

## ICPC REFERENCE NOTEBOOK

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### MACROS

```
#define s(n)          scanf("%d",&n)
#define sc(n)         scanf("%c",&n)
#define sl(n)         scanf("%ld",&n)
#define sll(n)        scanf("%lld",&n)
#define sf(n)         scanf("%lf",&n)
#define ssp(n)        scanf("%[^\n] %*c",n)
#define prt(x)        printf("%d\n",x);
#define plt(x)        printf("%lld\n",x);

#define INF           0x3f3f3f3f
#define EPS           1e-12

#define bitcount      __builtin_popcount
#define gcd            __gcd

#define forall(i,a,b)  for(int i=a;i<b;i++)
#define foreach(v, c)  for( typeof( (c).begin()) v = (c).begin(); v !=
(c).end(); ++v)
#define all(a)         a.begin(), a.end()
#define rall(a)        a.rbegin(),a.rend()

#define in(a,b)        ( (b).find(a) != (b).end())
#define pb            push_back
#define fill(a,v)      memset(a, v, sizeof a)
#define sz(a)          ((int)(a.size()))
#define mp            make_pair
#define dot(a,b)        ((conj(a)*(b)).X)
#define cross(a,b)      ((conj(a)*(b)).imag())
#define normalize(v)    ((v)/length(v))
#define rotate(p,about,theta) ((p-about)*exp(point(0,theta))+about)
#define pointEqu(a,b)   (comp(a.X,b.X)==0 && comp(a.Y,b.Y)==0)

#define maX(a,b)        ( (a) > (b) ? (a) : (b))
#define miN(a,b)        ( (a) < (b) ? (a) : (b))
#define checkbit(n,b)   ( (n >> b) & 1)
```

```
#define strjoin( x, y )      x ## y
#define DREP(a)              sort(all(a)); a.erase(unique(all(a)),a.end())
#define INDEX(arr,ind)       (lower_bound(all(arr),ind)-arr.begin())
```

```
typedef pair<int, int> ii;
typedef vector<ii> vii;
typedef vector<int> vi;
typedef stringstream ss;
typedef vector<string> vs;
typedef vector<double> vd;
typedef vector<vector<int>> vvi;
typedef long long ll;
typedef long double ld;
```

```
//g++ abc.cpp -o abc -DDEBUG
```

```
#ifdef DEBUG
```

```
    #define trace3(x,y,z)    cerr<<__FUNCTION__<<":"<<__LINE__<<":
"#x" = "<<x<<" | "#y" = "<<y<<" | "#z" = "<<z<<endl;
```

```
#else
```

```
    #define trace3(x,y,z)
```

```
#endif
```

### FUNCTIONS

#### FastRead

```
//ios::sync_with_stdio(false);
```

```
//#include<cstdio>
```

```
inline long long int frl()
```

```
{
```

```
    register long long int c=getchar();
```

```
    long long int x=0LL, neg=0LL;
```

```
    //Bool neg is better?
```

```
    for(; ((c<48LL || c>57LL) && c != '-' && c!=EOF); c = getchar());
```

```
    if(c==EOF) return EOF;
```

```
    if(c=='-')
```

```
    {
```

```
        neg = 1LL;
```

```
        c = getchar();
```

```

}
for(; c>47LL && c<58LL ; c = getchar()) {
    x = (x<<1LL) + (x<<3LL) + c - 48LL;
}
if(neg) x = -x;
return x;
}

```

### Power/GCD/LCM

```

ll power(ll a, ll b) {
    ll r = 1;
    while(b) {
        if(b & 1) r = r * a;
        a = a * a;
        b >>= 1;
    }
    return r;
}

```

```

ll gcd(ll a, ll b){
    return b==0?a:gcd(b,a%b);
}

```

```

ll lcm(ll a, ll b){
    return (a/gcd(a,b))*b;
}

```

```

nCr
long long C(int n, int r)
{
    if(r>n) return 0;
    if(r > n / 2) r = n - r; // because C(n, r) == C(n, n - r)
    long long ans = 1;
    int i;
    for(i = 1; i <= r; i++)
    {
        ans *= n - r + i;
        ans /= i;
    }
    return ans;
}

```

```

}

```

### Tobinary

```

int tobinary(bitset<8>x)
{
    string
    mystring=x.to_string<char,std::string::traits_type,std::string::allocator_type>
    e>();
    return atoi(mystring.c_str());
}

```

### a<sup>b</sup> mod T

```

/* Iterative Function to calculate (x^n)%p in O(logy) */
int power(int x, unsigned int y, int p)
{
    int res = 1;    // Initialize result
    x = x % p; // Update x if it is more than or equal to p
    while (y > 0)
    {
        // If y is odd, multiply x with result
        if (y & 1)
            res = (res*x) % p;

        // y must be even now
        y = y>>1; // y = y/2
        x = (x*x) % p;
    }
    return res;
}

```

### Modulo Arithmetic

```

#include<iostream>
#include<cstdio>
using namespace std;

```

```

int fast_pow(long long base, long long n, long long M)
{
    if(n==0)
        return 1;
}

```

```

    if(n==1)
    return base;
    long long halfn=fast_pow(base,n/2,M);
    if(n%2==0)
        return ( halfn * halfn ) % M;
    else
        return ( ( halfn * halfn ) % M ) * base ) % M;
}
int findMMI_fermat(int n,int M)
{
    return fast_pow(n,M-2,M);
}
int main()
{
    long long fact[100001];
    fact[0]=1;
    int i=1;
    int MOD=1000000007;
    while(i<=100000)
    {
        fact[i]=(fact[i-1]*i)%MOD;
        i++;
    }
    while(1)
    {
        int n,r;
        printf("Enter n: ");
        scanf(" %d",&n);
        printf("Enter r: ");
        scanf(" %d",&r);
        long long numerator,denominator,mmi_denominator,ans;
        numerator=fact[n];
        denominator=(fact[r]*fact[n-r])%MOD;
        mmi_denominator=findMMI_fermat(denominator,MOD);
        ans=(numerator*mmi_denominator)%MOD;
        printf("%lld\n",ans);
    }
    return 0;
}

```

## Base Conversion

```

int a,b; char sa[10000]; char sb[10000];
void rev(char s[]) {
    int l=strlen(s);
    for(int i=0; i<l-1-i; i++) swap(s[i],s[l-1-i]);
}
void multi(char s[], int k) {
    int i, c=0, d;
    for(i=0;s[i];i++)
    {
        d=(s[i]-'0')*k+c;
        c=d/b; d%=b;
        s[i]='0'+d;
    }
    while(c)
    {
        s[i]='0'+(c%b); i++;
        c/=b;
    }
    s[i]='\0';
}
void add(char s[], int k) {
    int i, c=k, d;
    for(i=0;s[i];i++)
    {
        d=(s[i]-'0')+c;
        c=d/b; d%=b;
        72
        s[i]='0'+d;
    }
    while(c)
    {
        s[i]='0'+(c%b); i++;
        c/=b;
    }
    s[i]='\0';
}
void trans(char s[]) {
    int i;
    for(i=0;s[i];i++)

```

```

    {
        char& c=s[i];
        if(c>='A' && c<='Z') c='0'+10+(c-'A');
        if(c>='a' && c<='z') c='0'+36+(c-'a');
    }
}

void itrans(char s[]) {
    int i;
    for(i=0;s[i];i++)
    {
        char& c=s[i]; int d=c-'0';
        if(d>=10 && d<=35) c='A'+(d-10);
        if(d>=36) c='a'+(d-36);
    }
}

int main() {
    int q; cin>>q;
    int i,j;
    while(q)
    {
        q--;
        cin>>a>>b>>sa; sb[0]='0'; sb[1]='\0';
        cout<<a<<" "<<sa<<endl;
        trans(sa);
        for(i=0;sa[i];i++)
        {
            multi(sb, a);
            add(sb, sa[i]-'0');
        }
        rev(sb);
        itrans(sb);
        cout<<b<<" "<<sb<<endl;
        cout<<endl;
    }
    return 0;
}

```

### Outline: O(n log n) algorithm for The Longest Increasing Subseq

```

set<int> st;
set<int>::iterator it;
...
st.clear();
for(i=0; i<n; i++)
{
    st.insert(a[i]); it=st.find(a[i]);
    it++; if(it!=st.end()) st.erase(it);
}
cout<<st.size()<<endl;

```

Outline: O(nm) algorithm for the LCS with O(n) sapce

```

    int m[2][1000]; // instead of [1000][1000]
    for(i=M; i>=0; i--)
    {
        ii = i&1;
        for(j=N; j>=0; j--)
        {
            if(i==M || j==N) { m[ii][j]=0; continue; }
            if(s1[i]==s2[j]) m[ii][j] = 1+m[1-ii][j+1];
            else m[ii][j] = max(m[ii][j+1], m[1-ii][j]);
        }
    }
    cout<<m[0][0]; // if you want m[x][y], write m[x&1][y];

```

### Manacher's Algo O(2n)

```

// Transform S into T.
// For example, S = "abba", T = "^#a#b#b#a#$".
// ^ and $ signs are sentinels appended to each end to avoid bounds checking
string preProcess(string s) {
    int n = s.length();
    if (n == 0) return "^$";
    string ret = "^";
    for (int i = 0; i < n; i++)
        ret += "#" + s.substr(i, 1);

    ret += "$";
    return ret;
}

```

```

string longestPalindrome(string s) {
    string T = preProcess(s);
    int n = T.length();
    int *P = new int[n];
    int C = 0, R = 0;
    for (int i = 1; i < n-1; i++) {
        int i_mirror = 2*C-i; // equals to i' = C - (i-C)

        P[i] = (R > i) ? min(R-i, P[i_mirror]) : 0;

        // Attempt to expand palindrome centered at i
        while (T[i + 1 + P[i]] == T[i - 1 - P[i]])
            P[i]++;

        // If palindrome centered at i expand past R,
        // adjust center based on expanded palindrome.
        if (i + P[i] > R) {
            C = i;
            R = i + P[i];
        }
    }

    // Find the maximum element in P.
    int maxLen = 0;
    int centerIndex = 0;
    for (int i = 1; i < n-1; i++) {
        if (P[i] > maxLen) {
            maxLen = P[i];
            centerIndex = i;
        }
    }
    delete[] P;

    return s.substr((centerIndex - 1 - maxLen)/2, maxLen);
}

```

## KMP O(n)

```

#include <cstdio>
#include <cstring>
#include <time.h>
using namespace std;

#define MAX_N 100010

char T[MAX_N], P[MAX_N]; // T = text, P = pattern
int b[MAX_N], n, m; // b = back table, n = length of T, m = length of P

void naiveMatching() {
    for (int i = 0; i < n; i++) { // try all potential starting indices
        bool found = true;
        for (int j = 0; j < m && found; j++) // use boolean flag `found'
            if (i + j >= n || P[j] != T[i + j]) // if mismatch found
                found = false; // abort this, shift starting index i by +1
        if (found) // if P[0 .. m - 1] == T[i .. i + m - 1]
            printf("P is found at index %d in T\n", i);
    }
}

void kmpPreprocess() { // call this before calling kmpSearch()
    int i = 0, j = -1; b[0] = -1; // starting values
    while (i < m) { // pre-process the pattern string P
        while (j >= 0 && P[i] != P[j]) j = b[j]; // if different, reset j using b
        i++; j++; // if same, advance both pointers
        b[i] = j; // observe i = 8, 9, 10, 11, 12 with j = 0, 1, 2, 3, 4
    } // in the example of P = "SEVENTY SEVEN" above
}

void kmpSearch() { // this is similar as kmpPreprocess(), but on string T
    int i = 0, j = 0; // starting values
    while (i < n) { // search through string T
        while (j >= 0 && T[i] != P[j]) j = b[j]; // if different, reset j using b
        i++; j++; // if same, advance both pointers
        if (j == m) { // a match found when j == m
            printf("P is found at index %d in T\n", i - j);
            j = b[j]; // prepare j for the next possible match
        }
    }
}

int main() {

```

```

strcpy(T, "I DO NOT LIKE SEVENTY SEV BUT SEVENTY SEVENTY
SEVEN");
strcpy(P, "SEVENTY SEVEN");
n = (int)strlen(T);
m = (int)strlen(P);

```

```

//if the end of line character is read too, uncomment the line below
//T[n-1] = 0; n--; P[m-1] = 0; m--;

```

```

printf("T = '%s'\n", T);
printf("P = '%s'\n", P);
naiveMatching();
printf("KMP\n");
kmpPreprocess();
kmpSearch();
printf("String Library\n");
char *pos = strstr(T, P);
while (pos != NULL) {
    printf("P is found at index %d in T\n", pos - T);
    pos = strstr(pos + 1, P);
}
return 0;
}

```

### Subset Sum Problem $O(\text{sum} * n)$

```

// Returns true if there is a subset of set[] with sun equal to given sum
bool isSubsetSum(int set[], int n, int sum)
{
    // The value of subset[i][j] will be true if there is a
    // subset of set[0..j-1] with sum equal to i
    bool subset[sum+1][n+1];

    // If sum is 0, then answer is true
    for (int i = 0; i <= n; i++)
        subset[0][i] = true;

    // If sum is not 0 and set is empty, then answer is false
    for (int i = 1; i <= sum; i++)
        subset[i][0] = false;

```

```

// Fill the subset table in bottom up manner
for (int i = 1; i <= sum; i++)
{
    for (int j = 1; j <= n; j++)
    {
        subset[i][j] = subset[i][j-1];
        if (i >= set[j-1])
            subset[i][j] = subset[i][j] ||
                subset[i - set[j-1]][j-1];
    }
}

/* // uncomment this code to print table
for (int i = 0; i <= sum; i++)
{
    for (int j = 0; j <= n; j++)
        printf ("%4d", subset[i][j]);
    printf("\n");
} */

return subset[sum][n];
}

```

```

int main()
{
    int set[] = {3, 34, 4, 12, 5, 2};
    int sum = 9;
    int n = sizeof(set)/sizeof(set[0]);
    if (isSubsetSum(set, n, sum) == true)
        printf("Found a subset with given sum");
    else
        printf("No subset with given sum");
    return 0;
}

```

## Prime Sieve of Eratosthenes

```
typedef long long ll;
typedef vector<int> vi;
typedef map<int, int> mii;
```

```
ll _sieve_size;
bitset<10000010> bs; // 10^7 should be enough for most cases
vi primes; // compact list of primes in form of vector<int>
```

// first part

```
void sieve(ll upperbound) { // create list of primes in [0..upperbound]
    _sieve_size = upperbound + 1; // add 1 to include upperbound
    bs.set(); // set all bits to 1
    bs[0] = bs[1] = 0; // except index 0 and 1
    for (ll i = 2; i <= _sieve_size; i++) if (bs[i]) {
        // cross out multiples of i starting from i * i!
        for (ll j = i * i; j <= _sieve_size; j += i) bs[j] = 0;
        primes.push_back((int)i); // also add this vector containing list of primes
    } // call this method in main method
```

```
bool isPrime(ll N) { // a good enough deterministic prime tester
    if (N <= _sieve_size) return bs[N]; // O(1) for small primes
    for (int i = 0; i < (int)primes.size(); i++)
        if (N % primes[i] == 0) return false;
    return true; // it takes longer time if N is a large prime!
} // note: only work for N <= (last prime in vi "primes")^2
```

// second part

```
vi primeFactors(ll N) { // remember: vi is vector of integers, ll is long long
    vi factors; // vi `primes' (generated by sieve) is optional
    ll PF_idx = 0, PF = primes[PF_idx]; // using PF = 2, 3, 4, ..., is also ok
    while (N != 1 && (PF * PF <= N)) { // stop at sqrt(N), but N can get smaller
        while (N % PF == 0) { N /= PF; factors.push_back(PF); } // remove this PF
        PF = primes[++PF_idx]; // only consider primes!
    }
    if (N != 1) factors.push_back(N); // special case if N is actually a prime
```

```
    return factors; // if pf exceeds 32-bit integer, you have to change vi
}
```

// third part

```
ll numPF(ll N) {
    ll PF_idx = 0, PF = primes[PF_idx], ans = 0;
    while (N != 1 && (PF * PF <= N)) {
        while (N % PF == 0) { N /= PF; ans++; }
        PF = primes[++PF_idx];
    }
    if (N != 1) ans++;
    return ans;
}
```

```
ll numDiffPF(ll N) {
    ll PF_idx = 0, PF = primes[PF_idx], ans = 0;
    while (N != 1 && (PF * PF <= N)) {
        if (N % PF == 0) ans++; // count this pf only once
        while (N % PF == 0) N /= PF;
        PF = primes[++PF_idx];
    }
    if (N != 1) ans++;
    return ans;
}
```

```
ll sumPF(ll N) {
    ll PF_idx = 0, PF = primes[PF_idx], ans = 0;
    while (N != 1 && (PF * PF <= N)) {
        while (N % PF == 0) { N /= PF; ans += PF; }
        PF = primes[++PF_idx];
    }
    if (N != 1) ans += N;
    return ans;
}
```

```
ll numDiv(ll N) {
    ll PF_idx = 0, PF = primes[PF_idx], ans = 1; // start from ans = 1
    while (N != 1 && (PF * PF <= N)) {
        ll power = 0; // count the power
```

```

while (N % PF == 0) { N /= PF; power++; }
ans *= (power + 1);           // according to the formula
PF = primes[++PF_idx];
}
if (N != 1) ans *= 2;         // (last factor has pow = 1, we add 1 to it)
return ans;
}

ll sumDiv(ll N) {
ll PF_idx = 0, PF = primes[PF_idx], ans = 1;           // start from ans = 1
while (N != 1 && (PF * PF <= N)) {
ll power = 0;
while (N % PF == 0) { N /= PF; power++; }
ans *= ((ll)pow((double)PF, power + 1.0) - 1) / (PF - 1);    // formula
PF = primes[++PF_idx];
}
if (N != 1) ans *= ((ll)pow((double)N, 2.0) - 1) / (N - 1);    // last one
return ans;
}

ll EulerPhi(ll N) {
ll PF_idx = 0, PF = primes[PF_idx], ans = N;           // start from ans = N
while (N != 1 && (PF * PF <= N)) {
if (N % PF == 0) ans -= ans / PF;           // only count unique factor
while (N % PF == 0) N /= PF;
PF = primes[++PF_idx];
}
if (N != 1) ans -= ans / N;                 // last factor
return ans;
}

int main() {
// first part: the Sieve of Eratosthenes
sieve(10000000);           // can go up to 10^7 (need few seconds)
printf("%d\n", isPrime(2147483647));           // 10-digits prime
printf("%d\n", isPrime(136117223861LL));       // not a prime, 104729*1299709

// second part: prime factors
vi res = primeFactors(2147483647); // slowest, 2147483647 is a prime
for (vi::iterator i = res.begin(); i != res.end(); i++) printf("> %d\n", *i);

```

```

res = primeFactors(136117223861LL); // slow, 2 large pfactors
104729*1299709
for (vi::iterator i = res.begin(); i != res.end(); i++) printf("# %d\n", *i);

res = primeFactors(142391208960LL); // faster, 2^10*3^4*5*7^4*11*13
for (vi::iterator i = res.begin(); i != res.end(); i++) printf("! %d\n", *i);

//res = primeFactors((ll)(1010189899 * 1010189899)); // "error"
//for (vi::iterator i = res.begin(); i != res.end(); i++) printf("^ %d\n", *i);

// third part: prime factors variants
printf("numPF(%d) = %lld\n", 50, numPF(50)); // 2^1 * 5^2 => 3
printf("numDiffPF(%d) = %lld\n", 50, numDiffPF(50)); // 2^1 * 5^2 => 2
printf("sumPF(%d) = %lld\n", 50, sumPF(50)); // 2^1 * 5^2 => 2 + 5 + 5 = 12
printf("numDiv(%d) = %lld\n", 50, numDiv(50)); // 1, 2, 5, 10, 25, 50, 6 divisors
printf("sumDiv(%d) = %lld\n", 50, sumDiv(50)); // 1 + 2 + 5 + 10 + 25 + 50 = 93
printf("EulerPhi(%d) = %lld\n", 50, EulerPhi(50)); // 20 integers < 50 are
relatively prime with 50

return 0;
}

```

## Segment Tree

```

typedef vector<int> vi;
class SegmentTree {           // the segment tree is stored like a heap array
private: vi st, A;           // recall that vi is: typedef vector<int> vi;
int n;
int left(int p) { return p << 1; } // same as binary heap operations
int right(int p) { return (p << 1) + 1; }

void build(int p, int L, int R) {           // O(n log n)
if (L == R)           // as L == R, either one is fine
st[p] = L;           // store the index
else {           // recursively compute the values
build(left(p), L, (L + R) / 2);
build(right(p), (L + R) / 2 + 1, R);
int p1 = st[left(p)], p2 = st[right(p)];
st[p] = (A[p1] <= A[p2]) ? p1 : p2;
}
}

```



```
}}

```

```
int rmq(int p, int L, int R, int i, int j) { // O(log n)
    if (i > R || j < L) return -1; // current segment outside query range
    if (L >= i && R <= j) return st[p]; // inside query range

    // compute the min position in the left and right part of the interval
    int p1 = rmq(left(p), L, (L+R) / 2, i, j);
    int p2 = rmq(right(p), (L+R) / 2 + 1, R, i, j);

    if (p1 == -1) return p2; // if we try to access segment outside query
    if (p2 == -1) return p1; // same as above
    return (A[p1] <= A[p2]) ? p1 : p2; } // as in build routine

int update_point(int p, int L, int R, int idx, int new_value) {
    // this update code is still preliminary, i == j
    // must be able to update range in the future!
    int i = idx, j = idx;

    // if the current interval does not intersect
    // the update interval, return this st node value!
    if (i > R || j < L)
        return st[p];

    // if the current interval is included in the update range,
    // update that st[node]
    if (L == i && R == j) {
        A[i] = new_value; // update the underlying array
        return st[p] = L; // this index
    }

    // compute the minimum pition in the
    // left and right part of the interval
    int p1, p2;
    p1 = update_point(left(p), L, (L + R) / 2, idx, new_value);
    p2 = update_point(right(p), (L + R) / 2 + 1, R, idx, new_value);

    // return the pition where the overall minimum is
    return st[p] = (A[p1] <= A[p2]) ? p1 : p2;
}
```

```
public:

```

```
SegmentTree(const vi &_A) {
    A = _A; n = (int)A.size(); // copy content for local usage
    st.assign(4 * n, 0); // create large enough vector of zeroes
    build(1, 0, n - 1); // recursive build
}
```

```
int rmq(int i, int j) { return rmq(1, 0, n - 1, i, j); } // overloading

```

```
int update_point(int idx, int new_value) {
    return update_point(1, 0, n - 1, idx, new_value); }
};

```

```
int main() {
    int arr[] = { 18, 17, 13, 19, 15, 11, 20 }; // the original array
    vi A(arr, arr + 7); // copy the contents to a vector
    SegmentTree st(A);

```

```
    printf("    idx 0, 1, 2, 3, 4, 5, 6\n");
    printf("    A is {18,17,13,19,15, 11,20}\n");
    printf("RMQ(1, 3) = %d\n", st.rmq(1, 3)); // answer = index 2
    printf("RMQ(4, 6) = %d\n", st.rmq(4, 6)); // answer = index 5
    printf("RMQ(3, 4) = %d\n", st.rmq(3, 4)); // answer = index 4
    printf("RMQ(0, 0) = %d\n", st.rmq(0, 0)); // answer = index 0
    printf("RMQ(0, 1) = %d\n", st.rmq(0, 1)); // answer = index 1
    printf("RMQ(0, 6) = %d\n", st.rmq(0, 6)); // answer = index 5

```

```
    printf("    idx 0, 1, 2, 3, 4, 5, 6\n");
    printf("Now, modify A into {18,17,13,19,15,100,20}\n");
    st.update_point(5, 100); // update A[5] from 11 to 100
    printf("These values do not change\n");
    printf("RMQ(1, 3) = %d\n", st.rmq(1, 3)); // 2
    printf("RMQ(3, 4) = %d\n", st.rmq(3, 4)); // 4
    printf("RMQ(0, 0) = %d\n", st.rmq(0, 0)); // 0
    printf("RMQ(0, 1) = %d\n", st.rmq(0, 1)); // 1
    printf("These values change\n");
    printf("RMQ(0, 6) = %d\n", st.rmq(0, 6)); // 5->2
    printf("RMQ(4, 6) = %d\n", st.rmq(4, 6)); // 5->4
    printf("RMQ(4, 5) = %d\n", st.rmq(4, 5)); // 5->4

```

```
return 0;}
```

## Fenwick Tree

```
#include <iostream>
using namespace std;
#define LOGSZ 17
int tree[(1<<LOGSZ)+1];
int N = (1<<LOGSZ);
// add v to value at x
void set(int x, int v) {
    while(x <= N) {
        tree[x] += v;
        x += (x & -x);
    }
}
// get cumulative sum up to and including x
int get(int x) {
    int res = 0;
    while(x) {
        res += tree[x];
        x -= (x & -x);
    }
    return res;
}
// get largest value with cumulative sum less than or equal to x;
// for smallest, pass x-1 and add 1 to result
int getind(int x) {
    int idx = 0, mask = N;
    while(mask && idx < N) {
        int t = idx + mask;
        if(x >= tree[t]) {
            idx = t;
            x -= tree[t];
        }
        mask >>= 1;
    }
    return idx;
}
```

## String Trie

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <stdbool.h>
#define ARRAY_SIZE(a) sizeof(a)/sizeof(a[0])
// Alphabet size (# of symbols)
#define ALPHABET_SIZE (26)
// Converts key current character into index
// use only 'a' through 'z' and lower case
#define CHAR_TO_INDEX(c) ((int)c - (int)'a')

// trie node
struct TrieNode
{
    struct TrieNode *children[ALPHABET_SIZE];
    // isLeaf is true if the node represents
    // end of a word
    bool isLeaf;
};

// Returns new trie node (initialized to NULLs)
struct TrieNode *getNode(void)
{
    struct TrieNode *pNode = NULL;
    pNode = (struct TrieNode *)malloc(sizeof(struct TrieNode));
    if (pNode)
    {
        int i;
        pNode->isLeaf = false;
        for (i = 0; i < ALPHABET_SIZE; i++)
            pNode->children[i] = NULL;
    }
    return pNode;
}
// If not present, inserts key into trie
// If the key is prefix of trie node, just marks leaf node
void insert(struct TrieNode *root, const char *key)
{
    int level;
```

```

int length = strlen(key);
int index;
struct TrieNode *pCrawl = root;

for (level = 0; level < length; level++)
{
    index = CHAR_TO_INDEX(key[level]);
    if (!pCrawl->children[index])
        pCrawl->children[index] = getNode();
    pCrawl = pCrawl->children[index];
}
// mark last node as leaf
pCrawl->isLeaf = true;
}
// Returns true if key presents in trie, else false
bool search(struct TrieNode *root, const char *key)
{
    int level;
    int length = strlen(key);
    int index;
    struct TrieNode *pCrawl = root;

    for (level = 0; level < length; level++)
    {
        index = CHAR_TO_INDEX(key[level]);
        if (!pCrawl->children[index])
            return false;
        pCrawl = pCrawl->children[index];
    }
    return (pCrawl != NULL && pCrawl->isLeaf);
}

int main()
{
    // Input keys (use only 'a' through 'z' and lower case)
    char keys[][8] = { "the", "a", "there", "answer", "any",
                       "by", "bye", "their" };

    char output[][32] = { "Not present in trie", "Present in trie" };
    struct TrieNode *root = getNode();
    // Construct trie
    int i;

```

```

    for (i = 0; i < ARRAY_SIZE(keys); i++)
        insert(root, keys[i]);
    // Search for different keys
    printf("%s --- %s\n", "the", output[search(root, "the")]);
    printf("%s --- %s\n", "these", output[search(root, "these")]);
    printf("%s --- %s\n", "their", output[search(root, "their")]);
    printf("%s --- %s\n", "thaw", output[search(root, "thaw")]);
    return 0;
}

Dijkstra's Algo

// Implementation of Dijkstra's algorithm using adjacency lists
// and priority queue for efficiency.
// Running time: O(|E| log |V|)
const int INF = 2000000000;
typedef pair<int, int> PII;
int main() {
    int N, s, t;
    scanf("%d%d%d", &N, &s, &t);
    vector<vector<PII>> edges(N);
    for (int i = 0; i < N; i++) {
        int M;
        scanf("%d", &M);
        for (int j = 0; j < M; j++) {
            int vertex, dist;
            scanf("%d%d", &vertex, &dist);
            edges[i].push_back(make_pair(dist, vertex)); // note order
        }
    }
    // use priority queue in which top element has the "smallest" priority
    priority_queue<PII, vector<PII>, greater<PII>> Q;
    vector<int> dist(N, INF), dad(N, -1);
    Q.push(make_pair(0, s));
    dist[s] = 0;
    while (!Q.empty()) {
        PII p = Q.top();
        Q.pop();
        int here = p.second;
        if (here == t) break;
    }
}

```

```

        if (dist[here] != p.first) continue;
        for (vector<PII>::iterator it = edges[here].begin(); it !=
edges[here].end(); it++)
        {
            if (dist[here] + it->first < dist[it->second])
            {
                dist[it->second] = dist[here] + it->first;
                dad[it->second] = here;
                Q.push(make_pair(dist[it->second], it->second));
            }
        }
    }

    printf("%d\n", dist[t]);
    if (dist[t] < INF)
        for (int i = t; i != -1; i = dad[i])
            printf("%d%c", i, (i == s ? 'f' : 'f' * f * f));

    return 0;
}
/*
Sample input:
5 0 4
2 1 2 3 1
2 2 4 4 5
3 1 4 3 3 4 1
2 0 1 2 3
2 1 5 2 1
Expected:
5
4 2 3 0
*/

```

## Prim & Kruskal MST

```

typedef pair<int, int> ii;
typedef vector<int> vi;
typedef vector<ii> vii;

```

// Union-Find Disjoint Sets Library written in OOP manner, using both path compression and union by rank heuristics

```
class UnionFind { // OOP style
```

```

private:
    vi p, rank, setSize; // remember: vi is vector<int>
    int numSets;
public:
    UnionFind(int N) {
        setSize.assign(N, 1); numSets = N; rank.assign(N, 0);
        p.assign(N, 0); for (int i = 0; i < N; i++) p[i] = i; }
    int findSet(int i) { return (p[i] == i) ? i : (p[i] = findSet(p[i])); }
    bool isSameSet(int i, int j) { return findSet(i) == findSet(j); }
    void unionSet(int i, int j) {
        if (!isSameSet(i, j)) { numSets--;
            int x = findSet(i), y = findSet(j);
            // rank is used to keep the tree short
            if (rank[x] > rank[y]) { p[y] = x; setSize[x] += setSize[y]; }
            else { p[x] = y; setSize[y] += setSize[x];
                if (rank[x] == rank[y]) rank[y]++; } } }
    int numDisjointSets() { return numSets; }
    int sizeOfSet(int i) { return setSize[findSet(i)]; }
};

```

```

vector<vii> AdjList;
vi taken; // global boolean flag to avoid cycle
priority_queue<ii> pq; // priority queue to help choose shorter edges

```

```

void process(int vtx) { // so, we use -ve sign to reverse the sort order
    taken[vtx] = 1;
    for (int j = 0; j < (int)AdjList[vtx].size(); j++) {
        ii v = AdjList[vtx][j];
        if (!taken[v.first]) pq.push(ii(-v.second, -v.first));
    } // sort by (inc) weight then by (inc) id
}

```

```

int main() {
    int V, E, u, v, w;
    /*
    // Graph in Figure 4.10 left, format: list of weighted edges
    // This example shows another form of reading graph input
    5 7
    0 1 4
    0 2 4
    0 3 6
    0 4 6
    */
}

```

```

1 2 2
2 3 8
3 4 9
*/
freopen("in_03.txt", "r", stdin);

scanf("%d %d", &V, &E);
// Kruskal's algorithm merged with Prim's algorithm
AdjList.assign(V, vii());
vector< pair<int, ii> > EdgeList; // (weight, two vertices) of the edge
for (int i = 0; i < E; i++) {
    scanf("%d %d %d", &u, &v, &w); // read the triple: (u, v, w)
    EdgeList.push_back(make_pair(w, ii(u, v))); // (w, u, v)
    AdjList[u].push_back(ii(v, w));
    AdjList[v].push_back(ii(u, w));
}
sort(EdgeList.begin(), EdgeList.end()); // sort by edge weight O(E log E)
// note: pair object has built-in comparison function

int mst_cost = 0;
UnionFind UF(V); // all V are disjoint sets initially
for (int i = 0; i < E; i++) { // for each edge, O(E)
    pair<int, ii> front = EdgeList[i];
    if (!UF.isSameSet(front.second.first, front.second.second)) { // check
        mst_cost += front.first; // add the weight of e to MST
        UF.unionSet(front.second.first, front.second.second); // link them
    } } // note: the runtime cost of UFDS is very light

// note: the number of disjoint sets must eventually be 1 for a valid MST
printf("MST cost = %d (Kruskal's)\n", mst_cost);

// inside int main() --- assume the graph is stored in AdjList, pq is empty
taken.assign(V, 0); // no vertex is taken at the beginning
process(0); // take vertex 0 and process all edges incident to vertex 0
mst_cost = 0;
while (!pq.empty()) { // repeat until V vertices (E=V-1 edges) are taken
    ii front = pq.top(); pq.pop();
    u = -front.second, w = -front.first; // negate the id and weight again
    if (!taken[u]) // we have not connected this vertex yet
        mst_cost += w, process(u); // take u, process all edges incident to u
} // each edge is in pq only once!

```

```

printf("MST cost = %d (Prim's)\n", mst_cost);

```

```

return 0;

```

### DFS Depth First Search

```

class Graph

```

```

{
    int V; // No. of vertices
    list<int> *adj; // Pointer to an array containing adj lists
    void DFSUtil(int v, bool visited[]); // A func used by DFS
public:
    Graph(int V); // Constructor
    void addEdge(int v, int w); // function to add an edge to graph
    void DFS(); // prints DFS traversal of the complete graph
};

```

```

Graph::Graph(int V)

```

```

{
    this->V = V;
    adj = new list<int>[V];
}
void Graph::addEdge(int v, int w)
{
    adj[v].push_back(w); // Add w to v's list.
}
void Graph::DFSUtil(int v, bool visited[])
{
    visited[v] = true;
    cout << v << " ";

```

```

// Recur for all the vertices adjacent to this vertex
list<int>::iterator i;
for(i = adj[v].begin(); i != adj[v].end(); ++i)
    if(!visited[*i])
        DFSUtil(*i, visited);
}

```

```

// The function to do DFS traversal. It uses recursive DFSUtil()

```

```

void Graph::DFS()
{

```

```

// Mark all the vertices as not visited
bool *visited = new bool[V];
for (int i = 0; i < V; i++)
    visited[i] = false;

// Call the recursive helper function to print DFS traversal
// starting from all vertices one by one
for (int i = 0; i < V; i++)
    if (visited[i] == false)
        DFSUtil(i, visited);
}
int main()
{
    Graph g(4);
    g.addEdge(0, 1);
    g.addEdge(0, 2);
    g.addEdge(1, 2);
    g.addEdge(2, 0);
    g.addEdge(2, 3);
    g.addEdge(3, 3);

    cout << "Following is Depth First Traversal\n";
    g.DFS();

    return 0;
}

```

### BFS Breadth First Search

```
int V, E, a, b, s;
```

```
vector<vii> AdjList;
vi p;           // addition: the predecessor/parent vector
```

```
void printPath(int u) { // simple function to extract information from `vi p'
    if (u == s) { printf("%d", u); return; }
    printPath(p[u]); // recursive call: to make the output format: s -> ... -> t
    printf(" %d", u); }

```

```
int main() {
    /*

```

```

// format: list of unweighted edges
// This example shows another form of reading graph input
13 16
0 1  1 2  2 3  0 4  1 5  2 6  3 7  5 6
4 8  8 9  5 10  6 11  7 12  9 10  10 11  11 12
*/
freopen("in_04.txt", "r", stdin);
scanf("%d %d", &V, &E);

```

```

AdjList.assign(V, vii()); // assign blank vectors of pair<int, int>s to AdjList
for (int i = 0; i < E; i++) {
    scanf("%d %d", &a, &b);
    AdjList[a].push_back(ii(b, 0));
    AdjList[b].push_back(ii(a, 0));
}
// as an example, we start from this source
s = 5;

```

```

// BFS routine
// inside int main() -- we do not use recursion, thus we do not need to create
separate function!
vi dist(V, 1000000000); dist[s] = 0; // distance to source is 0 (default)
queue<int> q; q.push(s);           // start from source
p.assign(V, -1); // to store parent information (p must be a global variable!)
int layer = -1; // for our output printing purpose addition of
bool isBipartite = true; //one boolean flag, initially true

```

```

while (!q.empty()) {
    int u = q.front(); q.pop();
    if (dist[u] != layer) printf("\nLayer %d: ", dist[u]);
    layer = dist[u];
    printf("visit %d, ", u);
    for (int j = 0; j < (int)AdjList[u].size(); j++) {
        ii v = AdjList[u][j]; // for each neighbors of u
        if (dist[v.first] == 1000000000) {
            dist[v.first] = dist[u] + 1; // v unvisited + reachable
            p[v.first] = u; // addition: the parent of vertex v->first is u
            q.push(v.first); // enqueue v for next step
        }
        else if ((dist[v.first] % 2) == (dist[u] % 2)) // same parity
            isBipartite = false;
    }
}

```

```

    } }

printf("\nShortest path: ");
printPath(7, printf("\n"));
printf("isBipartite? %d\n", isBipartite);
return 0;
}

```

### Lowest Common Ancestor LCA

```

const int max_nodes, log_max_nodes;
int num_nodes, log_num_nodes, root;
vector<int> children[max_nodes]; // children[i] contains the children of node i
int A[max_nodes][log_max_nodes+1]; // A[i][j] is the 2^j-th ancestor of node i, or
-1 if that
ancestor does not exist
int L[max_nodes]; // L[i] is the distance between node i and the root
// floor of the binary logarithm of n
int lb(unsigned int n)
{
    if(n==0)
        return -1;
    int p = 0;
    if (n >= 1<<16) { n >>= 16; p += 16; }
    if (n >= 1<<8) { n >>= 8; p += 8; }
    if (n >= 1<<4) { n >>= 4; p += 4; }
    if (n >= 1<<2) { n >>= 2; p += 2; }
    if (n >= 1<<1) { p += 1; }
    return p;
}
void DFS(int i, int l)
{
    L[i] = l;
    for(int j = 0; j < children[i].size(); j++)
        DFS(children[i][j], l+1);
}
int LCA(int p, int q)
{
    // ensure node p is at least as deep as node q
    if(L[p] < L[q])

```

```

        swap(p, q);
    // "binary search" for the ancestor of node p situated on the same level as q
    for(int i = log_num_nodes; i >= 0; i--)
        if(L[p] - (1<<i) >= L[q])
            p = A[p][i];
    if(p == q)
        return p;
    // "binary search" for the LCA
    for(int i = log_num_nodes; i >= 0; i--)
        if(A[p][i] != -1 && A[p][i] != A[q][i])
        {
            p = A[p][i];
            q = A[q][i];
        }
    return A[p][0];
}
int main(int argc, char* argv[])
{
    // read num_nodes, the total number of nodes
    log_num_nodes = lb(num_nodes);
    for(int i = 0; i < num_nodes; i++)
    {
        int p;
        // read p, the parent of node i or -1 if node i is the root
        A[i][0] = p;
        if(p != -1)
            children[p].push_back(i);
        else
            root = i;
    }
    // precompute A using dynamic programming
    for(int j = 1; j <= log_num_nodes; j++)
        for(int i = 0; i < num_nodes; i++)
            if(A[i][j-1] != -1)
                A[i][j] = A[A[i][j-1]][j-1];
            else
                A[i][j] = -1;
    // precompute L
    DFS(root, 0);
    return 0;
}

```



## Tricks in cmath

```
// when the number is too large. use powl instead of pow.  
// will provide you more accuracy.  
powl(a, b)
```

```
(int)round(p, (1.0/n)) // nth root of p
```

## Initialize array with predefined value

```
// for 1d array, use STL fill_n or fill to  
initialize array fill(a, a+size_of_a,  
value)
```

```
fill_n(a, size_of_a, value)
```

```
//for 2d array, if want to fill in 0 or -1  
memset(a, 0, sizeof(a));
```

```
// otherwise, use a loop of fill or fill_n  
through every a[i] fill(a[i], a[i]+size_of_ai,  
value) //from 0 to number of row.
```

## Java

### StringBuilder Use of Functions

```
import java.lang.StringBuilder;
```

```
public class String_builder {  
    public static void main(String[] args) {
```

```
        // Create a new StringBuilder.  
        StringBuilder builder1 = new StringBuilder();  
        // Loop and append values.  
        for (int i = 0; i < 5; i++) {  
            builder1.append("abc ");  
        }  
        // Convert to string.  
        String result = builder1.toString();  
        System.out.println(result);
```

```
        // " INSERT"  
        StringBuilder builder2 = new StringBuilder("abc");  
        // Insert this substring at position 2.  
        builder2.insert(2, "xyz");  
        System.out.println(builder2);//abxyzc
```

```
        // INDEX-OF  
        StringBuilder builder3 = new StringBuilder("abc");  
        // Try to find this substring.  
        int result1 = builder3.indexOf("bc");  
        System.out.println(result1);// 1  
        // This substring does not exist.  
        int result2 = builder3.indexOf("de");  
        System.out.println(result2);// -1
```

```
        // DELETE
```



```

StringBuilder builder4 = new StringBuilder("carrot");
// Delete characters from index 2 to index 5.
builder4.delete(2, 5);
System.out.println(builder4); // cat

// REPLACE
StringBuilder b = new StringBuilder("abc");
// Replace second character with "xyz".
b.replace(1, 2, "xyz");
System.out.println(b); // axyzc

// SUBSTRING
StringBuilder builder = new StringBuilder();
builder.append("Forest");
String firstTwo = builder.substring(0, 2);
System.out.println(firstTwo); // Fo

// REVERSE
StringBuilder builder5 = new StringBuilder();
builder5.append("abc");
builder5.reverse();
System.out.println(builder5);

```

```

}

```

### Decimal Formatter

```

import java.util.Scanner;
import java.util.Formatter;
public class readdouble {
    public static void main(String args[]){
        Scanner ob=new Scanner(System.in);
        float s = ob.nextFloat();
        Formatter fmt = new Formatter();
        fmt = new Formatter();
        fmt.format("%.2f",s);
        System.out.println(fmt);}}

```

### Fast Read

```

import java.io.BufferedReader;
import java.io.IOException;
import java.io.InputStreamReader;

```

```

import java.util.Scanner;
import java.util.StringTokenizer;
import java.lang.*;
public class fastread {
    static class FastReader {
        BufferedReader br;
        StringTokenizer st;

        public FastReader() {
            br = new BufferedReader(new
InputStreamReader(System.in));
        }

        String next() {
            while (st == null || !st.hasMoreElements()) {
                try {
                    st = new StringTokenizer(br.readLine());
                } catch (IOException e) {
                    e.printStackTrace();
                }
            }
            return st.nextToken();
        }
        int nextInt() {
            return Integer.parseInt(next());
        }
        long nextLong() {
            return Long.parseLong(next());
        }
        double nextDouble() {
            return Double.parseDouble(next());
        }
        String nextLine() {
            String str = "";
            try {
                str = br.readLine();
            } catch (IOException e) {
                e.printStackTrace();
            }
            return str;
        }
    }
}

```

```

    }
    public static void main(String[] args) {
        FastReader s = new FastReader();
        int t = s.nextInt();
        while (t-- > 0) {

        }
    }
}

```

### Factorial Using BigInteger

```

public static void calculateFactorial(int n) {

    BigInteger result = BigInteger.ONE;
    for (int i=1; i<=n; i++) {
        result = result.multiply(BigInteger.valueOf(i));
    }
    System.out.println(n + "!" = " + result);}

```

### BigInteger Functions

```

import java.math.BigInteger;
public class BigIntegerDemo {
    public static void main(String[] args) {

        BigInteger b1 = new BigInteger("9876543219876543210000000000");
        BigInteger b2 = new BigInteger("9876543219876543210000000000");

        BigInteger product = b1.multiply(b2);
        BigInteger division = b1.divide(b2);
        System.out.println("product = " + product);
        System.out.println("division = " + division);
        int a, b;
        BigInteger A, B;
        a = 54;
        b = 23;
        A = BigInteger.valueOf(54);
        B = BigInteger.valueOf(37);
        A = new BigInteger("54");
        B = new BigInteger("123456789123456789");
        A = BigInteger.ONE;
        int c = a + b;
        BigInteger C = A.add(B); // Other similar function are subtract() multiply(),
        divide(), remainder(), mod()
    }
}

```

```

String str = "123456789";
BigInteger C = A.add(new BigInteger(str));
int val = 123456789;
BigInteger C = A.add(BigInteger.valueOf(val));

```

//Extraction of value from BigInteger:

```

int x = A.intValue(); // value should be in limit of int x
long y = A.longValue(); // value should be in limit of long y
String z = A.toString();

```

// Comparison

```

if (a < b) {} // For primitive int
if (A.compareTo(B) < 0) {} // For BigInteger
// Equality
if (A.equals(B)) {} // A is equal to B

```

### Check Prime for BigIntegers

```

import java.util.*;
import java.math.*;
class CheckPrimeTest
{
    //Function to check and return prime numbers
    static boolean checkPrime(long n)
    {
        // Converting long to BigInteger
        BigInteger b = new BigInteger(String.valueOf(n));
        return b.isProbablePrime(1);
        // returns whether prime or not
        return Long.parseLong(b.nextProbablePrime().toString());
        // returns next probable prime, long
    }
    // Driver method
    public static void main (String[] args) throws java.lang.Exception
    {
        long n = 13;
        System.out.println(checkPrime(n));
    }
}

```

### Stack Queue

```

class ch2_04_stack_queue {
    public static void main(String[] args) {
        Stack<Character> s = new Stack<Character>();
    }
}

```

```

// Queue is abstract, must be instantiated with LinkedList
// (special case for Java Queue)
Queue<Character> q = new LinkedList<Character>();

Deque<Character> d = new LinkedList<Character>();

System.out.println(s.isEmpty());    // currently s is empty, true
System.out.println("=====");
s.push('a'); //push b,c
// stack is LIFO, thus the content of s is currently like this:
System.out.println(s.peek());        // output 'c'
s.pop();                             // pop topmost
System.out.println(s.peek());        // output 'b'
while (!s.isEmpty()) {              // stack s still has 2 more items
    q.offer(s.peek()); // enqueue 'b', and then 'a' (the method name in Java Queue
for push/enqueue operation is 'offer')
    s.pop(); }
q.offer('z');                        // add one more item
System.out.println(q.peek());        // prints 'b'
// in Java, it is harder to see the back of the queue...
// output 'b', 'a', then 'z' (until queue is empty), according to the insertion order
above
System.out.println("=====");
while (!q.isEmpty()) {
    System.out.printf("%c\n", q.peek());    // take the front first
    q.poll();                             // before popping (dequeue-ing) it
}
System.out.println("=====");
d.addLast('a');
d.addLast('b');
d.addLast('c');
System.out.printf("%c - %c\n", d.getFirst(), d.getLast()); // prints 'a - c'
d.addFirst('d');
System.out.printf("%c - %c\n", d.getFirst(), d.getLast()); // prints 'd - c'
d.pollLast();
System.out.printf("%c - %c\n", d.getFirst(), d.getLast()); // prints 'd - b'
d.pollFirst();
System.out.printf("%c - %c\n", d.getFirst(), d.getLast()); } // prints 'a - b'

```

## KMP

```

import java.util.*;
class ch6_02_kmp {
    char[] T, P; // T = text, P = pattern
    int n, m; // n = length of T, m = length of P
    int [] b; // b = back table
    void naiveMatching() {
        for (int i = 0; i < n; i++) { // try all potential starting indices
            Boolean found = true;
            for (int j = 0; j < m && found; j++) // use boolean flag `found`
                if (i + j >= n || P[j] != T[i + j]) // if mismatch found
                    found = false; // abort this, shift starting index i by +1
            if (found) // if P[0 .. m - 1] == T[i .. i + m - 1]
                System.out.printf("P is found at index %d in T\n", i);
        } }

    void kmpPreprocess() { // call this before calling kmpSearch()
        int i = 0, j = -1; b[0] = -1; // starting values
        while (i < m) { // pre-process the pattern string P
            while (j >= 0 && P[i] != P[j]) j = b[j]; // if different, reset j using b
            i++; j++; // if same, advance both pointers
            b[i] = j; // observe i = 8, 9, 10, 11, 12 with j = 0, 1, 2, 3, 4
        } } // in the example of P = "SEVENTY SEVEN" above

    void kmpSearch() { // this is similar as kmpPreprocess(), but on string T
        int i = 0, j = 0; // starting values
        while (i < n) { // search through string T
            while (j >= 0 && T[i] != P[j]) j = b[j]; // if different, reset j using b
            i++; j++; // if same, advance both pointers
            if (j == m) { // a match found when j == m
                System.out.printf("P is found at index %d in T\n", i - j);
                j = b[j]; // prepare j for the next possible match
            } } }

    void run() {
        String Tstr = "I DO NOT LIKE SEVENTY SEV BUT SEVENTY SEVENTY SEVEN";
        String Pstr = "SEVENTY SEVEN";
        T = new String(Tstr).toCharArray();
        P = new String(Pstr).toCharArray();
        n = T.length;
        m = P.length;
    }
}

```

```

System.out.println(T);
System.out.println(P);
System.out.println();

System.out.printf("Naive Mathing\n");
naiveMatching();
System.out.println();

System.out.printf("KMP\n");
b = new int[100010];
kmpPreprocess();
kmpSearch();
System.out.println();

System.out.printf("String Library\n");
int pos = Tstr.indexOf(Pstr);
while (pos != -1) {
    System.out.printf("P is found at index %d in T\n", pos);
    pos = Tstr.indexOf(Pstr, pos + 1);
}
System.out.println();
}
public static void main(String[] args)
{
    new ch6_02_kmp().run();
}
}

```

### Binomial coefficient

```

#define MAXN 100 // largest n or m

long binomial_coefficient(n,m) // compute n choose m

int n,m;

{int i,j;

long bc[MAXN][MAXN];

    for (i=0; i<=n; i++) bc[i][0] = 1;

    for (j=0; j<=n; j++) bc[j][j] = 1;

```

```

    for (i=1; i<=n; i++)

        for (j=1; j<i; j++)

            bc[i][j] = bc[i-1][j-1] + bc[i-1][j];

    return bc[n][m];

}

```

### Euler's totient function

```

//      the positive integers less than or equal to n that are relatively prime to n.
int phi (int n)

{

int result = n;

for (int i=2; i*i<=n; ++i) if(n%i==0)

{

while(n%i==0) n /= i;

result -= result / i;

}

if (n > 1)

result -= result / n; return result;

}

```

## 0/1 Knapsack problems

```
#include<iostream>

using namespace std;

int f[1000]={0};

int n=0, m=0;

int main(void)

{
    cin >> n >> m;

    for (int i=1;i<=n;i++)
    {
        int price=0, value=0;

        cin >> price >> value;

        for (int j=m;j>=price;j--)

            if (f[j-price]+value>f[j])

                f[j]=f[j-price]+value;
    }

    cout << f[m] << endl;

    return 0;
}
```

## Longest common subsequence (LCS)

```
int dp[1001][1001];

int lcs(const string &s, const string &t)

{

    int m = s.size(), n = t.size();

    if (m == 0 || n == 0) return 0;
```

```
    for (int i=0; i<=m; ++i)

        dp[i][0] = 0;

    for (int j=1; j<=n; ++j)

        dp[0][j] = 0;

    for (int i=0; i<m; ++i)

        for (int j=0; j<n; ++j)

            if (s[i] == t[j])

                dp[i+1][j+1] = dp[i][j]+1;

            else

                dp[i+1][j+1] =
                    max(dp[i+1][j], dp[i][j+1]);

    return dp[m][n];
}
```

## Maxmium Matrix

```
int a[150][150]={0};

int c[200]={0};

int maxarray(int n)

{

    int b=0, sum=-100000000;

    for (int i=1;i<=n;i++)

    {

        if (b>0) b+=c[i];
```

```

else b=c[i];
if (b>sum) sum=b;
}
return sum;
}
int maxmatrix(int n)
{
int sum=-100000000, max=0;
for (int i=1;i<=n;i++)
{
for (int j=1;j<=n;j++)
c[j]=0;
for (int j=i;j<=n;j++)
{
for (int k=1;k<=n;k++)
c[k]+=a[j][k];
max=maxarray(n);
if (max>sum) sum=max;
}
}
return sum;
}
int main(void)
{
int n=0;

```

```

cin >> n;
for (int i=1;i<=n;i++)
for (int j=1;j<=n;j++)
cin >> a[i][j];
cout << maxmatrix(n);
return 0;
}

```

### Count number of ways to partition a set into k subsets

$$S(n, k) = k * S(n-1, k) + S(n-1, k-1)$$

### Flood fill algorithm

```

//component(i) denotes the
//component that node i is in
void flood_fill(new_component)
do
num_visited = 0
for all nodes i
if component(i) = -2
num_visited = num_visited + 1
component(i) = new_component
for all neighbors j of node i
if component(j) = nil
component(j) = -2
until num_visited = 0
void find_components()

```

```

num_components = 0

for all nodes i

component(node i) = nil

for all nodes i

if component(node i) is nil

num_components = num_components + 1

component(i) = -2

flood_fill(component num_components)

```

### SPFA — shortest path

```

int q[3001]={0}; // queue for node

int d[1001]={0}; // record shortest path from start to ith node bool f[1001]={0};

int a[1001][1001]={0}; // adjacency list

int w[1001][1001]={0}; // adjacency matrix

int main(void)

{

int n=0, m=0;

cin >> n >> m;

for (int i=1;i<=m;i++)

{

int x=0, y=0, z=0;

cin >> x >> y >> z; // node x to node y has weight z

a[x][0]++;

a[x][a[x][0]]=y;

w[x][y]=z;

```

```

/*

//      for undirected graph a[x][0]++; a[y][a[y][0]]=x; w[y][x]=z;

*/

}

int s=0, e=0;

cin >> s >> e; // s: start, e: end

SPFA(s);

cout << d[e] << endl;

return 0;

}

void SPFA(int v0)

{

int t,h,u,v;

for (int i=0;i<1001;i++) d[i]=INT_MAX;

for (int i=0;i<1001;i++) f[i]=false;

d[v0]=0;

h=0; t=1; q[1]=v0; f[v0]=true;

while (h!=t)

{

h++;

if (h>3000) h=1;

u=q[h];

for (int j=1; j<=a[u][0];j++)

{

```

```

v=a[u][j]

if (d[u]+w[u][v]<d[v]) // change to > if calculating longest path
{
d[v]=d[u]+w[u][v];
if (!f[v])
{
t++;
if (t>3000) t=1;
q[t]=v;
f[v]=true;
}
}
f[u]=false;
}
}

```

### Floyd-Warshall algorithm – shortest path of all pairs

```

//map[i][j]=infinity at start void floyd()
{
for (int k=1; k<=n; k++)
for (int i=1; i<=n; i++)
for (int j=1; j<=n; j++)
if (i!=j && j!=k && i!=k)
if (map[i][k]+map[k][j]<map[i][j])
map[i][j]=map[i][k]+map[k][j];}

```

### Strings

```

string str("The Geeks for Geeks");
// find() returns position to first
// occurrence of substring "Geeks"
// Prints 4
cout << "First occurrence of \"Geeks\" starts from : ";
cout << str.find("Geeks") << endl;

string str="We think in generalities, but we live in
details.";
string str2 = str.substr (3,5);      // "think"
size_t pos = str.find("live");      // position of "live"
in str
string str3 = str.substr (pos);      // get from "live" to
the end
//OUTPUT: think live in details.

string str1 ("green apple");
string str2 ("red apple");
if (str1.compare(str2) != 0)
    cout << str1 << " is not " << str2 << '\n';
if (str1.compare(6,5,"apple") == 0)
    cout << "still, " << str1 << " is an apple\n";
if (str2.compare(str2.size()-5,5,"apple") == 0)
    cout << "and " << str2 << " is also an apple\n";
if (str1.compare(6,5,str2,4,5) == 0)
    cout << "therefore, both are apples\n";
/*OUTPUT: green apple is not red apple
still, green apple is an apple
and red apple is also an apple
therefore, both are apples*/

```