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An Audio Band Sigma-Delta Modulator with 104.7dB SNDR

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1 Introduction

This report details the design of a Sigma-Delta modulator in a design exercise. The specifications of this modulator are described in section 2. Full simulation of the design in macro-model in Cadence was not completed due to time constraints but no problems are anticipated.

Time constraints were aggravated due to experimentation with a CIFB design that required extensive modification in Simulink to be successfully verified. Unfortunately, there were many bugs encountered due to inexperience editing Simulink models. Finally, this design was abandoned in favour of a more established design that could meet the specifications.

A 2+1 MASH converter was chosen with an OSR of 128 to give adequate margin on the specifications. It is shown that this is a robust design that is capable of meeting the specifications. Due to time constraints it was not feasible to implement all the required extra blocks to build this modulator in Cadence. Verification of the operation of the macro-model was performed on a first order modulator instead, as most noise is expected to be attributed to the first stage.

2 Design

The required specifications are shown in table 2.1. These specifications are a relatively low signal bandwidth and a very high SNDR that is characteristic of an audio band ADC. In this section different options are evaluated and chosen from to meet these specifications.

Specification	Value
Supply Voltage (V_{dd})	3.3V
Differential Input Voltage	$1.8V_{rms}$
Reference voltage V_{refn}	0V
Reference voltage V_{refp}	$0.9 \times V_{dd}$
Signal to Noise Ratio	103dB
Total Harmonic Distortion at full-scale	-85dB
NO audio band limit cycles or tones	N/A
A flat audio band noise profile	N/A
Exclusive voltage references	N/A
Clock Frequency	12.288MHz

Table 2.1: A summary of the specifications required for this Sigma-Delta ADC.

2.1 Noise in Switched Capacitor Integrators

For any size of modulator the noise will be dominated by the first integrator at the input[1]. Shown in table 2.2 are the required input capacitor sizings for different OSRs and for a presumed SNDR of 106dB for a small margin on the specifications. Also shown in table 2.2 are the required g_m s of the amplifiers in the first integrator for these capacitor sizes and settling errors required.

Quantisation noise is intended to be a very small part of the noise budget([2], p.437) - making the initial SNDR target 123dB. The capacitor sizes are found by equating the expected quantisation noise for a 123dB SNDR with the expected kT/C noise on the capacitor:

$$\frac{mkT}{COSR} = N_q^2 = \frac{V_{inRMS}^2}{10^{\frac{SNDR}{10}}} = \frac{1.8^2}{10^{\frac{106}{10}}} = 8.14 \times 10^{-11}$$
 (2.1)

$$C = \frac{mkT}{OSRN_q^2} = \frac{4 \times 1.23 \times 10^{-23} \times 293}{OSR \times 8.14 \times 10^{-11}}$$
 (2.2)

Where V_{inRMS} is the RMS differential voltage range and m=4 for a differential circuit.

To find the required g_m , linear settling is assumed, and the settling time is dependent on OSR:

$$\tau_{settling} = \frac{256 \times T_{clk}}{2 \times OSR} \tag{2.3}$$

Where $\tau_{settling}$ is the settling time. To settle to within $\sqrt{8.14 \times 10^{-11}} = 9.02 \times 10^{-6} V_{RMS}$ over

OSR	Required Capacitor Size (F)	Required Amplifier g_m (S)
2	8.855×10^{-11}	2.305×10^{-4}
4	4.427×10^{-11}	2.305×10^{-4}
8	2.214×10^{-11}	2.305×10^{-4}
16	1.107×10^{-11}	2.305×10^{-4}
32	5.534×10^{-12}	2.305×10^{-4}
64	2.767×10^{-12}	2.305×10^{-4}
128	1.384×10^{-12}	2.305×10^{-4}
256	6.918×10^{-13}	2.305×10^{-4}

Table 2.2: A table summarising the required capacitor sizes and amplifier g_m s for different OSRs.

the $1.8V_{RMS}$ range of the circuit:

$$e^{\frac{-\tau_{settling}g_m}{C}} = \frac{9.02 \times 10^{-6}}{1.8} \tag{2.4}$$

$$e^{\frac{-\tau_{settling}g_m}{C}} = \frac{9.02 \times 10^{-6}}{1.8}$$

$$g_m = -\frac{C \times \ln \frac{9.02 \times 10^{-6}}{1.8}}{\tau_{settling}}$$
(2.4)

Neglecting second order effects it appears that there is no downside to choosing a high OSR in the design of a Sigma-Delta modulator. Effects such as slew rate and switch delays will affect these problems, however. Without more complex simulation analysis it is difficult to quantify these other effects and it can only be said that these effects will exist. Therefore, a high OSR is recommended for this design.

2.2Modulator Choice

Shown in table 2.3 are the major possible options that are projected based on graphs by Schreier & Temes([3], p.112-113) and lecture notes. This list is also limited to the options that are possible using the provided tools.

This list is reduced in that many of the CIFB designs are impossible to realise due to time constraints - they would require learning how to edit Simulink designs to add different quantisers and additional modulator stages. Initial attempts to edit Simulink designs were unsuccessful, therefore limiting the possibilities to third order designs with different OSRs.

It was possible to use MASH converter designs existing to meet the specifications with a lower OSR than would be required by a CIFB design. Unfortunately it has been shown in section 2.1 that this is not a first order concern - in fact, it is recommended to pick the highest possible OSR. A problem with MASH converter designs anticipated would be noise leakage([3], p.132) due to mismatches in the transfer functions of the different stages.

An additional problem with a MASH converter design is that simulations showed it would not have a completely flat audio band noise profile. This can be seen in figure 2.1 and can be compared with figure 2.2.

Table 2.3: A table summarising design options evaluated during the design.

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Architecture	Order	OSR	Peak Nominal Observed SNDR(dB)	Notes	
CIFB	3	128	109.0	Margin on specifications not high enough.	
CIFB	3	256	128.1		
MASH	2 + 1	128	126.8	Stable, established design.	
MASH	1+1+1	128	126.9	Error correcting abilities less effective than 2+1 design.	

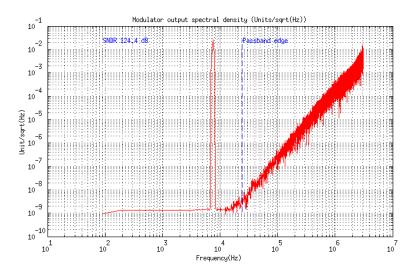


Figure 2.1: An example of a possible nominal MASH SNDR profile with a sine wave input.

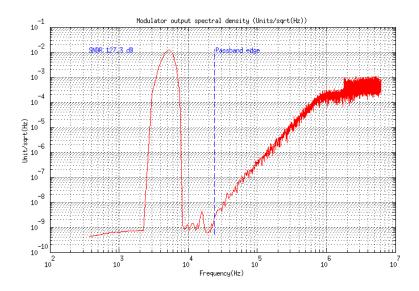


Figure 2.2: An example of a possible nominal CIFB SNDR profile with a sine wave input.

Originally, a 3rd order CIFB design with an OSR of 256 was chosen as the design as it was able to meet the flat audio band noise profile requirement thanks to its optimised NTF. Other advantages include it's simplicity with single-bit feedback and the anticipation of efficiency with the optimised transfer function. Unfortunately, this design proved impossible due to stability and requirements for modification in Simulink that were unsuccessful.

The second choice was a MASH 2+1 converter with an OSR of 128. Problems outlined above have been considered in the verification of the design in section 3.

2.3 Schematic

The top level functional diagram of a two stage 2+1 MASH modulator is shown in figure 2.3. This design comprises several standard blocks that can be further broken down into their circuit implementations.

2.3.1 Silva-Steensgaard Modulator

The first stage in this design is a second order modulator in a configuration known as a Silva-Steensgaard modulator. A differential circuit implementation of this circuit is shown in figure 2.4.

The gain elements and summing elements in this part of the design are implemented using capacitors. A differential multi-bit ADC and DAC must be implemented for this design to be created. A flash ADC implements the 2-bit ADC and an example circuit seen in figure 2.5 could be used to create the reference voltages if applied differentially.

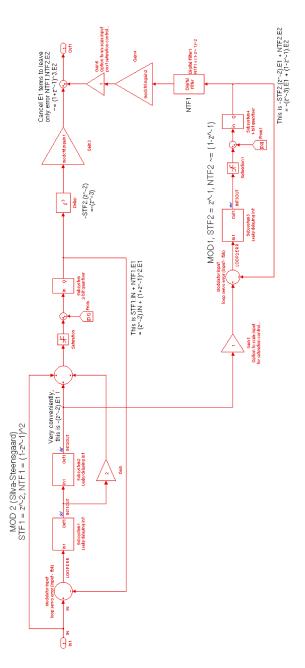


Figure 2.3: Top level functional block diagram of the MASH modulator chosen in this design.

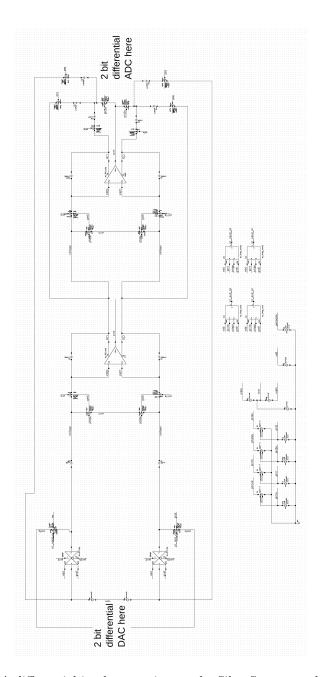


Figure 2.4: A differential implementation on the Silva-Steensgaard modulator.

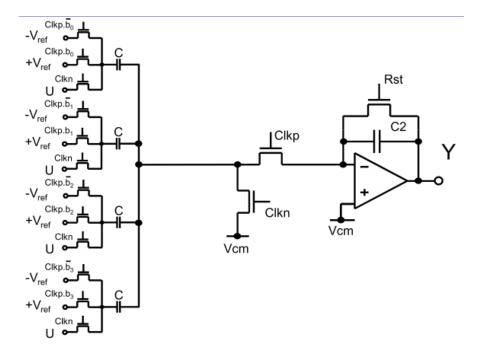


Figure 2.5: A multi-bit DAC switched capacitor implementation[4].

2.3.2 First Order Modulator

An example schematic for the first order modulator involved in this design is shown in figure 2.6. This is the second modulator in the design and is a standard differential modulator design.

A latched comparator is required to implement the single bit quantiser in the design. Designing this is a transistor level piece of design, and was not included in the design of the circuit.

2.3.3 Digital Signal Processing

The final signal processing in this modulator design is performed in the digital domain. A three cycle delay element, two gain operations and a summing element must be implemented in the digital design. This will also have to be combined with a digital filter after quantising prior to mixing.

Without any of these components in the library available to the design at this point the implementation in Cadence could not be completed. It will be demonstrated that this design will be successful upon completion.

2.4 Component Sizing

The components in the first integrator are assumed to contribute the vast majority of the noise in the design. Due to this, only the switches and capacitors in this part of the design are

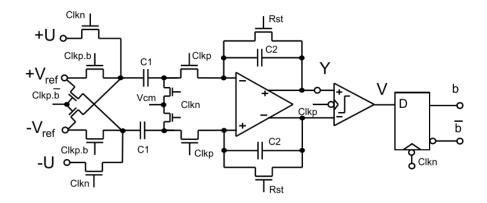


Figure 2.6: A differential implementation of a first order modulator[4].

considered in terms of their noise contribution. The required capacitor size for a 256 OSR and noise expectation comparable to an SQNR of 106dB is shown in table 2.2.

The switches in the design must also be sized - similarly to the expected g_m required for settling. Effective resistance of the switches must be designed in order that the voltage settles to within the required accuracy:

$$R_{switch} = -\frac{\tau_{settling}}{C \ln \frac{9.02 \times 10^{-6}}{1.8}} \tag{2.6}$$

This evaluates to an effective switch resistance of 4819.59Ω .

The required g_m of the amplifier contributes to the required sizing of the input devices for the amplifier - along with estimations of bias currents required. An approximate minimum bias current can be estimated by the current required to slew the entire signal range in half a settling period.

$$I = \frac{dV}{dt}C = \frac{2 \times 1.8}{4.069 \times 10^{-8}} (6.918 \times 10^{-13}) = 6.121 \times 10^{-5} A$$
 (2.7)

A bias current of approximately $100\mu A$ is therefore recommended in the input amplifier. Assuming an AMS process it is therefore possible to size the input devices for the settling requirements.

$$g_m = \sqrt{\frac{2K_p'W|I_D|}{L}} \tag{2.8}$$

$$g_m = \sqrt{\frac{2K'_p W |I_D|}{L}}$$

$$\frac{W}{L} = \frac{g_m^2}{2K'_p |I_D|} = \frac{(2.305 \times 10^{-4})^2}{2(14 \times 10^{-6})(100 \times 10^{-6})} = 18.975$$
(2.8)

Where $K'_p = 14\mu A/V^2$ - assuming PMOS input devices for lower noise performance. Requirements for wider devices due to slewing or gain requirements could change this estimation, but it provides a lower bound.

The remaining components - switches and capacitors in the design - will all be sized smaller than those at the input as the input referred effect of these components will be negligible. Schreier & Temes estimate the influence of capacitors in further stages to be approximately 0.01%([2], p.441) of the input capacitor's contribution. From this, it can be estimated that capacitors of 20fF would be a safe value, and this would ease settling requirements in the circuit - switches could be up to 50 times more resistive, and therefore 50 times less wide.

2.5 Conclusion

The design of this circuit was mainly a process of choosing a modulator architecture and OSR. Initial choices failed in simulation, forcing the choice of a dependable architecture. A 2+1 MASH converter with an OSR of 128 was chosen and the sizes of the various components were estimated.

3 Verification

Verification in matlab involved running many sweep tests of all possible signal amplitudes and DC levels. These tests were also run with non-ideal parameters set within the model to simulate a real circuit implementation.

3.1 DC Stability

Tones at the output of a modulator will degrade the SQNR performance of a circuit during normal operation. Also, the effects of DC inputs on the stability of the loop must also be investigated to find the input range of the modulator over which it is stable. The effect on output DC response from an input DC sweep due to finite amplifier gain is another important factor. The transient output of this modulator was inspected for various input voltages and found to be stable.

3.1.1 DC input voltage - DC output voltage

The effect of finite gain amplifiers on a design can be to cause "dead zones" to appear in the transfer function of DC input to DC output. This design is expected to be resistant to this effect as it is effectively a third order design and the width of the dead zone can be expected to be proportional to $\frac{1}{4^3}$.

The results of this design to this test are shown in figure 3.1. No dead zones are visible at any zoom level - the dead zones produced are smaller than the resolution of the sweep. This suggests it is likely the non-linearity will not affect the design.

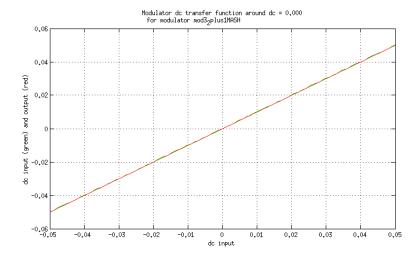


Figure 3.1: DC input voltage to DC output voltage for a finite gain of 1000.

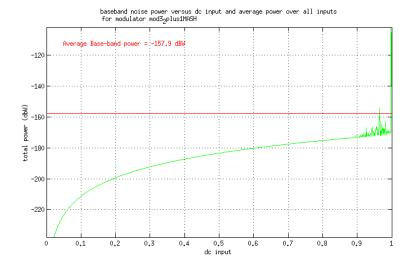


Figure 3.2: Nominal baseband power resulting from a sweep of DC inputs.

3.2 DC input voltage - baseband power

A sweep of DC input voltages while monitoring the baseband power will detect tones appearing at those input voltages. The result of this test is shown in figure 3.2. This was run with saturation limits in both integrators equal to 2.546V, to reflect the signal range required of the real circuits.

The baseband power never exceeds -103dB, so it can be expected that the circuit is well within specification.

3.3 SQNR Stability

To verify the performance of a Sigma-Delta modulator it is necessary to verify the resolution of the circuit at many input amplitudes and in cases involving non-ideal components. The cases tested here are:

- Capacitor mismatch
- $\bullet\,$ Finite gain
- Stage mismatch
- Finite signal swing

Without mismatch, but with a finite gain of 1000 and a finite signal swing equal to that expected in the amplifier of 2.546V differential, the results of a sweep of input sine amplitudes is shown in figure 3.3.

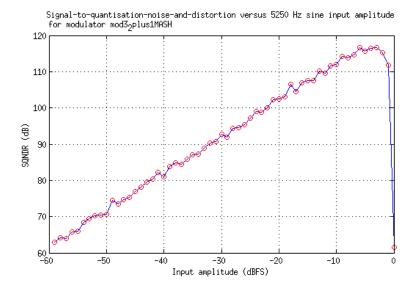


Figure 3.3: SQNR resulting from a sweep of different input amplitudes of a sine wave without mismatch is shown.

3.3.1 Capacitor Mismatch

Capacitor mismatch causes a mismatch in the multiplication stages of the amplifier. In the matlab model there are various precise multiplication elements that can be varied. The variation expected in capacitors is 0.4%, so a variation in these values of 0.4% must be tested. For a design margin, this can be increased to 1% mismatch on the two gains to modify in the design, shown in figure 2.3.

Applying gain mismatch of 1% in all four possible configurations; the worst observed result is shown in figure 3.4 - swept for all input amplitudes. The worst observed was a combination of 99% mgain 2 and 101% mgain 1. Figure 3.4 shows that the circuit is still able to meet the specification.

3.3.2 Effect of Noise Leakage

Noise leakage is governed by the mismatch of transfer functions from the fist and second stages of the modulator([3], p.132). This requires modifying gain components defining the individual stages. With the worst case gains from the previous section set, these two internal gain blocks were modified by 1% mismatch to find the worst combination. The result is shown in a sweep of all input amplitudes in figure 3.5.

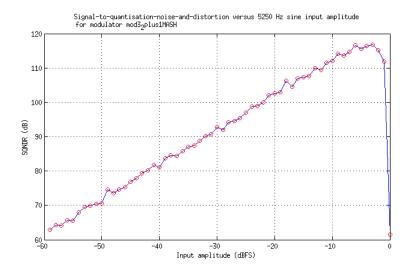


Figure 3.4: SQNR resulting from a sweep of different input amplitudes of a sine wave with capacitor mismatch is shown.

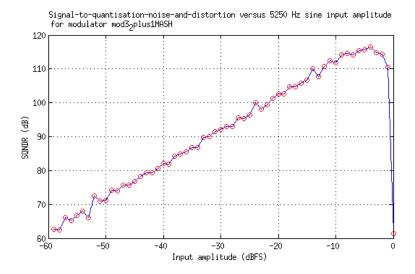


Figure 3.5: SQNR resulting from a sweep of different input amplitudes of a sine wave with transfer function mismatch is shown.

Table 3.1: The final capacitor and g_m sizings found through simulation of a first order modulator.

Component	Value
input g_m	$500\mu A/V$
output g_m	$500\mu A/V$
input R_{ds}	$2M\Omega$
output R_{ds}	$20k\Omega$
C_{in} and C_{fbk}	8pF

3.4 Cadence Tests

To show that the sizing of devices in section 2.4 is correct, the modulator should be simulated to show that the input referred noise is as low as expected. Unfortunately, the full modulator was not implemented in Cadence, making this full simulation impossible. To prove that the sizing is adequate a first order modulator noise simulation was performed with the input capacitor and g_m sizing calculated applied.

First order calculations proved to be inaccurate at this point and it was necessary to further increase the size of the input capacitors to meet the noise requirements. It was also necessary to increase the amplifier input g_m , output g_m was also scaled approximately in anticipation of the effect of higher capacitance on settling requirements - although, settling was not tested. The final values producing the noise results seen in Appendix A.1 can be seen in table 3.1.

The final thermal noise power achieved is therefore $10.2\mu V$, this can be combined with the worst case expected SQNR to create an estimate of SNDR for this design. Worst case SNDR was observed in section 3.3.2 was 116.9dB, this equates to $2.57\mu V$ RMS noise. Combining these in quadrature yields $10.52\mu V$ and an effective SNDR of 104.7dB SNDR. By extension, as this includes distortion, this means that the THD specification will also be met.

3.5 Conclusion

Although a full simulation of a macro-model implementation of the modulator has not been completed, the simulation results presented here show that this circuit is capable of meeting the specifications as described. Non-ideal effects have been considered in the matlab simulations and noise has been investigated in the Cadence simulations. From these results the circuit can be expected to work if completed.

4 Conclusion

This design exercise has resulted in a delta-sigma modulator design that is very likely to be successful. It is expected that this modulator is able to meet the required SNDR specification. Also, implementation and non-ideal component implications have been taken into account.

References

- [1] Henderson R. Sigma-Delta Data Converters Lecture 8. Edinburgh: University of Edinburgh; 2013.
- [2] Steensgaard J, Silva J, Schreier R, Temes GC. Noise in Switched-Capacitor Delta-Sigma Data Converters. In: Understanding Sigma-Delta Data Converters. Wiley; 2004. .
- [3] Schreier R, Temes GC. Higher-Order Delta-Sigma Modulation. In: Understanding Sigma-Delta Data Converters. Wiley; 2004. .
- [4] Henderson R. Sigma-Delta Data Converters Lecture 7. Edinburgh: University of Edinburgh; 2013

A Appendices

A.1 Noise Results

Below are the detailed noise results for the first order Sigma-Delta modulator simulated:

Danis	D	Notes Controller	% O.S. T. + - 3
Device	Param	Noise Contribution	% Of Total
/MP1	fn	0.00109039	11.67
/MP0	fn	0.00109039	11.67
/MN5	fn	0.000967633	9.19
/MN4	fn	0.000967632	9.19
/MN2	id	0.000794298	6.19
/MN3	id	0.000794297	6.19
/MN5	id	0.000693841	4.72
/MN4	id	0.000693841	4.72
/MP1	id	0.000679872	4.54
/MP0	id	0.000679869	4.54
/ISAMP/MNO	id	0.000640003	4.02
/ISAMN/MNO	id	0.000640003	4.02
/MN3	rd	0.000524886	2.70
/MN3	rs	0.000524886	2.70
/MN2	rs	0.000524886	2.70
/MN2	rd	0.000524885	2.70
/MN1	id	0.000438385	1.89
/MNO	id	0.000438382	1.89
/ISAMP/MPO	id	0.000315646	0.98
/ISAMN/MPO	id	0.000315646	0.98
/IAMP/RO	rn	0.000310759	0.95
/IAMP/R2	rn	0.000310757	0.95
/MN2	fn	0.000143192	0.20
/MN3	fn	0.000143175	0.20
/MNO	fn	0.000134174	0.18
/MN1	fn	0.000134169	0.18
/ISAMP/MNO	fn	8.94553e-05	0.08
/ISAMN/MNO	fn	8.94512e-05	0.08
/ISAMN/MPO	fn	1.32172e-05	0.00
/ISAMP/MPO	fn	1.32171e-05	0.00
/MP1	rd	4.04961e-07	0.00
/ISAMP/MPO	rd	3.85577e-07	0.00
/MPO	rd	3.38168e-07	0.00
/ISAMN/MPO	rd	3.38168e-07	0.00
/MN4	rd	2.3952e-07	0.00
/MN5	rd	2.39226e-07	0.00
/MN1	rd	2.28542e-07	0.00

/ISAMN/MNO	rd	2.21252e-07	0.00
/MNO	rd	2.04225e-07	0.00
/ISAMP/MNO	rd	2.04225e-07	0.00
/I12/R1	rn	7.04327e-13	0.00
/I12/R0	rn	2.57454e-14	0.00
/MP1	rs	1.1224e-19	0.00
/MN4	rs	8.2846e-20	0.00
/MN5	rs	8.15679e-20	0.00
/MN1	rs	6.73873e-20	0.00
/ISAMN/MPO	rs	2.59885e-23	0.00
/ISAMP/MPO	rs	2.06917e-23	0.00
/MNO	rs	1.91568e-23	0.00
/ISAMN/MNO	rs	1.09014e-23	0.00
/ISAMP/MNO	rs	1.05909e-26	0.00
/MPO	rs	1.84227e-27	0.00
/IAMP/RODSINP	rn	0	0.00
/IAMP/RODSINP	fn	0	0.00
/IAMP/RNOISEP	rn	0	0.00
/IAMP/RNOISEP	fn	0	0.00
/IAMP/RNOISEN	rn	0	0.00
/IAMP/RNOISEN	fn	0	0.00
/IAMP/RDSINN	rn	0	0.00
/IAMP/RDSINN	fn	0	0.00
/IAMP/R2	fn	0	0.00
/IAMP/RO	fn	0	0.00
/I12/R1	fn	0	0.00
/I12/R0	fn	0	0.00

Integrated Noise Summary (in $\mbox{\em V}\mbox{\em Sorted}$ By Noise Contributors

Total Summarized Noise = 0.00319233

Total Input Referred Noise = 1.01957e-05

The above noise summary info is for pnoise data