

Complementary mass measurements of N~Z isotopes at IGISOL and RIKEN



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Outline

- Motivation
- Mass measurements at RIBF/RIKEN
- Mass measurements at IGISOL/JYU
- Summary and Outlook



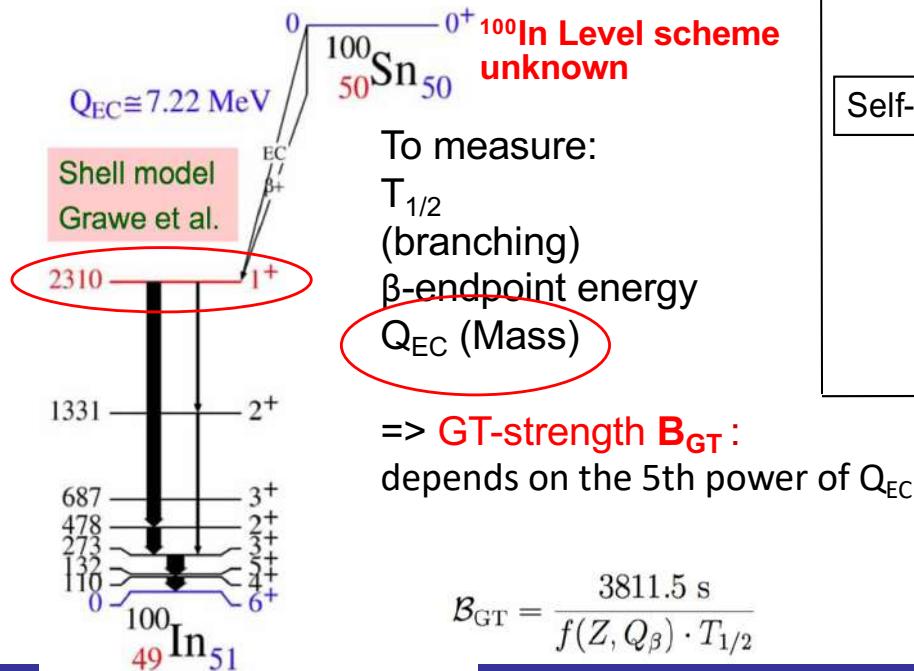


nuclear structure&fundamental physics

1. Wigner energy/ np pairing
2. Mapping proton drip-line
3. Isospin symmetry breaking
4. Deformation/Doubly-magic ($N=Z=40, 50$)
5. Test of mass models
6. Shell closures and evolution
7. New isomers
8. Standard model tests (CVC)

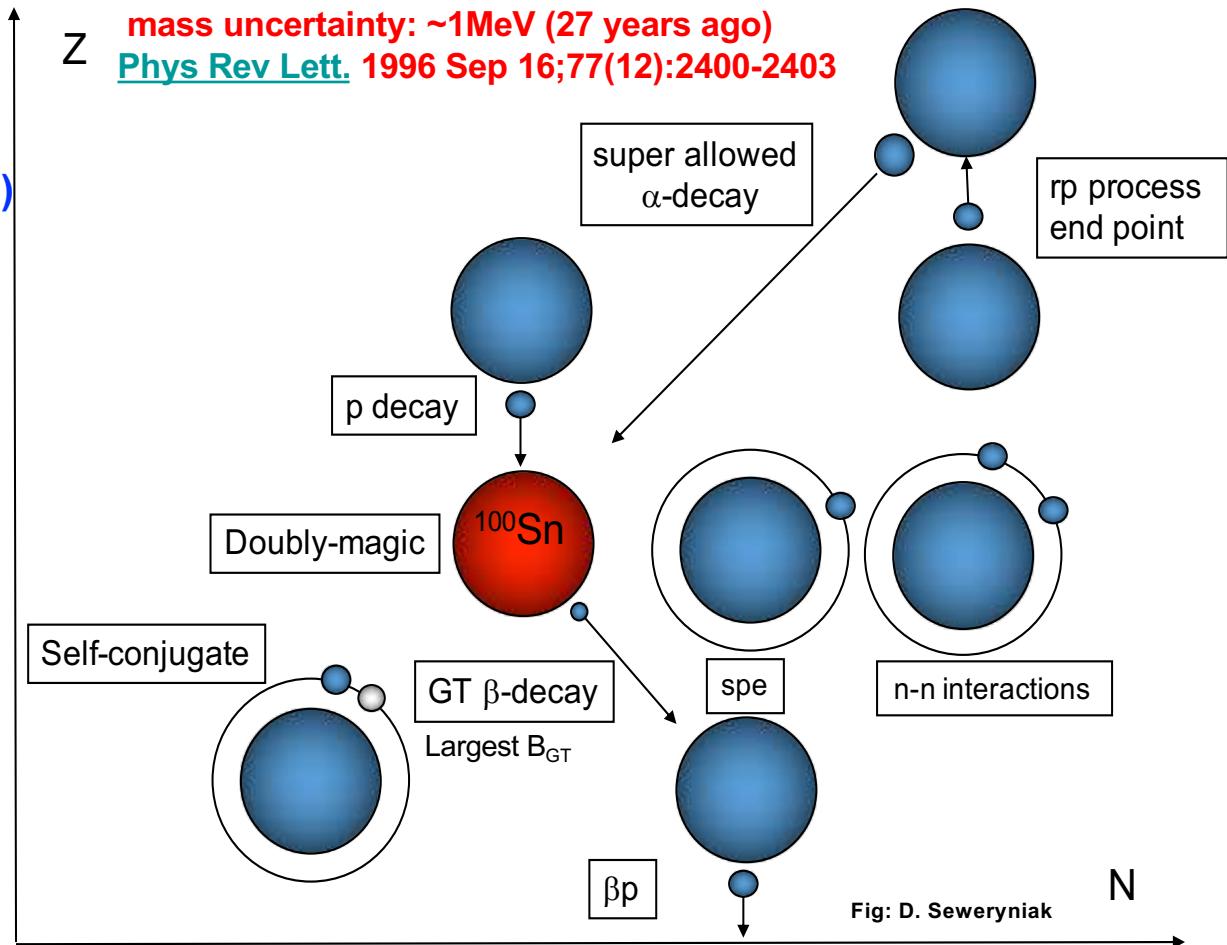
Nuclear Astrophysics

Modelling vp-, rp-processes



^{100}Sn physics

mass uncertainty: ~1MeV (27 years ago)
[Phys Rev Lett. 1996 Sep 16;77\(12\):2400-2403](#)



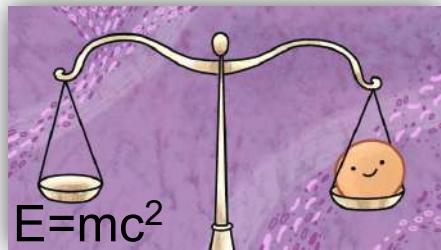
Discrepancy of Q_{EC} from GSI and RIKEN 450 keV

C. B. Hinke et al., *Nature* 486, 341 (2012).

D. Lubos et al., *Phys. Rev. Lett.* 122, 222502 (2019).



Mass excess



Nuclear mass \leftrightarrow nuclear binding energy:

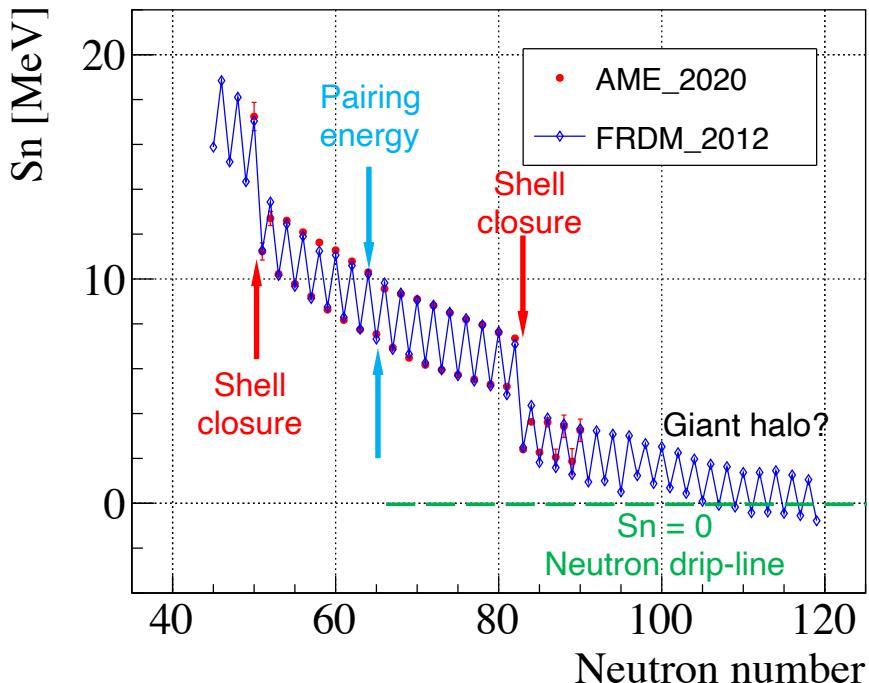
$$M(N, Z) = Z \cdot m_p + N \cdot m_n - B(N, Z)/c^2$$

Several masses \leftrightarrow Binding energy derivatives, such as S_n, S_{2n}, \dots :

$$S_n(N, Z) = M(N - 1, Z) + m_n - M(N, Z) = B(N, Z)/c^2 - B(N - 1, Z)/c^2$$

Nuclear structure

tin ($Z = 50$) one neutron separation energy



Nuclear astrophysics

For example:
rp process



X-ray burst

J. Grindlay et al., *Astrophys. J.* 205 (1976) L127.

time-scale $\propto e^{(Q/kT)} / A(Q)$
isotope production $\propto A(Q) \cdot e^{(Q/kT)}$
energy production $\propto A(Q) \cdot Q \cdot e^{(Q/kT)}$
Common parameter: Q (mass difference)

Final Composition (rp process):

X-ray burst model uncertainty: Q values

Exponential dependence on masses!

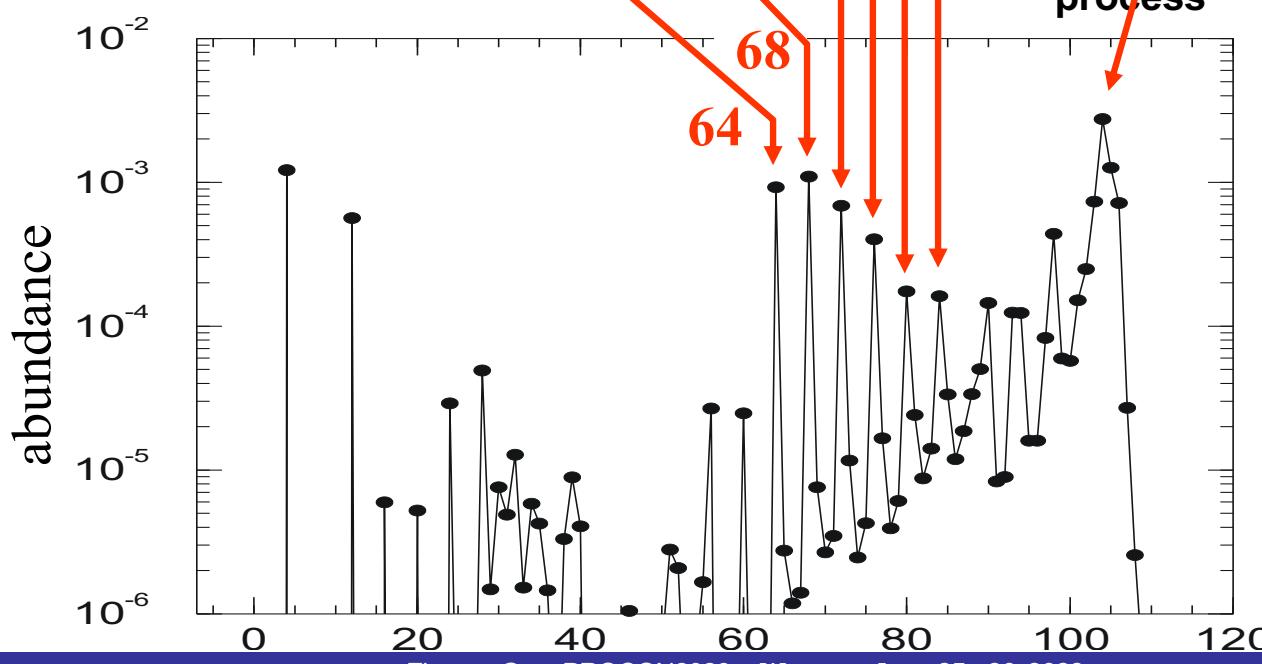
$$\frac{Y_{n+1}}{Y_n} = \rho_n \frac{G_{n+1}}{2G_n} \left(\frac{A_{n+1}}{A_n} \frac{2\pi\hbar^2}{m_u kT} \right)^{3/2} \exp\left(\frac{S_{n+1}}{kT}\right)$$

slow β decay

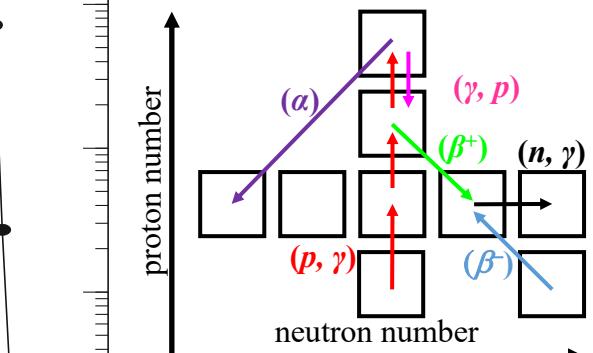
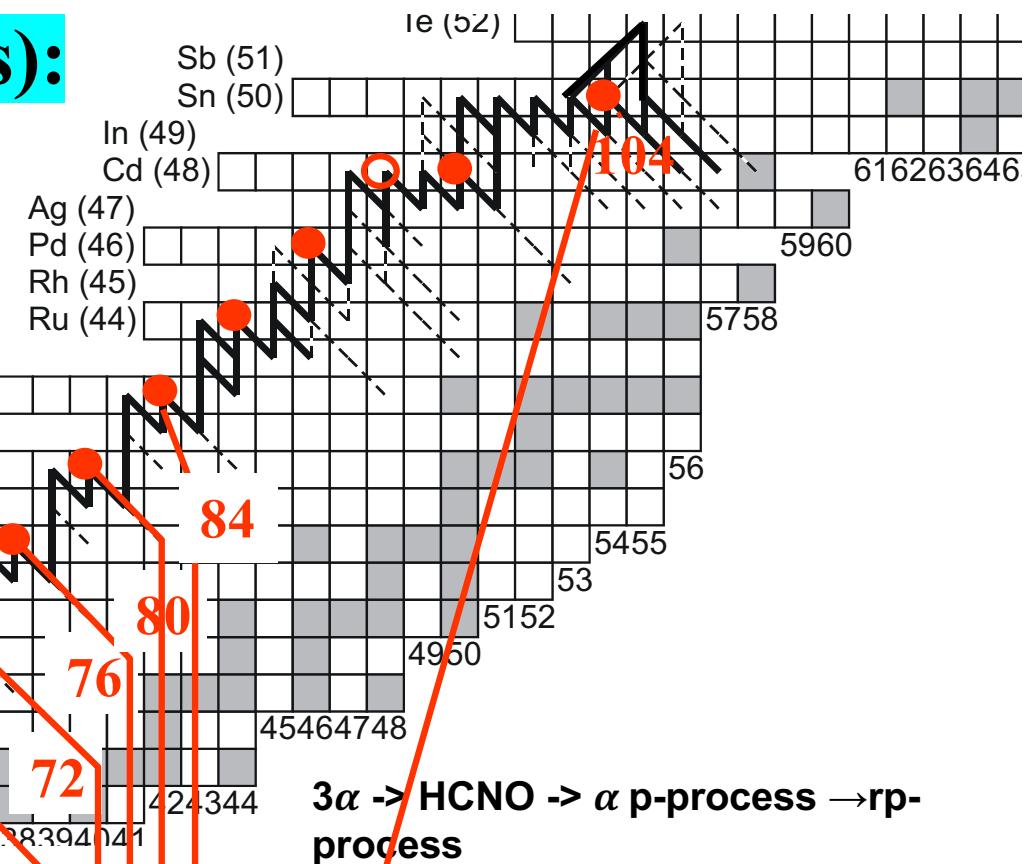
● (waiting point)

Schatz et al. Phys. Rev. Lett. 68 (2001) 3471

Schatz et al. 1998

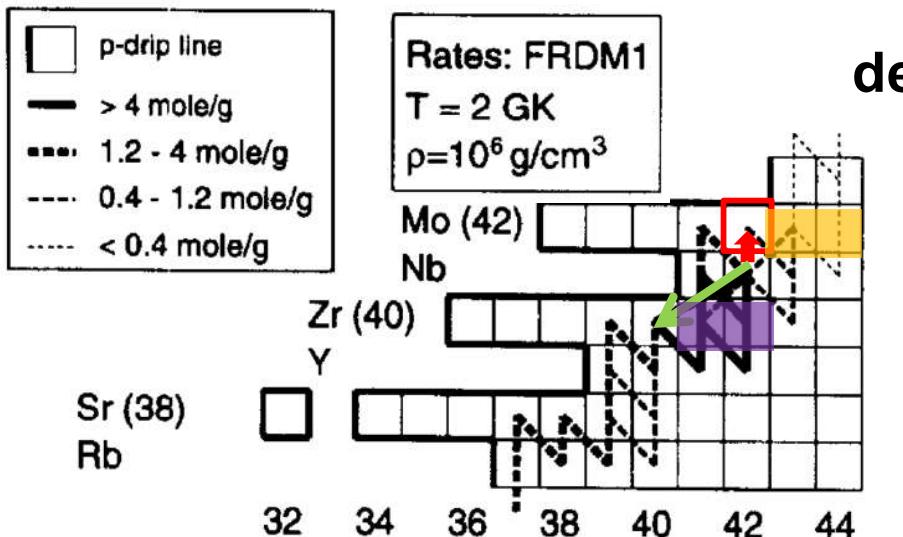


Mass number ⁴

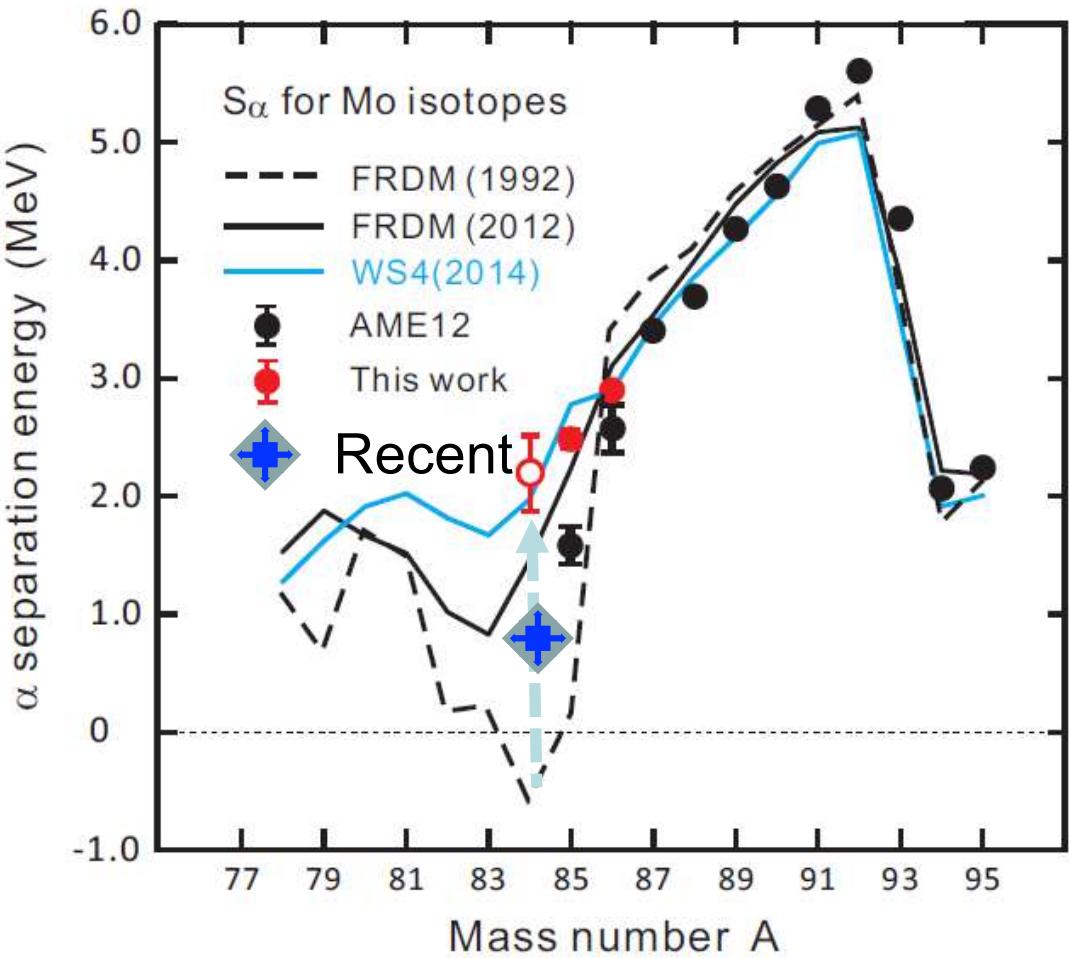


Impact on rp-process

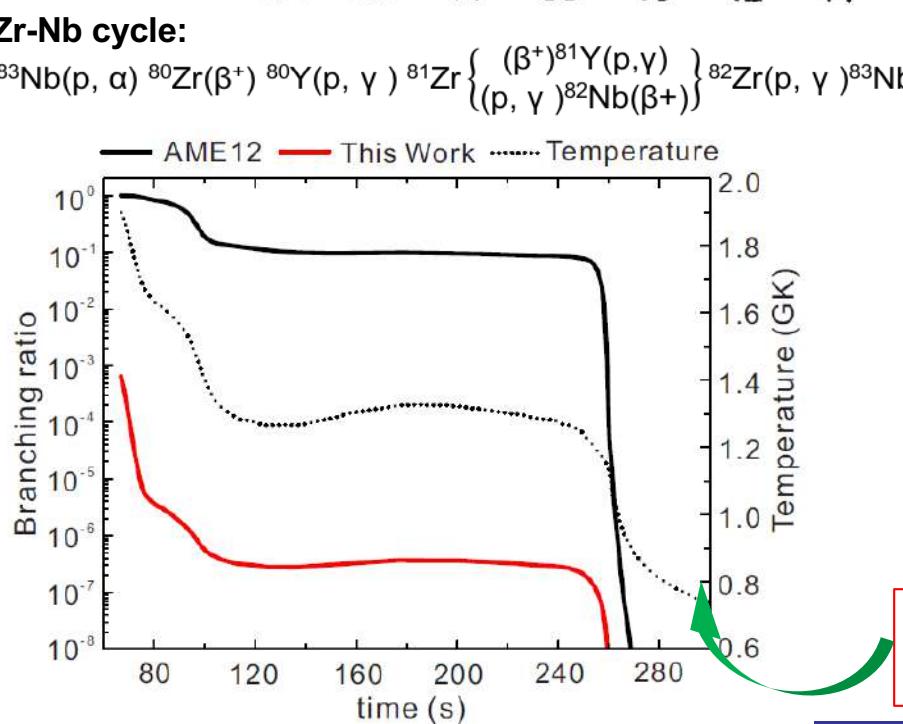
H. Schatz et al. / Physics Reports 294 (1998) 167–263



Mass of ^{84}Mo needed for determination of α separation energy of ^{84}Mo

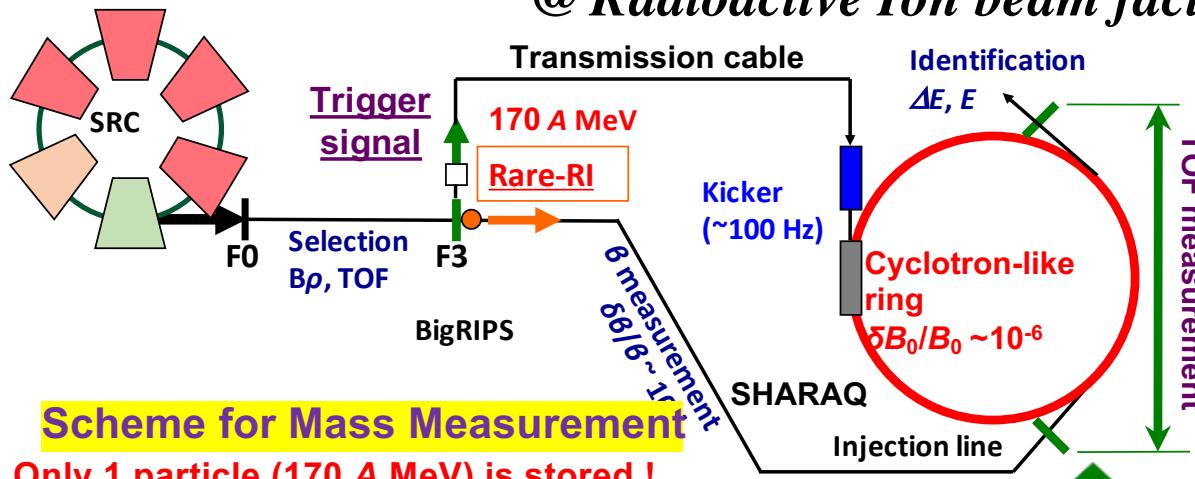


masses of $^{83,84}\text{Mo}$, ^{82}Nb , ^{83}Nb , would redefine fraction of the reaction flow branching into the Zr–Nb cycle



Scheme for Mass Measurement and location of Rare-RI Ring (R3)

@ Radioactive Ion beam factory (RIBF)



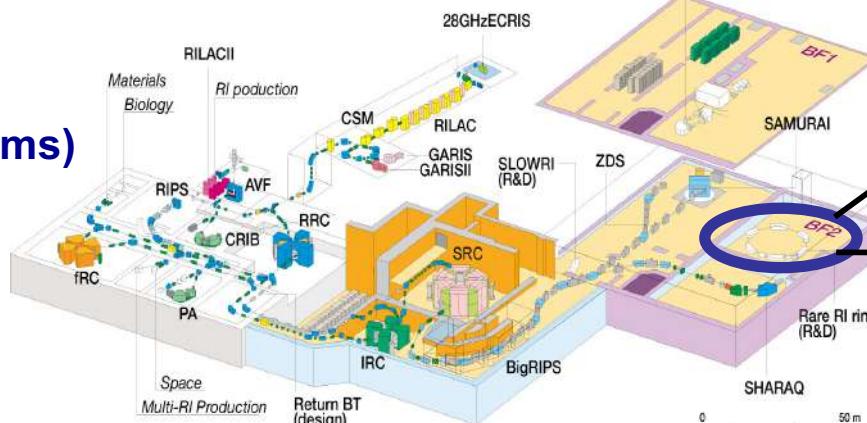
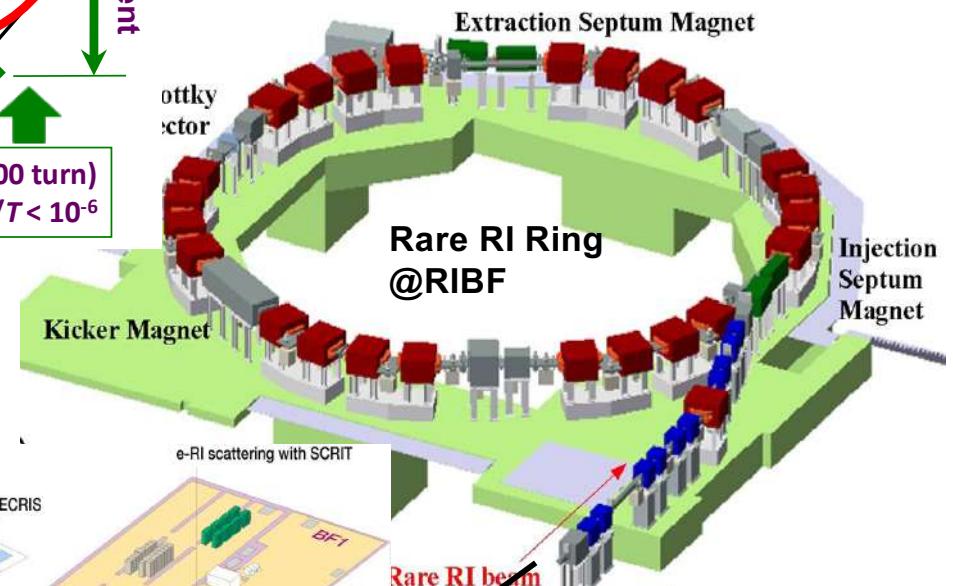
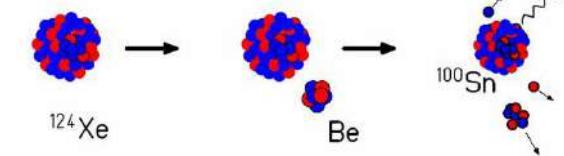
Isochronous mass spectrometry

- Isochronous field $\sim 10^{-6}$
- Beam-triggered individual injection



Short measurement time (<1 ms)
Good resolution ($\sim 10^{-6}$)
High efficiency ($\sim 100\%$)

Projectile fragmentation of heavy ion beams:



Location of
Rare-RI Ring
at RIKEN RIBF

Particle identification scheme at BigRIPS-HA

TOF-B ρ - ΔE method with track reconstruction → Improve B ρ and TOF resolution

Measure TOF, B ρ , ΔE @ 2nd stage

+ isomeric
γ-rays

Z, A/Q

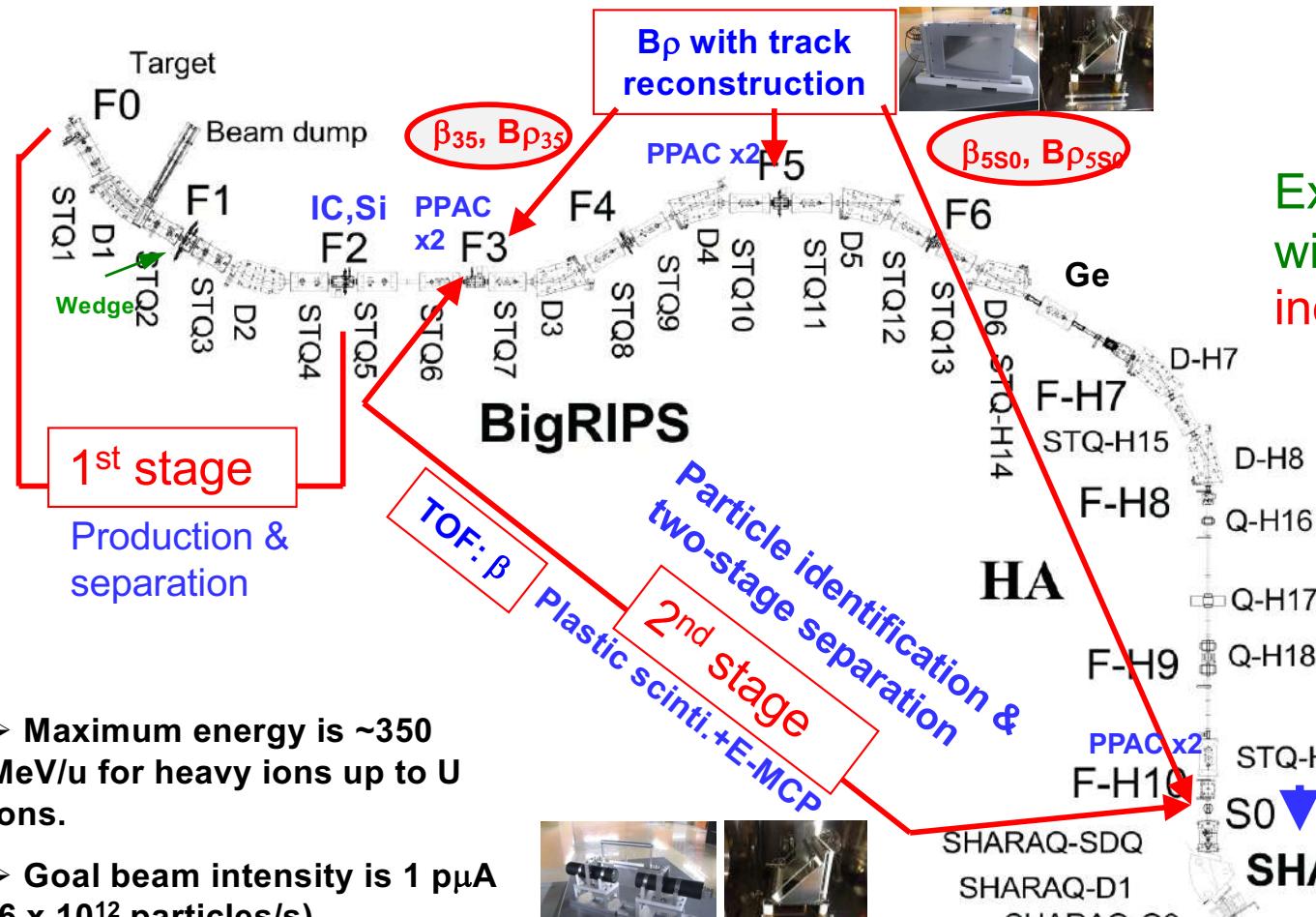
$$Z \leftarrow -dE/dx = f(Z, \beta)$$

$$A/Q = \frac{B\rho}{\gamma\beta m_u}$$

Two-stage separator

1st stage: F0-F2
2nd stage: F3-S0

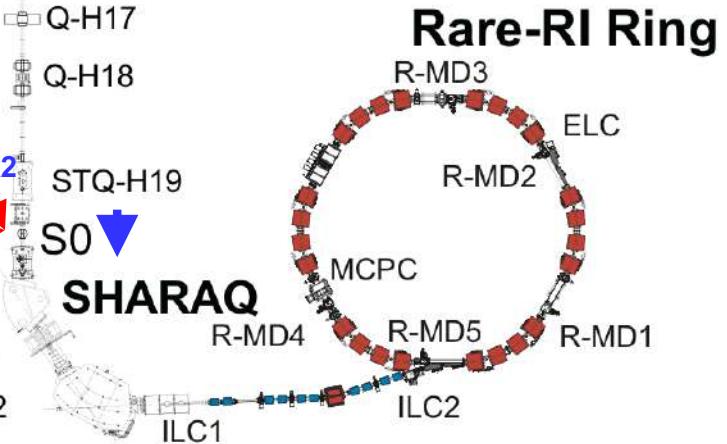
ΔE : IC, Si
Isomer γ-ray: Ge
TOF: Scintillator,
E-MCP, BE-MCP
Position: PPAC



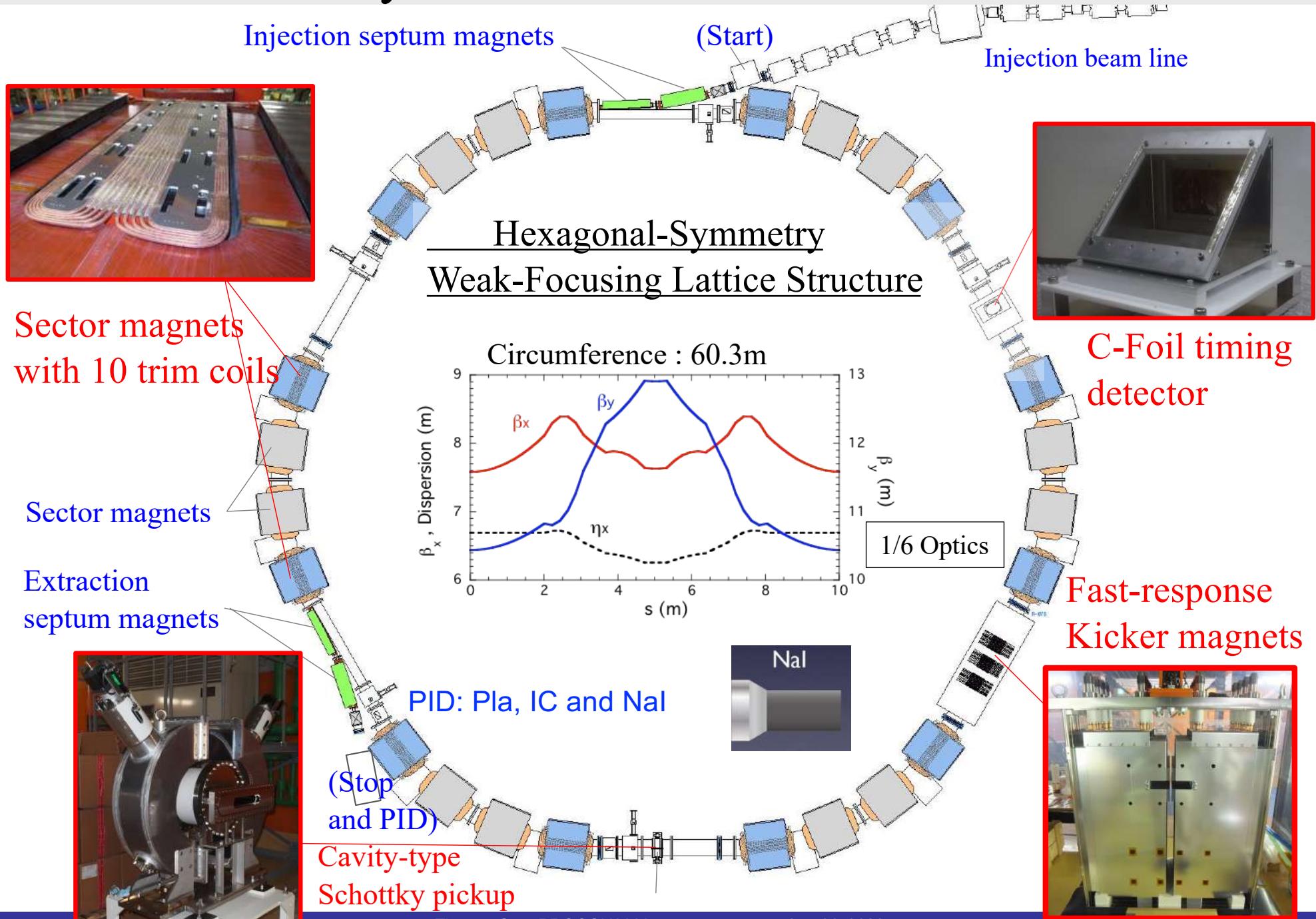
Excellent particle identification
without measuring TKE →PID
including charge states

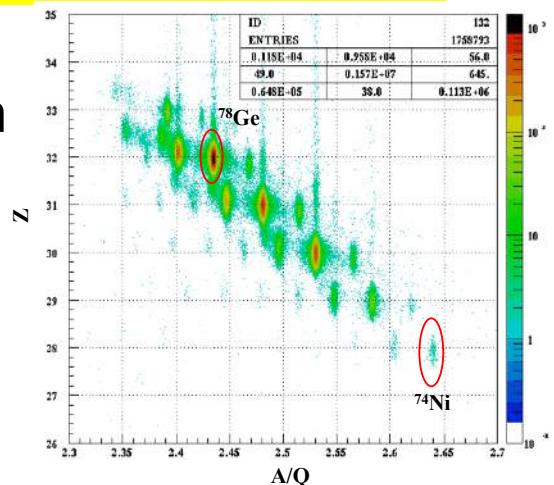
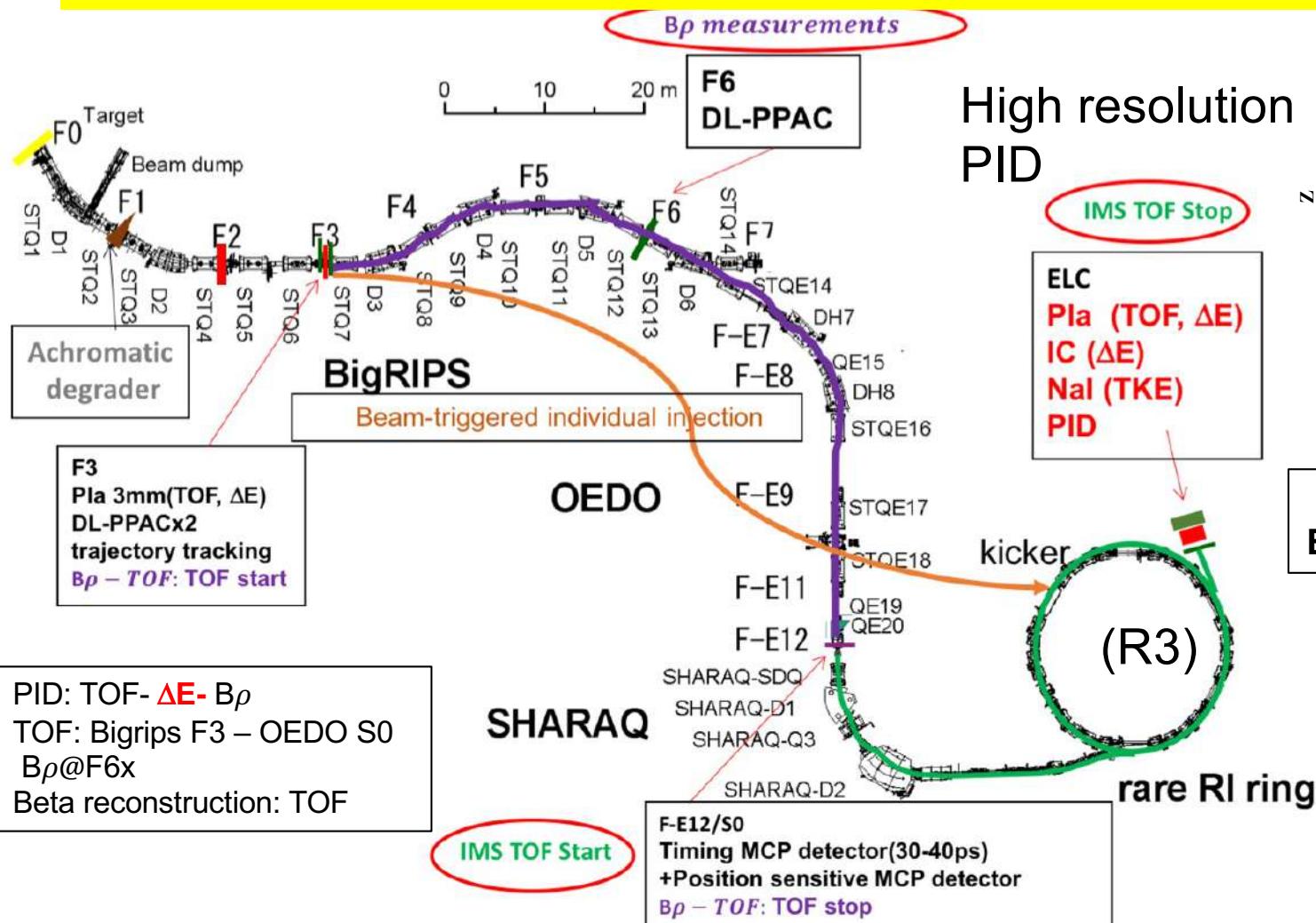
➤ Maximum energy is ~350 MeV/u for heavy ions up to U ions.

➤ Goal beam intensity is 1 pμA (6 × 10¹² particles/s).
Max. beam power ~100 kW



R3: Cyclotron-like Lattice Structure





B ρ – TOF mass is By-product part of IMS runs

F3-S0:
Efficiency 70-90%
Momentum acceptance $\pm 0.5\%$
Rare-RI Ring:
Efficiency 1 %
Momentum acceptance $\pm 0.3\%$

IMS (Isochronous mass spectrometry) method.
Revolution time Correction by beta/ B ρ measurements:

$$\left(\frac{m}{q}\right)_1 = \left(\frac{m}{q}\right)_0 \frac{T_1}{T_0} \frac{\gamma_0}{\gamma_1} = \left(\frac{m}{q}\right)_0 \frac{T_1}{T_0} \sqrt{\frac{1 - \beta_1^2}{1 - \left(\frac{T_1}{T_0} \beta_1\right)^2}}$$

Mass measurements by B ρ – TOF , TOF (F3-S0) and B ρ measurements at F6/F5:

$$\frac{m_0}{q} = \frac{B\rho}{\gamma L/t} = B\rho \sqrt{\left(\frac{t}{L}\right)^2 - \left(\frac{1}{c}\right)_0^2}$$

Principle of Mass Measurement at the Rare-RI Ring

cyclotron frequency

$$f_c = \frac{1}{2\pi} \frac{qB}{m}$$

Isochronous optics

$$B = B_0 \gamma$$

m/q	: charge-to-mass ratio
T	: revolution time
Index	
0	: reference ion
1	: ion of interest

$$\left. \begin{array}{l} \frac{m_0}{q_0} \gamma_0 \beta_0 = \frac{m_1}{q_1} \gamma_1 \beta_1 \\ \beta_0 T_0 = \beta_1 T_1 \end{array} \right\}$$

$$T_0 = 2\pi \frac{m_0}{q} \frac{1}{B} \gamma_0 = 2\pi \frac{m_0}{q} \frac{1}{B_0}$$

$$\text{For } m_1/q = m_0/q + \Delta(m_0/q)$$

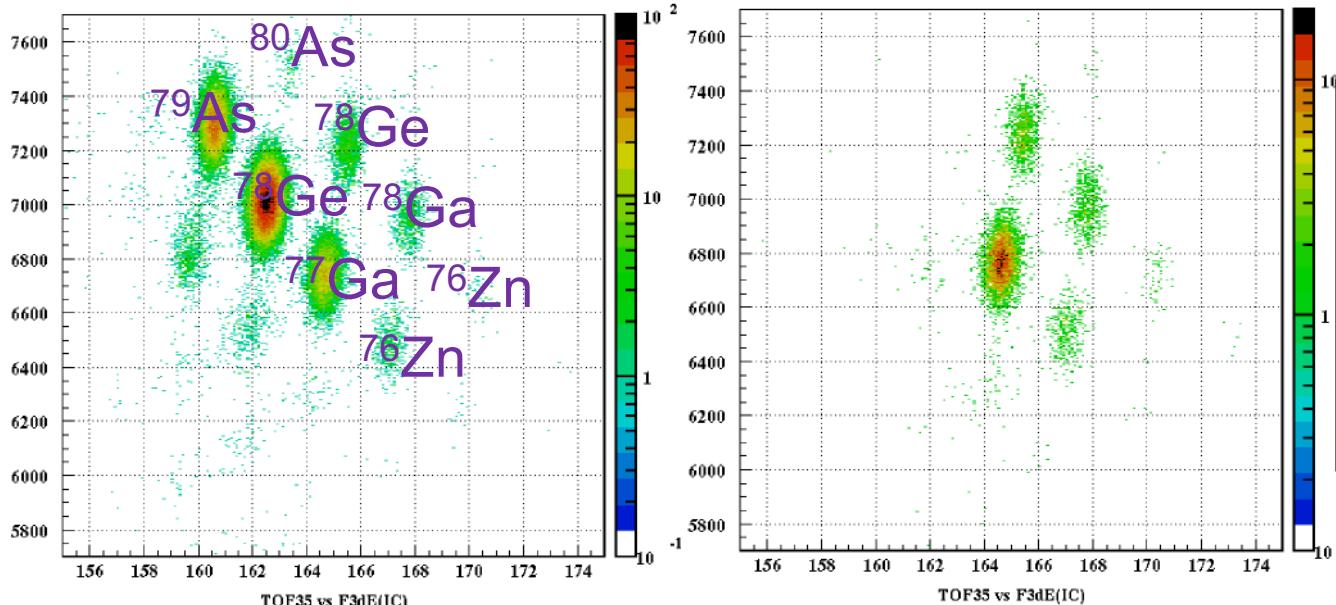
$$\frac{m_1}{q} = \left(\frac{m_0}{q} \right) \frac{T_1}{T_0} \frac{\gamma_0}{\gamma_1} = \left(\frac{m_0}{q} \right) \frac{T_1}{T_0} \sqrt{\frac{1 - \beta_1^2}{1 - \left(\frac{T_1}{T_0} \beta_1 \right)^2}}$$

$$\left(\frac{m}{q} \right)_1 = \left(\frac{m}{q} \right)_0 \frac{T_1}{T_0} \frac{\gamma_0}{\gamma_1} = \left(\frac{m}{q} \right)_0 \frac{T_1}{T_0} \sqrt{\frac{1 - \left(\frac{T_0}{T_1} \right)^2}{\left(\frac{(m/q)_0}{(B\rho)_0} c \right)^2} + 1}$$

→ Need to measure velocity precisely

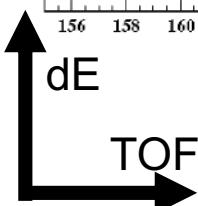
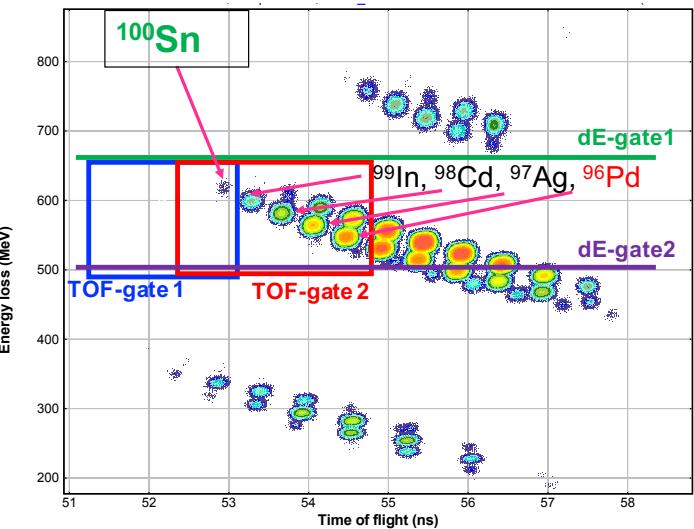
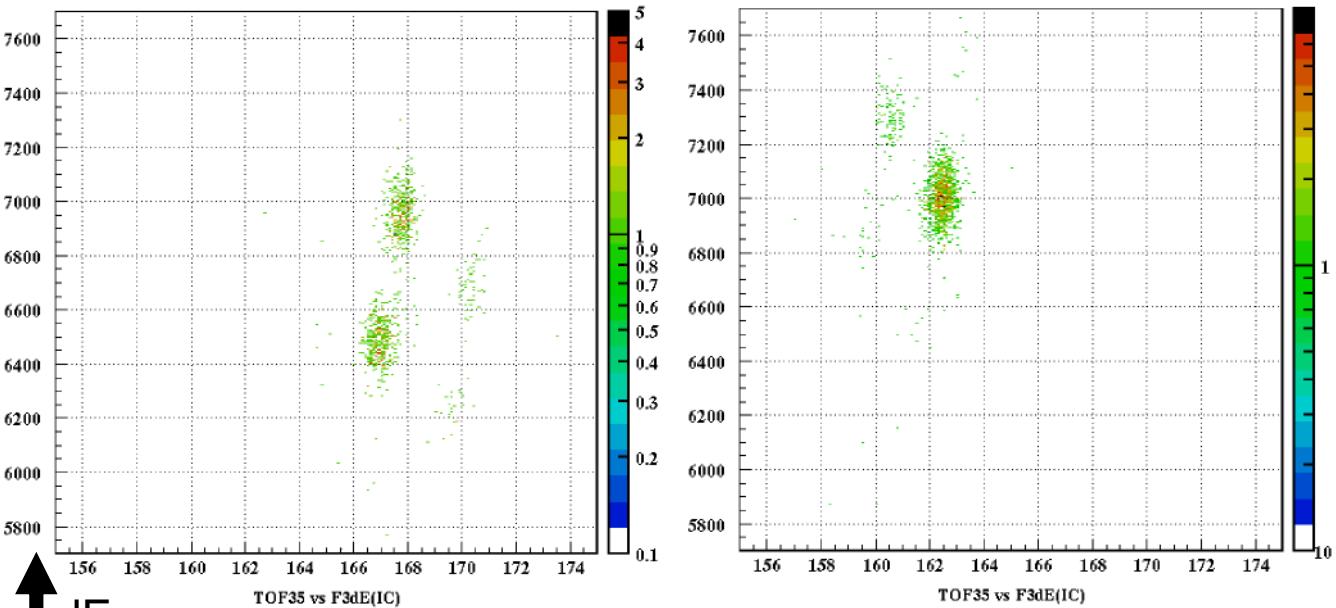
$B\rho$ measurement is important here!

dE-TOF gate Selection method



Setting TOF-gate1 and TOF-gate2 rates ratio to be 9:1

The two TOF gates set in 'or' logic (for example, 'N=Z and more exotic area' for TOF-gate 1 in 90 Hz and additional reference in TOF-gate 2 to be 10 Hz)



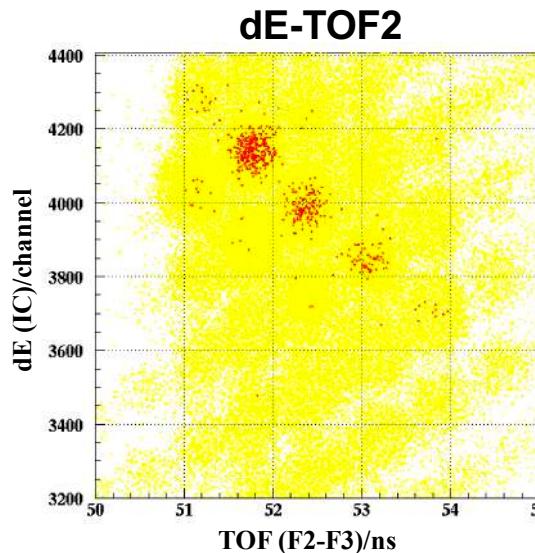
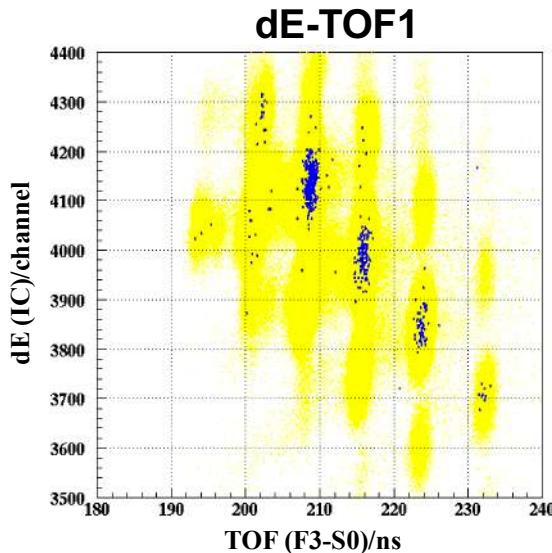
Ion species of interest are selected as triggering ions for injection to R3

Event-by-event PID with TOF(beamline)-B ρ -dE-E-TOF(in-Ring)

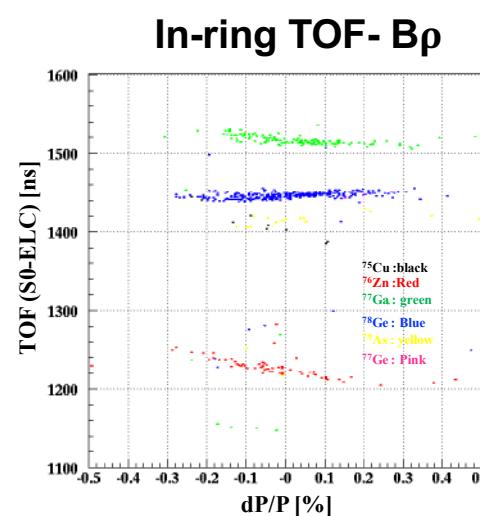
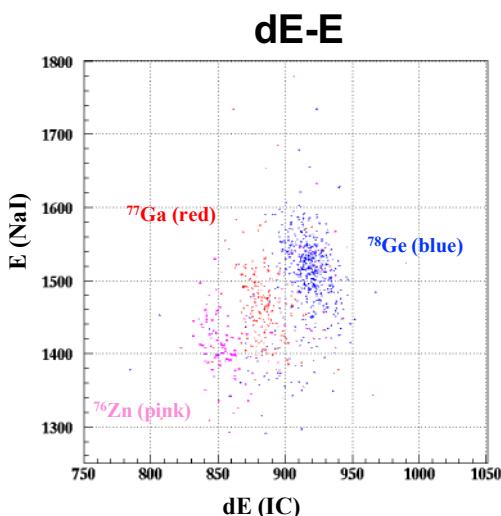
Zhuang Ge, Tomohiro Uesaka et al., Hyperfine Interact (2019) 240: 92

Unambiguously identification with single ion sensitivity

TOF: beamline (**F2-F3 and F3-S0**), dE: beamline IC



Yellow: all ions detected at S0
Blue: extracted from R3

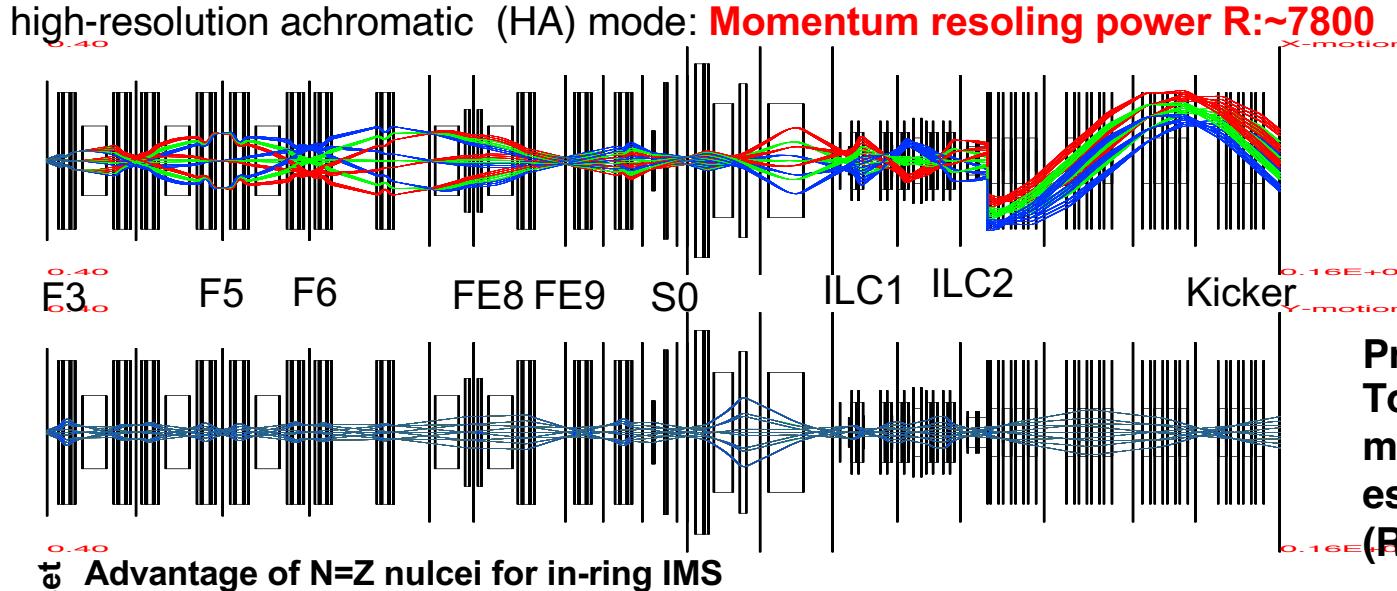


dE: IC, E: ring-extraction NaI

B ρ : beamline, TOF: in ring

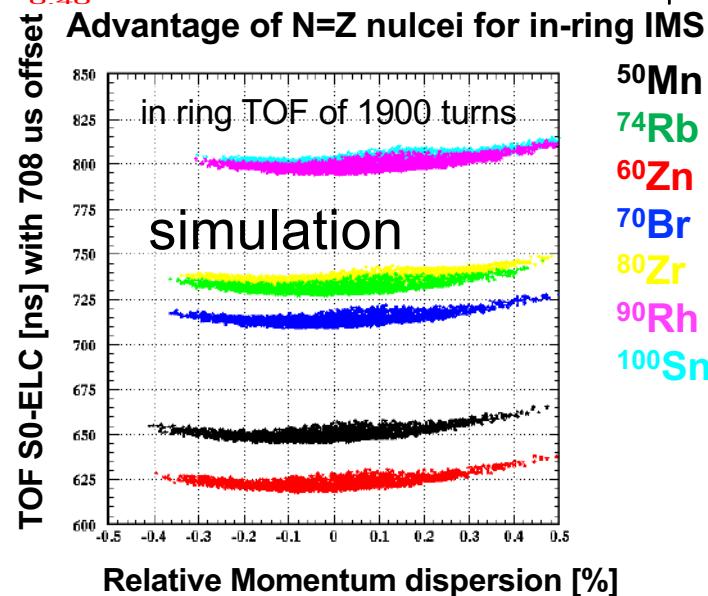
Optics design with high momentum resolving power and ion transportation simulation

Zhuang Ge, Tomohiro Uesaka et al., Hyperfine Interact (2019) 240: 92

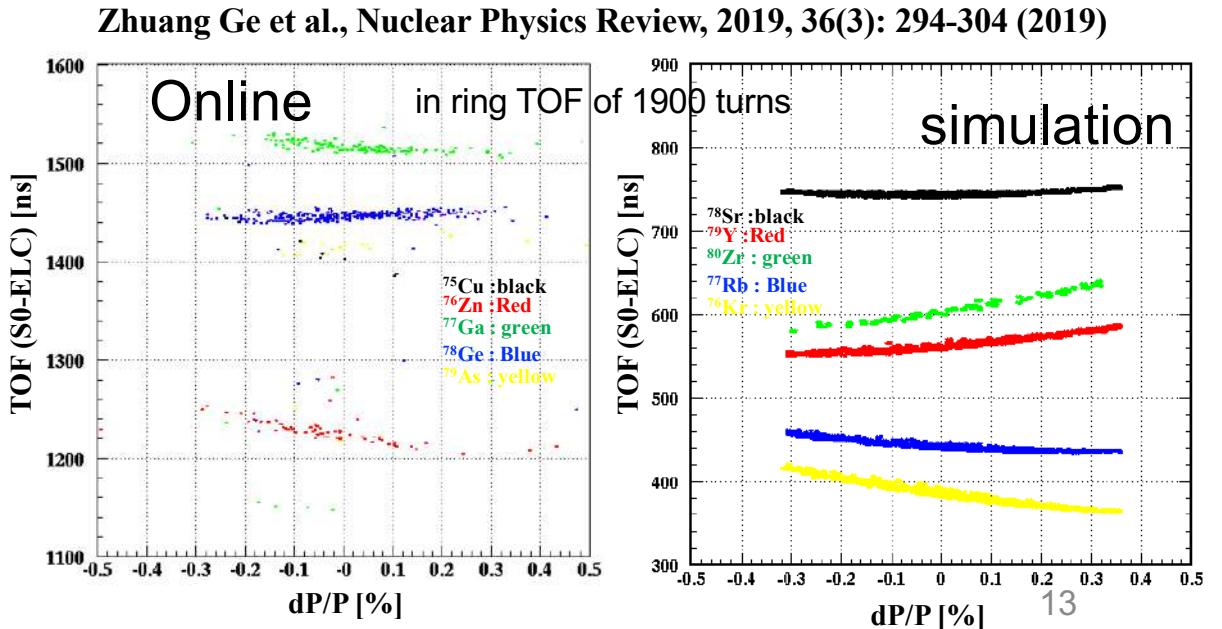


Dispersion matching is considered: no influence on the Bp-ToF method precision if the settings are optimized for the storage ring operating as IMS

Precision (1.5×10^{-5} - 2×10^{-6}) of Bp-ToF is estimated based on nomal mode (R: 3300) for a save estimation. We will use HA mode (R: 7800)



N=Z simulation (Z=25-50): all nuclei in isochronous
In a same setting from F3 to R3, all with high
resolving power

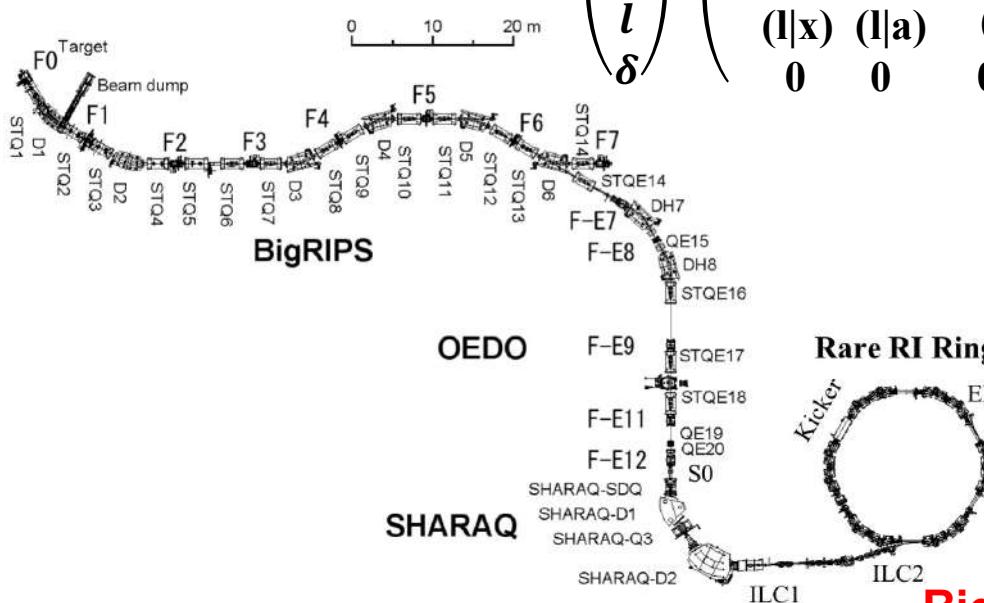


Ion optics design (beam-line and storage ring)

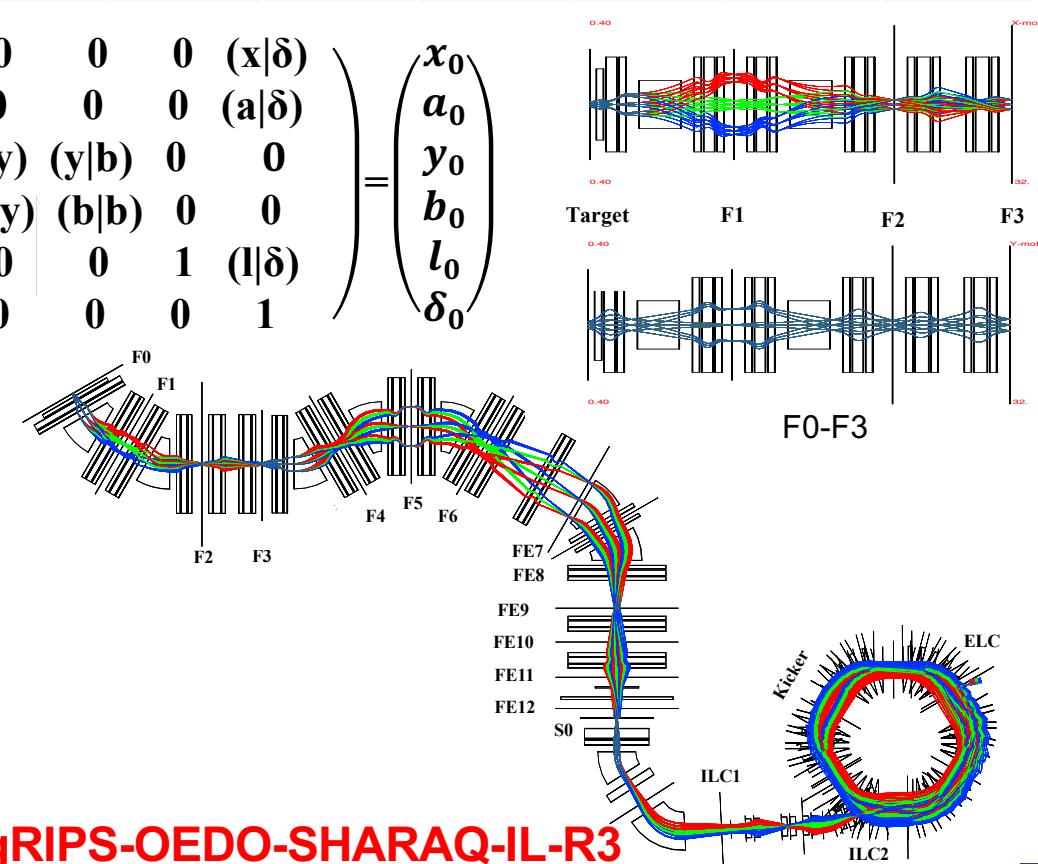
	(x x)	(x a)	(a x)	(a a)	(y y)	(y b)	(b y)	(b b)	(x dp)	(a dp)	(l dp)	L dEk
F3F4	-0.966	0	0	-1.03	-3.88	0	-0.04	-0.26	-1.86	-1.89	4.04	2.187439
F3F5	-0.01	-9.6	0.1	0	1.298	0	-0.06	0.77	0.108	0.505	8.81	4.771546
F3F6	0.965	0	0	1.036	-3.88	0	0	-0.257	7.54	0.368	11.62	6.296793
F3FE7	-0.394	9.7	-0.1	0.016	1.17	-2.386	0.438	-0.039	0.316	-0.803	17.21	9.323857
F3FE9	-0.854	0	-0.14	-0.527	2.67	0	-0.55	0.373	0	0.297	26.94	14.59592
F3S0	2.18	0	0.58	0.46	-2.27	0	0	-0.44	0	0.258	36.09	19.54942
F3ILC1	1.38	-0.58	1.87	-0.06	3.34	0.02	0.76	0.304	-4.15	0.66	44.26	23.98
F3ILC2	-6.18	0	0.83	-0.16	-2.6	0.48	0.476	-0.465	-5.78	-0.66	54.08	29.2974
F3KC	-9.1	1.04	-0.3	-0.07	-2.53	3.71	-0.42	0.22	-7	0	58.43	31.65375

Transfer matrix :

$$\begin{pmatrix} x \\ a \\ y \\ b \\ l \\ \delta \end{pmatrix} = \begin{pmatrix} (x|x) & (x|a) & 0 & 0 & 0 & (x|\delta) \\ (a|x) & (a|a) & 0 & 0 & 0 & (a|\delta) \\ 0 & 0 & (y|y) & (y|b) & 0 & 0 \\ 0 & 0 & (b|y) & (b|b) & 0 & 0 \\ (l|x) & (l|a) & 0 & 0 & 1 & (l|\delta) \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x_0 \\ a_0 \\ y_0 \\ b_0 \\ l_0 \\ \delta_0 \end{pmatrix}$$



BigRIPS-OEDO-SHARAQ-IL-R3



Optics Design of beam-line

Standard mode

Largest Dispersion function
@F5

$$(x|dp) \sim 3.3 \text{ m}/\%$$

$$(x|x) \sim 1.02$$

@F5x

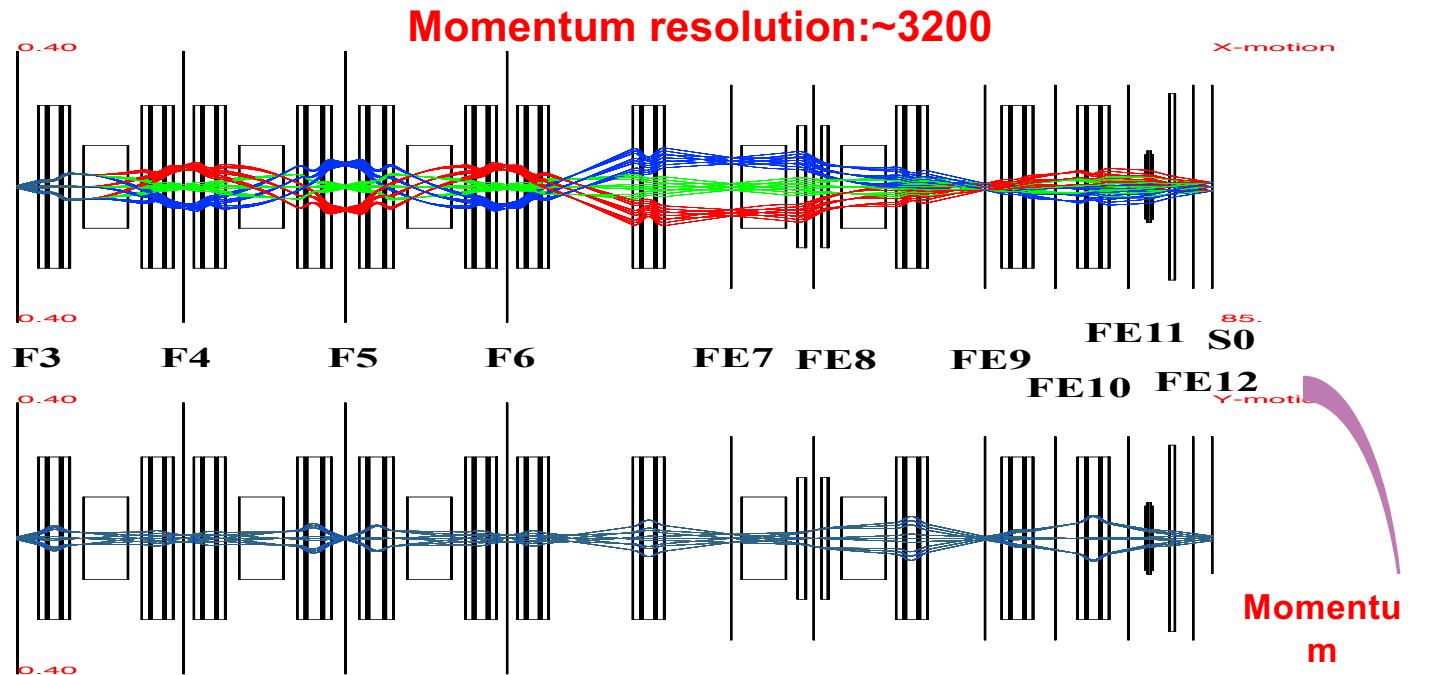
Dispersive focus:

X: F4,F5,F6,FE7; Y:

F4,F5,F6,FE7

double achromatic focus:

F3, FE9, S0



High-resolution (HA) mode

Largest Dispersion function
@F6

$$(x|dp) \sim 7.6 \text{ m}/\%$$

$$(x|x) \sim 0.9$$

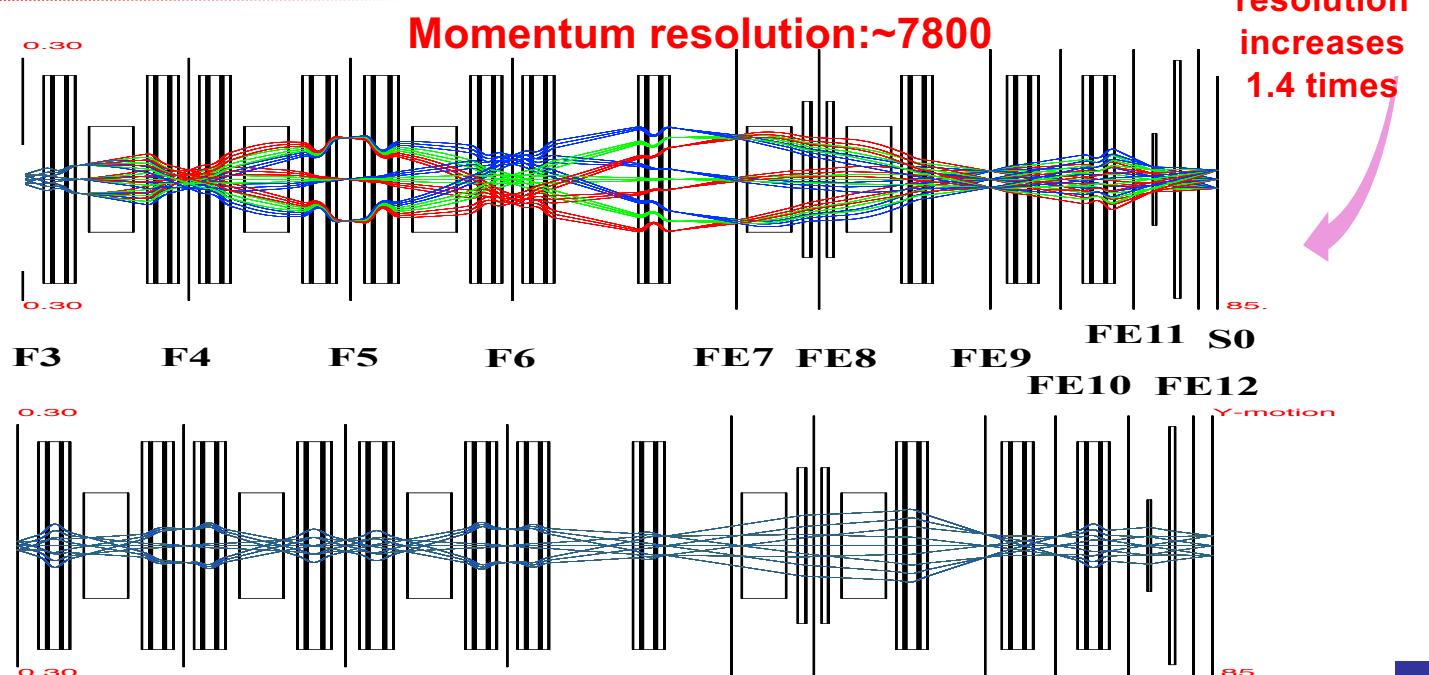
@F6x

Dispersive focus:

X: F4,F6; Y: F4,F5,F6

double achromatic focus:

F3,FE9, S0



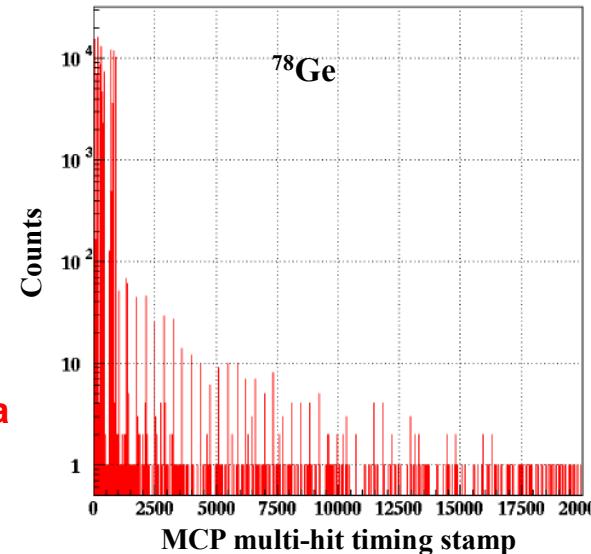
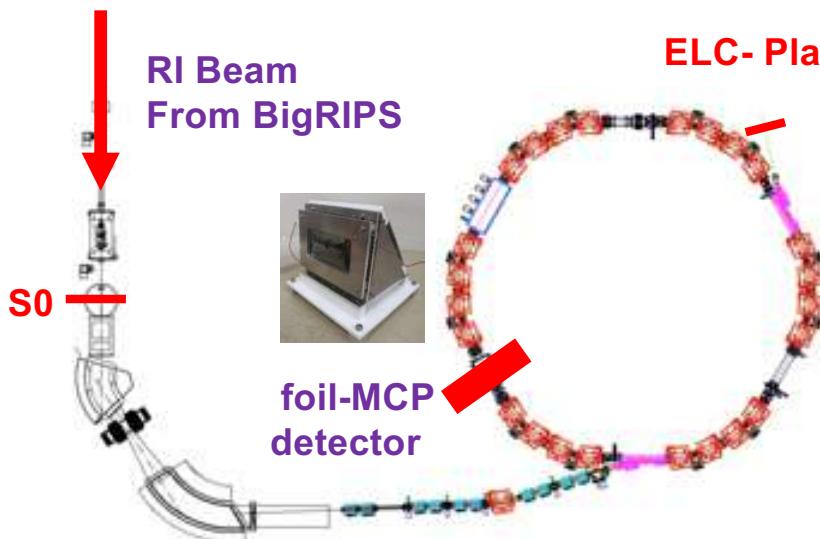
Revolution time determination



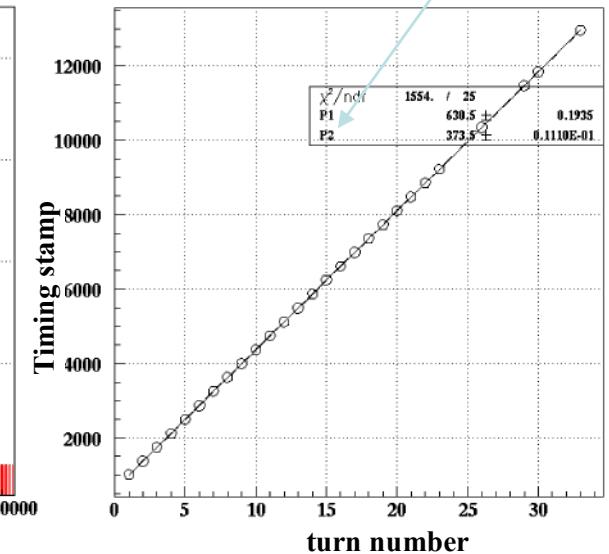
Circulation of turn number for each ion can be calculated from the Total TOF($s_0 \rightarrow \text{ELC}$) subtract the double kicker TOF over the MCP measured evolution time

$$N = \frac{\text{TOF}_{(S_0 \rightarrow \text{ELC})}^{\text{total}} - \text{TOF}_{(S_0 \rightarrow \text{ELC})}^{\text{doublekicker}}}{T}$$

To remove the non-isochronous TOF from S_0 to kicker center and kicker center to ELC



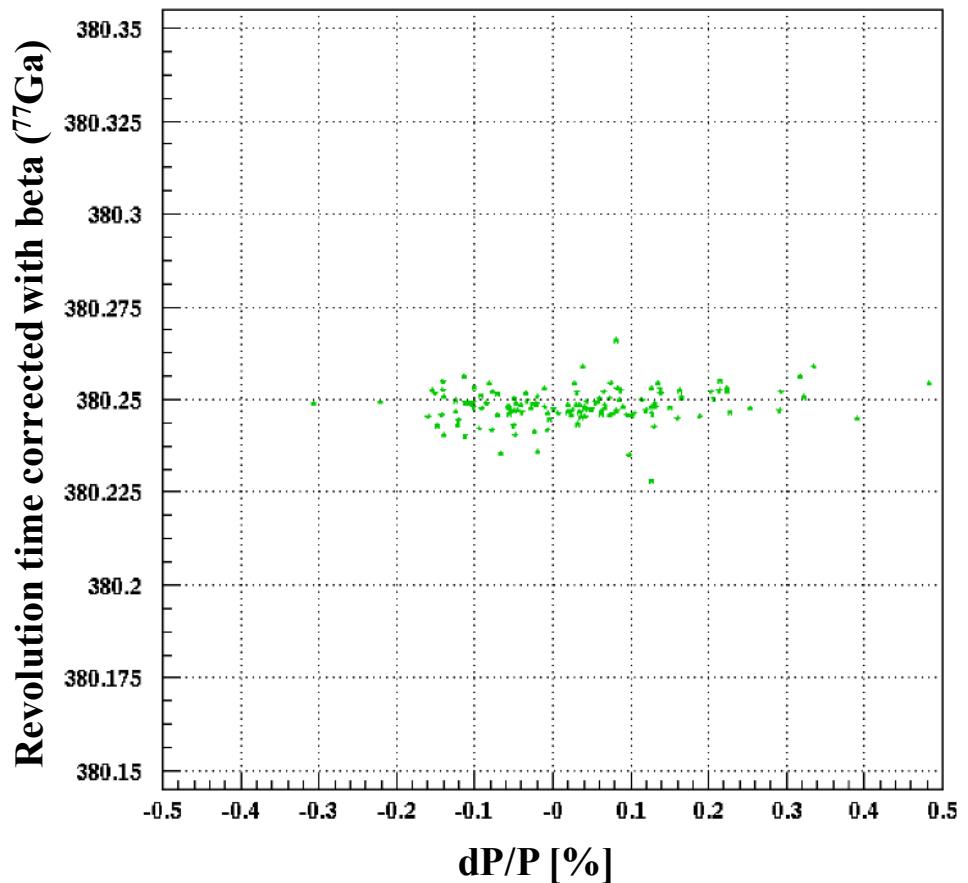
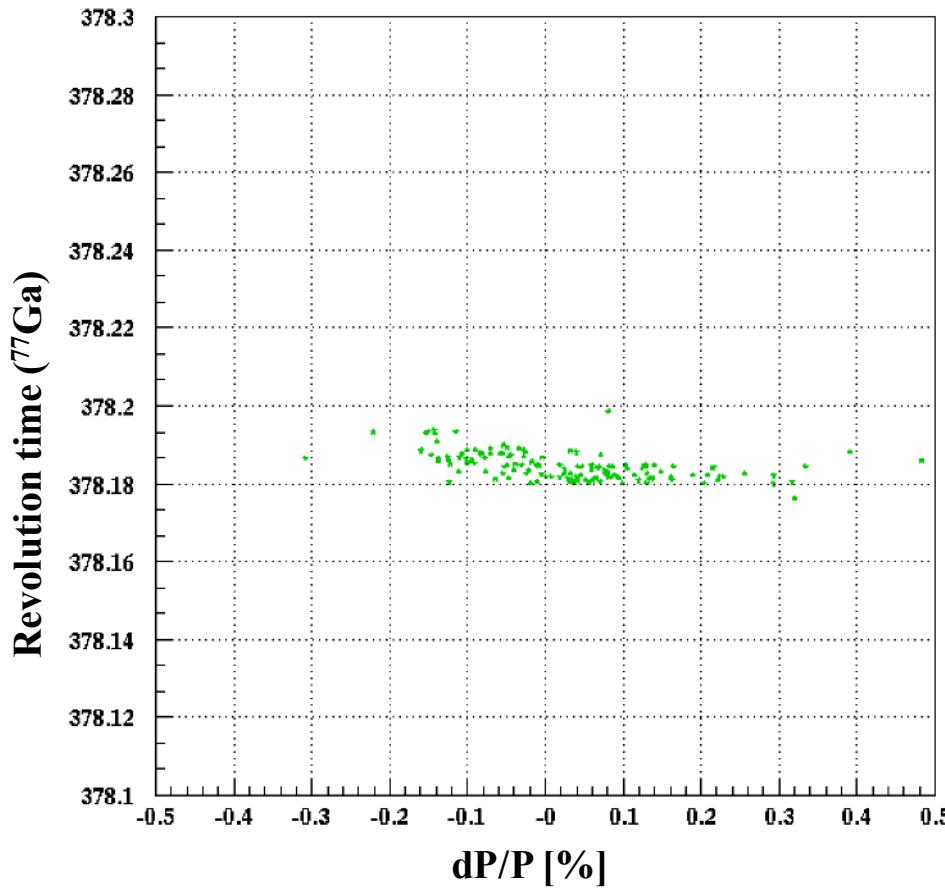
Multi-hit time stamp: $t = P_2 * N + P_1$
Revolution time: $T = P_2$



other particle's revolution time can be deduced from the relationship (assuming passing the same orbit):

$$\beta_0 T_0 = \beta_1 T_1$$

Mass measurements by IMS method



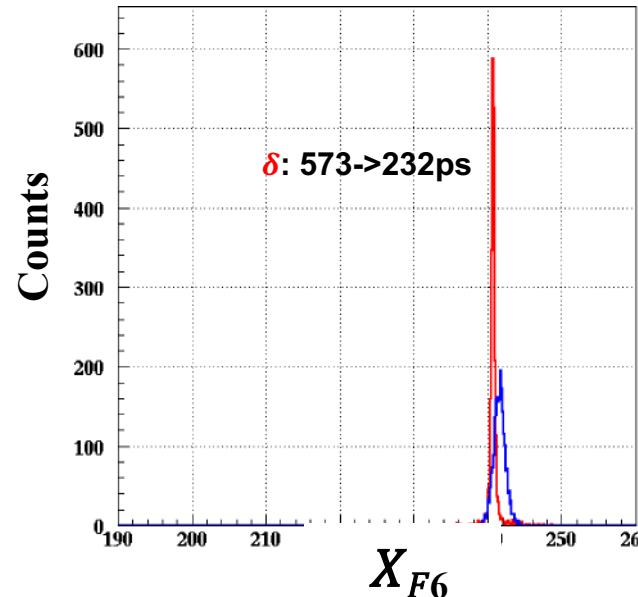
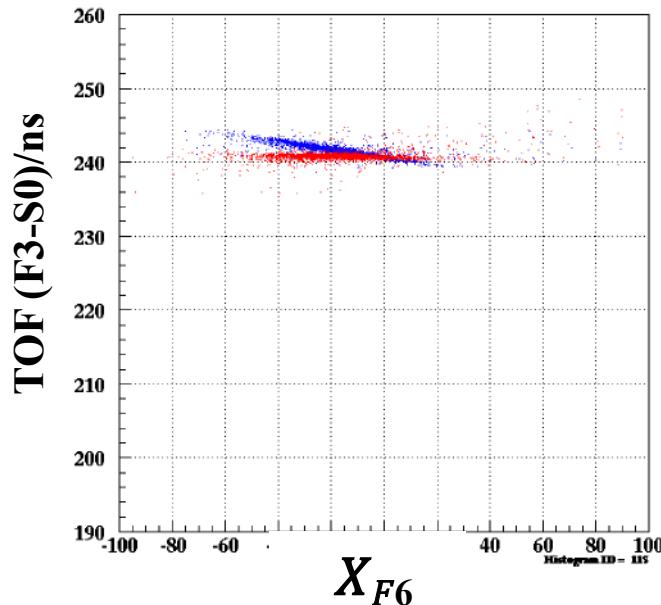
$$\left(\frac{m}{q}\right)_1 = \left(\frac{m}{q}\right)_0 \frac{T_1}{T_0} \frac{\gamma_0}{\gamma_1} = \left(\frac{m}{q}\right)_0 \frac{T_1}{T_0} \sqrt{\frac{1 - \beta_1^2}{1 - \left(\frac{T_1}{T_0} \beta_1\right)^2}}$$

Mass accuracy: $\sim 10^{-6}$

**Revolution time Correction by velocity measurements,
Velocity is deduced from TOF (F3-S0):**

Mass measurements by $B\rho - TOF$ method

TOF determination with magnetic rigidity correction



Mass measurements by $B\rho - TOF$ method:

$$\frac{m_0}{q} = \frac{B\rho}{\gamma L/t} = B\rho \sqrt{\left(\frac{t}{L}\right)^2 - \left(\frac{1}{c}\right)^2}$$

$$\frac{m_0}{\sigma_{m_0}} = 1/\sqrt{\frac{\sigma_{(B\rho)}^2}{(B\rho)^2} + \frac{1}{k^2} \left(\frac{\sigma_t^2}{t^2} + \frac{\sigma_L^2}{L^2} \right)}$$

$$k = 1 - (L/(ct))^2$$

X_{F6} : Proportional to momentum of ions

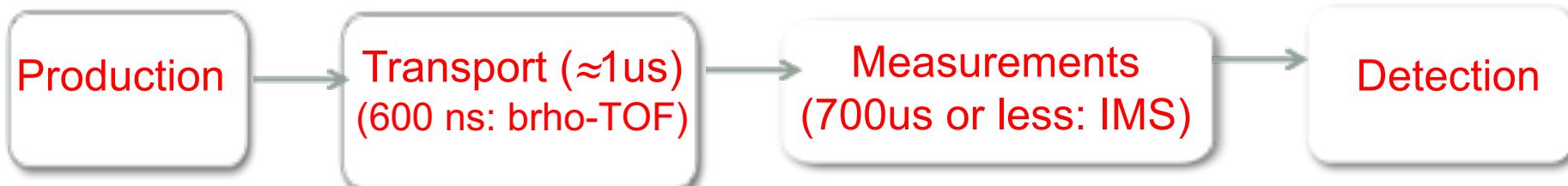
$$\chi^2 = \sum_{\text{calibrants}} \frac{((m/q)_{\text{lit}} - f(\tau, z))^2}{(\sigma_{\text{lit}})_i^2 + (\sigma_{\text{stat}})_i^2 + \sigma_{\text{sys}}^2}$$

$$(\sigma_{\text{stat}})_i^2 = \left(\frac{\partial f(\tau, z)}{\partial \tau} \right)^2 \times \sigma_i^2(\tau)$$

$m/q = f(T, A/Z, Z, A)$:
Calibration function to deduce mass
Beam-line resolution: $\sim 2 \times 10^{-4}$

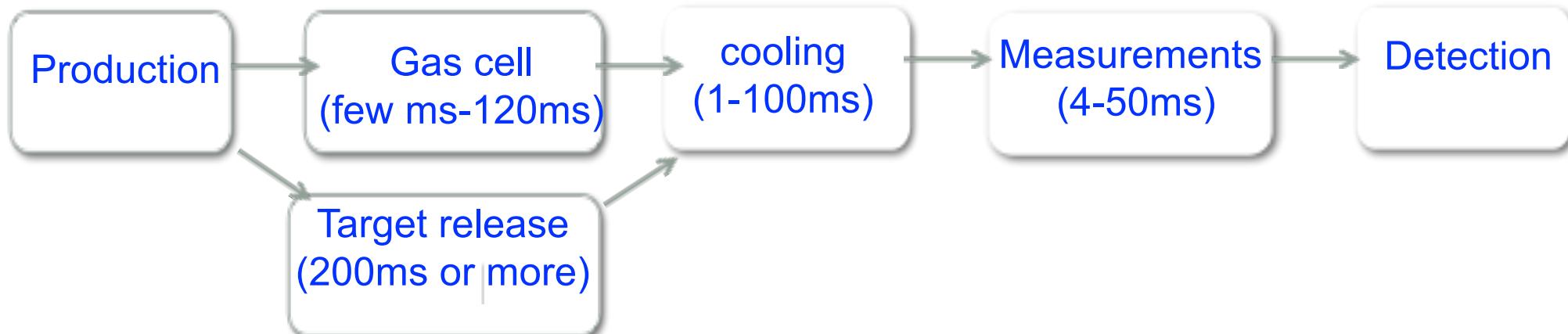


BigRIPS&Rare-RI Ring @RIBF



- ***background free and single ion sensitivity (event by even PID) of highly charged ions***

MRTOF/Penning-trap @ In-flight/ISOL- facilities



ISOL (chemical sensitivity)

- ***Cooled and bunched ion beam with backgrounds of molecules and adduct ions***

Proposed cases in RIKEN (No. 2)



Nuclear Astrophysics

vp-, rp-process
(waiting point, Zr-Nr cycle)
abundance of P-nuclei
($^{92,94}\text{Mo}$ and $^{96,98}\text{Ru}, ^{84}\text{Sr}$ isotopes)

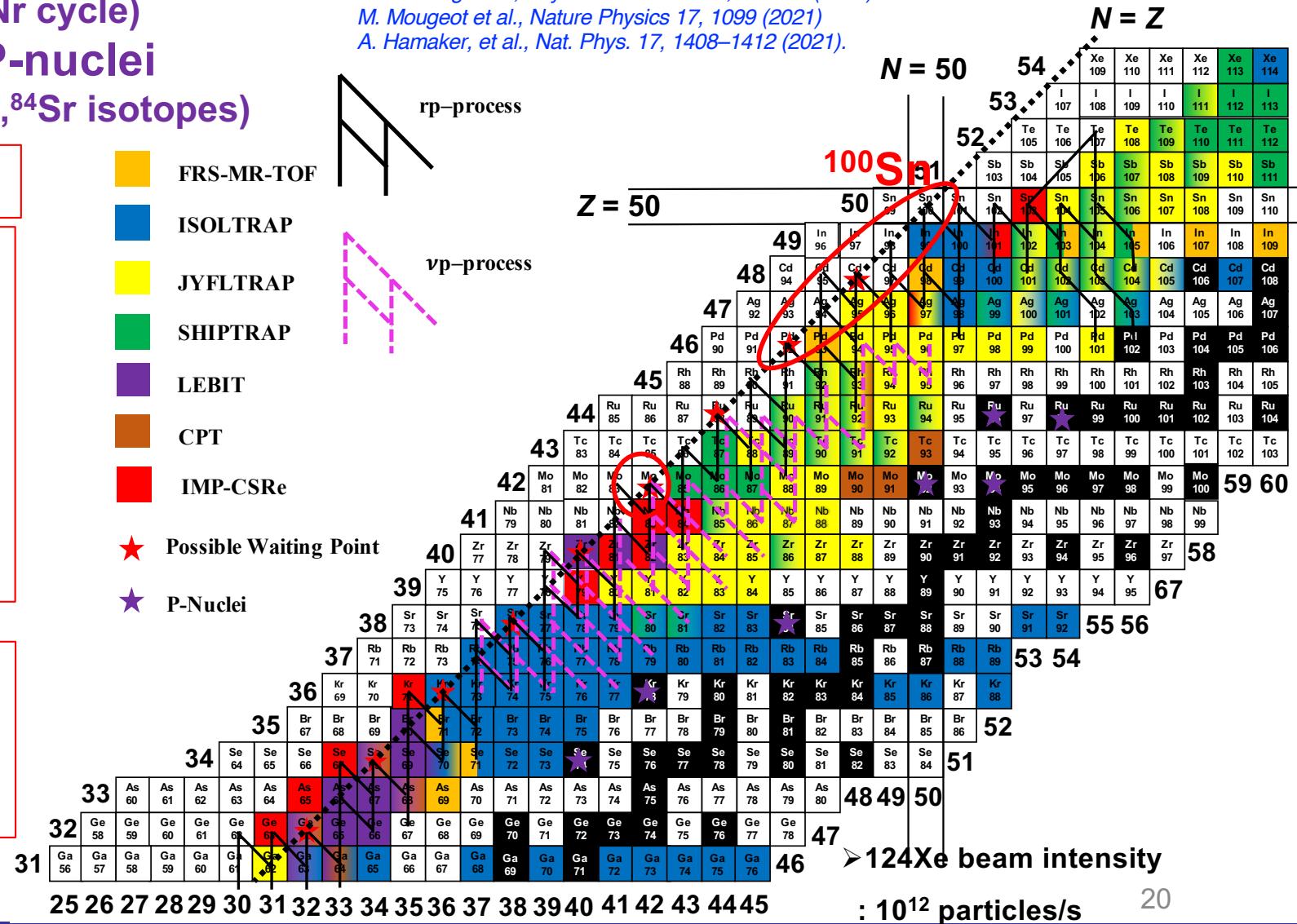
goals	
FRS-MR-TOF	
ISOLTRAP	
JYFLTRAP	
SHIPTRAP	
LEBIT	
CPT	
IMP-CSRe	
★ Possible Waiting Point	
★ P-Nuclei	
84Mo, 83Nb, 93Pd, 92Pd, 94Ag, 96Cd, 98In, 100Sn	
90Rh, 86Tc, 83Mo, 93Ag	
By-product: Magnetic- rigidity-time-of- flight (Bp-TOF) With BigRIPS in conjunction with OEDO beam-line	

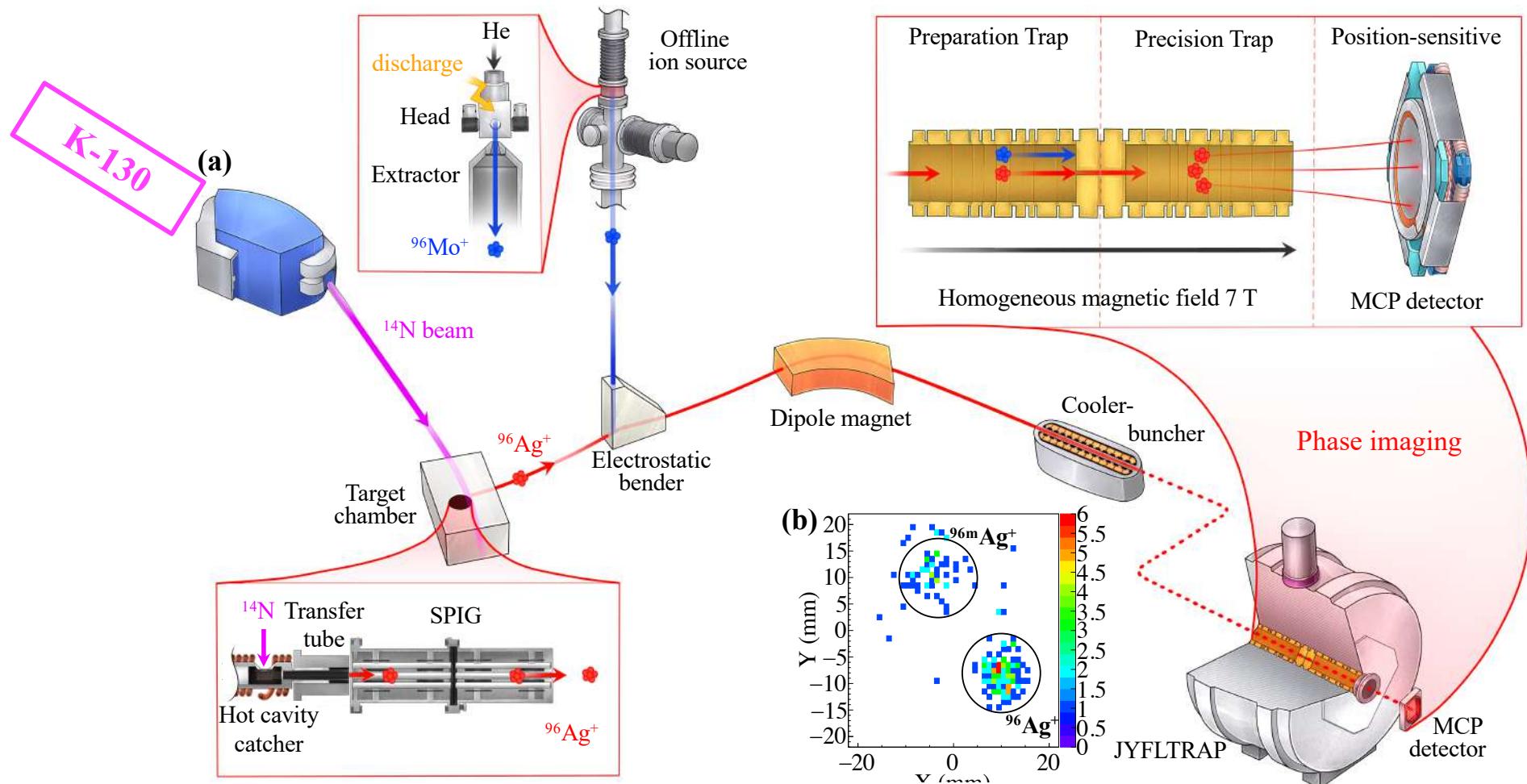
Main settings:
Isochronous
mass
spectrometry
(IMS)
By
Rare-RI Ring

By-product:
Magnetic-
rigidity-time-of-
flight
(Bp-TOF)
With
BigRIPS in
conjunction
with OEDO
beam-line

- C. Weber et al., Phys. Rev. C 78, 054310 (2008)
 V.-V. Elomaa et al., Phys. Rev. Lett. 102, 252501 (2011)
 E. Haettner et al., Phys. Rev. Lett. 106, 122501 (2011)
 F. Herfurth et al., Eur. Phys. J. A, 47, 75 (2011)
 X. Tu et al., Phys. Rev. Lett. 106, 112501 (2011)
 Y.M. Xing, et al., Physics Letters B 781 358–363 (2018)
 C. Hornung et al., Physics Letters B 802, 135200 (2020)
 M. Mougeot et al., Nature Physics 17, 1099 (2021)
 A. Hamaker, et al., Nat. Phys. 17, 1408–1412 (2021).

got 9 days
of beam time





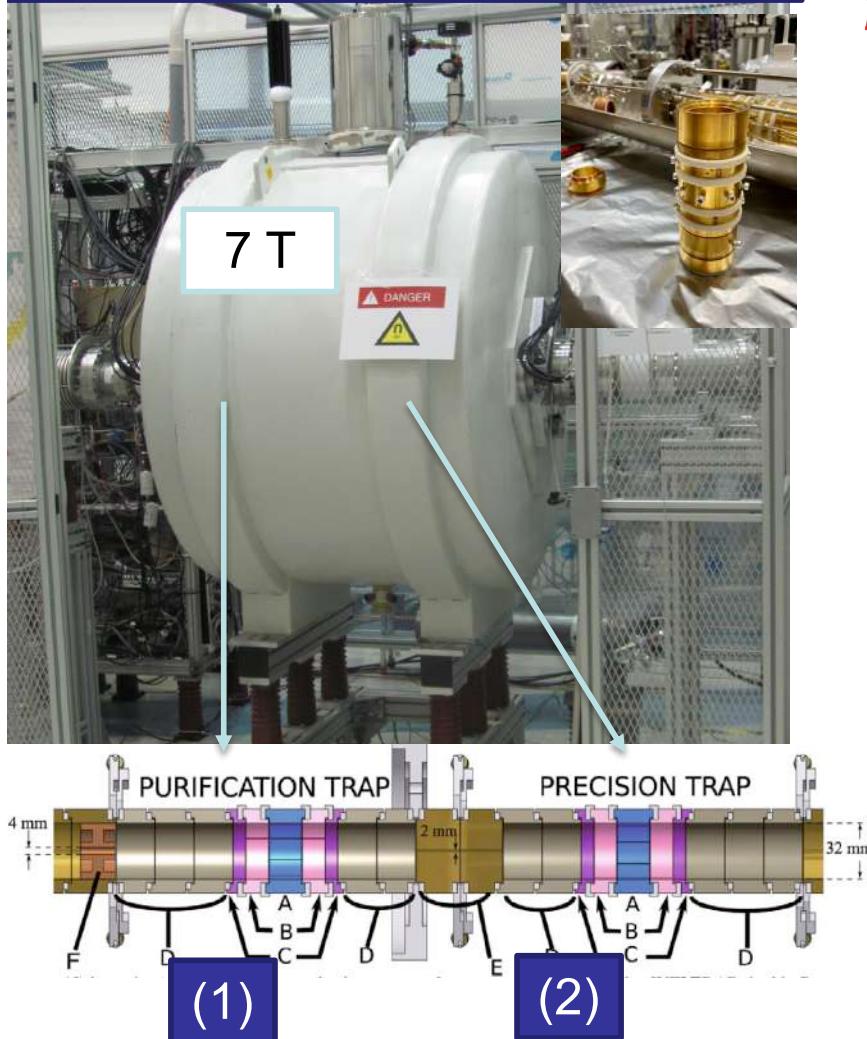
❖ Production of ions of interest:

- Proton beam of 5-65 MeV
- Proton-induced fission
- P/heavy ion-induced fusion-evaporation
- Target
 - ^{nat}U : 15mg/cm²
 - natural-abundance/enriched target ~ few mg/cm²

❖ Production of reference nucleus:

- Co-produced from the Target chamber
- Electrode of reference material installed in the spark source

JYFLTRAP double Penning trap



Eronen et al., EPJA 48 (2012) 46

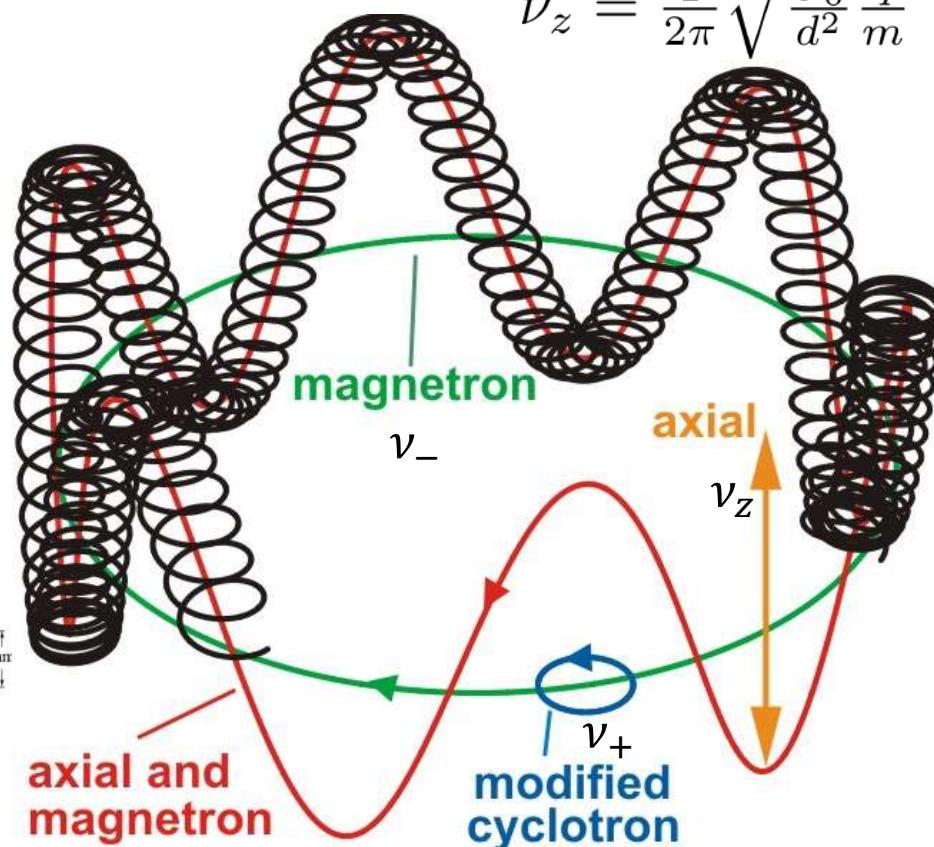
Cyclotron frequency

$$\nu_c = \frac{1}{2\pi} \frac{q}{m} B$$

Penning trap eigenfrequencies:

$$\nu_{\pm} = \frac{1}{2} \left(\nu_c \pm \sqrt{\nu_c^2 - 2\nu_z^2} \right)$$

$$\nu_z = \frac{1}{2\pi} \sqrt{\frac{U_0}{d^2}} \frac{q}{m}$$



Invariance theorem:

$$\nu_c^2 = \nu_-^2 + \nu_+^2 + \nu_z^2$$

95-97Ag mass measurements



94 48 Cd 46	95 48 Cd 47	96 48 Cd 48	97 48 Cd 49	98 48 Cd 50	99 48 Cd 51
80# ms 0+ M = 40440# (500#) β^+ ? $\beta^+ p^2$	32 ms 9/2+ M = 47060# (570#) β^+ ? 100% $\beta^+ p = 4.6$ (11%)	51 ms 10+ M = 53560# (600#) β^+ ? 100% $\beta^+ p = 4.6$ (11%)	103 ms 0+ M = 59360# (680#) β^+ ? 100% $\beta^+ p = 4.6$ (11%)	130 us 1/2+ M = 65160# (720#) β^+ ? 100% $\beta^+ p = 4.6$ (11%)	145 us 0+ M = 69160# (820#) β^+ ? 100% $\beta^+ p = 4.6$ (11%)
92 47 Ag 45	93 47 Ag 46	94 47 Ag 47	95 47 Ag 48	96 47 Ag 49	97 47 Ag 50
1# ms M = 37530# (400#) β^+ ? p^2	228 ns 9/2+ M = 46400# (400#) β^+ ? p^2	400 ns 21+ M = 52400# (400#) β^+ ? 100% $\beta^+ p = 0$	<16 ns 3/2+ M = 56300# (200#) β^+ ? 100% $\beta^+ p = 0$	170 us 9/2+ M = 59800# (400#) β^+ ? 100% $\beta^+ p = 0$	103.2 us 1/2+ M = 64100# (400#) β^+ ? 100% $\beta^+ p = 0$
91 46 Pd 45	92 46 Pd 46	93 46 Pd 47	94 46 Pd 48	95 46 Pd 49	96 46 Pd 50
32 ms 7/2+ M = 46170# (420#) β^+ ? 100% $\beta^+ p = 3.1$ (10%)	1.06 s 0+ M = 54780 (350) β^+ ? 100% $\beta^+ p = 1.8$ (2%)	1.17 s (9/2+) M = 58980 (370) β^+ ? 100% $\beta^+ p = 7.4$ (2%)	208 ns 1/2+ M = 57700 (100) β^+ ? 100% $\beta^+ p = 0$	13.3 s (21/2+) Ex 1075.1 (0.14) β^+ ? 89 (3%) $\beta^+ p = 11.3$ (3%)	7.4 s 9/2+ Ex 1051.3 (0.14) β^+ ? 100% $\beta^+ p = 23.5$ (5%)
95 Silver Z: 47 N: 48 Base : NUBASE Parity (Z,N) : all ASS ACCURACY (keV) u < 1 1 ≤ u < 2 2 ≤ u < 4 4 ≤ u < 12 12 ≤ u < 60 60 ≤ u < 200 200 ≤ u Extrapolated Mass Unknown Mass					

Cyclotron frequency:

$$\nu_c = \nu_+ + \nu_- = \frac{qB}{2\pi m}$$

Frequency ratio r :

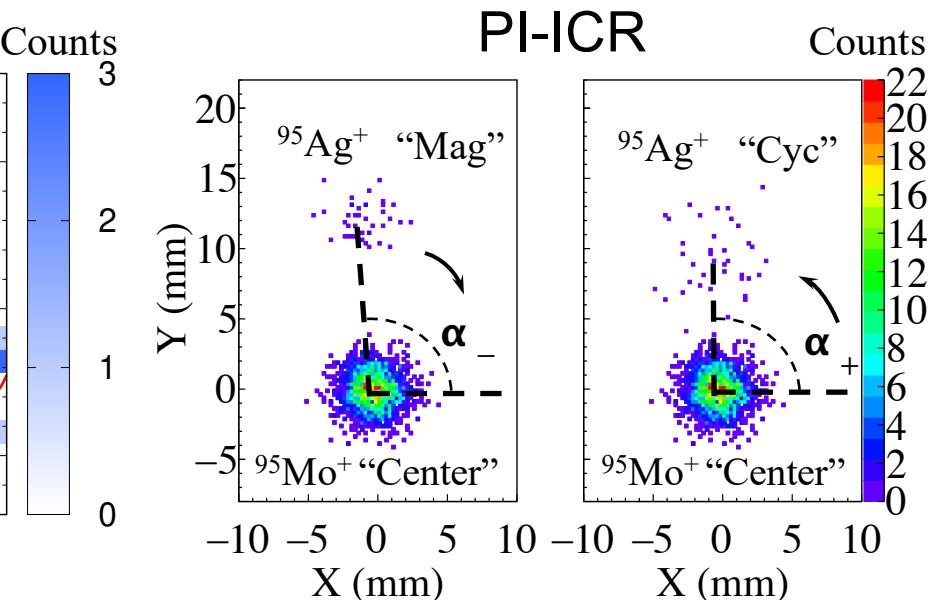
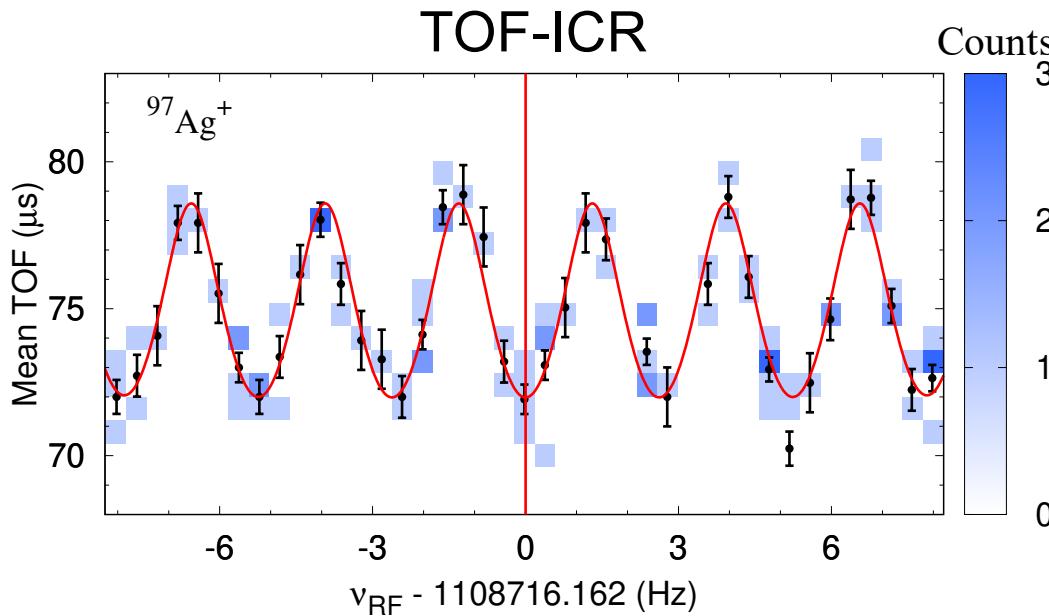
$$r = \frac{\nu_1}{\nu_2}$$

Q -value:

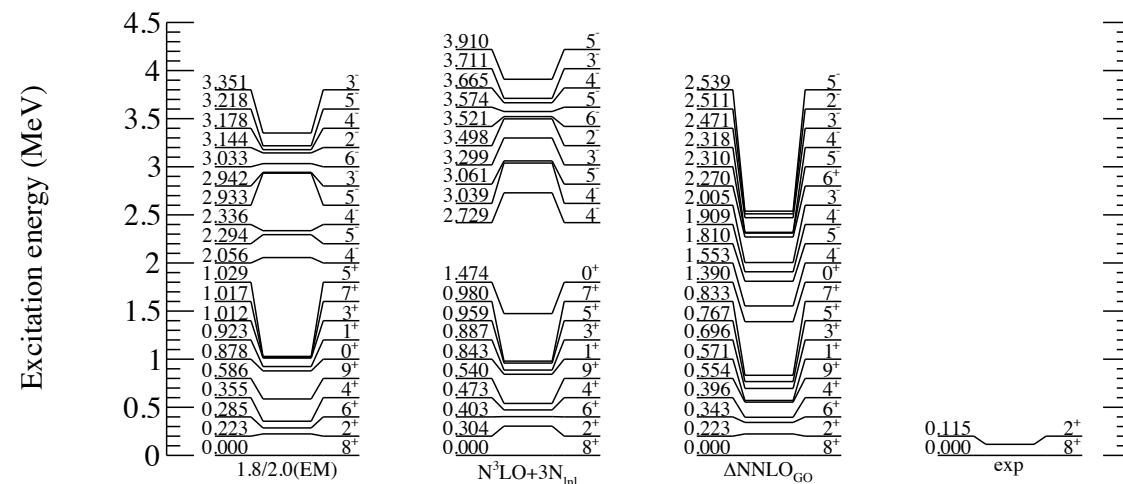
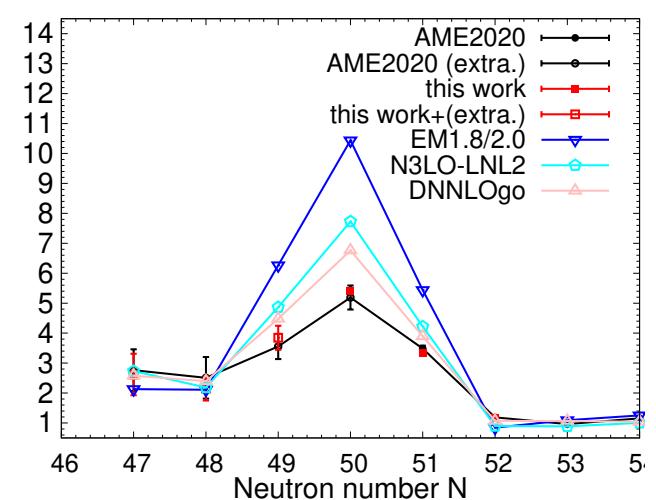
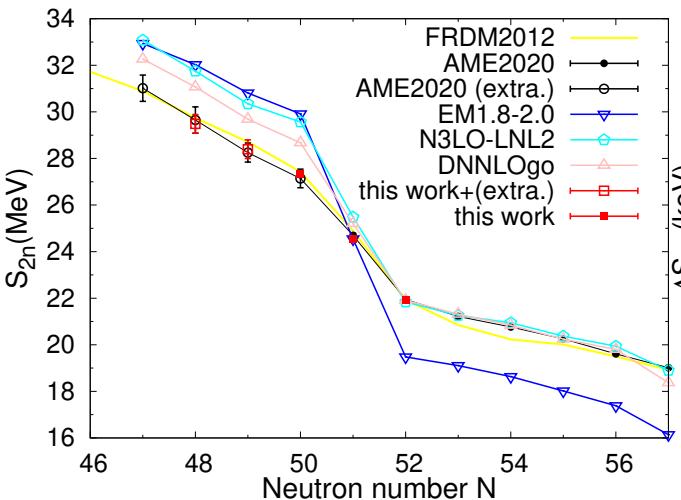
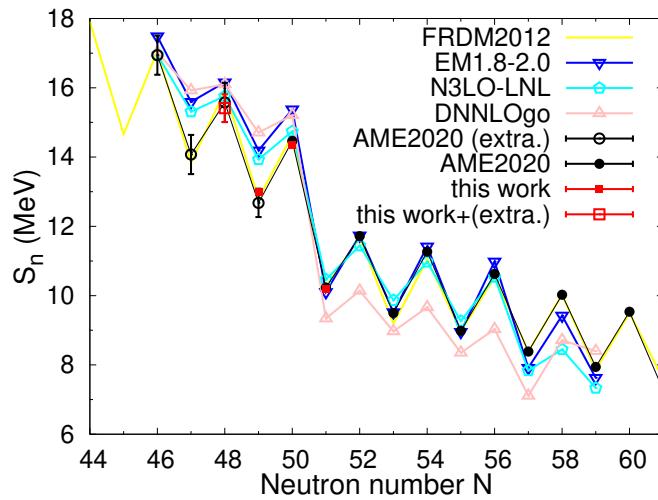
$$Q = M_2 - M_1 = (r - 1)(M_1 - m_e) + m_e$$

Mass:

$$M_2 = r(M_1 - m_e) + m_e$$

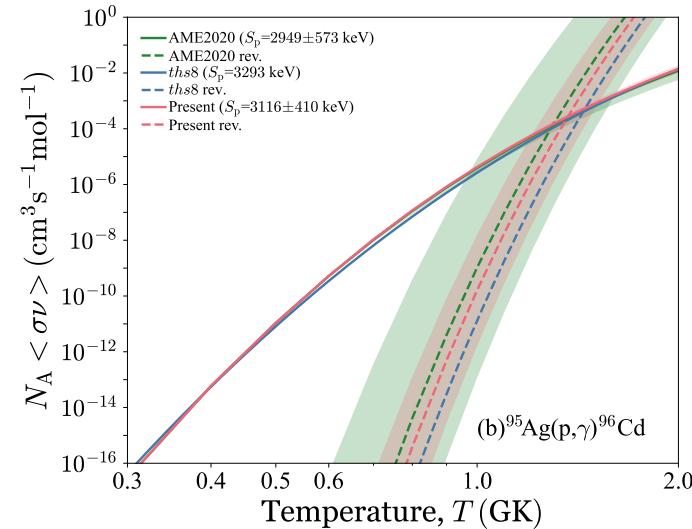
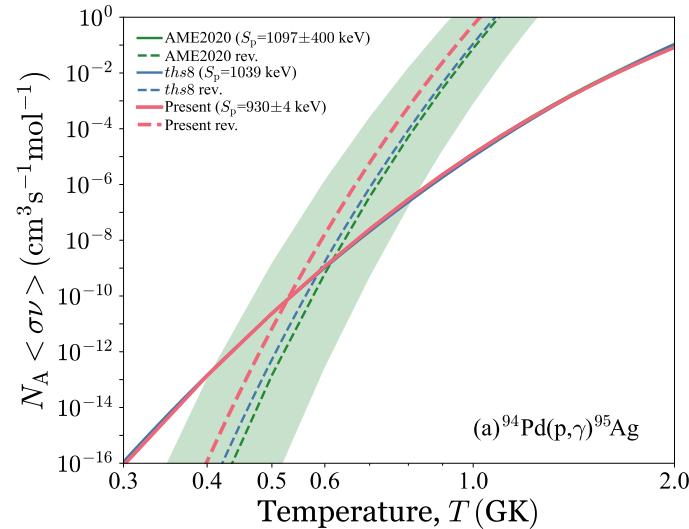


ab-initio calculation crosswa the N=50 shell

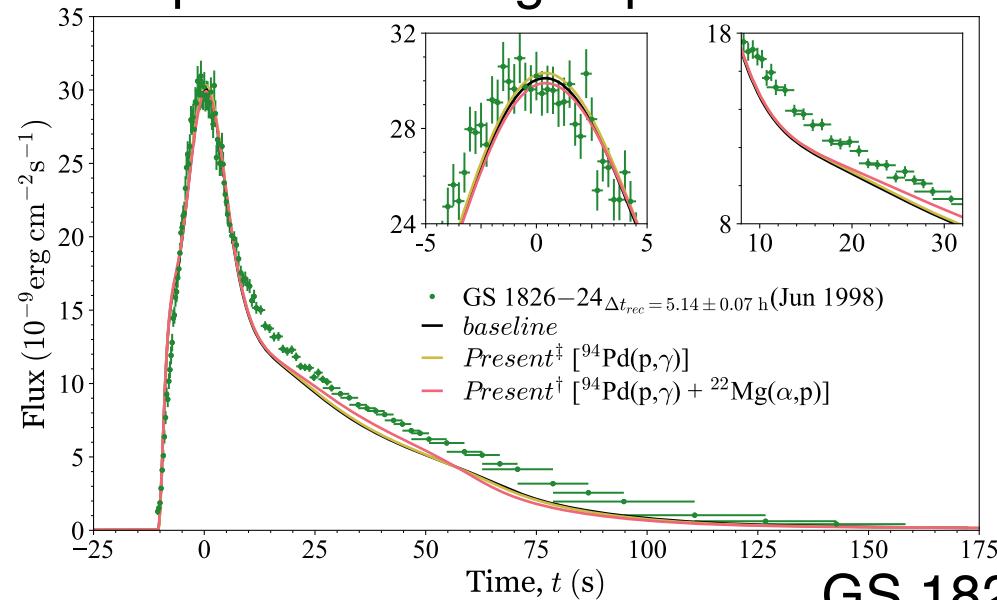


energy level of 96Ag isomeric state

*Influence on Forward and reverse
thermonuclear reaction rates*



Impact on averaged periodic burst light curves



GS 1826-24 clocked burster

Summary and outlook

- ❖ Technique developments at R3 and Mass measurements with IMS and Brho-TOF method
 - Ion of interest selection and Particle identification
 - Optics design
 - mass measurement with IMS with R3
 - mass measurements with Brho-TOF method at the BigRIPS-OEDO beamline
 - Mass measurements with complementary methods at RIBF
- ❖ Mass measurements of ground states and isomers by fusion evaporation reactions at IGISOL with JYFLTRAP
 - mass measurements of ^{95}Ag for the first time
 - New direct mass measurement of $^{96-97}\text{Ag}$ and first direct measurement of the isomer ^{96m}Ag
 - Ab-initio calculations of nuclear binding for the Ag isotopes and implications of N=50 shell
 - Impact on nuclear astrophysics
- ❖ Outlook: towards more exotic nuclei for mass measurements of heavy $N=Z$ nuclei up to ^{100}Sn @ **IGISOL/RIKEN/GSI-FAIR**
 - **Mass measurement with IMS (storage ring), Brho-TOF (BigRIPS) at RIBF, JYFLTRAP, MROF at IGISOL and collaboration with MR-TOF at GSI-FAIR**

Acknowledgements



university of
groningen

UNIVERSITY OF JYVÄSKYLÄ



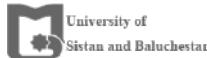
UPPSALA
UNIVERSITET

THE UNIVERSITY
of EDINBURGH



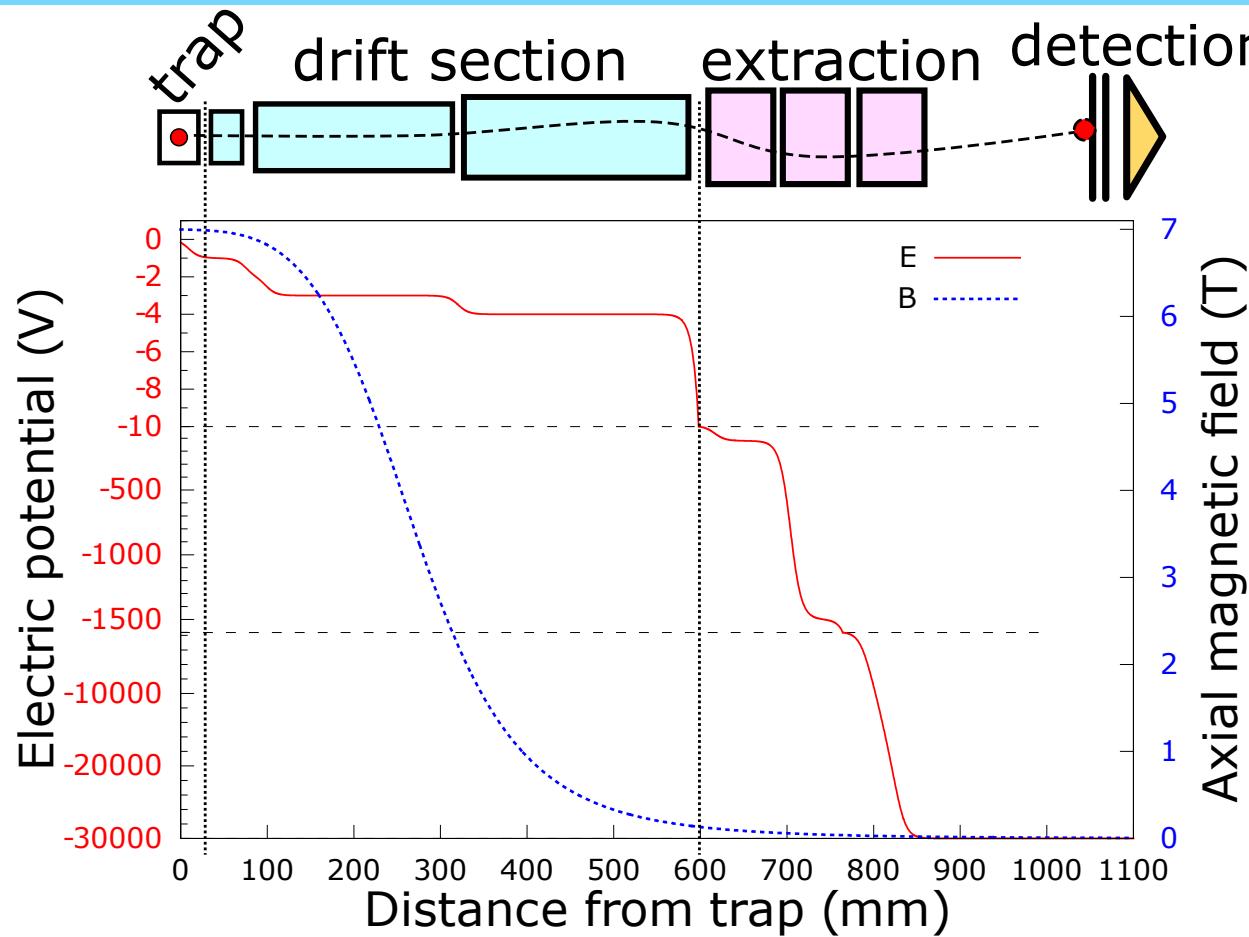
LUDWIG-
MAXIMILIANS-
UNIVERSITÄT
MÜNCHEN

MICHIGAN STATE
UNIVERSITY



Fundings: Academy of Finland under the Finnish Centre of Excellence Programme 2012-2017 (Nuclear and Accelerator Based Physics Research at JYFL) and projects No. 306980, 312544, 275389, 284516, 295207, 314733, 315179, 327629, 320062 and 345869. The support by the EU Horizon 2020 research and innovation programme under grant No. 771036 (ERC CoG MAIDEN) is acknowledged. This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No. 861198-LISA-H2020-MSCA-ITN-2019.

TOF-ICR method



Flight-of-time (TOF) from trap to MCP detector:

$$T(\omega) = \int_0^{z'} \sqrt{\frac{m}{2(E_0 - qU(z) - \mu B(z))}} dz$$

E_0 : initial axial kinetic energy of the ion,

$U(z)$: electrostatic potential and

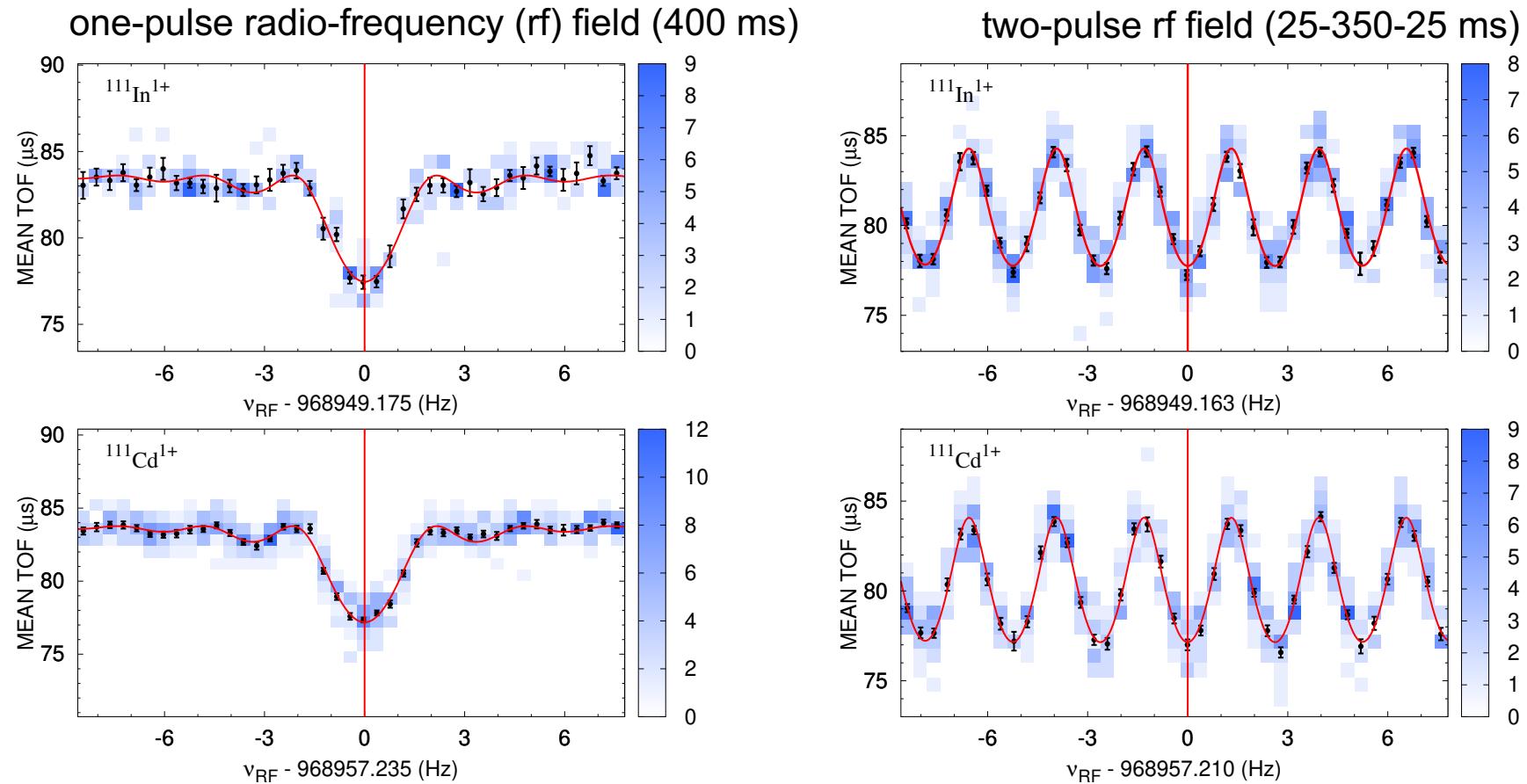
$B(z)$: the magnetic field along the flight path

T. Eronen et al. / Progress in Particle and Nuclear Physics 91 (2016) 259–293

Measurement procedure:

scanning the quadrupolar excitation frequency v_{RF} around the cyclotron frequency v_c and determining the frequency resulting in the shortest flight time from the trap to the MCP detector

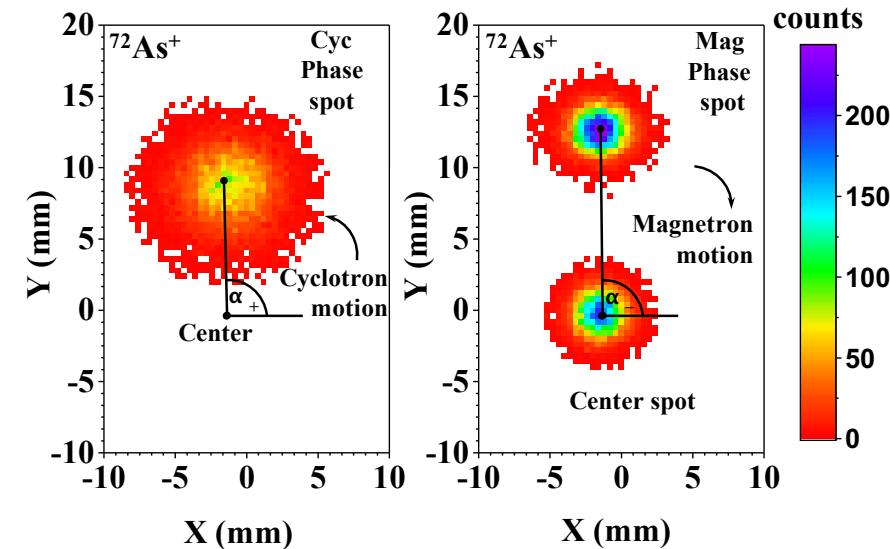
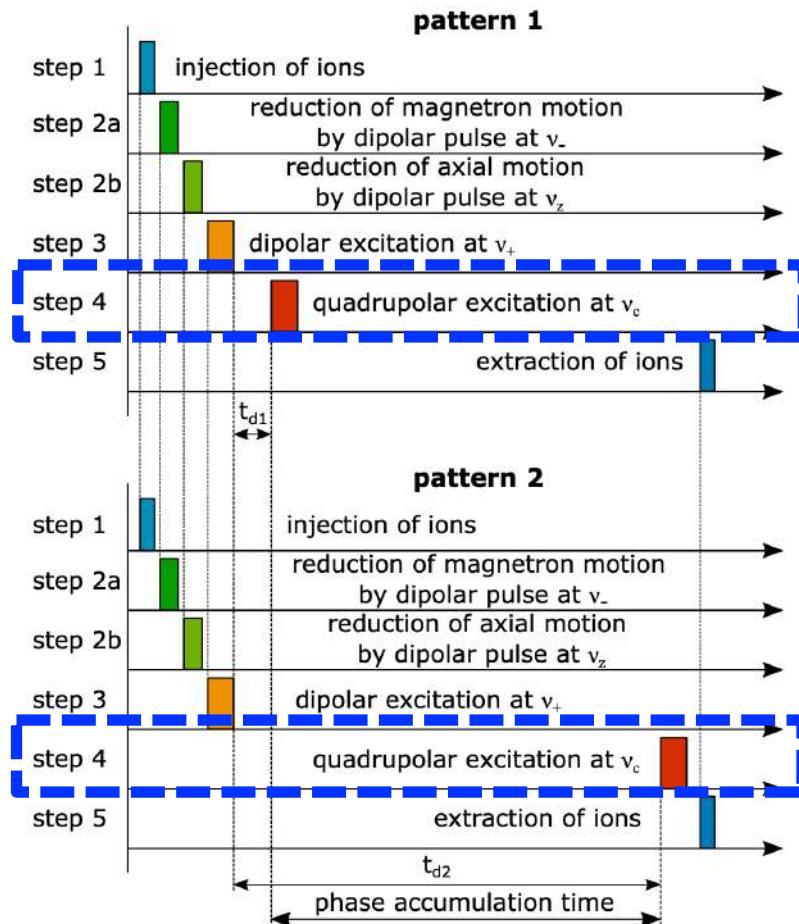
TOF-ICR method



Interleaved measurements of Ion-of-interest and reference (^{111}In and ^{111}Cd)

Phase-imaging Ion-Cyclotron-Resonance (PI-ICR)

KIRIN



Dipolar excitation at v_+

- Direct conversion to magnetron motion
→ Magnetron phase
- Accumulation then conversion to magnetron motion
→ Modified cyclotron phase

- Cyclotron frequency:

$$\nu_c = \nu_+ + \nu_- = \frac{qB}{2\pi m}$$

- Frequency ratio r :

$$r = \frac{\nu_1}{\nu_2}$$

Determine

Eronen et al., EPJA 48 (2012) 46

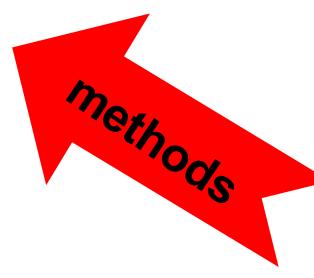
1. TOF-ICR

Time-of-Flight Ion-Cyclotron-Resonance (TOF-ICR) technique
G. Gräfft et al., Zeitschrift für Physik A: Atombaukunde 297, 35 (1980).

a. ICR
 b. Ramsey TOF-

2. PI-ICR

Phase-imaging Ion-Cyclotron-Resonance (PI-ICR) technique
S. Eliseev et al., Phys. Rev. Lett. 110, 082501 (2013).



- Q -value:

$$Q = M_2 - M_1 = (r - 1)(M_1 - m_e) + m_e$$

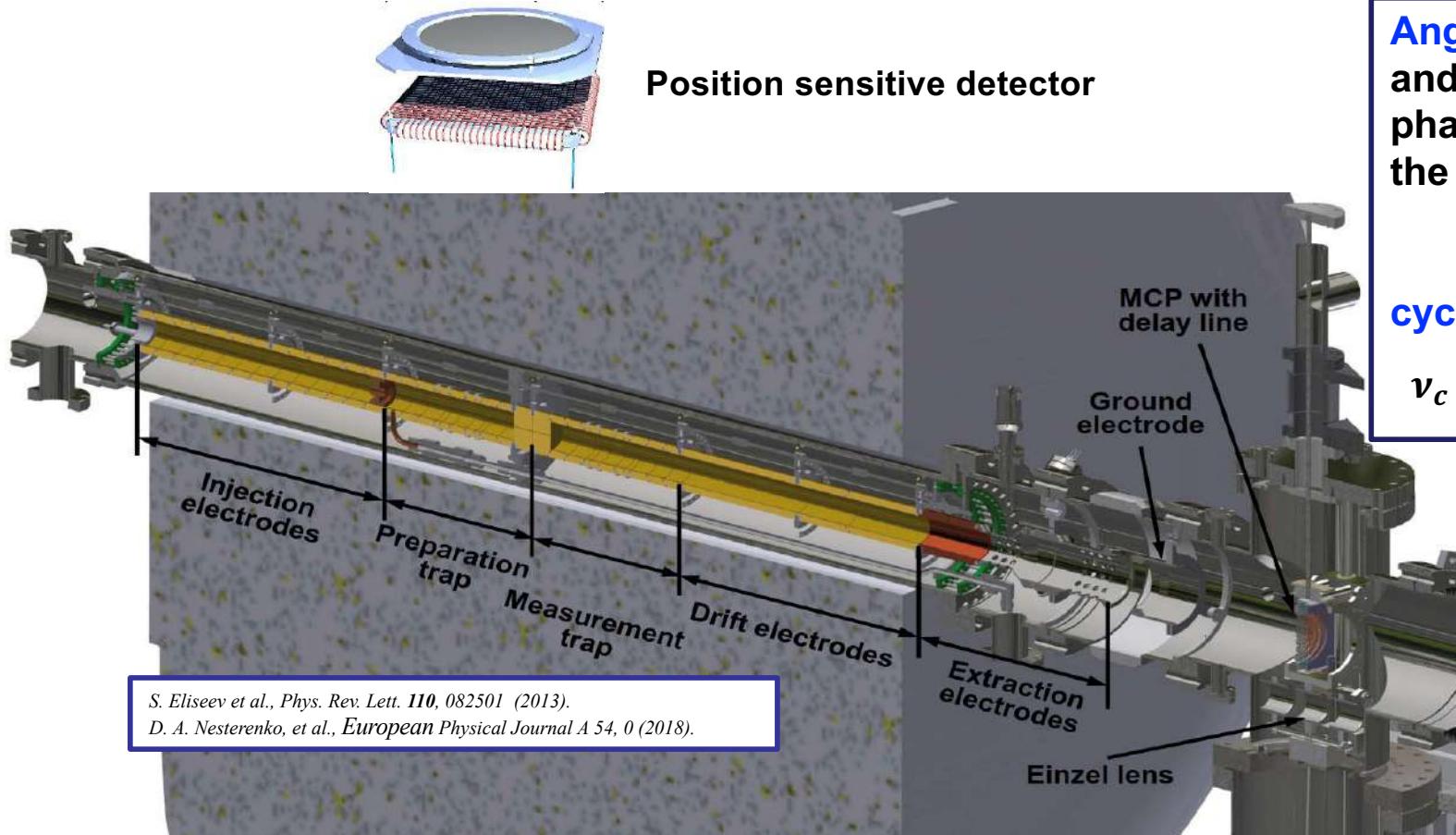
- Mass:

$$M_2 = r(M_1 - m_e) + m_e$$

Phase-imaging Ion-Cyclotron-Resonance (PI-ICR)

RIKEN

Delay-Line Microchanel Channel Plate (MCP) Detector from Roentdek GmbH



Angle between cyclotron and magnetron motion phases with respect to the center spot:

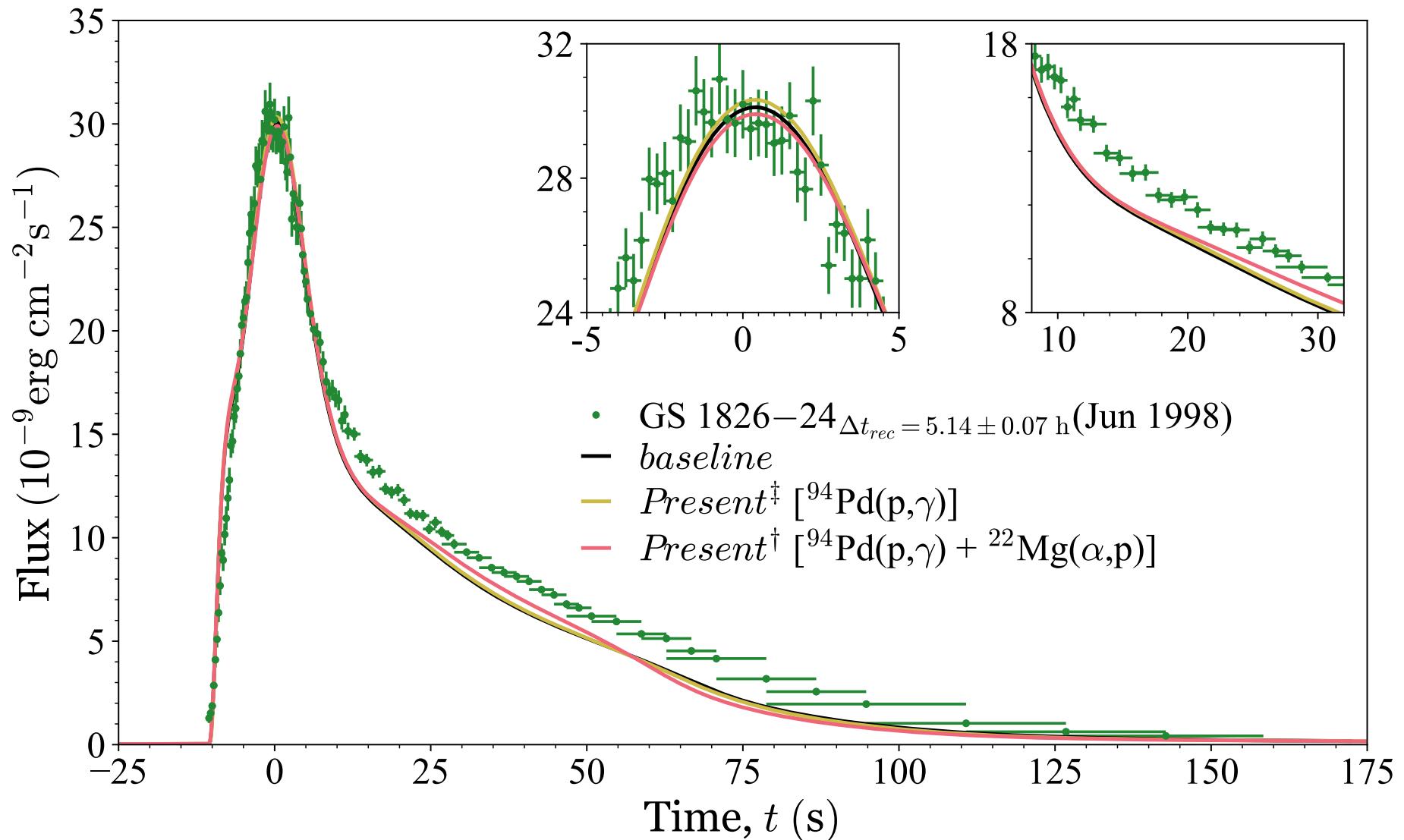
$$\alpha_c = \alpha_- + \alpha_+$$

cyclotron frequency:

$$\nu_c = \nu_+ + \nu_- = \frac{\alpha_c + 2\pi n}{2\pi t}$$

Impact on averaged periodic burst light curves

GS 1826–24 clocked burster



Detectors at beam-line

- Standard beam-line detectors at BigRIPS for TOF, $B\rho$, ΔE measurement for PID
- Clover-type Ge detectors for isomer measurement



(1). Delay-line PPAC



(2). Plastic Scintillator



(3). Ionization



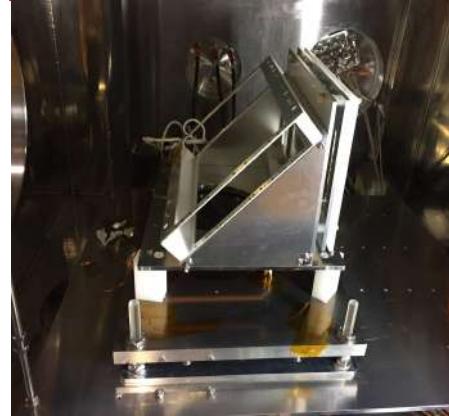
(4). BE-MCP



(5). γ -ray (Ge)
detector



(6). Si detector



(7). E-MCP

Function of detectors:

ΔE :

IC, Si

Isomer γ -ray:

Clover-Ge

TOF:

Scintillator, E-MCP,
BE-MCP

Position:

DL-PPAC, CD-PPAC

Collaboration list

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Theory
experiment

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⁸ School of Computing, Engineering and Mathematics, University of Brighton, Brighton BN2 4JG, United Kingdom

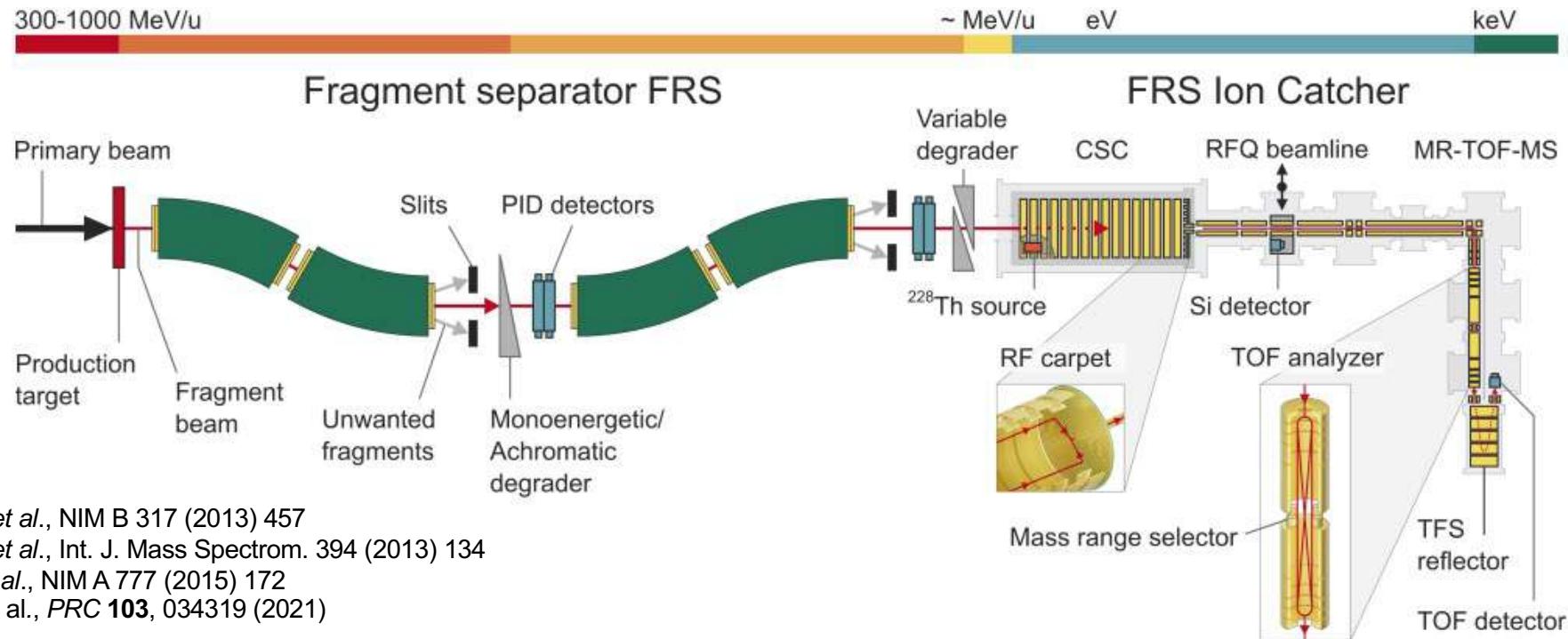
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Academy of Finland projects No. 306980, 312544, 275389, 284516, 295207, 314733 and 320062.

EU Horizon 2020 research and innovation program under grant No. 771036 (ERC CoG MAIDEN)

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J. Jaatinen and R. Seppälä, for preparing the production target



W.R. Plaß *et al.*, NIM B 317 (2013) 457

W.R. Plaß *et al.*, Int. J. Mass Spectrom. 394 (2013) 134

T. Dickel *et al.*, NIM A 777 (2015) 172

I. Mardor *et al.*, PRC 103, 034319 (2021)

❖ Fragment separator FRS:

- Production & separation of exotic nuclei via projectile fragmentation/fission

❖ Cryogenic Stopping cell (CSC):

- universal, fast, efficient stopping and extraction
- cooled short-lived ($T_{1/2} \sim \text{ms}$) exotic nuclei

❖ RF Quadrupole beamline:

- for low-energy ion transport
- Operate as a mass filter
- Background Suppression (molecular and ions)

76 m

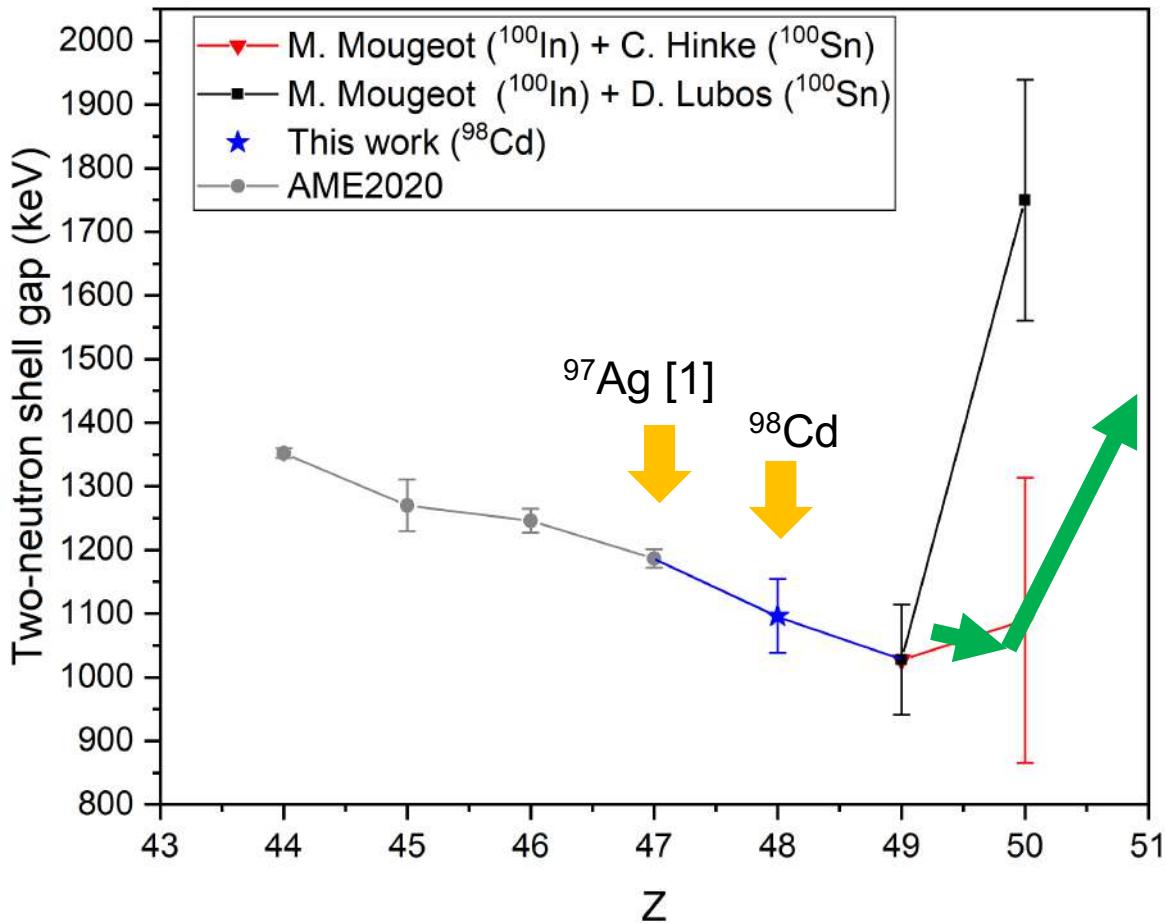
4 m

❖ MR-TOF-MS

fast, sensitive, broadband and non-scanning

- Resolving power: 1,000,000
- resolve isomers (hundreds of keV)
- Mass accuracy: 1.7×10^{-8}
- Sensitivity: a few detected ions
- Rate capacity: 10^6 ions/s
- Cycle times: a few ms

Two-neutron shell gap (shifted for $N+2$)



A. Mollaebrahimi et al., (*in preparation*)

$$\Delta_{2n}(Z, N+2) = ME(Z, N) - 2ME(Z, N+2) + ME(Z, N+4)$$

- The mass of ^{100}In is measured in [**M. Mugeot et al.**] paper and then the mass of ^{100}Sn is derived by using two Q_{EC} values from [**C. Hinke et al.**] and [**D. Lubos et al.**]
- The Q_{EC} from [**D. Lubos et al.**] was unfavorable in comparison to ab-initio calculation done in [**M. Mugeot et al.**]

M. Mugeot et al., *Nature Physics* (2021)

C. Hinke et al., *Nature* **486** (2012)

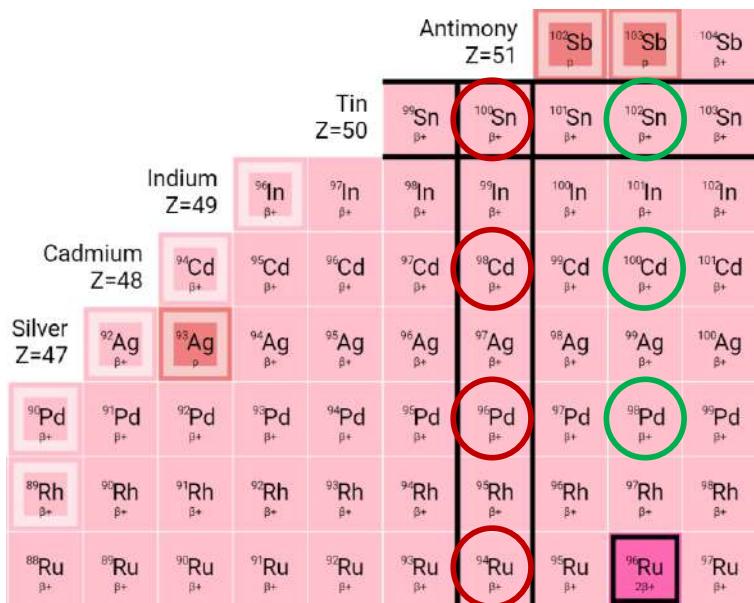
D. Lubos et al., *Physical Review Letters* **122** (2019)

[1] C. Hornung et al., *Physics Letters B* **802** (2020)

Gamow-Teller strength for even-even isotones at $N=50$

$$B(GT) = \frac{2\pi^3 \hbar^7 \ln(2)}{m_e^2 c^4 G_F^2 V_{ud}^2 (G_A/G_V)^2 f t_{1/2}} = \frac{3885 \pm 14 s}{f(z, \epsilon_0) t_{1/2}}$$

- Even-even isotones at $N=50$ with 0^+ initial states
- Proton from shell $1g_{9/2}$ changes to neutron in shell $1g_{7/2}$
- $B(GT)$ are calculated based on the latest (Q_{EC} , $t_{1/2}$ and decay scheme)



A. Plochocki et al., Zeitschrift fur Physik A 342 (1992)

A. Stoltz et al., GSI Scientific Reports 1 (2001)

A. Stoltz et al., AIP conference proceeding 610 (2002)

C. Hinke et al., Nature 486 (2012)

D. Lubos et al., Physical Review Letters 122 (2019)

A. Mollaebrahimi et al.

