

1. Conjugate harmonic function of $\ln(x^2 + y^2)$ is:

- ☐ $5 \cot^{-1}\left(\frac{2x}{y}\right)$
- ☐ $2 \cot^{-1}\left(\frac{y}{x}\right)$
- ☐ $5 \tan^{-1}\left(\frac{2x}{y}\right)$
- ☒ $2 \tan^{-1}\left(\frac{y}{x}\right)$

2. Value of the integral $\int_0^{1+i} (x - y + ix^2) dz$

- ☐ $\frac{5}{2} + \frac{5}{7}i$
- ☐ $\frac{3}{2} + \frac{5}{6}i$
- ☒ $-\frac{1}{2} + \frac{5}{6}i$
- ☐ $\frac{1}{2} + \frac{1}{6}i$

3. Evaluate $\int_{[z_1, z_2]} (x^2 + y^2) dz$ where $z_1 = 2 + i, z_2 = -1 - i$

- ☐ $-6 - \frac{1}{3}i$
- ☒ $-4 - \frac{8}{3}i$
- ☐ $-1 - \frac{2}{3}i$
- ☐ $-3 - \frac{4}{3}i$

4. The line integral $\oint_C z^2 dz$ where C is the parabolic path of $y = 2x^2$ is

☒ $-\frac{1}{3}(11 + 2i)$

☐ $\frac{4}{3}(5 - 2i)$

☐ $\frac{2}{5}(3 + 7i)$

☐ $\frac{2}{3}(-13 + 5i)$

5. Evaluate the limit of $\lim_{z \rightarrow i} \frac{z^3 + (1-3i)z^2 + (i-3)z + 2+i}{z-i}$ using L'Hospital's rule.

☐ i

☐ $\frac{i}{3}$

☐ 3

☒ $3i$