

# Sources of capital growth

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## ABSTRACT

Data from national accounts show no effect of change in net saving or consumption, in ratio to market-value capital, on change in growth rate of market-value capital (capital acceleration). Thus it appears that capital growth and acceleration arrive without help from net saving or consumption restraint. We explore ways in which this is possible, and discuss implications for economic teaching and public policy.

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## 1. Introduction and overview

Many economists over the centuries have reasoned that net saving, or equivalently net investment<sup>1</sup>, should tend to give equal capital growth. Economists since the early nineteenth century have added the proviso that net saving cannot safely outpace innovation; more capital must mean capital redesigned for greater productivity if economies are to escape risk of capital glut and diminishing returns (West (1815), Ricardo (1815), Malthus (1815)). Roy Harrod (1939) described that limit for safe net saving, meaning the rate of imagining and developing new ideas for more productive forms of capital, as the “warranted rate”. Harrod, and many other economists of his time and since, have focused on growth of output rather than of capital, but have modeled growth of output by first assuming the equivalence of net saving and capital growth, within the warranted rate, and then looking for effects of that capital growth on later output growth.

Some other economists, including John Rae (1834) and John Stuart Mill (1848) (see Appendix C), argued that capital growth might also be explained by a rise in productivity of capital and labor already extant. Ways might found for existing factors to produce more, that is, and so to allow more consumption, or more capital growth, or any mix of the two, without inputs of net saving. Robert Solow (1957) allowed that possibility for “disembodied” growth, where plant and products already existing are repurposed or redeployed in more productive ways.

We test between those two explanations of capital growth, by net saving or by increase in productivity of capital and labor already in existence, by comparing net saving to concurrent change in market-value capital in 86 countries. As changes in net saving are expected to be associated with opposite changes in consumption, we also compare change in consumption to concurrent change in capital growth (capital acceleration). All data are drawn from national accounts of those countries as collated on the free website [World Inequality Database](#).

Those test results from data for net saving/capital ratio and for consumption/capital ratio are easiest to reconcile in an interpretation that change in neither affects change in capital growth rate.<sup>2</sup> This finding would support the views of Rae and Mill, and of Solow as to disembodied growth. It would suggest that capital growth, even in acceleration, arrives without help from net saving or consumption restraint. Net saving, if so, raises the physical quantity of capital, but not the aggregate value, and so reduces the value per unit.

The data are most easily explained by the present value principle, and by production efficiencies enabled through innovation. Value is created in the mind of the market at the moment when prospective cash flows are discounted. It is created only if the market sees a path, step by step, from the start, to practical realization of those prospective cash flows. Then capital growth arrives when the market first evaluates prospective cash flows, and is realized eventually in physical outcomes insofar as the market has predicted correctly. That is to say that capital growth, in the mind of the market, precedes and pays for any needed investment in new plant and equipment.

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<sup>1</sup>As reported in national accounts; they differ only by statistical discrepancy. Also see Appendix A.

<sup>2</sup>Another interpretation allows that net saving may account for 6.4% of capital growth. See Section 4 below.

Meanwhile the innovator acquires materials and plant capacity and labor skills at market prices determined by their uses in current technology, but applies them more productively until competition catches up. It is that temporary market advantage to the innovator which explains capital growth without net saving in a practical and mechanical sense, while the present value principle gives the explanation in terms of market valuation. This idea will be called “free growth theory” for easy reference.

It predicts only at the largest scales, and only for the private sector. Individuals and groups and even small economies can grow through investment from outside. That possibility is foreclosed only at the scale of all capital and all economies together. The public sector, meanwhile, responds to political rather than market choices, and grows or shrinks accordingly.

If free growth theory is right, tax policy and other policy to encourage saving over consumption should be reviewed. These policies include the higher tax on ordinary income than on capital gains, and the double tax on corporate dividends.

Inferences for economic teaching include the obvious ones for growth theory and for net saving in general. They include others as well. One of the central doctrines of the marginalist revolution has held that market realization converges to producer cost, when that cost includes imputed interest on assets owned. Net saving gives producer cost, and falls short of market realization in the presence of technological growth from new ideas. Meanwhile the doctrine that net income equals consumption plus net saving is put into question by evidence offered here suggesting that net saving increases the physical quantity of capital, but not the aggregate value. In general, economics might consider relying less on book value and net investment, and more on market value and on the power of ideas.

## 2. Net saving, capital growth and capital acceleration

This study compares net saving  $S_{net}$  to concurrent growth in market-value capital  $K$  from data in national accounts. Capital growth  $\Delta K_i$  in each year  $i$  for each reporting country is found as  $K_i - K_{i-1}$ , and compared to  $S_{net,i}$  reported for that year and country. As we will be testing for differences between  $\Delta K$  and  $S_{net,i}$ , we begin by writing

$$\Delta K_i = z_i S_{net,i} + Q_i. \quad (1)$$

Here “net saving efficiency”  $z$  is the fraction of  $S_{net}$  actually realized in growth of capital value  $K$ .  $Q$  means the sum of market noise, which may prove positive or negative or zero, plus any part of capital growth explained by concurrent productivity gain as described by Rae and Mill, and by Solow as to disembodied growth. We call this sum of noise and productivity gain “free growth” in that it costs no net saving.

The object of testing is to find effects of  $S_{net}$  on concurrent  $\Delta K$ , and so to help evaluate historic and current teachings as to those effects. We submitted above that most teaching, with exceptions noted as to Rae, Mill, and Solow, and within the warranted rate, predicts net saving to differ from concurrent growth in market-value capital only by market noise which tends to balance out over scale and time. Free growth  $Q$  in Eq. (1), in that case, will give the market noise converging to zero. That consensus prediction, which we will challenge, will here be called “thrift theory”;  $S_{net}$ , in thrift theory, is expected to converge to  $\Delta K$  if held within the warranted rate. That is,

$$E(z) = 1, \quad E(\Delta K) = S_{net} \quad \text{and} \quad E(Q) = 0, \quad \text{if} \quad \frac{\Sigma S_{net}}{\Sigma K} \leq u, \quad \text{in thrift theory}, \quad (2)$$

where:

1.  $\Sigma S_{net}$  is collective net saving over the economy
2.  $\Sigma K$  is collective capital over the economy before current  $\Sigma S_{net}$ , and
3.  $u$  is the warranted rate.

Free growth theory makes the opposite prediction that net saving adds no capital value, and that capital growth, at the largest scales in the private sector, is explained wholly by increased productivity of skills and materials already present. Thus, referring to Eq. (1), it predicts:

$$E(z) = 0 \quad \text{and} \quad E(\Delta K) = Q \quad \text{in free growth theory.} \quad (3)$$

$E(z)$ ,  $E(\Delta K)$  and  $E(Q)$  here give the expected values of  $z$ ,  $\Delta K$  and  $Q$  respectively. Expected value means predicted average of outcomes over all observations. We will test those predictions against data for saving and capital growth

taken from national accounts. As secular economic growth has tended to make later stocks and flows larger than earlier ones, we first divide by  $K$  (normalize) to avoid overweighting of more recent years in finding that average. Division of Eq. (1) by  $K_{i-1}$  gives

$$\frac{(\Delta K)_i}{K_{i-1}} = \frac{z_i S_{net,i}}{K_{i-1}} + \frac{Q_i}{K_{i-1}} . \quad (4)$$

The first term in Eq. (4) gives capital growth rate  $g(K)$ . The fraction in the second term is a variant of the Keynesian net saving rate  $s_{net}$  where capital rather than output becomes the denominator. This flow will show as  $s^*$ , with the subscript "net" left implicit, and with the understanding that the denominator shows market-value capital rather than output. The third term in Eq. (4) will be called free growth rate and shown as  $q_s$ . That is,

$$g(K)_i = \frac{(\Delta K)_i}{K_{i-1}} , \quad s_i^* = \frac{S_{net,i}}{K_{i-1}} , \quad \text{and} \quad q_i = \frac{Q_i}{K_{i-1}} ,$$

so that Eq. (4) can be shown more compactly as

$$g(K)_i = z_i s_i^* + q_i . \quad (5)$$

By the definition  $q = \frac{Q}{K}$ , an expected value  $E(Q) = 0$  implies  $E(q) = 0$ . Application of Eq. (2) to Eq. (5) now gives

$$E(g(K)) = s^* \quad \text{and} \quad E(q) , \quad \text{under thrift assumptions,} \quad (6)$$

where "thrift assumptions" are that thrift theory is correct and that the warranted rate is not exceeded. Eqs. (2) and (4), meanwhile, give

$$E(g(K)) = q \quad \text{in free growth theory.} \quad (7)$$

Note here that free growth theory makes no prediction as to the quantity  $s_i^*$ . Rather it predicts  $E(z) = 0$  in Eq. (5), so that  $s_i^*$  takes no part in calculation of  $\Delta g(K)_i$ .

The prediction in Eq. (6) can be tested directly from data for market-value capital and net saving in national accounts. We define the "auxiliary thrift index" by

$$\theta^* = \frac{s^*}{g(K)} , \quad \text{that is, and test the prediction}$$

$$E(\theta^*) = 1 \quad \text{under thrift assumptions.}$$

Results show in Fig. 1 and Tables 1 and 2. They show  $\theta^*$  as averaging something near  $\frac{1}{2}$ , and with wide variance from country to country and from year to year. Regression of  $s^*$  on  $g(K)$  is found at 0.2103. Free growth theory, again, makes no prediction as to relationships between net saving and capital growth.

The concepts of correlation, covariance and regression are founded on the principle that causal relationships among variables tend to be revealed in simultaneous changes. Thus the two theories are best tested in their implications for changes in capital growth, which we call capital acceleration and show as  $\Delta g(K)$ . First note that Eq. (5) allows

$$(\Delta g(K))_i = (\Delta(zs^*))_i + (\Delta q)_i , \quad \text{where} \quad (8)$$

$$(\Delta g(K))_i = (g(K))_i - (g(K))_{i-1} , \quad (\Delta(zs^*))_i = z_i s_i^* - z_{i-1} s_{i-1}^* , \quad \text{and} \quad (\Delta q)_i = q_i - q_{i-1} .$$

For any variables  $a$  and  $b$ , we may reason  $E(a - b) = E(a) - E(b)$ . By this and by Eqs. (7) and (8), then,

$$E(g(K)) = \Delta s^* \quad \text{and} \quad E(\Delta q) = 0 , \quad \text{under thrift assumptions.} \quad (9)$$

Division of Eq. (8) by capital acceleration, and rearrangement, gives

$$\frac{(\Delta(zs^*))_i}{(\Delta g(K))_i} + \frac{(\Delta q)_i}{(\Delta g(K))_i} = 1 . \quad (10)$$

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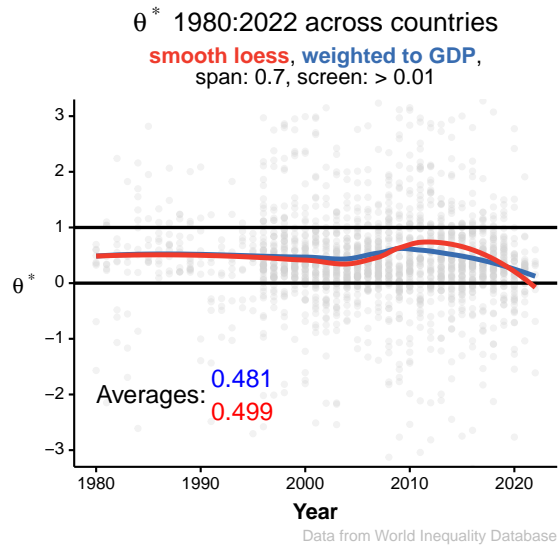


Fig. 1:  $\theta^*$  (86 countries)

**Table 1**

Regression of  $s^*$  on  $g(K)$  (Screen = 0.01).  $H_0$  per thrift theory:  $g(K) \cong s^*$  &  $\overline{\theta^*} \cong 1$ .

	$s^*$
Regression of $s^*$ on $g(K)$	0.1857*** (0.0423)
Observations	1,826
$R^2$	0.77165
Within $R^2$	0.13962
Year fixed effects	✓
Country fixed effects	✓

## Sources of capital growth

**Table 2**Average  $\theta^*$  in 86 countries (screen = 0.01). Number of years clearing screen shown in ( )

Country	Period	$\bar{\theta}^*$	Country	Period	$\bar{\theta}^*$
Armenia	1996 - 2020 (23)	-0.63	Italy	1980 - 2022 (36)	0.13
Aruba	1996 - 2001 (6)	1.25	Japan	1980 - 2021 (29)	0.19
Australia	1980 - 2018 (33)	0.24	Kazakhstan	1997 - 2022 (25)	0.60
Austria	1996 - 2021 (23)	0.83	Kuwait	2003 - 2017 (14)	1.11
Azerbaijan	1996 - 2020 (23)	1.57	Kyrgyzstan	1996 - 2021 (24)	0.46
Bahrain	2009 - 2013 (5)	-2.43	Latvia	1996 - 2021 (24)	-0.23
Belgium	1996 - 2021 (21)	0.61	Lithuania	1996 - 2021 (24)	0.13
Bolivia	1998 - 2015 (17)	0.40	Luxembourg	1996 - 2021 (22)	0.03
Botswana	1996 - 1999 (4)	3.54	Malaysia	2007 - 2015 (9)	2.52
Brazil	1996 - 2019 (21)	0.25	Malta	1996 - 2021 (23)	0.16
British Virgin Islands	1996 - 1999 (4)	2.45	Mauritius	2014 - 2018 (5)	0.04
Bulgaria	1996 - 2016 (16)	0.14	Mexico	1996 - 2021 (22)	0.15
Burkina Faso	2000 - 2019 (20)	0.23	Moldova	1996 - 2019 (22)	-0.91
Cameroon	1996 - 2019 (24)	1.10	Mongolia	2006 - 2020 (15)	0.10
Canada	1980 - 2022 (38)	0.37	Morocco	1999 - 2021 (23)	1.13
Cape Verde	2008 - 2017 (9)	0.53	Netherlands	1996 - 2021 (23)	0.51
Chile	1997 - 2021 (19)	0.84	New Zealand	1996 - 2019 (21)	0.78
China	1992 - 2020 (29)	0.81	Nicaragua	2007 - 2018 (12)	0.08
Colombia	1996 - 2022 (27)	0.60	Niger	1996 - 2019 (24)	0.90
Costa Rica	2013 - 2020 (6)	0.21	Norway	1981 - 2021 (38)	0.95
Croatia	1996 - 2021 (24)	0.43	Peru	2008 - 2021 (14)	0.76
Curaçao	2001 - 2016 (14)	1.26	Philippines	1996 - 2022 (27)	1.76
Cyprus	1996 - 2021 (25)	0.07	Poland	1996 - 2021 (25)	0.71
Czechia	1994 - 2020 (20)	0.17	Portugal	1996 - 2022 (24)	0.00
Côte d'Ivoire	1996 - 2000 (5)	0.29	Qatar	2002 - 2017 (14)	1.89
Denmark	1996 - 2022 (26)	0.22	Romania	1996 - 2020 (22)	0.03
Dominican Republic	1996 - 2016 (10)	1.52	Russia	1996 - 2017 (13)	-0.19
Ecuador	2008 - 2020 (13)	0.53	Saudi Arabia	2003 - 2009 (7)	2.65
Egypt	1997 - 2015 (19)	0.92	Senegal	2015 - 2021 (7)	0.24
El Salvador	2015 - 2019 (5)	-0.62	Serbia	1998 - 2021 (23)	0.61
Estonia	1996 - 2021 (24)	0.45	Slovakia	1996 - 2022 (24)	0.15
Finland	1996 - 2021 (23)	0.17	Slovenia	1996 - 2021 (20)	0.28
France	1980 - 2021 (35)	0.26	South Africa	1996 - 2022 (24)	0.28
Germany	1980 - 2022 (38)	0.70	South Korea	1996 - 2020 (24)	0.63
Greece	1996 - 2021 (26)	0.17	Spain	1995 - 2021 (25)	0.32
Guatemala	2002 - 2021 (20)	-0.72	Sweden	1980 - 2021 (37)	0.41
Guinea	2004 - 2010 (5)	0.72	Switzerland	1993 - 2021 (25)	0.69
Honduras	2001 - 2015 (14)	-0.57	Tunisia	1996 - 2011 (16)	0.29
Hong Kong	1997 - 2011 (15)	0.90	Turkey	2010 - 2017 (8)	1.32
Hungary	1996 - 2021 (21)	0.14	USA	1980 - 2021 (38)	0.31
Iceland	2001 - 2014 (14)	0.22	Ukraine	1996 - 2019 (21)	0.17
India	1999 - 2019 (21)	0.57	United Kingdom	1981 - 2021 (36)	0.16
Indonesia	2017 - 2019 (3)	0.94	Uruguay	2016 - 2017 (2)	1.16
Iran	1997 - 2017 (20)	4.96	Uzbekistan	2011 - 2021 (10)	0.21
Ireland	1996 - 2021 (22)	0.26	Vanuatu	2002 - 2007 (6)	0.29
Israel	1996 - 2019 (24)	0.46	Venezuela	1998 - 2019 (20)	0.55

Note: Thrift theory predicts  $\bar{\theta}^* \cong 1$ . Free growth theory makes no prediction for these data.

Define  $\theta_{s,i} = \frac{(\Delta z^*)_i}{(\Delta g(K))_i}$  and  $\varphi_{s,i} = \frac{(\Delta q)_i}{(\Delta g(K))_i}$  to restate Eq. (10) as

$$\theta_{s,i} + \varphi_{s,i} = 1. \quad (11)$$

Next define  $\theta_s = E(\theta_{s,i})$  and  $\varphi_s = E(\varphi_{s,i})$ . By Eq. (11), then,

$$\theta_s + \varphi_s = 1. \quad \text{Eq. (9) now implies} \quad (12)$$

$$\theta_s = 1 \quad \text{and} \quad \varphi_s = 0, \quad \text{under thrift assumptions.} \quad (13)$$

Eq. (11) enables measurement of effects of thrift and free growth in a given period  $i$ , that is, while Eq. (12) does the same for all periods together.

$\theta$  and  $\varphi$  will be called the “thrift index” and “free growth index” respectively.  $\theta_s$  and  $\varphi_s$  give their values as found from data for change in net saving. Expected values, again, are predicted averages of outcomes. Thus Eq. (13) and thrift theory can be tested by finding average values of  $\theta_{s,i}$  and comparing findings to the expected value  $\theta = 1$ . First we find

$$\overline{\theta_{s,i}} = \frac{1}{m} \sum \theta_{s,i} \quad \text{and} \quad \overline{\varphi_{s,i}} = \frac{1}{m} \sum \varphi_{s,i},$$

where  $m$  is the number of observed values of  $\theta_{s,i}$  and  $\varphi_{s,i}$ , and test the predictions

$$\overline{\theta_{s,i}} \cong 1 \quad \text{and} \quad \overline{\varphi_{s,i}} \cong 0, \quad \text{under thrift assumptions.}$$

Calculations of  $\overline{\theta_{s,i}}$  and  $\overline{\varphi_{s,i}}$  are not expected to show 1 and 0 exactly, under thrift assumptions, so that  $\overline{\theta_{s,i}}$  and  $\overline{\varphi_{s,i}}$  are not exactly equal to  $\theta_s$  and  $\varphi_s$ , because the number of samples  $m$  is finite.

Fig. 2 shows average values of  $\theta_{s,i}$  and  $\varphi_{s,i}$  for 86 countries, both unweighted and weighted to GDP, over the period 1980-2022. Table 3 shows associated regressions of  $\Delta s^*$  and  $\Delta g_s$  respectively on  $\Delta g(K)$  at 0.1000 and 0.9000. Average values of  $\varphi_s$  for the 86 individual countries show in Table 4. To control distortions brought by small absolute denominators, years were screened out where  $|\Delta g(K)|$  was found at less than 0.01 (see Section 13). Results show  $\overline{\varphi_{s,i}} = 0.936$  and  $\overline{\theta_{s,i}} = 0.064$  for data weighted to GDP. These findings largely support free growth theory, but could suggest a small role (6.4%) for thrift as well. This possibility will be discussed in Section 4. We will first test thrift theory from a different approach.

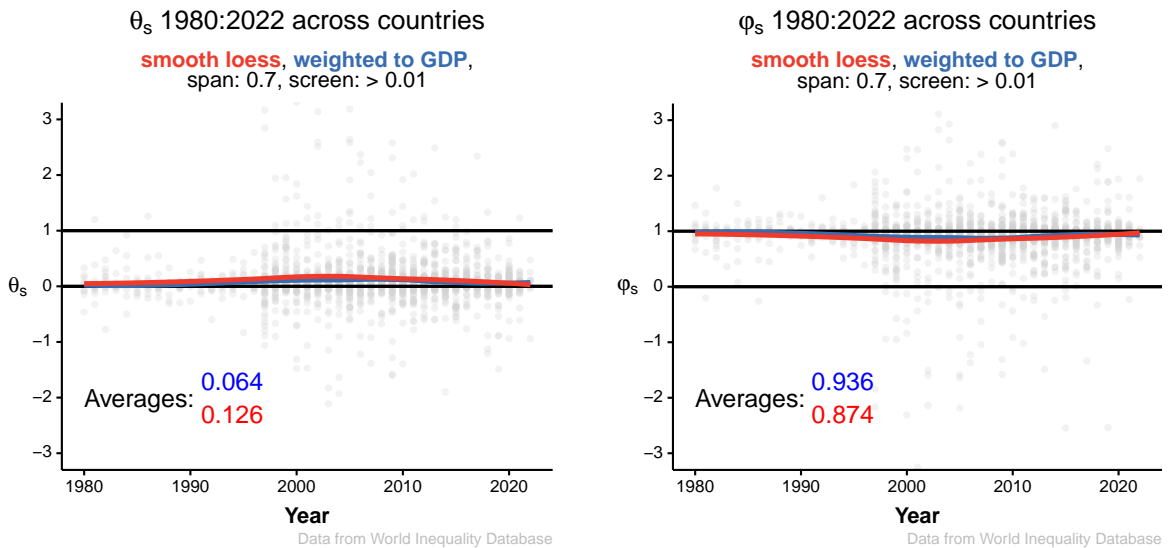


Fig. 2: Thrift and free growth indexes derived from net saving (86 countries).

**Table 3**Regression of  $\Delta s^*$  and  $\Delta q_s$  on  $\Delta g(K)$  (Screen = 0.01).  $H_0$  per thrift theory:  $\Delta g(K) \cong \Delta s^*$  &  $\Delta q_s \cong 0$ 

	$\Delta s^*$	$\Delta q_s$
Regression of value shown on $\Delta g(K)$	0.1000*** (0.0145)	0.9000*** (0.0145)
Observations	1,574	1,574
R <sup>2</sup>	0.32867	0.96233
Within R <sup>2</sup>	0.22713	0.95965
Year fixed effects	✓	✓
Country fixed effects	✓	✓

### 3. Consumption and capital growth

The concept of cash flow is little used in economics, aside from finance and in present value calculations. It is defined implicitly in the equation

$$P = \Delta K + F, \quad (14)$$

where  $P$  and  $F$  mean net profit and cash flow respectively<sup>3</sup>. Cash flow means the net outflow of value, in cash or kind, from an asset to its owner for consumption  $C$  or for reinvestment in other assets. This flow of spending is augmented by pay  $\Pi$ <sup>4</sup>. At the scale of the closed economy, meaning of all assets together, reinvestment cancels to zero. At this scale, then, the sum of spending  $F + \Pi$  is spent on consumption alone. That is,

$$\Pi + F = C \quad (15)$$

at the collective scale. Eq. (14), meanwhile, may be arranged as  $F = P - \Delta K$ . Substitution of this in Eq. (15), with rearrangement, gives

$$\Delta K = \Pi + P - C. \quad (16)$$

Thrift theory, which expects  $\Delta K = S_{net}$ , writes this as

$$S_{net} = \Pi + P - C, \quad \text{under thrift assumptions.} \quad (17)$$

Pay, net profit<sup>5</sup> and consumption can all be measured, to an extent, as can market-value capital, so that this prediction of thrift theory could be measured directly. Comparison between Eqs. (16) and (17), however, shows that such a test, given perfect data in national accounts, would only repeat that of Eq. (6). As before, the two theories are tested most revealingly in capital acceleration. Given the definitions<sup>6</sup>

$$\pi_i = \frac{\Pi_i}{K_{i-1}}, \quad p_i = \frac{P_i}{K_{i-1}} \quad \text{and} \quad c_i^* = \frac{C_i}{K_{i-1}},$$

Eq. (16) can be divided by capital to reach

$$g(K)_i = \pi_i + p_i - c_i^*, \quad \text{implying} \quad (18)$$

$$(\Delta g(K))_i = \Delta \pi_i + \Delta p_i - \Delta c_i^*, \quad \text{where} \quad (19)$$

$$\Delta \pi_i = \pi_i - \pi_{i-1}, \quad \Delta p_i = p_i - p_{i-1} \quad \text{and} \quad \Delta c_i^* = c_i^* - c_{i-1}^*,$$

<sup>3</sup>We have found no standard notation for cash flow.

<sup>4</sup>Compensation of employees plus a share of mixed income. We avoid the standard notation  $W$ , which is also used for work, as we prefer to distinguish pay from work.

<sup>5</sup>Jordà, Knoll, Kuvshinov, Schularick and Taylor (2019), The rate of return on everything.

<sup>6</sup>The notation  $c^*$ , as with  $s^*$ , shows an asterisk to distinguish its meaning  $c^* = \frac{C}{K}$  from the Keynesian  $c = \frac{C}{Y}$

as before. Thrift theory expects  $\Delta g(K) = \Delta s^* = \Delta \pi + \Delta p - \Delta c$  by Eqs. (9) and (17). It further expects changes in productivity, as realized in the pay/capital and profit/capital ratios  $\pi$  and  $p$ , to converge to zero as market noise, so that the only source of net saving is in consumption restraint  $-\Delta c^*$ . Thus

$$E(\Delta g(k)) = -\Delta c^* \quad \text{and} \quad E(\Delta \pi) = E(\Delta p) = 0, \quad \text{under thrift assumptions.} \quad (20)$$

Free growth theory, conversely, predicts that net saving contributes nothing to capital growth, and hence that net saving through consumption restraint, at the collective scale and in the private sector, is sacrifice with nothing in return. Free growth theory expects rather that costless increases in the ratios of pay and net profit to capital, enabled by greater productivity of human and physical capital already present, account for all capital growth and acceleration. Referring to Eq. (19), however, it predicts

$$E(\Delta g(k)) = \Delta \pi + \Delta p \quad \text{and} \quad E(\Delta c^*) = 0, \quad \text{by first approximation only, in free growth theory,} \quad (21)$$

for reasons shown in Section 4. As in Eq. (10), we prepare to test thrift theory by first dividing Eq. (20) by capital acceleration to reach

$$E\left(\frac{-\Delta c^*}{\Delta g(K)}\right) = 1, \quad \text{under thrift assumptions.} \quad (22)$$

Define  $\theta_{c,i} = \frac{-\Delta c_i^*}{\Delta g(K)_i}$  and  $\varphi_{c,i} = 1 - \theta_{c,i}$  to re-express Eq. (22) as

$$\theta_{c,i} + \varphi_{c,i} = 1. \quad (23)$$

By Eqs. (20) through (23), further,

$$E(\theta_c) = 1 \quad \text{and} \quad E(\varphi_c) = 0, \quad \text{under thrift assumptions.} \quad (24)$$

Define  $\theta_c = E(\theta_c)$  and  $\varphi_c = E(\varphi_c)$  to re-express Eqs. (23) and (24) respectively as

$$\theta_c + \varphi_c = 1, \quad \text{and} \quad (25)$$

$$\theta_c = 1 \quad \text{and} \quad \varphi_c = 0, \quad \text{under thrift assumptions.} \quad (26)$$

We infer  $\theta_c \cong \overline{\theta_{c,i}}$  and  $\varphi_c \cong \overline{\varphi_{c,i}}$  as before, and test thrift theory by comparing average yearly values of  $\theta_{c,i}$  and  $\varphi_{c,i}$  to its predictions  $\overline{\theta_{c,i}} \cong 1$  and  $\overline{\varphi_{c,i}} \cong 0$ .

Fig. 3 shows results of tests of these predictions from data for consumption reported in national accounts. Consumption was measured as the sum of personal consumption expenditure PCE and government consumption expenditure GCE. Capital K was again measured at market value. Again, years showing  $|\Delta g(K)| < .01$  were screened out to control small denominator effects. The generally higher values of  $\varphi_c$  (1.142) then  $\varphi_s$  (0.936) shown in the data will be discussed in Section 4.



**Table 4**Average  $\varphi_{s,i}$  and  $\varphi_{c,i}$  in 86 countries (screen = 0.01). Number of years clearing screen shown in ( )

Country	Period	$\overline{\varphi_{s,i}}$	$\overline{\varphi_{c,i}}$	Country	Period	$\overline{\varphi_{s,i}}$	$\overline{\varphi_{c,i}}$
Armenia	1997 - 2020 (20)	0.88	1.18	Italy	1981 - 2021 (22)	0.94	1.12
Aruba	1997 - 2001 (5)	-0.22	8.44	Japan	1981 - 2021 (30)	0.95	1.13
Australia	1974 - 2019 (35)	0.97	1.08	Kazakhstan	1997 - 2022 (23)	0.92	1.16
Austria	1997 - 2021 (16)	0.90	1.13	Kuwait	2005 - 2017 (11)	0.96	1.13
Azerbaijan	1997 - 2020 (23)	0.25	2.20	Kyrgyzstan	1998 - 2021 (22)	0.77	1.29
Bahrain	2010 - 2013 (4)	0.59	1.32	Latvia	1998 - 2021 (20)	0.99	1.15
Belgium	1997 - 2021 (19)	0.95	1.06	Lithuania	1997 - 2021 (18)	0.90	1.19
Bolivia	1999 - 2014 (12)	0.96	1.12	Luxembourg	1997 - 2021 (25)	1.00	1.02
Botswana	1997 - 2000 (4)	0.76	1.27	Malaysia	2008 - 2015 (7)	0.99	1.19
Brazil	1998 - 2020 (22)	0.90	1.24	Malta	1997 - 2021 (23)	0.92	1.04
British Virgin Islands	1997 - 1998 (2)	-1.24	-2.20	Mauritius	2015 - 2018 (4)	0.98	0.99
Bulgaria	1997 - 2017 (15)	1.03	1.19	Mexico	1997 - 2021 (22)	0.94	1.16
Burkina Faso	2001 - 2019 (16)	0.96	1.28	Moldova	1997 - 2019 (21)	0.89	1.27
Cameroon	1997 - 2019 (19)	0.82	2.71	Mongolia	2008 - 2021 (11)	0.90	1.06
Canada	1974 - 2022 (41)	0.91	1.08	Morocco	2000 - 2021 (17)	0.81	1.27
Cape Verde	2009 - 2016 (8)	0.73	2.02	Netherlands	1997 - 2021 (20)	0.97	1.08
Chile	1998 - 2021 (22)	0.94	1.48	New Zealand	1997 - 2019 (18)	0.86	1.02
China	1993 - 2020 (23)	0.91	1.05	Nicaragua	2008 - 2019 (12)	0.94	1.13
Colombia	1997 - 2022 (18)	1.03	2.39	Niger	1997 - 2019 (19)	0.78	1.87
Costa Rica	2014 - 2020 (6)	0.96	1.25	Norway	1982 - 2021 (34)	0.88	1.08
Croatia	1997 - 2021 (22)	0.81	2.09	Peru	2009 - 2021 (11)	0.96	1.30
Curaçao	2002 - 2016 (14)	0.59	0.51	Philippines	1997 - 2022 (20)	0.63	1.20
Cyprus	1997 - 2021 (23)	1.06	1.16	Poland	1997 - 2021 (15)	0.80	1.07
Czechia	1995 - 2021 (19)	1.03	1.08	Portugal	1997 - 2022 (17)	0.98	1.08
Côte d'Ivoire	1997 - 2000 (4)	1.03	1.05	Qatar	2004 - 2018 (12)	0.71	0.86
Denmark	1997 - 2022 (22)	0.95	1.14	Romania	1997 - 2020 (14)	0.98	1.16
Dominican Republic	2007 - 2015 (9)	0.85	1.41	Russia	1997 - 2018 (14)	0.91	1.11
Ecuador	2009 - 2020 (12)	0.83	1.91	Saudi Arabia	2005 - 2009 (3)	-1.23	0.02
Egypt	1998 - 2015 (16)	0.87	2.14	Senegal	2018 - 2021 (3)	0.81	2.31
El Salvador	2016 - 2019 (4)	0.02	-2.32	Serbia	1999 - 2021 (22)	0.78	1.67
Estonia	1997 - 2021 (19)	0.94	1.11	Slovakia	1997 - 2021 (18)	0.91	1.18
Finland	1997 - 2022 (21)	1.02	1.20	Slovenia	1997 - 2021 (20)	0.90	1.07
France	1972 - 2021 (33)	0.91	1.16	South Africa	1997 - 2022 (21)	0.90	1.13
Germany	1972 - 2022 (31)	0.95	1.14	South Korea	1997 - 2020 (15)	0.96	1.05
Greece	1997 - 2021 (24)	0.76	1.47	Spain	1996 - 2021 (23)	0.96	1.11
Guatemala	2003 - 2021 (11)	0.85	1.32	Sweden	1974 - 2022 (41)	0.98	1.15
Guinea	2005 - 2010 (6)	0.92	1.23	Switzerland	1993 - 2020 (24)	0.92	1.09
Honduras	2003 - 2015 (10)	0.60	0.85	Tunisia	1997 - 2011 (12)	0.68	1.17
Hong Kong	1997 - 2011 (13)	0.96	1.25	Turkey	2011 - 2015 (5)	1.16	1.54
Hungary	1997 - 2021 (21)	0.93	1.10	USA	1972 - 2021 (44)	0.98	1.13
Iceland	2002 - 2014 (12)	0.90	1.12	Ukraine	1997 - 2020 (23)	0.95	1.18
India	2000 - 2019 (14)	0.81	0.99	United Kingdom	1972 - 2021 (42)	0.98	1.21
Indonesia	2019 - 2019 (1)	1.41	0.98	Uruguay	2017 - 2017 (1)	0.44	0.98
Iran	1998 - 2018 (19)	-0.09	1.09	Uzbekistan	2012 - 2021 (9)	0.95	1.14
Ireland	1997 - 2021 (23)	0.98	1.23	Vanuatu	2003 - 2007 (3)	0.85	1.19
Israel	1997 - 2017 (18)	0.93	1.72	Venezuela	1999 - 2019 (20)	0.69	1.13

Note: Thrift theory predicts  $\overline{\varphi_{s,i}} \cong \overline{\varphi_{c,i}} \cong 0$ . Free growth theory predicts  $\overline{\varphi_{s,i}} \cong \overline{\varphi_{c,i}} \cong 1$ .

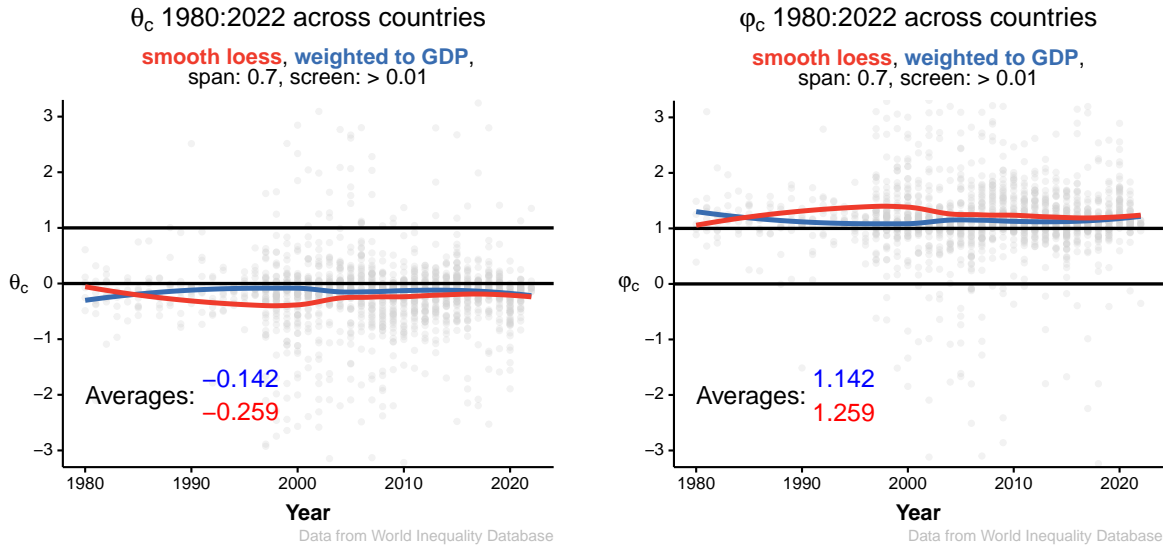


Fig. 3: Thrift and free growth indexes derived from consumption (86 countries).

Table 5

Regression of  $-\Delta c^*$  and  $\Delta q_c$  on  $\Delta g(K)$  (Screen = 0.01).  $H_0$  per thrift theory:  $\Delta g(K) \cong -\Delta c^* \& \Delta q_c \cong 0$

	$-\Delta c^*$	$\Delta q_c$
Regression of value shown on $\Delta g(K)$	-0.3760*** (0.1055)	1.376*** (0.1055)
Observations	1,548	1,548
R <sup>2</sup>	0.53993	0.88294
Within R <sup>2</sup>	0.31853	0.86226
Year fixed effects	✓	✓
Country fixed effects	✓	✓

#### 4. Differences in test results

Fig. 2 and Table 3 show  $\theta_s$  to average 0.064, and regression of  $\Delta s^*$  on  $\Delta g(K)$  to average 0.100, across all years and countries GDP-weighted. Fig. 3 and Table 5, meanwhile, showed these overall averages as  $-0.142$  for  $\theta_c$ , and as  $-0.376$  for regression of  $-\Delta c^*$  on  $\Delta g(K)$ . These differences might be explained by systematic mismeasurements of  $C$ ,  $K$  and  $S_{net}$  in national accounts. In that case, the evidence would leave open the possibility of some role for net saving (6.4%) in capital growth.

There is another possible interpretation. Regression or correlation or covariance among variables such as net saving and capital growth suggests causal relationship among them, but does not in itself reveal the direction of causality. Thrift theory accepts the natural inference that net saving is the cause, and capital growth the effect. Logic and experience, however, also suggest that adverse shocks such as war or depression might lower capital values despite all saving and investment, and might then motivate negative net saving (dissaving), meaning suspension of replacement saving, in order to maintain consumption. When peace and prosperity return, higher incomes will allow restoration of replacement saving to offset depreciation. Capital growth need not depend on positive net saving at any point, but rather allows an upward normalization of net saving from a negative value to zero. In this interpretation, change in capital growth becomes the cause, rather than the effect, of change in net saving.

This possibility could help explain differences between the measurements of GDP-weighted  $\varphi_s(0.936)$  and  $\varphi_c(1.142)$ , without need to assume systematic mismeasurements of  $S_{net}$ ,  $K$  and  $C$ . Note here that the finding  $\varphi > 1$  is possible in principle when gain in productivity allows growth in capital and consumption at the same time (see the quote from Mill in Appendix C.) We welcome further study to resolve these uncertainties.

## 5. Mechanics of free growth

Some growth is capital widening, where structures and implements increase in number but do not change in design. Capital widening, however, is practical only so far before glut and diminishing returns set in. Further growth from that point must come from capital deepening, meaning improvements in the design of capital. Solow (1956) noted a kind of middle ground between capital widening and capital deepening in the disembodied growth mentioned earlier; ships carrying coals to Newcastle can raise prospective cash flows, and hence present value, by reversing the business plan. But Solow, who came to conclusions similar to ours from different evidence, puzzled as to how capital growth without net saving could be possible for capital deepening through “embodied” growth, where products of new design are made from plant of new design.<sup>7</sup>

The solution, we suggest, is that embodied growth is disembodied growth on a finer scale. At each step toward realization of the new plant and products, raw materials and products and labor skills and plant capacity currently available on the market are adapted to new uses. The innovator pays for these inputs at a market price determined by their value in established productive uses, but applies them innovatively to realize higher prospective cash flows, and hence higher present values, to the innovator (Marshall (1890), Schumpeter and Opie (1934)). This difference in present value realized less price paid will here be called the “innovator’s reserve”, meaning reserve price for inputs of capital and labor.<sup>8</sup> The innovator’s reserve quantifies the part of free growth explained by productivity gain as distinct from random market noise. As such, it is the quantity added to depreciation saving to enable embodied growth, so that net saving is never needed.

Our findings support those of Piketty and Zucman (2014) and Kurz (2023) as to the market power of innovators to explain capital growth beyond net saving. Again, we go farther by questioning the assumption that net saving contributes even a part of capital growth.

## 6. Optimum investment policy

Data and arguments adduced, with uncertainties discussed in Section 4, suggest that the optimum amount of saving, at the global scale, is replacement saving to offset depreciation, and nothing more. That would not mean book depreciation, as this study has stressed differences between book and market values. Up to a point, it should be possible to analyze the composition of market capital, and to model depreciation of the whole. A better plan, as Solow (1956) wrote in response to Harrod’s knife edge argument (Harrod, 1939), is to trust the market to maximize rate of return, and to sense the point where glut begins and returns fall.<sup>9</sup> Markets do so imperfectly when tax and other public policy reward saving over distributions and consumption. Findings in this paper suggest review of such policies. These include the double tax on dividends, and the greater tax rate on ordinary income than on capital gains. Effects of removing the double tax, and removing the difference between tax rates on ordinary income and on capital gains, could be revenue-neutral and non-partisan if the corporate tax were raised to match, if the tax rates on ordinary income and on capital gains met somewhere between, and if thoughtful grandfathering eased the transition.

## 7. Inferences for national accounts and macroeconomics

Eq. (16) was presented as a tautology or logical certainty. Cash flow  $F$  from all physical capital  $K$  together at the collective scale, that is, means outflow of value from  $K$  net of any inflow into  $K$  from any source, meaning from pay  $\Pi$  as well as plowback of cash flow. Thus the sum  $F + \Pi$  is spent on consumption  $C$  alone by exhaust of alternatives.

<sup>7</sup>The terms capital deepening, capital widening, embodied growth and disembodied growth are all Solow’s.

<sup>8</sup>i.e., capital and labor inputs are worth more to the innovator in that the innovator applies them in ways to realize greater returns. The present value of additional cash flow enabled by this advantage in return quantifies the innovator’s reserve and equivalently the non-random component of free growth.

<sup>9</sup>Harrod had argued that saving must hit the warranted rate exactly or risk positive feedback through the operation of the output/capital ratio (accelerator).

Meanwhile cash flow is net profit  $P$  less capital growth  $\Delta K$ .<sup>10</sup> This reasoning gave  $F + \Pi = C$ ,  $F = P - \Delta K$ , and consequently  $\Pi + P = C + \Delta K$  (Eq. (16)).

Kuznets and the other founders of national accounts, under the influence of Keynes, seem to have reasoned alike. National accounts are double-entry  $T$  accounts where net product  $C + \Delta K$  is equated to net "factor payments"  $\Pi + P$ . National accounts, however, equate capital growth to net saving/investment, and effectively write Eq. (16) as  $\Pi + P = C + S_{net}$ . We have attempted to show that net saving does not tend to equate to capital growth, and indeed contributes no part of capital growth. If our argument proves correct, then national accounts, and the teachings of macroeconomics (macro) which they express, are constructed on a fundamental misperception. We would therefore welcome any critiques of our findings as a matter of academic and public interest.

## 8. Inferences for microeconomics

Microeconomics ("micro") studies the mutual effects of supply, demand and price. It teaches that producer cost, including interest as the cost of time, tends to equilibrate to market value realized. We have proposed an exception in the innovator's reserve; the innovator pays the going rates for skills and materials needed, but applies them to make products of greater market value.

## 9. Inferences for inflation

If free growth theory is correct, then net investment adds a superfluous cost to capital growth, while decreasing market value per unit through capital glut. Both effects would tend to contribute directly to capital inflation, and indirectly to inflation of consumer goods by adding depreciation costs. This consideration adds to the case for urgent attention to our argument, and for more study to confirm or refute it.

## 10. Net output

The concept of net output is found in our discussions, but not in our equations. Net output means value added. Appendix B will show an argument that to equate value added to the sum of consumption and capital growth, and neither less nor more, would miss two components, one negative and one positive, in value added to human capital, and that both of these components are unmeasurable by known means. Since we work here from measurable data for consumption and net saving and market value capital, we did our best to reason from those three quantities alone.

## 11. Data sources

All our data are drawn from Distributional National Accounts (DINA) from the free online database World Inequality Database (WID). This source collates data from national accounts and tax data of 105 countries in constant currency units, and adjusts them where needed to conform to current standards of the System of National Accounts (SNA) published by the United Nations. We show results for the 86 of those countries which report all three of the factors, namely net saving, consumption and market-value capital, needed for deriving the thrift and free growth indexes. WID's source for these data is national accounts.

Consumption  $C$  in our text and equations is reproduced from the sum of Government Final Consumption Expenditure (mcongo)<sup>11</sup> and Private Expenditures of Households and NPISH (mconhn). This sums government expenditure GCE and personal consumption expenditure PCE. Net saving  $S_{net}$  and market-value  $K$  are taken from net national saving (msavin) and market-value Capital Wealth (mnweal) respectively. GDP, which we use only for weighting purposes in Figs. 1 and 2, is reproduced from GDP (mgdpro).

## 12. Accessing our results and methods

Tables and other displays of our findings for each country, and showing our methods of calculation, can be accessed at the web appendix ([https://web-appendix.shinyapps.io/Sources\\_of\\_Capital\\_Growth](https://web-appendix.shinyapps.io/Sources_of_Capital_Growth)).

<sup>10</sup>Or equivalently gross profit less capital growth less depreciation.

<sup>11</sup>WID code

### 13. Displays

Eqs. (12) and (25) show  $\theta_s + \varphi_s = 1$  and  $\theta_c + \varphi_c = 1$ . Some displays here and in the web appendix save space by showing  $\varphi_s$  and  $\varphi_c$  only, leaving  $\theta_s$  and  $\theta_c$  implicit as their complements to unity. The web appendix includes displays of  $\varphi_s$  and  $\varphi_c$  for each year in each country over the report period. These tend to show upward and downward spikes in values of  $\varphi_s$  and  $\varphi_c$  in some years. Those spikes tend to be associated with small absolute values of denominators, in these cases  $\Delta g(K)$ , in those countries and years. Small denominators magnify errors in measurements of numerators. Worse, when denominators are small, small mismeasurements in them might reverse the term in sign.

To maximize reliability of test results, we apply a range of screens to omit years where absolute denominators fall below a given threshold. Some displays show data for all years, regardless of denominator size. Others screen out all years where absolute denominators are less than .01, then .025, then continuing upward in increments of .025 to a maximum screen of .15.  $\varphi_s$  and  $\varphi_c$  are plotted for each country unscreened and at each of the seven successive levels of screening. All displays applied a screen of .01. The denominator whose absolute value is screened is capital acceleration  $\Delta g(K)$  or capital growth rate  $g(K)$  in all displays.

Screening out years where absolute  $\Delta g(K)$  or  $g(K)$  is small would cost little in informative value even if measurements were exact. In those years, there is little capital acceleration or capital growth, positive or negative, for either thrift theory or free growth theory to explain. Market noise alone might account for  $\Delta g(K)$  or  $g(K)$  in such years. Screening reduces the number of observations, but increases the reliability and informative value of each.

### 14. Disclaimers

We accept that capital growth is impossible without capital replacement first, to make up losses to depreciation, and that the only source of capital replacement is replacement investment. Thus we accept the necessity and efficacy of replacement investment. We dispute only the efficacy of net investment in realizing capital growth after replacement investment has made up for depreciation.

### 15. Discussion and conclusions

Capital glut is the condition warned against by West, Ricardo, Malthus and Harrod. It is loosely defined as oversupply of capital at the current state of technology. We will not attempt a more exact definition here. Findings shown in our displays, anyhow, suggest that net saving raises the physical quantity of capital, say in number of shops, manufacturing plants or finished goods of similar design, without raising aggregate value of capital, and so contributes to capital glut.

These findings challenge the teachings that capital growth is effected by net saving enabled by consumption restraint, and that producer cost, including imputed interest as the opportunity cost of capital, converges to market realization. Evidence showing  $\overline{\varphi_{s,i}} \cong 1$  and  $\overline{\varphi_{c,i}} \cong 1$  suggests that all capital growth is free, and consequently that market realization, in the presence of innovation, exceeds producer cost by the entirety of capital growth. Meanwhile the same evidence, which indicates that net saving adds no capital value, suggests a review of the teachings that consumption plus net saving gives net income, and that consumption plus net investment gives net output. Appendix B will also question the latter teachings.

Embodied growth is disembodied growth on a finer scale. It redeploys or repurposes existing labor skills, raw materials, and plant capacity, as well as existing finished goods, to achieve higher returns than available from the customary uses which determine their prices. The present value of yields from this advantage in return, or equivalently the innovator's reserve, defines the non-random component in free growth.

### Appendix A. Equivalence of saving and investment

Any usage which treats saving and investment as equal must deal with the fact that saving held in cash is not investment in the usual sense of spending on productive capital, and contributes nothing to output. Keynes (1936) defined that unspent saving as intended saving, and actual saving as the part so spent.

We suggest that investors seek to maximize return, within risk tolerance, and will sometimes hold saving in cash or equivalents at zero return in recessions and depressions when positive returns cannot be found, and so when investing in the usual sense would tend to reduce capital and output rather than increase them. Thus investment could have the

usual meaning in usual times, when prospective returns bring animal spirits, and could include saving in cash when not. It is in this sense that we equate saving to investment.

## Appendix B. Net output with human capital

Human capital is impractical to measure, as it leaves little market record other than for its rental income in pay and investment cost in schooling. Thus national accounts leave it implicit, and allow us to infer what we can from data for pay and schooling. Those accounts are founded on the principle, sound when terms are appropriately redefined, that net output, or value added, is expressed in the sum of capital growth and net outflow from the value-added chain. In national accounts, then, where physical capital is the whole of capital while net outflow of the chain is the whole of consumption, the reasoning is

$$Y = \Delta K + C, \quad \text{neglecting human capital.}^{12} \quad (\text{B.1})$$

It is possible in principle to model a value-added chain which includes human capital, and to compare findings with those shown in Eq. (B.1). Let human capital  $H$ , in that new model, stand as the last link in the value-added chain. Adapting the classic illustration of the value added principle, say that farms produce wheat, mills convert the wheat to flour, bakeries convert the flour into bread, and humans convert some of the bread, called invested consumption, into human capital. The net outflow from this extended value-added chain is not all of consumption, but only pure consumption, meaning the part remaining after the part invested in human capital (invested consumption) is subtracted<sup>13</sup>. By this reasoning, the principle that net output is expressed in capital growth plus net outflow gives

$$Y = \Delta K + \Delta H + C_p, \quad \text{allowing human capital,} \quad (\text{B.2})$$

where  $C_p$  gives pure consumption.

Yoram Ben-Porath (1967) reasoned that growth in human capital equals invested consumption plus self-invested work less human depreciation<sup>14</sup>. Let  $C_s$ ,  $W_s$  and  $D(H)$  show these flows respectively. Thus the combined arguments of Schultz and Ben-Porath arrive at

$$C = C_s + C_p \quad \text{and} \quad \Delta H = C_s + W_s - D(H), \quad \text{allowing human capital.} \quad (\text{B.3})$$

Substitution of these equations into Eq. (B.2) finds

$$Y = \Delta K + C_s + W_s - D(H) + C_p \quad \text{and consequently} \\ Y = \Delta K + C + W_s - D(H), \quad \text{allowing human capital,} \quad (\text{B.4})$$

if Schultz and Ben-Porath and the reasoning here are right.

## Appendix C. Mill's statement of the free growth idea

Mill (1848), book 1, chapter 5, section 4, includes:

If it were said, for instance, that the only way to accelerate the increase of capital is by increase of saving, the idea would probably be suggested of greater abstinence, and increased privation. But it is obvious that whatever increases the productive power of labour creates an additional fund to make savings from, and enables capital to be enlarged not only without additional privation, but concurrently with an increase of personal consumption.

This passage may be the first clear statement of what we call free growth theory. His use of the words "accelerate" and "concurrently" suggest that his path of reasoning was something like ours, and that he meant what we call free growth rather than the alternating phases of higher and lower saving rates pictured in thrift theory.

<sup>12</sup>Where  $\Delta K$ , mistakenly, we argue, is measured as  $S_{net}$ .

<sup>13</sup>The concepts of invested consumption, pure consumption, self-invested work and human depreciation were introduced in Schultz (1961).

<sup>14</sup>Equation 4 in Ben-Porath's paper, summarizing his first three equations. His terms and notation differ from ours. The concepts of invested consumption were also introduced by Schultz (1961).

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