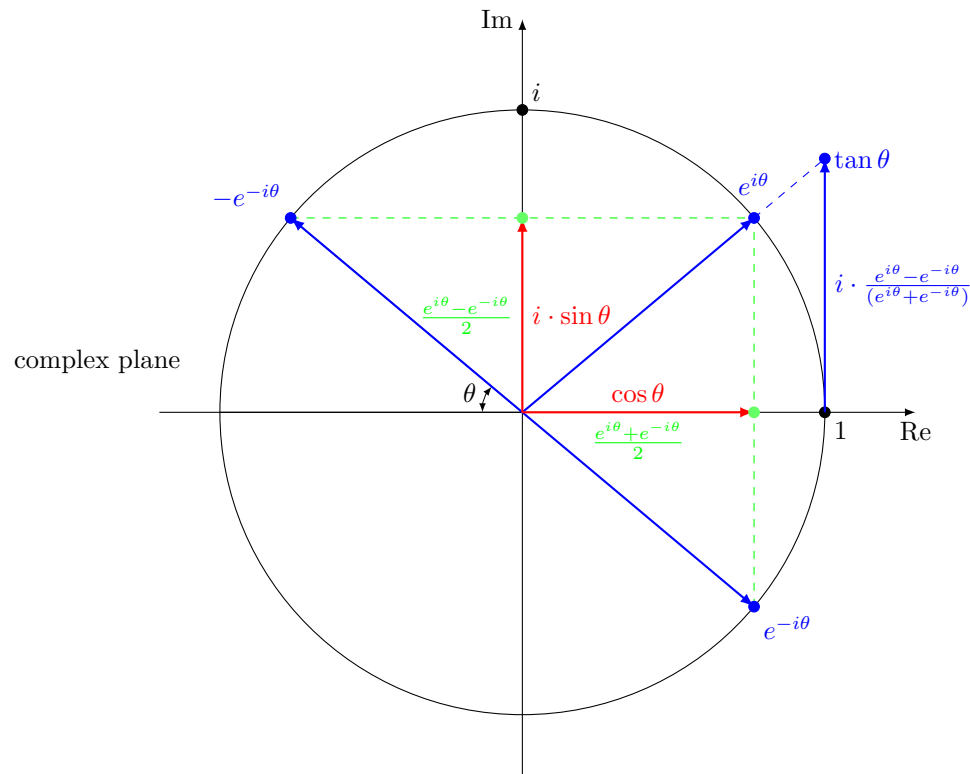


Relationship between sine, cosine, tangent and exponential function



$$e^{i\theta} = \cos \theta + i \cdot \sin \theta,$$

$$e^{-i\theta} = \cos(-\theta) + i \cdot \sin(-\theta) = \cos \theta - i \cdot \sin \theta.$$

$$\cos \theta = \operatorname{Re} (e^{i\theta}) = \frac{e^{i\theta} + e^{-i\theta}}{2},$$

$$\sin \theta = \operatorname{Im} (e^{i\theta}) = \frac{e^{i\theta} - e^{-i\theta}}{2i}.$$

$$\cos i\theta = \frac{e^{-\theta} + e^{\theta}}{2} = \cosh \theta,$$

$$\sin i\theta = \frac{e^{-\theta} - e^{\theta}}{2i} = \frac{e^{\theta} - e^{-\theta}}{2} \cdot i = i \cdot \sinh \theta.$$

$$\tan \theta = \frac{e^{i\theta} - e^{-i\theta}}{i(e^{i\theta} + e^{-i\theta})},$$

$$\tanh \theta = \frac{e^{\theta} - e^{-\theta}}{e^{\theta} + e^{-\theta}}.$$