Quantum Transport in Nanoporous Graphene

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Abstract: Abstract...



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I. INTRODUCTION

II. QUANTUM TRANSPORT

A. Ballistic quantum transport

As graphene is two dimensional material that consists of carbon atoms arranged in a hexagonal pattern, features in such a material can approach nanometer and sub nanometer

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scales. Because of the small scale the electrical properties and the electrical nature of the material is greatly changed. Normal drift-diffusion current models describe

B. π -orbitals and π -electrons

The main scope of this paper is dealing with electron transport in novel nanoporous graphene devices. When modeling such transport one needs to adress the orbital structure of carbon lattices and later this will motivate the use of tight-binding and Green's functions. In its basic form graphene can be devided into rings of carbon atoms as shown in Fig. 1. In the (x, y)-plane the carbon atoms are bound in sp^2 orbitals as shown in Fig. 2.

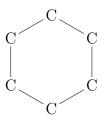


Figure 1: Graphene lattices consists of hexagonal arrangements of carbon atoms.

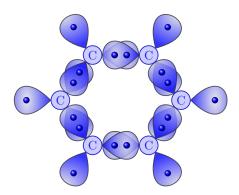


Figure 2: Carbon atoms

in a hexagonal lattice are sp^2 hybradised in the (x, y)-plane.

This hybradisation lock all but one valence electron for the carbon atoms. These electrons exists in a p-orbital in the z-direction. Fig. 3 shows the valence orbitals of carbon.

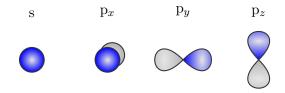


Figure 3: The valence orbitals of carbon.

The last electron in the p_z orbital does not mix with the tightly bound s, p_x and p_y electrons and moves more freely. Thus these electrons have higher energies compared to the sp^2 electrons and occupy states at the Fermi level. These electrons dominates transport in the graphene lattice. The p_z orbital is also known as the π -orbital and as such the electron lying there is called a π -electron. Through a carbon lattice the π -electrons will travel through π -orbitals, switching sign as they go as shown in Fig. 4.

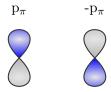


Figure 4: When going from one carbon atom to another, the π -electron goes betwenn p_{π} and $-p_{\pi}$.

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C. Tight-binding

Now that the transport carrying electrons are defined, one must choose a formalism for the transport itself. Introducing: "The Tight-Binding approximation". In this approximation the electrons are considered being tightly bound to the atoms. Contrary to a free electron gass approximation, the electrons does not spend time in between orbitals, but jump from orbital in atom a to orbital in atom b. In this world view the Hamiltonian operator is a matrix of hopping elements for a collection of neighbouring atomic orbitals, i.e. molecular orbitals. This can be done by describing the orbitals as a Linear Combination

of Atomic Orbitals (LCAO). The solution to the Schrödinger equation is then:

$$\Psi_{\text{MO}} = \sum_{\alpha,R} c_{\alpha,R} \phi_{\alpha}(R) \tag{C.1}$$

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 G. Calogero, N. R. Papior, B. Kretz, A. Garcia-Lekue, T. Frederiksen, and M. Brandbyge, Electron Transport in Nanoporous Graphene: Probing the Talbot Effect, Nano Letters 19, 576 (2019).

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Hand in report