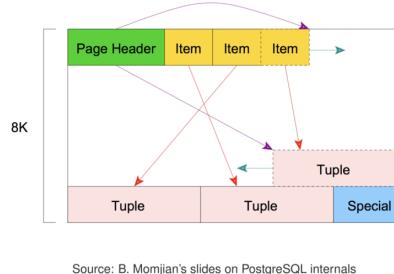
#### Fixed-Length Records:



#### Variable-Length Records:



## PostgreSQL's Slotted Page Organization



Source: B. Momjian's slides on PostgreSQL internals

### Record Formats: Organizing fields within a record.

- **Fixed-Length Records**
  - ▶ Fields are stored consecutively

F1	F2	F3	F4
----	----	----	----
- **Variable-Length Records**
  - ▶ Delimit fields with special symbols
  - ▶ Use an array of field offsets

F1	\$	F2	\$	F3	\$	F4
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Each  $o_i$  is an offset to beginning of field  $F_i$

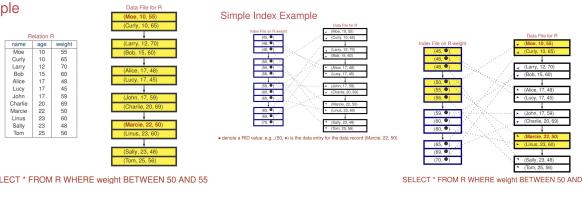
## 2. Indexing

Need some auxiliary data structure to make efficient queries.

### Index

- An **index** is a data structure to speed up retrieval of data records based on some search key.
- A **search key** is a sequence of  $k$  data attributes,  $k \geq 1$ . (A search key is aka *composite search key* if  $k > 1$ , e.g. (state, city).)
- An index is a **unique index** if search key is a candidate key, otherwise it is **non-unique index**.
- An index is stored as a file, records in index file referred to as **data entries**.

#### Example



### Index Types

Two main types of indexes

- **Tree-based Index:** Based on sorting of search key values (E.g. ISAM,  $B^+$ -tree)
- **Hash-based Index:** Data entries accessed using hashing function (E.g. static/ extendible / linear hashing)
- Considerations when choosing an index:
  - Search Performance (Equality search:  $k = v$ , use hash-based.) (Range search, use tree)
  - Storage overhead
  - Update performance

## Tree-based Indexing: $B^+$ -Tree

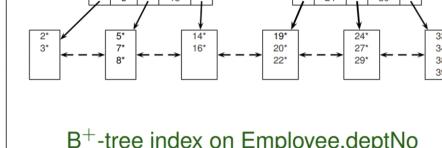
$B^+$  tree is a dynamic structure that adjusts to changes in the file gracefully, most widely used index structure as it adjusts well to changes and supports both equality and range queries.

- **Balanced tree:** Operations (insert, delete) on tree keep it balanced.
- **Internal nodes** direct the search.
- **Leaf nodes** contain the data entries. Leaf pages linked using page pointers for easy traversal of sequence of leaf pages in either direction.
- **Value  $d$**  is parameter of  $B^+$ -tree, called order of the tree, is a measure of capacity of a tree node. Each node contains  $m$  entries, where  $d \leq m \leq 2d$ , except root node, where  $1 \leq m \leq 2d$

### $B^+$ -tree Index

#### $B^+$ -tree Index

Employee	
name	deptNo
Alice	5
Bob	13
Charlie	19
Curly	39
Dave	38
Eve	14
Fred	33
Harry	2
John	34
Ken	6
Larry	27
Linus	24
Lucy	3
Marcie	22
Moe	29
Sally	20
Tom	7



- Each node is either a **leaf node** (bottom-most level) or an internal node.
- Top-most internal node is the **root node** located at **level 0**.
- **Height of Tree** = number of level of internal nodes. (Leaf nodes are at level  $h$  where  $h =$  height of tree).
- Nodes at same level are **sibling nodes** if they have the same parent node.
- **Leaf Nodes:**

- Leaf nodes store sorted data entries.
- $k^*$  denote data entry of form  $(k, RID)$ , where  $k$  = search key value of corresponding data record,  $RID =$  RID of data record.
- Lead nodes are doubly-linked to adjacent nodes.

- **Internal Nodes:**

- Internal nodes store index entries of the form  $(p: pointer, k: separator)$  ( $p_0, k_1, p_1, k_2, p_2, \dots, p_n$ )
- $k_1 < k_2 < \dots < K_n$
- Each  $(k_i, p_i)$  is an **index entry**,  $k_i$  serves as **separator** between node contents pointed to by  $p_{i-1}$  &  $p_i$
- $p_i$  = disk page address (root node of an index subtree  $T_i$ )

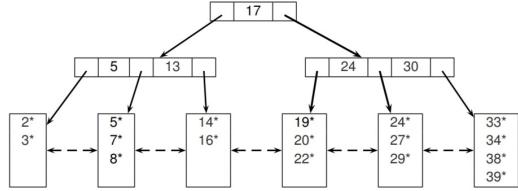
## $B^+$ -tree Index Properties

### Properties of $B^+$ -tree Index

- Dynamic index structure; adapts to data updates gracefully
- Height-balanced index structure
- Order of index tree,  $d \in \mathbb{Z}^+$

1. Controls space utilization of index nodes
2. Each non-root node contains  $m$  entries, where  $m \in [d, 2d]$
3. The root node contains  $m$  entries, where  $m \in [1, 2d]$

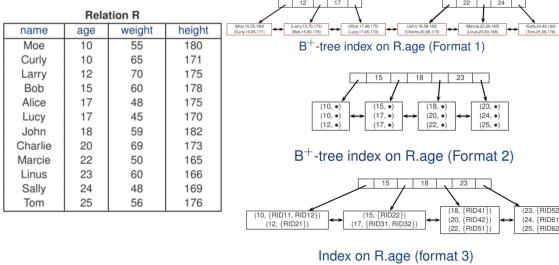
#### Example: $B^+$ -tree with order = 2



### Formats of Data Entries in B-Tree

- Format 1:  $k^*$  is actual data record (with search key value  $k$ )
- Format 2:  $k^*$  is of form  $(k, rid)$ , where rid is record identifier of record with search key value  $k$ .
- Format 3:  $k^*$  is of form  $(k, rid-list)$ , where rid-list is list of record identifiers of data records with search key value  $k$ .
- Note, examples assume Format 2.

#### Formats of Data Entries: Example

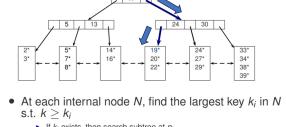


Index on R.age (format 3)

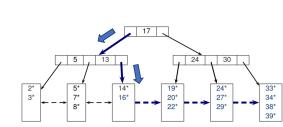
### $B^+$ -tree Search Algorithms

- Search algorithm finds the leaf node a given data entry belongs to.
- We assume no duplicates, no data entries same key value. Note in practice, duplicates arise whenever search key does not contain candidate key, must be dealt with.

#### Equality Search ( $k = 19$ )



#### Range Search ( $k \geq 15$ )



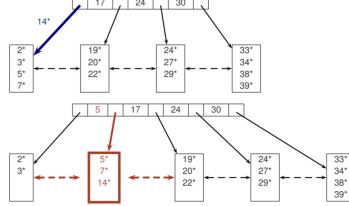
### $B^+$ -Tree Insertion

- Algorithm for insertion takes an entry, finds the leaf node where it belongs, and inserts it there.
- Occasionally, a node is full and must be split. (More than  $2d$  entries) When node is split, entry pointing to the node created by the split must be inserted into the parent.
- If the (old) root is split, a new root node is created and height of tree increases by 1.

### Splitting of overflowed node

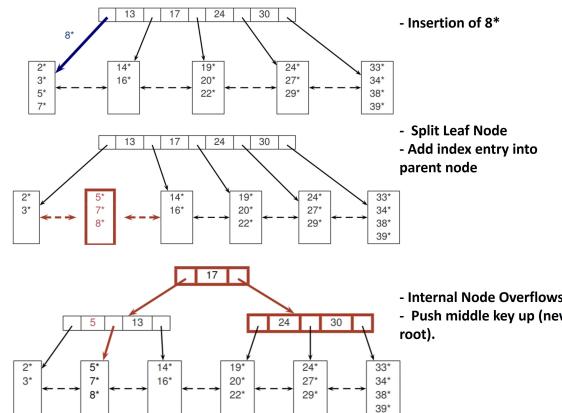
- Split overflowed leaf node by distributing  $d + 1$  entries to new leaf node.
- Create a new entry index using smallest key in leaf node.
- Insert new index entry into parent node of overflowed node.

#### Inserting 14\* (Splitting of overflowed node)

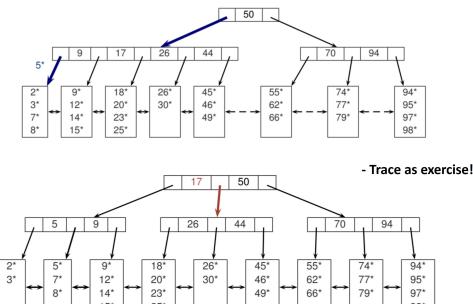


- Sometimes, node split is propagated upwards to ancestor internal nodes.
- When splitting an internal node, the middle key is pushed to parent node.

#### Inserting 8\* (Propagation of node splits)



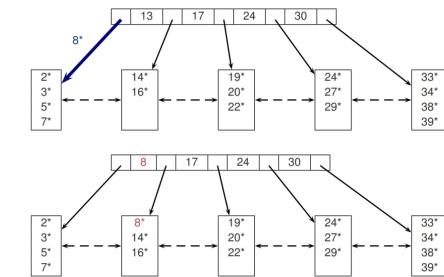
#### Inserting 5\* (Propagation of node splits)



### Redistributing of data entries in Overflow

- A node split can sometimes be avoided by distributing entries from overflowed node to a non-full adjacent sibling node.

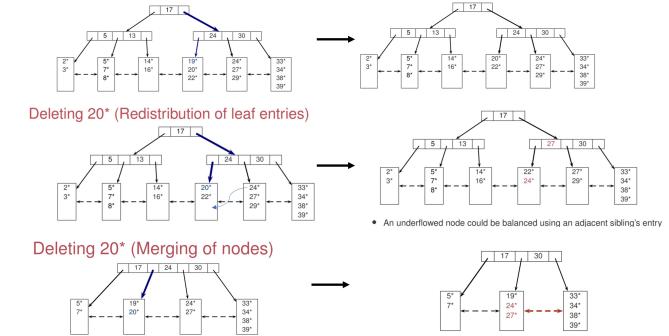
#### Inserting 8\* (Redistribution of data entries)



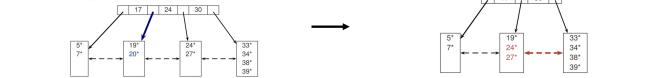
### $B^+$ -Tree Deletion

- Algorithm for deletion takes an entry, finds leaf node it belongs to, and deletes it.
- Underflowed node: When node is at minimum occupancy before deletion, and goes below threshold, we must either redistribute entries from adjacent sibling, or merge node with sibling to maintain minimum occupancy.
- Merging: Underflowed node needs to be merged if each of adjacent sibling nodes has exactly  $d$  entries.

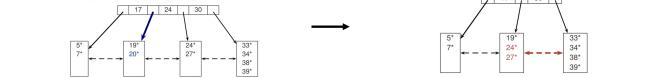
#### Deleting 19\* (Simple Case)



#### Deleting 20\* (Redistribution of leaf entries)

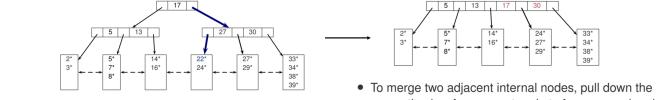


#### Deleting 20\* (Merging of nodes)

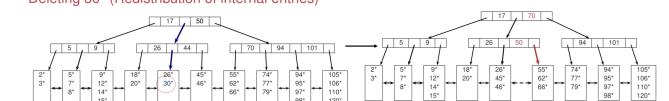


- Node mergers may propagate upwards.

#### Deleting 22\* (Propagation of node merges)



#### Deleting 30\* (Redistribution of internal entries)



- Chances are high that redistribution is possible if node has two siblings, and unlike merging, redistribution is guaranteed to propagate no further than parent node. Also, pages have more space, reducing likelihood of split on subsequent insertions.

## B<sup>+</sup> Tree Bulk Loading

- Entries added to a B<sup>+</sup> in two ways.

- Have existing collection of data records with B<sup>+</sup> tree index on it.  
When record added to collection, corresponding entry added to B<sup>+</sup> tree. (Insert, Delete individually)
- Have collection of data records we want to create new B<sup>+</sup> tree index on some key field(s). Start with an empty tree. Inserting one by one expensive due to overhead, systems provide **bulk loading** utility.

### Bulk Loading:

- Sort data entries  $k*$  to be inserted into B<sup>+</sup> tree according to search key  $k$ . (Here,  $d = 1$ ).
- Allocate empty page to serve as root. Insert a pointer to first page of (sorted entries into it).

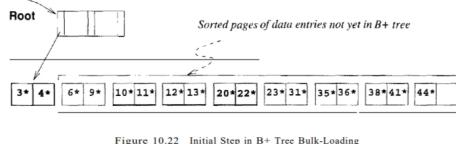


Figure 10.22 Initial Step in B+ Tree Bulk-Loading

- Add one entry to root page for each page of sorted data entries.  
Proceed until root page is full. Here, we must split root and create a new root page.

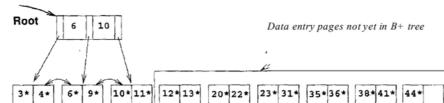


Figure 10.23 Root Page Fills up in B+ Tree Bulk-Loading

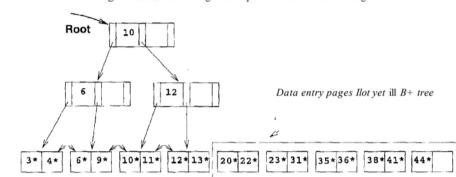


Figure 10.24 Page Split during B+ Tree Bulk-Loading

- To continue, entries for leaf pages **always inserted into right-most index page just above the leaf level**. When right-most page above leaf level fills up, it is split.

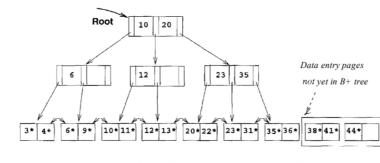
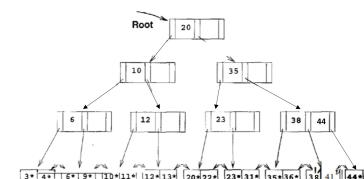


Figure 10.25 Before Adding Entry for Leaf Page Containing 38\*



## 3. Hash-based Indexing

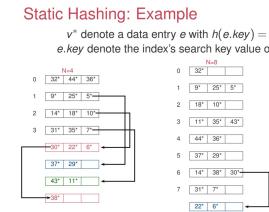
- Used for **equality queries**, not for range queries.
- Hashing techniques:** **Static hashing, dynamic hashing** (linear hashing, extendible hashing, etc).

### Static Hashing

- Data stored in  $N$  buckets**, fixed at creation time. Bucket consists of **one primary data page & chain** of zero or more overflow data pages.
- $v^*$  represents data entry  $e$  with  $h(e.key) = v$ , not search entry with RID.
- Problem with static hashing:** As data grows, longer overflow chain, efficiency drops. Need to periodically rehash and increase no. of buckets.

#### Static Hashing

- Data is stored in  $N$  buckets  $B_0, B_1, \dots, B_{N-1}$
- $N$  is fixed at creation time
- Hashing function  $h(\cdot)$  is used to identify the bucket to store a record.
  - A record with search key  $K$  is inserted into bucket  $B_i$ , where  $i = h(K) \mod N$
  - $\{K\}$  maps the search key value into a bit string
- Each bucket consists of **one primary data page** & a chain of zero or more overflow data pages



### Dynamic Hashing: Linear Hashing

- Hash file grows / shrinks linearly, systematic **splitting of buckets**.
- Overflow pages needed as overflowed bucket may not be split immediately.
- Hashing function changes dynamically and at given instant, **at most two (successive) hashing functions** used by the scheme during search.
- Each bucket has primary data page & chain of zero+ overflow pages.
- Insert in bucket  $B_i$  overflows if all pages in  $B_i$  (primary + overflow) full.

#### Linear Hashing (cont.)

- Assume initial file size of  $N_0$  buckets
  - Buckets  $B_0, B_1, \dots, B_{N_0-1}$
- File grows linearly by **splitting buckets** in rounds
  - At each round, buckets are split sequentially:  $B_i$  is split before  $B_{i+1}$
- How to split a bucket  $B_i$ ?
  - Add a new bucket  $B_i'$  (known as split image of  $B_i$ )
  - Redistribute entries in  $B_i$  between  $B_i$  &  $B_i'$
- File size increases by one bucket after each bucket split
- At the end of one round of splitting (i.e., every bucket at the start of the round has been split), file size is doubled
- Let  $N_i$  denote the file size at the beginning of round  $i$  ( $i=0, 1, \dots$ )
  - $N_0 = N_0$
  - At the end of round  $i$ ,  $N_i$  new buckets are added:  $B_{N_0}, B_{N_0+1}, \dots, B_{N_i-1}$ 
    - In round  $i$ , the split image of  $B_i$  is  $B_{N_i+i}$  for  $j \in [0, N_i - 1]$

#### Splitting Buckets

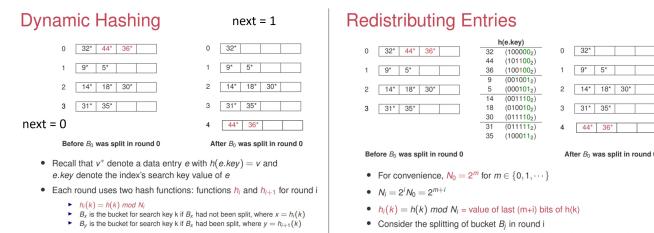
- Assume  $N_0 = 4$ 
  - In round 0, split image of bucket  $B_i$  is  $B_{i+1}$ , for  $i \in [0, 3]$
- In round 1,  $N_1 = 8$  & split image of bucket  $B_i$  is  $B_{i+4}$ , for  $i \in [0, 7]$ 
  - Before  $B_i$  was split in round 0
  - After  $B_i$  was split in round 0

### Dynamicity of Linear Hashing

#### Dynamic Hashing

next = 1

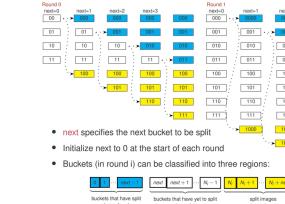
- Recall that  $v^*$  denote a data entry  $e$  with  $h(e.key) = v$  and  $e$  key denote the index's search key value of  $e$
- Each round uses two hash functions: functions  $h_i$  and  $h_{i+1}$  for round  $i$ 
  - $h_i(v) = h_{i+1}(v) \bmod N$
  - $B_i$  is the bucket for search key  $v$  if  $B_i$  had not been split, where  $x = h_i(v)$
  - $B_i$  is the bucket for search key  $v$  if  $B_i$  had been split, where  $y = h_{i+1}(v)$
- Keep track of which bucket to be split next using variable next



### Linear (Hashing) Splitting of Buckets (Insertion)

- Number in buckets represent the rightmost bit values.
- Split Criteria:** variable, could be when some bucket overflow, space utilization of file above some threshold etc.
- Level:** We use level to denote splitting round number (use with next).

### Splitting Buckets



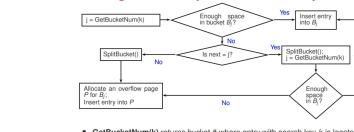
### When to split a bucket?

- The time to split the next bucket can be decided with various criteria:
  - Split whenever some bucket overflows
  - Split whenever space utilization of file is above some threshold
  - etc.
- Overflow pages are needed since an overflowed bucket might not be split immediately
- We shall assume that a bucket split is triggered whenever some **bucket overflows**
  - Bucket  $B_j$  overflows if it needs to be inserted into  $B_j$  and all the pages in  $B_j$  (i.e., primary + overflow pages) are full
- We use **level** to denote the splitting round number

### Examples: Linear Hashing Search & Insert

- Even though overflowed bucket split, not necessary mean enough space if bit value not right. Still require overflow page.
- Using **level and next**, we determine how many additional bits to consider in **second hashing function**.
- Second hashing function:** Is simply looking at the m rightmost bits of the hash.

#### Inserting data entry with search key k

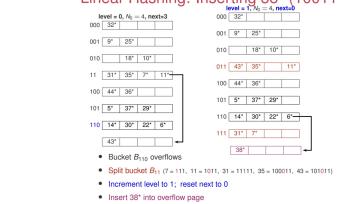


#### Example:

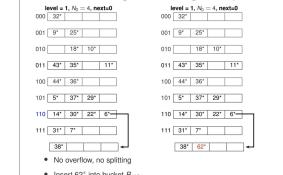
##### Linear Hashing: Inserting 43\* (101011)



##### Linear Hashing: Inserting 38\* (100110)



##### Linear Hashing: Inserting 62\* (111110)

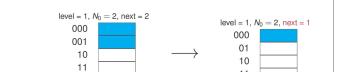


### Linear Hashing Deletion

- Opposite of insertion.
- Two cases:** 1. (Next  $\neq 0$ ), 2. (Next = 0, and level  $> 0$ .)

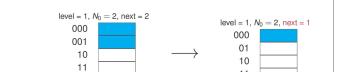
#### Linear Hashing: Deletion

- Locate bucket and delete entry
- If the last bucket  $B_{next-1}$  becomes empty, it can be removed
- Case 1:** If  $(next > 0)$ 
  - Decrement next by one



#### Linear Hashing: Deletion (cont.)

- Case 2:** If  $(next = 0)$  and  $(level > 0)$ 
  - Update next to point to the last bucket in previous level  $B_{next-1-1}$
  - Decrement level by one



#### Linear Hashing Performance, Summary

#### Linear Hashing: Performance

- One disk I/O unless the bucket has overflow pages
  - On average 1.2 disk I/O for uniform data distribution
  - Worst case:  $O(n)$  cost is linear in the number of data entries
- Poor space utilization with skewed data distribution

#### Linear Hashing: Summary

- File grows dynamically by splitting buckets linearly
  - Each bucket split adds one new bucket to file
- The bucket  $B_j$  for a search key  $k$  is determined using two hash functions ( $h_i$  and  $h_{i+1}$ )
  - Assume initial file has  $2^m$  buckets & total number of bits in key is  $m$
  - Bucket  $B_j$  is not yet been split in current round;  $\rightarrow h_i(k) \leq j < h_{i+1}(k)$
- In this course, we assume a bucket split is triggered whenever some bucket overflows due to an insertion
- Overflow pages are required for an overflowed bucket if it is not the next bucket to be split

## Dynamic Hashing: Extendible Hashing

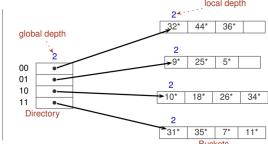
- Similar to Linear Hashing:** we want **bucket number to grow dynamically**, and use some **number of least significant bits of  $h(k)$**  to determine bucket address for search key  $k$ .
- Difference:** Add new bucket (as split image) when existing bucket overflows, No overflow pages (except when number of collisions exceed page capacity, two page entries collide if they have same  $h(.)$  hash value).

## Extendible Hashing

- Extendible hashing:** dynamically updatable disk-based index structure, implements hashing scheme utilizing a **directory of pointers to buckets**.
- Overflows handled by doubling the directory which logically doubles the number of buckets. **Physically, only the overflow bucket is split.**

### Extendible Hashing

- Uses a directory of pointers to buckets
- Directory has  $2^d$  entries
- Each entry has a unique  $d$ -bit address  $b_1b_2 \dots b_db_d$
- Two directory entries are said to correspond if their addresses differ only in the  $i^{th}$  bit (i.e.,  $b_i$ ), such entries are called corresponding entries.
- Each bucket maintains a local depth denoted by  $\ell \in [0, d]$
- All entries in a bucket with local depth  $\ell$  have the same last  $\ell$  bits in  $h(.)$



## Extendible Hashing Performance

- Performance:** At most 2 disk I/O for equality selection, at most 1 I/O if directory fits in main memory.
- Handling collision:** Two data entries **collide** if same hashed value, overflow pages need when number of collisions exceed page capacity.
- Compared with B+-tree index exact match queries ( $\log$  number of I/Os), E. Hashing better expected query cost  $O(1)$  I/O.

## Extendible Hashing: Handling Bucket Overflow

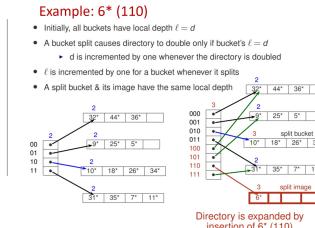
- Main idea: Determine if there is empty directory entry to point to new bucket. **2 Cases:** decision to split, or use empty directory entry.

### Case 1: Split bucket local depth = global depth

#### Extendible Hashing

##### Handling Bucket Overflow (Case 1)

- When a bucket overflows, it is split
  - Allocate a new bucket its **split image**
  - Redistribute entries (including new entry) between split bucket & its split image
- Case 1:** Split bucket's local depth is equal to global depth
  - When the directory is doubled,
  - Each new directory entry (except for the entry for the split image) points to the same bucket as its corresponding entry
- Number of directory entries pointing to a bucket =  $2^{d-\ell}$

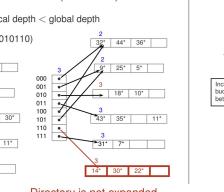


### Case 2: Split bucket local depth < global depth.

#### Extendible Hashing

##### Handling Bucket Overflow (Case 2)

- Case 2:** Split bucket's local depth < global depth
- Example: Inserting 22\* (010110)



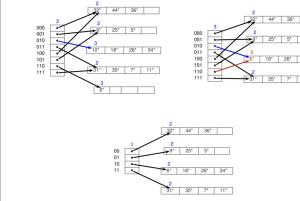
## Extendible Hashing Deletion

- To delete entry, simply locate Bucket and delete.
- Merging:** Mergeable if entries can fit within a bucket, and same local depth,  $j$  differs on in  $l^{th}$  bit.

### Extendible Hashing: Deletion

- Locate bucket  $B_j$  containing entry & delete entry
- If  $B_j$  becomes empty,  $B_j$  can be merged with the bucket  $B_i$  where both buckets have the same local depth  $\ell$  and  $i & j$  differs only in the  $l^{th}$  bit
  - $B_i$  is deallocated
  - $B_i$ 's local depth is decremented by one
  - Directory entries that point to  $B_i$  are updated to point to  $B_j$
- More generally,  $B_i$  &  $B_j$  (with same local depth  $\ell$  and  $i & j$  differs only in the  $l^{th}$  bit) can be merged if their entries can fit within a bucket
- If each pair of corresponding entries point to the same bucket, directory can be halved
  - $d$  is decremented by one

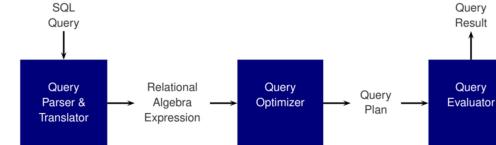
### Example: Deleting 10\* (1010)



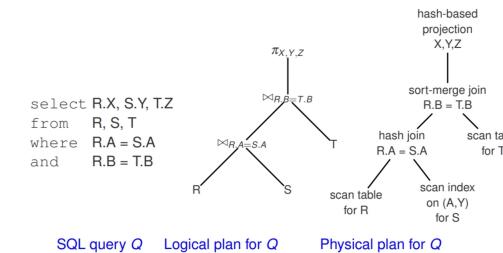
## 4. Query Evaluation: Sorting & Selection

DBMS describes data it manages using tables, indexes (metadata), which is stored in special tables (system catalogs). This data used to find best way to evaluate a query.

### Query Processing



### Query Plans



- SQL queries translate into extended form of relational algebra
- Query evaluation plans represented as tree of relational operators, with labels identifying algorithm to use at each node.
- R. operators building blocks for evaluating queries, implementation of operators optimized for good perf.

## External Sorting

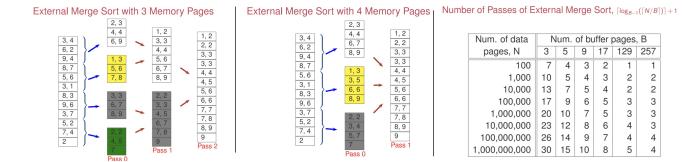
Sorting collection of records on some (search) key is useful and required in variety of situations, including

- Some sorted table of results: `SELECT * FROM student ORDER BY age .`
- Bulk loading a  $B^+$ -tree index
- Implementation of other relational algebra operators (e.g. projection, join), which require some sorting step.

When data to be sorted too large to fit into available main memory. Need some **external sorting algorithm**. Algos seek to minimize cost of disk accesses.

## External Merge Sort

- Main Idea:** Pass 0: Creating initial sorted runs (each of  $X$  memory pages), then continue during merging passes till you get final sorted pass.
- Sort entire file by breaking into smaller subfiles, sorting subfiles and merging using minimal amount of main memory at given time.
- Each sorted subfile is referred to as a run.**
- Sorting 11-page data  $R$  using 3 vs 4 memory pages:



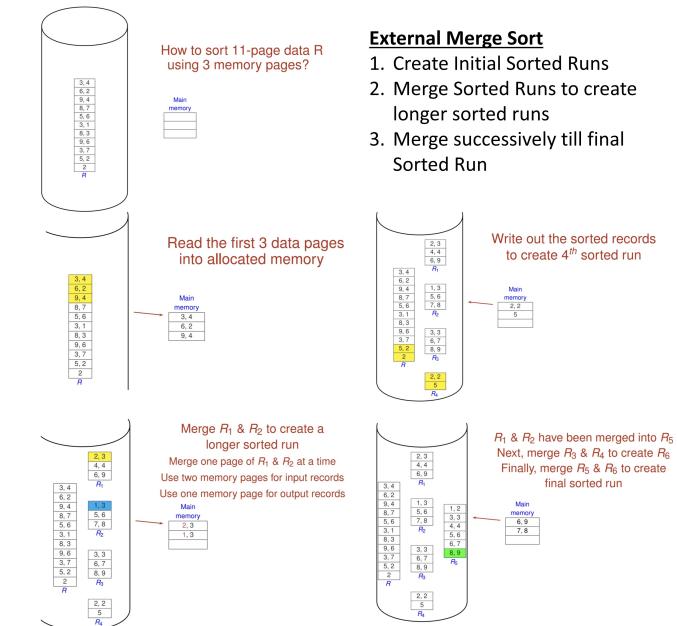
## External Merge Sort Analysis

- Note:** We consider only I/O costs, which approx by counting no. of pages read/written as per cost model. (Simple cost model to convey main idea).

### External Merge Sort

- Pass  $i$ ,  $i \geq 1$ : Merging of sorted runs
  - Use  $B-1$  buffer pages for input & one buffer page for output
  - Performs  $(B-1)$ -way merge
- Analysis:**
  - $N_0$  = number of sorted runs created in pass 0 =  $\lceil N/B \rceil$
  - Total number of passes =  $\lceil \log_2(\lceil N_0 \rceil) \rceil + 1$
  - Size of each sorted run =  $B$  pages (except possibly for last run)
  - \* Each pass reads  $N$  pages & writes  $N$  pages

### External Merge Sort Steps



## External Sort Optimization: I/O Cost vs. No. of I/Os

- Cost Metric:** No. of page I/Os.
- Only an approx of true I/O costs, ignores effect of **block(ed)** I/O, **single request to read/write several consecutive pages can be cheaper** than read/write same number of pages through independent I/O requests.
- Others:** Consider CPU costs as well, can use *double buffering* to keep CPU busy while I/O op. in progress.

## External Sort, Block(ed) Page I/O Optimization

### Non-Block(ed) Page I/O

- Consider only No. of page I/O as metric:** Minimize no. of passes in sorting, as each page in file read and written in each pass.
- This means we maximise fan-in **during merging** (aka, how many runs merged per pass), allocate just one buffer pool page per run, and one buffer page for output of merge.
- Hence, (B-1)-way merge per run, minimizing number of passes in sorting algorithm.

### Block(ed) Page I/O

- Optimization:** Access in blocks may reduce average cost to read/write single page, consideration to read/write in units of more than one page, or R/W in units of a **buffer block**.
- Buffer block**, of  $b$  pages.  $B$  is total number of buffer pages for sorting.

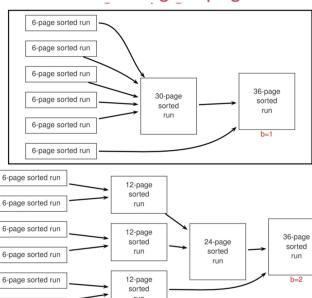
#### Optimization with Blocked I/O

- Read and write in units of **buffer blocks** of  $b$  pages
- Given an allocation of  $B$  buffer pages for sorting,
  - Allocate one block ( $b$  pages) for output
  - Remaining space can accommodate  $\lceil \frac{B-b}{b} \rceil$  blocks for input
  - Thus, can merge at most  $\lceil \frac{B-b}{b} \rceil$  sorted runs in each merge pass
- Analysis:**
  - $N$  = number of pages in file to be sorted
  - $B$  = number of available buffer pages
  - $b$  = number of pages of each buffer block
  - $N_b$  = number of initial sorted runs =  $\lceil N/B \rceil$
  - $F$  = number of runs that can be merged at each merge pass =  $\lceil \frac{B}{b} \rceil - 1$
  - Number of passes =  $\lceil \log_F(N_b) \rceil + 1$

- Set aside one buffer block for output of merge. ( $B - b$ ). One buffer block per input run ( $\frac{B-b}{b}$ ).

- Means can merge** at most floor( $\frac{B-b}{b}$ ) sorted runs in each merge pass.

#### Blocked I/O: Sorting 36-page data with $B=6$



#### Overall:

- Larger buffer blocks, (lower average page I/O cost).
- But num. passes increase, num page I/O increase.

- Decrease per-page I/O cost tradeoffs Increase No. of page I/Os.**

## Sorting using $B^+$ -trees

- When table to be sorted has existing  $B^+$ -tree index on sorting attributes.
  - Format 1: Sequentially scan leaf pages of  $B^+$ -tree.
  - Format 2/3: Sequentially scan leaf pages of  $B^+$ -tree. For each leaf page visited, retrieve data records using RIDs.

## Selection $\sigma_p(R)$

Select rows from Relation  $R$  that satisfy selection predicate  $p$

- Index Matching:** Index **matches** selection predicate if index can be used to evaluate it. Consider Hash index, and  $B^+$  Tree index.

### Access Path

- Access path** refers to the given way of accessing data records/entries.
  - Table scan:** scan all data pages.
  - Index scan:** scan all index pages.
  - Index Intersection:** Combine results from multiple index scans (e.g. intersect, union).
- Index scan/intersect follow by **RID lookups** to retrieve data records.

### Selectivity of Access Path

#### Selectivity of Access Path:

Number of index & data pages retrieved to access data record/entries

#### Most Selective Access Path:

(Smallest selectivity), retrieves fewest pages.

$Q_1: \text{select weight from } R \text{ where weight between 51 and 59}$   
 $Q_2: \text{select * from } R \text{ where weight between 51 and 59}$

- Most Selective Access Path minimizes cost of data retrieval.**

### Covering Index

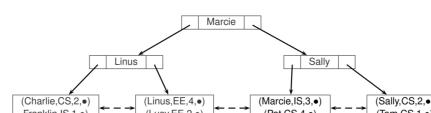
- An index  $I$  is a **covering index** for a query  $Q$  if all the attributes referenced in  $Q$  are part of the key or include column(s) of /
- $Q$  can be evaluated using  $I$  without any RID lookup
- Such an evaluation plan is known as **index-only plan**

#### Example:

- Consider query  $Q$ :  
 $\text{select major from Student where name = 'Bob'}$ 
  - An index on (name, major) is a covering index for  $Q$
  - An index on (name) is not a covering index for  $Q$
  - An index on (name) with include columns (address, major) is a covering index for  $Q$

### $B^+$ -Tree: Include Columns (In Index)

- Relation: Student(sid, name, major, year, address).
- $B^+$ -tree index on Student:  
`create index stu_name_index on Student (name) include (major, year);`

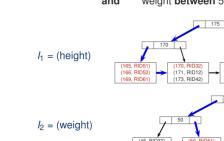


Query: `select major from Student where name = 'Lucy'`;

## $B^+$ -Tree: Selection Evaluation

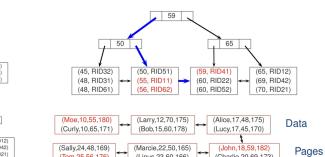
### $B^+$ -tree : Index Intersection

`select height, weight from Student where height between 164 and 170 and weight between 50 and 59`



### $B^+$ -tree : Index Scan + RID Lookups

`select name from Student where weight between 55 and 59 and age ≥ 20`



### CNF Predicates

- Selectivity of an access path** depends on primary conjuncts in selection condition (w.r.t. index involved.)
- Each conjunct acts as filter on table, fraction of tuples satisfying given conjunct called reduction factor.

- A **term** is of the form  $R.A \text{ op } c$  or  $R.A_i \text{ op } R.A_j$
- A **conjunct** consists of one or more terms connected by  $\vee$
- A conjunct that contains  $\vee$  is said to be **disjunctive** (or contains a disjunction)
- A **conjunctive normal form (CNF) predicate** consists of one or more conjuncts connected by  $\wedge$

**disjunctive conjunct**  
 $(\text{rating} \geq 8 \vee \text{director} = \text{"Coen"}) \wedge (\text{year} > 2003) \wedge (\text{language} = \text{"English"})$

**term/conjunct**      **term/conjunct**      **term/conjunct**      **term/conjunct**

- Non-equality Comparison Operators:**  $<$ ,  $\leq$ ,  $>$ ,  $\geq$ ,  $<>$ , between, in.

### Tree Index matching CNF Selection

- Determines if Index is useful / appropriate, if index can be used to retrieve just the tuples that satisfy the condition.

### $B^+$ -tree : Matching predicates

- $B^+$ -tree index  $I = (K_1, K_2, \dots, K_n)$
- Non-disjunctive CNF predicate  $p$
- $I$  matches  $p$  if  $p$  is of the form:

$$(K_1 = c_1) \wedge \dots \wedge (K_{i-1} = c_{i-1}) \wedge (K_i \text{ op } c_i), i \in [1, n]$$

zero or more equality predicates

- where  $(K_1, \dots, K_n)$  is a prefix of the key of  $I$ , and
- there is at most one non-equality comparison operator which must be on the last attribute of the prefix (i.e.,  $K_i$ )

Note: This definition is stronger than R&G's definition

### $B^+$ -tree : Matching predicates (cont.)

Example: Which predicates does  $I = (\text{age}, \text{weight}, \text{height})$  match?

- $\text{age} \geq 20$  Yes, match
- $\text{weight} = 80$  No
- $(\text{age} = 20) \wedge (\text{weight} = 70)$  Yes, match
- $(\text{age} = 20) \wedge (\text{weight} < 70)$  Yes, match
- $(\text{age} > 20) \wedge (\text{weight} = 70)$  No
- $(\text{age} = 20) \wedge (\text{height} = 170)$  Yes, match
- $(\text{height} > 180) \wedge (\text{weight} = 65) \wedge (\text{age} = 20)$  Yes, match
- $(\text{age} = 20) \wedge (\text{weight} \leq 65) \wedge (\text{height} = 180)$  No

### Hash Index matching CNF Selection

#### Hash Index: Matching predicates

Determines if entry lies in the bucket.

- Hash index  $I = (K_1, K_2, \dots, K_n)$
- Non-disjunctive CNF predicate  $p$
- $I$  matches  $p$  if  $p$  is of the form:

$$(K_1 = c_1) \wedge (K_2 = c_2) \wedge \dots \wedge (K_n = c_n)$$

#### Hash Index: Matching predicates (cont.)

Example: Which predicates does  $I = (\text{age}, \text{weight}, \text{height})$  match?

- $\text{age} \geq 20$
- $\text{weight} = 80$
- $(\text{age} = 20) \wedge (\text{weight} < 70)$
- $(\text{age} = 20) \wedge (\text{height} = 170)$
- $(\text{height} = 180) \wedge (\text{weight} = 65) \wedge (\text{age} = 20)$
- $(\text{age} = 20) \wedge (\text{weight} \leq 65) \wedge (\text{height} = 180)$

## Examples of Index matching CNF Selection

Example: B<sup>+</sup>-tree on (age,weight,height)

$p_1$ : (age = 20)



$p_2$ : (age = 18)  $\wedge$  (weight  $\geq$  50)

$p_2$



### EXAMPLE

- A relation R(a, b, c, d)
- Does the index match the predicate?

Predicate	B+ tree on (a,b,c)	Hash index on (a,b,c)
a=5 and b=3	yes	no
a=5 and b=4	yes	no
b=3	no	no
a=5 and c=10	no	no
a=5 and b=3 and c=1	yes	yes
a=5 and b=3 and c=1 and d > 6	yes	yes

a=5 and b=3 and c=1 are primary conjuncts here

CIS544 (Fall 2011); Park Kweon

## Primary and Covered Conjuncts

- Primary Conjuncts:** Subset of conjuncts in selection predicate  $p$  that index  $I$  matches.
- In general, only subset of conjuncts of predicate matches index.
- Covered Conjunct:** Conjunct C in predicate  $p$  covered if all attributes in  $C$  appear in the key, or *include column(s)* of index  $I$ .
- Primary conjuncts subset of covered conjuncts.

## Cost of Evaluation of Selection Predicate $p$

Notation	Meaning
$r$	relational algebra expression
$  r  $	number of tuples in output of $r$
$ r $	number of pages in output of $r$
$b_d$	number of data records that can fit on a page
$b_i$	number of data entries that can fit on a page
$F$	average fanout of B <sup>+</sup> -tree index (i.e., number of pointers to child nodes)
$h$	height of B <sup>+</sup> -tree index (i.e., number of levels of internal nodes)
$h = \lceil \log_F(\lceil \frac{  R  }{b_i} \rceil) \rceil$	if format-2 index on table $R$
$B$	number of available buffer pages

## Cost of B<sup>+</sup>-tree Index Evaluation of $p$

Let  $p'$  = primary conjuncts of  $p$ ,  $p_c$  = covered conjuncts of  $p$

1. Navigate internal nodes to locate first leaf page

$$Cost_{internal} = \begin{cases} \lceil \log_F(\lceil \frac{||R||}{b_i} \rceil) \rceil & \text{if } I \text{ is a format-1 index,} \\ \lceil \log_F(\lceil \frac{||R||}{b_i} \rceil) \rceil & \text{otherwise.} \end{cases}$$

2. Scan leaf pages to access all qualifying data entries

$$Cost_{leaf} = \begin{cases} \lceil \frac{||\sigma_{p'}(R)||}{b_d} \rceil & \text{if } I \text{ is a format-1 index,} \\ \lceil \frac{||\sigma_{p'}(R)||}{b_i} \rceil & \text{otherwise.} \end{cases}$$

3. Retrieve qualified data records via RID lookups

$$Cost_{rid} = \begin{cases} 0 & \text{if } I \text{ is covering or format-1 index,} \\ ||\sigma_{p_c}(R)|| & \text{otherwise.} \end{cases}$$

Cost of RID lookups could be reduced by first sorting the RIDs

$$\lceil \frac{||\sigma_{p_c}(R)||}{b_d} \rceil \leq Cost_{rid} \leq \min\{||\sigma_{p_c}(R)||, |R|\}$$

## Cost of Hash Index Evaluation of $p$

- Let  $p'$  = primary conjuncts of  $p$
- For format-1 index
  - Cost to retrieve data records: at least  $\lceil \frac{||\sigma_{p'}(R)||}{b_d} \rceil$

- For format-2 index

- Cost to retrieve data entries: at least  $\lceil \frac{||\sigma_{p'}(R)||}{b_i} \rceil$

$$\text{Cost to retrieve data records} = \begin{cases} 0 & \text{if } I \text{ is a covering index,} \\ \lceil \frac{||\sigma_{p_c}(R)||}{b_d} \rceil & \text{otherwise.} \end{cases}$$

## Evaluating Non-Disjunctive / Disjunctive Conjuncts

### Evaluating Non-Disjunctive Conjuncts

- Consider the query  $\sigma_p(R)$ , where  $p = (\text{age} = 21) \wedge (\text{weight} \geq 70) \wedge (\text{height} = 180)$
- Suppose the available unclustered indexes on  $R$  are
  - a hash index  $H_{age}$  on (age), and
  - a B<sup>+</sup>-tree index  $T_{weight}$  on (weight)
- What are the possible strategies to evaluate the following predicates?

- $p_1 = (\text{age} = 21) \vee (\text{height} = 180)$
- $p_2 = ((\text{age} = 21) \vee (\text{height} = 180)) \wedge (\text{weight} \geq 70)$
- $p_3 = (\text{age} = 21) \vee (\text{weight} \geq 70)$

### Evaluating Disjunctive Conjuncts

- Suppose the available unclustered indexes are
  - a hash index  $H_{age}$  on (age), and
  - a B<sup>+</sup>-tree index  $T_{weight}$  on (weight)
- What are the possible strategies to evaluate the following predicates?

- Possible strategies to evaluate Disjunctive / Non-Disjunctive predicates

- File scan, Use both (fetch RID, take Union), Use B+ tree etc.

### Example

- B<sup>+</sup>-tree index  $I = (\text{age}, \text{weight}, \text{height})$ , Format 2

- Query: select \* from R where  $p$

- $p = (\text{age} = 18) \wedge (\text{weight} = 60) \wedge (\text{height} = 3)$

- $p = (\text{age} \geq 18) \wedge (\text{weight} \geq 60)$

- $||R|| = 12$ ,  $||\sigma_p(R)|| = 9$ ,  $||\sigma_{p_c}(R)|| = 2$

- $b_d = 2$ ,  $b_i = 2$ , Height of  $I = 2$

- Evaluation cost of  $p$  using  $I = 2 + \lceil \frac{9}{2} \rceil + 2 = 9$

