Machine Learning using Python

Scikit-learn

Scikit-learn (sklearn) is the main Python package for machine learning. It is a widely-used and well-regarded package. However, there are a couple of challenges to using it given the usual pandas -based data munging pipeline.

- 1. sklearn requires that all inputs be numeric, and in fact, numpy arrays.
- 2. sklearn requires that all categorical variables by replaced by 0/1 dummy variables
- 3. sklearn requires us to separate the predictors from the outcome. We need to have one x matrix for the predictors and one y vector for the outcome.

The big issue, of course, is the first point. Given we used pandas precisely because we wanted to be able to keep heterogenous data. We have to be able to convert non-numeric data to numeric. pandas does help us out with this problem.

- 1. First of all, we know that all pandas Series and DataFrame objects can be converted to numpy arrays using the values or to numpy functions.
- 2. Second, we can easily extract a single variable from the data set using either the usual extracton methods or the pop function.
- 3. Third, pandas gives us a way to convert all categorical values to numeric dummy variables using the get_dummies function. This is actually a more desirable solution than what you will see in cyberspace, which is to use the OneHotEncoder function from sklearn.
 - This is generally fine since many machine learning models look for interactions internally and don't
 need them to be overtly specified. The main exceptions to this are linear and logistic regression. For
 those, we can use the formula methods described in the Statistical Modeling module to generate
 the appropriately transformed design matrix.
 - If the outcome variable is not numeric, we can LabelEncoder function from the sklearn.preprocessing submodule to convert it.

I just threw a bunch of jargon at you. Let's see what this means.

Transforming the outcome/target

```
In [1]: import numpy as np
   import pandas as pd
   import sklearn
   import statsmodels.api as sm
   import matplotlib.pyplot as plt
   import seaborn as sns

iris = sm.datasets.get_rdataset('iris').data
   iris.head()
```

Out[1]:

	Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
0	5.1	3.5	1.4	0.2	setosa
1	4.9	3.0	1.4	0.2	setosa
2	4.7	3.2	1.3	0.2	setosa
3	4.6	3.1	1.5	0.2	setosa
4	5.0	3.6	1.4	0.2	setosa

Let's hit the first issue first. We need to separate out the outcome (the variable we want to predict) from the predictors (in this case the sepal and petal measurements).

```
In [2]: y = iris['Species']
X = iris.drop('Species', axis = 1) # drops column, makes a copy
```

Another way to do this is

```
In [3]: y = iris.pop('Species')
```

If you look at this, iris now only has 4 columns. So we could just use iris after the pop application, as the predictor set

We still have to update y to become numeric. This is where the sklearn functions start to be handy

```
In [4]: from sklearn.preprocessing import LabelEncoder
  le = LabelEncoder()
  y = le.fit transform(y)
  У
0,
     1,
     1,
     1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
  2,
     2,
```

Let's talk about this code, since it's very typical of the way the sklearn code works. First, we import a method (LabelEncoder) from the appropriate sklearn module. The second line, le = LabelEncoder() works to "turn on" the method. This is like taking a power tool off the shelf and plugging it in to a socket. It's now ready to work. The third line does the actual work. The fit_transform function transforms the data you input into it based on the method it is then attached to.

Let's make a quick analogy. You can plug in both a power washer and a jackhammer to get them ready to go. You can then apply each of them to your driveway. They "transform" the driveway in different ways depending on which tool is used. The washer would "transform" the driveway by cleaning it, while the jackhammer would transform the driveway by breaking it.

There's an interesting invisible quirk to the code, though. The object le also got transformed during this process. There were pieces added to it during the fit transform process.

```
In [5]: le = LabelEncoder()
d1 = dir(le)

In [6]: y = le.fit_transform( pd.read_csv('data/iris.csv')['species'])
d2 = dir(le)
set(d2).difference(set(d1)) # set of things in d2 but not in d1

Out[6]: {'classes_'}
```

So we see that there is a new component added, called classes .

```
In [7]: le.classes_
Out[7]: array(['setosa', 'versicolor', 'virginica'], dtype=object)
```

So the original labels aren't destroyed; they are being stored. This can be useful.

So we can transform back from the numeric to the labels. Keep this in hand, since it will prove useful after we have done some predictions using a ML model, which will give numeric predictions.

Transforming the predictors

Let's look at a second example. The diamonds dataset has several categorical variables that would need to be transformed.

```
In [9]: diamonds = pd.read_csv('data/diamonds.csv.gz')

y = diamonds.pop('price').values
X = pd.get_dummies(diamonds)

# Alternatively
# import patsy
# f = '~ np.log(carat) + + clarity + depth + cut * color'
# X = patsy.dmatrix(f, data=diamonds)
In [10]: type(X)
Out[10]: pandas.core.frame.DataFrame
```

In [11]: X.info()

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 53940 entries, 0 to 53939
Data columns (total 26 columns):
                    Non-Null Count Dtype
 #
     Column
     _____
                    _____
                                    ____
 0
                    53940 non-null
                                   float64
     carat
 1
     depth
                    53940 non-null float64
 2
     table
                    53940 non-null float64
 3
     х
                    53940 non-null
                                   float64
 4
                    53940 non-null float64
    У
 5
                    53940 non-null
                                   float64
 6
    cut Fair
                    53940 non-null
                                    uint8
 7
                                   uint8
     cut_Good
                    53940 non-null
 8
     cut Ideal
                    53940 non-null
                                    uint8
 9
     cut_Premium
                    53940 non-null
                                   uint8
                                   uint8
                    53940 non-null
 10
    cut_Very Good
 11
    color D
                    53940 non-null
                                    uint8
 12
     color E
                    53940 non-null
                                    uint8
 13
    color_F
                    53940 non-null
                                    uint8
 14
    color G
                    53940 non-null
                                   uint8
 15
    color H
                    53940 non-null
                                    uint8
 16
    color I
                    53940 non-null
                                   uint8
    color J
 17
                    53940 non-null
                                    uint8
 18
    clarity I1
                    53940 non-null
                                    uint8
 19
    clarity_IF
                    53940 non-null
                                   uint8
 20
    clarity SI1
                    53940 non-null
                                   uint8
 21
    clarity_SI2
                    53940 non-null
                                   uint8
 22 clarity_VS1
                    53940 non-null
                                    uint8
 23
    clarity VS2
                    53940 non-null
                                    uint8
 24
    clarity_VVS1
                    53940 non-null
                                    uint8
 25
    clarity_VVS2
                    53940 non-null
                                    uint8
dtypes: float64(6), uint8(20)
memory usage: 3.5 MB
```

So everything is now numeric!!. Let's take a peek inside.

So, it looks like the continuous variables remain intact, but the categorical variables got exploded out. Each variable name has a level with it, which represents the particular level it is representing. Each of these variables, called dummy variables, are numerical 0/1 variables. For example, color_F is 1 for those diamonds which have color F, and 0 otherwise.

```
In [13]: pd.crosstab(X['color_F'], diamonds['color'])
Out[13]:
             color
                          Ε
                                      G
                                           Н
                                                 ı
                                                      J
           color F
                0 6775 9797
                                0 11292
                                         8304
                                              5422
                                                   2808
                1
                     0
                           0 9542
                                      0
                                            0
                                                 0
                                                      0
```

Supervised Learning

We will first look at supervised learning methods.

Code to call it	ML method
sklearn.tree.DecisionTreeClassifier, sklearn.tree.DecisionTreeRegressor	Decision Tree
<pre>sklearn.ensemble.RandomForestClassifier, sklearn.ensemble.RandomForestRegressor</pre>	Random Forest
sklearn.linear_model.LinearRegression	Linear Regression
sklearn.linear_model.LogisticRegression	Logistic Regression
sklearn.svm.LinearSVC, sklearn.svm.LinearSVR	Support Vector Machines

The general method that the code will follow is:

```
from sklearn... import Machine
machine = Machine(*parameters*)
machine.fit(X, y)
```

A quick example

```
In [14]: from sklearn.linear_model import LinearRegression
    from sklearn.tree import DecisionTreeRegressor

lm = LinearRegression()
    dt = DecisionTreeRegressor()
```

Lets manufacture some data

```
In [15]: x = np.linspace(0, 10, 200)
y = 2 + 3*x - 5*(x**2)
d = pd.DataFrame({'x': x})

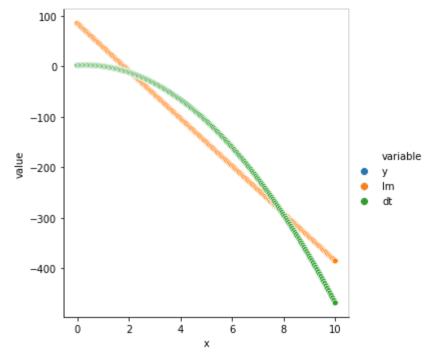
lm.fit(d,y);
dt.fit(d, y);

p1 = lm.predict(d)
p2 = dt.predict(d)

d['y'] = y
d['lm'] = p1
d['dt'] = p2

D = pd.melt(d, id_vars = 'x')

sns.relplot(data=D, x = 'x', y = 'value', hue = 'variable');
plt.show()
```



A data analytic example

7 of 23

```
In [16]:
         diamonds = pd.read csv('data/diamonds.csv.gz')
         diamonds.info()
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 53940 entries, 0 to 53939
         Data columns (total 10 columns):
                       Non-Null Count Dtype
              Column
          0
                       53940 non-null float64
              carat
                       53940 non-null object
          1
              cut
          2
              color
                       53940 non-null object
          3
              clarity 53940 non-null object
          4
              depth
                       53940 non-null float64
          5
              table
                       53940 non-null float64
              price
                       53940 non-null int64
          6
          7
                       53940 non-null float64
              Х
          8
              У
                       53940 non-null float64
          9
                       53940 non-null float64
         dtypes: float64(6), int64(1), object(3)
         memory usage: 4.1+ MB
```

First, lets separate out the outcome (price) and the predictors

```
In [17]: y = diamonds.pop('price')
```

For many machine learning problems, it is useful to scale the numeric predictors so that they have mean 0 and variance 1. First we need to separate out the categorical and numeric variables

```
In [18]: d1 = diamonds.select_dtypes(include = 'number')
d2 = diamonds.select_dtypes(exclude = 'number')
```

Now let's scale the columns of d1

```
In [19]: from sklearn.preprocessing import scale
         bl = scale(d1)
         bl
Out[19]: array([[-1.19816781, -0.17409151, -1.09967199, -1.58783745, -1.536195
         56,
                 -1.57112919],
                [-1.24036129, -1.36073849, 1.58552871, -1.64132529, -1.658774]
         19,
                 -1.74117497],
                [-1.19816781, -3.38501862, 3.37566251, -1.49869105, -1.457395]
         02,
                 -1.74117497],
                [-0.20662095, 0.73334442, 1.13799526, -0.06343409, -0.047740]
         83,
                  0.03013526],
                [0.13092691, -0.52310533, 0.24292836, 0.37338325, 0.337506]
         27,
                  0.28520393],
                [-0.10113725, 0.31452784, -1.09967199, 0.08811478, 0.118615]
         87,
                  0.14349912]])
```

Woops!! We get a numpy array, not a DataFrame!!

```
In [20]: bl = pd.DataFrame(scale(d1))
bl.columns = list(d1.columns)
d1 = bl
```

Now, let's recode the categorical variables into dummy variables.

```
In [21]: d2 = pd.get_dummies(d2)
```

and put them back together

```
In [22]: X = pd.concat([d1,d2], axis = 1)
```

Next we need to split the data into a training set and a test set. Usually we do this as an 80/20 split. The purpose of the test set is to see how well the model works on an "external" data set. We don't touch the test set until we're done with all our model building in the training set. We usually do the split using random numbers. We'll put 40,000 observations in the training set.

There is another way to do this

```
In [24]: from sklearn.model_selection import train_test_split

X_train, X_test, y_train, y_test = train_test_split(X, y , test_size = 0.2, random_state= 40)
```

Now we will fit our models to the training data. Let's use a decision tree model, a random forest model, and a linear regression.

```
In [25]: from sklearn.linear_model import LinearRegression
    from sklearn.tree import DecisionTreeRegressor
    from sklearn.ensemble import RandomForestRegressor

lm = LinearRegression();
    dt = DecisionTreeRegressor();
    rf = RandomForestRegressor();
```

Now we will use our training data to fit the models

```
In [26]: lm.fit(X_train, y_train);
    dt.fit(X_train, y_train);
    rf.fit(X_train, y_train);
```

We now need to see how well the model fit the data. We'll use the R2 statistic to be our metric of choice to evaluate the model fit.

```
In [27]: from sklearn.metrics import r2_score

pd.DataFrame({
    'Model': ['Linear regression','Decision tree','Random forest'],
    'R2': [r2_score(y_train, lm.predict(X_train)),
        r2_score(y_train, dt.predict(X_train)),
        r2_score(y_train, rf.predict(X_train))]
})

Out[27]:

Model R2
```

	Model	R2
0	Linear regression	0.920264
1	Decision tree	0.999997
2	Random forest	0.997360

This is pretty amazing. However, we know that if we try and predict using the same data we used to train the model, we get better than expected results. One way to get a better idea about the true performance of the model when we will try it on external data is to do cross-validation.

Visualizing a decision tree

scikit-learn provides a decent way of visualizing a decision tree using a program called *Graphviz*, which is a dedicated graph and network visualization program.

carat <= 0.416 mse = 15852573.11 samples = 43152 value = 3925.87 Out[28]: y <= -0.183 mse = 1250735.975 y <= 1.279 nse = 15319732.951 samples = 27947 samples = 15205 value = 8136.181 value = 1635.185 y <= -0.648 mse = 267632.084 carat <= 0.12 mse = 781351.904 clarity_SI2 <= 0.5 y <= 1.822 mse = 11615083.581 nse = 4663622.549 samples = 19909 value = 1054.442 samples = 8038 value = 3073.602 samples = 10283 value = 6130.315 samples = 4922 value = 12326.819 mse = 56682.753 samples = 14037 value = 788.904 mse = 200417.909 mse = 408841.396 mse = 663914.604 = 902632.244 samples = 3152 value = 10919.98 samples = 5872 value = 1689.212 samples = 5742 value = 2727.454 samples = 2296 value = 3939.274 samples = 7603 value = 6644.344 samples = 2680 value = 4672.047

```
In [29]: graph.render('graphs/image', view=False, format='pdf');
    graph.render('graphs/image', view = False, format = 'png');
```

Cross-validation

In cross-validation, we split the dataset up into 5 equal parts randomly. We then train the model using 4 parts and predict the data on the 5th part. We do for all possible groups of 4 parts. We then consider the overall performance of prediction.

There is nothing special about the 5 splits. If you use 5 splits, it is called 5-fold cross-validation (CV), if you use 10 splits, it is 10-fold CV. If you use all but one subject as training data, and that one subject as test data, and cycle through all the subjects, that is called leave-one-out CV (L OOCV). All these methods are widely used, but 5- and 10-fold CV are often used as a balance between effectiveness and computational efficiency.

scikit-learn makes this pretty easy, using the <code>cross_val_score</code> function.

Improving models through cross-validation

The cross-validation error, as we've seen, gives us a better estimate of how well our model predicts on new data. We can use this to tune models by tweaking their parameters to get models that reasonably will perform better.

Each model that we fit has a set of parameters that govern how it proceeds to fit the data. These can bee seen using the <code>get_params</code> function.

```
In [31]: dt.get_params()
le.get_params()
Out[31]: {}
```

Linear regression is entirely determined by the functional form of the prediction equation,i.e., the "formula" we use. It doesn't have any parameters to tune per se. Improving a linear regression involves playing with the different predictors and transforming them to improve the predictions. This involve subjects called *regression diagnostics* and *feature engineering* that we will leave to Google for now.

We can tune different parameters for the decision tree to try and see if some combination of parameters can improve predictions. One way to do this, since we're using a computer, is a grid search. This means that we can set out sets of values of the parameters we want to tune, and the computer will go through every combination of those values to see how the model performs, and will provide the "best" model.

We would specify the values as a dictionary to the function <code>GridSearchCV</code>, which would optimize based on the cross-validation error.

So how does this do on the test set?

So this predictor is doing slightly better on the test set than the training set. This is often an indicator that the model is overfitting on the data. This is probable here, given the extremely high R2 values for this model.

Feature selection

We can also use cross-validation to do recursive feature selection (or backwards elimination), based on a predictive score. This is different from usual stepwise selection methods which are based on a succession of hypothesis tests.

```
In [34]: from sklearn.feature selection import RFECV
         selector = RFECV(lm, cv = 5, scoring = 'r2')
         selector = selector.fit(X train, y train)
         selector.support
Out[34]: array([ True, False, False,
                                       True, False, False,
                                                            True, False,
                                                                           True,
                 True,
                        True,
                               True,
                                       True,
                                              True,
                                                     True, False,
                                                                    True,
                                                                           True,
                 True,
                        True, False,
                                       True,
                                              True,
                                                     True,
                                                            True,
                                                                    True])
```

The support gives the set of predictors (True) that are finally selected.

This is indicating that the best predictive model for the linear regression includes carat, cut, color and clarity, and width of the stone.

Logistic regression

We noted that logistic regression is available both through **statsmodels** and through **scikit-learn**. Let's now try to fit a logistic regression model using **scikit-learn**. We will use the same Titanic dataset we used earlier.

```
In [36]: import pandas as pd
         import statsmodels.api as sm
         import statsmodels.formula.api as smf
         from sklearn.linear model import LogisticRegression
         titanic = sm.datasets.get rdataset('Titanic','Stat2Data').data.dropna
         ()
         titanic.info()
         <class 'pandas.core.frame.DataFrame'>
         Int64Index: 756 entries, 0 to 1312
         Data columns (total 6 columns):
          #
              Column
                        Non-Null Count Dtype
              Name
          0
                        756 non-null
                                        object
              PClass
                        756 non-null
                                        object
          1
                                        float64
          2
              Age
                        756 non-null
          3
                        756 non-null
                                        object
              Sex
          4
              Survived 756 non-null
                                        int64
                        756 non-null
          5
              SexCode
                                        int64
         dtypes: float64(1), int64(2), object(3)
         memory usage: 41.3+ KB
```

We will model Survived on the age, sex and passenger class of passengers.

There are a few differences that are now evident between this model and the model we fit using **statsmodels**. As a reminder, we fit this model again below.

```
In [38]: titanic1 = titanic.loc[X_train.index,:]
    titanic2 = titanic.loc[X_test.index,:]
    mod_logistic = smf.glm('Survived ~ Age + Sex + PClass', data=titanic1,
        family = sm.families.Binomial()).fit()
    mod_logistic.summary()
```

Out[38]:

Generalized Linear Model Regression Results

604	No. Observations:	Survived	Dep. Variable:
599	Df Residuals:	GLM	Model:
4	Df Model:	Binomial	Model Family:
1.0000	Scale:	logit	Link Function:
-282.34	Log-Likelihood:	IRLS	Method:
564.68	Deviance:	Wed, 09 Dec 2020	Date:
666.	Pearson chi2:	12:39:47	Time:

No. Iterations: 5

Covariance Type: nonrobust

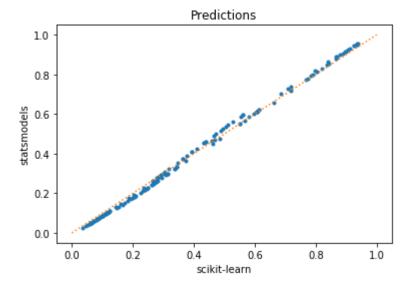
	coef	std err	z	P> z	[0.025	0.975]
Intercept	3.6795	0.440	8.362	0.000	2.817	4.542
Sex[T.male]	-2.5138	0.221	-11.353	0.000	-2.948	-2.080
PClass[T.2nd]	-1.2057	0.290	-4.155	0.000	-1.774	-0.637
PClass[T.3rd]	-2.5974	0.305	-8.528	0.000	-3.194	-2.000
Age	-0.0367	0.008	-4.385	0.000	-0.053	-0.020

We can see the objects that are available to us from the two models using dir(lrm) and dir(mod_logistic). We find that lrm does not give us any parameter estimates, p-values or summary methods. It is much leaner, and, in line with other machine learning models, emphasizes predictions. So if you want to find associations between predictors and outcome, you will have to use the statsmodels version.

Let's compare the predictions.

```
In [39]: plt.clf()
    p1 = lrm.predict_proba(X_test)[:,1]
    p2 = mod_logistic.predict(titanic2)

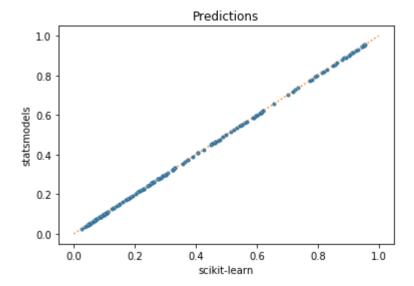
    plt.plot(p1, p2, '.');
    plt.plot([0,1],[0,1], ':');
    plt.xlabel('scikit-learn');
    plt.ylabel('statsmodels');
    plt.title('Predictions');
    plt.show()
```



First note that the prediction functions work a bit differently. For <code>lrm</code> we have to explicitly ask for the probability predictions, whereas those are automatically provided for <code>mod_logistic</code>. We also find that the predictions aren't exactly the same. This is because <code>lrm</code>, by default, runs a penalized regression using the lasso criteria (L2 norm), rather than the non-penalized version that <code>mod_logistic</code> runs. We can specify no penalty for <code>lrm</code> and can see much closer agreement between the two models.

```
In [40]: lrm = LogisticRegression(penalty='none')
    lrm.fit(X_train, y_train)
    p1 = lrm.predict_proba(X_test)[:,1]

    plt.clf()
    plt.plot(p1, p2, '.');
    plt.plot([0,1],[0,1], ':');
    plt.xlabel('scikit-learn');
    plt.ylabel('statsmodels');
    plt.title('Predictions');
    plt.show()
```



Unsupervised learning

Unsupervised learning is a class of machine learning methods where we are just trying to identify patterns in the data without any labels. This is in contrast to *supervised learning*, which are the modeling methods we have discussed above.

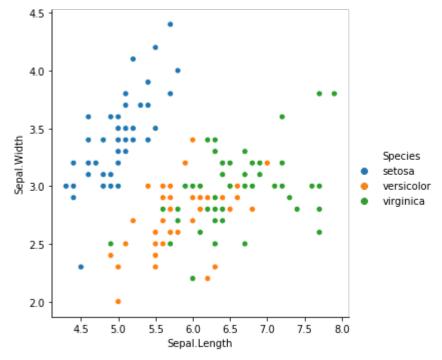
Most unsupervised learning methods fall broadly into a set of algorithms called *cluster analysis*. **scikit-learn** provides several clustering algorithms.

We will demonstrate the two more popular choices -- K-Means and Agglomerative clustering (also known as hierarchical clustering). We will use the classic Fisher's Iris data for this demonstration.

```
In [41]: import statsmodels.api as sm
  import pandas as pd
  import matplotlib.pyplot as plt
  import seaborn as sns

from sklearn.cluster import KMeans, AgglomerativeClustering

iris = sm.datasets.get_rdataset('iris').data
  sns.relplot(data=iris, x = 'Sepal.Length',y = 'Sepal.Width', hue = 'Species');
```



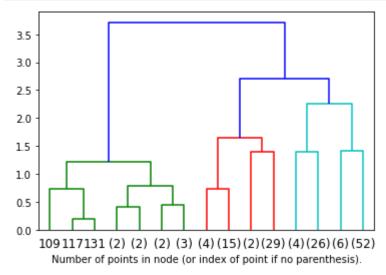
The K-Means algorithm takes a pre-specified number of clusters as input, and then tries to find contiguous regions of the data to parse into clusters.

```
In [42]: km = KMeans(n_clusters = 3)
km.fit(iris[['Sepal.Length','Sepal.Width']]);
```

```
In [43]:
        km.labels
2,
              2,
              2, 2, 2, 2, 2, 2, 1, 1, 1, 0, 1, 0, 1, 0, 1, 0, 0, 0, 0, 0, 0,
        1,
              0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 1,
        0,
              0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1, 1, 1, 1, 0, 1, 1,
        1,
              1, 1, 1, 0, 0, 1, 1, 1, 1, 0, 1, 0, 1, 0, 1, 1, 0, 0, 1, 1, 1,
        1,
              1, 0, 0, 1, 1, 1, 0, 1, 1, 1, 0, 1, 1, 1, 0, 1, 1, 0], dtype=i
        nt32)
In [44]:
        iris['km labels'] = km.labels
        iris['km labels'] = iris.km labels.astype('category')
        sns.relplot(data=iris, x = 'Sepal.Length', y = 'Sepal.Width',
                  hue = 'km labels');
          4.5
          4.0
          3.5
        Sepal.Width
                                               km labels
          3.0
          2.5
          2.0
               4.5
                   5.0
                       5.5
                          6.0
                              6.5
                                  7.0
                                      7.5
                                          8.0
                        Sepal.Length
```

Agglomerative clustering takes a different approach. It starts by coalescing individual points successively, based on a distance metric and a principle for how to coalesce groups of points (called *linkage*). The number of clusters can then be determined either visually or via different cutoffs.

```
In [47]: from scipy.cluster.hierarchy import dendrogram
         ## The following is from https://scikit-learn.org/stable/auto_examples
         /cluster/plot agglomerative dendrogram.html
         def plot dendrogram(model, **kwargs):
             # Create linkage matrix and then plot the dendrogram
             # create the counts of samples under each node
             counts = np.zeros(model.children .shape[0])
             n samples = len(model.labels )
             for i, merge in enumerate(model.children ):
                 current count = 0
                 for child idx in merge:
                      if child idx < n samples:</pre>
                          current count += 1 # leaf node
                      else:
                         current count += counts[child idx - n samples]
                 counts[i] = current count
             linkage matrix = np.column stack([model.children , model.distances
                                                counts]).astype(float)
             # Plot the corresponding dendrogram
             dendrogram(linkage_matrix, **kwargs)
         plot dendrogram(hc, truncate mode='level', p=3)
         plt.xlabel("Number of points in node (or index of point if no parenthe
         sis).")
         plt.show()
```



```
In [49]:
     hc.labels
0,
           0, 0, 0, 0, 0, 0, 2, 2, 2, 2, 2, 2, 2, 0, 2, 0, 0, 2, 2, 2, 2,
      2,
           2,
           2, 2, 2, 2, 2, 0, 2, 2, 2, 0, 2, 2, 2, 1, 2, 2, 1, 0, 1, 2,
      1,
           2, 2, 2, 2, 2, 2, 2, 1, 1, 2, 2, 2, 1, 2, 2, 1, 2, 2, 1, 1,
      1,
           In [50]: iris['hc labels'] = pd.Series(hc.labels ).astype('category')
      sns.relplot(data=iris, x = 'Sepal.Length', y= 'Sepal.Width',
              hue = 'hc labels');
        4.5
        4.0
        3.5
      Sepal.Width
                                     hc_labels
        3.0
        2.5
        2.0
           4.5
              5.0
                 5.5
                     6.0
                        6.5
                           7.0
                              7.5
                                 8.0
                   Sepal.Length
```

Play around with different linkage methods to see how these clusters change.