

ISLAMIC UNIVERSITY OF TECHNOLOGY (IUT)
ORGANISATION OF ISLAMIC COOPERATION (OIC)
Department of Computer Science and Engineering (CSE)

MID EXAMINATION**SUMMER SEMESTER, 2019-2020****DURATION: 1 Hour 30 Minutes****FULL MARKS: 75****CSE 4803: Graph Theory****Programmable calculators are not allowed. Answer all the questions.**

Figures in the right margin indicate marks.

1. a) Determine whether or not the following sequences represent simple graph. If the sequence represents simple graph, draw a corresponding graph. If not, justify. 9
- i. (2, 3, 3, 4, 4, 5)
 - ii. (2, 3, 4, 4, 5)
 - iii. Your Student ID (comma separated digits, sorted in ascending order)
 - iv. (1, 3, 3, 3)
 - v. (1, 2, 2, 3, 4, 4)
 - vi. (1, 3, 3, 4, 5, 6, 6)
- b) One of your friends from CEE department has designed an apartment floor. Consider the drawing of an apartment with doors in Figure 1 as your friends drawing. 9

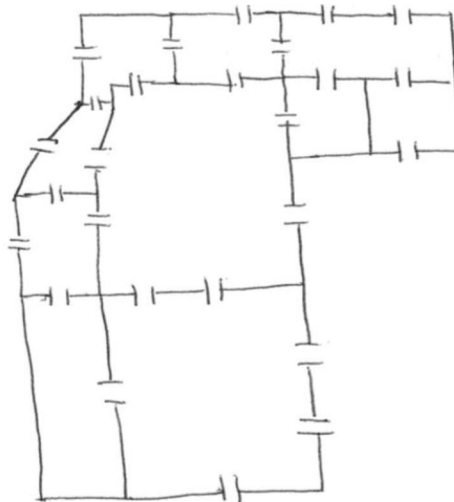


Figure 1: Floor Plan

- i. Can you find a continuous line that passes through each door exactly once? If not, At least how many doors are needed to be closed to have a continuous line that passes through each door exactly once?
 - ii. If we transform this floor plan into a graph, what should the vertices and the edges represent? What does the graph look like?
 - iii. Find a continuous line that passes through each door exactly once after closing the minimum numbers of doors.
- c) As a *Tom & Jerry* fan in your childhood, you used to draw *Jerry* mouse as your favorite character. One of such drawing is depicted in Figure 2(a). This drawing can be translated into a graph shown in Figure 2(b). 2.5

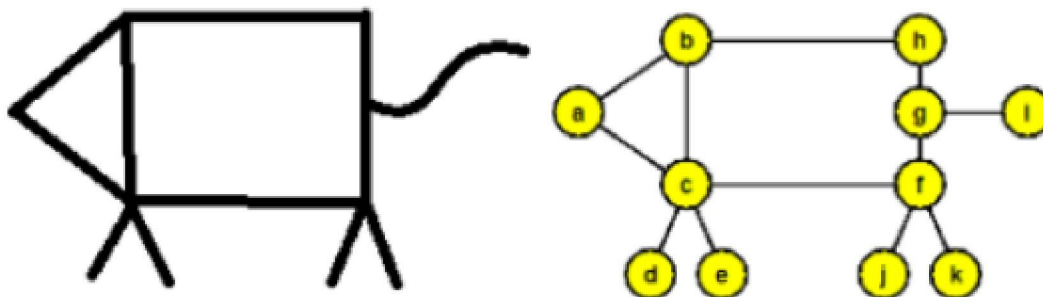


Figure 2: (a) A conceptual drawing of *Jerry* mouse, (b) Translation of the given mouse into a graph
Find the number of the minimum trails as possible covering the given graph? Draw the trails with distinguishable patterns.

[Hine: An Euler/semi Euler graph needs only one trail.]

- d) Consider the graph G in Figure 3. Is G Eulerian? Is G Hamiltonian? Is G bipartite? Justify your answers. 4.5

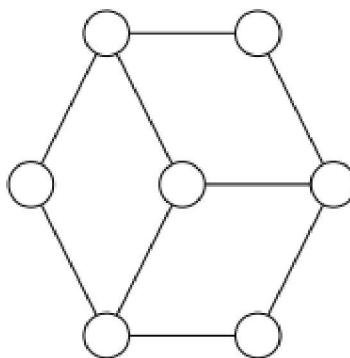


Figure 3: Simple graph G

2. a) How many isomers does Hexane (C_6H_{14}) have? Draw the structure of the carbon atoms in each isomer. 5
- b) Connected acyclic graphs are known as *Tree*. 4+4
- A finite tree T has at least one vertex v of degree 4, and at least one vertex w of degree 3. Show that T has at least 5 leaves.
 - Let T be a tree with p vertices of degree 1 and q other vertices. What is the sum of the degrees of the vertices of degree greater than 1?
- c) In Springfield Nuclear Power plant, there are 16 staff houses. An inexperienced engineer was hired to develop a network that will connect all the houses together. The engineer built a grid-like architecture for the network which is shown in Figure 4. This plan is submitted to you (an expert) for your approval. 12

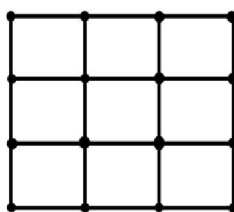


Figure 4: Designed network architecture

- What are the Vertex and Edge connectivity of this graph?
- If you are asked to check all the connection starting from the top-left house and returning to it. What is the minimum unit of distance you need to cover? Given that all the connections have unit distance?
- Can you design a more stable architecture? If not, describe why. Otherwise, draw the network.

3. a) Draw 4 simple completely regular planar graphs with vertex degree ≥ 3 . 8
- b) Show that, if G is a 3-connected plane graph, then its geometric dual is a simple graph. 4
- c) Determine if the following graphs in Figure 5 are planar. If yes, give a planar representation. 8
If not justify. [Hint: drawing is not a justification]

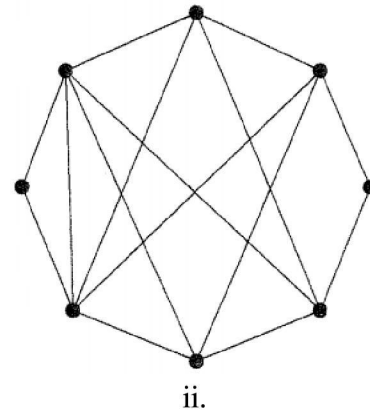
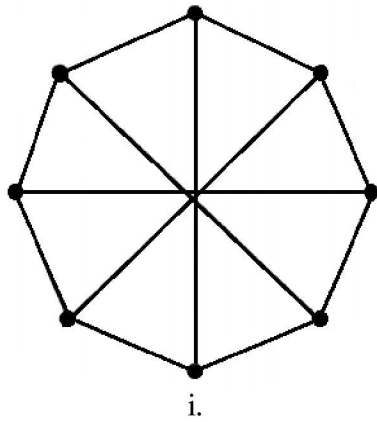


Figure 5: Graphs for question 3(c)

- d) A 5-regular planar graph has triangular regions. Find all possible number of vertices, edges and regions. 5