

# RAG with Differential Privacy

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## Abstract

Retrieval-Augmented Generation (RAG) has emerged as the dominant technique to provide *Large Language Models* (LLM) with fresh and relevant context, mitigating the risk of hallucinations and improving the overall quality of responses in environments with fast moving knowledge bases. However, the integration of external documents into the generation process raises significant privacy concerns. Indeed, when added to a prompt, it is not possible to guarantee a response will not inadvertently expose confidential data, leading to potential breaches of privacy and ethical dilemmas. This paper explores a practical solution to this problem suitable to general knowledge extraction from personal data. It shows *differentially private token generation* is a viable approach to private RAG.

## Introduction

Retrieval-Augmented Generation (RAG) has become a leading approach to enhance the capabilities of Large Language Models (LLMs) by supplying them with up-to-date and pertinent information. This method is particularly valuable in environments where knowledge bases are rapidly evolving, such as news websites, social media platforms, or scientific research databases. By integrating fresh context, RAG helps mitigate the risk of “hallucinations”—instances where the model generates plausible but factually incorrect information—and significantly improves the overall quality and relevance of the responses generated by the LLM.

However, incorporating external documents into the generation process introduces substantial privacy concerns. When these documents are included in the input prompt for the LLM, there is no foolproof way to ensure that the generated response will not accidentally reveal sensitive or confidential data (Qi et al. 2024). This potential for inadvertent data exposure can lead to serious breaches of privacy and presents significant ethical challenges. For instance, if an LLM is used in a healthcare setting and it accidentally includes patient information from an external document in its response, it could violate patient confidentiality and legal regulations.

This paper describes a practical solution (DP-RAG) aimed at addressing these privacy concerns with *Differential Privacy* (DP). The solution is based on two pillars:

- A method to collect documents related to the question in a way that does not prevent its output to be used in a DP mechanism.
- A method to use the collected documents to prompt a LLM and produce a response with DP guarantees.

The paper describes also some empirical tests and shows that *DP-RAG* is most effective in context where enough documents give elements of response.

## Related Work

In general there are 2 families of approaches to add new knowledge to an LLM. The first *Fine Tuning* (FT) and the other is *Retrieval Augmented Generation* (RAG). In both these approaches, adding privacy can be done, through simple heuristics with human validation such as *masking* or using a systematic and principle-based approach such as *Differential Privacy*.

## Private Fine-Tuning

A straightforward approach to adding knowledge to an existing LLM is to continue its training with the new knowledge or to Fine Tune (FT) it. However, this raises challenges when dealing with private data, as LLMs tend to memorize training data. (see (Shokri et al. 2017) or (Carlini et al. 2021)).

To mitigate this privacy risk, it is possible to redact sensitive content prior to the FT process (aka. *masking*), but this operation is not very reliable and requires judgment on what should be redacted. This is a difficult manual operation based on the perceived sensitivity of each field and how it can be used to re-identify an individual, especially when combined with other publicly available data. Overall, it is very easy to get wrong; leaning too much on the side of prudence can yield useless data, while trying to optimize utility may result in leaking sensitive information.

A solution to this problem is to leverage *Differential Privacy*, a theoretical framework enabling the computation of aggregates with formal privacy guarantees (See (Dwork, Roth, et al. 2014)).

The most common approach to Private LLM FT is to use Differentially-Private-Stochastic-Gradient-Descent (DP-SGD, see (Abadi et al. 2016) and (Ponomareva et al. 2023)). DP-SGD is about clipping gradients and adding them some noise while running your ordinary SGD (or standard variants such as *Adam*, etc.). This method requires the data to be organized per *privacy unit* (typically a privacy unit will be a user). Every training example should belong to one and only one privacy unit<sup>1</sup>.

But, when new documents are frequently added to the private knowledge base FT may not be the best approach.

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<sup>1</sup>Note that observations (examples) can be grouped into composite observations if one user contributes to many observations.

## Private RAG

When FT is not the best approach to adding new knowledge, DP-FT cannot help with privacy. In these cases, DP can still be leveraged in different ways. A straightforward approach to DP RAG is to generate synthetic documents with differential privacy out of the private document pool and retrieve documents from the synthetic pool instead of the private one. Another approach is to generate the LLM response in a DP way.

The approach of generating synthetic documents usable for RAG has been explored by (Zeng et al. 2024) but without DP guarantees. There are three main approaches to the problem of generating DP Synthetic Data (SD):

- Fine-Tuning a pretrained generative model with DP to generate synthetic documents.
- Use some form of automated prompt tuning to generate synthetic prompts or context documents.
- And use DP aggregated generation.

Fine-Tuning a pretrained generative model with DP can be done with DP-SGD ((Abadi et al. 2016) and (Ponomareva et al. 2023)) as mentioned above. An application to synthetic text generation is described there: (Yue et al. 2023). This method is technically complex, as, DP-SGD can be challenging to implement efficiently (Bu et al. 2023).

In (Hong et al. 2024), the authors use an automated prompt tuning technique developed in (Sordani et al. 2023) and (Zhou et al. 2023) and make it differentially private. From the evaluations presented, it seems to compare favorably to DP-FT synthetic data approaches. Similar methods, based on DP-automated prompt tuning are exposed in (Lin et al. 2024) for images and (Xie et al. 2024) for text.

A last approach to generating synthetic data is based on DP aggregation of data. (Lebensold et al. 2024) or (Wu et al. 2023) show how to aggregate images or text in their embedding space (aka. Embedding Space Aggregation). Aggregating data privately is also the approach of (Tang et al. 2024), but they do it at the token level.

This last method greatly inspired the approach described in this document, though not for SD, but to directly generate RAG output from private documents.

## DP-RAG

To overcome the limitations of DP FT or SD-based RAG, we developed and tested a novel approach, build upon recent works on DP In-Context Learning (ICL) (see (Wu et al. 2023) and particularly (Tang et al. 2024)).

### Overview

DP-RAG is made of 2 main components:

- A method to collect documents related to the question in a way that does not prevent its output to be used in a DP mechanism.
- A method to use the collected documents to prompt a LLM and produce a response with DP guarantees.

To understand the need for these components, let's describe what RAG is usually made of, and the assumptions we make for its private variant (DP-RAG).

A LLM:  $\mathcal{L}$  is a function, taking some text, in the form of a sequence of tokens:  $x = \langle x_0, x_1, \dots, x_{n-1} \rangle$  as input and outputting a probability distribution of the next token  $x_n$  conditional on  $x$ :

$$\mathcal{L}(y, x) = \mathcal{L}(s, \langle x_0, x_1, \dots, x_{n-1} \rangle) = \Pr(x_n = y | \mathcal{L}, x_0, x_1, \dots, x_{n-1})$$

We assume we have a set of  $N$  documents:  $d_1, d_2, \dots, d_N$  containing domain specific knowledge. These documents are also sequences of tokens:  $d_i = \langle d_{i,1}, d_{i,2}, \dots, d_{i,m} \rangle$ . We also assume these documents are *privacy sensitive*, and make the relatively strong assumption that each document relates to only one individual that we call *privacy unit* (PU)<sup>2</sup>.

## Differential Privacy and its application to RAG

A (randomized) algorithm:  $\mathcal{A}$  provides  $(\epsilon, \delta)$ -Differential Privacy

$$\Pr[\mathcal{A}(D_1) \in S] \leq e^\epsilon \Pr[\mathcal{A}(D_2) \in S] + \delta.$$

See (Dwork, Roth, et al. 2014) for more background on DP.

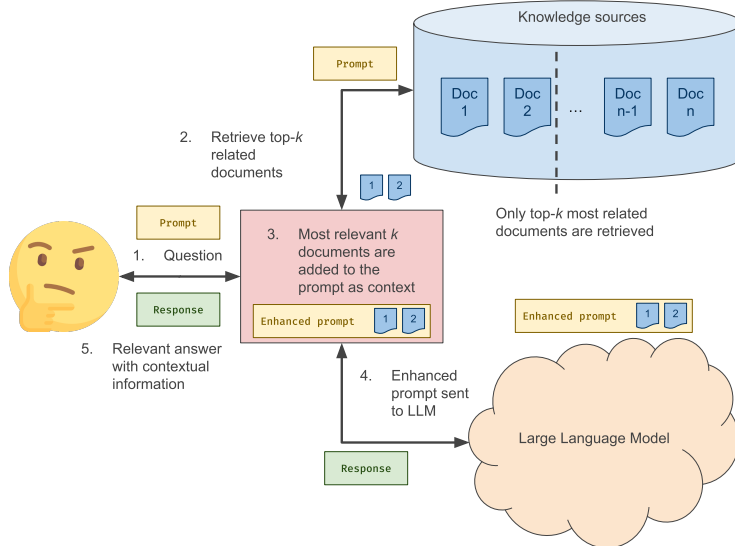


Figure 1: A broad picture of how RAG works

<sup>2</sup>Such structuration of documents by privacy unit can sometime be achieved by cutting documents and grouping all the content relative to one PU in one document.

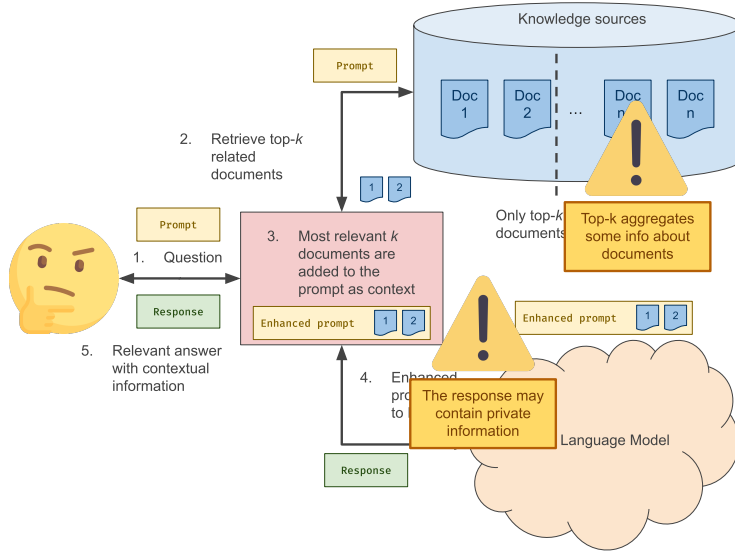


Figure 2: A broad picture of how RAG works

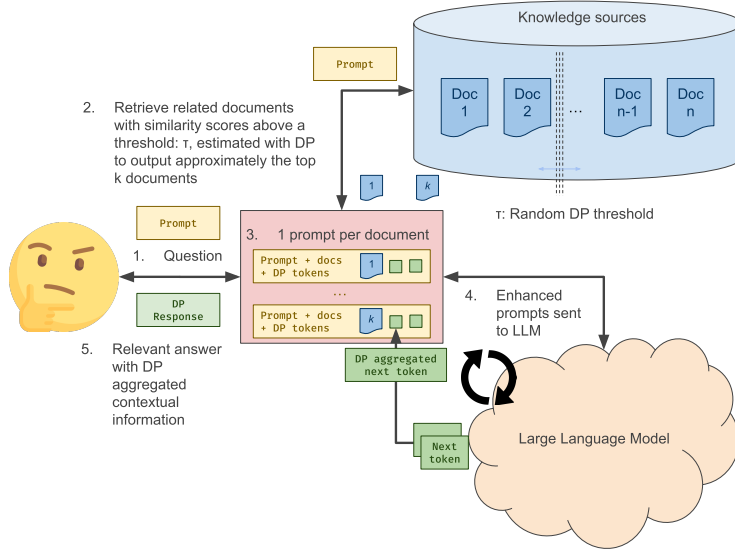


Figure 3: In DP-RAG,  $k$  smaller queries are sent to the LLM, rather than a single query (approximately)  $k$  times larger.

# Privacy Unit Preserving Document Retrieval

## Differentially Private In-Context Learning

(Durfee and Rogers 2019) could be used for token selection

## Evaluation

## Conclusion

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