Chapter 19

Other Topics in Accelerated Life Testing

W. Q. Meeker, L. A. Escobar, and F. G. Pascual Iowa State University, Louisiana State University, and Washington State University.

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Chapter 19 Other Topics in Accelerated Life Testing

Topics discussed in this chapter are:

An ALT with interval-censored data.

Using Bayesian methods to rescue an ALT

An ALT with two accelerating variables.

- A multifactor ALT with a single accelerating variable.
- Pitfalls of accelerated testing.

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Chapter 19

Other Topics in Accelerated Life Testing

Segment 1

An ALT with Interval-Censored Data

New-Technology IC Device ALT Data Analysis

19-3

Analysis of Interval-Censored ALT Data on a New-Technology IC Device

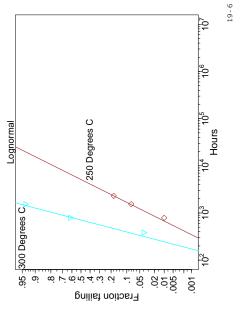
- Tests were run at 150, 175, 200, 250, and 300°C.
- Developers were interested in B01 life at 100°C.
- Failures had been found only at the two higher temperatures.
- After early failures at 250 and 300°C, there was some concern that no failures would be observed at 175°C before decision time.
- Thus the 200°C test was started later than the others.

19-4

New-Technology IC Device ALT Data

Number of Temperature Devices °C	150	175	200	250	250	250	250	300	300	300	300
Number of Devices	20	20	20	1	e	2	41	4	27	16	3
Status	Right Censored	Right Censored	Right Censored	Failed	Failed	Failed	Right Censored	Failed	Failed	Failed	Right Censored
urs Upper				788	1536	2304		384	788	1536	
Hours Lower Up	1536	1536	96	384	788	1536	2304	192	384	788	1536

Lognormal Multiple Probability Plot New-Technology Integrated Circuit Device ALT ML Fits Different Shape Parameters σ_i $\widehat{\Pr}[T(\text{Temp}_i) \le t] = \Phi_{\text{norm}} \Big[\frac{\log(t) - \widehat{\mu}_i}{\widehat{\sigma}_i} \Big], \ i = 250,300$



Individual Lognormal ML Estimation Results for the New-Technology IC Device

Lognormal Multiple Probability Plot New-Technology Integrated Circuit Device ALT ML Fits Equal Shape Parameter σ

 $\widehat{\Pr}[T(\mathsf{Temp}_i) \leq t] = \Phi_{\mathsf{norm}} \big|_{\substack{|\log(t_j) - \widehat{\mu}_i \\ \widehat{\sigma}}} \big|, \ i = 250, 300$

Lognormal

300 Degrees C

250 Degrees C

 $\omega \not \vdash \tilde{\omega} \tilde{\kappa} \dot{4} \tilde{\omega} \, \vec{\omega}$

Fraction failing

.05

9.0.00

				95% App	95% Approximate
Temp		ML	Standard	Confidenc	Confidence Intervals
Ç	Parameter Estimate	Estimate	Error	Lower	Upper
250	$t_{0.01}$	674.4	249.0	249.0 327.1	1390.4
	ο	0.87	0.26	0.26 0.48	1.57
300	$t_{0.01}$	244.6	35.9	35.9 183.5	326.1
	σ	0 .46	0.05	0.05 0.36	0.58

The confidence intervals are based on the Wald method.

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19-8

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10⁶

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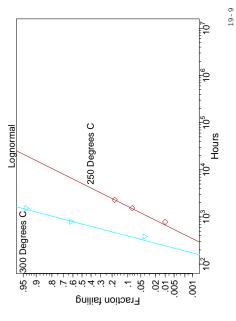
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104 Hours

Lognormal Multiple Probability Plot New-Technology Integrated Circuit Device ALT ML Fits Different Shape Parameters σ_i

$$\widehat{\Pr}[T(\mathbf{Temp}_i) \leq t] = \Phi_{\mathbf{norm}}\big[\frac{\log(t) - \widehat{\mu}_i}{\widehat{\sigma}_i}\big], \; i = 250, 300$$



Individual Lognormal ML Estimation Results for the New-Technology IC Device with Equal Shape σ

				95% Approximate	oximate
Temp		ML	Standard	Confidence Interval	e Interval
Ç	Parameter Estimate	Estimate	Error	Lower	Upper
250	$t_{0.1}$	1054.4	132.6	824.1	1349.0
300 t _{0.1}	$t_{0.1}$	213.0	33.0	157.2	288.7
	Q	0.52	0.52 0.057	0.42	0.64

The confidence intervals are based on the Wald method.

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Likelihood for Lognormal Distribution Simple Regression Model with Interval-Censored Data

The likelihood for independent observations grouped into ${\cal K}$ bins is

$$L(\beta_0,\beta_1,\sigma) = \prod_{k=1}^K [\Phi_{\mathsf{norm}}(z_{ak}) - \Phi_{\mathsf{norm}}(z_{\ell k})]^{\omega,\delta_k} [1 - \Phi_{\mathsf{norm}}(z_{\ell k})]^{\omega,(1-\delta_k)}$$

where data_k =
$$(x_k, t_{\ell k}, t_{uk}, \delta_k, \omega_k)$$
, $\mu(x_k) = \beta_0 + \beta_1 x_k$, $x_k = 11604.52/(^{\circ}C_k + 273.15)$,

$$z_{\ell k} = \frac{\log(t_{\ell k}) - \mu_k}{\sigma}, \quad z_{uk} = \frac{\log(t_{uk}) - \mu_k}{\sigma}$$

 ω_k is the number of observations in bin k, (

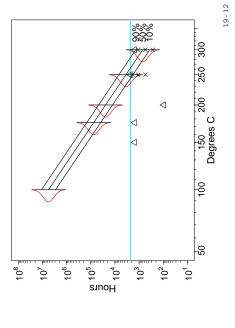
$$\delta_k = \left\{ \begin{array}{ll} 1 & \text{interval-censored observation,} \\ 0 & \text{right-censored observation,} \end{array} \right.$$

and $\Phi_{\rm norm}(z)$ is the standardized normal cdf.

The parameters are $\theta = (\beta_0, \beta_1, \sigma)$.

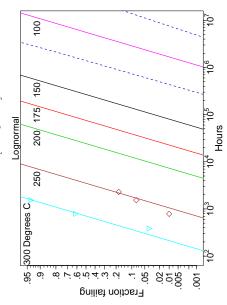


$$\log[\hat{t}_p(x)] = \hat{\mu}(x) + \Phi_{\mathsf{norm}}^{-1}(p)\hat{\sigma}, \ \hat{\mu}(x) = \hat{\beta}_0 + \hat{\beta}_1 x$$



Lognormal Probability Plot Showing the Arrhenius-Lognormal Model ML Estimation Results for the New-Technology IC Device

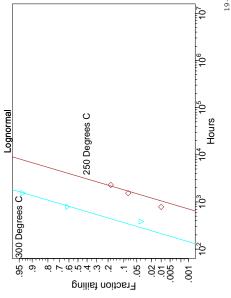
$$\widehat{\Pr}[T(\mathbf{Temp}) \leq t] = \Phi_{\mathbf{norm}}\big[\frac{\log(t) - \widehat{\mu}(x)}{\widehat{\sigma}}\big], \ \widehat{\mu}(x) = \widehat{\beta}_0 + \widehat{\beta}_1 x$$

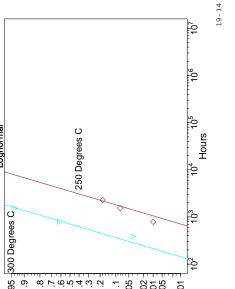


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$$\widehat{\Pr}[T(\mathbf{Temp}_i) \leq t] = \Phi_{\mathbf{norm}} \frac{[\log(i) - \widehat{\mu}_i]}{\sigma}, \ i = 250, 30$$





Arrhenius-Lognormal Model ML Estimation Results for the New-Technology IC Device

			95% Apr	95% Approximate
	ML	Standard	Confidenc	Confidence Intervals
Parameter	Estimate	Error	Lower	Upper
β_0	-10.2	1.5	1.5 -13.2	-7.2
β_1	0.83	0.07	0.68	0.97
σ	0.52	0.06	0.42	0.64

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Lognormal Model-Fitting Summary New-Technology IC Device

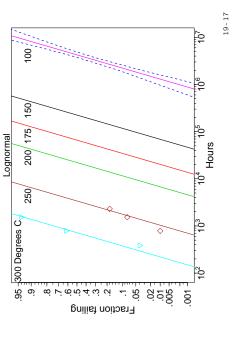
# Faraiii	4	3/6	ĸ	2
AIC	180.0	182.7	182.7	370.8
-77(0)	172.0	176.7	176.7	366.8
INIONEI	SepDists	EqualSig	RegrModel	Pooled

Likelihood-Ratio Tests

<i>p</i> -value	0.028	1.0	< 0.001	
dof	1	m	П	
LR Statistic dof	4.72	0.0	190.1	
Comparison	SepDists vs EqualSig	EqualSig vs RegrModel	RegrModel vs Pooled	

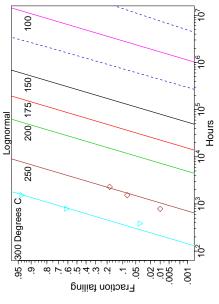
19-16

Lognormal Probability Plot Showing the Arrhenius-Lognormal Model ML Estimation Results for the New-Technology IC Device with Given $E_a=0.80\,$ $\widehat{\Pr}[T(\mathbf{Temp}) \leq t] = \Phi_{\mathbf{norm}} \left[\frac{\log(t) - \widehat{\mu}(x)}{\widehat{\sigma}} \right], \ \widehat{\mu}(x) = \widehat{\beta}_0 + 0.80x \right]$





$$\widehat{\Pr}[T(\mathbf{Temp}) \leq t] = \Phi_{\mathbf{norm}}\big[\frac{\log(t) - \widehat{\mu}(x)}{\widehat{\sigma}}\big], \ \widehat{\mu}(x) = \widehat{\beta}_0 + \widehat{\beta}_1 x$$



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Other Topics in Accelerated Life Testing

Segment 2

Bayesian Analysis for the New-Technology IC Device ALT

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New-Technology IC Device ALT Problem and Rescue

- Failures at 300°C were caused by a different failure mode and had to be dropped (or right-censored).
- With failures at only 250°C, there is no information in the data about β_1 , the effective activation energy.
- Previous experience with the same failure mode suggested a prior distribution for $\beta_1.$
- Bayesian estimation could be used to estimate the failuretime distribution at 100°C.

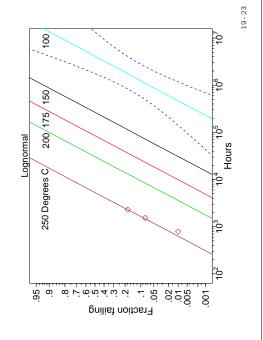
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New-Technology IC Device Prior Distributions

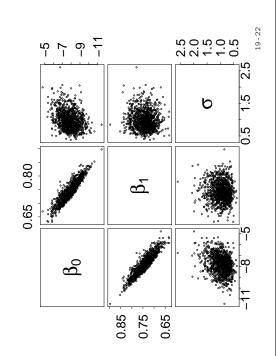
Prior Distributions	<pre><lnorm>(100, 10000) <lnorm>(0.65, 0.85) <lnorm>(0.05, 5.0)</lnorm></lnorm></lnorm></pre>
Parameter	$t_{0.1}(250)$ β_1 σ

19-21

Lognormal Probability Plot Showing the Arrhenius-Lognormal Model Bayesian Estimation Results for the New-Technology IC Device



Pairs Plot of the Joint Posterior Distribution Draws for the New-Technology IC Device



Chapter 19

Other Topics in Accelerated Life Testing

Segment 3

An ALT with Two Accelerating Variables

Increasing Temperature and Current to Estimate an LED Failure-Time Distribution

Temperature/Current ALT for LEDs

Scatter Plot of the LED ALT Data Showing Hours to Failure Versus Temperature with Current Indicated by

Different Symbols

- ALT light emitting diode (LED) with two accelerating variables.
- Purpose of the test was to evaluate an LED for suitability for use in an LED flashlight.
- Actual response was percent drop in light output.
- An LED fails when light output decreases to 60% of the initial light output.
- . There were no failures during the accelerated test
- Degradation data mapped into pseudo failure times by fitting a straight line to the degradation path and extrapolating to the failure level.
- Non-rectangular design due to ambient versus junction temperature.

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19-26

130

120

110

90 100 Degrees C

8

70

9

30 mA 40 mA

O+

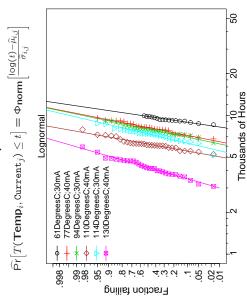
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Thousands of Hours

+ ## # ### +###

ω

Lognormal Multiple Probability Plot LED ALT Data Different Shape Parameters



. 28 19-20- $\left[\frac{\log(t) - \widehat{\mu}_{i,j}}{\widehat{\sigma}}\right]$ Plot Lognormal Multiple Probability P LED ALT Data ML Estimates Equal Shape Parameter 20 $\widehat{\mathsf{Pr}}[T(\mathsf{Temp}_i, \mathtt{Current}_j) \leq t] = \Phi_{\mathsf{norm}}$ 5 10 Thousands of Hours ognormal-61DegreesC;30mA 77DegreesC;40mA 94DegreesC;30mA 110DegreesC;30mA 114DegreesC;30mA 130DegreesC;40mA S 866 98 0; ∞; ∠; 0; 4 to 0 202 05 Fraction failing

LED ALT Lognormal/Arrhenius/Inverse-Power Relationship Models

19-27

Model 1:
$$\mu(x)=eta_0+eta_1x_1+eta_2x_2$$

 $= \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_1 x_2$

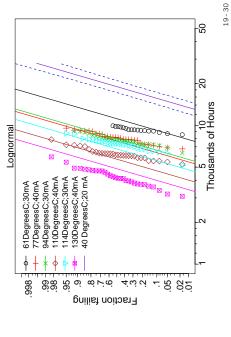
Model 2: $\mu(x)$

where

- $x_1 = 11604.52/(\text{Temp} \,^{\circ}\text{C} + 273.15),$
- $x_2 = \log(\text{Current})$
- ullet $eta_2=E_a$ and
- σ is constant.

Lognormal Multiple Probability Plot of the LED ALT Data Arrhenius-Inverse-Power Relationship Lognormal Model (with no Interaction)

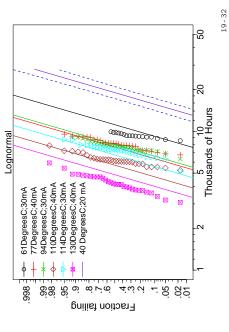
$$\widehat{\Pr}[T(\texttt{Temp},\texttt{Current}) \leq t] = \Phi_{\texttt{norm}}\Big[\frac{\log(t) - (\widehat{\beta}_0 + \widehat{\beta}_1 x_1 + \widehat{\beta}_2 x_2)}{\widehat{\sigma}}\Big]$$



-20 $\widehat{\Pr}\left[T(\mathbf{Temp}_i, \mathtt{Current}_j) \leq t\right] = \Phi_{\mathbf{norm}}\Big|\frac{\log(t) - \widehat{\mu}_{i,j}}{\widehat{\sigma}}$ Lognormal Multiple Probability Plot LED ALT Data ML Estimates Equal Shape Parameter 20 5 10 Thousands of Hours Lognormal 61 DegreesC;30mA 77 DegreesC;40mA 94 DegreesC;30mA 110 DegreesC;30mA 114 DegreesC;30mA 130 DegreesC;40mA -866 0; ∞, ∠, 0; 98 . 65 20 20 20 Fraction failing

Lognormal Multiple Probability Plot of the LED ALT Data Arrhenius-Inverse-Power Relationship Lognormal Model (with no Interaction)

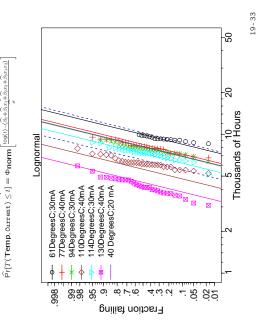




ALT Data Arrhenius-Inverse-Power Relationship Lognormal Lognormal Multiple Probability Plot of the LED

19-31

Model (with Interaction)



LED Lognormal Regression Model-Fitting Summary Using the Bad Data

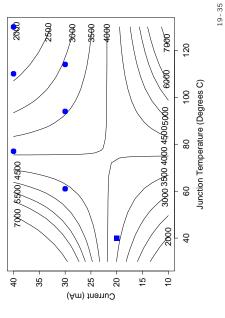
Model	$-2\mathcal{L}(\theta)$	AIC	# Param
SepDists	389.9	413.9	12
EqualSig	402.0	416.0	7
Additive RegrModel	485.9	493.9	4
Interaction RegrModel	437.7	447.7	2
Pooled	737.7	741.7	2

Likelihood-Ratio Tests

34

19-

LED ALT 0.10 Quantile Estimates (with Interaction) $\widehat{\Pr}[T(\mathbf{Temp}, \mathtt{Current}) \leq t] = \Phi_{\mathbf{norm}}\Big[\frac{\log(t) - (\widehat{\beta}_0 + \widehat{\beta}_1 x_1 + \widehat{\beta}_2 x_2)}{\widehat{\sigma}}\Big]$



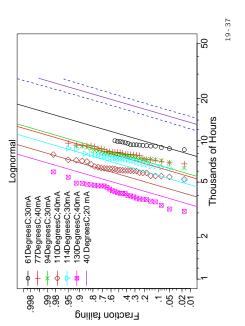
Other Topics in Accelerated Life Testing Chapter 19

Segment

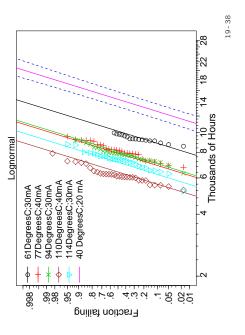
Fixing the LED ALT Analysis

Lognormal Multiple Probability Plot of the LED ALT Data Arrhenius-Inverse-Power Relationship Lognormal Model (with no Interaction)

 $\widetilde{\Pr}[T(\mathbf{Temp},\mathtt{Current}) \leq t] = \Phi_{\mathbf{norm}}\Big[\frac{\log(t) - (\widehat{\beta}_0 + \widehat{\beta}_1 x_1 + \widehat{\beta}_2 x_2)}{\widehat{\sigma}}\Big]$



Lognormal Multiple Probability Plot of the Good LED ALT Data Arrhenius-Inverse-Power Relationship Lognormal Model (with no Interaction) $\widehat{\Pr}[T(\mathsf{Temp}, \texttt{Current}) \le t] = \Phi_{\mathsf{norm}} \Big[\underbrace{|og(t) - (\widehat{s}_0 + \widehat{b}_{str})|}_{\widehat{p}_s(t)} \Big]$



LED Lognormal Regression Model-Fitting Summary

LED ALT 0.10 Quantile Estimates Based on Good

Data

 $\widehat{\Pr}[T(\mathbf{Temp},\mathtt{Current}) \leq t] = \Phi_{\mathbf{norm}}\Big[\frac{\log(t) - (\widehat{\beta_0} + \widehat{\beta_1}x_1 + \widehat{\beta_2}x_2)}{\widehat{\sigma}}\Big]$

ata	# Param	10	9	4	^
ood Da	AIC	353.5	350.1	355.0	5143
Using the Good Data	$-2\mathcal{L}(\theta)$	333.5	338.1	347.0	510.3
Usin	Model	SepDists	EqualSig	RegrModel	Pooled

Likelihood-Ratio Tests

500			
Comparison	LR statistic	dof	p-value
SepDists vs EqualSig	4.62	4	0.33
EqualSig vs RegrModel	8.94	7	0.011
RegrModel vs Pooled	163.2	7	< 0.001

19-40

Junction Temperature (Degrees C)

19-39

2900

8000

10 - 9000

15

(Am) fromuD

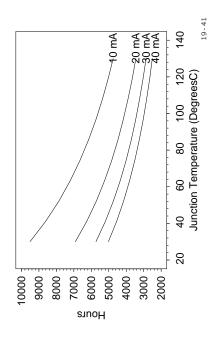
3500

4990

3000

LED ALT 0.10 Quantile Estimates Versus Temperature at Different Current Levels Based on Good Data

 $\widehat{\Pr}[T(\mathbf{Temp}, \mathtt{Current}) \leq t] = \Phi_{\mathbf{norm}} \begin{bmatrix} \log(t) - (\beta_0 + \widehat{\beta}_1 x_1 + \widehat{\beta}_2 x_2) \\ \widehat{\sigma} \end{bmatrix}$



Chapter 19 Other Topics in Accelerated Life Testing

Segment 5

A Multi-Factor ALT with One Accelerating Variable

the Fatigue Life of a New Spring An Experiment to Estimate

New Spring Accelerated Test Data Pairs Plot

- Large factorial accelerated test experiment. Three factors, 12 combinations of levels, and 9 reps at each combination.
- springs tested until failure or to a maximum of 500,000 thousand cycles All 108
- Goals:
- Compare New and Old processing methods.
- at least Determine if B10 life (the 0.10 quantile) is 500,000 thousand cycles at 30 mils stroke.
- Data from Meeker, Escobar, and Zayac (2003).

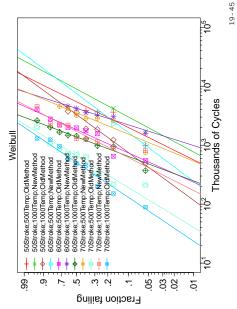
19-43

5000 4000 3000 2000 1000 1000 900 800 700 600 500 19-44 Method 4. Temperature degrees F 700 R-400 00000 0 65 Stroke 8 -22 G −4 ∞mo Thousands of cycles 1.8-1.6-1.2 70 --09 22 20

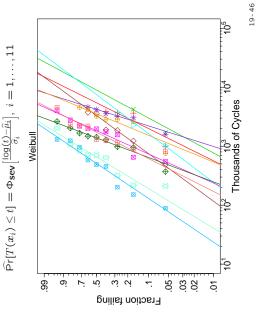
Weibull Multiple Probability Plot New Spring Data Individual Weibull ML Fit at Each Combination Different Shape Parameters

$$\widehat{\Pr}[T(x_i) \leq t] = \Phi_{ extsf{sev}}[rac{|\widehat{\log}(t) - \widehat{\mu}_i|}{\sigma_i}], \ i = 1, \dots, 11$$

$$\underbrace{\text{Weibull}}_{ extsf{99 } + extsf{50Strake500Temp:OldMethod}}_{ extsf{99 } + extsf{50Strake500Temp:OldMethod}}_{ extsf{90 } + extsf{50Strake500Temp:OldMethod}}$$

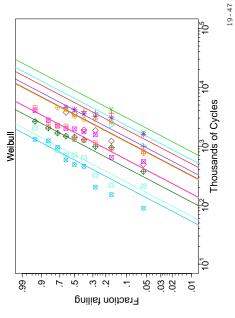


Weibull Multiple Probability Plot New Spring Data Individual Weibull ML Fit at Each Combination Different Shape Parameters



Weibull Multiple Probability Plot New Spring Data Individual Weibull ML Fit at Each Combination Equal Shape Parameter

Equal Shape Parameter
$$\widehat{\Pr}[T(x_i) \leq t] = \Phi_{\mathsf{SeV}}\big[\frac{\log(t) - \widehat{\mu}_i}{\sigma}\big], \ i = 1, \dots, 11$$



New Spring Failure-Time Regression Model

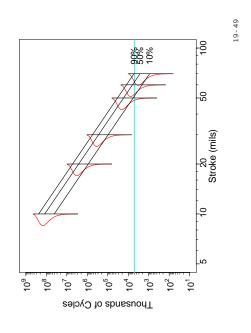
$$x = (Stroke, Temp, Method)$$

$$\mathrm{Log}(\mathrm{Life}) = \beta_0 + \beta_1 \log(\mathrm{Stroke}) + \beta_2 \mathrm{Temp} + \beta_3 \mathrm{Method}$$

where

$$\mathsf{Method} = \left\{ \begin{array}{ll} 1 & \mathsf{Old} \\ 0 & \mathsf{New} \end{array} \right.$$

New Spring Conditional Model Plot Conditional on Temperature 600°F and the New Method

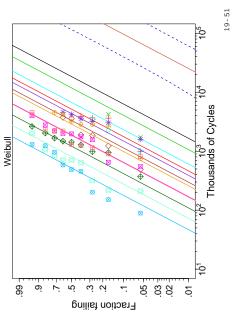


Weibull Multiple Probability Plot New Spring Data Weibull Regression Model Equal Shape Parameter

$$\widehat{\Pr}[T(x_i) \leq t] = \Phi_{\text{SeV}} \Big[\frac{|\operatorname{og}(t)_- \widehat{\mu}(x_i)|}{\widehat{\sigma}} \Big], \ \widehat{\mu}(x) = \widehat{\beta}_0 + \widehat{\beta}' x$$

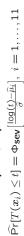
Weibull Multiple Probability Plot New Spring Data Weibull Regression Model Equal Shape Parameter

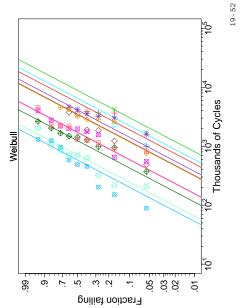
$$\widehat{\Pr}[T(x_i) \leq t] = \Phi_{\mathbf{Sev}}\big[\frac{\log(t) - \widehat{\mu}(x_i)}{\widehat{\sigma}}\big], \ \widehat{\mu}(x) = \widehat{\beta}_0 + \widehat{\beta}'x$$



Weibull Multiple Probability Plot New Spring Data Individual Weibull ML Fit at Each Combination Equal Shape Parameter

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New Spring Data Weibull Model-Fitting Summary

S	# Param	22	12/13	2	7
	AIC	1286	1276	1266	1366
	$-2\mathcal{L}(\theta)$	1242	1252	1256	1362
	Model	SepDists	EqualSig	RegrModel	Pooled

Likelihood-Ratio Tests

Comparison	LR Statistic dof	dof	<i>p</i> -value
SepDists vs EqualSig	10.13	10	0.43
EqualSig vs RegrModel	4.19	00	0.84
RegrModel vs Pooled	106.0	n	< 0.001

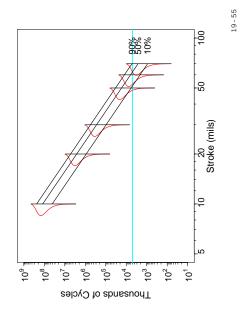
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Other Topics in Accelerated Life Testing

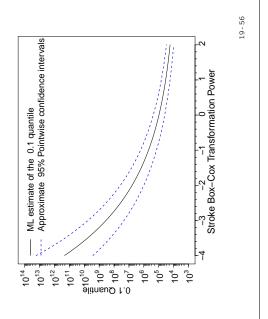
Segment 6

Model Sensitivity Analysis

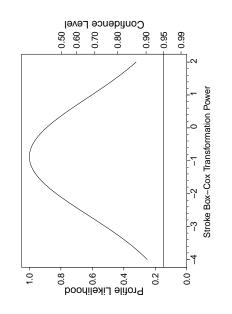
New Spring Conditional Model Plot Conditional on Temperature 600°F and the New Method



New Spring Box-Cox Sensitivity Analysis B10 at 30 mils and 600 Degrees F



New Spring Box-Cox Sensitivity Analysis Profile



Chapter 19

Other Topics in Accelerated Life Testing

Segment 7

Pitfalls of Accelerated Testing

Accelerated Life T

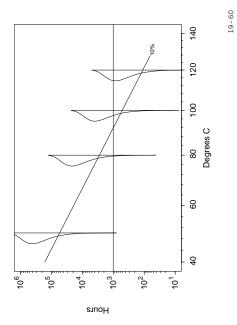
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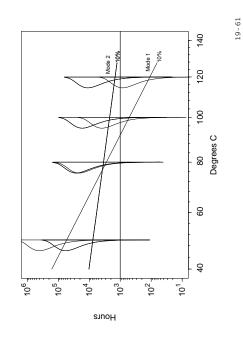
Pitfalls of Accelerated Testing

- Pitfalls arise in
- ▶ Accelerated test planning,
- ► Accelerated test execution, and
- ► Accelerated test interpretation.
- Several papers have been written describing acceleratedtest pitfalls. These include Meeker and Escobar (1998) and Meeker, Sarakakis, and Gerokostopoulos (2013).

Temperature-Accelerated Life Test for an IC Device



Unmasked Failure Mode with Lower Activation Energy for an IC Device

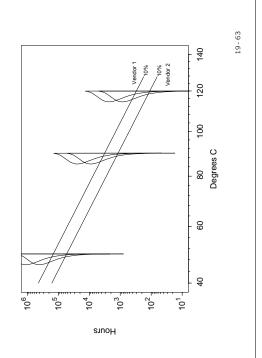


Pitfall 4: Masked Failure Mode

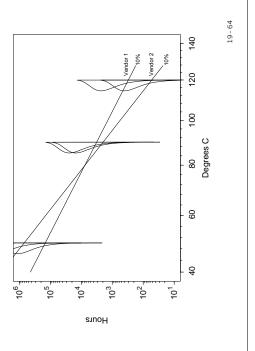
- Accelerated test may focus on one known failure mode, masking another!
- Masked failure modes may be the first one to show up in the field.
- Masked failure modes could dominate in the field.
- Suggestions:
- ▶ Know (anticipate) different failure modes.
- ▶ Limit acceleration and test at levels of accelerating variables such that each failure mode will be observed at two or more levels of the accelerating variable.
- ▶ Identify failure modes of all failures.
- ► Analyze failure modes separately.

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Comparison of Two Products Simple Comparison



Comparison of Two Products Questionable Comparison



Pitfall 5: Faulty Comparison

- It is sometimes claimed that Accelerated Testing is not useful for predicting reliability, but is useful for comparing alternatives.
- Comparisons can, however, also be misleading.
- Beware of comparing products that have different kinds of failures.
- Suggestions:
- Know (anticipate) different failure modes.
- ▶ Identify failure modes of all failures.
- ▶ Analyze failure modes separately.
- ► Understand the physical reason for any differences.

Pitfall 6: Acceleration Factors Can Cause Deceleration!

- Increased temperature in an **accelerated** circuit-pack reliability audit resulted in fewer failures than in the field because of lower humidity in the **accelerated** test.
- Higher than usual use rate of a mechanical device in an accelerated test inhibited a corrosion mechanism that eventually caused serious field problems.
- Automobile air conditioners failed due to a material drying
 out degradation, lack of use in winter (not seen in continuous accelerated testing).
- Inkjet pens fail from infrequent use.
- Suggestion: Understand failure mechanisms and how they are affected by experimental variables.

Pitfall 7: Untested Design/Production Changes

- Lead-acid battery cell designed for 40 years of service.
- New epoxy seal to inhibit creep of electrolyte up the positive post.
- Accelerated life test described in published article demonstrated 40 year life under normal operating conditions.
- 200,000 units in service after 2 years of manufacturing.
- First failure after 2 years of service; third and fourth failures followed shortly thereafter.
- Improper epoxy cure combined with charge/discharge cycles hastened failure.
- Most of the population had to be replaced with a re-designed cell.

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