Mon deterministie Automate :-> Non-Determinism means a choice of mores for an automaton. Rather than Plescribing a unique more in each situation, we allow a set of Possible moves. Formally, we achieve this by defining the pargition function so that its sange is a set of Rossible

Destriction! - A nondeterministic finite automate or NFA in defined by the quadraple M=[B, E, S, 90, F), where Q, E, 40, Fare defined as for deterministic finite automate, but 8: Qx(EU(x))->2Q

Mote that There are There regor differences of this definition and the definition of a dea.

De In a mon deterministic altometa, The range of diss in The Conserge, so that its value is not a single element of Q. but a subset abit. This subset defines the set of all Possible states that can be leasted by The Transition. It for instance, The Current state is ano trie symbol a is lead, and 8(an, a) = 790,92},

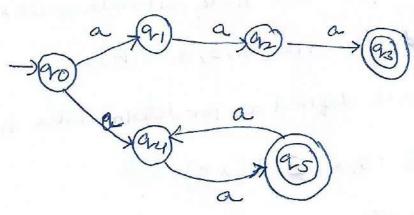
tren either to or 92 Could be the rest state of the nfa.

D) Also we allow I as the second argument of S. This Means that no fa can make a Transition without consuming an (3) Finally, in an NFA, The Set $\{ \{ \{ \{ \}_{i,j} \} \} \}$

no transition defined for this specified situation.

A String is accepted by an NFA if there is some sequence of Possible moves thatwill Put The Machine in a final state at the end of the String. A String is lejected (Treat is, not lessible accepted) only if There is no Possible sequence of moves by which a final state cause leaveled Ex!— Confider the Timestin

Ex! - Consider the Transition graph in figure, it describes a non deterministic automata since Trece are Two Transition



Ex! - Transition system for a rondeterministic autometin

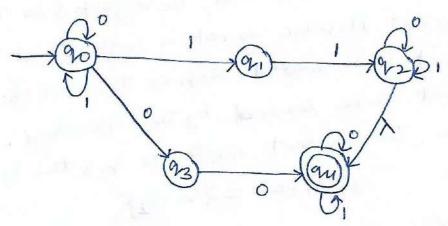
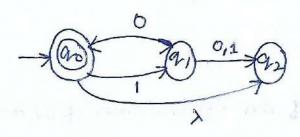


Fig: - NDA/NFA autometion with entry Hove

Example:- A Hondeterministie automaton is shown in figure. It is non deterministic not only because Several edges with the same label originate from one verter, but also because it has 1- Transition. some transitions, such as of (9210), are unspecified in the graph. This is to be interpreted as a Transition to the empty set, that is, & (22,0) = \$. The autome accepts strings >, 1010, and 101010, but not 110 and 10100. Note that for 10 there are two althoutive walks, one ladio to 9 the other to az. Even Though as is not a final state, The String in accepted because one walk leads to a final state



Finite state Machine (FSM) FA with OIP A-NFA NFA DFA

QX \(\su\{\lambda\right\} \righta_2\alpha\right\} \ \alpha \times \(\sim\{\lambda\right\} \righta_2\right\} \\ \alpha \times \(\sim\{\lambda\right\} \righta_2\right\} \\ \alpha \times \(\sim\{\lambda\right\} \righta_2\right\} \\ \alpha \times \(\sim\{\lambda\right\} \right\} \\ \alpha \times \(\sim\{\lambda\right\} \right\} \\ \alpha \times \\ \alpha \times \\ \alpha \times \\ \alpha \times \\ \al Mealy machine Moore Machine associated ontput with with states \rightarrow \bigcirc $^{\circ/1}$ ->(1)2°

- The equivalence of DFA and NDFA: we naturally Try to first the solution HW DFA and NDFA. Intuitively, we now seed theat:
- (i) A DFA can simulate the behaviour of MDFA by increasing the number of states. (In other woods, a DFA ($\alpha, \xi, \delta, q_0, F$) canbe viewed as an NDFA ($\alpha, \xi, \delta', q_0, F$) by defining $\delta'(q, \alpha) = \{\delta(q, \alpha)\}.$)
 - (ii) Any NDFA is a Mose General machine without being Mose Powerful.

* we row give a Theosen of on equivalence of DFA and NDFA.

Theosem:
For every NDFA. There exists a DFA which

Simulates The behaviour of NDFA. Alternatively, if L is

The ser accepted by NDFA, Then There exists DFA which

accepts L.

Proof! - let M= (B, Z, S, 90, F) be an NDFA accepting L.
We construct a DFA M' as:

M'= (Q', E, S, 90, F')

Lar, 92, - 2i) any state in Q' is denoted by

- (i) % = (20) and
- (11) F' is The set all sussets of a Contain an element of F.

(S) (S) $(S(a_3,a_1), ---a_i, a_i) = S(a_1,a_1) \cup S(a_2,a_1)$ $\cup S(a_3,a_1) \cup ---- \cup S(a_i,a_1)$.

Equivalently,

If and only if
$$S(\{a_1, --a_i\}, a) = \{P_1, P_2 --P_i\}$$

to the state of

Example! - Construct a delerministic autometers equipments $M = (\{90,91\}, \{0,1\}, \delta, 90, \{90\})$

where S is defined by its state table (a)

2)	State/2	0	
	->(90)	go	91
	op.	9-1	(2012)

Solution! - for The deterministic automators M,

(i) The states are subset of [20, 21], i.e, \$, [20],(21), [20],(21);

- (i) [90) is the initial state;
- (11) [90) and [90, 91] are the Biral states as there are the only states contains 90; and
- (1) Sin defined by the state table sien by Table and a.

Table! - State table of M, For example

Arte/Z	0	1
ϕ	ø	ø
[90]	[20]	Carj
Lanj	[21]	[90,91]
[90,91]	[90,91]	[20,2,]

The states go and on appear in the rows Corresponding to go and on and the column corresponding to o.

108/a so, 8 ([90,4,],0) = (90,91].

beken M has n states, The corresponding finite automator has in states. Has ever, we need not Consmut of for all These in States, but only For Those states that are leachable from [90].

This is secured on interst is only in construction MI accepting T(H). 80, noe start the construction of 8 for [90]. We continue by considering only the states appearing certifier under the 11P columns and Constructing 8 for such states. we halt when to more than states appear under The Injust Columns.

Example: hiel a deterministic acceptor equivalent to M= (120, an, any, {a, b}, 8, ao, {any) were S is given by table given below State / 90,91 good 1 The delerministic automation M, Equivalent to

H is defined as follows:

MI= (20, 20, 5, [20], F')

where

F= [[92], [90,92], [91,92], [90,9,12]

nee start The Construction by considering [90] first, we get (an) and [40,94]. Then we construct & Fur[2] and [90,91]. [ar, ,92] is a real state appears unde

the input columns. Ablir consmety Sfor Carilles)

we donot get any new states and to we tearninate the Consmittings. The state passe in sienty

Table! - State table of MI for about ex.

State 12	0	b
Caro	[aoias]	L92]
[az]	\$	[20121]
[90,91]	[207	[90,9,]

Ex! - Construct a deterministic Brite automation

equivalent to

M= ({90,00,02,92,934, } 2153, 8, 90, 993})

Losee 8 is given by table tolloip

Table 1- State talk

state /=	· a	ь
> 90	90,91	Re
cu,	a_	an
012	93	93
93		02

18-1"- let 8 = {ao, an, an, as} then the DFA M, equiveleisto M is 8 iren by M1 = (28, {a16}, 8, [90], F)

Where F consists of:

[03], [00,92], [0,93], [22,93], [20,94,23], [0,192,93], [0,192,93] and [90,94,22,93] and better & in defined by Sinen state take ford, Table: - State table for MI

State/ $[a_0]$ [ao, 91] [ao]

[ao, 91] [ao, 91, 92] [ao, 91, 92]

[ano, 91, 92] [ao, 91, 92] [ao, 91, 92]

[ao, 91, 92, 93] [ao, 91, 92] [ao, 91, 92]

[ao, 91, 92, 93] [ao, 91, 92, 93]

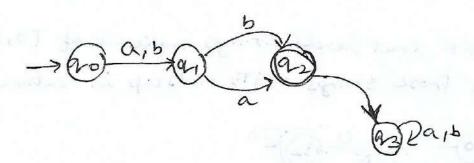
Some question on DFA



a. Consmut a DFA, that accepts set afall string over Z= {a,b} af length 2

Soln!-

L= Jaa, ab, ba, bb}



L for if abb

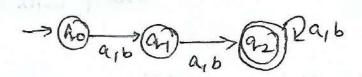
or aba

case occurre

A. Construct a DFA, That accept set of all strings over Z={a13} hatere length is atleast 2.

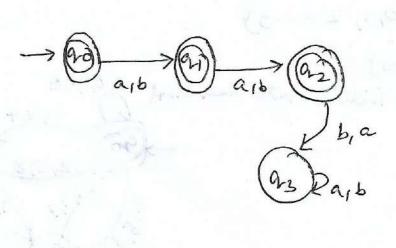
24 Ji-

L= 200 pb, ba, bb, aaa, aab, --- 3



Z= gaib3, 1W/52

801ⁿ!-L=jë,a,b,aa,ab,ba,bb}

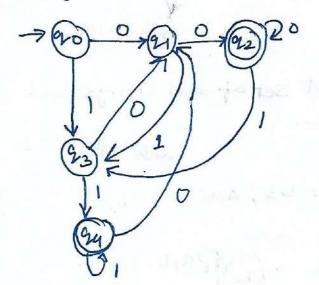


* ILE is The Part of The lang then always makes initial state as final state

->
$$O^{20}$$
 L $O^{21/0}$

where $\Sigma = \{0,1\}$ => $O^{*1}(0+1)$ *

* Design a DFA treat leads Strings made up at [0,13 and accept only those Strings waits ends up in either over 11.



Here the FA has two different. "
Sinal states on and on.
92 state accepts 3 mig ending with 11.

* Construct a DFA that accepts the set of natural numbers it which are divisible by 3.

801":- Let $M = \{8, \xi, 90, \delta, F\}$ be a DFA with $S = \{90, 91, 92\}$ $\Sigma = \{0, 1, 2 - --9\}$ $F = \{90\}$

i.e. here to its initial state and hirst State also.

0,36,9 1,4,7 0,3,6,9 1,4,7 2,5,8 1,4,7 2,5,8