| TL;DR                                | 1 |
|--------------------------------------|---|
| Overview with Motivation/Explanation | 1 |
| Git                                  | 3 |
| Pushing to Git                       | 3 |
| Overview of Programming              | 4 |
| PercolationDFSFast                   | 4 |
| PercolationBFS                       | 5 |
| PercolationUF                        | 6 |
| Instance variables for PercolationUF | 6 |
| Constructor for PercolationUF        | 6 |
| Methods for PercolationUF            | 6 |
| Testing PercolationUF                | 7 |
| Analysis                             | 7 |
| Submitting                           | 8 |
| Reflect                              | 8 |
| Grading                              | 8 |

## TL;DR

You're encouraged to use the <u>TL;DR document</u> to understand what to do and how to do it at a very high level.

You can talk with one person, a partner, when completing the analysis. You cannot have a partner in developing code, that should be your own effort as is typical with 201 assignments. You can discuss and collaborate deeply on the analysis with your analysis partner.

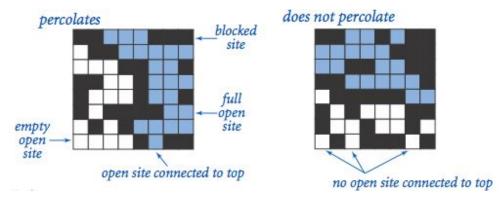
## Overview with Motivation/Explanation

In this assignment, you will write a program to estimate the value of the <u>percolation threshold</u> via <u>Monte Carlo</u> simulation. In doing so, you will better understand depth-first-search, union-find structures, and the use of computer simulations for statistical inquiry. *Your goal will be to explore trade-offs in several approaches to estimate the percolation threshold in an NxN system.* 

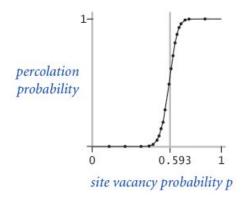
Given a porous landscape with water on the surface (or oil below), under what conditions will the water be able to drain through to the bottom (or the oil to gush through to the surface)? Given a composite systems comprised of randomly distributed insulating and metallic materials, what fraction of the materials need to be metallic so that the composite system is an electrical conductor? Scientists have defined an abstract process known as percolation to model such situations.

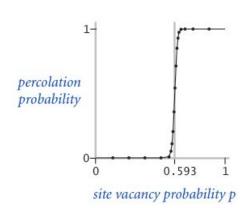
We model a percolation system using an N-by-N grid of sites. *Each site is either open or blocked*. *A full site is an open site that can be connected to an open site in the top row via a chain of neighboring (left, right, up, down) open sites*. In diagrams we color full sites blue to model water flowing from the top through the system. We say the *system percolates if there is at least one full site in the bottom row*. In other words, a system percolates if there is a path of open sites from the top row to the bottom row. For the porous substance example, the open sites correspond to empty space through which water might flow, so that a system that percolates lets water fill open sites, flowing from top to bottom.

For more on percolation see the <u>Princeton Case Study</u>.



The percolation threshold problem is: if sites are independently set to be open with probability p (and therefore blocked with probability 1 - p), what is the probability that the system percolates? In other words, in a N-by-N grid, would the system percolate if  $N^2p$  randomly chosen cells are opened? When p equals 0, the system does not percolate; when p equals 1, the system percolates. The plots below show the site vacancy probability p versus the percolation probability for 20-by-20 random grid (left) and 100-by-100 random grid (right).





When N is sufficiently large, there is a threshold value  $p^*$  such that when  $p < p^*$  a random N-by-N grid almost never percolates, and when  $p > p^*$ , a random N-by-N grid almost always percolates. No mathematical solution for determining the percolation threshold  $p^*$  has yet been derived. Your task is to write a suite of computer programs to visualize the percolation process and estimate  $p^*$  using Monte Carlo techniques. As you can see above, the percolation threshold in an NxN grid is about 0.593. The size of the grid doesn't matter as your simulations will show.

The videos linked here show (1) an interactive simulation where you choose to open sites and (2) help explain the techniques you'll read about. These videos may be helpful after reading the assignment, or to get grounded before reading.

These videos help understand two parts of the assignment.

Open, full, DFS, and what percolation means

1. https://www.youtube.com/watch?v=ikVliuCR4pk

From DFS to Union-Find: two approaches compared/contrasted

2. <a href="https://www.youtube.com/watch?v=lpYvgV5m1qM">https://www.youtube.com/watch?v=lpYvgV5m1qM</a>

### Git

Fork, clone, and import the cloned project from the file system. Use this URL from the course GitLab site: <a href="https://coursework.cs.duke.edu/201spring19/percolation">https://coursework.cs.duke.edu/201spring19/percolation</a>. Be sure to fork first (see screen shot). Then Clone using the SSH URL after using a terminal window to cd into your Eclipse workspace. Recall

File>Import>General>Existing Projects into Workspace -- then navigate to where you cloned the diyad project.

DO NOT DO NOT import using the Git open -- use General>Existing Projects Into Workspace.

### Pushing to Git

that **you should import using** the

When you make a series of changes you want to 'save', you'll push those changes to your GitLab repository. You should do this after major changes, certainly every hour or so of coding. You'll need to use the standard Git sequence to commit and push to GitLab:

```
git add .
git commit -m 'a short description of your commit here'
git push
```

## Overview of Programming

You'll create three new implementations of the IPercolate interface: one that uses a faster DFS, one that uses BFS, and one that uses the Union-Find algorithm rather than DFS/BFS.

- Create a subclass of PercolationDFS named PercolationDFSFast that has a
  different implementation of the method updateOnOpen that will make the
  implementation faster.
- 2. Create a subclass of PercolationDFSFast named PercolationBFS that has a different implementation of the method dfs. This implementation will use BFS with a Queue rather than recursion.
- 3. Create class PercolationUF that implements the IPercolate interface. By using a Union-Find data structure, this class serves as a bridge between classes that implement the IUnionFind interface and those running a percolation simulation (that implement IPercolate).

You'll time each of the three and report on the timings in the analysis.txt file you create.

For each class you create you'll use one of the JUnit testing files to test your implementation. You'll need to change the class each uses to test your implementation. You should also use the InteractivePercolationVisualizer to help verify your classes work correctly.

### PercolationDFSFast

Your new class PecolationDFSFast will extend PercolationDFS and thus inherit state and methods from that class.

- 1. You'll need to create a constructor with an int/size parameter that calls super to initialize the state in the parent class.
- 2. You'll need to @Override updateOnOpen to be more efficient.

In the updateOnOpen from PercolationDFS all cells marked as FULL are "cleared" or changed so that they're marked as OPEN, then the method dfs is called from every cell on the top row. Calling dfs on any open cell will explore all paths from that cell and mark all open cells as FULL. This is very inefficient since cells marked as FULL are cleared each time a new cell is opened, then marked as FULL, then cleared and the process repeats for each newly open cell, e.g., in a simulation.

You'll change this method so it does **not** clear all cells, but instead calls dfs once if the newly open cell should be marked as **FULL** because it's in the top row or because it's adjacent to an already **FULL** cell.

- 1. Determine if the newly open cell (parameters row and col of updateOnOpen) should be marked as full. To check:
  - a. Is the cell in the top row? If so, it should be marked as full.
  - b. Is the cell adjacent to a full cell? If so it should be marked as full.
- 2. If the cell should be marked as full, call dfs (row, col)

Note that you'll make one call of dfs. The dfs method is inherited and does not change. You must call dfs and NOT super.dfs in the code you write. The dfs implementation will mark an open cell as FULL and make recursive calls for each neighbor. The dfs implementation checks for cells already marked as FULL or that are not OPEN and does not visit these cells.

#### PercolationBFS

This class extends the PercolationDFSFast class you wrote previously. You'll override the dfs method inherited from PercolationDFS to use a Queue and a breadth-first-search (BFS) approach. Use the ideas from <a href="IterativeBlobModel.java">IterativeBlobModel.java</a> we've seen in class, but you'll create queue of int values and not Pair values. The dfs method will be called from the inherited updateOnOpen from PercolationDFSFast.

- 1. You'll need to create a constructor with an int/size parameter that calls super to initialize the state in the parent class.
- 2. You'll need to @Override dfs to use a Queue as explained below.

Create a <code>Queue<Integer></code> from a <code>LinkedList</code> object since that class implements the <code>Queue</code> interface (see <a href="IterativeBlobModel.java">IterativeBlobModel.java</a> for details). Whereas the original dfs used recursion, this method will first mark the cell at (row,col) as <code>FULL</code> and put the cell on the queue, then repeat the following process:

- Dequeue a cell. (All cells in the queue should have been marked as FULL)
- Check the dequeued cell's four neighbors. If the neighboring cell is open and not full,
  it should be marked as full and enqueued. This is similar to the check in the recursive
  dfs method where cells that are marked as open but not full are visited by the recursive
  call.

To map (row,col) pairs to an integer value, use row\*size + col, where size is the N in the NxN grid, e.g., use myGrid.length for size. When dequeuing an int value, you can determine the corresponding (row,col) using value/size and value%size, respectively. You can use a helper method to do this, or simply use row\*myGrid.length + size each time an int value is required.

#### PercolationUF

This class implements the IPercolate interface and will use an IUnionFind object to keep track of open and full cells. See the video at the beginning of the assignment for general ideas. Each of the NxN cells is mapped to a number, and these numbers represent the set for the disjoint-set/union-find algorithm. You'll need two additional numbers, VTOP and VBOTTOM, for a total of N²+2 values.

#### Instance variables for PercolationUF

- 1. A two-dimensional array of boolean values, myGrid, that represents whether a cell is open. Initially myGrid[r][c] should be false which is the default value when you create the grid. Each time a cell (r,c) is open, myGrid[r][c] will be set to true.
- 2. An integer myOpenCount which is the number of open cells, i.e., the number of true values in myGrid.
- 3. An IUnionFind object myFinder to store/reference the IUnionFind object passed to the constructor (which should be a QuickUWPC object in this assignment).
- 4. Two final values for **VTOP** and **VBOTTOM**, set to size\*size and size\*size+1, for example, in the constructor.

```
private final int VTOP;
private final int VBOTTOM;
```

#### Constructor for PercolationUF

Create a constructor PercolationUF (int size, IUnionFind finder) that will construct and initialize the NxN grid stored in the instance variable myGrid (where N is given by the size parameter). The constructor should initialize the IUnionFind object of size NxN + 2 by calling finder.initialize appropriately and then storing this object in the appropriate instance variable which is myFinder.

#### Methods for PercolationUF

You must @Override each method from the IPercolate interface. As with methods you can see in PercolationDFS, these methods you write with (row,col) parameters should throw exceptions when the (row,col) are not in bounds.

As with the Queue described in <u>PercolationBFS</u> above you'll need to map a (row,col) pair to an int value to use with the <u>IUnionFind</u> object referenced by <u>myFinder</u>. Be sure to deal with <u>VTOP</u> and <u>VBOTTOM</u> as well.

- 1. Method isOpen throws an Exception when needed and otherwise simply returns the appropriate myGrid value.
- 2. Method isFull throws an Exception when needed and otherwise checks if the (row,col) cell is connected to VTOP.

- 3. Method percolates checks to see if VTOP is connected to VBOTTOM.
- 4. Method numberOfOpenSites simply returns the value of the appropriate instance variable.
- 5. Method open throws an Exception when needed, checks to be sure the cell is not already open, and then marks the cell as open and connects with open neighbors as described below.

When a cell is marked as open, you'll write code to check each of the cell's four neighbors. If any of these cells is open, the newly marked cell and the open neighbor should be connected by a call to myFinder.union. If the newly marked cell is in the top row it should be connected to VTOP by a call to myFinder.union. If the newly marked cell is in the bottom row it should be connected to VBOTTOM by a call to myFinder.union.

#### Testing PercolationUF

You can test using TestUFPercolation. Create a QuickUWPC object to use with your PercolationUF object and run JUnit tests. You should also use the InteractivePercolationVisualizer to help verify your classes work correctly. You'll need to uncomment/comment a line in getPercolation of the TestUFPercolation class.

### Analysis

Copy/Paste the runs described below and answer the questions indicated in the analysis.txt file. Here is a copy of the file.

You're given PercolationStats.java which performs benchmarks for an IPercolate object using grid sizes of 100, 200, 400, 800, 1600, and 3200. If you don't change the value of the public RANDOM\_SEED variable you should see the same mean values of the Percolation threshold shown below. Your timing values may vary, but for all implementations using 20 trials you should see the same mean and standard deviation values.

| simul | ation data | for 20 | trials  |
|-------|------------|--------|---------|
| grid  | mean       | stddev | time    |
| 100   | 0.593      | 0.014  | 0.142   |
| 200   | 0.591      | 0.010  | 0.150   |
| 400   | 0.590      | 0.006  | 0.958   |
| 800   | 0.594      | 0.004  | 5.925   |
| 1600  | 0.592      | 0.002  | 39.266  |
| 3200  | 0.593      | 0.001  | 183.074 |

Copy/paste the results for each IPercolate Object (PercolationDFSFast, PercolationUF) as indicated in the analysis.txt file. Then answer these questions using data from PercolationUF with QuickUWPC.

- 1. How does doubling the grid size affect running time (keeping # trials fixed)
- 2. How does doubling the number of trials affect running time.
- 3. Estimate the largest grid size you can run in 24 hours with 20 trials. Explain your reasoning.

After completing the analysis questions you should push to Git and run the autograder again to make sure you response is submitted to Gradescope. Please note that Analysis is part of the assignment, and Gradescope is the only portal to submit the assignment, including the analysis. We reserve the right to reject your analysis submission if you forget to upload it to Gradescope, even if it's in your Git repo.

## Submitting

You'll submit the code to Gradescope after pushing program and analysis.txt file to GitLab.

### Reflect

Complete the Reflect form <u>linked here</u>.

You must complete the Reflect form to get all points, but you should NOT complete the reflect form until you're done with all the coding portion of the assignment. Since you may uncover bugs from the autograder, you should wait until you've completed debugging and coding before completing the reflect form.

# Grading

| Points | Grading Criteria                      |  |
|--------|---------------------------------------|--|
| 6      | PercolationDFSFast                    |  |
| 6      | PercolationBFS                        |  |
| 6      | PercolationUF                         |  |
| 8      | Analysis, UTAs will grade and comment |  |

22-26: A 17-21: B 11-16: C 7-10: D

Due date: on time 4/16, 24 hours no penalty until 4/17, 10% late on 4/22, then 20% and so on.