

# Introduction to Choice Models

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# Outlook

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- Choice Models
  - Utility theory
  - Logit versus multinomial logit
  - Model fit
  - Interpretation of coefficients
- Business Applications

# Choice Models

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## 1. Observe choice:

- Buy/not buy                      – direct marketers
- Brand bought                    – packaged goods

## 2. Capture related characteristics data:

- Demographics
- Attitudes/perceptions
- Market conditions (price, promotion, etc.)

## 3. Link

- 1 to 2 via “choice model” – the model *predicts* customers’ probabilities of purchase and also *reveals* importance of characteristics.

# Choice Models

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## **Binary Choice**

- Buy or Not Buy
- Yes or No
- Own or Don't own

## **Multinomial Choice**

- Wisk, All, Tide, and Yes
- Bus, Train, or Plane
- Yes, No, Don't Know

Choices are mutually exclusive. The customer chooses only one of the options at a given choice occasion.

# Underlying Assumptions

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- Consumers are rational utility maximizers
  - Well-ordered preferences for any set of choice alternatives
- Alternative with maximum utility is chosen
- Utility assigned to alternatives is unobserved
- Observables are available about
  - the chosen alternatives (Tide, Wisk, etc.)
  - customer characteristics (age, income, etc.)
  - products (price, feature, display, etc.)
- Translating utilities to choice probabilities

# Utility Theory and Model Formulation

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# Consumer Behavior Assumptions

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- In a multinomial logit, the choices reflect tradeoffs the consumer must face
  - Tide is of high quality but of higher price
  - Cheer is not so good, but the price is lower
- These tradeoffs are captured in the consumer's utility function for each choice alternative

# How the Model Maps Utilities to Choices?

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- $j$  indexes the choices ( $J$  of them)
  - No need to assume equal choices
- $i$  indexes people ( $N$  of them)
- $Y_{ij} = 1$  if person  $i$  selects option  $j$ ,  $= 0$  otherwise
- $U_{ij}$  is the utility or net benefit of person  $i$  if they select option  $j$



# How the Model Maps Utilities to Choices?

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- $j$  indexes the choices among “Tide,” “Wisk,” “YES,” “Cheer” ( $J = 4$ )
  - No need to assume equal choices
- $i$  indexes people ( $N$  of them)
- $Y_{ij} = 1$  if person  $i$  selects option  $j$ ,  $= 0$  otherwise
- $U_{ij}$  is the utility or net benefit of person  $i$  if they select option  $j$
- Suppose customer chooses Tide ( $j = 1$ )

# How the Model Maps Utilities to Choices?

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- Then there are a set of 3 (J - 1) inequalities that must be true
- $U_{itide} > U_{iwisk}$
- $U_{itide} > U_{iYES}$
- $U_{itide} > U_{icheer}$
- Choice of Tide dominates the other
- A multinomial logit model will ensure the coefficients reflect these behavioral assumptions about consumers

# Compute Choice Scores

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Relay C (Binary Logit)

Probability of retaining customer i =

$$P_i = \frac{e^{(U_i)}}{1 + e^{(U_i)}}$$

(Multinomial Logit)

Probability of customer i choosing j =

$$P_{ij} = \frac{e^{(U_{ij})}}{\sum_{k=1}^K e^{(U_{ik})}}$$

Probability of customer i choosing  
alternative “Cheer” among choices  
“Tide,” “Wisk,” “YES,” “Cheer”

$$= P_{icheer} = \frac{e^{(U_{icheer})}}{e^{(U_{itide})} + e^{(U_{iwisk})} + e^{(U_{iYES})} + e^{(U_{iCheer})}}$$

# Map to Market Share

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$$p_{ij} = \frac{e^{u_{ij}}}{\sum_k e^{u_{ik}}}$$

$$m_j = \frac{\sum_{i=1}^n p_{ij}}{n}$$

$u_{ij}$  = Total utility of product bundle  $j$  for consumer  $i$

$p_{ij}$  = Proportion of purchases that consumer  $i$  makes of product  $j$  or

$p_{ij}$  = probability that consumer  $i$  will choose product  $j$

Market share for product  $j$  ( $m_j$ ) = average  $p_{ij}$  across consumers

# Business Applications

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## Conjoint Analysis, Part 1

# Why Conjoint Analysis?

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Asking direct questions about preferences often leads to unenlightening answers.

- What load would you like to pay on your mutual fund?
- What annual fee would you like?
- Would you like online access to your funds?

**Consumers want everything and they want it for free!**

# How Has the Method Been Applied?

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New Card Benefits

Room Configuration



THE RITZ-CARLTON®



Baltimore Ravens Logo



New Hotel Concept for  
Business Travelers

New Services



First AT&T cell phones

# Why Do Firms Use It?

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Firms want to increase profits by providing the product features that consumers value.



*What  
happened  
to “free”  
airline  
meals?*



# Why Do Firms Use It?

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Firms want to increase profits by providing the product features that consumers value.

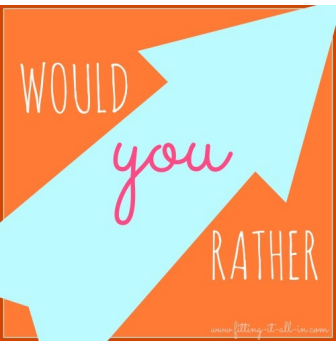
**Fly to SFO for  
\$499  
(includes meal)**



**Fly to SFO for  
\$489  
(without meal)**



*What  
happened  
to “free”  
airline  
meals?*



# Alternatively, Directly Asking Can Be Misleading . . .

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When people are directly asked, . . .

**“Durability  
+ Quality  
+ Reliability”**

. . . but from the conjoint consumers really care about  
**Price + Design**

# It Works with Services Too...

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*All that is needed is a decomposition of the attributes*



Mutual Fund = Past Returns + Fees + Brand Name + Online Access

# What about B2B?

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*If you were Boeing, what are your customers willing to pay for your new aircraft?*

Value of Aircraft =

- + Capacity
- + Max Range
- + Fuel Efficiency
- + Price
- + Service Contract + . . .



# What about Clothing?

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# Business Applications

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## Conjoint Analysis, Part 2

# Aid for Pricing Decisions

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- Sellers want to increase profits by providing cost-effective products that consumers value.
- First step in this process is to determine the trade-offs consumers are willing to make among various attributes.

# Choice-Based Conjoint Analysis



Below are several offers for a Kitchen Mixer from different retailers. Each Kitchen Mixer is for the same original price of \$350, but for a different deal or shipping fee. Please indicate which product you would most likely purchase.

Eligible for  
**amazon.com**  
Prime

	Price	Shipping	Notes	
	\$280.00 <del>\$350</del> (Save 20%)	\$39.99 3 Days	30 days return policy Item may be placed on back-order 1-3 days	<input type="radio"/>
	\$315.00 <del>\$350</del> (Save 10%)	Free 2 Days	No return policy Item may be placed on back-order 1-3 days	<input type="radio"/>
	\$350.00	\$19.99 1 Day	No return policy Item is in stock and ships immediately	<input type="radio"/>
None of these choices				<input type="radio"/>

Next



# Choice-Based Example: Parent-Teen Decision-Making

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Assess how a parent-teen dyad evaluates the following levels of each personal computer attribute:

Attributes	Levels
Computer brand	IBM emachines
Microprocessor brand	Intel Pentium III AMD K6-2
Microprocessor speed	600 MHz 433 MHz
Warranty	2-year warranty No warranty
Price	\$1,299 \$1,799

# Choice Tasks

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Below, we describe three personal computer (PC) alternatives with different features. Please check (in the space provided) the PC you prefer the most.

Please check one PC even if you do not like any of the three alternatives. We are only interested in your most preferred choice from the available alternatives. While evaluating these alternatives, please focus only on the features included in the study because alternatives are identical in every other respect.

Please do not skip any questions.

# Choice Tasks

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**Question 1:** Please check (in the space provided) the PC you prefer the most.

Alternative 1: IBM PC Intel Pentium III 433 MHz 2-yr warranty service \$1,799		Alternative 2: eMachines PC Intel Pentium III 600 MHz 2-yr warranty service \$1,299		Alternative 3: IBM PC AMD K6-2 433 MHz No warranty service \$1,799
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**Question 2:** Please check (in the space provided) the PC you prefer the most.

Alternative 1: eMachines PC AMD K6-2 433 MHz 2-yr warranty service \$1,799		Alternative 2: IBM PC AMD K6-2 600 MHz 2-yr warranty service \$1,299		Alternative 3: IBM PC Intel Pentium III 600 MHz No warranty service \$1,299
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# Discrete Choice Model

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$$\Pr( "1" \text{ gets chosen} ) = \frac{\exp(V_1)}{\sum_{k=1}^3 \exp(V_k)}$$

$$V_1 = \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \beta_4 X_4 + \beta_5 X_5$$

where

$X_1 = 1$  if computer brand is IBM and 0 otherwise

$X_2 = 1$  if microprocessor brand is Intel and 0 otherwise

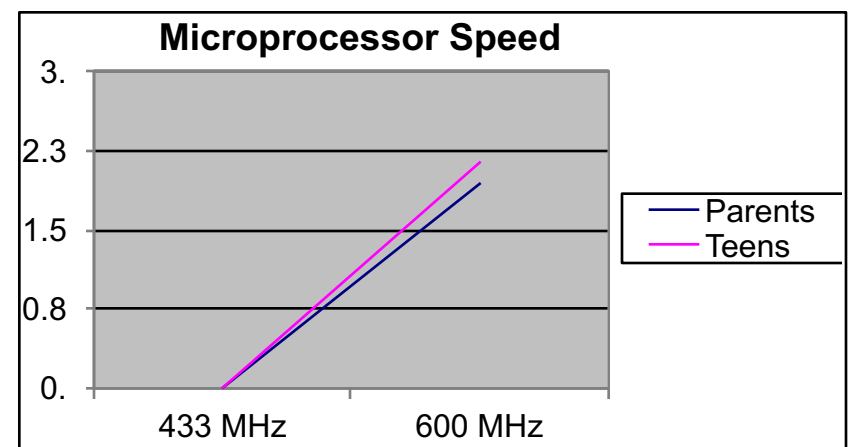
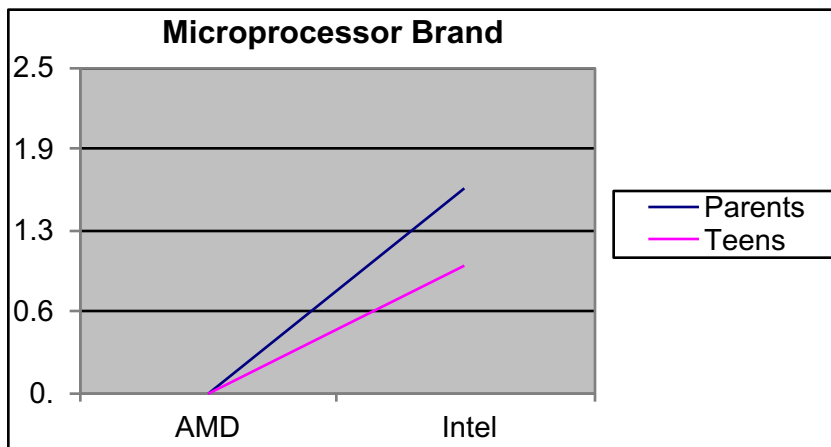
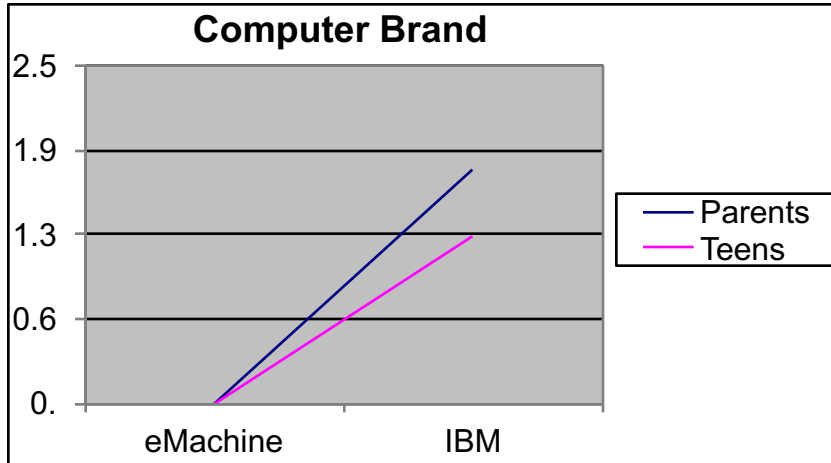
$X_3 = 1$  if microprocessor speed is 600 MHz

$X_4 = 1$  if warranty is two years and 0 otherwise

$X_5 = 1$  if price is \$1,799 and 0 otherwise

The baseline PC is eMachine; AMD; 433 MHz; no warranty; \$1,799

# Utilities for Different PC Attributes



# Business Applications

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## Conjoint Analysis, Part 3

# Embedded Premium Promotion: Why It Works and How to Make It More Effective

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In this paper we define an embedded premium (EP) as an enhancement that involves a social cause added on to a product or service. We characterize EP as a sales promotion strategy and juxtapose it with traditional approaches, such as discounts and rebates. Across three experiments, using a nationwide Internet panel and employing stated measures and model-based inference, we find that at low denominations EP is more effective than an equivalent price discount. We describe how an EP's social association may influence consumer choice quite differently than price promotions and, contrary to the asymmetric price promotion effect documented in the promotions literature, we find that EP benefits an unknown brand more than a known brand. Our hierarchical Bayes approach uncovers heterogeneity in EP effectiveness that can be explained by affinity toward the focal charity, personal motivations, and demographic markers. An identifiable segment of individuals prefer the "other" over "self," suggesting possible EP optimization and segmentation strategies. Two such strategies, customization and coverage, are empirically tested, and the former is shown to be very effective. Our findings have broad implications for brand managers with regard to resource allocation and EP program return on investment (ROI), as well as important social welfare implications.

*Key words:* embedded premium; sales promotion; consumer choice; hierarchical Bayes; ROI; cause-related marketing

*History:* This paper was received January 17, 2006, and was with the authors 1 month for 1 revision; processed by Peter Lenk.

# Choice-Based Conjoint Example

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Attribute	Levels
Brand	National Bank, Capital One
Interest rate	9.9% APR, 12.9% APR
Payback percentage	1%, 5%
Payback destination	WHO, WHO & Habitat, charity of choice, cash back



# Choice-Based Conjoint

## Arora and Henderson 2007

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- Respondents indicate their charity preference by selecting one cause from five:
  - American Cancer Society, World Health Organization, Habitat for Humanity, SchoolWise, National Wildlife Federation
- Choice-based conjoint, 16 tasks
- Respondent characteristics
  - Usage, cause affinity, demographics

# Example Choice Task

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\*If evaluating a credit card offer with a charitable donation option that lets you decide who receives your money, which one of these five organizations would you choose to support? (click one)

- ☐ American Cancer Society
- ☐ World Health Organization
- ☐ Habitat for Humanity
- ☐ SchoolWise (for local schools)
- ☐ National Wildlife Federation

<ul style="list-style-type: none"><li>➤ Capital One Visa</li><li>➤ 9.9% Fixed APR</li><li>➤ 1 % of your monthly charges donated to the World Health Organization and Habitat for Humanity</li></ul>	<ul style="list-style-type: none"><li>➤ Capital One Visa</li><li>➤ 12.9% Fixed APR</li><li>➤ 1 % of your monthly charges donated to the charity you selected</li></ul>	<ul style="list-style-type: none"><li>➤ National Bank Visa</li><li>➤ 9.9% Fixed APR</li><li>➤ 5% of your monthly charges credited back to you</li></ul>
A	B	C

# Data Collection

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## National Internet Survey (n = 495)

- 60% female
- 62% married
- 57% over age 44
- 41% w/ at least bachelor's degree
- 24% w/ household income > \$75K

# Choice Design Matrix Coding

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Nine dummy variables

- Brand [x1] (Capital One = 1)
- Interest rate [x2] (9.9% = 1)
- Level \* Payee interaction [x3..x9]

# Model Specification

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$$U_{ij} = \beta_{1,ij}X_1 + \beta_{2,ij}X_2 + \beta_{3,ij}X_3 +$$

Capital One      9.9% APR      1% Cash

$$\beta_{4,ij}X_4 + \beta_{5,ij}X_5 + \beta_{6,ij}X_6 +$$

5% Cash      5% WHO      1% Both

$$\beta_{7,ij}X_7 + \beta_{8,ij}X_8 + \beta_{9,ij}X_9$$

5% Both      1% Choose      5% Choose

# Business Applications

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Cross-Selling



Predicting customer behavior is so difficult that companies spend millions inundating – and alienating – customers. Here's a way to crunch the data that makes it possible to offer customers what they want, when they want it.

# Knowing What to Sell, When, and to Whom

by V. Kumar, Rajkumar Venkatesan, and Werner Reinartz

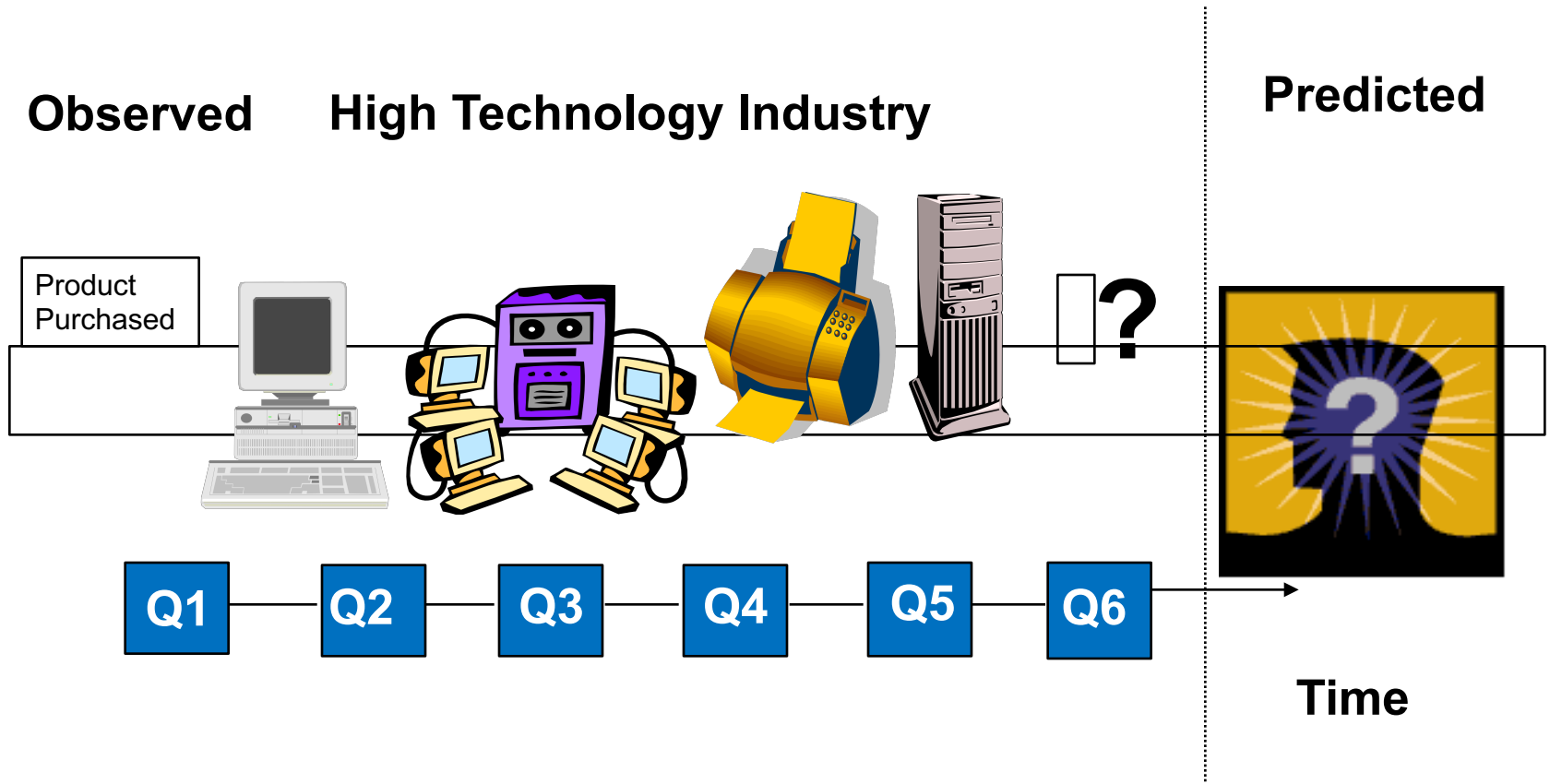
# Propensity Modeling for Cross-Selling

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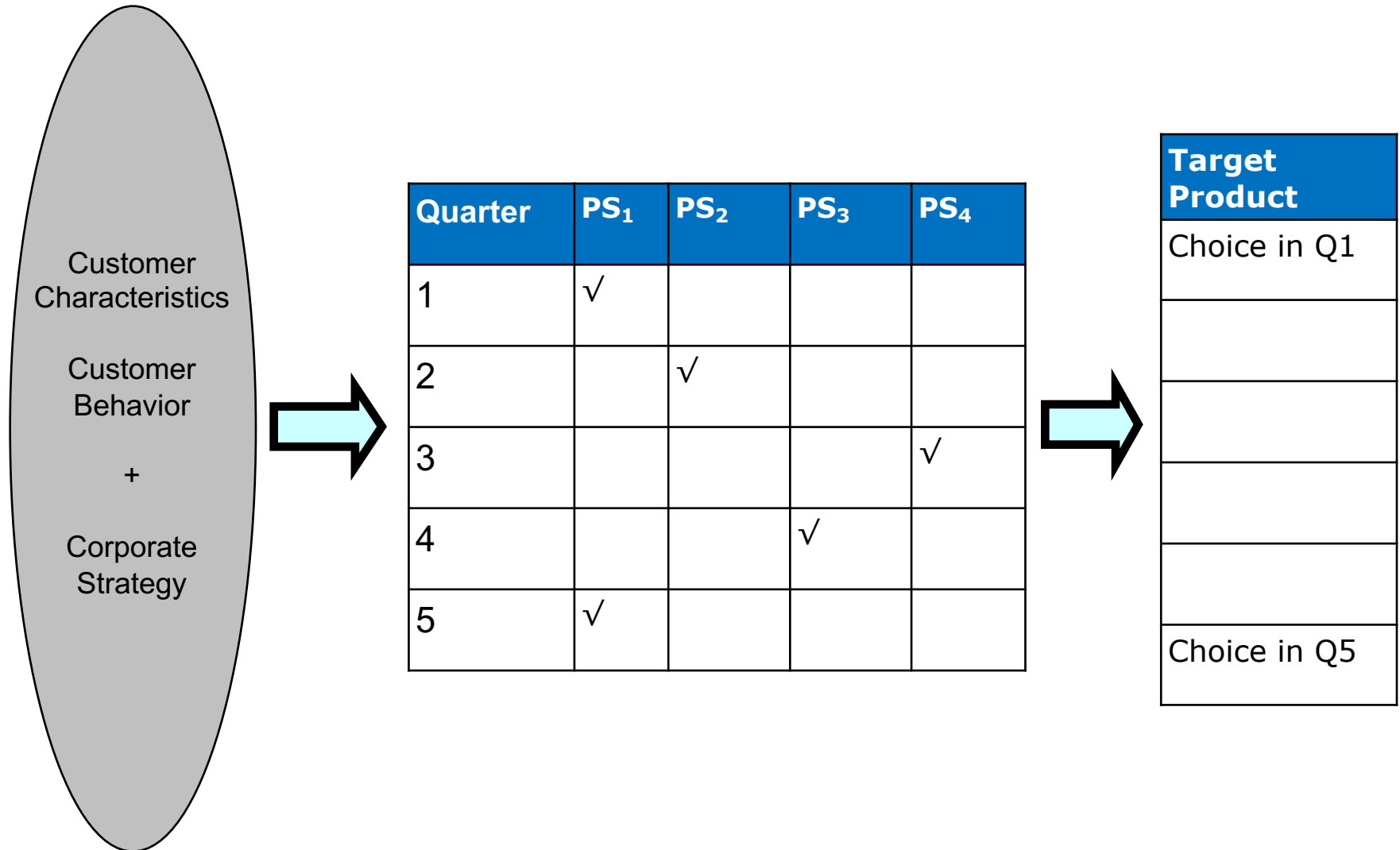
- Important to understand when a customer is “ready” for their next purchase.
- Some of this depends on the reality of budget cycles.
- Some of this depends on the complexity of the client’s business.
- But some also depends on some predictable patterns in company behavior that can be modeled.



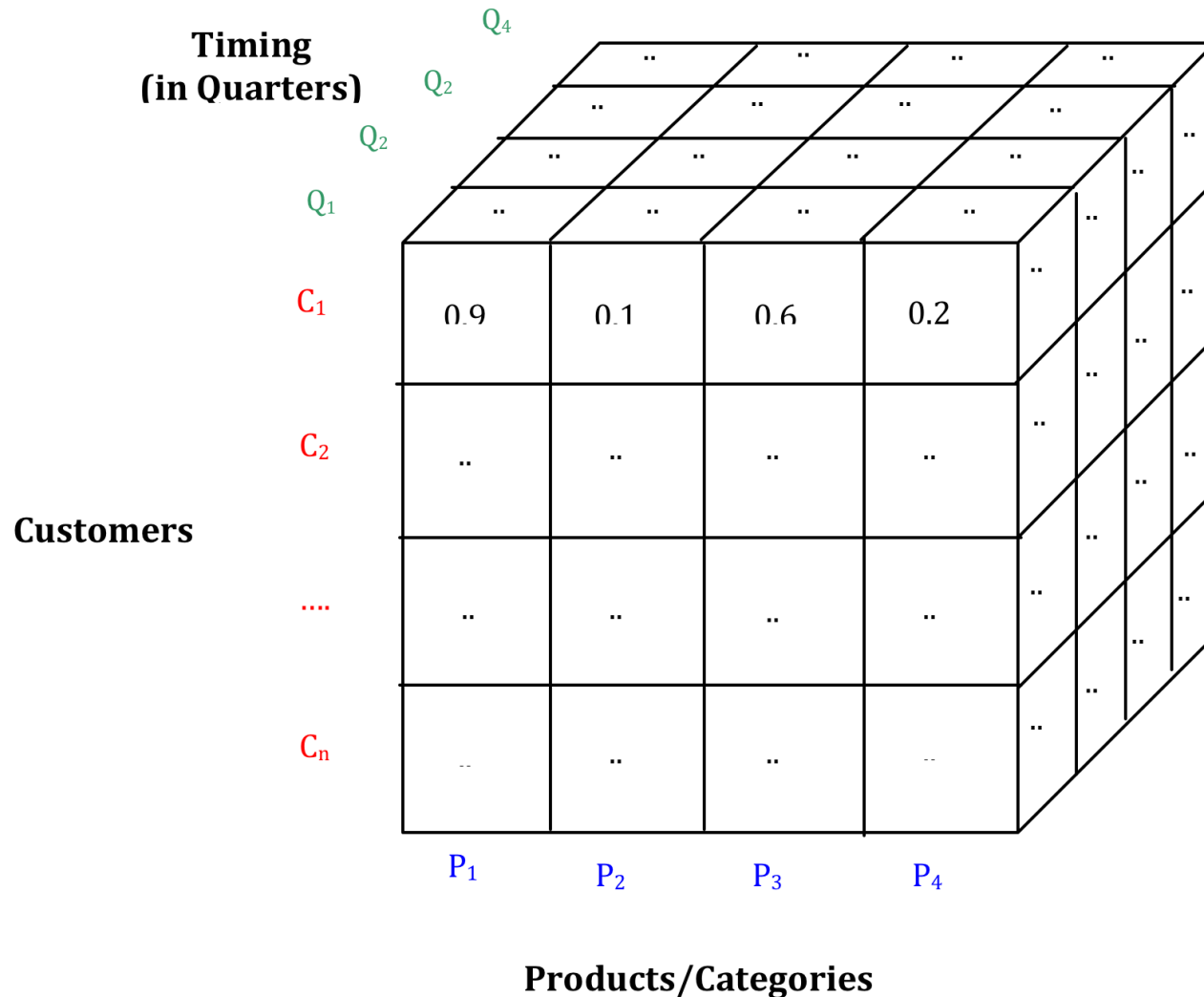
# Research Issue: Purchase Sequence



# Multiple Product Adoption



# Customer Profitability Cube



# Customer Development—Marketing Sales Interface

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## *Year over Year Changes from Implementing a Customer-Focused Sales Force*

	Lift in Test Group	Test Group: Customer-Focused Sales Campaign	Control Group: Product-Focused Sales Campaign
<b>Financial Metrics</b>			
Revenue (\$)	204%	1,828*** (15,710) <sup>b</sup>	898* (15,263)
Number of Contacts before Purchase	-4%	-4** (11)	1 (11)
Profits (\$)	4%	3,734*** (9,519)	890* (8,694)
Return on Investment	1538%	2*** (1.5)	0.13 (1.3)

<sup>b</sup> Values in the parentheses represent the levels in the pre-experiment time period.

<sup>c</sup> The Relational Metrics are measured in a 10-point interval scale, where 10 represents Completely Agree and 1 represents Completely Disagree.

\* Significant at  $\alpha = 0.10$ , \*\* Significant at  $\alpha = 0.05$ , \*\*\* Significant at  $\alpha = .01$

# Conclusion

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# Conclusion

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- Multinomial logit regressions are used when consumers choose one out of many options. Typical examples include brand choice in grocery stores.
- Similar to the propensity models, multinomial logit regressions also follow the utility theory of consumer behavior.
- Conjoint analysis is a major application of multinomial choice.
  - A conjoint analysis allows the researcher to evaluate trade-offs consumers make among different features of a product, including price and brand name.
- Cross-selling or predicting the next product to buy is another application of multinomial logit regressions.