

Chapter 2.11

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TESC

Jan 28, 2009

- 1

$$S_0 = \{P(x, f(y), z), P(g(a), f(w), u), P(v, f(b), c)\}$$

$$D_1 = \{x, g(a), v\}$$

$$\sigma_1 = \{x/g(a), v/g(a)\}$$

$$S_1 = S_0\sigma_1 = \{P(g(a), f(g), z), P(g(a), f(2), u), P(g(a), f(b)c)\}$$

$$D_2 = \{y, w, b\}$$

$$\sigma_2 = \{y/b, w/b\}$$

$$S_2 = S_1\sigma_2 = \{P(g(a), f(b), z), P(g(a), f(b), u), P(g(a), f(b), c)\}$$

$$D_3 = \{z, u, c\}$$

$$\sigma_3 = \{a/c, u/c\}$$

$$S_3 = S_2\sigma_3 = \{P(g(a), f(b), c)\}$$

- 2 $\{P(x, a), P(b, c)\}$ can't be unified since we can't unify the two constants a, c . $\{P(f(x), z), P(a, w)\}$ can't be unified because we can't unify $a, f(x)$.
- 3 Show that composition of substitutions is not commutative. We only need to find one example. Suppose that $\sigma = \{x/y\}$ and $\lambda = \{y/c\}$. Then $f(x, y)\sigma\lambda = (f(x, y)\sigma)\lambda = f(y, y)\lambda = f(c, c)$. But $f(x, y)\lambda\sigma = (f(x, y)\lambda)\sigma = f(x, c)\sigma = f(y, c)$. These are not the same.