

Formal Languages

Ch 4 (p 140-142): 19,27,30,33

19.

$$G: S \rightarrow A'F_1 \mid AF_2 \mid a$$

$$F_1 \rightarrow AF_3$$

$$F_2 \rightarrow BC$$

$$F_3 \rightarrow B'B$$

$$A' \rightarrow a$$

$$B' \rightarrow b$$

$$A \rightarrow A'A$$

$$B \rightarrow B'F_4 \mid b$$

$$F_4 \rightarrow BF_5$$

$$F_5 \rightarrow C'C$$

$$C' \rightarrow c$$

$$C \rightarrow A'F_6$$

$$F_6 \rightarrow B'C'$$

27.

(a)

$$B: (b^*abab^*) \mid (aab^*abab^*(ab \mid ba)^*)$$

(b)

$$S \rightarrow A \mid B$$

$$A \rightarrow aaB \mid aaBZ$$

$$Z \rightarrow abZ \mid baZ \mid ab \mid ba$$

$$B \rightarrow bB \mid aba \mid abaX$$

$$X \rightarrow bX$$

30.

$$S \rightarrow a \mid aAB'$$

$$A \rightarrow b \mid aA' \mid aA'AB' \mid aAB' A'AB' \mid aAB'A'$$

$$B' \rightarrow b$$

$$A' \rightarrow a$$

33.

Original grammar:

$$S \rightarrow BA \mid AB \mid \cdot \backslash$$

$$A \rightarrow BB \mid AA \mid a$$

$$B \rightarrow AA \mid b$$

Removal of left-recursive rules:

$$S \rightarrow BA \mid AB \mid \cdot \backslash$$

$$A \rightarrow BB \mid a \mid BBZ \mid aZ$$

$$B \rightarrow AA \mid b$$

$Z \rightarrow AAZ \mid AA$

Replacement of first variables in incorrect order:

$S \rightarrow BA \mid AB \mid \cdot \backslash$
 $A \rightarrow BB \mid a \mid BBZ \mid aZ$
 $B \rightarrow BBA \mid aA \mid BBZA \mid aZA$
 $Z \rightarrow AAZ \mid AA$

Removal of left-recursive rules:

$S \rightarrow BA \mid AB \mid \cdot \backslash$
 $A \rightarrow BB \mid a \mid BBZ \mid aZ$
 $B \rightarrow aA \mid aZA \mid aAZ' \mid aZAZ'$
 $Z \rightarrow AAZ \mid AA$
 $Z' \rightarrow BBAZ' \mid BBZAZ' \mid BBA \mid BBZA$

Replacement of $A \rightarrow Bw$ productions

$S \rightarrow BA \mid AB \mid \cdot \backslash$
 $A \rightarrow aAB \mid aZAB \mid aAZ'B \mid aZAZ'B \mid a \mid aABZ \mid aZABZ \mid aAZ'BZ \mid aZAZ'BZ \mid aZ$
 $B \rightarrow aA \mid aZA \mid aAZ' \mid aZAZ'$
 $Z \rightarrow AAZ \mid AA$
 $Z' \rightarrow BBAZ' \mid BBZAZ' \mid BBA \mid BBZA$

Replacement of $S \rightarrow Bw$ productions:

$S \rightarrow aAA \mid aZAA \mid aAZ'A \mid aZAZ'A \mid AB \mid \cdot \backslash$
 $A \rightarrow aAB \mid aZAB \mid aAZ'B \mid aZAZ'B \mid a \mid aABZ \mid aZABZ \mid aAZ'BZ \mid aZAZ'BZ \mid aZ$
 $B \rightarrow aA \mid aZA \mid aAZ' \mid aZAZ'$
 $Z \rightarrow AAZ \mid AA$
 $Z' \rightarrow BBAZ' \mid BBZAZ' \mid BBA \mid BBZA$

Replacement of $S \rightarrow Aw$ rules:

$S \rightarrow aAA \mid aZAA \mid aAZ'A \mid aZAZ'A \mid aABB \mid aZABB \mid aAZ'BB \mid aZAZ'BB \mid aB \mid aABZB \mid aZABZB \mid aAZ'BZB \mid aZAZ'BZB \mid aZB \mid \cdot \backslash$
 $A \rightarrow aAB \mid aZAB \mid aAZ'B \mid aZAZ'B \mid a \mid aABZ \mid aZABZ \mid aAZ'BZ \mid aZAZ'BZ \mid aZ$
 $B \rightarrow aA \mid aZA \mid aAZ' \mid aZAZ'$
 $Z \rightarrow AAZ \mid AA$
 $Z' \rightarrow BBAZ' \mid BBZAZ' \mid BBA \mid BBZA$

Replacement of $Z \rightarrow Aw$ rules:

$S \rightarrow aAA \mid aZAA \mid aAZ'A \mid aZAZ'A \mid aABB \mid aZABB \mid aAZ'BB \mid aZAZ'BB \mid aB \mid aABZB \mid aZABZB \mid aAZ'BZB \mid aZAZ'BZB \mid aZB \mid \cdot \backslash$

$A \rightarrow aAB \mid aZAB \mid aAZ'B \mid aZAZ'B \mid a \mid aABZ \mid aZABZ \mid aAZ'BZ \mid aZAZ'BZ \mid aZ$
 $B \rightarrow aA \mid aZA \mid aAZ' \mid aZAZ'$
 $Z \rightarrow aABAZ \mid aZABAZ \mid aAZ'BAZ \mid aZAZ'BAZ \mid aAZ \mid aABZAZ \mid aZABZAZ \mid aAZ'BZAZ \mid$
 $aZAZ'BZAZ \mid aZAZ \mid aABA \mid aZABA \mid aAZ'BA \mid aZAZ'BA \mid aA \mid aABZA \mid aZABZA \mid aAZ'BZA \mid$
 $aZAZ'BZA \mid aZA$
 $Z' \rightarrow BBAZ' \mid BBZAZ' \mid BBA \mid BBZA$

Replacement of $Z' \rightarrow Bw$ rules (final form):

$S \rightarrow aAA \mid aZAA \mid aAZ'A \mid aZAZ'A \mid aABB \mid aZABB \mid aAZ'BB \mid aZAZ'BB \mid aB \mid aABZB \mid$
 $aZABZB \mid aAZ'BZB \mid aZAZ'BZB \mid aZB \mid \cdot$
 $A \rightarrow aAB \mid aZAB \mid aAZ'B \mid aZAZ'B \mid a \mid aABZ \mid aZABZ \mid aAZ'BZ \mid aZAZ'BZ \mid aZ$
 $B \rightarrow aA \mid aZA \mid aAZ' \mid aZAZ'$
 $Z \rightarrow aABAZ \mid aZABAZ \mid aAZ'BAZ \mid aZAZ'BAZ \mid aAZ \mid aABZAZ \mid aZABZAZ \mid aAZ'BZAZ \mid$
 $aZAZ'BZAZ \mid aZAZ \mid aABA \mid aZABA \mid aAZ'BA \mid aZAZ'BA \mid aA \mid aABZA \mid aZABZA \mid aAZ'BZA \mid$
 $aZAZ'BZA \mid aZA$
 $Z' \rightarrow aABAZ' \mid aZABAZ' \mid aAZ'BAZ' \mid aZAZ'BAZ' \mid aABZAZ' \mid aZABZAZ' \mid aAZ'BZAZ' \mid$
 $aZAZ'BZAZ' \mid aABA \mid aZABA \mid aAZ'BA \mid aZAZ'BA \mid aABZA \mid aZABZA \mid aAZ'BZA \mid aZAZ'BZA$