libcasimir Documentation

Release 0.4.2

Michael Hartmann

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OVERVIEW AND FEATURES

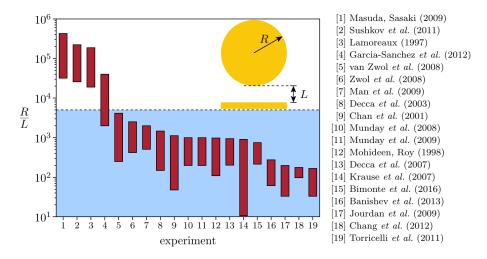


Fig. 1: Experiments in the plane-sphere geometry. The blue area denotes the aspect ratios that are accessible using libcasimir. The inset depicts the plane-sphere geometry.

libcasimir is an implementation of the Casimir effect in the plane-sphere geometry. The geometry consists of a sphere of radius R separated by a distance L from an infinite plate. The main goal of the library and the associated programs is to compute the free energy $\mathcal F$ depending on the radius of the sphere, the separation between sphere and plate, the temperature, and the dielectric properties of the objects. The library is highly optimized and allows you - depending on parameters and your hardware - to compute the free energy for aspect ratios up to $R/L \sim 10\,000$.

1.1 Features

- Calculate the free energy for different separations and temperatures
- Calculate the free energy in the high temperature limit
- Full support for perfect reflectors, Drude metals, and generic metals described by a user-defined dielectric function
- libcasimir is fast and reliable
- ready to use programs: you don't have to modify the code
- libcasimir is free software you may use it or even modify it

1.2 Further reading

Some of the numerical ideas used in this library are described in Hartmann, Ingold, Maia Neto, "Advancing numerics for the Casimir effect to experimentally relevant aspect ratios", Phys. Scr. 93, 114003 (2018). A more detailed description can be found in Hartmann, "Casimir effect in the plane-sphere geometry: Beyond the proximity force approximation", phd thesis (2018).

CHAPTER

TWO

INSTALLATION

In the following, we assume the operating system to be Ubuntu 18.04. The commands should also work on other Debian-like systems.

2.1 Compilation

The easiest way to get the source code is to use git. To install git, run

```
$ sudo apt install git
```

in a terminal. Once git is installed, the command

```
$ git clone https://github.com/michael-hartmann/libcasimir-dev.git
```

will get you the complete libcasimir repository and stores it in the directory libcasimir-dev/.

The libcasimir library and the programs are written in C and C++ using LAPACK and MPI. In order to compile the source files, you need a C and C++ compiler, the development files for LAPACK and MPI, and the build tools make and cmake. You can install all dependencies with:

```
\$ sudo apt install gcc g++ libc6-dev libc++-dev cmake make libopenmpi-dev openmpi-bin_ \hookrightarrow liblapack-dev libgfortran-7-dev gfortran-7
```

In order to compile the code, create a directory bin, run cmake followed by make:

```
$ cd libcasimir-src/
$ mkdir bin
$ cd bin/
$ cmake ../src
$ make
```

This command compiles the HODLR library and the libcasimir library and builds the shared objects libhodlr.so and libcasimir.so. Then, the programs casimir and casimir_logdetD are built. Note that you can also specify different compilers setting the variables CC and CXX. Here is an example how to use the Intel C and C++ compilers:

```
$ CC=icc CXX=icpc cmake ../src
$ make
```

In order to run the programs, the system must be able to find the libraries libhodlr.so and libcasimir.so. As the libraries are not in the default search path, you have to add the directories to LD_LIBRARY_PATH

```
$ export LD_LIBRARY_PATH=$LD_LIBRARY_PATH:/home/hendrik/libcasimir-dev/bin
```

where we have assumed that the libcasimir repository is in the directory /home/hendrik.

2.2 Testing

In order to check whether the compilation was successful, you can build and run the unit tests in bin/:

```
$ make tests
$ ./casimir_tests
```

All tests should pass. Running the tests takes up (depending on your hardware) about 7 minutes.

2.3 Improving performance

In order to improve performance, it might be necessary to tweak some compiler options. Be default, the optimization level is -03 which should give reasonable performance.

If you are running your code on the same machine where you compile the code, or the target machine supports the same instruction set, the option -march=native may increase performance. When there are problems, the program will crash with a message similar to "illegal instruction code". On my Intel Core i7 machine, this option gives a performance boost of $\sim 5\%$. To compile the code with this option, run:

```
$ cmake ../src -DOPT="-03 -march=native"
```

Similarily, link time optimization -flto might also increase performance. However, this option has basically no influence on the performance.

CHAPTER

THREE

PROGRAMS

3.1 casimir

The program casimir computes the free Casimir energy \mathcal{F} for the plane-sphere geometry as a sum

$$\mathcal{F} = \frac{k_{\rm B}T}{2} \sum_{n=-\infty}^{\infty} \sum_{m=-\infty}^{\infty} \log \det \left(1 - \mathcal{M}^m(\xi_n)\right)$$

over the Matsubara frequencies $\xi_n = 2\pi n k_{\rm B} T/\hbar$. For zero temperature T=0, the sum over the Matsubara frequencies becomes an integration.

The program supports a wide variety of options. You can get a summary of all options using casimir --help. By default, the temperature is set to T=0, and the sphere and plane are assumed to be perfect reflectors.

3.1.1 Mandatory options

There are two mandatory options: the separation L between sphere and plane, and the radius of the sphere R. The program expects the lengths given in units of meters. As an example, the following command computes the Casimir interaction at T=0 for perfect reflectors for a sphere of radius $R=50\mu m$ and a separation $L=2\mu m$:

```
$ mpirun -n 8 ./casimir -R 50e-6 -L 2e-6
```

The command mpirun will set up the environment for MPI and the flag -n specifies how many processes the program should use. If you want to utilize the full capacity of your machine and your processor has N cores, set -n to N+1. The output of this command looks similar to:

```
# compiler: gcc
# compile time: Jan 2 2019 12:35:13
# compiled on: Linux jonas.physik.uni-augsburg.de 4.9.0-8-amd64 #1 SMP Debian 4.9.130-
→2 (2018-10-27) x86_64 GNU/Linux
# git HEAD: 51b8df47618d15747e59321aee77e1f86fab32a8
# git branch: master
# pid: 23336
# start time: Thu Jan 3 12:27:38 2019
#
# LbyR = 0.04
# RbyL = 25
# L = 2e-06
# R = 5e-05
# T = 0
# cutoff = 1e-09
# epsrel = 1e-06
```

The output is in the format of a CSV file and additional comments start with a pound (#). The program first outputs some information on the compilation, i.e., time of compilation, name of compiler, machine where it was compiled and so on. Then, information about the geometry (radius, seperation, aspect ratio and inverse of aspect ratio), numerical parameters (cutoff, epsrel, iepsrel, ldim, cores) are printed. We will discuss the numerical parameters in more detail later. The value of cores is the number of MPI processes that are used for the computation. Then, the determinant of the scattering matrix for different Matsubara frequencies are printed. The comment starting with ier gives the result of the integration and is and ier=0 if the integration was successful. The program ends by printing the result of the computation. The free energy is outputed in units of $(L+R)/\hbar c$, i.e., for this example the free energy is

$$\mathcal{F} \approx \frac{-26.54\hbar c}{50\mu\mathrm{m} + 2\mu\mathrm{m}} \approx -1.61 \times 10^{-20}\mathrm{J}.$$

The PFA result in this case is $\mathcal{F}_{PFA} \approx -1.64 \times 10^{-20} \text{J}$.

The desired relative accuracy of the integration over the Matsubara frequencies can be set using --epsrel. By default, EPSREL is 10^{-6} . Note that the integrand needs to be sufficiently smooth. In particular, for very low values of EPSREL you might need to decrease the value of CUTOFF using --cutoff. The value of CUTOFF determines when the summation over m is stopped:

$$\frac{\log \det (1 - \mathcal{M}^m(\xi))}{\log \det (1 - \mathcal{M}^0(\xi))} < \text{CUTOFF}$$

The default value of CUTOFF is 10^{-9} . As a rule of thumb, in order that the integrand is sufficiently smooth for the integration routine, CUTOFF should be at least two orders of magnitude smaller than EPSREL.

By default, the integration routine uses an adaptive Gauss-Kronrod method provided by CQUADPACK. For perfect reflectors it is sometimes faster to use an adaptive exponentially convergent Fourier-Chebshev quadrature scheme (FCQS), see Boyd, "Exponentially convergent Fourier-Chebshev quadrature schemes on bounded and infinite intervals", JOSC 2, 2 (1987). You can use FCQS using the flag --fcqs. Since the adaptive algorithm is not well tested, this option is considered experimental.

3.1.2 Temperature

You can set the temperature using -T. The following program computes the free energy just like in the last example but at room temperature T = 300K:

```
$ mpirun -n 8 ./casimir -R 50e-6 -L 2e-6 -T 300
# compiler: gcc
# compile time: Jan 2 2019 12:35:13
# compiled on: Linux jonas.physik.uni-augsburg.de 4.9.0-8-amd64 #1 SMP Debian 4.9.130-
→2 (2018-10-27) x86_64 GNU/Linux
# git HEAD: 51b8df47618d15747e59321aee77e1f86fab32a8
# git branch: master
# pid: 24111
# start time: Thu Jan 3 12:51:15 2019
\# LbyR = 0.04
\# RbyL = 25
\# L = 2e-06
\# R = 5e-05
\# T = 300
# using Matsubara spectrum decomposition (MSD)
\# cutoff = 1e-09
# epsrel = 1e-06
# iepsrel = 1e-08
# 1dim = 176
# cores = 8
# model = perfect reflectors
# xi*(L+R)/c=0, logdetD=-6.16165739556559, t=0.025461
# xi*(L+R)/c=42.8046294355951, logdetD=-0.230987113168236, t=1.22125
# xi*(L+R)/c=85.6092588711902, logdetD=-0.00858232692932167, t=1.186
# xi*(L+R)/c=128.413888306785, logdetD=-0.000319205031747869, t=1.10549
\# xi*(L+R)/c=171.21851774238, logdetD=-1.18538336130793e-05, t=0.949226
\# xi*(L+R)/c=214.023147177976, logdetD=-4.39335203111237e-07, t=0.77597
# 302 determinants computed
# stop time: Thu Jan 3 12:51:21 2019
# L/R, L, R, T, ldim, E*(L+R)/(hbar*c)
0.039999999999999, 2e-06, 5e-05, 300, 176, -45.24539531432269
```

For finite temperature the free energy is no longer given as an integral, but as a sum over the Matsubara frequencies ξ_n . The summation is stopped once

$$\frac{\log \det (1 - \mathcal{M}(\xi_n))}{\log \det (1 - \mathcal{M}(0))} < \text{EPSREL}.$$

By default, EPSREL is 10^{-6} . You can change the value of EPSREL using the option --epsrel.

By default, the free energy is computed summing over the Matsubara frequencies ξ_n , also called Matsubara spectrum decomposition (MSD). Another option is to compute the free energy using Padé spectrum decomposition (PSD). PSD is an optimal sum-over-poles expansion scheme, more information can be found in Hu, Xu, Yan, "Padé spectrum decompositions of quantum distribution functions and optimal hierarchical equations of motion construction for quantum open systems", J. Chem. Phys. 133, 101106 (2010). The PSD requires less terms to be computed compared to the MSD. You can tell the program to use PSD with the flag --psd. The order is determined automatically to achieve a relative error of the order specified by --epsrel. You can also manually set the order using --psd-order. Since the automatic determination of the order is not well tested, this option is considered experimental.

If you are only interested in the high-temperature limit, the flag --ht will only compute $\log \det(1 - \mathcal{M}(0))$ and output the Casimir energy in the limit $T \to \infty$ in units of $k_B T$.

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3.1.3 Material parameters

Up to this point, we have assumed that the sphere and the plate are perfect reflectors. If you want to model the sphere and the plate using the plasma model, you can set the plasma frequency using --omegap. The plasma frequency is expected in units of eV/\hbar . For example, for $R=50\mu m$, L=800nm, T=300K, and gold (plasma frequency $\omega_P=9eV/\hbar$), the Casimir free energy using the plasma model is:

```
mpirun -n 8 ./casimir -R 50e-6 -L 1e-6 -T 300 --omegap 9
# compiler: gcc
# compile time: Jan 2 2019 12:35:13
# compiled on: Linux jonas.physik.uni-augsburg.de 4.9.0-8-amd64 #1 SMP Debian 4.9.130-
→2 (2018-10-27) x86_64 GNU/Linux
# git HEAD: 51b8df47618d15747e59321aee77e1f86fab32a8
# git branch: master
# pid: 25590
# start time: Thu Jan 3 13:45:32 2019
\# LbyR = 0.02
\# RbyL = 50
\# L = 1e-06
\# R = 5e-05
# T = 300
# using Matsubara spectrum decomposition (MSD)
\# cutoff = 1e-09
\# epsrel = 1e-06
# iepsrel = 1e-08
# 1dim = 351
\# cores = 8
# omegap = 9
# gamma = 0
# model = plasma
\# xi*(L+R)/c=0, logdetD=-12.9879117945873, t=0.386934
# xi*(L+R)/c=41.9814634849106, logdetD=-2.25212799211675, t=8.56138
# xi*(L+R)/c=83.9629269698212, logdetD=-0.399130249157291, t=8.79863
# xi*(L+R)/c=125.944390454732, logdetD=-0.0715772034739604, t=8.86131
# xi*(L+R)/c=167.925853939642, logdetD=-0.0128539503490175, t=8.90524
# xi*(L+R)/c=209.907317424553, logdetD=-0.00230798551800234, t=8.56306
# xi*(L+R)/c=251.888780909464, logdetD=-0.000414281644513791, t=8.18385
# xi*(L+R)/c=293.870244394374, logdetD=-7.43406394982715e-05, t=7.62512
# xi*(L+R)/c=335.851707879285, logdetD=-1.33358593258147e-05, t=6.89742
# xi*(L+R)/c=377.833171364195, logdetD=-2.39148466183249e-06, t=6.48929
# 685 determinants computed
# stop time: Thu Jan 3 13:46:45 2019
# L/R, L, R, T, ldim, E*(L+R)/(hbar*c)
0.02, 1e-06, 5e-05, 300, 351, -123.3743917511159
```

To describe the objects using the Drude model, you can additional specify the relaxation frequency γ (also in units of eV/\hbar). For gold, $\gamma = 35 meV/\hbar$, so the same example as above for Drude gives:

```
mpirun -n 8 ./casimir -R 50e-6 -L 1e-6 -T 300 --omegap 9 --gamma 0.035

# compiler: gcc
# compile time: Jan 2 2019 12:35:13
# compiled on: Linux jonas.physik.uni-augsburg.de 4.9.0-8-amd64 #1 SMP Debian 4.9.130-

→2 (2018-10-27) x86_64 GNU/Linux
```

```
# git HEAD: 51b8df47618d15747e59321aee77e1f86fab32a8
# git branch: master
# pid: 25643
# start time: Thu Jan 3 13:48:50 2019
\# LbyR = 0.02
# RbvL = 50
\# L = 1e-06
\# R = 5e-05
# T = 300
# using Matsubara spectrum decomposition (MSD)
\# cutoff = 1e-09
# epsrel = 1e-06
\# iepsrel = 1e-08
# 1dim = 351
\# cores = 8
# omegap = 9
# gamma = 0.035
# model = drude
\# xi*(L+R)/c=0, logdetD=-7.09741176750412, t=0.000463963
# xi*(L+R)/c=41.9814634849106, logdetD=-2.23320258322643, t=8.40539
# xi*(L+R)/c=83.9629269698212, logdetD=-0.396003476948632, t=8.85682
# xi*(L+R)/c=125.944390454732, logdetD=-0.071024911146045, t=9.09324
# xi*(L+R)/c=167.925853939642, logdetD=-0.0127552647899639, t=8.74376
# xi*(L+R)/c=209.907317424553, logdetD=-0.00229031081195299, t=8.5974
# xi*(L+R)/c=251.888780909464, logdetD=-0.000411115126231591, t=8.13146
# xi*(L+R)/c=293.870244394374, logdetD=-7.3773492717613e-05, t=7.64662
# xi*(L+R)/c=335.851707879285, logdetD=-1.32343284458642e-05, t=7.20287
# xi*(L+R)/c=377.833171364195, logdetD=-2.37331945823411e-06, t=6.58019
# 627 determinants computed
# stop time: Thu Jan 3 13:50:03 2019
\# L/R, L, R, T, ldim, E*(L+R)/(hbar*c)
0.02, 1e-06, 5e-05, 300, 351, -83.71300491448063
```

The Casimir energy in the high-temperature limit for the Drude and the plasma model differ by a factor of 2. This is the reason why in this example the Casimir energy using the plasma model is considerably larger than using the Drude model.

General materials can be described using --material which expects the path to a material file. A material file has the following format:

(continues on next page)

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```
1.488620000000000E+018 1.002550948190463
1.503810000000000E+018 1.002504731170786
1.5190000000000000E+018 1.002459773692494
```

Each line either starts with a pound (#) or contains a frequency ξ in units of rad/s and the corresponding value of the dielectric function $\epsilon(i\xi)$ separated by spaces. The frequencies have to be in ascending order. The dielectric function for an arbitrary frequency is then computed using linear interpolation. For frequencies smaller than the smallest frequency provided in the file, the dielectric function is computed using the Drude model

$$\epsilon(i\xi) = 1 + \frac{\omega_P^2}{\xi(\xi + \gamma)}$$

with the plasma frequency given by omegap_low and the relaxation frequency given by gamma_low. If omegap_low and gamma_low are not given in the file, the dielectric function is assumed to be 1. The behaviour for frequencies larger than the largest provided frequency is analougous.

Here is an example that computes the Casimir energy for a sphere of $R=50\mu\mathrm{m}$ at separation $L=1\mu\mathrm{m}$ at room temperature $T=300\mathrm{K}$ for real gold:

```
💲 mpirun -n 8 ./casimir -R 50e-6 -L 1e-6 -T 300 --material ../materials/gold.csv
# compiler: gcc
# compile time: Jan 7 2019 10:28:24
# compiled on: Linux jonas.physik.uni-augsburg.de 4.9.0-8-amd64 #1 SMP Debian 4.9.130-
→2 (2018-10-27) x86_64 GNU/Linux
# git HEAD: 5c3f8f083f2af60bd680646adc94997b179c350c
# git branch: master
# pid: 4840
# start time: Mon Jan 7 10:28:44 2019
\# LbyR = 0.02
\# RbyL = 50
\# L = 1e-06
\# R = 5e-05
# T = 300
# using Matsubara spectrum decomposition (MSD)
\# cutoff = 1e-09
\# epsrel = 1e-06
\# iepsrel = 1e-08
# 1dim = 351
# cores = 8
# filename = ../materials/gold.csv
# model = optical data (xi=0: Drude)
# plasma = -12.9879117939843 (logdetD(xi=0) for plasma model with omegap=9eV)
# xi*(L+R)/c=0, logdetD=-7.09741176750412, t=0.352728
# xi*(L+R)/c=41.9814634849106, logdetD=-2.23788117126162, t=8.44477
# xi*(L+R)/c=83.9629269698212, logdetD=-0.397789450092019, t=8.8778
# xi*(L+R)/c=125.944390454732, logdetD=-0.0716100613017328, t=9.09214
# xi*(L+R)/c=167.925853939642, logdetD=-0.0129251607796874, t=9.02829
# xi*(L+R)/c=209.907317424553, logdetD=-0.00233585322790776, t=8.67091
# xi*(L+R)/c=251.888780909464, logdetD=-0.000422670611527527, t=8.18489
# xi*(L+R)/c=293.870244394374, logdetD=-7.65823629633713e-05, t=7.80386
# xi*(L+R)/c=335.851707879285, logdetD=-1.38953641418705e-05, t=7.10853
\# xi*(L+R)/c=377.833171364195, logdetD=-2.52460509493263e-06, t=6.50239
# 682 determinants computed
# stop time: Mon Jan 7 10:29:58 2019
```

```
#
# L/R, L, R, T, ldim, E*(L+R)/(hbar*c)
0.02, 1e-06, 5e-05, 300, 351, -83.81029275263388
```

The energy printed in the last line assumes a Drude model for the zero-th Matsubara frequency. If you want to use the plasma model for the zero-th Matsubara frequency, you can use the value given by # plasma =. This number, i.e., -12.9879... is given in units of $k_{\rm B}T/2$ and corresponds to the additional contribution in the high-temperature limit to the energy in the plasma model. In this example, the free energy using the Drude model for zero-frequency is

$$\mathcal{F}_{\mathrm{Drude}} \approx -83.8 \frac{\hbar c}{L+R} \approx -5.19 \times 10^{-20} \mathrm{J},$$

and assuming the plasma model for zero frequency

$$\mathcal{F}_{\text{plasma}} \approx \mathcal{F}_{\text{Drude}} + \frac{-12.98k_{\text{B}}T}{2} \approx -7.88 \times 10^{-20} \text{J}.$$

3.1.4 Truncation of the vector space

The truncation of the vector space is described in more detail in Hartmann, "Casimir effect in the plane-sphere geometry: Beyond the proximity force approximation", phd thesis (2018). You can either specify the dimension of the vector space using --ldim, or you choose the vector space using the parameter --eta:

$$\ell_{\rm dim} = \max(20, \lceil \eta R/L \rceil)$$
.

The estimated error due to the truncation of the vector space depending on eta is given by:

numerical error	10^{-2}	10^{-3}	10^{-4}	10^{-5}	10^{-6}	10^{-7}	10^{-8}
eta	2.8	4	5.2	6.4	7.6	8.8	10

3.1.5 Other options

The computation of the matrix elements of the round-trip operator contain an integration. The desired relative error for this integration can be set using --iepsrel. The default value of 10^{-8} should be sufficient for almost all purposes. If you want to compute the Casimir energy to very high accuracy, to 10^{-7} or better, you might want to set a smaller value.

3.2 casimir_logdetD

The program casimir_logdetD computes

$$\log \det (1 - \mathcal{M}^m(\xi))$$
.

depending on m, ξ, R , and L The options -L, -R, --ldim, --material, and --iepsrel are the same as for the program casimir.

Besides -L and -R, further mandatory options are -m and --xi. The frequency given by --xi is expected in units of (L+R)/c. In addition, you can specify the algorithm used to compute the determinant with --detalg. Valid options are HODLR, QR, LU, and Cholesky.

A typical output looks like

```
$ ./casimir_logdetD -R 100e-6 -L 1e-6 -m 1 --xi 1.5

# ./casimir_logdetD, -R, 100e-6, -L, 1e-6, -m, 1, --xi, 1.5

# L/R = 0.009999999999999999

# L = 1e-06

# R = 0.0001

# ldim = 501

# epsrel = 1.0e-08

# detalg = HODLR

#

L, R, \( \xi \) (L+R)/c, m, logdet(Id-M), ldim, time

1e-06, 0.0001, 1.5, 1, -6.417998208796558, 501, 0.492086
```

Sometimes, it is useful to output the round-trip matrix in numpy format. If the environment variable CASIMIR_DUMP is set and detalg is not HODLR, the round-trip matrix will be saved to the filename contained in CASIMIR_DUMP. Also note that if detalg is Cholesky, only the upper half of the matrix is computed. Here is an example:

```
$ CASIMIR_DUMP=M.npy ./casimir_logdetD -R 100e-6 -L 1e-6 -m 1 --xi 1.5 --detalq LU
# ./casimir_logdetD, -R, 100e-6, -L, 1e-6, -m, 1, --xi, 1.5, --detalg, LU
        = 0.0099999999999998
# L/R
# L
        = 1e-06
       = 0.0001
# R
# ldim
         = 501
# epsrel = 1.0e-08
# detalg = LU
# L, R, \xi * (L+R)/c, m, logdet(Id-M), ldim, time
1e-06, 0.0001, 1.5, 1, -6.417998208796549, 501, 0.833277
$ ls -lah M.npy
-rw----- 1 hartmmic g-103665 7,7M Jan 4 15:16 M.npy
$ python
Python 3.6.5 | packaged by conda-forge | (default, Apr 6 2018, 13:39:56)
[GCC 4.8.2 20140120 (Red Hat 4.8.2-15)] on linux
Type "help", "copyright", "credits" or "license" for more information.
>>> import numpy as np
>>> M = np.load("M.npy")
                            # load matrix
>>> dim,_ = M.shape  # get dimension
>>> Id = np.eye(dim)  # identity matrix
>>> np.linalg.slogdet(Id-M) # compute determinant
(1.0, -6.417998208796572)
```

3.3 cylinder

The program cylinder computes the Casimir interaction in the cylinder-plane geometry. The radius of the cylinder is given by $\neg R$ and the separation between cylinder and plate is given by $\neg R$. Both lengths are expected in meters. At the moment, only perfect reflectors at zero temperature is supported.

This example computes the Casimir free energy for a cylinder of radius $R = 100 \mu m$ and a separation of d = 100 nm:

```
$ ./cylinder -R 100e-6 -d 100e-9
# R/d = 1000
# d = 1e-07
# R = 0.0001
# T = 0
```

Here, L denotes the length of the cylinder. E_D and E_N correspond Dirichlet and Neumann boundary conditions, E_EM is the energy for the electromagnetic field, $E_EM = E_D + E_N$.

3.3. cylinder

CHAPTER

FOUR

API DOCUMENTATION

The documentation of the API is available at manual/api.pdf or can be generated running

\$ doxygen doxygen.conf

in the directory src/. The documentation will be generated in src/doc/. You need doxygen installed on your computer.