

<< IntU`

Package IntU version 0.1.25 (last modification: 14/09/2011).

Main functionality

? IntegrateUnitaryHaar

IntegrateUnitaryHaar[*integrand*, {*var*, *dim*}] gives the definite integral on unitary group with respect to Haar, accepting the following arguments:

- *integrand* – polynomial type expression of variable *var* with indices placed as subscripts, can contain any other symbolic expression of other variables,
- *var* – symbol of variable for integration,
- *dim* – the dimension of a unitary group, must be a positive integer.

IntegrateUnitaryHaar[*f*, {*u*, *d1*}, {*v*, *d2*} ...] gives multiple integral.

? IntegrateUnitaryHaarIndices

IntegrateUnitaryHaarIndices{*I1*, *J1*, *I2*, *J2*}, *dim*] gives an the definite integral on unitary group with respect to Haar for given indices. see [Collins & Śniady 2006].

Weingarten function

? Weingarten

Weingarten[*type*, *dim*] – returns the value of *Weingarten* function defined in [Collins & Śniady 2006] accepts the following arguments

- *type* – an integer partition which corresponds to cycle type of permutation,
- *dim* – the dimension of a unitary group, must be a positive integer.

? CharacterSymmetricGroup

CharacterSymmetricGroup[*part*, *type*] – gives the character of the symmetric group $\chi^{part}(type)$ Parameter *type* is optional. The default value is set to a trivial partition and in this case the function returns the dimension of the irreducible representation of symmetric group indexed by *part*, If *type* is specified the value of the character is calculated by Murnaghan–Nakayama rule using *MNInner* algorithm provided in [Bernstein 2004].

? SchurPolynomialAt1

SchurPolynomialAt1[*part*, *dim*] – returns the value of Schur polynomial s_{part} at *d* –dimensional point (1,1,...,1), i.e. the dimension of irreducible representation of $U(dim)$ corresponding to *part*.

Helper functions

? **PermutationTypePartition**

PermutationTypePartition[*perm*] – gives the partition which represents the cycle type of the permutation *perm*.

? **MultinomialBeta**

MultinomialBeta[*p*] – gives for *d* –dimensional vector of non negative

numbers p_1, p_2, \dots, p_d the value of multinomial Beta function defined as $\frac{\prod \Gamma(p_i)}{\Gamma(\sum p_i)}$.

? **ConjugatePartition**

ConjugatePartition[*part*] – gives a conjugate of a partition *part*.

? **CardinalityConjugacyClassPartition**

CardinalityConjugacyClassPartition[*part*] – gives a cardinality of conjugacy class for permutation with cycle type given by partition *part*.

? **BinaryPartition**

BinaryPartition[*part*] – gives a binary representation of a partition *part*. This function is needed for the implementation of *MNInner* algorithm in function **CharacterSymmetricGroup**.

References

[**Bernstein 2004**] D. Bernstein, The computational complexity of rules for the character table of S_n , Journal of Symbolic Computation, Volume 37, Issue 6 (2004), pp. 727-748.

[Collins & **Sniady 2006**] B. Collins and P. Sniady, Integration with Respect to the Haar Measure on Unitary, Orthogonal and Symplectic Group, Communications in Mathematical Physics, Volume 264, Number 3 (2006), pp. 773-795.