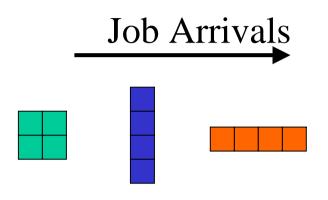
A Robust Scheduling Strategy for Moldable Jobs

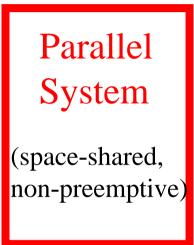
Sudha Srinivasan, Savitha Krishnamoorthy and P. Sadayappan

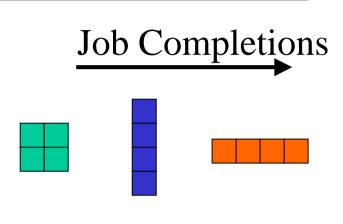
The Ohio State University, USA

Background: Job Scheduling



$$p=16$$
 $p=32$ $p=8$
 $t_r=2h$ $t_r=1h$ $t_r=4h$
 $t_a=2h$ $t_a=1h$ $t_a=0h$



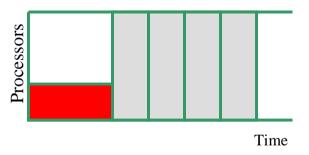


$$t_c = 6h t_c = 5h t_c = 4h$$

- Goals:
 - Minimize job response time (t_c-t_a)
 - Avoid job starvation; Provide fairness
 - Maximize system utilization
- First-Come-First-Served policy is fair but utilization is low
- Back-filling is used to improve utilization and response time

Backfilling

 A later arriving job is allowed to overtake previously queued jobs if its early execution will not delay others



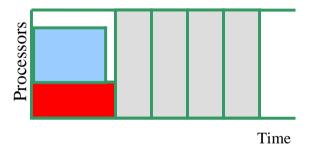
Backfilling

 A later arriving job is allowed to overtake previously queued jobs if its early execution will not delay others



Backfilling

 A later arriving job is allowed to overtake previously queued jobs if its early execution will not delay others



Conservative vs. Aggressive Backfill

Conservative

 Every job is given a reservation when it enters the system; a job is allowed to backfill only if it does not violate any of the reservations.

Aggressive

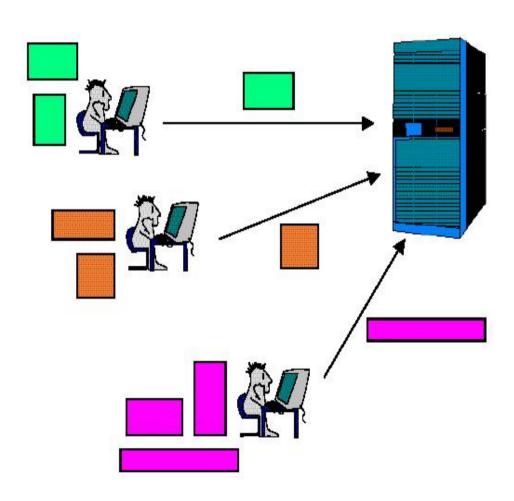
 Only the job at the head of the queue is given a reservation; a job is allowed to backfill if it does not violate this single reservation

Moldable Job Scheduling

- With current job schedulers, each job requests a specific number of processors, e.g. 64
- But most jobs are not so rigid, but are "moldable", e.g. the same job could run on 32 or 64 or 128 processors
- User makes choice at job submission time based on perceived trade-off between run time and wait time:
 - Large number of processors => lower execution time, but wait time will likely be longer
 - Small number of processors => lower wait time, but execution time is higher
- Why not let the scheduler decide the number of processors for each job, to optimize response time?
 - How many processors should each job be allocated?

Greedy Partition Size Choice

- Earliest proposed approach:
 Submit-time Greedy Choice +
 Conservative Backfill (Cirne)
- When job is submitted, earliest feasible reservation is determined for several possible partition sizes
- Partition size with earliest completion time is selected; job shape is frozen and reservation is made



Greedy Moldable Scheduling: Job Profile

Partition size	% Rigid Jobs	% Greedy Moldable Jobs
1	44.46	23.38
2	7.88	3.48
3-4	13.1	4.24
5-8	9.88	1.1
9-16	12.34	0
17-32	6.54	0
33-64	3.44	1.02
65-100	1.44	0.72
129-256	0.68	1.4
>256	0.24	64.66

- Rigid job trace (CTC from Feitelson's archive) used to evaluate Greedy moldable scheduling
- The majority of parallel jobs tend to choose very wide partition sizes with the Greedy scheme
- Light jobs (low processor-time product) suffer due to reduced backfilling opportunities

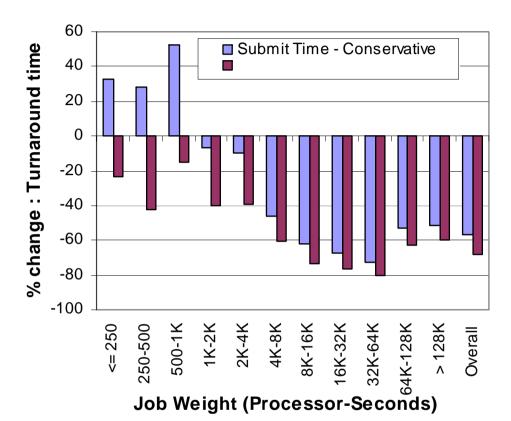
Work-Proportional "Fair-share" Limits

- Locally greedy choice for a job is often very wide:
 - Fills up processors, and reduces backfill opportunities
 - Uses more processor-seconds than narrow choice; lowers efficiency and increases offered load to system
- Use a load-sensitive "fair-share" limit to bound number of processors allowed for a job:
 - High limit at light loads and low limit at high loads

$$FS(i) = Nprocs * \frac{Processor_Seconds(i)}{\sum Processor_Seconds(j)}$$

$$Maxprocs(i) = Min(0.9 \times Nprocs, FS(i))$$

- Submit-time Conservative Fair-share Strategy
 - Similar to submit-time greedy strategy except for limit on max-procs for job
- Schedule-time Aggressive Fair-Share Strategy
 - Defers job's partition choice to start-time; hence can use aggressive back-fill



Enhancing Robustness

- Previously proposed moldable scheduling schemes
 - showed improved overall performance, but
 - sometimes improved some job categories (e.g. heavy jobs) while degrading other categories
- A robust moldable scheduling strategy should:
 - improve performance of all (most) job categories without significant detriment to any category
 - work well at low system loads as well as high loads
 - work well for jobs with high as well as poor scalability
 - work well under restrictions on partition sizes allowed for jobs
 (e.g. minimum number due to memory requirements or max. # due to poor scalability)
- Focus of this paper: making moldable schemes robust

Assessing Robustness of Scheduling Strategies

- We used Downey's model for job scalability:
 - Parameter σ models the coefficient of variance in parallelism:
 - $\sigma = 0 \Rightarrow \text{perfect job scalability}; S(n) = n$
 - Higher the value of σ , poorer the scalability
 - Given a σ for a job, and the run-time and number of processors from job trace, the run-time for a different processor count is found using Downey's model
- Range of allowed processor counts: limit by Range Factor (RF):
 - RF=1 => all partition sizes between 1 and Nprocs allowed
 - RF=2 => for a N-proc trace job, only one-half the range allowed, i.e. [(N+1)/2 ... (N+P)/2]
- Load variation: scaled all job run-times by a Load-Factor (LF):
 - With LF = 125%, each job's run-time is increased by 25%

Modifying the Fair-Share Strategy

- The Weight-Proportional Fair-Share (WPFS) model:
 - tends to assign #procs α job's weight, i.e. proc-seconds product
 - thus it attempts to equalize the run-times of all jobs
 - run-time dominated heavy jobs benefit while light jobs suffer
- Another extreme possibility: Equi-Processor Fair-Share (EPFS):
 - equal number of processors to all the jobs, light or heavy
 - would benefit light jobs but severely hurt heavy jobs
- These two schemes "equalize" jobs along orthogonal dimensions:
 - WPFS equalizes job run-time; #procs proportional to job weight
 - EPFS equalizes #procs; job run-time is proportional to job weight
- Considered a more "balanced" fair-share scheme that "split" a heavier job's weight across both the processor and time dimension:
 - A job with 4 times another job's weight is given twice as many processors,
 so that its run-time is twice as high

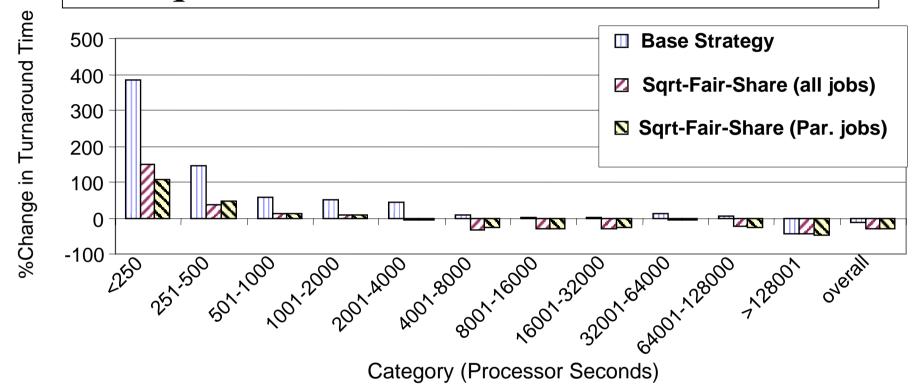
Square-Root Fair-Share Allocation

• A balance between the two extremes of WPFS and EPFS is achieved by the following square-root fair-share formula:

$$FairShare(i) = \left(\frac{\sqrt{Weight_i}}{\sum_{j} \sqrt{Weight_j}}\right) Numprocs$$

- Two variants:
 - Consider all jobs in determining job's fair-share limit
 - Consider only parallel jobs for computing fair-share limit

Square-Root Fair-Share Allocation



Performance with Sqrt-FS (SDSC log): Sigma=0, LF=100; RF=1

- Enhancements compared with Base Strategy: Schedule-time aggressive, Weight-Proportion Fair-Share; LF=100%, RF=1, σ=0
- All but the heaviest category improves; but lightest four categories are still worse than with rigid scheduling

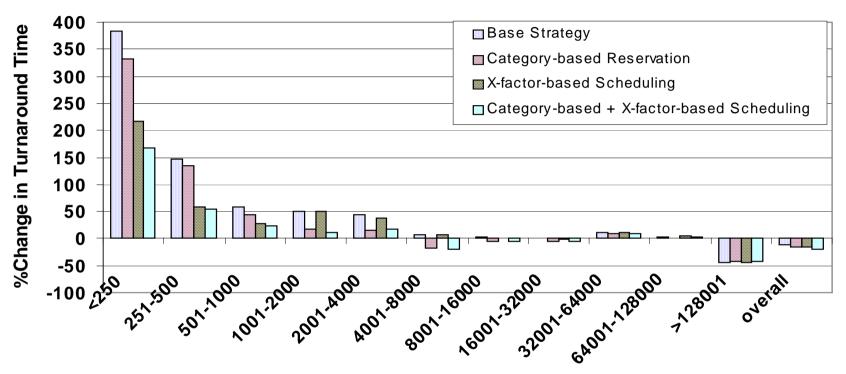
Enhanced Reservation Policies

- Category-based reservation:
 - Jobs partitioned into categories based on their weight
 - Multiple queues; reservation for job at head of each queue
- Xfactor-based reservation:
 - eXpansion-factor computed for each job, based on Expected Sequential Run Time (ESRT):

$$Xfactor = \frac{ESRT + Queue_Time}{ESRT}$$

Job is given reservation when XFactor exceeds threshold

Enhanced Reservation Policies: Performance

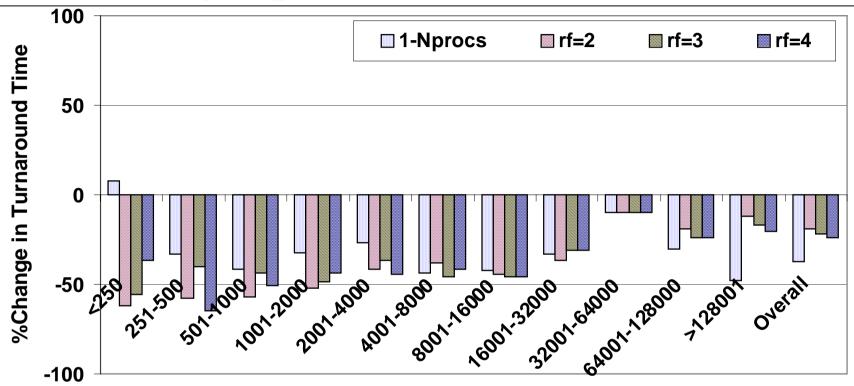


Category (Processor Seconds)

LF=100%, RF=1 and Sigma=0 (SDSC log)

- Category-based reservation improves all but the heaviest category
- X-factor-based reservation provides good improvement for lightest (three) categories; little/no improvement for others
- Combining category-based and X-factor-based reservations provides overall improvement corresponding to the better of both

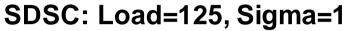
Combining Sqrt-FS & Enhanced Reservations

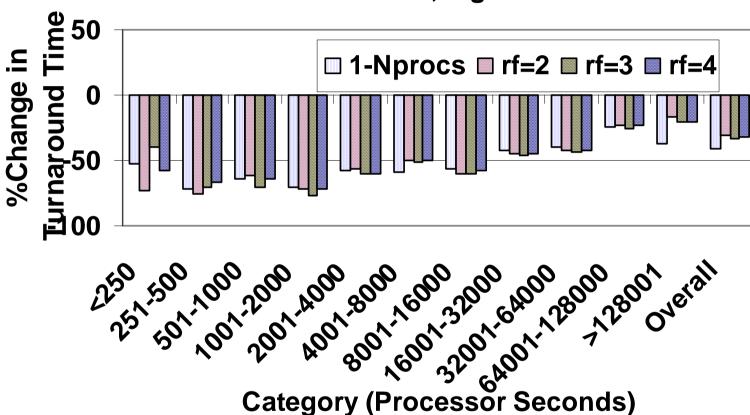


Category (Processor Seconds)

- All job categories do well when enhancements combined
- Benefit for light categories better than "sum of parts"
 - Sqrt-FS limits heavy jobs' procs: more back-fill for light jobs
 - Light jobs benefit from category-wise and Xfactor reservations

Evaluation under Imperfect Scalability



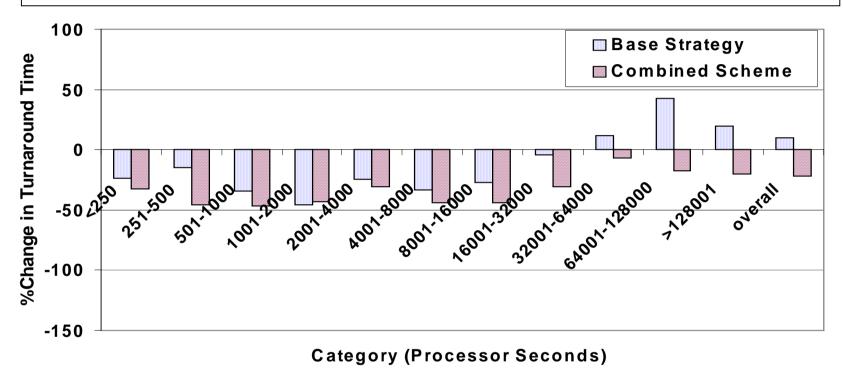


• Performance of all job categories improves, for various values of range factor

Evaluation with "Real" Scalability Data

- Evaluations so far used real job workload traces from Supercomputer Centers, but hypothetical scalability parameters (σ and RF)
- We also used NAS Parallel Benchmarks (NPB) performance data to model scalability
 - 8 applications' speedup characteristics on CRAY-T3E
 - Processor request-range is assumed to be the range represented by the available data for each application
 - Each job in SDSC job trace assumed to have scalability characteristic of one of the 8 NAS Parallel Benchmarks
 - Interpolation used to determine the execution times on different numbers of processors

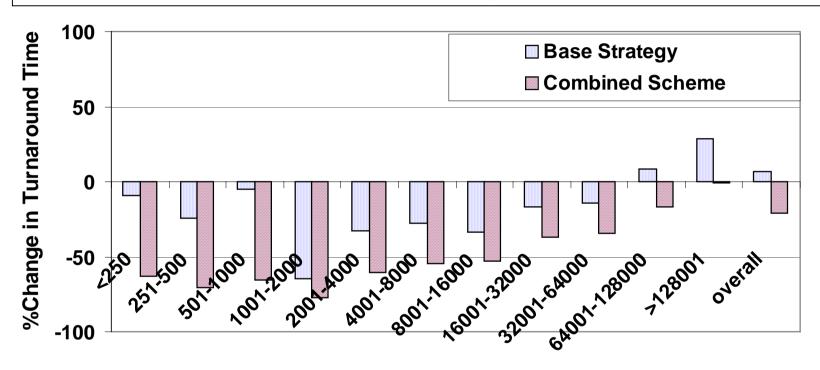
NPB-Based Scalability: Performance



Performance: LF = 100; SDSC log; NPB-based Scalability

 Performance of all job categories improves with new moldable strategy

NPB-Based Scalability: Performance



Category (Processor Seconds)

Performance: LF = 125; SDSC log; NPB-based Scalability

• Performance of all job categories improves with new scheme; better than base scheme for all categories

Conclusions

- Previous moldable scheduling schemes
 - Shown to be effective under some scenarios
 - But detrimental for some job categories especially when scalability is poor
- Modifications proposed to enhance robustness
 - Modified fair-share allocation based on square-root of job weights
 - Category-wise reservations; Xfactor-based reservations
 - Each of these enhancements provided some benefits, but when combined provided significantly greater benefits
 - All job categories improve over rigid scheduling, over wide range of simulation parameters