

Towards Automating Blockchain Consensus Verification with IsabeLLM

Formal Verification of Bitcoin's Proof of Work

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February 3, 2026

What is Blockchain?

- Blockchain enables **peer-to-peer digital transactions** without trusted intermediaries
- Relies on **consensus protocols** for agreement between nodes
- Must work correctly even in **adversarial environments**

Key Challenge

Consensus must be designed and implemented correctly to prevent malicious behavior

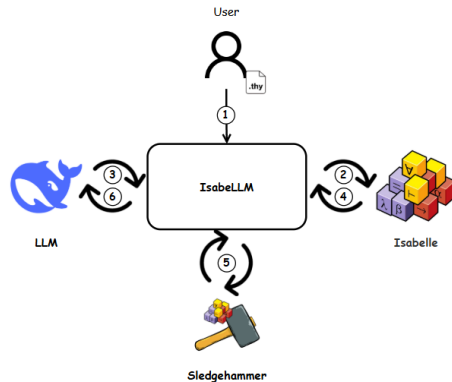
The Problem with Consensus Verification

- Consensus bugs can lead to catastrophic failures
- **Formal verification** ensures correctness
- Requires high expertise and significant effort
- Often omitted during development

Introducing IsabeLLM

IsabeLLM integrates:

- **Isabelle** proof assistant
- **Large Language Model** (DeepSeek R1 API)



IsabeLLM Key Features

- **Automates proof generation**
- **Assists human experts**
- Generates correct proofs for non-trivial lemmas
- Reduces formal verification barrier to entry

Bitcoin's Proof of Work Consensus

- Nodes compete to solve computational puzzles
- Longest valid chain wins
- Probabilistic finality (no absolute guarantees)
- Novel formal model developed using IsabelleLLM

Verification Results

Key Achievement

IsabeLLM generated **correct proofs** for **all non-trivial lemmas** in the Bitcoin PoW verification

- Verified liveness properties
- Verified safety properties
- Handled complex adversarial scenarios

Key Contributions

- ① **IsabeLLM**: Novel LLM+Isabelle integration for proof automation
- ② **Novel Bitcoin PoW model** with full formal verification
- ③ Demonstrated effectiveness on complex real-world protocol
- ④ Generated correct proofs for all non-trivial lemmas

Future Work

- Extend to other consensus protocols (Ethereum, Tendermint)
- Improve LLM reasoning capabilities
- Develop interactive proof assistance interface
- Scale to larger protocol models

Questions?

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