

# Project 1 (Water Pitcher)

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**Course:** Artificial Intelligence

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## Overview

The Water Pitcher problem is:

- You have several finite-capacity pitchers (3 liters, 5 liters, etc.) plus one **infinite** pitcher.
- Your goal is to measure out a specific target quantity of water into the infinite pitcher.
- Each move (pouring or filling) has a cost of 1 step.
- You want the **shortest** sequence of steps that results in the infinite pitcher holding the target amount.

## File Structure

- **main.py**
  - `parse_file`: Reads capacities and target from file.
  - `can_measure`: Checks if target is possible (via GCD).
  - `heuristic`: **Lower bound** for  $A^* = \text{ceil}(\text{remaining} / \text{smallest\_pitcher})$  (never overestimates).
  - `fill / pour`: Generate next states.
  - `a_star`: Runs  $A^*$  to find shortest solution or -1 if impossible.
- **test.py**
  - Uses `unittest` to validate parsing, measuring, heuristic correctness, pouring/filling operations, and final  $A^*$  results.

**Tests ensure that:**

- The input file is correctly parsed.
- Feasibility of measuring the target with given containers is accurately determined.
- The heuristic function provides reasonable estimates.
- Filling and pouring operations produce correct new states.
- The overall  $A^*$  search algorithm correctly identifies both unsolvable and trivial cases.

## $A^*$ Overview

$A^*$  expands states in order of their priority  $f = g + h$ , where:

- $g$  = the number of steps taken so far.

- **h** = the heuristic (our **lower bound** on how many more steps are needed).

### Why the Lower Bound Is Crucial

```
def heuristic(state, goal, sizes):
    needed = goal - state[-1]
    if not needed:
        return 0
    finite = sizes[:-1]
    return math.inf if not finite else ceil(abs(needed) / min(finite))
```

- The heuristic here in the code snippet, doesn't *overestimate* the remaining cost, so it is **admissible**.
- An admissible heuristic guarantees that A\* always finds the optimal (shortest) path. Without a valid lower bound, it would just be a uniform-cost search, losing A\*'s efficiency advantage.

### Run program:

```
python main.py input1.txt
```

### Run test:

```
python -m unittest test.py
```