Tunneling through a fluctuating barrier: Two-level model

Informal supplementary Mathematica.NB

"https://journals.aps.org/pre/abstract/10.1103/PhysRevE.61 .4890"

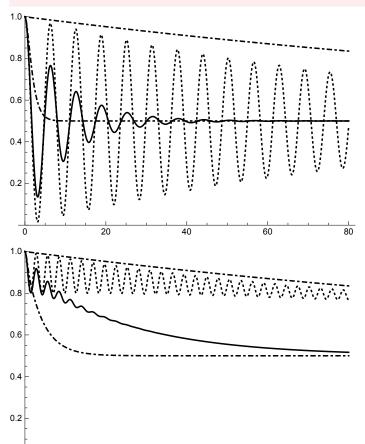
```
SapiroLoginov[\{\kappa_{-}, \epsilon_{-}, \Delta 0_{-}, \Delta 1_{-}, \nu_{-}\}, initC_, tf_] := Block[\{A, R, t, init, out\},
        \{-2\kappa, -\epsilon, 0, 0, 0, 0\},\
        \{\epsilon, -2\kappa, \Delta 0, 0, 0, \Delta 1\},\
        \{0, -\Delta 0, 0, 0, -\Delta 1, 0\},\
        \{0, 0, 0, -2\kappa - 2\nu, -\epsilon, 0\},\
        \{0, 0, \Delta 1, \epsilon, -2\kappa - 2\nu, \Delta 0\},\
        \{0, -\Delta 1, 0, 0, -\Delta 0, -2 \gamma\}
      };
     init = PadRight[initC, 6];
     NDSolveValue[{R'[t] == A.R[t], R[0] == init}, R, {t, 0, tf}]
   ];
(*eq 3 (a.b.c)*)
(\star\{\kappa_{-},\epsilon_{-},\Delta\theta_{-},\Delta\mathbf{1}_{-},\nu_{-}\}
 list of paramter*)
(*initC
 list of numbers of same 3b automatic are zero Padding to right *)
```

```
(*genetat fig for 4 parameter*)
plotFig4[\Delta 1_, \epsilon_] := Block[\{\Delta 0 = 1, \nu = 0, \}
                      \kappa, sol, p, pl1, pl2, pl3, pl4},
                 (*----*)
               \kappa = .01;
               sol = SapiroLoginov[\{\kappa, \epsilon, \Delta 0, \Delta 1, \nu\}, \{0, 0, 1\}, 80];
               p[t_{-}] := .5 (sol[t][[3]] + 1);
               pl1 = Plot[p[t], \{t, 0, 80\}, PlotRange \rightarrow \{0, 1\}, PlotStyle \rightarrow \{Dotted, Black\}];
                (*----*)
               \kappa = .1;
                sol = SapiroLoginov[\{\kappa, \epsilon, \Delta 0, \Delta 1, \nu\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, 
               p[t_{]} := .5 (sol[t][[3]] + 1);
               pl2 = Plot[p[t], \{t, 0, 80\}, PlotRange \rightarrow \{0, 1\}, PlotStyle \rightarrow \{Black\}];
                (*----*)
              \kappa = 1;
               sol = SapiroLoginov[\{\kappa, \epsilon, \Delta 0, \Delta 1, \nu\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, 
               p[t_{-}] := .5 (sol[t][[3]] + 1);
               pl3 = Plot[p[t], \{t, 0, 80\}, PlotRange \rightarrow \{0, 1\}, PlotStyle \rightarrow \{DotDashed, Black\}];
                (*----*)
               \kappa = 100;
               sol = SapiroLoginov[\{\kappa, \epsilon, \Delta 0, \Delta 1, \nu\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, \{0, 0, 1\}, 
                p[t_{-}] := .5 (sol[t][[3]] + 1);
               pl4 = Plot[p[t], \{t, 0, 80\}, PlotRange \rightarrow \{0, 1\}, PlotStyle \rightarrow \{DotDashed, Black\}];
                (*----*)
                Show[pl1, pl2, pl3, pl4]
```

```
(*fig 1 a*)
\Delta 1 = 0; \epsilon = 0;
plotFig4[\Delta1, \epsilon]
(*fig 1 b*)
\Delta 1 = 0; \epsilon = 2;
plotFig4[\Delta1, \epsilon]
```

80

60



40

0

20

