



NEOTOMA  
PALEOECOLOGY  
DATABASE



EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

---

# Depth-age models

What are they for and how to make them?  
Some examples using the EPD

**Petr Kuneš and Graciela Gil-Romera**

[petr.kunes@natur.cuni.cz](mailto:petr.kunes@natur.cuni.cz) | [graciela.gil@ipe.csic.es](mailto:graciela.gil@ipe.csic.es)

<https://petr.kunes.net/> | <https://gilromera.com/>

---



NEOTOMA  
PALEOECOLOGY  
DATABASE



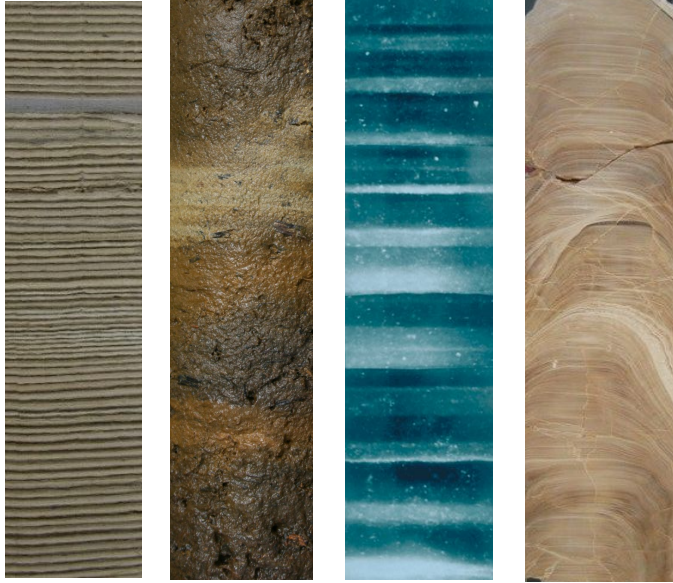
EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

**Our palaeoecological  
interpretations can only be as  
good as our chronological  
(un)certainties.**

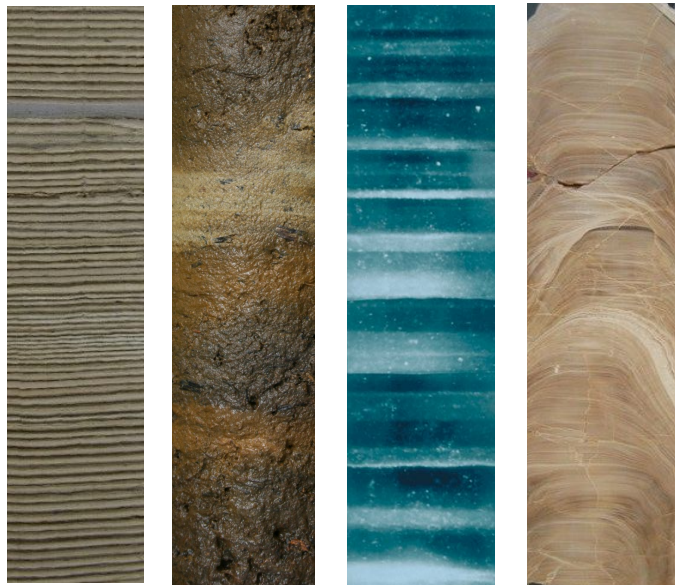


**Our palaeoecological  
interpretations can only be as  
good as our chronological  
uncertainties.**





**Our palaeoecological  
interpretations can only be as  
good as our chronological  
uncertainties.**

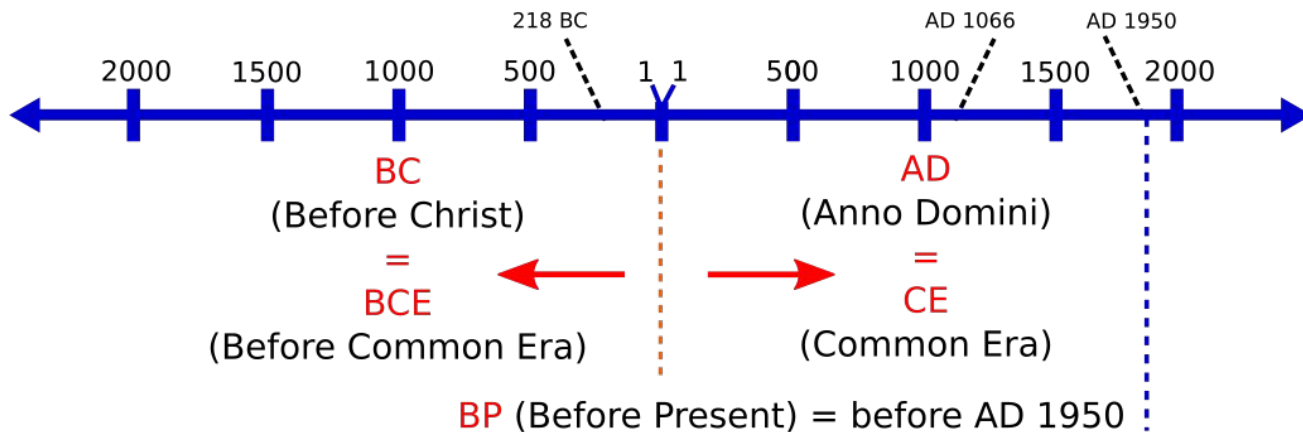




# What is our timeline?

(not entering orbital descriptions)

## BC - BCE and AD - CE Terms



- BC/AD: Before Christ - Anno Domini
- BCE-CE: Before Common Era - Common Era
- BP: Before Present, 1950 CE

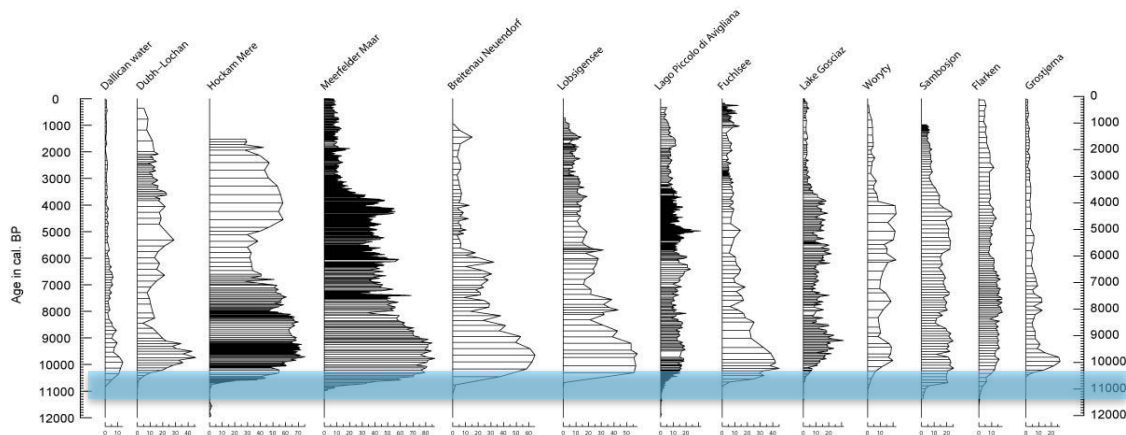
**No-zero value**



# Dating techniques - absolute vs relative



*Corylus*





# Dating techniques - absolute vs relative

Quaternary Science Reviews 117 (2015) 1–41



ELSEVIER

Contents lists available at ScienceDirect

## Quaternary Science Reviews

journal homepage: [www.elsevier.com/locate/quascirev](http://www.elsevier.com/locate/quascirev)



Invited review

### Varves in lake sediments – a review

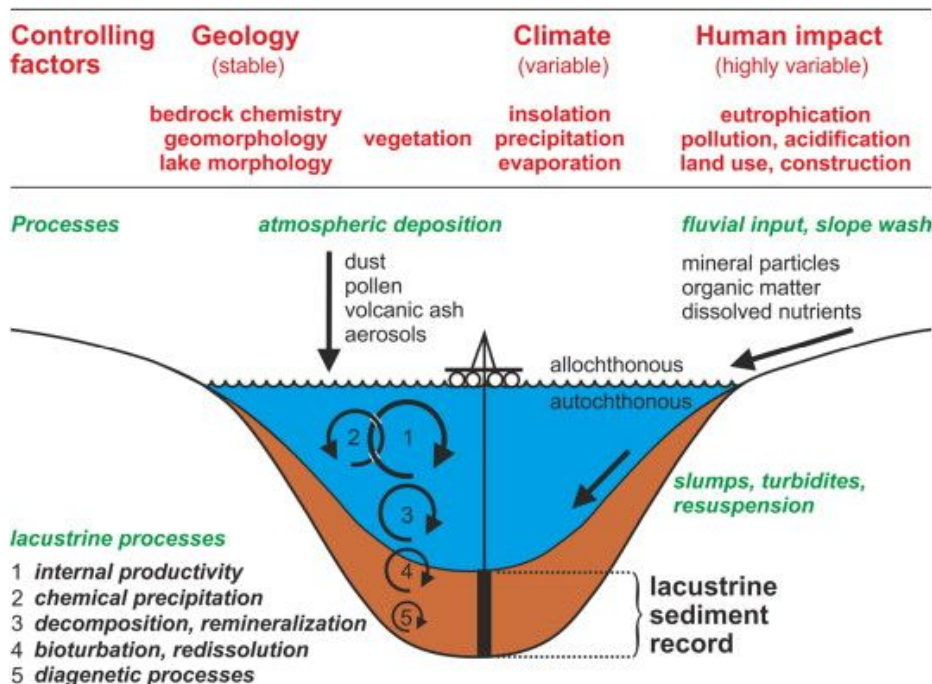
Bernd Zolitschka <sup>a, \*</sup>, Pierre Francus <sup>b, c</sup>, Antti E.K. Ojala <sup>d</sup>, Arndt Schimmelmann <sup>e</sup>







# Dating techniques - absolute vs relative



[Zolitschka, B., et al 2015. Varves in lake sediments – a review. Quaternary Science Reviews 117, 1–41.](#)





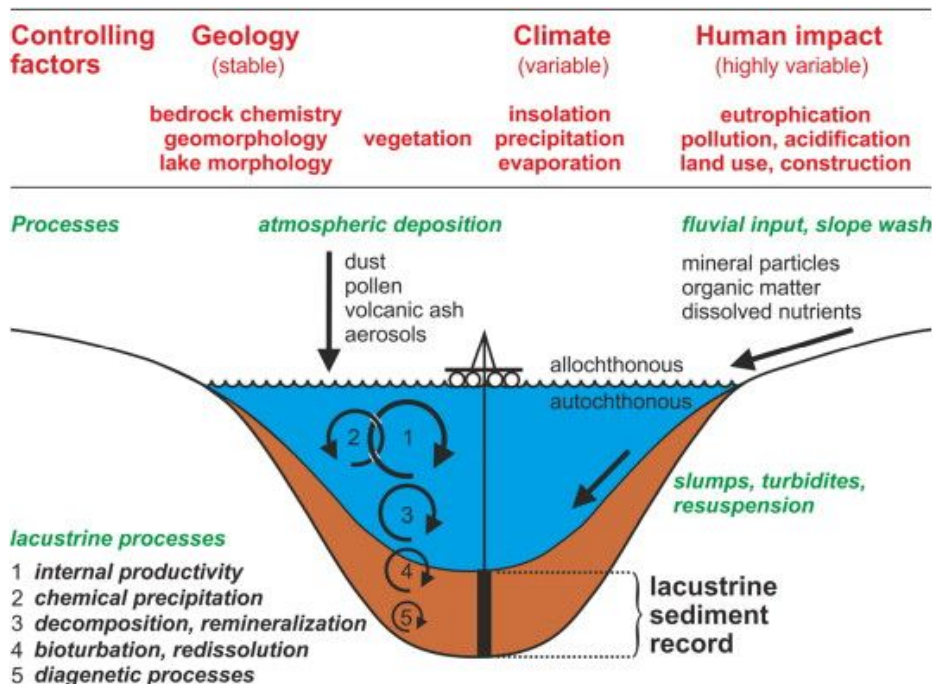
# Dating techniques - absolute vs relative

## Radiometric dating

- $^{14}\text{C}$
- U/Th
- $^{210}\text{Pb}$
- $^{36}\text{Cl}$
- $^{40}\text{Ar}$
- Luminescence (not technically a radiometric one)



[Zolitschka, B., et al 2015. Varves in lake sediments – a review. Quaternary Science Reviews 117, 1–41.](#)





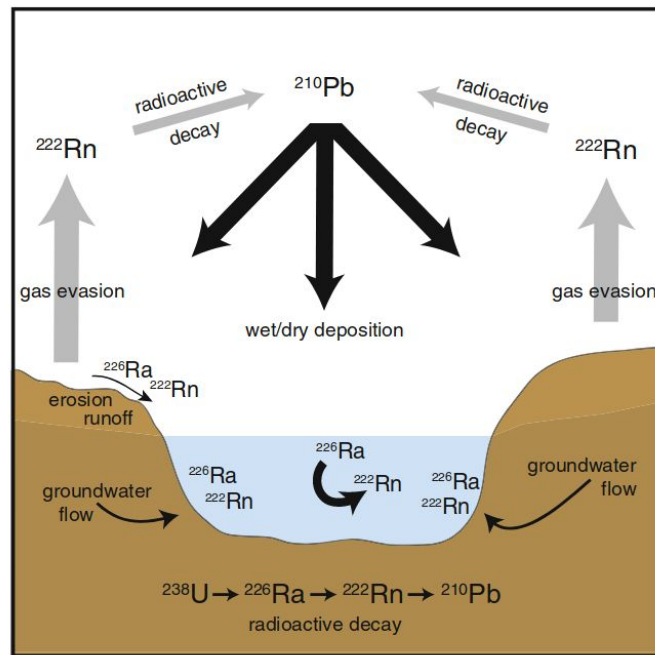
## Radiometric dating

- **$^{210}\text{Pb}$**

Pb-210 is a naturally occurring radionuclide of the  $^{238}\text{U}$  radioactive decay chain and has a half-life of 22.23 years.

- Does not experience seasonal variations, and atmospheric concentration is constant  $\rightarrow$  No need to transform into calendar years, so no calibration.
- Needs different depositional models.

## Dating techniques - absolute vs relative

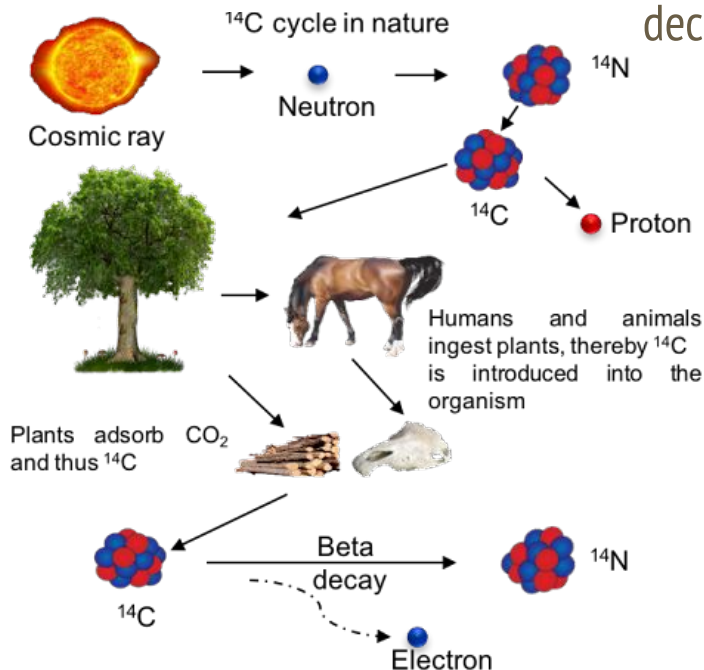




# Dating techniques - absolute vs relative

## Radiometric dating $^{14}\text{C}$

All living organisms fix  $^{14}\text{C}$ , a carbon isotope which half-life time decay is known.



When an animal or plant dies, it will not take in any more carbon, and the  $^{14}\text{C}$  present will begin to decay. We can thus measure how long it's been since the animal or plant died by comparing the presence of  $^{14}\text{C}$  with the known half-life.



# Calibrating, why and how?

## Radiometric dating $^{14}\text{C}$

$^{14}\text{C}$  dating provides “radiocarbon measurements”, i.e. a date that we cannot accurately place in a calendar:

### Changing atmospheric concentration of $^{14}\text{C}$ over time

- fluctuations in the Earth's geomagnetic moment,
- fossil fuel burning,
- and nuclear testing.

$^{14}\text{C}$



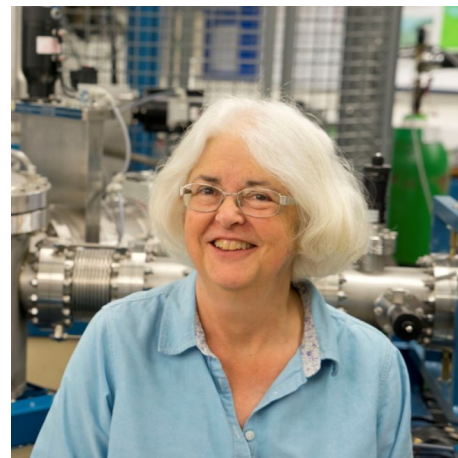


Radiometric dating  $^{14}\text{C}$

## Calibrating, why and how?

Calibration algorithm = curve

“Bristlecone pines” rings *Pinus longaeva* D.K.Bailey



Paula Reimer





NEOTOMA  
PALEOECOLOGY  
DATABASE

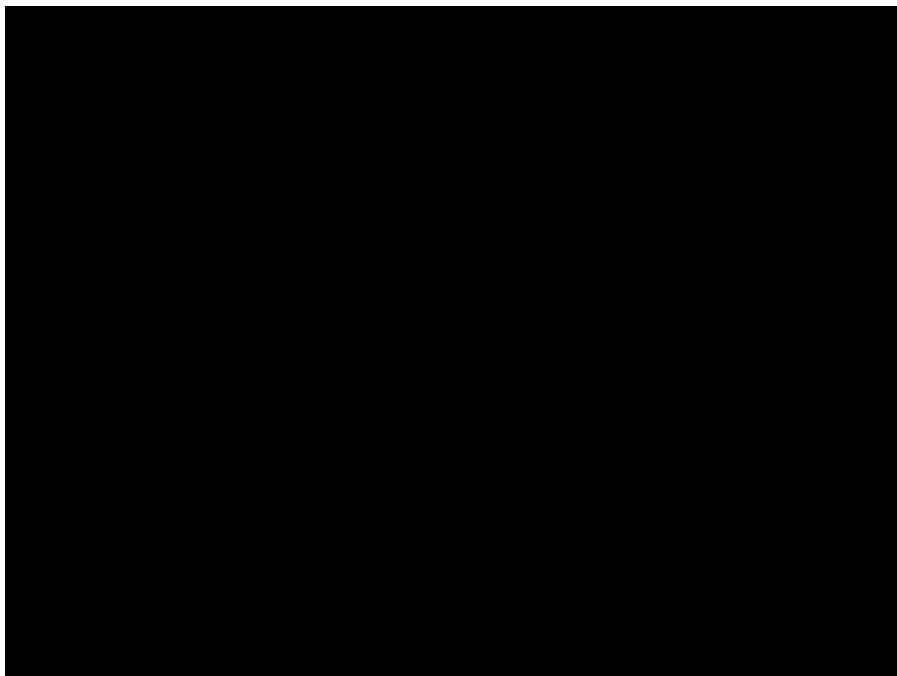


EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

# Calibrating, why and how?

Calibration algorithm = curve



Maarten Blaauw

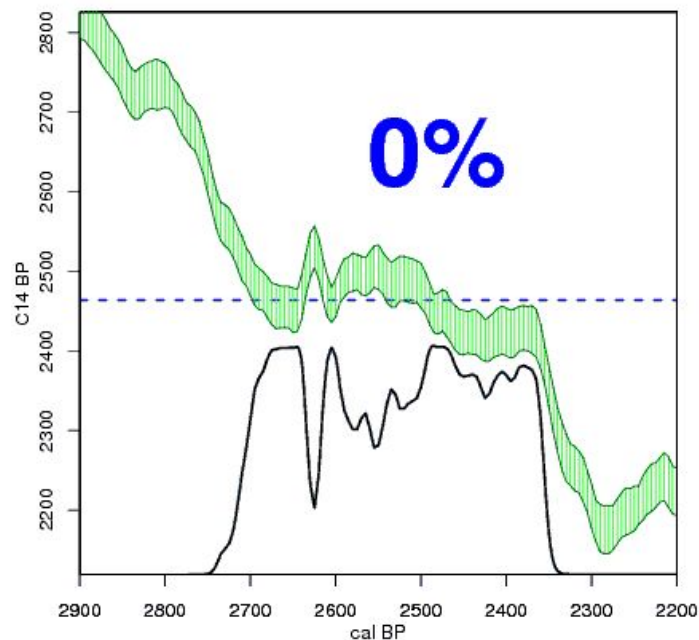
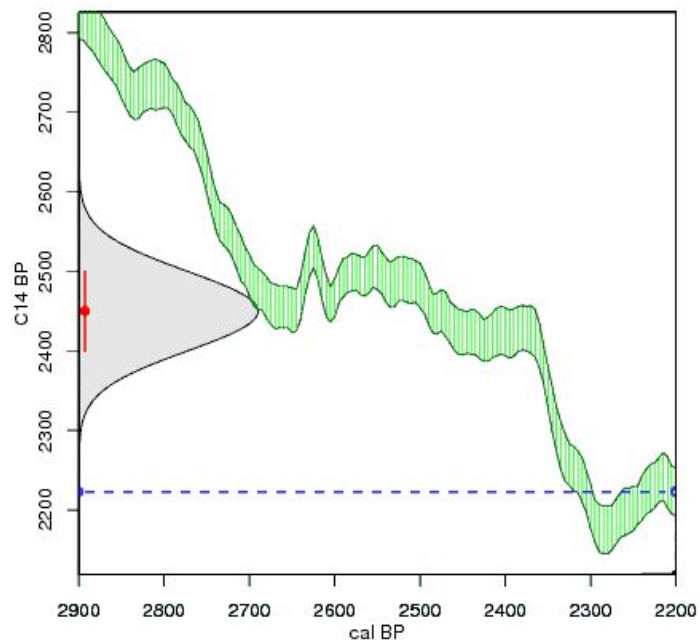
<https://maarten14c.github.io/>

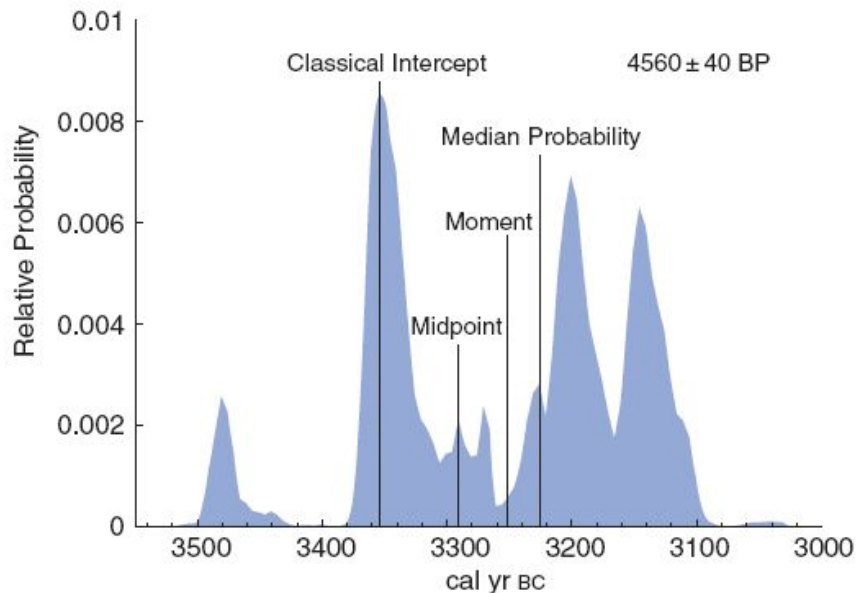




# Calibrating, why and how?

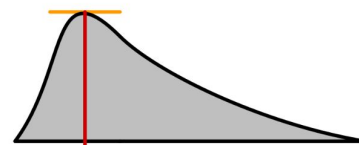
## Calibration of a single date



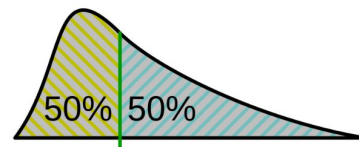


**Figure 4** Age estimators for the probability distribution of the radiocarbon age  $4560 \pm 40$  BP calculated with the IntCal04 calibration curve, including the classical intercept of the radiocarbon age with the calibration curve, the midpoint of the 95% cal age ranges, the median probability, and the moment or weighted average of the probability distribution.

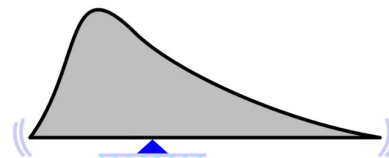
## Let's calibrate!



mode



median



mean



NEOTOMA  
PALEOECOLOGY  
DATABASE



EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

# Let's calibrate!

Open your script and the handout and let's calibrate!



NEOTOMA  
PALEOECOLOGY  
DATABASE



EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

# Coming back to our aim: depth and age



Maarten Blaauw

All models will make assumptions  
that you'll carry with you in your  
interpretations.





NEOTOMA  
PALEOECOLOGY  
DATABASE



EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES



ELSEVIER

Quaternary Science Reviews 23 (2004) 1–5

Rapid Communication

All age–depth models are wrong: but how badly?

R.J. Telford<sup>a,\*</sup>, E. Heegaard<sup>a,b</sup>, H.J.B. Birks<sup>a,b,c</sup>

<sup>a</sup> *Bjerknes Centre for Climate Research, University of Bergen, Allégaten 55, N-5007 Bergen, Norway*

<sup>b</sup> *Botanical Institut*

<sup>c</sup> *Environmental Change Research*

Received

**All age–depth models are wrong,  
but are getting better**

**Mathias Trachsel<sup>1,2</sup> and Richard J Telford<sup>1,3</sup>**

All models will make assumptions that you'll carry with you in your interpretations.

**Coming back to our aim:  
depth and age**

The Holocene

1–10

© The Author(s) 2016

Reprints and permissions:

[sagepub.co.uk/journalsPermissions.nav](http://sagepub.co.uk/journalsPermissions.nav)

DOI: 10.1177/0959683616675939

[hol.sagepub.com](http://hol.sagepub.com)





NEOTOMA  
PALEOECOLOGY  
DATABASE



EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

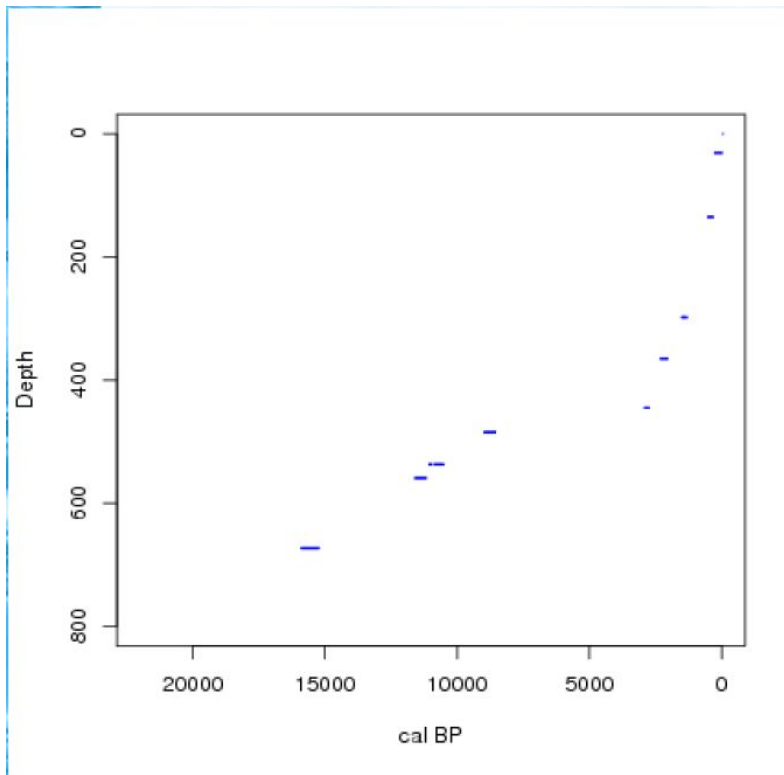
# Depth and age: classical modeling, CLAM



800cm

nine  $^{14}\text{C}$  dates

! core longer than last tie point







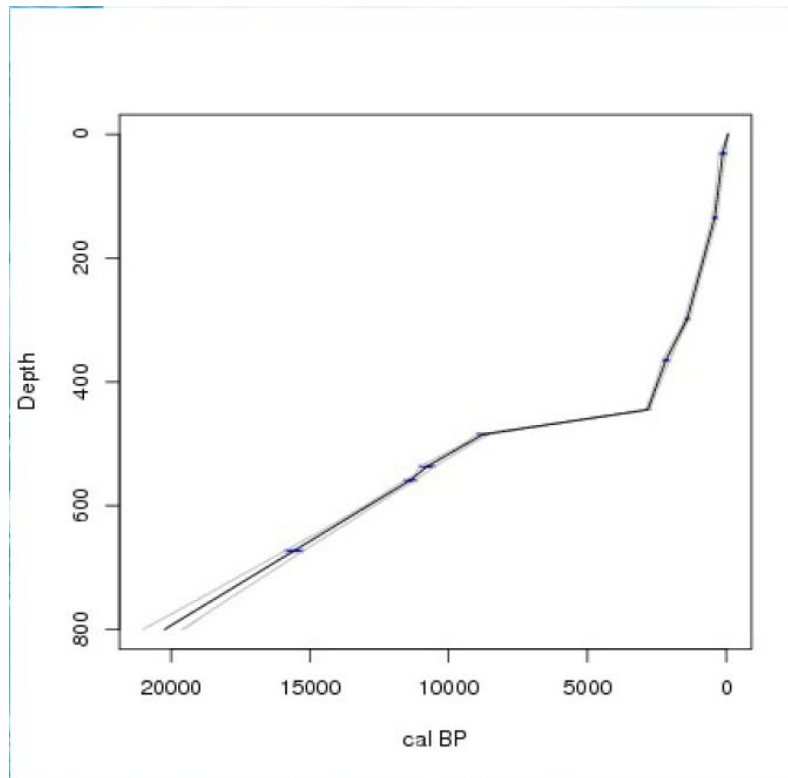
# Depth and age: classical modeling, CLAM



800cm | nine 14C dates

## Linear interpolation

- Extrapolation
- Reliable dates?





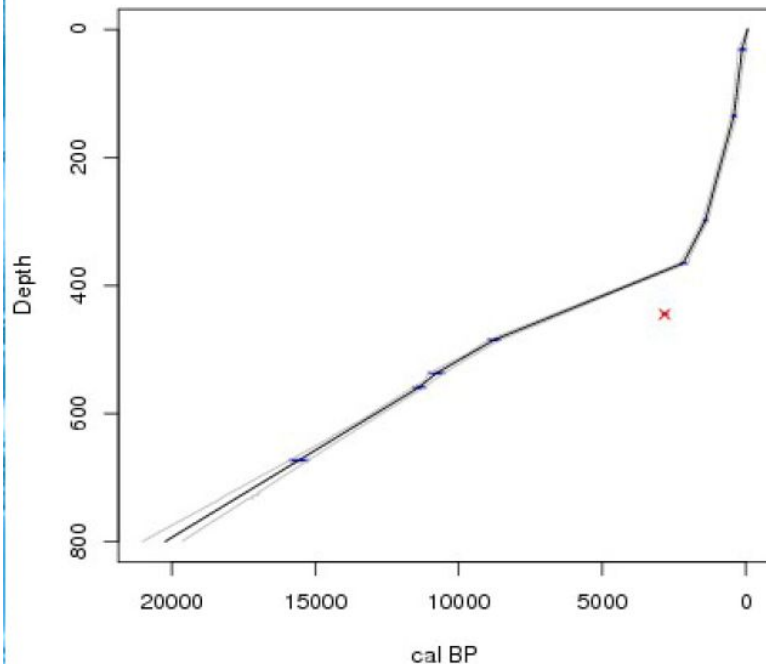
# Depth and age: classical modeling, CLAM



800cm | nine 14C dates

**Linear interpolation**

- Outlier?
- Else?





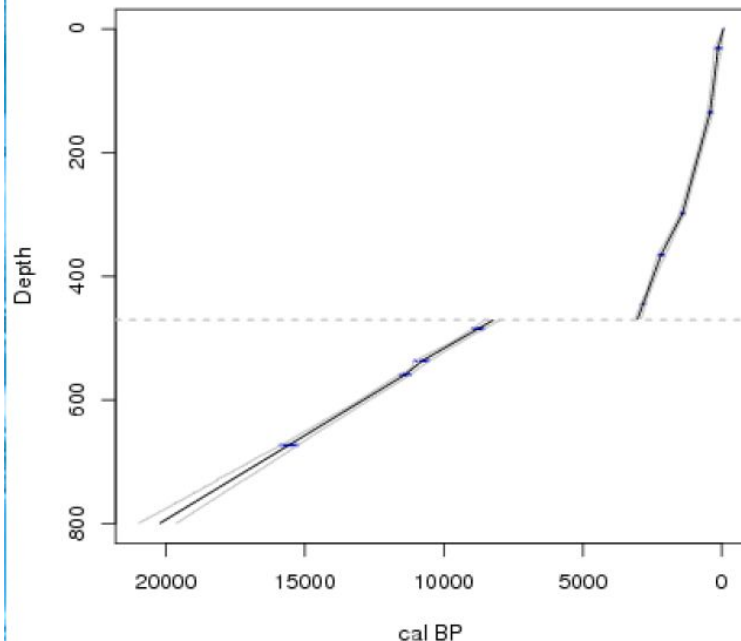
# Depth and age: classical modeling, CLAM

800cm | nine 14C dates

## Linear interpolation

- Hiatus?

Time “jump” with no  
sedimentation: erosion, cold spells,  
sediment lost/alterations.





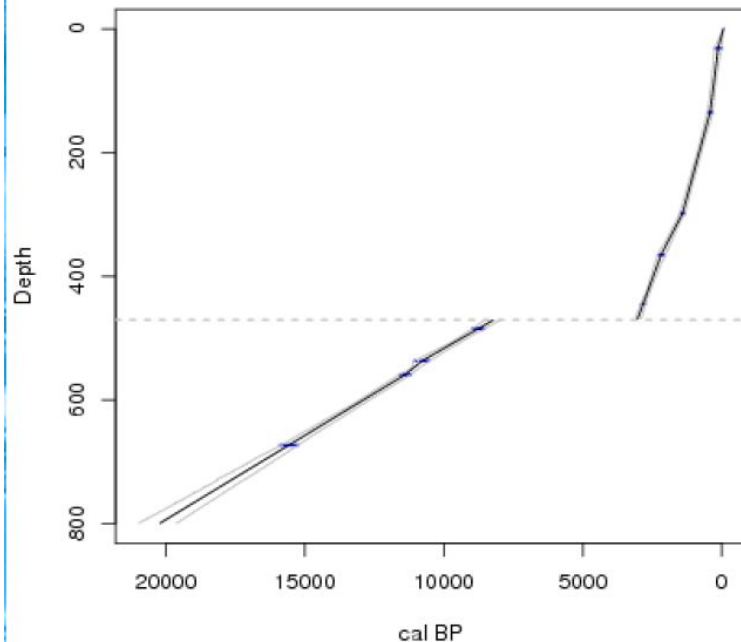
# Depth and age: classical modeling, CLAM

800cm | nine 14C dates

## Linear interpolation

- Hiatus?

Time “jump” with no  
sedimentation: erosion, cold spells,  
sediment lost/alterations.



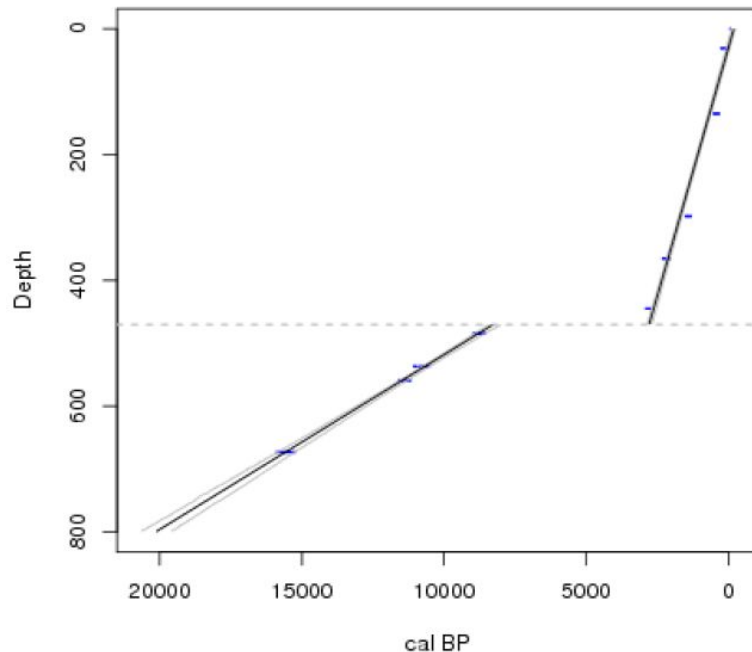


# Depth and age: classical modeling, CLAM

800cm | nine  $^{14}\text{C}$  dates

## Linear regression

Does not make optimal fitting but  
over-optimistic uncertainties.



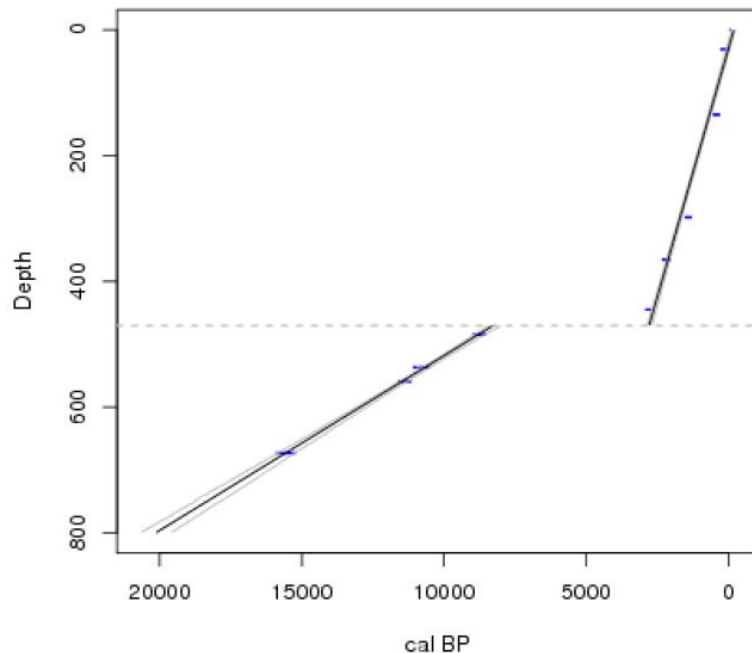


# Depth and age: classical modeling, CLAM

800cm | nine  $^{14}\text{C}$  dates

## Linear regression

Does not make optimal fitting but  
over-optimistic uncertainties.





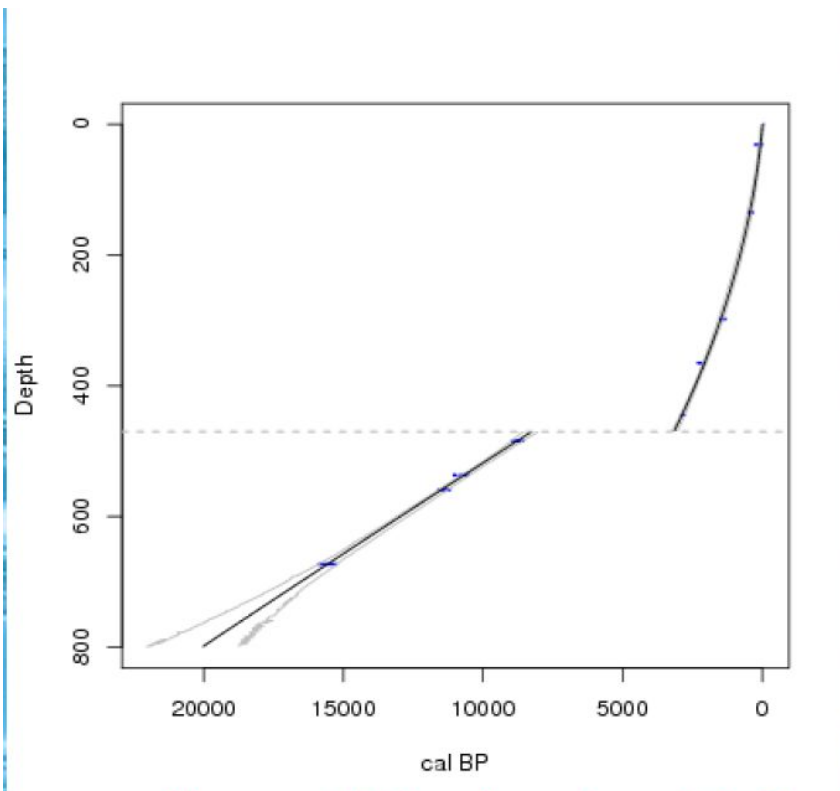


# Depth and age: classical modeling, CLAM

800cm | nine 14C dates

## Polynomial

Interesting sedimentation for the last 5ka, but extrapolation also produces funny uncertainties.

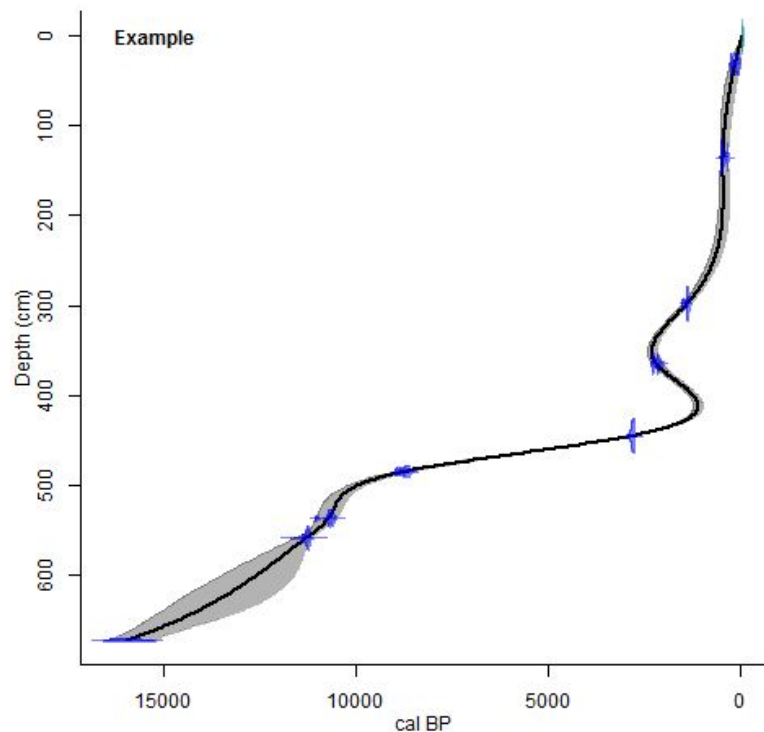




# Depth and age: classical modeling, CLAM

## Splines

May produce aberrant  
sedimentation patterns (like going  
back in time)

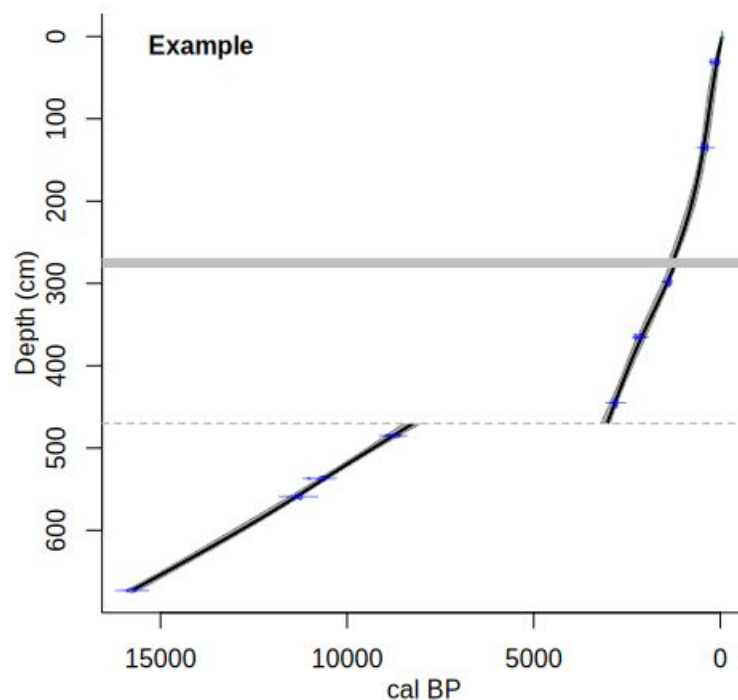
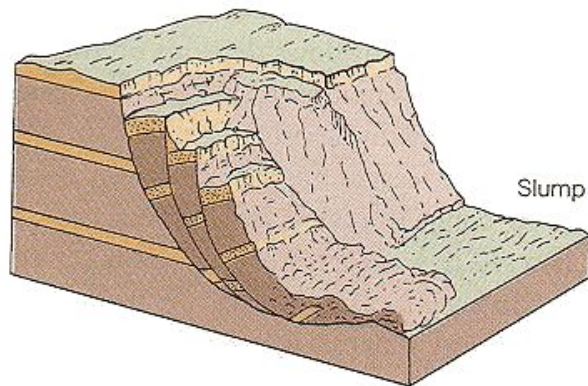




# Depth and age: classical modeling, CLAM

## Slumps

Instant events of sedimentation that can also be modeled.





NEOTOMA  
PALEOECOLOGY  
DATABASE



EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

# Depth and age: classical modeling, CLAM

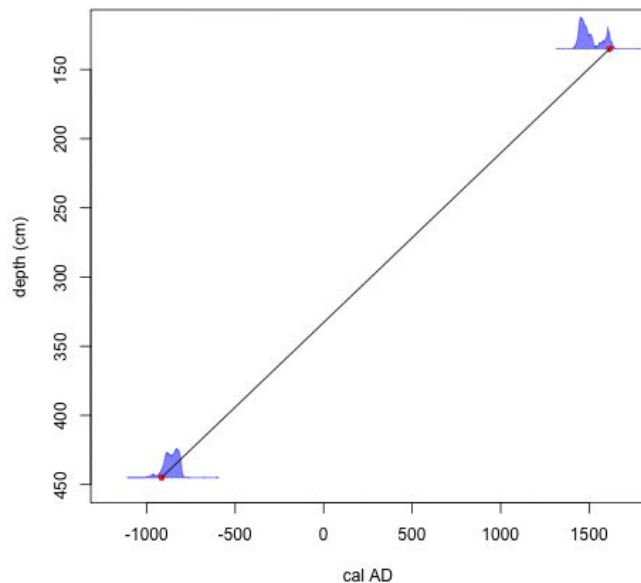
Let's try some depth-age modelling with CLAM!



# How is uncertainty treated? CLAM

## Linear interpolation vs flexible random process

The further away the more certain



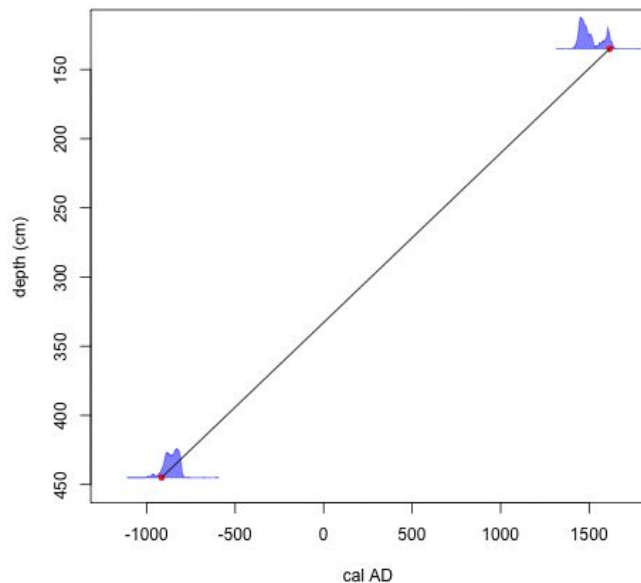


# How is uncertainty treated?

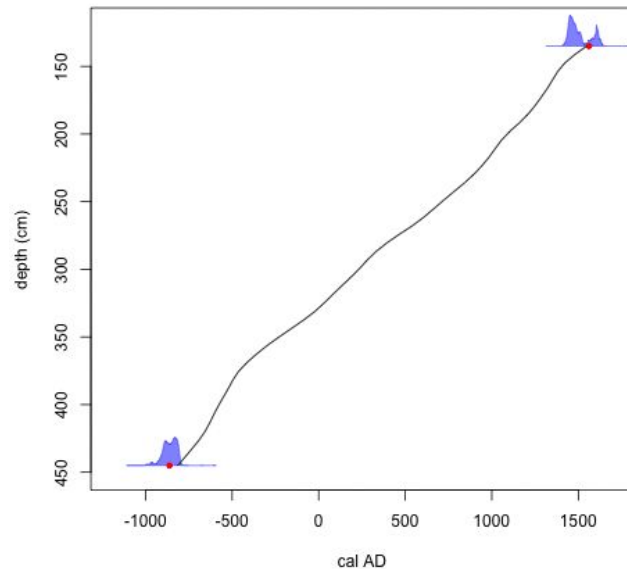
## CLAM

### Linear interpolation vs flexible random process

The further away the more certain



The further away the less certain



Monte Carlo  
iteration





NEOTOMA  
PALEOECOLOGY  
DATABASE



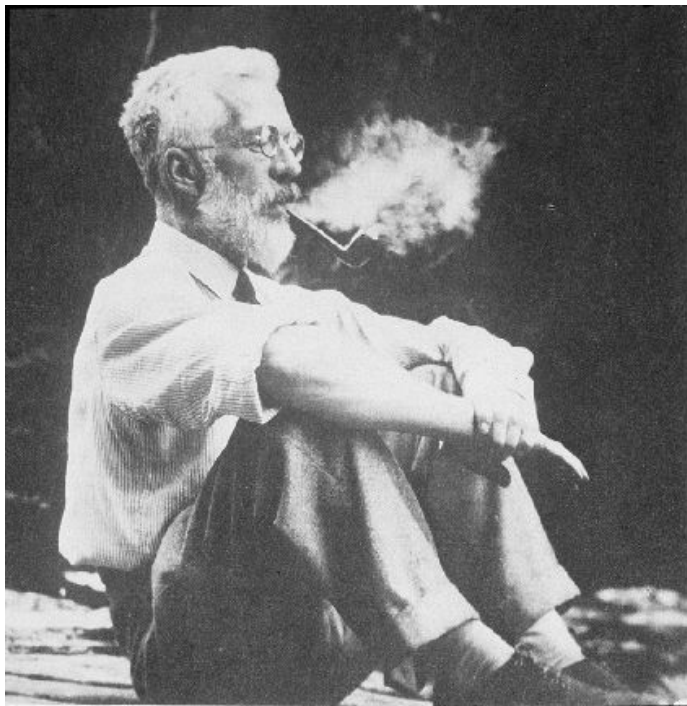
EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

# How is uncertainty treated?

## Bayesian inference

Sir Ronald Fisher (1890-1962)



Rev. Thomas Bayes (1701-1760)

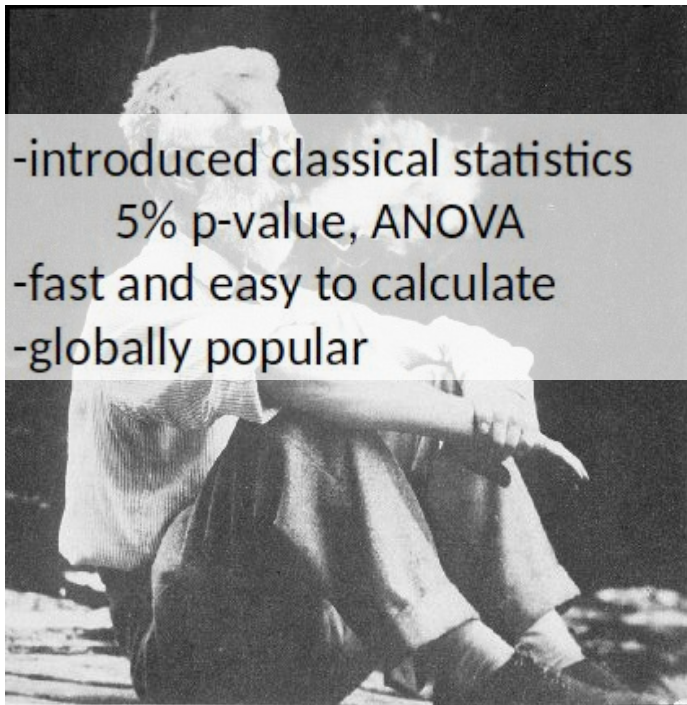




# How is uncertainty treated?

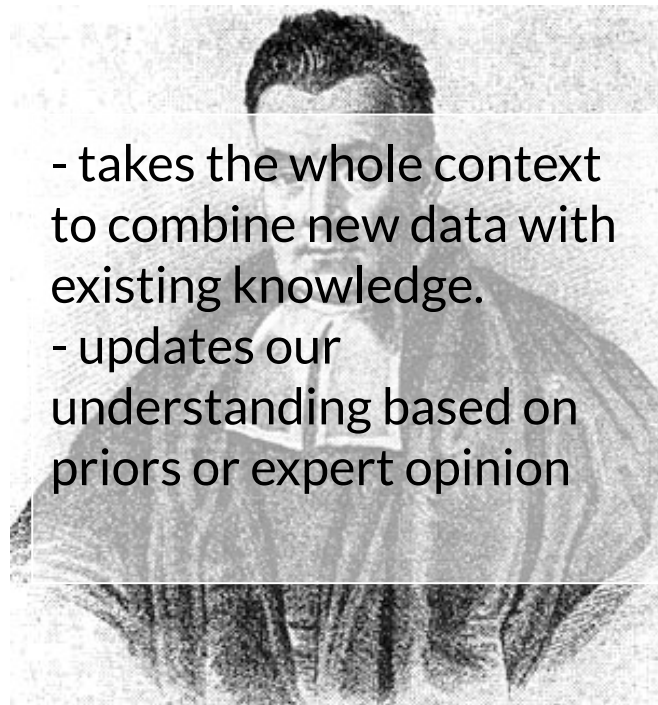
## Bayesian inference

Sir Ronald Fisher (1890-1962)



- introduced classical statistics  
5% p-value, ANOVA
- fast and easy to calculate
- globally popular

Rev. Thomas Bayes (1701-1760)



- takes the whole context  
to combine new data with  
existing knowledge.
- updates our  
understanding based on  
priors or expert opinion



# How is uncertainty treated?

## Bayesian inference

DID THE SUN JUST EXPLODE?  
(IT'S NIGHT, SO WE'RE NOT SURE.)

THIS NEUTRINO DETECTOR MEASURES  
WHETHER THE SUN HAS GONE NOVA.

THEN, IT ROLLS TWO DICE. IF THEY  
BOTH COME UP SIX, IT LIES TO US.  
OTHERWISE, IT TELLS THE TRUTH.

LET'S TRY.  
DETECTOR! HAS THE  
SUN GONE NOVA?

ROLL  
YES.

FREQUENTIST STATISTICIAN:

THE PROBABILITY OF THIS RESULT  
HAPPENING BY CHANCE IS  $\frac{1}{36} = 0.027$ .  
SINCE  $p < 0.05$ , I CONCLUDE  
THAT THE SUN HAS EXPLODED.

BAYESIAN STATISTICIAN:

BET YOU \$50  
IT HASN'T.

- Bayesian inference makes guesses based on information that is constantly updated.
- It is context-dependent.
- Can work asking about past events and future events.
- Examples:
  - Frequentist: coin, prob. of heads?
  - Bayesian: what's the probability that I have 30€ in my pocket?



# How is uncertainty treated? Bayesian inference

Update our understanding, by combining prior information with new data

$$p(A | B) \propto l(B | A) * p(A)$$
$$p(\text{prior} | \text{data}) \propto l(\text{data} | \text{prior}) * p(\text{prior})$$

How does this translate to building a depth age model?



# Bayesian age models

## How does this translate to building a depth age model?

- MCMC: Markov-chain Monte Carlo
  - Produce initial series of values that fit the data and obey the prior.
  - For next iteration, randomly change one value by a bit.
  - Accept if this enhances the fit, otherwise possibly accept.
  - Repeat millions of times (thin to reduce similarity between iterations)
- All iterations together approach the true distributions of the parameters



# Bayesian age models

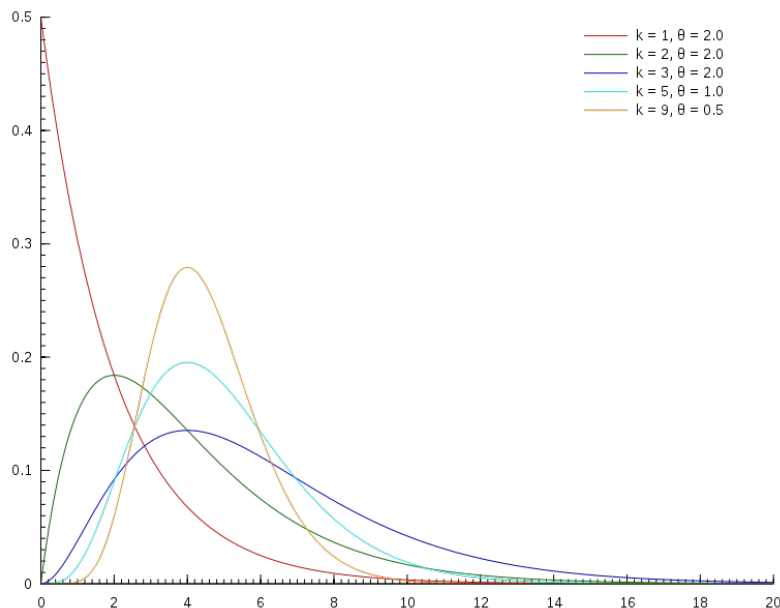
## Bacon

How does this translate to building a depth age model?

<https://vimeo.com/602543020>

<https://vimeo.com/602585449>

<https://vimeo.com/602585477>







# How is uncertainty treated? Bayesian inference

## How does this translate to building a depth age model?

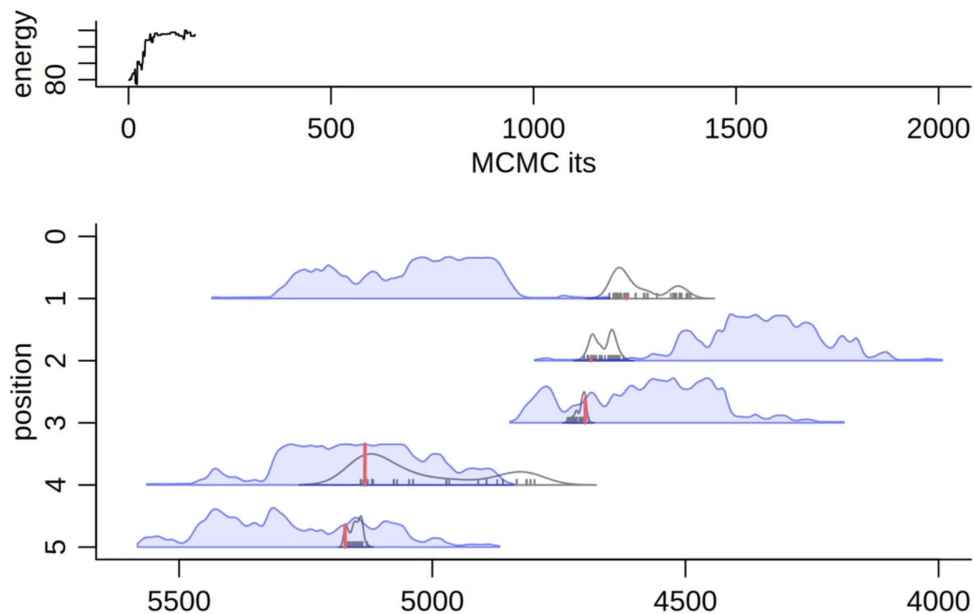
### Example: five radiocarbon dated depths from a sequence

- We model them to be in chronological order
- Simulate 5 initial 'ball-park' values (years) in chronological order
- Calculate how well they fit the calibrated radiocarbon dates
- Now randomly change one of the values by a bit
- Check that the values remain in chronological order
- Accept if the fit has enhanced, possibly accept if not
- Repeat millions of times (thin, remove burn-in)



# How is uncertainty treated? Bayesian inference

## How does this translate to building a depth age model?







# How is uncertainty treated? Bayesian inference

## How does this translate to building a depth age model?

### Piece-wise linear age-depth model

- Divide 200 cm core into 4 50cm-sections (section elbows not necessarily where dates are)
- Linear accumulation rate within each section (gamma prior distr)
- 4  $^{14}\text{C}$  dates
- For each iteration, calculate product of  $p(\text{priors}) * p(\text{dates})$

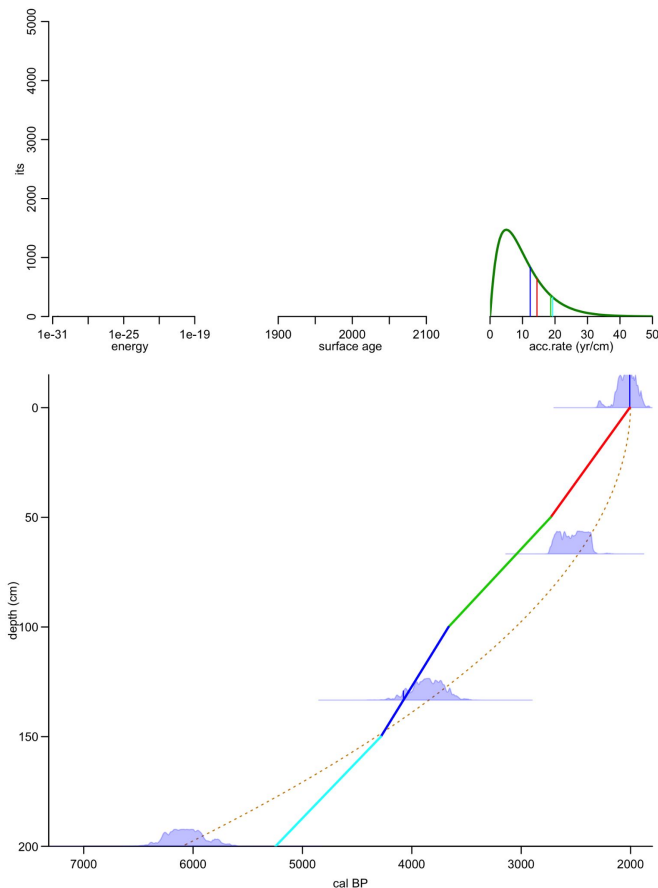


# How is uncertainty treated?

## Bayesian inference

- Ballpark iteration: simulate accs. from gamma prior
- 4 likelihoods for accs (heights of prob. distr.)
- Also simulate top date (uniform)
- This defines the entire model
- Now calculate fit of model w dates
- 4 likelihoods for dates

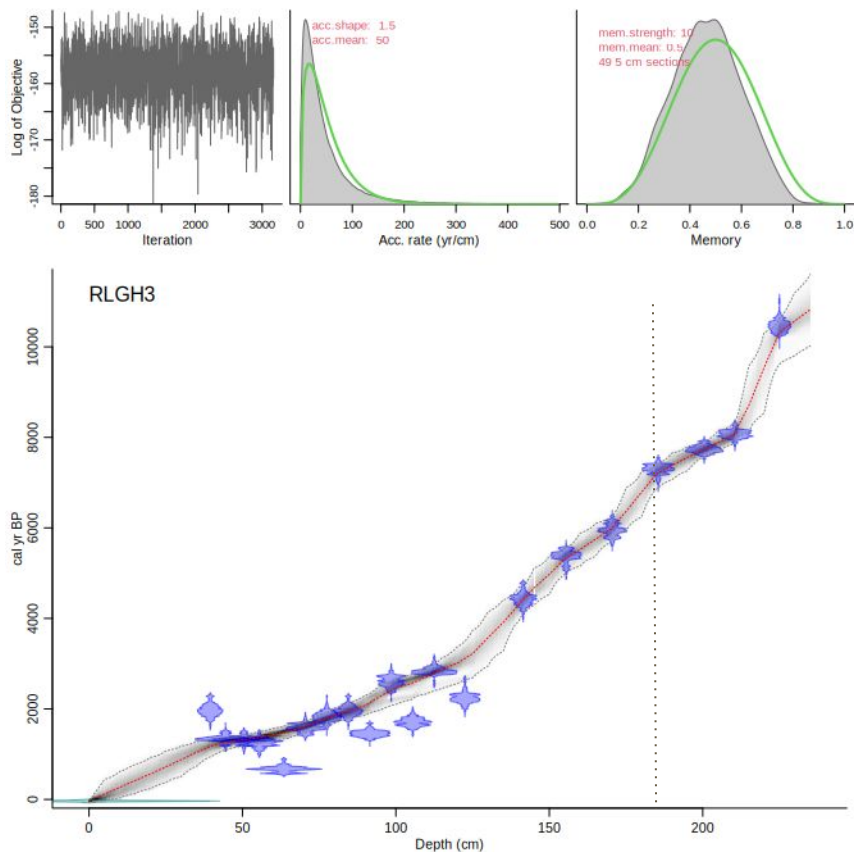
<https://vimeo.com/548372489>





# How is uncertainty treated?

## Bayesian inference

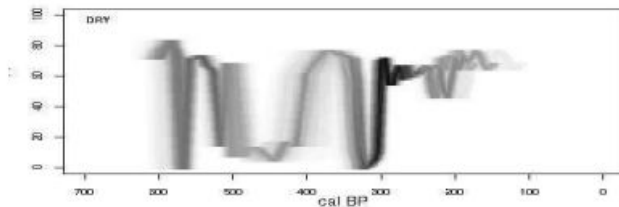
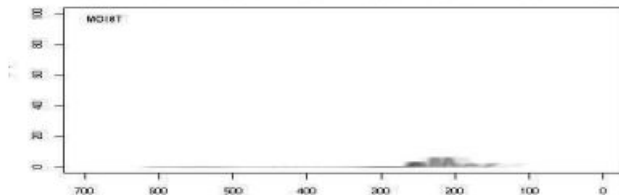
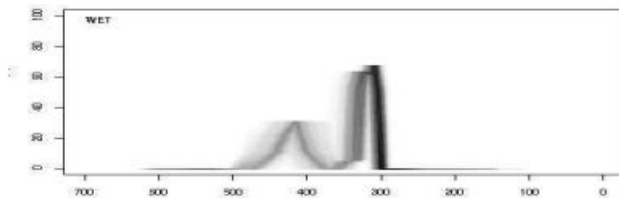
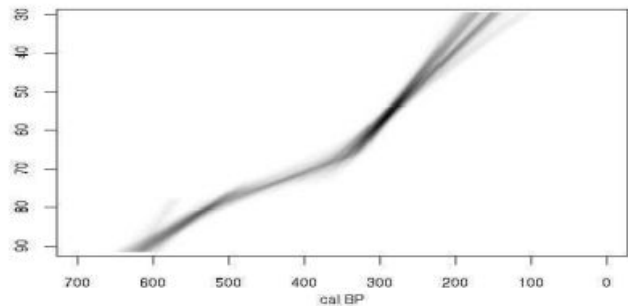
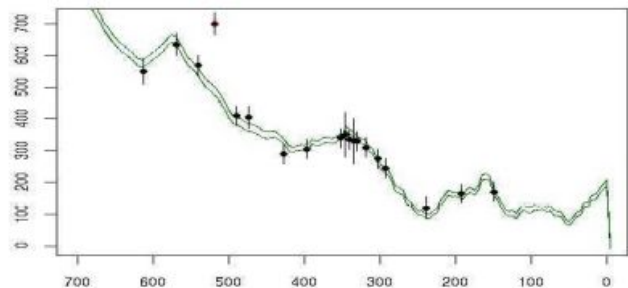


- Only accept iterations with correct order,
- Reduces error ranges,
- Removes outliers,
- Flexible modelling, can change the parameters in different sections.
- Easy to defend.



# How is uncertainty treated? Bayesian inference

- Including uncertainties into proxies
- Visual assessment of the sed. rate.





NEOTOMA  
PALEOECOLOGY  
DATABASE



EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

# How is uncertainty treated? Bayesian inference

Some practicals and examples!  
Hands on the scripts!



NEOTOMA  
PALEOECOLOGY  
DATABASE



EUROPEAN  
POLLEN  
DATABASE

PAGES  
PAST GLOBAL CHANGES

---

# Depth-age models

What are they for and how to make them?  
Some examples using the EPD

**Petr Kuneš and Graciela Gil-Romera**

[petr.kunes@natur.cuni.cz](mailto:petr.kunes@natur.cuni.cz) | [graciela.gil@ipe.csic.es](mailto:graciela.gil@ipe.csic.es)

<https://petr.kunes.net/> | <https://gilromera.com/>

---