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IMPORTANT SECURITY PROPERTIES



Confidentiality

No one else, except sender and receiver should understand the messages exchanged (encryption)



Authentication

Sender and receiver should confirm the identity of one another



Message Integrity

Sender and receiver want messages exchanged to be unaltered in transit. Altered messages should be detected.



Availability

Communication link between sender and receiver should be available



Access

Communication link between sender and receiver should be accessible

POSSIBLE SECURITY ATTACKS



Eavesdrop — Intercept messages



Alter messages — Actively insert messages into connection



Impersonate — Fake (**spoof**) source address in packet or any part of the packet



Denial of Service — Prevent service from being used by others



Hijack — Take over ongoing connection by removing sender or receiver unknowingly to either party

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CRYPTOGRAPHY

Protects **confidentiality**, hence **preventing** attackers from **eavesdropping**

H O W ?

plaintext:	abcdefghijklmnopqrstuvwxyz
	↓ ↓
ciphertext:	mnbvcxzasdfghjklpoiuytrewq

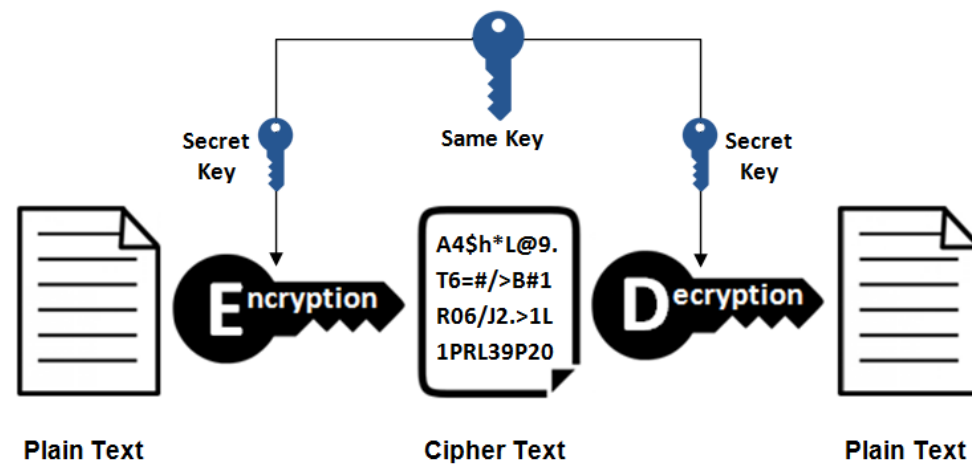
Naive attempt: Substitution Cipher

Mapping from a set of 26 letters to another set of 26 letters

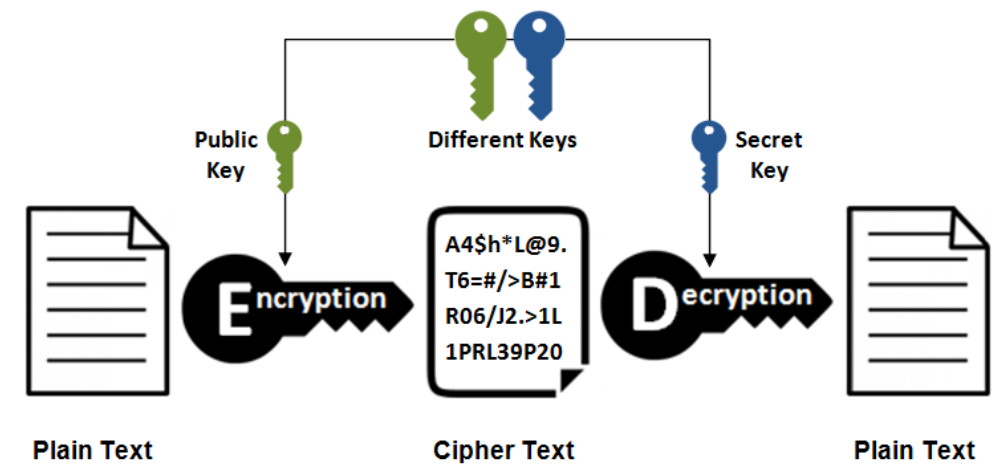
Disadvantage: the frequencies of the letters are not masked at all

CRYPTOGRAPHY

Protects **confidentiality**, hence
preventing attackers from **eavesdropping**
There's two good methods to encrypt and decrypt plaintext



Symmetric Key



Asymmetric Key

• SYMMETRIC KEY CRYPTO

encryption and decryption both uses the **same** key

Data Encryption Standard (DES):

- An algorithm to perform symmetric key cryptography
- 56-bit symmetric key
- 64-bit plaintext input (padding may be needed)
- 16 rounds of encryption to produce 64-bit encrypted output
- It was US encryption standard in 1993
- Can be decrypted using brute force in less than a day
- 3-DES to make it *more secure*

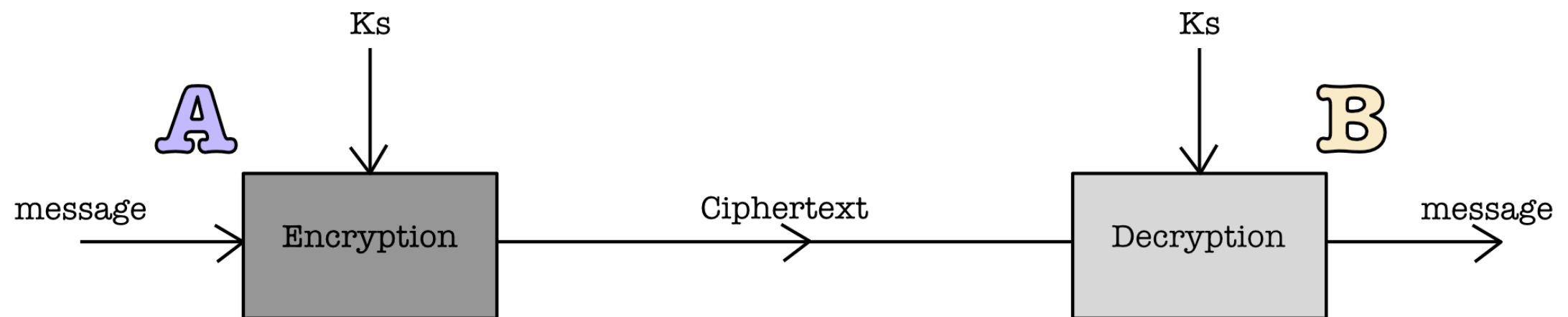
Advanced Encryption Standard (AES):

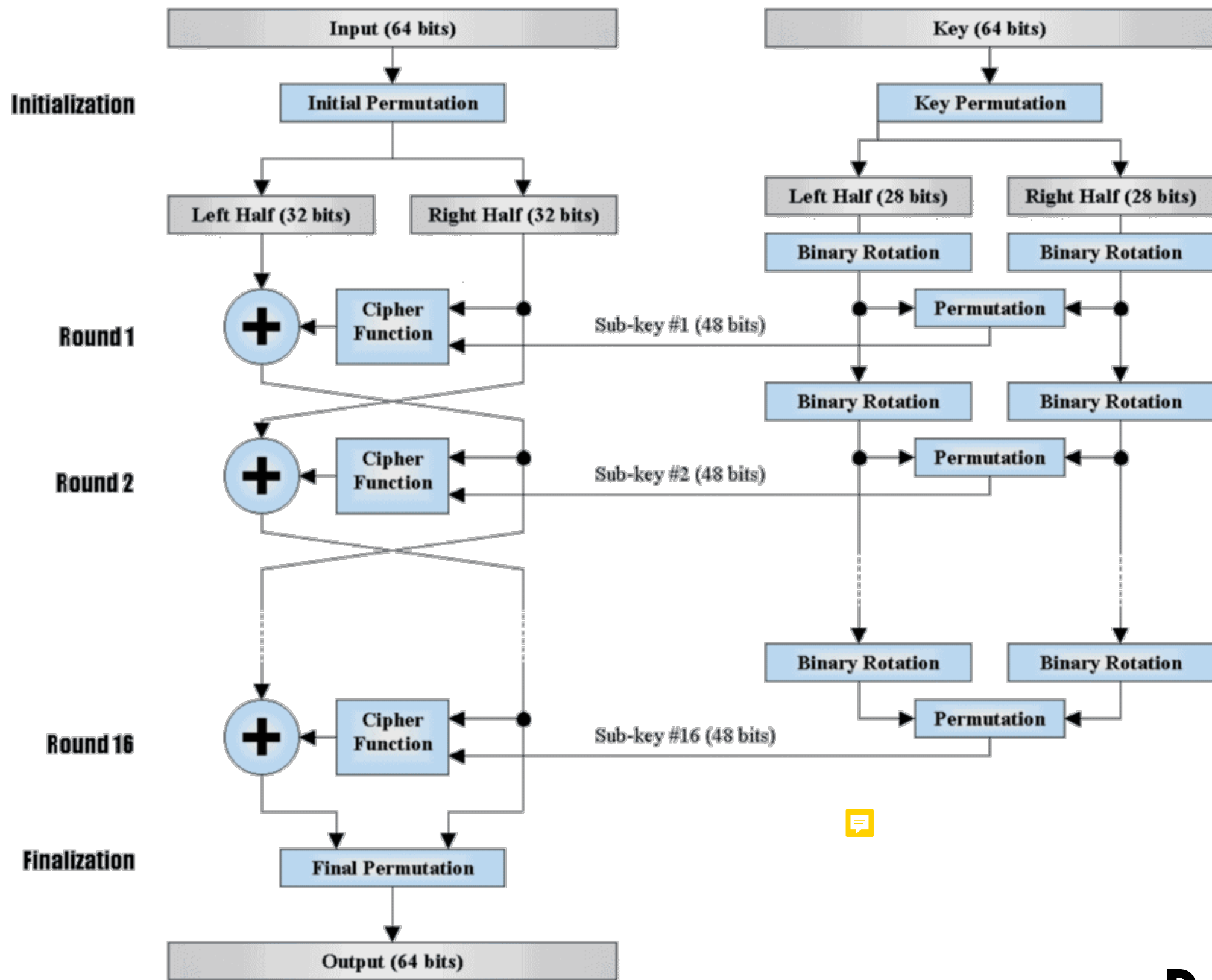
- A better algorithm to perform symmetric key cryptography
- 128, 192, or 256-bit symmetric key
- 128-bit plaintext input (padding may be needed)
- 10,12,14 rounds of encryption to produce 128-bit encrypted output
- Replaced DES in 2001,
- If 128-bit key is used, brute force decryption will take 1 billion *billion* years (yes, double billions right there), with a supercomputer

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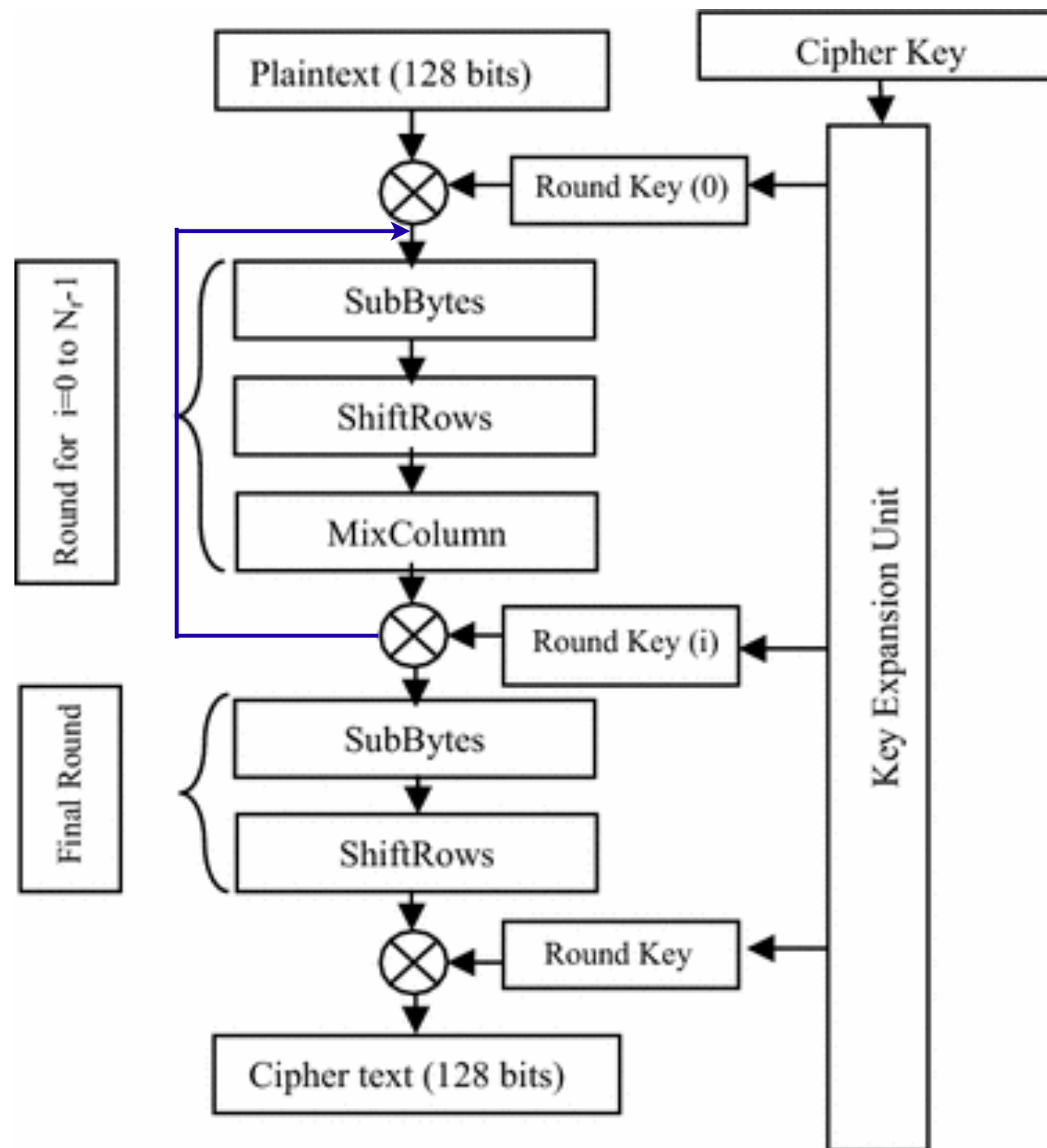
SYMMETRIC KEY CRYPTO

encryption and decryption both uses the **same** key





DES



A E S

• P U B L I C K E Y C R Y P T O

a.k.a **asymmetric** key cryptography

Rivest-Shamir-Adleman (RSA) algorithm (1977):

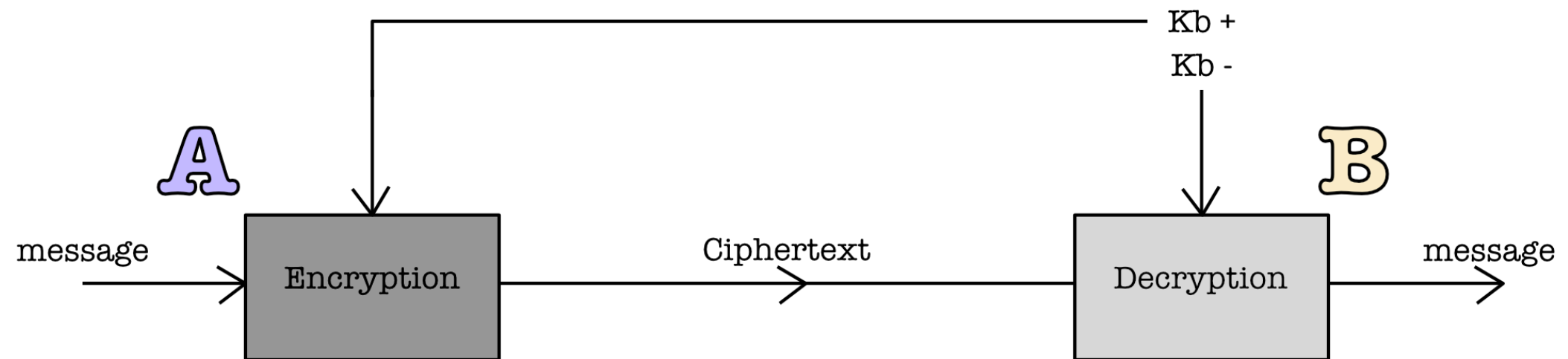
- Sender, receiver, do **not** share secret key
- **Public** encryption key **known to all**
- **Private** decryption key known only to receiver
- 1024 - 4096-bit asymmetric (public-private) key pair
- 1 round of encryption
- Input/output size: depends on key size

Two **important** requirements:

- Given **public** key, it is **impossible** to compute the private key
- Need a public-private key pair such that,
 - $\text{public}(m) = \text{encrypted message}$ ----- **encryption**
 - $\text{private}(\text{encrypted message}) = m$ ----- **decryption**

PUBLIC KEY CRYPTO

a.k.a **asymmetric** key cryptography



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R S A M A T H

Before that, some quick **modular arithmetic**

$$[(a \bmod n) \pm (b \bmod n)] \bmod n = (a \pm b) \bmod n$$

$$[(a \bmod n) * (b \bmod n)] \bmod n = (a * b) \bmod n$$

$$[(a \bmod n)^d] \bmod n = a^d \bmod n$$

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R S A M A T H

...and some quick message-to-number translation:

- Computer translates between bit patterns to the character you can see on screen, e.g using **UTF-8 encoding**
- You can represent a message by a
- integer number (simple binary to dec translation)
- Thus **encrypting a message is equivalent to encrypting a number**

Dec	Symbol	Binary	Dec	Symbol	Binary
65	A	0100 0001	83	S	0101 0011
66	B	0100 0010	84	T	0101 0100
67	C	0100 0011	85	U	0101 0101
68	D	0100 0100	86	V	0101 0110
69	E	0100 0101	87	W	0101 0111
70	F	0100 0110	88	X	0101 1000
71	G	0100 0111	89	Y	0101 1001
72	H	0100 1000	90	Z	0101 1010
73	I	0100 1001	91	[0101 1011
74	J	0100 1010	92	\	0101 1100
75	K	0100 1011	93]	0101 1101
76	L	0100 1100	94	^	0101 1110
77	M	0100 1101	95	_	0101 1111
78	N	0100 1110	96	`	0110 0000
79	O	0100 1111	97	a	0110 0001
80	P	0101 0000	98	b	0110 0010
81	Q	0101 0001	99	c	0110 0011
82	R	0101 0010	100	d	0110 0100

• RSA MATH

The RSA algorithm

1. Choose 2 large **prime** number : p & q (1024 bits each)

2. Compute:

$$n = pq, z = (p - 1)(q - 1)$$

relatively prime: dont share
common divisor except 1

eg 9 and 16

but 11 and 22 are not

3. Choose e, where $e < n$, and e,z are relatively prime to one another

4. Choose d, where $(ed-1) \bmod z = 0$

5. **Public key, is (n,e):**

$$c = m^e \bmod n \longrightarrow$$

m = message

(unencrypted), where

m must be < n

c = encrypted

message



6. **Private key, is (n,d):**

$$m = c^d \bmod n$$

7. An important property:

$$\text{if } k = m^d \bmod n,$$

$$k^e \bmod n = m = c^d \bmod n$$

$$x^y \bmod n = x^{(y \bmod z)} \bmod n \text{ for any } x, y$$

• R S A M A T H

The RSA algorithm: example

(note this is an example, so we choose small numbers for ease of calculation.)

1. Choose 2 large **prime** number : $p=5$ & $q=7$

2. Compute:

$$n = 5 * 7 = 35, z = (5 - 1)(7 - 1) = 24$$

3. Choose $e = 5$, where $e < n$, and e, z are relatively prime to one another

4. Choose $d = 29$, where $(ed-1) \bmod z = 0$

5. **Public key, is (n,e) :**

$$c = 12^5 \bmod 35 = 17$$

$m = 00001100$ (this is 12)

$c = 00010001$ (this is 17)

6. **Private key, is (n,d) :**

$$m = 17^{29} \bmod 35 = 12$$

7. An important property:

$$\text{if } k = m^d \bmod n,$$

$$k^e \bmod n = m = c^d \bmod n$$

$$x^y \bmod n = x^{(y \bmod z)} \bmod n \text{ for any } x, y$$

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R S A M A T H

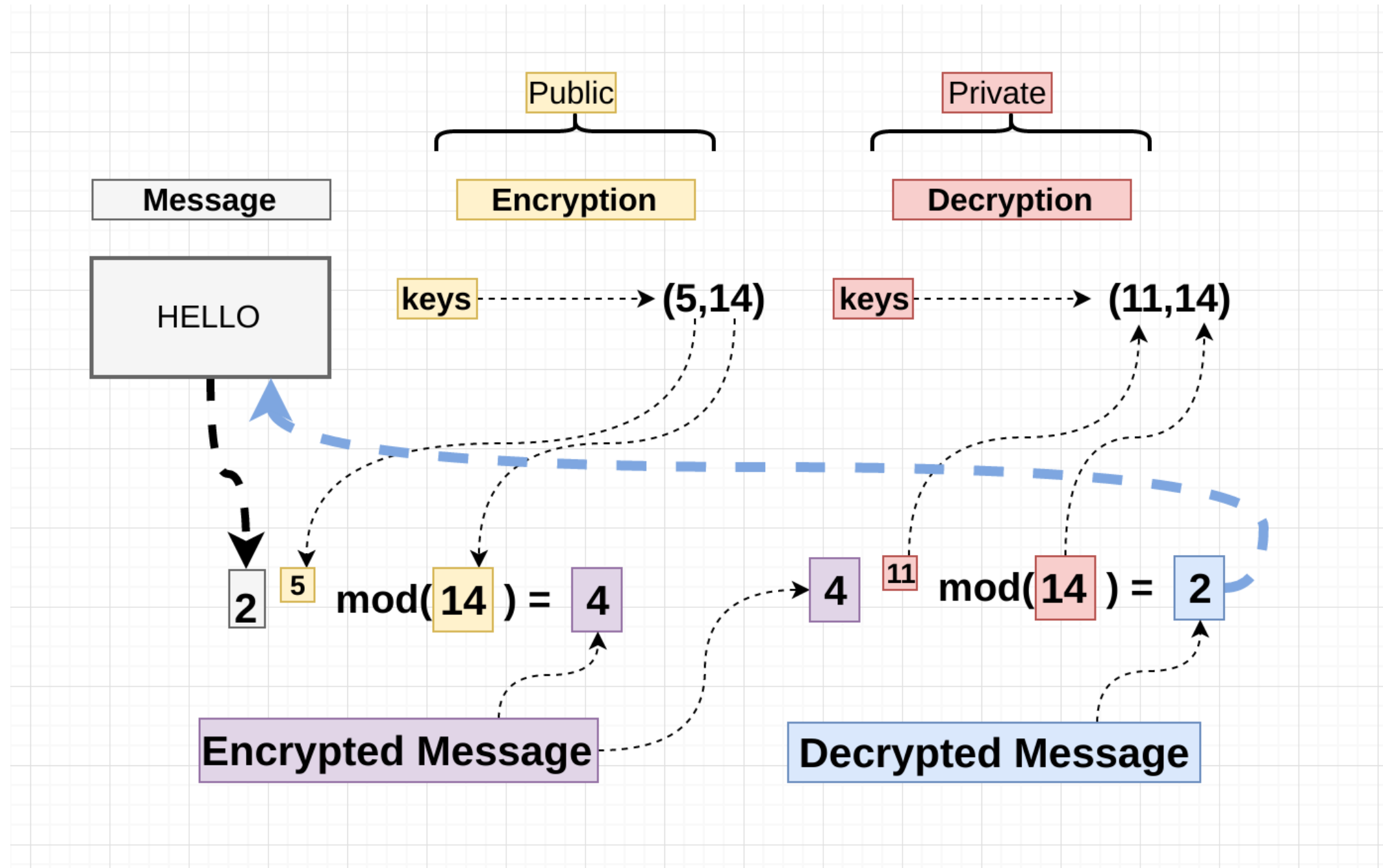
The RSA algorithm: proof

$$\begin{aligned}c &= m^e \mod n \\c^d \mod n &= (m^e \mod n)^d \mod n \\&= m^{ed} \mod n \\&= m^{(ed \mod z)} \mod n \\&= m^1 \mod n \text{ ----- Since } m < n\end{aligned}$$

$$x^y \mod n = x^{(y \mod z)} \mod n \text{ for any } x, y$$

R S A M A T H

The RSA algorithm: another example



• HOW SECURE IS RSA?

Very, very **secure** (1024 bit key above),
unless someone comes up with scalable quantum computers.

- Public key (n, e) is known to everybody. Private key (n, d) is only known to receiver
 - **Essentially, need to guess the value of d**
 - e is known and d is related to e : $(ed-1) \bmod \mathbf{z} = 0$
 - To find z, one has to know **p** and **q**
 - p and q is related to n : $n = p * q$
 - Hence, one has to be able to **perform prime factorization** of n to know p and q
 - If n is sufficiently large, e.g: 1024 bits, it is hard to find the correct prime factors of n (exponential complexity).
 - **To crack a simple 128-bit key, a supercomputer requires $\sim 10^{(39)}$ seconds.** The universe is younger than that.
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- The prime factorization problem falls under **NP**
 - Note: with *possible scalable quantum computing*, Shor's algorithm can solve prime factorisation in polynomial time.

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HOW PRACTICAL IS RSA?

Exponentiation in RSA is **computationally exhaustive**.

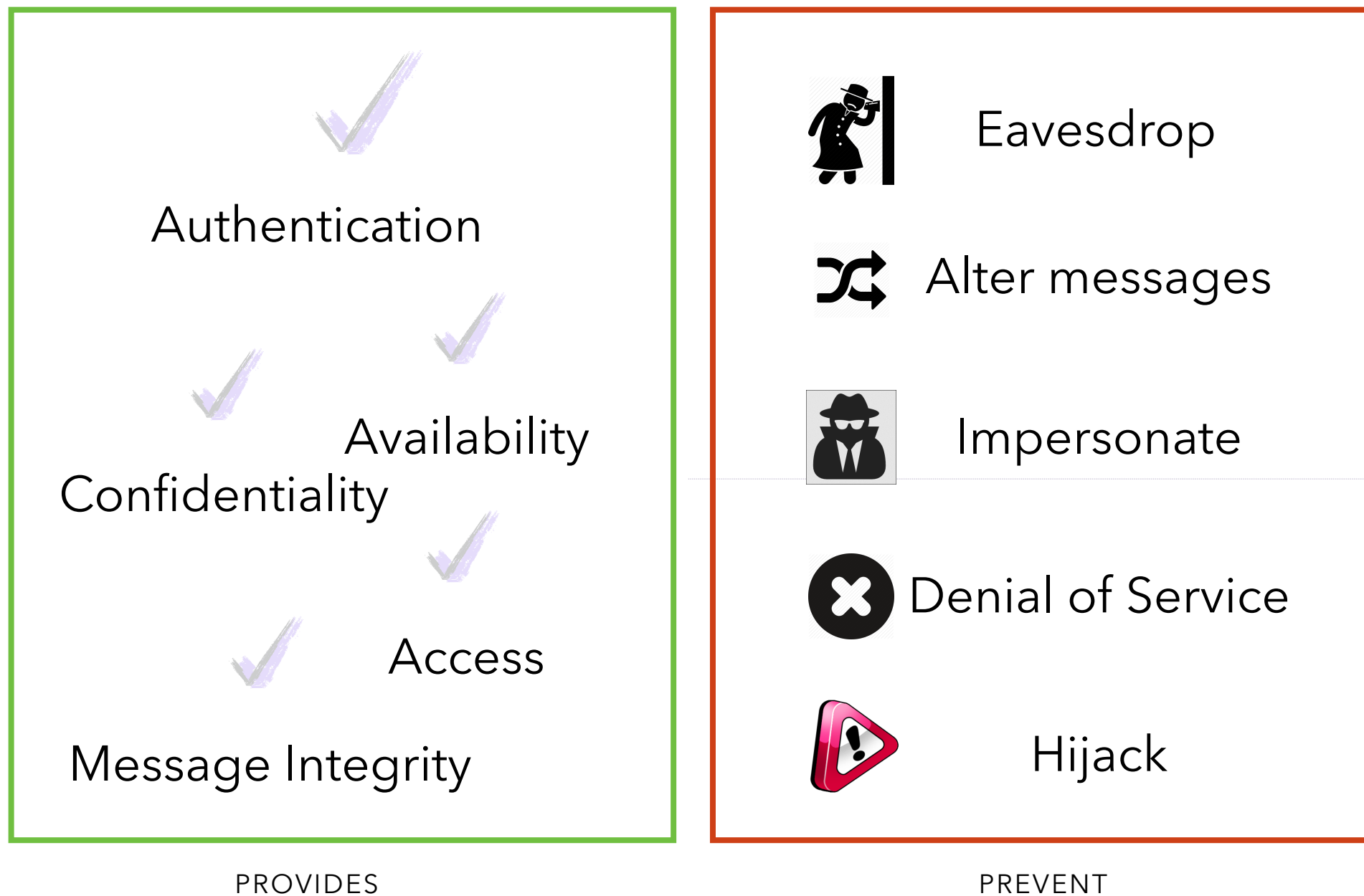
DES is 100x faster than RSA

- **USE SESSION KEY:**

1. Use public-key cryptography to establish a secure connection, meaning that we know for sure who the host at the end of the network line is
2. Generate **symmetric session key** and exchange between sender and receiver
3. **Use this symmetric session key** (instead of the public key) for lots of subsequent communications throughout the session

APPLICATION OF CRYPTOGRAPHY

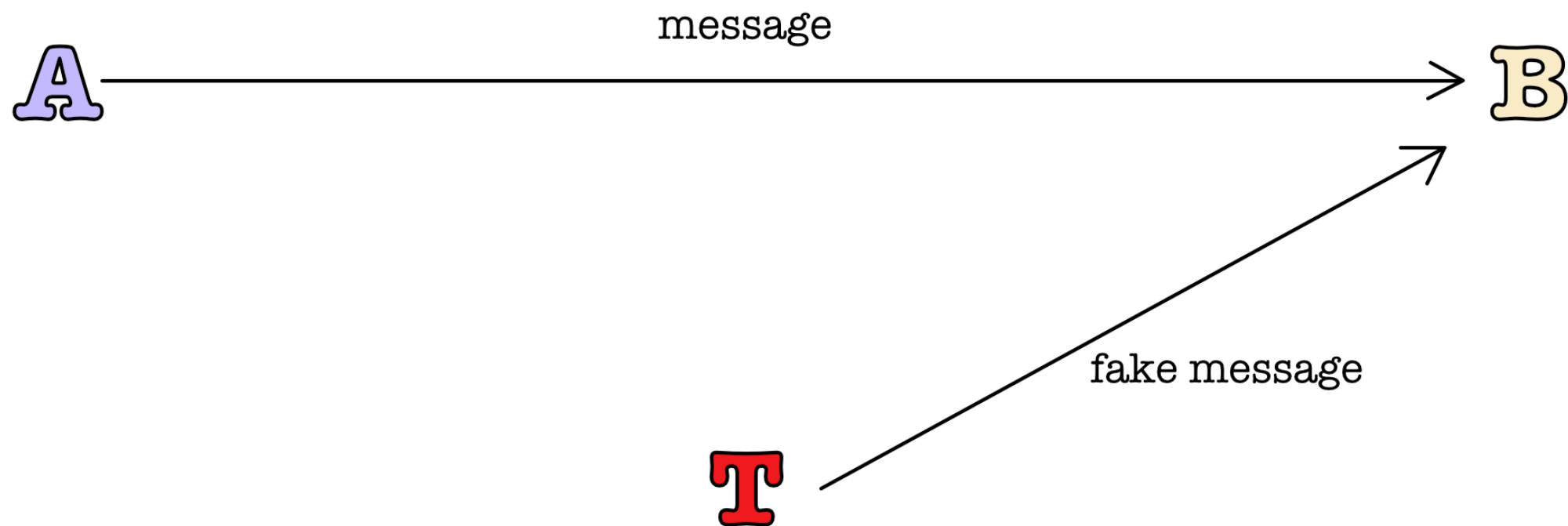
What kind of security properties can it give? And how does it defend against the attacks?



1. PROVIDING AUTHENTICATION

Need: **prevent impersonation**

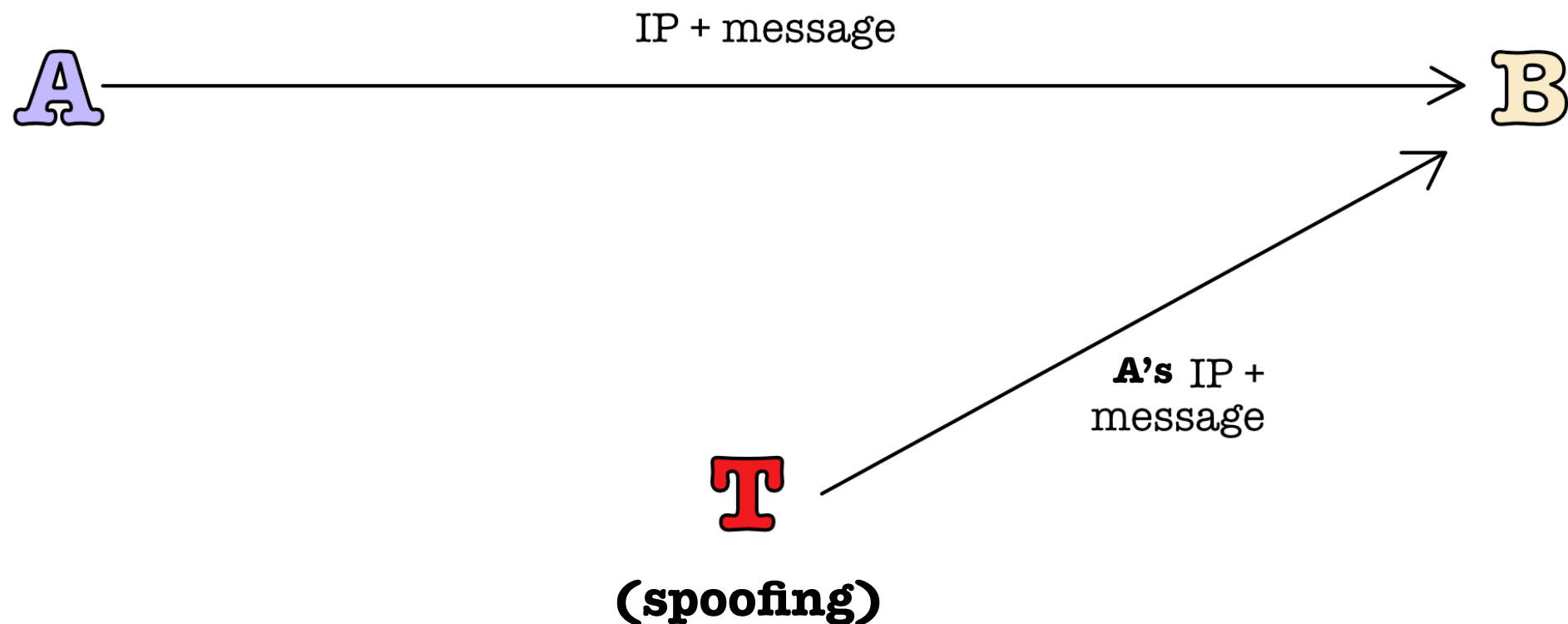
Lets consider this case without encryption first:



Without any encryption, B doesn't know who is the "real" A

1. PROVIDING AUTHENTICATION

Need: **prevent impersonation and spoofing**
Let's consider this case without encryption first:

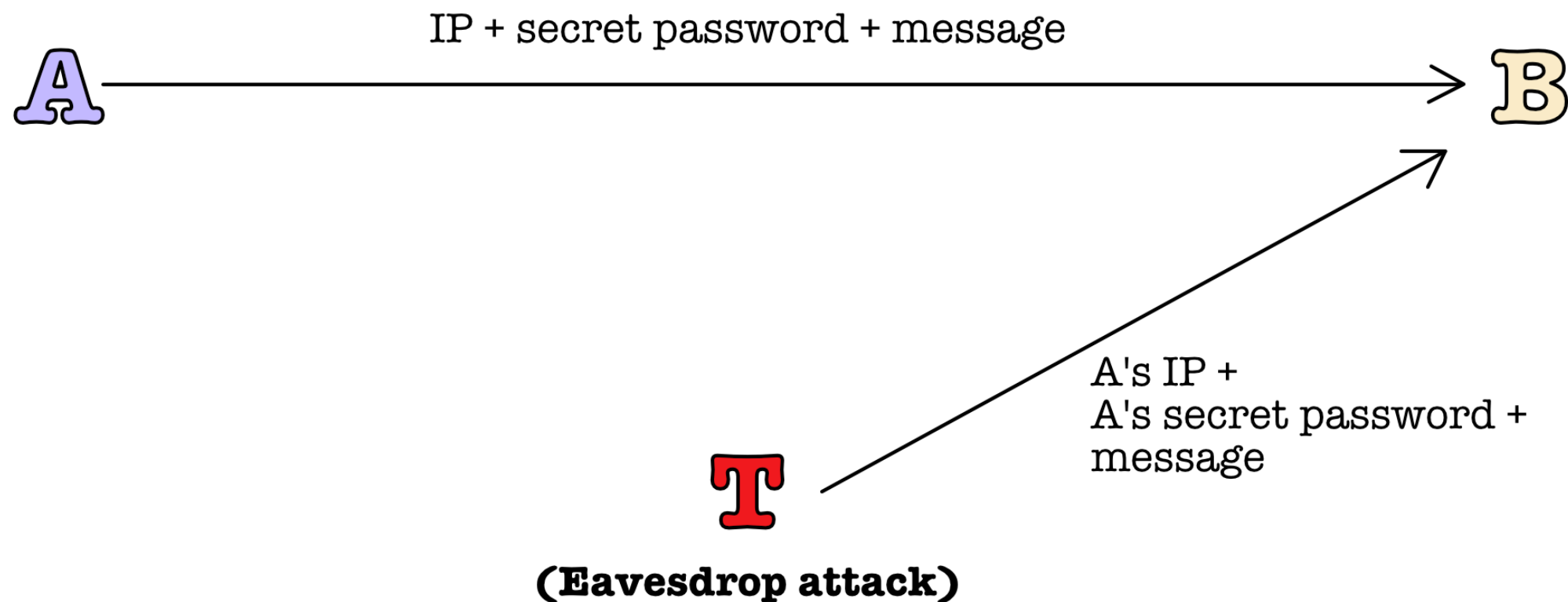


Without any encryption, B doesn't know who is the "real" A, even with IP address (IP is always changing depending on your network)

1. PROVIDING AUTHENTICATION

Need: **prevent impersonation, spoofing, and eavesdropping**

Lets consider this case without encryption first:

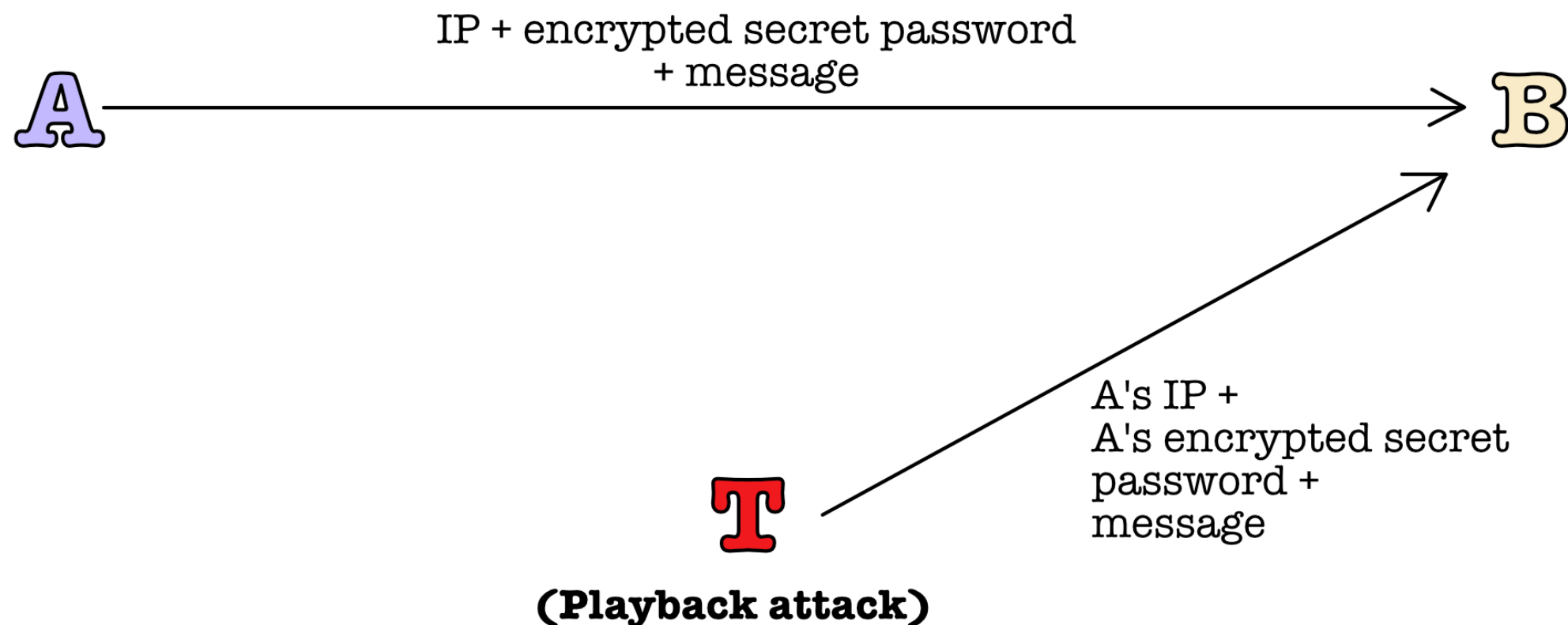


Without any encryption, B doesn't know who is the "real" A, even with IP address (IP is always changing depending on your network), and **nothing is secret in the internet**

1. PROVIDING AUTHENTICATION

Need: **prevent impersonation, spoofing, eavesdropping, and playback**

Some encryption is used here, but not enough



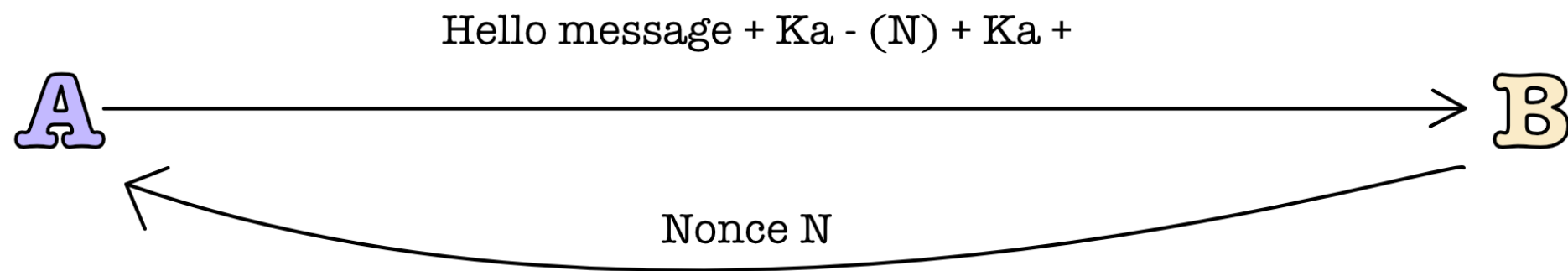
T can still just record and playback the "encrypted secret password". B cannot tell if its really A or T who is sending this.

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1. PROVIDING AUTHENTICATION

Need: **prevent impersonation, spoofing, eavesdropping, and playback**

Attempt 1: Lets use encryption and nonce



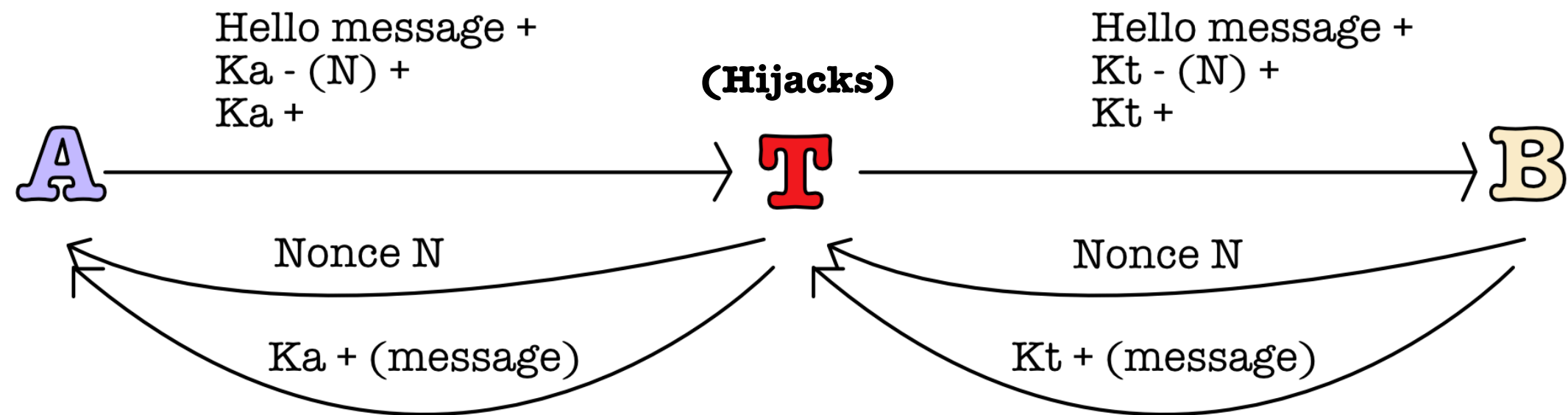
Encrypting message with private key is called **digital signature**

1. PROVIDING AUTHENTICATION

Need: **prevent impersonation, spoofing, eavesdropping, playback, and man in the middle attack**

Attempt 1: Lets use encryption and nonce

Failed by man-in-the-middle attack



1. PROVIDING AUTHENTICATION

Need: **prevent impersonation, spoofing, eavesdropping, playback, and man in the middle attack**

Attempt 1: Lets use encryption and nonce

Result: Failed by man-in-the-middle attack

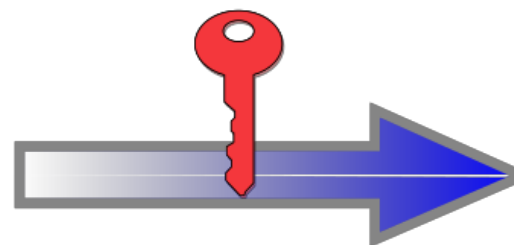
The loophole: B doesn't know whether A's public key he received indeed belongs to A

Solution: You need an **external party (called Certificate Authority: CA)** to verify that A's public key indeed **belongs to A**

Lets say Mario sends you: Identity Information and Public Key of Mario Rossi

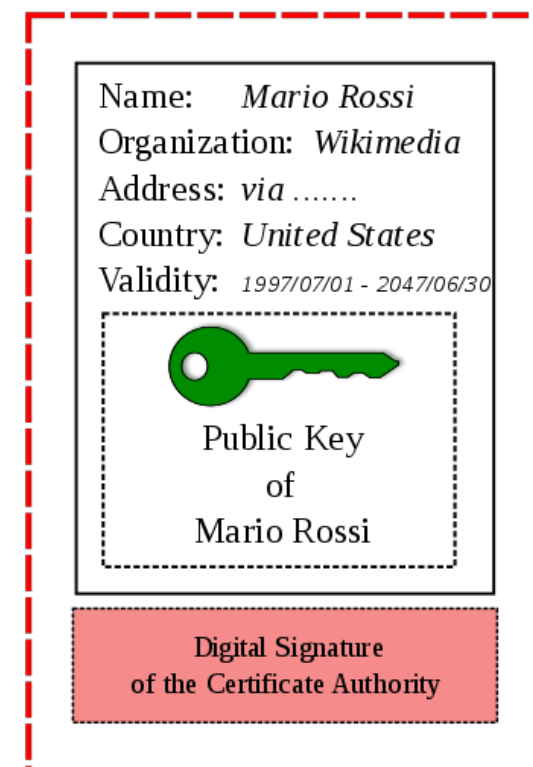


Certificate Authority
verifies the identity of Mario Rossi
and encrypts with its Private Key



**Checking if "Mario"
is indeed Mario**

Certificate of Mario Rossi



Digitally Signed by
Certificate Authority

1. PROVIDING AUTHENTICATION

Practical usage using **message digest**

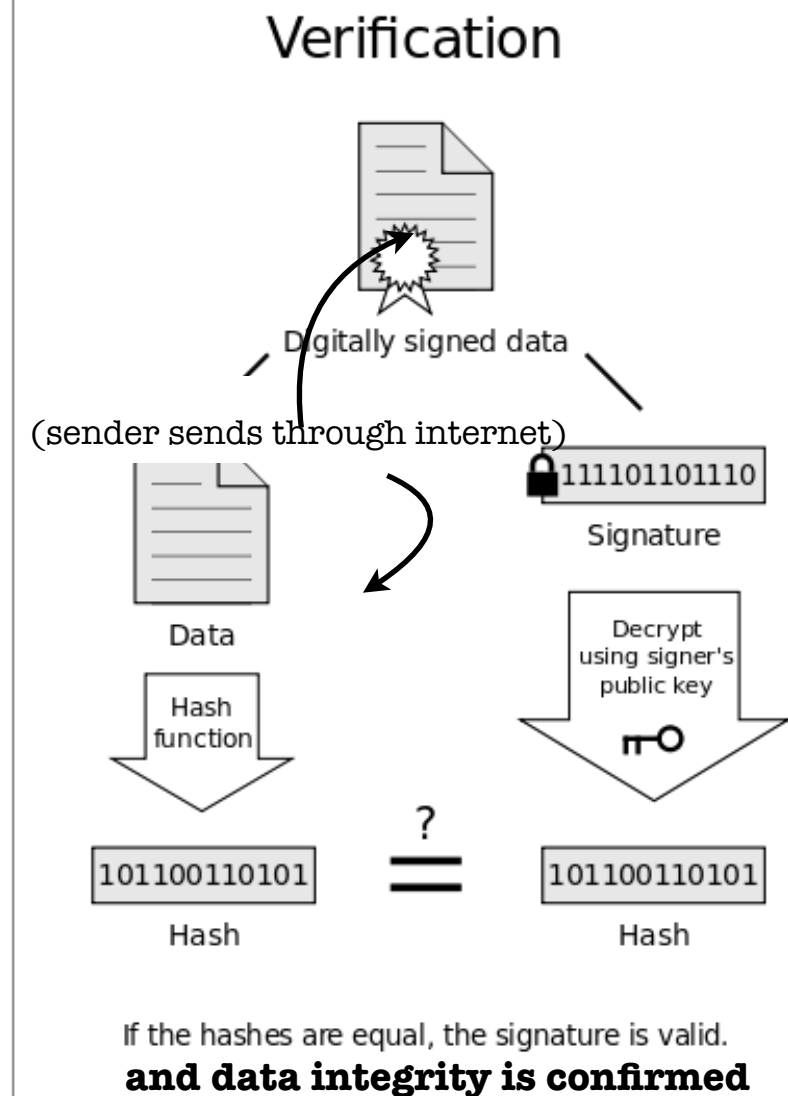
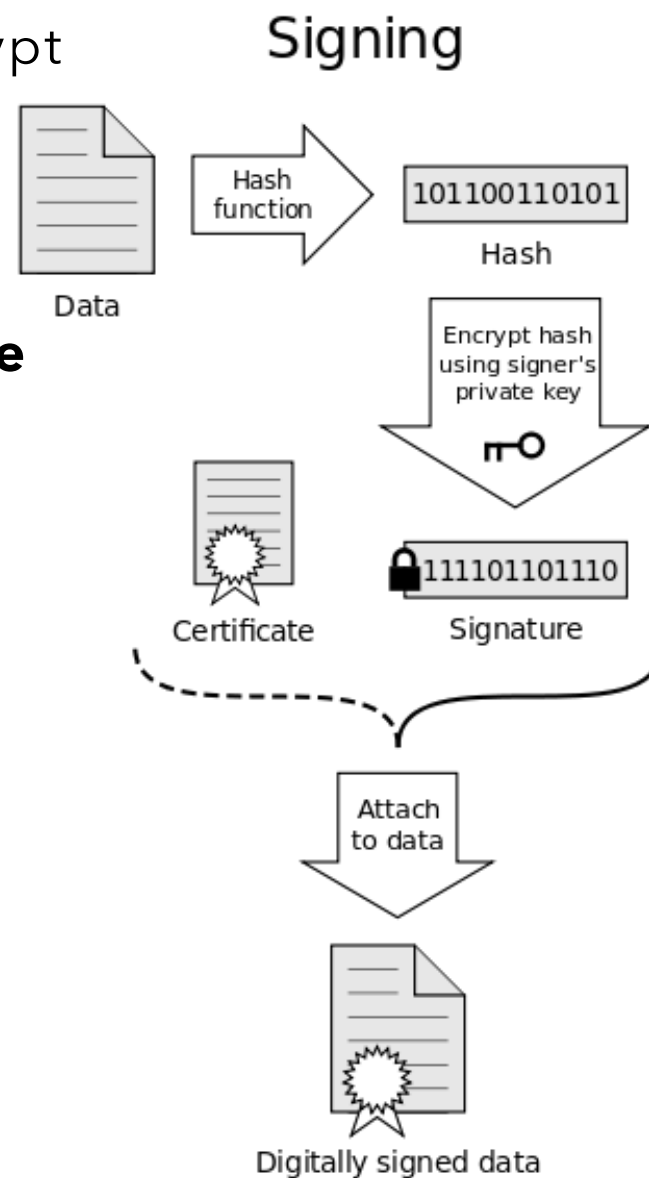
It is expensive to encrypt long messages using private key (RSA)

Solution: use message digest

Message digest:

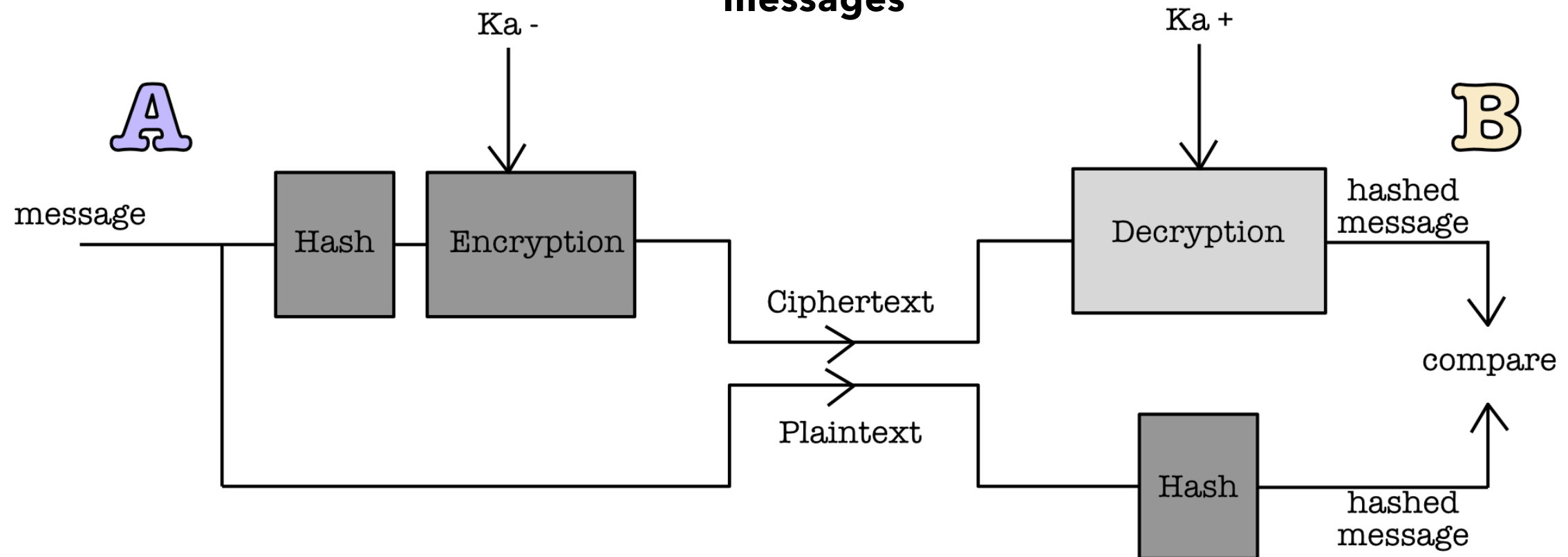
Hash long (arbitrary sized) messages to produce a **fixed size message digest**

Hash functions: MD5, SHA1



2. PROVIDING AUTHENTICATION AND MESSAGE INTEGRITY

Prevent impersonation, spoofing, eavesdropping, playback, and altering of messages



3. PROVIDING AUTHENTICATION, MESSAGE INTEGRITY, AND CONFIDENTIALITY

Eg: **secure e-mail, ssh, https**

Prevents prevent impersonation, spoofing, eavesdropping, playback and man-in-the-middle (hijacking)

