Wheastone Bridge Optimaization Using Factorial Experiments

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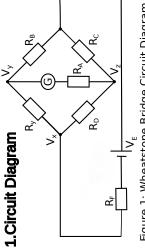


Figure 1: Wheatstone Bridge Circuit Diagram.

2.Iterative Design

varying each control factor by, initially, 10%. The result The iterations were performed by running experiments of these experiments was the ΔY value indicated on the right. Using this result it was then possible to regress the input factors into a model using RS/1 and use this model to find optimum values to minimise ΔY .

On each iteration the optimisation would find factors imited at the edges of the range chosen in the experiments. The range chosen for the next experiment chosen based on intuition - a percentage of the value was then based on this observation. These ranges were the factor was found to be limited at.

The graph on the right shows the AY acheived on each teration. This had to be plotted on a logarithmic scale for the higher iterations to be visible. Figure 2: Description of the design at different $^{10^{ ext{-4}}}$ terations and the improvements in ΔY .

3.Results

Iteration

Problem: When galvanometer current is between ± 0.2 mA, the indicated value is zero. The resistance change that causes currents ΔΥ2 two ΔΥ values seen here. and used in optimisation Above graph plots the shaded area Aim: to detect 2Ω resistors as accurately as possible using a is the maximum of the The AY value reported Original AY over 100 times the height of this graph n this range to flow therefore cannot be detected -0.2 0.0 0.2 Galvanometer current(mA) ΔY_1 1.995 acheived in iteration 16 The final **ΔY** value Wheatstone Bridge circuit was 0.0002 Ω 9 and 10 14 L3 15 16 (Ω)_y(Ω) 2.005 1.990 10^{1}_{1}

Calculations

each circuit to ensure it would balance at 2Ω. This was acheived in the Python code using the following equations, by It was necessary to calculate $R_{\scriptscriptstyle
m C}$ for asserting R_y at 2Ω .

$$R_C = \frac{\overline{R_B} \times R_D}{R_y} \quad R_C = \frac{R_B \times R_D}{2}$$

$$R_y = 2\Omega$$

in the Python code. Thevenin's theorem was applied at node V_{x} whole was added as a response to solve for voltages V_v and V_z. Yield was also added as resistor and the circuit Power dissipation of

 SS_{obs} SS_{reg}

 R^2

Observed SSobs of real responses

Regressed SS_{reg} of model and predicted responses:

As an arbitrary number of experiments could be run a cubic model was built using a full factorial

experiment to increase accuracy.

rule of thumb; below which model accuracy was

badly affected.

1. Control factor ranges

Methods

Perform experiment Test specifications

Optimise variables

Check model fit

6. Confirmation run

-10-50% variation on factors was a safe

improved by applying a y-transform, variance

weights or bisquare weights.

validate the optimised

A final experiment is

always required to

R² is composed of two square sums of observed

Fit of the model can be estimated by the reported R^2 (fit of the model to data) value. This can be additional response, estimating standard deviations able to detect 2Ω . οę number the

Statistical Analysis

However, in order to optimise the yield $\mathbb{S}^{2.00}$ of the circuit easily a Monte Carlo simulator was written in Python. Ideally, this would be run on the model because Using the distrib command it is to estimate the effect of on the model. it involves many experiments. tolerances possible resistor

dissipation and ΔY . The bottom graph is $^{1.95}$ plotted in the same manner to the top, 1.90 2 by using the Monte Carlo script to \$2.00 optimisation 2. Optimisation of yield regression model approach as in section output worst case 6ơ values for power The region of designs unable to detect the top graph - showing the design after a 20 resistor is indicated by shading in the same through but for the final design. was possible

6.53

19.2

115 N/A

00 00 00

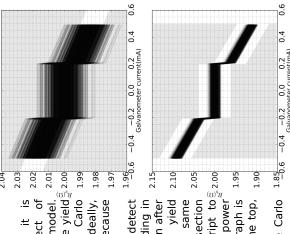
끆 1

Ŧ 1

+36.0=76.2Ω

N/A(-20)

For confirmation, a final Monte Carlo 1.856 -0.4 -0.2 was also run.



Yield (σ)

power (mW) Dissipated Max.(6σ)

Component rating (mW)

Component Tolerances

> II Chosen nponents

Monte Carlo on two optimised designs. Figure 3: Illustration of the results of

Setting a yield of 60 as a design constraint allowed the design to become viable and the final Monte Carlo test produced a worst case $6\sigma \Delta Y$ of $70m\Omega$.

Fina Con	$V_E = 1.500 V$	R _A =3.00 Ω	$R_B = 12.70$	$R_{\rm c} = 40.20$	R _D =12.00	$R_{\rm F}$ =1.00 Ω	
Optimisation Optimisation 2	$V_E=1.500 \text{ V}$	$R_A=1.0006 \Omega$	$R_B = 3.6994 \Omega$	$R_{\rm C} = 7.2199 \Omega$	$R_D = 3.9033 \Omega$	R_F =1.0001 Ω	
Δη: Optimisation 1	/ _E =33.810 V	$\Omega = 1.0000 \Omega$	$_{\rm B}$ =1.3413 Ω	$_{\rm C} = 1.2310 \Omega$	$\Omega = 1.8356 \Omega$	$_{\rm F} = 1.0002 \; \Omega$	

$R_F = 1.0002 \Omega$	$R_{\rm F}$ =1.0002 Ω $R_{\rm F}$ =1.0001 Ω	R _F =1.00 Ω
To obtain the	e greatest accuracy	To obtain the greatest accuracy possible the first set of
iterations were	e simply optimising	iterations were simply optimising AY without considering

A common battery voltage of 1.5 V was chosen as a easonable V_{E} . The power dissipated in each resistor was constrained below 0.1W in subsequent iterations. impractical design.

1% resistors were available from online suppliers in this design required 0.1% resistors to be viable. Only the required sizes. section 2. The high voltage and low resistance made it an any other design objectives. These are illustrated in

The resulting design had a ΔY of 7 m Ω . Unfortunately

Total power=167

12.4

00

3.1

00

The final circuit is guaranteed to be able to detect a 2Ω resistor to within 70mΩ, while consuming 167mW when balanced and for a resistor cost of E0.047