

RAG with Differential Privacy

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Abstract

Retrieval-Augmented Generation (RAG) has emerged as the dominant technique to provide *Large Language Models* (LLM) with fresh and relevant context, mitigating the risk of hallucinations and improving the overall quality of responses in environments with large and fast moving knowledge bases. However, the integration of external documents into the generation process raises significant privacy concerns. Indeed, when added to a prompt, it is not possible to guarantee a response will not inadvertently expose confidential data, leading to potential breaches of privacy and ethical dilemmas. This paper explores a practical solution to this problem suitable to general knowledge extraction from personal data. It shows *differentially private token generation* is a viable approach to private RAG.

Introduction

Retrieval-Augmented Generation (RAG, (Lewis et al. 2021)) has become a popular approach to enhance the capabilities of Large Language Models (LLMs) by supplying them with up-to-date and pertinent information. This method is particularly valuable in environments where knowledge bases are large and rapidly evolving, such as news websites, social media platforms, or scientific research databases. By integrating fresh context, RAG helps mitigate the risk of “hallucinations”—instances where the model generates plausible but factually incorrect information—and significantly improves the overall quality and relevance of the responses generated by the LLM.

However, incorporating external documents into the generation process introduces substantial privacy concerns. When these documents are included in the input prompt for the LLM, there is no foolproof way to ensure that the generated response will not accidentally reveal sensitive or confidential data (Qi et al. 2024). This potential for inadvertent data exposure can lead to serious breaches of privacy and presents significant ethical challenges. For instance, if an LLM is used in a healthcare setting and it accidentally includes patient information from an external document in its response, it could violate patient confidentiality and legal regulations.

This paper describes a practical solution (DP-RAG) aimed at addressing these privacy concerns with *Differential Privacy* (DP). The solution is based on two pillars:

- A method to collect documents related to the question in a way that does not prevent its output to be used in a DP mechanism.
- A method to use the collected documents to prompt a LLM and produce a response with DP guarantees.

The paper describes also some empirical tests and shows that *DP-RAG* is most effective in context where enough documents give elements of response.

Related Work

In general there are two families of approaches to add new knowledge to an LLM. The first is *Fine Tuning* (FT) and the other is *Retrieval Augmented Generation* (RAG). In both these approaches, adding privacy can be done, through simple heuristics with human validation such as *masking* or using a systematic and principle-based approach such as *Differential Privacy*.

Private Fine-Tuning

A straightforward approach to adding knowledge to an existing LLM is to continue its training with the new knowledge or to Fine Tune (FT) it. However, this raises challenges when dealing with private data, as LLMs tend to memorize training data. (see (Shokri et al. 2017) or (Carlini et al. 2021)).

To mitigate this privacy risk, it is possible to redact sensitive content prior to the FT process (aka. *masking*), but this operation is not very reliable and requires judgment on what should be redacted. This is a difficult manual operation based on the perceived sensitivity of each field and how it can be used to re-identify an individual, especially when combined with other publicly available data. Overall, it is very easy to get wrong; leaning too much on the side of prudence can yield useless data, while trying to optimize utility may result in leaking sensitive information.

A solution to this problem is to leverage *Differential Privacy*, a theoretical framework enabling the computation of aggregates with formal privacy guarantees (See (Dwork, Roth, et al. 2014)).

The most common approach to Private LLM FT is to use Differentially-Private-Stochastic-Gradient-Descent (DP-SGD, see (Abadi et al. 2016) and (Ponomareva et al. 2023)). DP-SGD is about clipping gradients and adding them some noise while running your ordinary SGD (or standard variants such as *Adam*, etc.). This method requires the data to be organized per *privacy unit* (typically a privacy unit will be a user). Every training example should belong to one and only one privacy unit¹.

But, when new documents are frequently added to the private knowledge base FT may not be the best approach.

¹Note that observations (examples) can be grouped into composite observations if one user contributes to many observations.

Private RAG

When FT is not the best approach to adding new knowledge and RAG would be preferred, DP-FT cannot help with privacy. In these cases, DP can still be leveraged in different ways. A straightforward approach to DP RAG is to generate synthetic documents with differential privacy out of the private knowledge base and then retrieve documents from this synthetic knowledge base instead of the private one. Another approach is to generate the LLM response in a DP way.

The approach of generating synthetic documents usable for RAG in privacy-sensitive contexts has been explored by (Zeng et al. 2024) but without DP guarantees. There are three main approaches to the problem of generating DP Synthetic Data (SD):

- Fine-Tuning a pretrained generative model with DP to generate synthetic documents.
- Use some form of automated prompt tuning to generate synthetic prompts or context documents.
- And use DP aggregated generation.

Fine-Tuning a pretrained generative model with DP can be done with DP-SGD ((Abadi et al. 2016) and (Ponomareva et al. 2023)) as mentioned above. An application to synthetic text generation is described there: (Yue et al. 2023). This method is technically complex, as, DP-SGD can be challenging to implement efficiently (Bu et al. 2023).

In (Hong et al. 2024), the authors use an automated prompt tuning technique developed in (Sordoni et al. 2023) and (Zhou et al. 2023) and make it differentially private. From the evaluations presented, it seems to compare favorably to DP-FT synthetic data approaches. Similar methods, based on DP-automated prompt tuning are exposed in (Lin et al. 2024) for images and (Xie et al. 2024) for text.

A last approach to generating synthetic data is based on DP aggregation of data. (Lebensold et al. 2024) or (Wu et al. 2023) show how to aggregate images or text in their embedding space (aka. Embedding Space Aggregation). Aggregating data privately is also the approach of (Tang et al. 2024), but they do it at the token level.

This last method greatly inspired the approach described in this document, though not for SD, but to directly generate RAG output from private documents.

DP-RAG

To overcome the limitations of DP FT or SD-based RAG, we developed and tested DP-RAG: a novel approach, build upon recent works on DP In-Context Learning (ICL) such as (Wu et al. 2023) and particularly (Tang et al. 2024).

- Contrary to (Wu et al. 2023), we aggregate outputs token by token.
- Our token aggregation method is different from both methods exposed in: (Tang et al. 2024) (*Gaussian* and *Report Noisy Max*).

- Because we implement the full RAG system, we developed a method to collect the *top-k* most similar documents in a way that does not jeopardize the possibility to run a DP mechanism on them.

Overview of DP-RAG

DP-RAG is made of two main components:

- A method to collect documents related to the question in a way that does not prevent its output to be used in a DP mechanism.
- A method to use the collected documents to prompt a LLM and produce a response with DP guarantees.

To understand the need for these components, let's describe what RAG is usually made of (see also (Lewis et al. 2021)) and introduce some notations (see Fig. 1).

A LLM: \mathcal{L} is a function, taking some text, in the form of a sequence of tokens: $x = \langle x_1, x_2, \dots, x_n \rangle$ as input and outputting a probability distribution of the next token x_{n+1} conditional on x :

$$\mathcal{L}(s, x) = \mathcal{L}(s, \langle x_1, x_2, \dots, x_n \rangle) = \Pr(x_{n+1} = s | \mathcal{L}, x_1, x_2, \dots, x_n)$$

We assume we have a set of N documents: $D = \{d_1, d_2, \dots, d_N\} \subset \mathcal{D}$ containing domain specific knowledge. These documents are also sequences of tokens: $d_i = \langle d_{i,1}, d_{i,2}, \dots, d_{i,l_i} \rangle$. We will, for simplicity, denote $\langle d_i, d_j \rangle$ the concatenation of two sequences of token, or a sequence and one token.

We also assume we have a similarity function $S : \mathcal{D}^2 \mapsto [-1, 1]$ which value is close to 1 when two documents are very similar, close to 0 when independent, and close to -1 when conveying opposite meaning. In this work S will be the cosine similarity between some embeddings of the documents, mapping them to some adequate d -dimensional vector space: \mathbb{R}^d :

$$S(d_i, d_j) = \frac{\langle E(d_i), E(d_j) \rangle}{\|E(d_i)\|_2 \|E(d_j)\|_2}$$

When receiving a query in the form of a sequence of token: $q = \langle q_1, q_2, \dots, q_{n_q} \rangle$, the similarity between q and each document is computed and the top k documents in term of similarity are collected:

$$d_{i_1}, d_{i_2}, \dots, d_{i_k} \text{ with } S(q, d_{i_1}) \geq S(q, d_{i_2}) \geq \dots \geq S(q, d_{i_k})$$

Then a new query q_{RAG} is built by concatenating the original query q with the top k documents and other elements (the operation is denoted $\langle \cdot, \dots, \cdot \rangle_{RAG}$)

$$q_{RAG} = \langle q, d_{i_1}, d_{i_2}, \dots, d_{i_k} \rangle_{RAG}$$

The augmented query is then sent to the LLM to compute the distribution of the next token (the first token of the response)

$$\mathcal{L}\left(r_1, \langle q, d_{i_1}, d_{i_2}, \dots, d_{i_k} \rangle_{RAG}\right)$$

The token is generated by sampling according to the distribution² or by selecting the mode of the distribution³.

The tokens of the response are then generated one by one in an auto-regressive manner. The generated response tokens are concatenated to the input sequence:

$$\mathcal{L}\left(r_{i+1}, \langle \langle q, d_{i_1}, d_{i_2}, \dots, d_{i_k} \rangle_{RAG}, r_1, r_2, \dots, r_i \rangle\right)$$

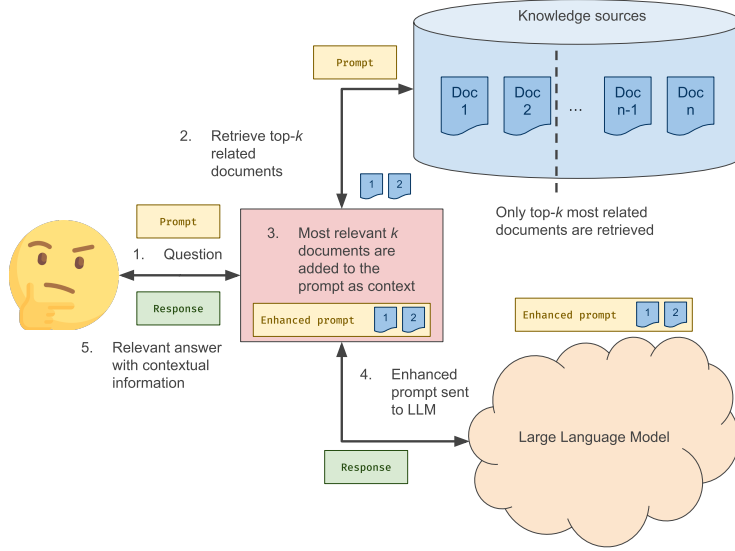


Figure 1: A broad picture of how RAG works

In the private variant of the problem (DP-RAG), we also assume the documents are *privacy sensitive*, and make the additional assumption that each document relates to only one individual that we call *privacy unit* (PU)⁴.

Differential Privacy and its application to RAG

A (randomized) algorithm: \mathcal{A} provides (ϵ, δ) -Differential Privacy *if and only if* for all event S and neighboring datasets D_0 and D_1 , we have:

$$\Pr[\mathcal{A}(D_0) \in S] \leq e^\epsilon \Pr[\mathcal{A}(D_1) \in S] + \delta$$

²or proportionally to some power $1/T$ of the distribution

³the most likely token or the limit when T goes to 0

⁴Such structuration of documents by privacy unit can sometime be achieved by cutting documents and grouping all the content relative to one PU in one document.

This means that for datasets that differ by one individual (i.e. neighboring datasets) the algorithm’s outputs are indistinguishable. This property guarantees that no bit of information can reasonably be learned about an individual. See (Dwork, Roth, et al. 2014) for a thorough introduction to DP.

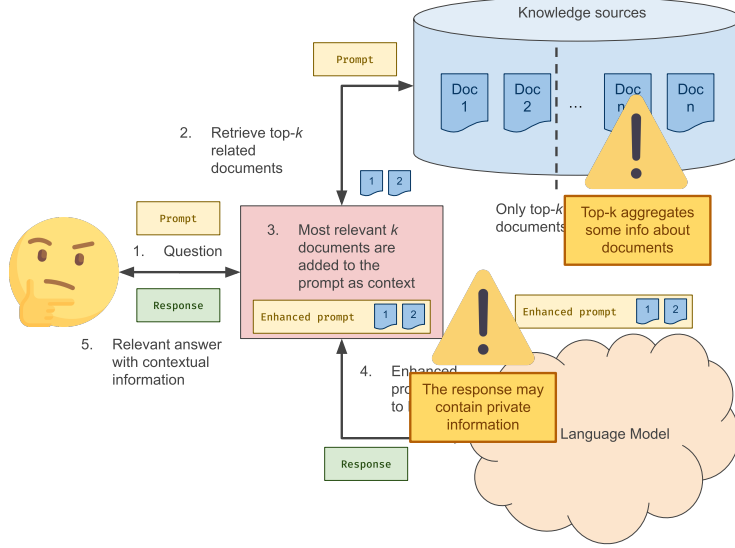


Figure 2: A broad picture of the main problems to overcome when considering DP RAG

There are two main challenges to implementing RAG with DP guarantees (see Fig. 2). One is to aggregate the knowledge from many documents with DP, the other, more subtle, consists in selecting the most relevant documents without jeopardizing our ability to apply a DP mechanism downstream.

Privacy Unit Preserving Document Retrieval

As mentionned above, DP deals with the concept of *neighboring* datasets. For this reason, it is convenient to assign each document to one and only one individual, or *privacy unity* (PU). Adding or removing one PU, comes down to adding or removing one document. In this context, one should be careful with the selection of the top-k most relevant document. Indeed, when selecting the top-k documents, adding or removing one document may affect the selection of other documents.

In DP-RAG, the similarity of each document with the query is computed:

$$s_1, s_2, \dots, s_N = S(q, d_1), S(q, d_2), \dots, S(q, d_N)$$

To estimate a threshold to select the top k documents with DP, we designed a utility function to be plugged into an exponential mechanism (Dwork, Roth, et al. 2014).

$$U(\tau) : [0, 1] \mapsto \mathbb{R} = - \left| \sum_i \mathbb{1}_{[0, s_i]}(\tau) - k \right|$$

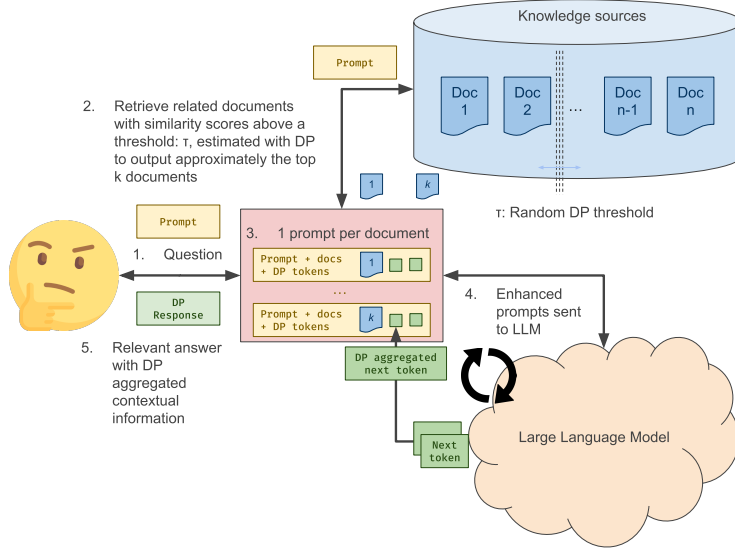


Figure 3: In DP-RAG, k smaller queries are sent to the LLM, rather than a single query (approximately) k times larger.

The DP top- k threshold τ_{DP} sampled from the exponential mechanism is used to select all the documents whose similarity is above τ_{DP} .

Differentially Private In-Context Learning

(Durfee and Rogers 2019) could be used for token selection

Evaluation

Conclusion

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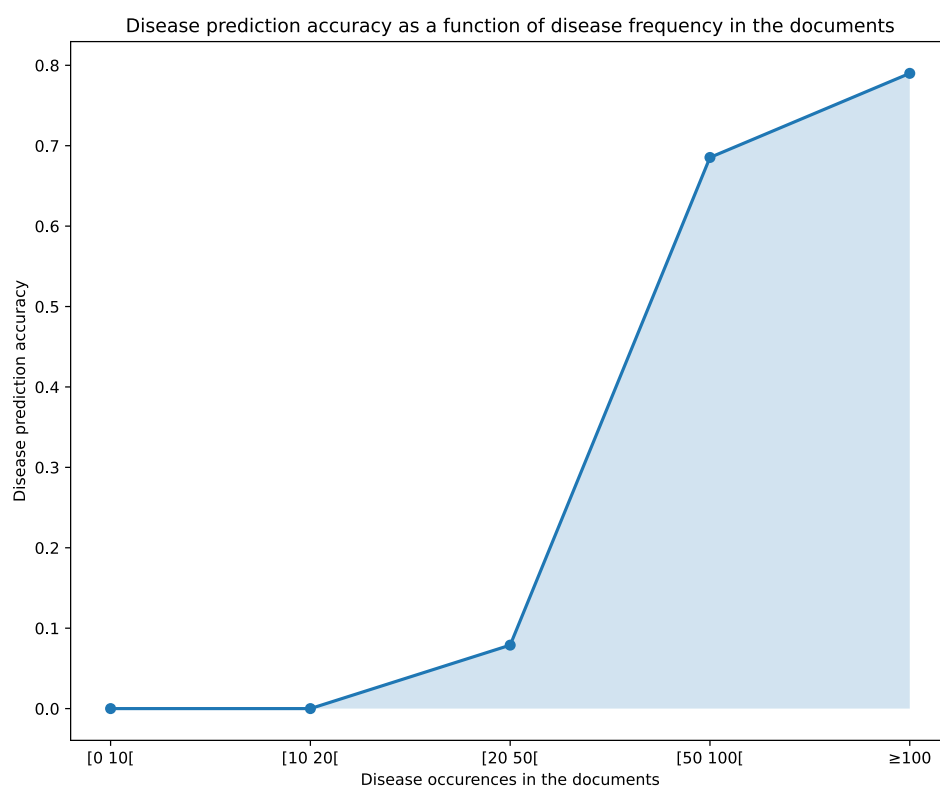


Figure 4: DP-RAG accuracy as a function of knowledge specificity

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