# DRL para controle de um levitador magnético

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### Ponto de Partida

#### Deep Reinforcement Learning for Process Control: A Primer for Beginners

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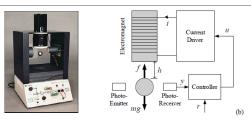
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#### Abstract

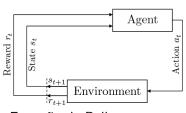
(a)

Advanced model-based controllers are well established in process industries. However, such controllers require regular maintenance to maintain acceptable performance. It is a common practice to monitor controller performance continuously and to initiate a remedial model re-identification procedure in the event of performance degradation. Such procedures are typically complicated and resource-intensive, and they often cause costly interruptions to normal operations. In this paper, we exploit recent developments in reinforcement learning and deep learning to develop a novel adaptive, model-free controller for general discrete-time processes. The DRI controller we propose is a data-based controller that learns the control policy in real time by merely interacting with the process. The effectiveness and benefits of the DRI, 'controller are demonstrated through many simulations.

Keywords: process control; model-free learning; reinforcement learning; deep learning; actor-critic networks



## Reinforcement Learning



Equação de Bellman:

$$R_t = \sum_{i=t}^{T} \gamma^{(i-t)} r(s_i, a_i)$$
 $J = \mathbb{E}_{s_i, a_i \sim \pi}[R_1]$ 

Política:  $\pi$  (ou  $\mu$  quando determinística).

$$Q^{\mu}(s_t, a_t) = \mathbb{E}_{r_t, s_{t+1} \sim E}[r(s_t, a_t) + \gamma Q^{\mu}(s_{t+1}, \mu(s_{t+1}))]$$

Onde, usualmente  $\mu = argmax_aQ(s_t, a_t)$ 

Ideia chave: construir um estimador para Q, com parâmetros  $\theta$  A perda é dada por:

$$L(\theta^{Q}) = \mathbb{E}[(r + \gamma \operatorname{argmax}_{a} Q(s_{t+1}, a_{t+1}) | \theta - Q(s_{t}, a_{t}) | \theta)^{2}]$$





#### Inovações principais:

Target network:

$$L(\theta^{Q}) = \mathbb{E}[(r + \gamma \operatorname{argmax}_{a} Q_{tgt}(s_{t+1}, a_{t+1}) | \theta - Q(s_{t}, a_{t}) | \theta)^{2}]$$

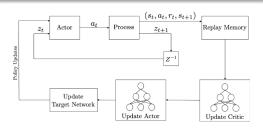
 Memory Buffer: Armazenamento e amostragem de transições.
 Amostra vai ser mais descorrelacionada e promove um aprendizado melhor do que o as amostras consecutivas.

## **DDPG**

- Usa as técnicas do DQN para implementar a atualização da rede Q
- Atualização contínua com uma média:  $\theta_{tet} \leftarrow \tau \theta + (1 \tau)\theta_{tet}$  com  $\tau << 1$
- Emprega a normalização dos valores
- Ator crítico: Uma rede para gerar as ações e outra para realizar a estimativa do Q
- Aprendizado pelo gradiente descendente de J a partir de valores de Q para atualizar  $\pi$ .
- Ações contínuas!



#### DRL Controller

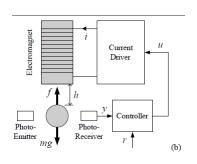


- Baseado no DDPG
- Utiliza uma técnica de gradient clip
- Adiciona a variável de referência no algoritmo
- Relaciona as abordagens dos problemas:

$$a_t=f^{-1}(u_t)$$
  $s_t=< y_t,y_{t-1},...y_{t-d},a_t,a_{t-1},...,a_{t-d},(y_t-y_{sp})> r_t=-|y_t-y_{sp}|$ , ou outra que se adapte ao problema, em função de  $y_t$  e  $y_{sp}$ .



## A planta estudada



$$f = K \frac{i^2}{h^2}$$

$$m \frac{d^2 h}{dt^2} = mg - K \frac{i^2}{h^2}$$

$$y = \gamma h + y_0, y \in (-2V, 2V)$$

$$i = \rho u + i_0, u \in (-3V, 5V)$$

$$\frac{d^2y}{dt^2} = \gamma g - \frac{K(\rho u + i_0)^2 \gamma^3}{m(y - y_0)^2}$$

$$\dot{x_1} = x_2 \dot{x_2} = \gamma g - \frac{K(\rho u + i_0)^2 \gamma^3}{m(y - y_0)^2}$$



## Resultado na Planta Proposta

$$s_t = <(y_t - ref), y_t, dy_t, u_t>$$
 $u_t = u_{t-1} + a_t$ 
 $ref o Const$ 

$$ref \in (-0.5, 0.5), run-by-run$$

$$rwd = -\exp(-e^2/0.05)$$

Erros quadráticos médios (0.0133):

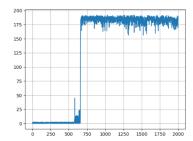
0.0256,

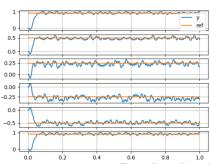
0.0090,

0.0037,

0.0053,

0.0103.





## Resultado na Planta Proposta

$$rwd = -\exp(-e^2/0.05)-0.75\Delta u^2$$

Erros quadráticos médios (0.0152):

0.0308,

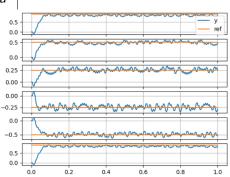
0.0095.

0.0042,

0.0044,

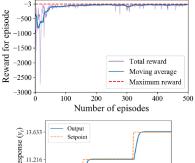
0.0111,

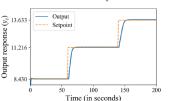
0.0308

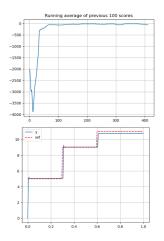


## Reprodução do Resultado Original

$$G(z) = \frac{0.05z^{-1}}{1 - 0.6z^{-1}}$$







## Conclusão

- As funções de recompensa apresentadas no artigo original não tratam bem problemas instáveis. A instabilidade gera o "morte prematura" do agente caso não hajam recompensas positivas para incrementos do número de passos dados.
- Apesar da solução funcionar bem nas plantas apresentadas no artigo original, houve dificuldade do emprego da técnica em uma planta instável.