Languages and Machines

Chap3: 1(abc), 2(abc), 4(ab), 12, 15, 21, 25

1. (a)

 $S \rightarrow abSc$

 $S \rightarrow ababScc$

 $S \rightarrow ababAcc$

 $S \rightarrow ababcAdcc$

 $S \rightarrow ababccddcc$

(b)

(c) ${ab}^n c^m d^m {c}^n$ $n \ge 0$ $m \ge 0$

2. *(a)*

 $S \rightarrow ASB$

 $S \, \to \, aAbSB$

 $S \rightarrow aaAbbSB$

 $S \rightarrow aabbSB$

 $S \rightarrow aabbB$ $S \rightarrow aabbba$

(b)

 $S \rightarrow ASB$

 $S \rightarrow aAbSB$

 $S \rightarrow abSB$

 $S \to abASBB$

 $S \, \to \, abaAbSBB$

 $S \rightarrow abaaAbbSBB$

 $S \rightarrow abaabbSBB$

 $S \rightarrow abaabbBB$

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```
S → abaabbbaBa
S → abaabbbabBaa
S → abaabbbabbaa
(c)
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Tree for part a:

Tree for part b:

(d) {a**b**}**{b**a**}** where, m, n >= 0 r > 0

4.

(a)

 $S \rightarrow AB$

 $S \ \to \ aAB$

 $S \ \to \ aaB$

 $S \rightarrow aaAB$

 $S \, \to \, aaaB$

 $S \rightarrow aaab$

(b)

 $S \rightarrow AB$

 $S \rightarrow AAB$

 $S \, \to \, AAb$

 $S \to Aab$

 $S \ \to \ aAab$

 $S \rightarrow aaab$

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12. $S \rightarrow aSb \mid . \setminus$

15.

 $S \,\to\, ABC$

 $A \to aA \ | \ . \setminus$

 $B \rightarrow bB \mid . \setminus$

 $C \rightarrow cC \mid . \setminus$

21.

 $S \to bS \mid A$

 $A \rightarrow aA \mid B$

 $B \rightarrow bbS \mid . \setminus$

25.

 $A \,\rightarrow\, aB \mid bD \mid . \backslash$

 $B \rightarrow aA \mid bC$

 $C \rightarrow aD \mid bB \mid . \setminus$

 $D \rightarrow bA \mid aC \mid . \setminus$