

```

GroundState[mat_?HermitianMatrixQ] := Module[{gr, u, e, m, len, pos},
  e = Eigenvalues[mat];
  m = Min[e];
  pos = Position[e, m] // Flatten;
  u = Eigenvectors[mat];
  gr = Mean[Table[Outer[Times, u[[i]], u[[i]]], {i, pos}]];
  Return[gr]
]

```

```

gts::warn =
  "to avoid overflow for temperature `1` ground state is calculated instead .";
ThermalState[rho_, t_, chop_: 10^-8] /; If[Chop[t, chop] ≠ 0, True, Message[gts::warn, t];
  True] := Module[{ther},
  ther =
    If[Chop[t, chop] == 0, GroundState[rho], MatrixExp[- rho/t] / Tr[MatrixExp[- rho/t]]];
  Return[ther]
]
(*not ≠ in if message while it is = inside if function *)

```

```

HeisenbergXYZ[jx_, jy_, jz_, dz_] :=
  jx * KroneckerProduct[PauliMatrix[1], PauliMatrix[1]] +
  jy * KroneckerProduct[PauliMatrix[2], PauliMatrix[2]] +
  jz * KroneckerProduct[PauliMatrix[3], PauliMatrix[3]] +
  dz * KroneckerProduct[PauliMatrix[1], PauliMatrix[2]] -
  dz * KroneckerProduct[PauliMatrix[2], PauliMatrix[1]]

localFisher[jx_, jy_, jz_, dz_, t_] := Block[{λ, W},
  λ = Eigenvalues[ThermalState[HeisenbergXYZ[jx, jy, jz, dz], t] // N];
  W[i_, j_] := Sum[(1 - KroneckerDelta[m, n]) *
    
$$\frac{2 \lambda[[m]] * \lambda[[n]]}{\lambda[[m]] + \lambda[[n]]} \text{KMatrix}[i][[m, n]] * \text{KMatrix}[j][[n, m]], \{n, 4\}, \{m, 4\}];
  Return[1 - Max[Table[W[i, i], {i, 3}]]]
]$$

```

```

In[93]:= Plot[{localFisher[-1, -.5, .1, 1, t], localFisher[-1, -.5, 1.6, 1, t]}, {t, .15, 4},
  PlotStyle -> {{Blue}, {Green, Dashed}}, PlotLegends -> {"Jz = 0.1", "Jz = 1.6"},
  AxesLabel -> {Style["T", Black, FontSize -> 15], Style["LQFI", Black, FontSize -> 15]}]

```

