In [29]:

```
area = [
    [0,0,0,0,0,0,0,0,0,0]
    [0,1,1,0,0,0,0,0,0,0,0]
    [0,1,1,0,0,0,0,0,0,0,0]
    [0,1,1,0,0,0,0,0,0,0,0]
    [0,1,1,0,0,0,0,0,0,0,0]
    [0,1,1,0,0,0,0,0,0,0,0]
    [0,1,1,0,0,0,0,0,0,0,0]
    [0,1,1,0,0,0,0,0,0,0,0]
    [0,1,1,1,1,1,1,1,1,1,0],
    [0,1,1,1,1,1,1,1,1,1,0],
    [0,0,0,0,0,0,0,0,0,0]
x = 42
section = [[0 for _ in range(x)] for _ in range(x)]
for i in range(1,x-1):
    for j in range(1,x-1):
        if i < x//3 *2 and j < x//3:
           section[i][j] = 1
       elif i >= x//3 *2:
           section[i][j] = 1
for i in section:
   print(i)
```

```
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0]
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0]
```

1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0] 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 0]

In [30]:

```
cnt = 0
for line in area:
   for i in range(len(line)):
        if line[i]:
           line[i] = cnt + 1
           cnt += 1
area
cnt = 0
for line in section:
   for i in range(len(line)):
       if line[i]:
           line[i] = cnt + 1
           cnt += 1
for i in section:
   print(i)
print(cnt)
```

```
[0, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 0, 0, 0, 0, 0, 0, 0, 0, 0,
[0, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 0, 0, 0, 0,
[0, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 0, 0, 0, 0,
[0, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 0, 0, 0, 0,
[0, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 0, 0, 0, 0,
[0, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 0, 0, 0, 0,
[0, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 0, 0, 0, 0,
[0, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 0, 0, 0, 0,
[0, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 0, 0, 0, 0,
[0, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 0, 0, 0, 0,
[0, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 0, 0, 0, 0,
[0, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 0, 0, 0, 0,
[0, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 0, 0, 0,
[0, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 0, 0, 0, 0,
[0, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 0, 0, 0, 0,
[0, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 0, 0, 0, 0,
[0, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 0, 0, 0, 0,
[0, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 0, 0, 0, 0,
[0, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 0, 0, 0, 0,
[0, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 0, 0, 0, 0,
[0, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 36
7, 368, 369, 370, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 383,
384, 385, 386, 387, 388, 389, 390, 391, 0]
[0, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 40
7, 408, 409, 410, 411, 412, 413, 414, 415, 416, 417, 418, 419, 420, 421, 422, 423,
```

```
424, 425, 426, 427, 428, 429, 430, 431, 0]
[0, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 44
7, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463,
464, 465, 466, 467, 468, 469, 470, 471, 0]
[0, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 48
7, 488, 489, 490, 491, 492, 493, 494, 495, 496, 497, 498, 499, 500, 501, 502, 503,
504, 505, 506, 507, 508, 509, 510, 511, 0]
[0, 512, 513, 514, 515, 516, 517, 518, 519, 520, 521, 522, 523, 524, 525, 526, 52
7, 528, 529, 530, 531, 532, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543,
544, 545, 546, 547, 548, 549, 550, 551, 0]
[0, 552, 553, 554, 555, 556, 557, 558, 559, 560, 561, 562, 563, 564, 565, 566, 56
7, 568, 569, 570, 571, 572, 573, 574, 575, 576, 577, 578, 579, 580, 581, 582, 583
584, 585, 586, 587, 588, 589, 590, 591, 0]
[0, 592, 593, 594, 595, 596, 597, 598, 599, 600, 601, 602, 603, 604, 605, 606, 60
7, 608, 609, 610, 611, 612, 613, 614, 615, 616, 617, 618, 619, 620, 621, 622, 623,
624, 625, 626, 627, 628, 629, 630, 631, 0]
[0, 632, 633, 634, 635, 636, 637, 638, 639, 640, 641, 642, 643, 644, 645, 646, 64
7, 648, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663,
664, 665, 666, 667, 668, 669, 670, 671, 0]
[0, 672, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 68
7, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 698, 699, 700, 701, 702, 703,
704, 705, 706, 707, 708, 709, 710, 711, 0]
[0, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 72
7, 728, 729, 730, 731, 732, 733, 734, 735, 736, 737, 738, 739, 740, 741, 742, 743,
744, 745, 746, 747, 748, 749, 750, 751, 0]
[0, 752, 753, 754, 755, 756, 757, 758, 759, 760, 761, 762, 763, 764, 765, 766, 76
7, 768, 769, 770, 771, 772, 773, 774, 775, 776, 777, 778, 779, 780, 781, 782, 783
784, 785, 786, 787, 788, 789, 790, 791, 0]
[0, 792, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804, 805, 806, 80
7, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823,
824, 825, 826, 827, 828, 829, 830, 831, 0]
[0, 832, 833, 834, 835, 836, 837, 838, 839, 840, 841, 842, 843, 844, 845, 846, 84
7, 848, 849, 850, 851, 852, 853, 854, 855, 856, 857, 858, 859, 860, 861, 862, 863,
864, 865, 866, 867, 868, 869, 870, 871, 0]
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]
871
```

In [18]:

```
#초기 빈 행렬식 A
# cnt가 미지수의 개수
A = [[O for _ in range(cnt+1)] for _ in range(cnt)]
# for i in A:
# print(i)
```

In [31]:

```
dx = [1, -1, 0, 0]
dy = [0, 0, 1, -1] #이동기
def solve(y, x, linenum):
    for k in range(4):
        next_y = y + dy[k]
        next_x = x + dx[k]
        if 0 <= next_x < len(section) and 0 <= next_y < len(section) and section[next_y][next_x
]:
            nodenum = section[next_y][next_x]-1
            A[Iinenum][nodenum] = -1
for y in range(len(section)):
    for x in range(len(section)):
        if section[y][x]:
            linenum = section[y][x]-1
            A[Iinenum][Iinenum] = 4
            solve(y,x,linenum)
for line in A:
    line[-1] = 0.005
# for line in A:
     print(line)
```

In []:

```
import numpy as np
n=cnt
A = np.array(A, dtype=float)
pivot_target = []
for i in range(0, n-1):
   for j in range(i+1, n):
       temp = A[i,i]/A[i,i]
       A[i,:] = A[i,:] - temp * A[i,:]
     print(np.matrix(A))
   # 대각행렬에 0이 있는 행은 pivot_target이라는 리스트에 추가.
   for x in range(i, n-1):
       if not A[x,x]:
           pivot_target.append(x)
   #pivot_target이 다 떨어질 때까지 반복하면서 피버팅
   while pivot_target:
         print("While 안에 들어옴")
         print(np.matrix(A))
#
       x = pivot_target.pop()
       for change_target in range(i+1, n-1):
           if A[x,change_target] and A[change_target,x]:
               A[[x,change_target]] = A[[change_target,x]]
x = np.zeros(shape=(n,1), dtype=float)
for i in range(n-1,-1,-1):
   if i==n-1:
       x[i]=A[i,n]/A[i,i]
   else:
       x[i]=A[i,n]/A[i,i]
       for j in range(1, n-i):
           x[i] = x[i] - (A[i,i+i]/A[i,i]) *x[i+i]
print(x)
```

In [21]:

```
xx = []
for i in range(len(x)):
    xx.append(float(x[i]))
xx
```

Out[21]:

- [0.008020878782066513,
- 0.013514652113405135,
- 0.017441522837290085.
- 0.02023620270620251,
- 0.022119759734645333,
- 0.023210580450816296,
- 0.02356813612998819,
- 0.023210637735106236,
- 0.022119862958078662,
- 0.020236331424997304,
- 0.01744165155750444,
- 0.013514755340028186,
- 0.008020936068914415,
- 0.013568863014860913.
- 0.023596206834263937,
- 0.031015236529552702,
- 0.03638352825287462,
- 0.04003225578156253,
- 0.042154425938631654,
- 0.042851326334030236,
- 0.0421545518523581,
- 0.04003248267221111,
- 0.036383811184406124,
- 0.031015519464992286,
- 0.02359643373369389.
- 0.013568988935629474,
- 0.0176583664431132.
- 0.03128607567923702,
- 0.04163968819378219,
- 0.049250417994180756,
- 0.05447130920009854.
- 0.05752354118811753,
- 0.05852819141514293,
- 0.057523760668084775,
- 0.05447170469400153,
- 0.0492509111754238,
- 0.04164018138436469,
- 0.03128647119412561,
- 0.017658585939909578.
- 0.020778527078354852,
- 0.03725004124578872,
- 0.05000702257215826,
- 0.0595071463299677.
- 0.06607902183653327,
- 0.06994023819859699,
- 0.0712141374703392,
- 0.0699405947108365.
- 0.06607966426028644,
- 0.05950794743892286,
- 0.050007823702917065.
- 0.03725068371853427,
- 0.020778883629883234,
- 0.023205700624517486, 0.04192853965340481,
- 0.05663121451909438,
- 0.06769212291699853,
- 0.07539739361746989,
- 0.07994425229939789,
- 0.08144752555678032,

- 0.07994481644463562,
- 0.07539841019738483.
- 0.06769339061706418,
- 0.056632482269846435,
- 0.04192955634721113,
- 0.023206264861089086,
- 0.025115735766310255,
- 0.04562720222421869,
- 0.0618971729338159, 0.07423273720146217,
- 0.08287417741694988.
- 0.08799185182474431,
- 0.08968689601274857,
- 0.08799273531354079,
- 0.08287576946755303,
- 0.07423472256210265,
- 0.061899158412193366,
- 0.0456287945393747,
- 0.02511661946726199,
- 0.026630040216504856,
- 0.048567360543343735,
- 0.0660975377904884.
- 0.07946747553808436,
- 0.08887472702412322,
- 0.09446208156988091,
- 0.09631547135592879,
- 0.09446345932922603,
- 0.08887720979718387.
- 0.07947057175160005,
- 0.06610063427744968,
- 0.04856984393083233,
- 0.026631418468584148,
- 0.027837064556365452,
- 0.05091466194216307,
- 0.06945814214670955.
- 0.08366490013626364,
- 0.09369517357157771,
- 0.09966627607472728,
- 0.1016494485118597,
- 0.09966842085025077,
- 0.0936990386403565,
- 0.08366972036966397,
- 0.069462963015173,
- 0.05091852843792073,
- 0.027839210476242264,
- 0.02880355606679391,
- 0.05279608052223356,
- 0.07215546871792317,
- 0.08703880928868288,
- 0.09757479105119668,
- 0.10385840064559083,
- 0.10594762576653194,
- 0.10386173691956097.
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- 0.08704630807152641,
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- 0.029581079188576657,
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- 0.07432884291406669,

- 0.08976007724934813,
- 0.10070678069893534,
- 0.1072449096899074,
- 0.10942091698911616,
- 0.10725009751713382,
- 0.10071613054586546,
- 0.08977173939645675,
- 0.07434050848649582,
- 0.07 10 10000 100 10002,
- 0.054319992905698944,
- 0.029586273188179024,
- 0.030210125325458692,
- 0.055536538823339185,
- 0.07608919032694147,
- 0.0919658760957077,
- 0.10324734480528916,
- 0.10999354042598719,
- 0.11224103498289145,
- 0.11000160561399276,
- 0.103261881725544,
- 0.09198401048193927,
- 0.07610733266816996,
- 0.05555109361868561.
- 0.030218204848552997,
- 0.03072288328991891,
- 0.05653620427890252,
- 0.07752550347465238,
- 0.09376689200125203,
- 0.10532318200052648.
- 0.10302010200032040
- 0.11224087222586071,
- 0.11454807690246972,
- 0.11225340823040184,
- 0.10534578026037855,
- 0.09379508813758639,
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- 0.031145203555314464,
- 0.05735989152769963,
- 0.07870972729151357,
- 0.09525300643412152,
- 0.10703761896970407,
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- 0.11645699217072485,
- 0.11411817014476647,
- 0.10707274294798189,
- 0.0952968437224686,
- 0.07875360748415947,
- 0.05739511191769016,
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- 0.05810323468576479,

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- 0.03179852307417463,
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- 0.1109250622399359,
- 0.09866119389861062,
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- 0.05960984486940156,
- 0.08195528343376376,
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- 0.11178360709986382,
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- 0.11938733797762482,
- 0.11198784000549483,
- 0.09960007347641228,
- 0.08221230128812532,
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- 0.03241170562904399,
- 0.03251516947772901,
- 0.06003954866319033,
- 0.0825804763681463,
- 0.10014175155384805,
- 0.11272237249850409,
- 0.12031589540080743,
- 0.12291062108366665,
- 0.12049079047810311,
- 0.11303888632800631,
- 0.10053895871341836,
- 0.08298057751236858,
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- 0.032695295074825256,
- 0.03272468375751639,
- 0.060452703937484475,
- 0.08318532182178309,
- 0.10091985465054523,
- 0.11364823593949705,
- 0.12135625927938651,
- 0.12402379792532289,0.12162631652311458,
- localhost:8888/nbconvert/html/TermProject.ipynb?download=false

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- 0.10153629753688638,
- 0.08380847633155558,
- 0.06095754030979646,
- 0.033006900953881944,
- 0.03293086161485211,
- 0.060861261507448056,
- 0.08378825233095635,
- 0.10170410928705276,
- 0.11459445732955226,
- 0.12243710785191861.
- 0.12520199481512378,
- 0.12285272157402341,
- 0.12203212131402041
- 0.11535032407202842,0.10265979898756256,
- 0.10200010000700200
- 0.08475948996717089,
- 0.06165221023737323,
- 0.03337476843090606,
- 0.033137501194444016,
- 0.06127322814649935,
- 0.08440231670754159,
- 0.10251387283715721.
- 0.11558837623974055,
- 0.12359571998361198,
- 0.12649435190923025,
- 0.12423225088582687,
- 0.1167508196115188,
- 0.10399308437416452.
- 0.08591747431219224,
- 0.06251704224161952,
- 0.03383996253236904,
- 0.0333459150164246,
- 0.06169183317656382,
- 0.08503391351555341,
- 0.10336068911429389.
- 0.11664945480864072,
- 0.12486304393355846,
- 0.12794744195235844,
- 0.12583111044853504,
- 0.11842761911405536.
- 0.10564424458538452,
- 0.08740028066581394,
- 0.06365852188454359,
- 0.034468039456950594,
- 0.03355432569469056,
- 0.062114276027777936,
- 0.08568081506381423,
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- 0.11778570994696998,
- 0.11776076001000000
- 0.12625955898962266,
- 0.1296012615181099,0.1277171298418995,
- 0.12048430181078293,
- 0.1077559941875042,
- 0.0893808818811354,
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In [24]:

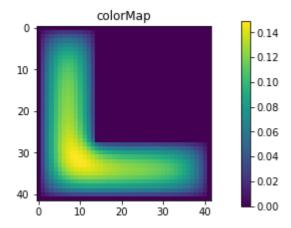
```
import numpy as np
import matplotlib.pyplot as plt

H = np.array(potential_section)

fig = plt.figure(figsize=(6, 3.2))

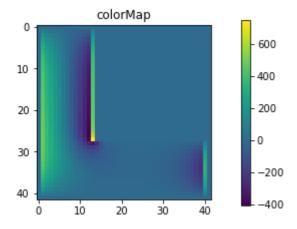
ax = fig.add_subplot(111)
    ax.set_title('colorMap')
    plt.imshow(H)
    ax.set_aspect('equal')

cax = fig.add_axes([0.12, 0.1, 0.78, 0.8])
    cax.get_xaxis().set_visible(False)
    cax.get_yaxis().set_visible(False)
    cax.patch.set_alpha(0)
    cax.set_frame_on(False)
    plt.colorbar(orientation='vertical')
    plt.show()
```



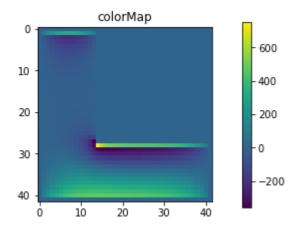
In [26]:

```
h = 0.003/42
tauzy = [[0 for _ in range(len(section))] for _ in range(len(section))]
tauzx = [[0 for _ in range(len(section))] for _ in range(len(section))]
for y in range(len(potential_section)):
    for x in range(1,len(potential_section)-1):
        prev_x = x-1
        next_x = x+1
        if not potential_section[y][prev_x]:
            tauzy[y][x] = (potential_section[y][x]-potential_section[y][prev_x])/h
        elif not potential_section[y][next_x]:
            tauzy[y][x] = (potential_section[y][x]-potential_section[y][next_x])/h
        else:
            tauzy[y][x] = (potential_section[y][next_x]-potential_section[y][prev_x])/(2*h)
H = np.array(tauzy)
fig = plt.figure(figsize=(6, 3.2))
ax = fig.add_subplot(111)
ax.set_title('colorMap')
plt.imshow(H)
ax.set_aspect('equal')
cax = fig.add_axes([0.12, 0.1, 0.78, 0.8])
cax.get_xaxis().set_visible(False)
cax.get_yaxis().set_visible(False)
cax.patch.set_alpha(0)
cax.set_frame_on(False)
plt.colorbar(orientation='vertical')
plt.show()
```



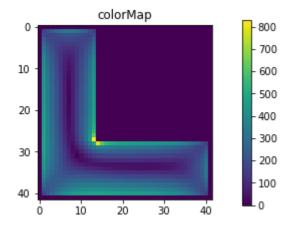
In [27]:

```
for y in range(1,len(potential_section)-1):
    for x in range(1,len(potential_section)-1):
        prev_y = y-1
        next_y = y+1
        if not potential_section[prev_y][x]:
            tauzx[y][x] = (potential_section[y][x]-potential_section[prev_y][x])/h
        elif not potential_section[y][next_x]:
            tauzx[y][x] = (potential_section[y][x]-potential_section[next_y][x])/h
        else:
            tauzx[y][x] = (potential\_section[next_y][x]-potential\_section[prev_y][x])/(2*h)
H = np.array(tauzx)
fig = plt.figure(figsize=(6, 3.2))
ax = fig.add\_subplot(111)
ax.set_title('colorMap')
plt.imshow(H)
ax.set_aspect('equal')
cax = fig.add_axes([0.12, 0.1, 0.78, 0.8])
cax.get_xaxis().set_visible(False)
cax.get_yaxis().set_visible(False)
cax.patch.set_alpha(0)
cax.set_frame_on(False)
plt.colorbar(orientation='vertical')
plt.show()
```



In [28]:

```
shear_stress = [[0 for _ in range(len(section))] for _ in range(len(section))]
for y in range(1, len(potential_section)-1):
    for x in range(1,len(potential_section)-1):
        if tauzy[y][x] or tauzx[y][x]:
            shear\_stress[y][x] = pow(tauzy[y][x]**2 + tauzx[y][x]**2, 0.5)
H = np.array(shear_stress)
fig = plt.figure(figsize=(6, 3.2))
ax = fig.add_subplot(111)
ax.set_title('colorMap')
plt.imshow(H)
ax.set_aspect('equal')
cax = fig.add_axes([0.12, 0.1, 0.78, 0.8])
cax.get_xaxis().set_visible(False)
cax.get_yaxis().set_visible(False)
cax.patch.set_alpha(0)
cax.set_frame_on(False)
plt.colorbar(orientation='vertical')
plt.show()
```



In []: