

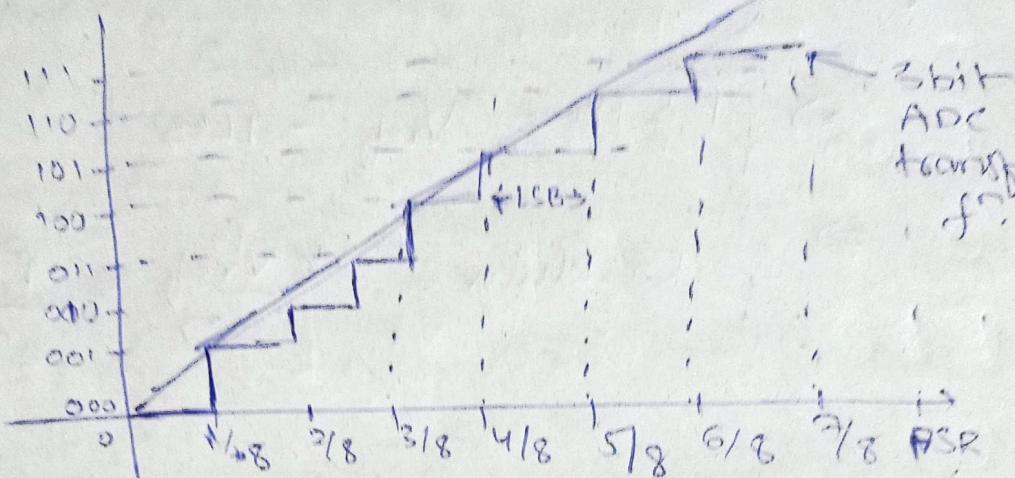
$$\text{Resolution} = \frac{\text{Full Scale Range FSR}}{2^{\text{no. of bits}}}$$

$$= \frac{V_{\max} - V_{\min}}{2^n}$$

$$\boxed{FSR \times \frac{V_{ref}}{2^n}} = \text{Resolution}$$

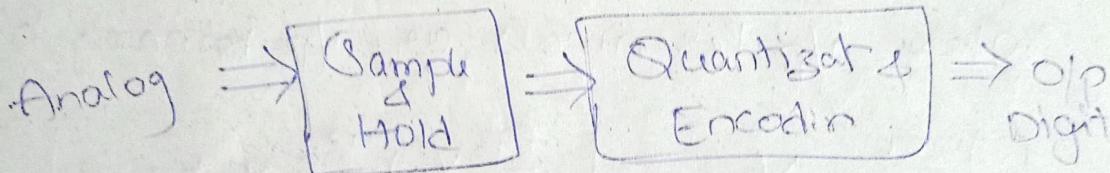
If full scale voltage of 8 bit ADC is
 $2V$ then Resolution = $\frac{2V}{2^3} = \frac{1}{4}$

Transfer fn of ADC & DAC
at 3 bit range of 0-1V at 2001 T_{600K}
full



$$\text{Quantization Error} = 1 \text{ LSB}$$

BDG of ADC :-



Important parameters of ADC & DAC

- Resolution
- Reference voltage | full scale Range
- Sampling time & conversion time | settling time
- Gain Error & Offset error
- Non-linearity (Integral & Differential)
- Total harmonics. fHDD

Binary weighted Resistor DAC

$$\text{Full scale o/p voltage} = \frac{2^n - 1}{2^n} \times V_{ref}$$

$$\Rightarrow FSD = V_{ref} - 1LSB$$

$$\Rightarrow \text{Resolution} = k \frac{V_{ref}}{2^n} = \frac{FSD}{2^n - 1}$$

$$V_o = -\frac{R_f}{R_1} V_{ref} \left(\frac{v_1}{R_1} + \frac{v_2}{R_2} + \dots \right)$$

\Rightarrow A Binary weighted Resistor DAC is simply a ~~an~~ Inverting summing amplifier where i/p terminals are i/p binary bits

$$\text{Where } V_o = - \left[\frac{R_f}{R_1} v_1 + \frac{R_f}{R_2} v_2 + \dots \right]$$

In Binary weighted register, O/P is a form of $R_1 = R, R_2 = 2R, R_3 = 8R, \dots$ 2^n order form

$$\Rightarrow V_o = -R_f \left[\frac{v_1}{R} + \frac{v_2}{2R} + \frac{v_3}{8R} + \dots \right]$$

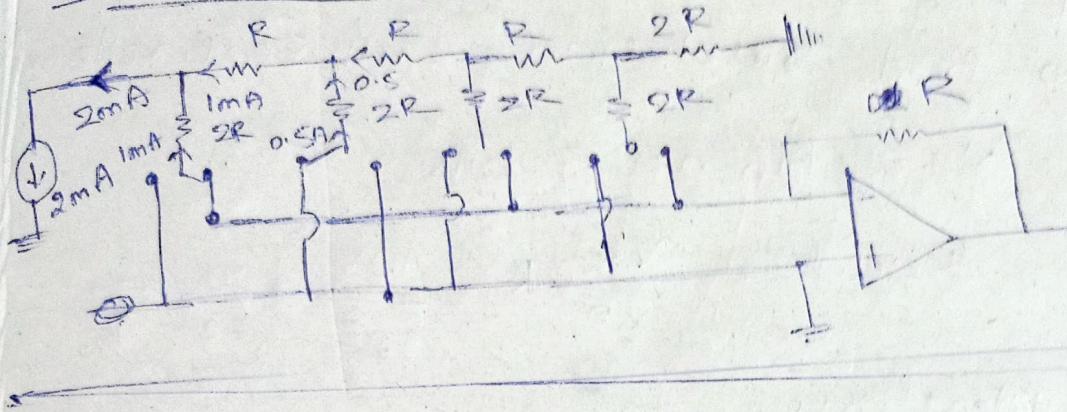
$$V_o = -\frac{R_f}{R} \left[\frac{v_1}{1} + \frac{v_2}{2} + \frac{v_3}{8} + \frac{v_4}{16} + \dots \right]$$

~~(*)~~ where v_1 is MSB $\{$ Date bit
 v_n is LSB

$$\therefore V_o = -R_f [B_o \cdot V_{ref} + \frac{B_1 V_{ref}}{2} + \dots]$$

$$\Rightarrow V_o = -\frac{R_f}{R} \cdot V_{ref}$$

Inverted R-2R LADDER DAC



DAC 3 bit when k = 1 :

Digital

0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1

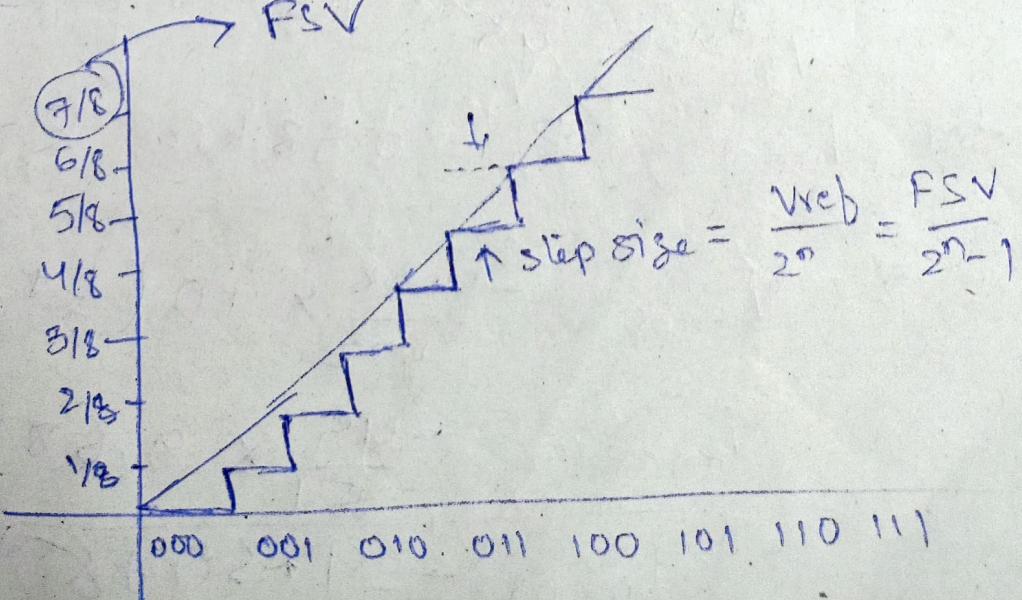
Analog

0	$V_{ref}/8$
	$2V_{ref}/8$
	$3V_{ref}/8$
	$4V_{ref}/8$
	$5V_{ref}/8$
	$6V_{ref}/8$
	$7V_{ref}/8$

No. of steps

$$= \frac{V_{ref}}{\text{resolution}}$$

Transfer function:-



① find ~~V_{max}~~ & V_{min} for 1111[°]/P with
binary weighted DAC, V_{ref} = 10V,
 $R_f = R = 1k\Omega$, Resistance Tolerance 2%
Also find resolution, full scale voltage

Ans: No. of bits n = 5 bits

$$\text{Resolution} = \frac{\text{Vref}}{2^n} K = \frac{10\text{V}}{2^5} = \frac{10}{32} = \frac{5}{16}$$

In Ideal case,

$$V_0 = -\frac{R_f}{R} V_{ref} \left[\frac{d_1}{2} + \frac{d_2}{4} + \frac{d_3}{8} + \frac{d_4}{16} + \frac{d_5}{32} \right]$$

$$V_0 = -10 \left[\frac{16+8+4+2+1}{3216} \right]$$

$$V_0 = -5 \times \frac{15}{16} = -\frac{75}{8} = -9.375$$

for V_{max} $\Rightarrow R_f = 1.02 \text{ k}\Omega$; $R = 0.98 \text{ k}\Omega$

$$\Rightarrow V_{\text{max}} = \frac{-1.02}{0.98} \times 10 \left(\frac{1}{2} + \frac{1}{4} u + \frac{1}{8} + \frac{1}{16} + \frac{1}{32} \right)$$

$$V_0 = -\frac{51}{45} \times 9.6875 = -10.0829$$

for V_{min} ; $R_f = 0.98 \text{ k}\Omega$, $R = 1.02 \text{ k}\Omega$

$$\Rightarrow V_{min} = \frac{-0.98}{1.07} \times 10 \left(3 + \frac{1}{4} \left(\frac{1}{8} + \frac{1}{16} + \frac{1}{32} \right) \right)$$

$$V_{min} = \frac{-45}{\pi} \times 9.6835$$

$$V_{\min} = -9.3078$$

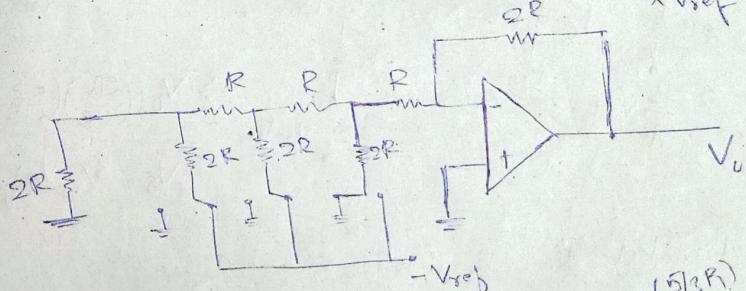
$$\text{full scale voltage} = \frac{2^n - 1}{2^n} \times V_{ref}$$

$$= \frac{31}{32} \times 10 = \frac{155}{16} = 10$$

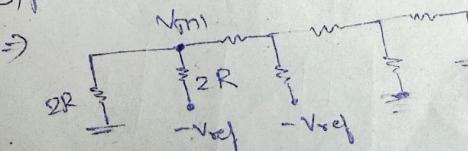
$$FSV = 9.6875$$

→ for accurate analog OIP tolerance should be 100.

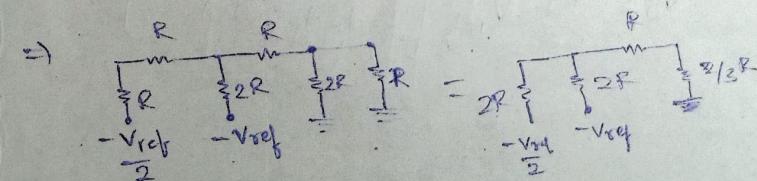
$$\text{R-2R Ladder: } \quad \text{Ans. } V_o = \left[\frac{a_n}{2^n} + \frac{a_{n-1}}{2^{n-1}} + \cdots + \frac{a_2}{2^2} + \frac{a_1}{2^1} \right] \times V_{in}$$



$$q_{1P} = 0.11$$

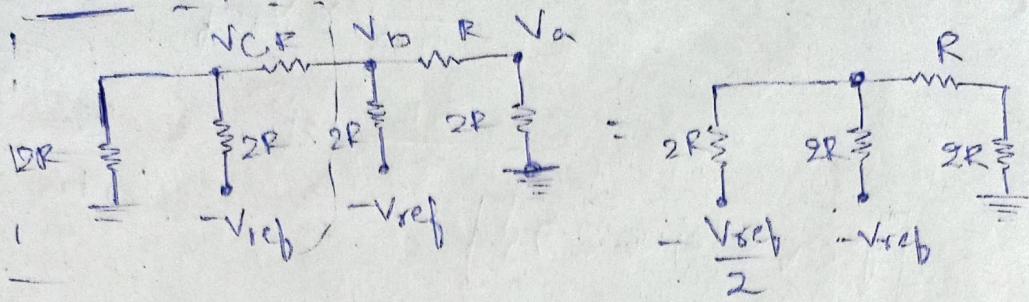


$$V_{Th1} = \frac{(-V_{ref}) 2R}{2R + R} = -\frac{V_{ref}}{2}; R_{Th} = R \quad (\because 2R \parallel R)$$



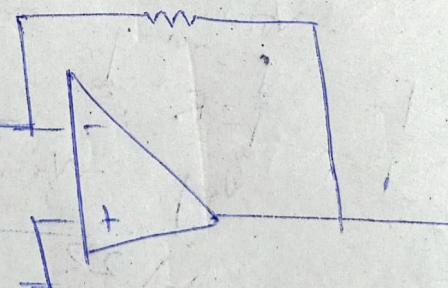
$$\Rightarrow \quad \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} \quad \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} \quad = \quad \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} \quad \begin{array}{c} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array}$$

-For 011 h



$$\frac{2R}{-\frac{3}{4}\text{V}_{\text{ref}}} = \frac{2R}{-\frac{3}{8}\text{V}_{\text{ref}}} \Rightarrow \text{V}_o = \left(\frac{2R}{2R}\right) \left(-\frac{3}{8}\text{V}_{\text{ref}}\right)$$
$$\Rightarrow \boxed{\text{V}_o = \frac{3}{8}\text{V}_{\text{ref}}}$$

Inverted R-2R LADDER



$$\text{V}_o = -\frac{R_f}{R} \text{V}_{\text{ref}} \left[\frac{1}{2}d_1 + \frac{1}{2}d_2 + \dots \right]$$

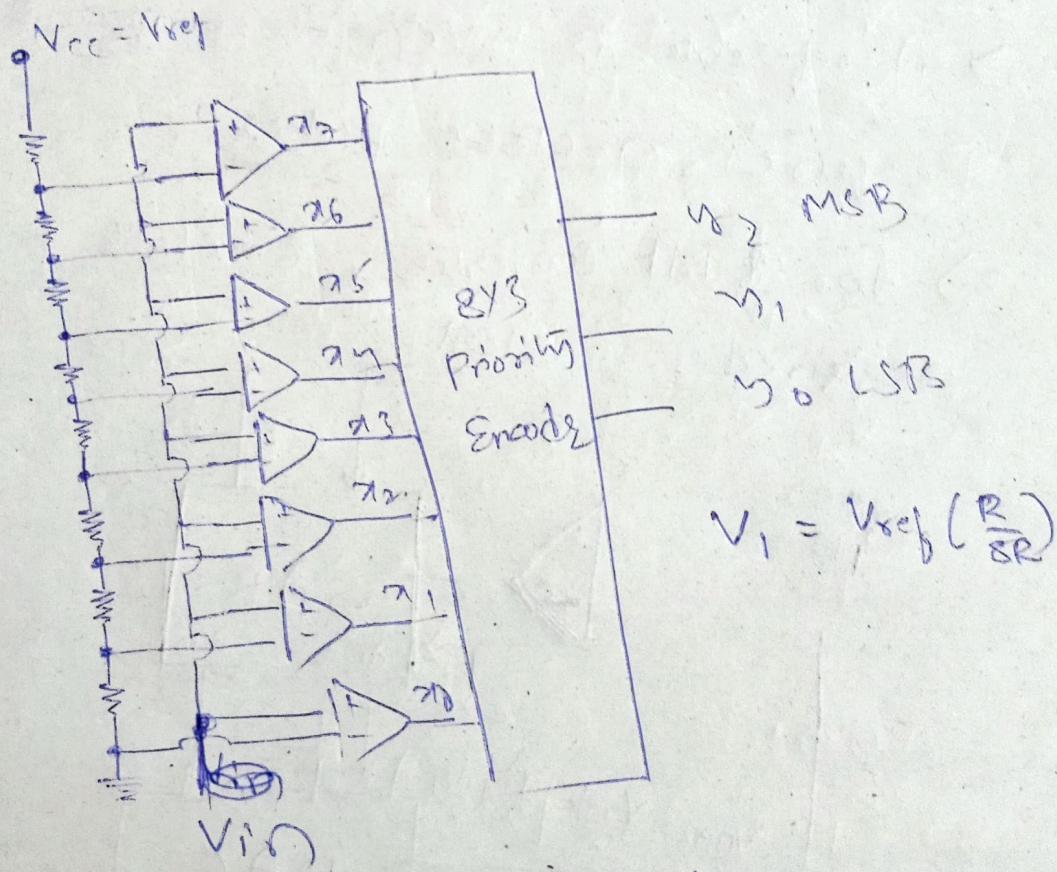
ADC Types:

(i) Direct type
(ii) Integrating type.

(i) Direct type ADC has: Flash ADC, counter type ADC, tracking / servo converter, successive approximation type.

(ii) Integrating type: Charge balancing ADC, Dual slope ADC.

Flash / parallel comparators ADC



It is made of voltage divider made of precision rectifier & comparators -
also a priority encoder.
→ It need only one clock cycle

→ let $V_{in} = 5.3V$, $V_{ref} = 8V$

→ i/p terminals have:

00011111
11100000

Priority is 5
so o/p is 101

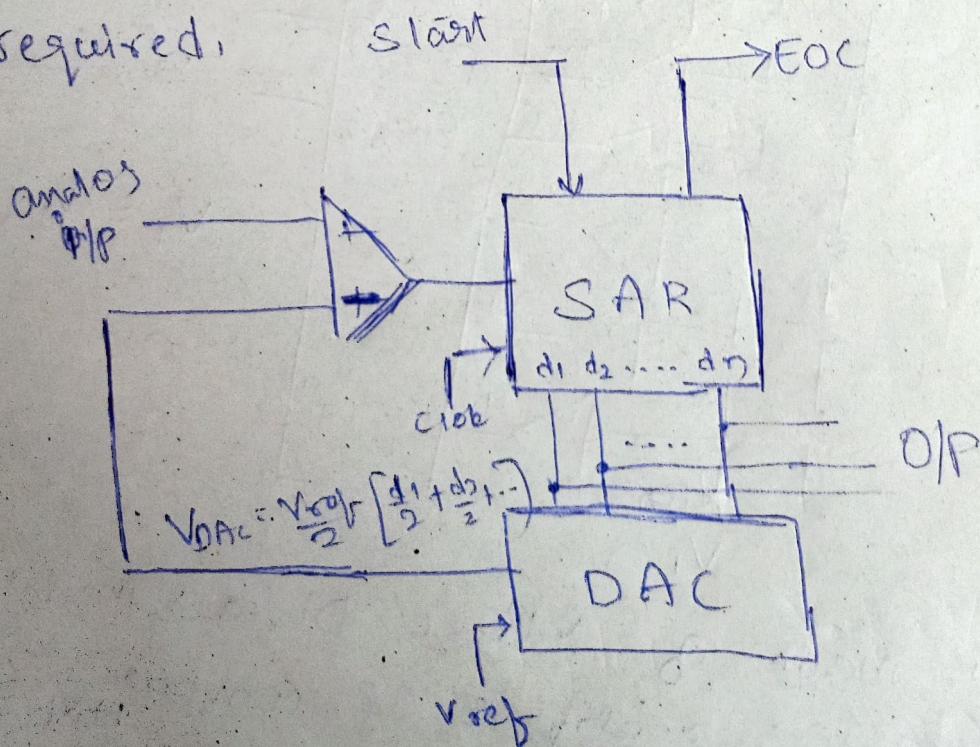
Successive Approximation Type ADC

→ Conversion time period doesn't depend upon on i/p voltage

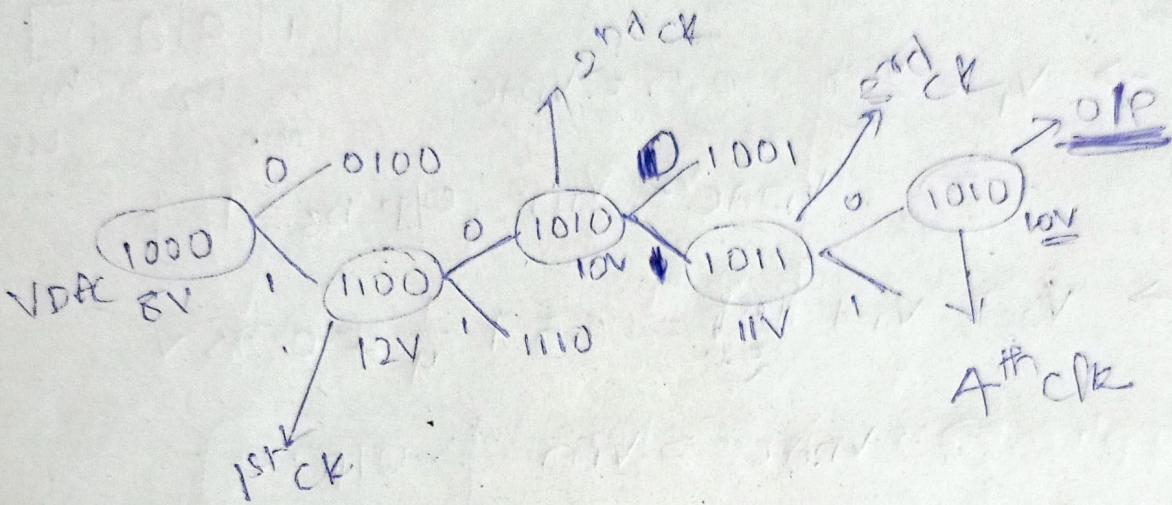
$$T_c \propto \text{no. of bits}$$

→ A reference is taken for comparison with o/p
Requires n-clock pulses

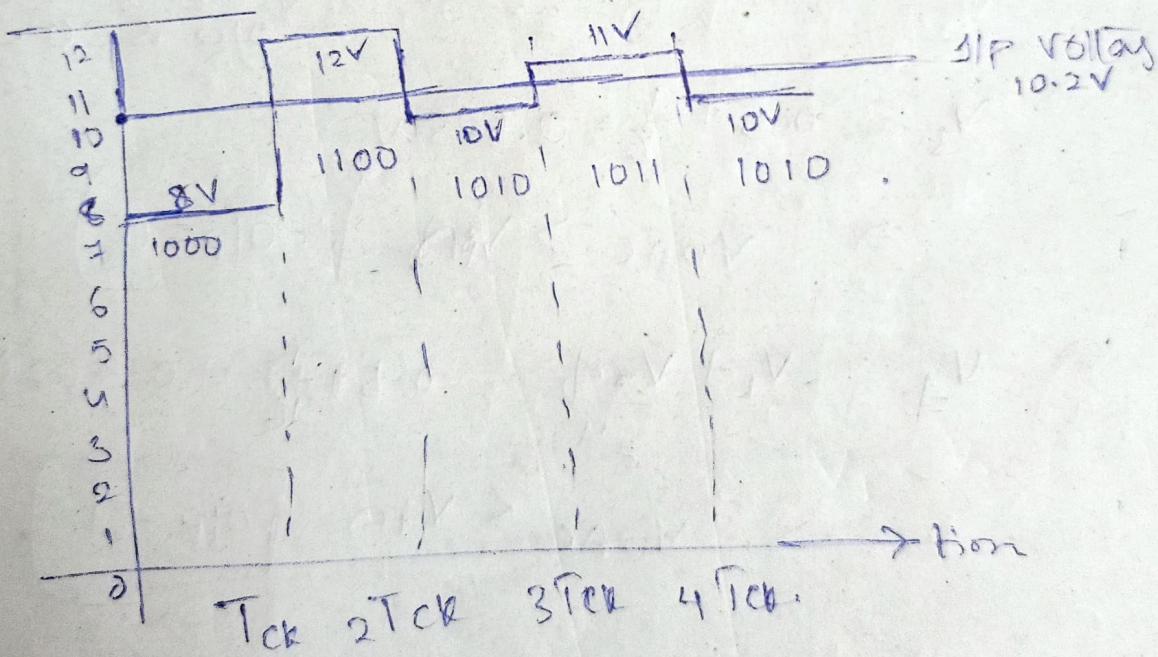
⇒ for 8 bit converter, 8-clock pulses are required.



Q:- Analog I/p $V_{in} = 10.2V$ & $V_{ref} = 16V$.
 Initially MSB = 1000 $\Rightarrow V_{DAC} = 8V$
 assuming 4-bit o/p no. of clock pulses is 4



Time Duration Graph / conversion time \Rightarrow SAR



\Rightarrow Conversion time is constant & independent

$$T_c = N T_{clk}, \quad N = \text{no. of bits}$$

Q:- To find digital Equivalent of V_{in}

= 0.6V for 4 bit ADC & $V_{ref} = 1V$

Ans's → for b_3 i.e., MSB

$$\rightarrow V_1 = \frac{V_{ref}}{2} = 0.5 = V_{DAC}$$

1	0	1	1
b_3	b_2	b_1	b_0

MSB LSB

$$\Rightarrow V_{DAC} < V_{in} \quad \boxed{O/P\ b_3 = 1}$$

$$\rightarrow V_2 = V_1 + \frac{V_{ref}}{2^2} = 0.5 + \frac{1}{4} \neq 0.75V$$

$$\Rightarrow V_{DAC} > V_{in} \quad \boxed{\therefore O/P = 0}$$

$$\rightarrow V_3 = V_1 + V_2 + \frac{V_{ref}}{2^3} \quad \left[\text{here } V_2 = 0 \because \text{its O/P is 0.}\right]$$

$$\Rightarrow V_3 = 0.5 + \frac{1}{8} = 0.625V$$

$$\Rightarrow V_{DAC} > V_{in} \quad \boxed{\therefore O/P = 0}$$

$$\Rightarrow V_4 = V_1 + \frac{V_{ref}}{2^4} = 0.5 + \frac{1}{16} = 0.5625$$

$$\Rightarrow V_{DAC} < V_{in} \quad \boxed{O/P = 1}$$

1001

$$\Rightarrow (1 \times 2^3 + 0 + 0 + 2^0 \times 1) = 9$$

$$(V_{out})_{0.6 \text{ for digital}} = \frac{V_{ref} \times O/P \text{ volt}}{2^n}$$

$$= \frac{1 \times 9}{2^4} = 0.5625$$

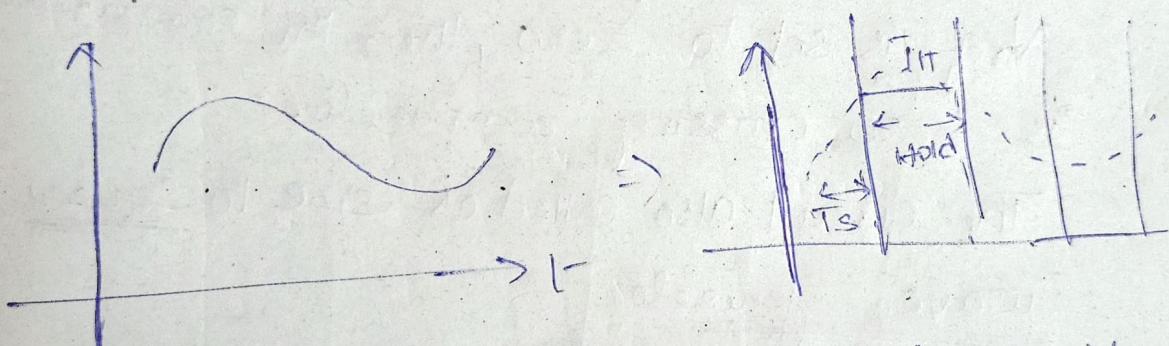
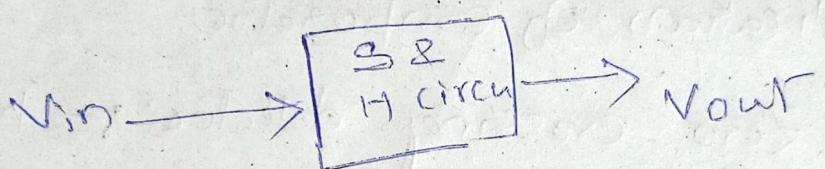
Unit-15 : Sam

→ Sample & Hold circuit

⇒ Used in sampling process, to make i/p signal discrete.

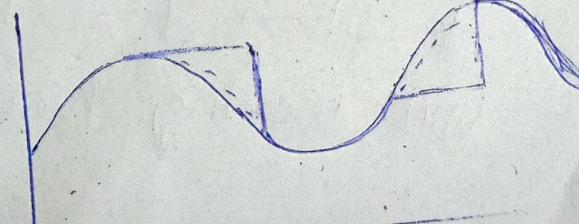
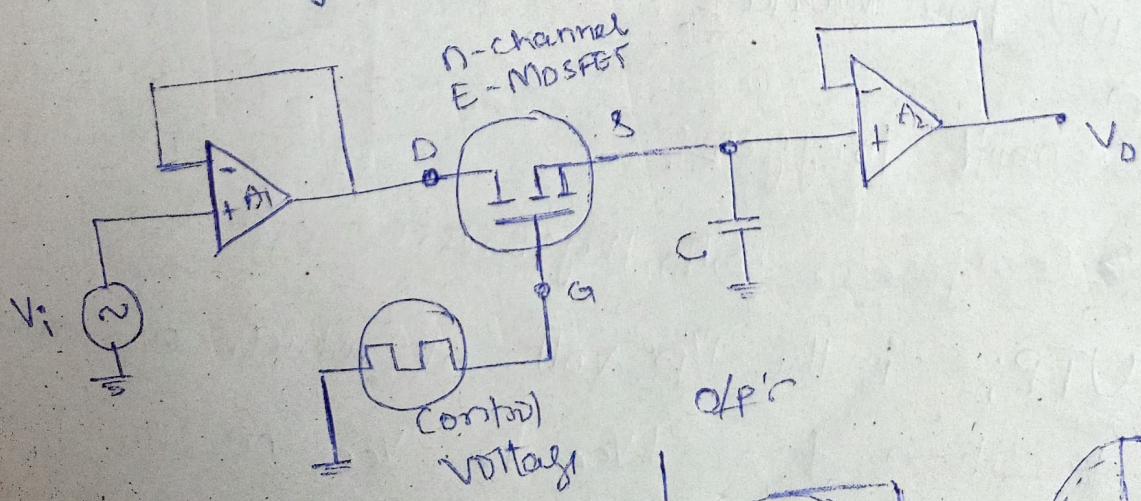
⇒ Used to convert Analog to Digital.

⇒ Samples i/p signal & holds it for some time period



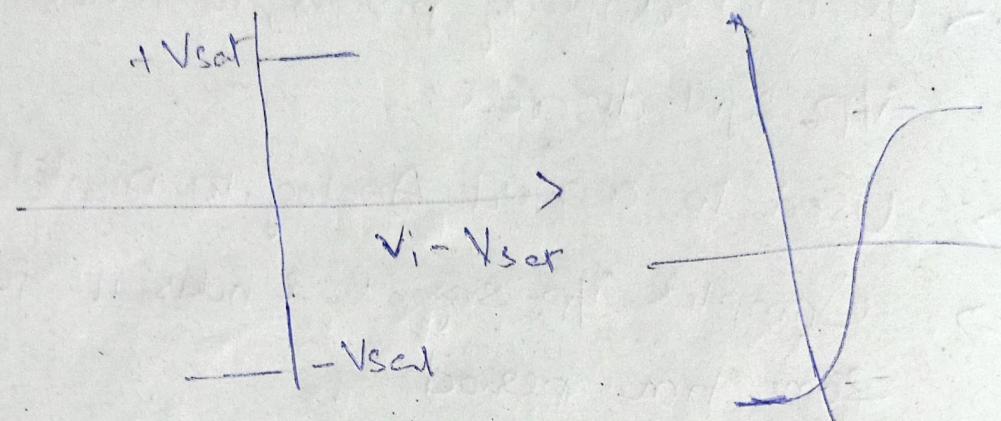
⇒ During T_s period O/P follows i/p

⇒ During T_H time O/P is constant hold



Comparators:-

Transfer fⁿ Ideal & practical



Applications of comparators

(i) Zero crossing detectors :- When

Ref is set to zero, then the comparator is zero crossing comparator.

The circuit also called as Sine to Square wave generator.

(ii) Window Detectors :- (LED turns on/off)

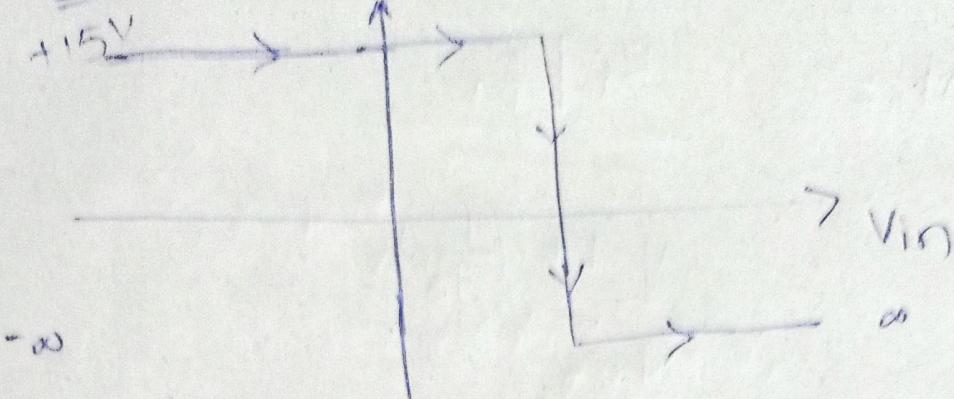
(iii) Time Marker :-

Schmitt Trigger:-

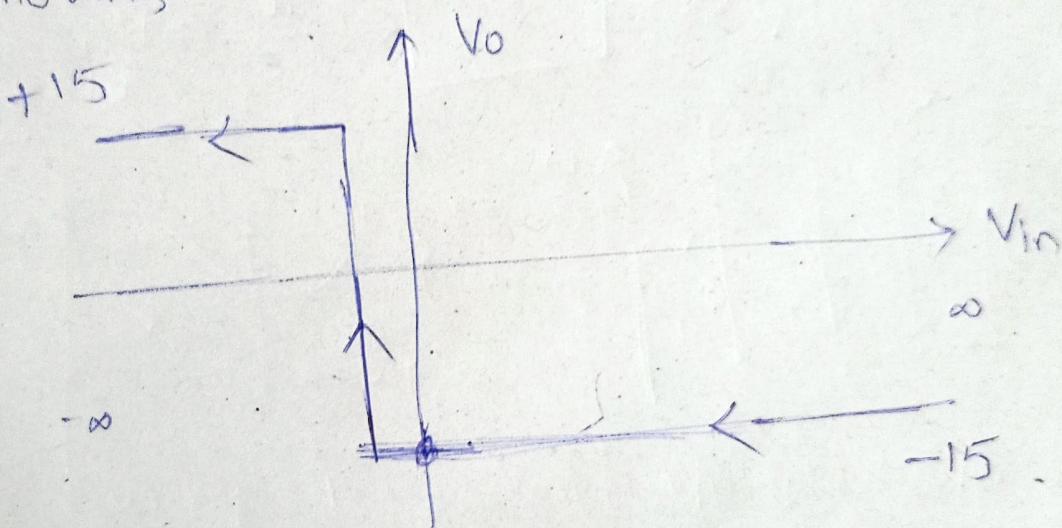
→ Comparator with Hysteresis

UTP :- is the I/P volt at which O/P makes transition from +V_{cc} to -V_{cc} as the I/P volt making forward dire

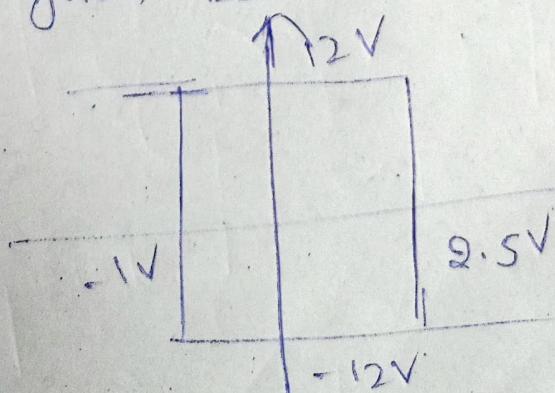
$\Rightarrow V_{TP}$



LTP is the i/p volt at which o/p volt crosses transition from $-V_{cc}$ to $+V_{cc}$ when o/p volt is moving reverse direction.



Design a Schmitt trigger by using the hysteresis given below.



$$V_{sat} = \pm 12$$

$$V_{UTh} = 2.5$$

$$V_L = 1V$$

$$A = 10 ; f = 10K$$

$$|A| = \frac{R_f / R_i}{\sqrt{1 + \left(\frac{f}{f_a}\right)^2}}$$

peak gain
or
3dB gain)

$$|A| = \frac{R_f / R_i}{\sqrt{1 + \left(\frac{f}{f_a}\right)^2}} = 10 \quad (\text{let } R_i = 10k)$$

$\boxed{R_f = 100k}$

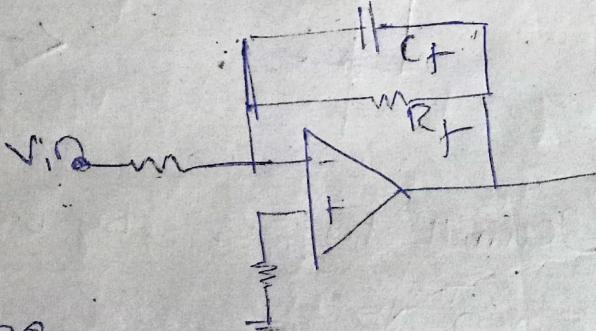
Let max freq. of integr. $f_b = 10\text{kHz}$

Corner freq. is f_a

$$\Rightarrow f_b = 10f_a$$

$$\Rightarrow f_a = 1\text{kHz}$$

corner freq. $f_a = \frac{1}{2\pi R_f C_f}$



$$R_f = 1.2M\Omega$$

$$R_i = 120k\Omega$$

$$C_f = 10nF$$

(ii) ~~R_f~~ Gain freq. $f_a = 10f_b$

$$f_b = \frac{1}{2\pi R_f C_f} = 13.26\text{ kHz}$$

$\boxed{f_a = 132.6\text{kHz}}$

(iii) $V_o = A \cdot V_{in}$

given $V_{in} = 5V$, & $f = 10\text{kHz}$

$$\Rightarrow A = \frac{R_f / R}{\sqrt{1 + (f/f_a)^2}}$$

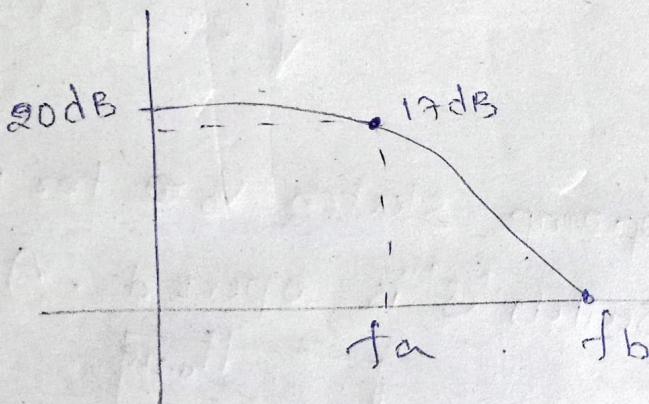
$$A = \frac{100/10}{\sqrt{1 + \left(\frac{10}{136.8}\right)^2}} = 0.01326$$

$$\Rightarrow V_o = 0.01326 \times 5 = 66.3 \text{ mV}$$

③ Sketch freqn response.

Given $R_i = 120 \text{ k}\Omega$, $R_f = 1.2 \text{ M}\Omega$, $G = 10^4$

$$|A| = 20 \log_{10} = 20$$



④ find R_i & R_f in lossy integrator so that

Peak gain is 20dB & the gain is 3dB from its peak $\omega = 10,000$; $C_f = 0.01 \mu\text{F}$

Ans / Given $20 \log |A| = 20 \log \frac{R_f}{R_i}$

Max gain $\left. \frac{dC}{d\omega} \right|_{\omega=20}$ $\Rightarrow 20 = 20 \log \frac{R_f}{R_i}$

$\Rightarrow \frac{R_f}{R_i} = 10$

$$f = \frac{\omega}{2\pi} = \frac{10,000}{2\pi}$$

8dB gain is ~~20~~ $20 - 3 = 17 \text{ dB}$

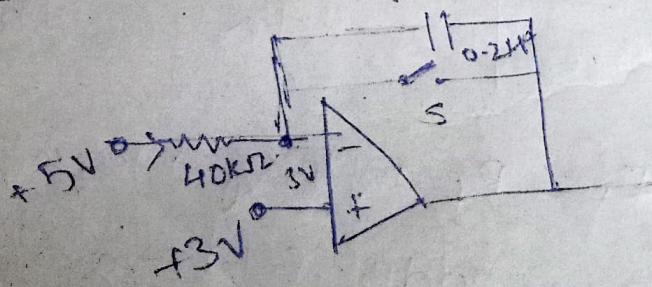
$$\Rightarrow 17 \text{ dB} = \frac{R_f/R_1}{\sqrt{1 + (f/f_a)^2}}$$

$$\Rightarrow \frac{17^2}{10^2} =$$

$$\Rightarrow 1 + (f/f_a)^2 = (10/7)^2 = \frac{100}{49} = \frac{189}{289}$$

$$\Rightarrow |A| = \frac{R_f/R_1}{\sqrt{(2\pi R_f C_f)^2 + 1}}$$

④ for opamp sketch V_o for 5msec after switch 'S' is opened.. Assume ideal



Ans

$$\frac{5-3V}{40 \times 10^3} = -\frac{1}{C_f R_f} \int v_i dt$$

$$\frac{1}{10^4} = -\frac{1}{1}$$

$$\frac{V_i - 3}{R_1} = C_f \frac{d}{dt} (V_o - V_0)$$

$$\Rightarrow \frac{2}{40K\Omega} = 0.2 \times 10^{-6} \frac{d}{dt} (3 - V_0)$$

$$\Rightarrow V_0 = \int \frac{2}{8 \times 10^{-5}} dt$$

$$V_0 = \frac{2}{8 \times 10^{-5}} \int_0^{50ms} dr$$

$$V_0 = \frac{2}{8 \times 10^{-5}} \cdot \frac{50 \times 10^{-3}}{2} = 12.5V$$

$$\boxed{V_0 = 12.5V}$$

Total output voltage

$$V_o = \int_0^{50} V_i + \left[V_{out} \right]_{t=0}$$

$$= -12.5 + 3 = -9.5V$$

$$\Rightarrow V_{out} = \frac{-1}{C_f R_1} \int_0^{t_1} (V_i - V_o) dr$$

$$\Rightarrow \int_0^{t_1} dr = \frac{-9.5 \times 8 \times 10^{-5}}{2}$$

$$\Rightarrow t_1 = 3.8 \times 10^{-3} = 3.8ms$$

