- 2. [FC] After you assign a value to a variable, consider all of its neighbors. Eliminate any options from its neighbors that are incompatible with the value you just assigned.
- 3. [PROP-1] If you eliminate options from a neighbor in the previous step, and that neighbor has only one option left, add that neighbor to the list of variables to propagate. Propagate all the variables in the list.

To propagate a singleton variable, take note of its one remaining option and consider each of its neighbors. You want to cross off values in the neighboring variables that are incompatible with the one remaining option. Then, if you cross off options in a neighboring variable, and that neighbor has only one option left, add that neighbor to the list of variables to propagate.

## 4. Depth first search + forward checking + propagation through reduced domains

This strategy eliminates impossible options from neighboring variables. If it successfully eliminates any options from those variables, it looks ahead to see what else it can eliminate.

- 1. [DFS] After you assign a value to a variable, examine all of the variables you've assigned values so far, and make sure those values are consistent with the constraints. If they aren't, backtrack.
- 2. [FC] After you assign a value to a variable, consider all of its neighbors. Eliminate any options from its neighbors that are incompatible with the value you just assigned.
- 3. [PROP-ANY] If you eliminate any options from a neighbor in the previous step, add that neighbor to the list of variables to propagate. Propagate all the variables in the list.

To propagate a reduced variable, take note of its remaining options and consider each of its neighbors. You want to cross off values in the neighboring variables that are incompatible with every one of the remaining options. If you cross off any values in a neighboring variable, add that neighbor to the list of variables to propagate.

**Note 1:** Notice that none of these pruning options ever assign values to a variable; they only remove values from consideration.

Note 2: There's always an implicit "escape clause" in a constraint satisfaction problem, namely:

If you ever eliminate *all* the options from a variable, then you can't solve the problem with the assignments you've made so far. Backtrack.

## \* Domain reduction before search begins

This procedure eliminates impossible options from domains before you even begin searching and assigning values to variables. Like strategy (4), it uses the subroutine for *propagating reduced* variables.

- 1. Add all the variables in the problem to the list of variables to propagate.
- 2. Until the list is empty, propagate each variable in the list.
- 3. [PROP-ANY] If you eliminate any options from a neighbor in the previous step, add that neighbor to the list of variables to propagate. Propagate all the variables in the list.

As before, to *propagate a reduced variable*, take note of its remaining options and consider each of its neighbors. You want to cross off values in the neighboring variables that are incompatible with every one of the remaining options. If you cross off any values in a neighboring variable, add that neighbor to the list of variables to propagate.