

# Stereo Vision

## An introduction with Applications

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# Outline

- Concept of Stereo Vision
- A brief description of Image
- Fundamentals of Computer Vision
- Implementation of Depth Camera
- Conclusion of this project
- Q&A

# Introduction to Computer Vision

- The ability of computers to see
  - From the perspective of engineering, it seeks to **automate tasks** that **the human visual system** can do.
- The extraction of a variety of information from images
  - Extract **form, color, and distance of objects** from the image.

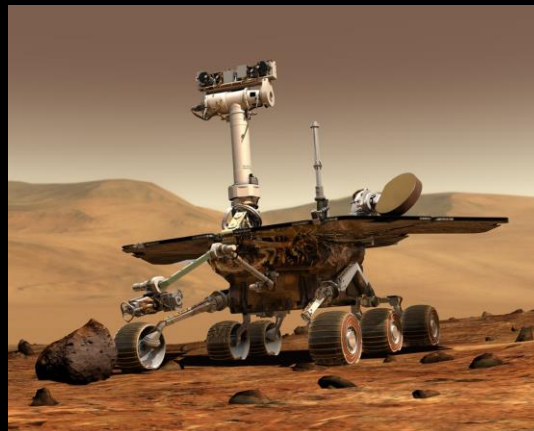
# Introduction to Computer Vision

- **Application**

- Information from the computer vision can be used in many areas.
- Image processing, Recognition, Detecting, etc.
- Photoshop, Robot vision, VR, AR, 3D Graphics of game, etc.

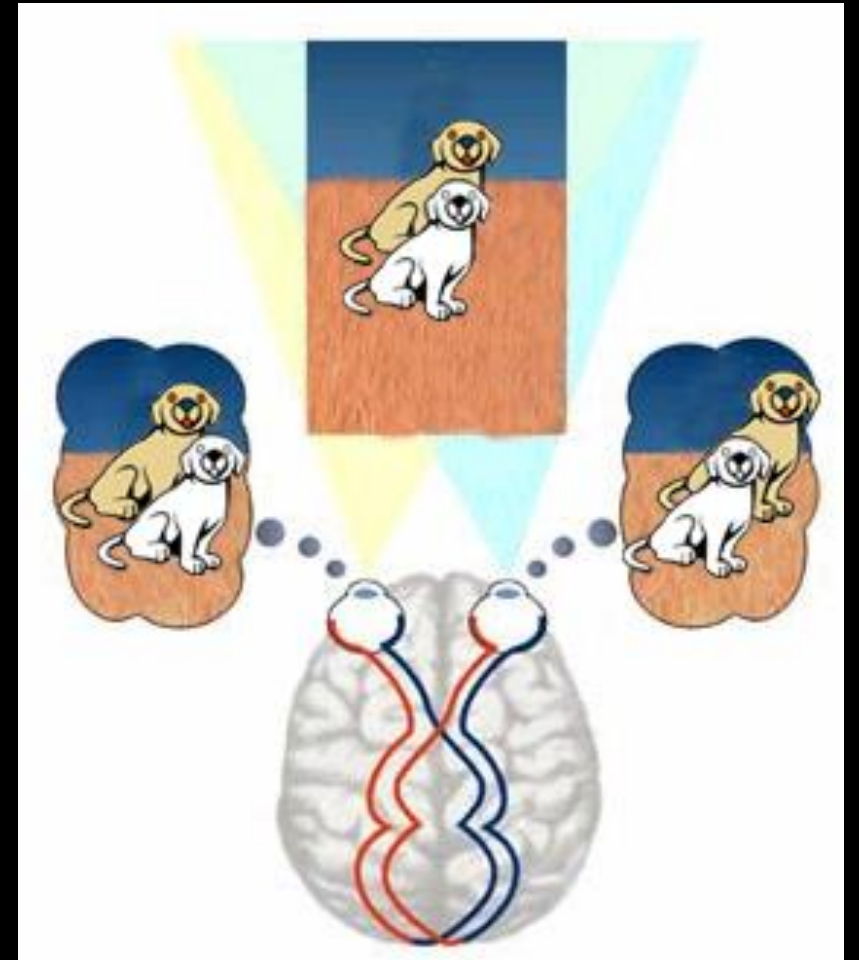
- **Background**

- Linear Algebra, Signal Processing, Calculus, Numerical Analysis, etc.



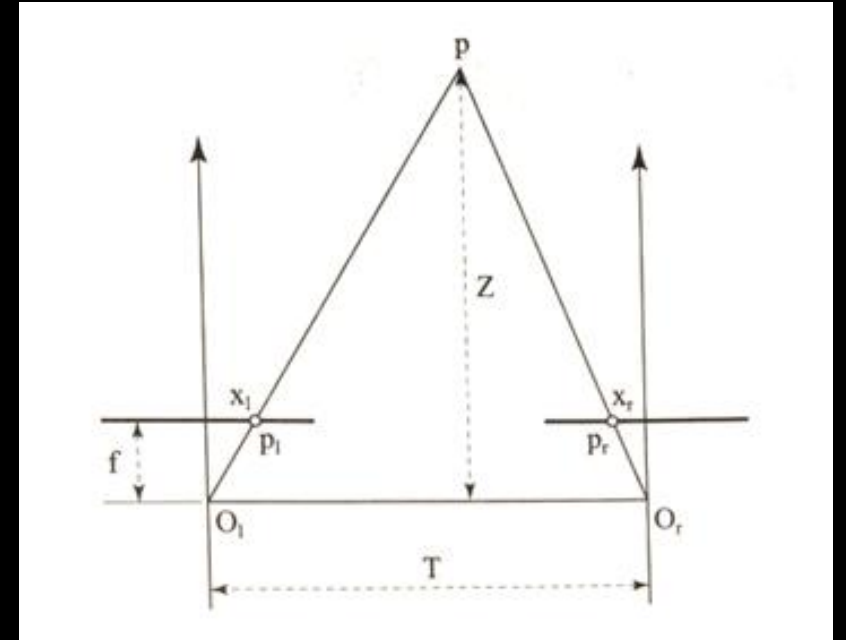
# What is Stereo Vision?

- Extraction of 3D information from two images
  - It is **same** as how humans look at objects and determine their distance!



# What is Stereo Vision?

- Extraction of 3D information from two images
  - If we have **two images of same scene**, we can get **depth information** from that in an intuitive way.
  - Next is an image and **some simple mathematical formulas** which proves that intuition.



$$f: x_l = Z: X, f: (-x_r) = Z: (T - X)$$

$$Z = \frac{fT}{x_l - x_r} = \frac{fT}{d}$$

# Example

- A stereo vision system estimates the disparity of a point as  $d = 10$  pixels
  - what is the depth( $Z$ ) of the point, if  $f = 500$  pixels and  $b = 10$  cm?

$$Z = f \frac{b}{d} = 500 \text{pix} \frac{10 \text{cm}}{10 \text{pix}} = 500 \text{cm}$$

- what is the uncertainty (standard deviation) of depth, if the standard deviation a feature in each image = 1 pixel?

$$\delta_z = Z \frac{\delta_d}{d} \quad \delta_d^2 = \delta_{x_L}^2 + \delta_{x_R}^2 = 2 \quad \therefore \delta_d = \sqrt{2}$$

$$= 500 \text{cm} \frac{\sqrt{2} \text{pix}}{10 \text{pix}} \cong 70 \text{cm}$$

# What is Image?

- Digital images are stored as **matrix of numbers**

- **Sampling**

ex) VGA : 640x480

UHD : 3840x2160

- **Quantization**

ex) 8bit (gray scale)

24bit (true RGB)

- **Image vs Text**

ex) UHD(true RGB) Image : 3840x2160x24bit = 23.7MB

Book : 250kB ~ 300kB



10	11	10	9	9	9	10	11	12	10	10	9	9	9	10	
10	10	10	10	10	11	10	16	26	59	69	16	10	11	9	10
10	10	10	11	16	27	49	62	89	134	147	34	12	11	15	15
10	10	11	20	43	109	153	162	165	175	171	110	22	47	73	39
9	10	37	117	166	184	187	193	180	170	171	166	65	84	65	14
10	43	165	186	185	185	189	181	158	115	135	154	123	92	16	16
35	159	183	178	174	155	118	90	77	44	28	77	138	45	51	88
79	176	186	174	150	102	78	56	35	19	14	43	102	47	146	102
89	177	186	179	175	139	104	47	25	36	90	140	141	34	135	33
98	171	181	185	189	188	158	95	68	172	198	186	188	48	84	39
114	155	177	188	192	198	193	164	154	201	209	204	210	151	43	114
142	144	167	173	178	174	172	166	178	190	202	208	209	208	115	35
150	154	161	168	168	162	176	177	175	172	183	189	203	210	171	39
155	151	162	170	164	177	186	183	167	138	173	190	193	209	175	40



# What is Image?

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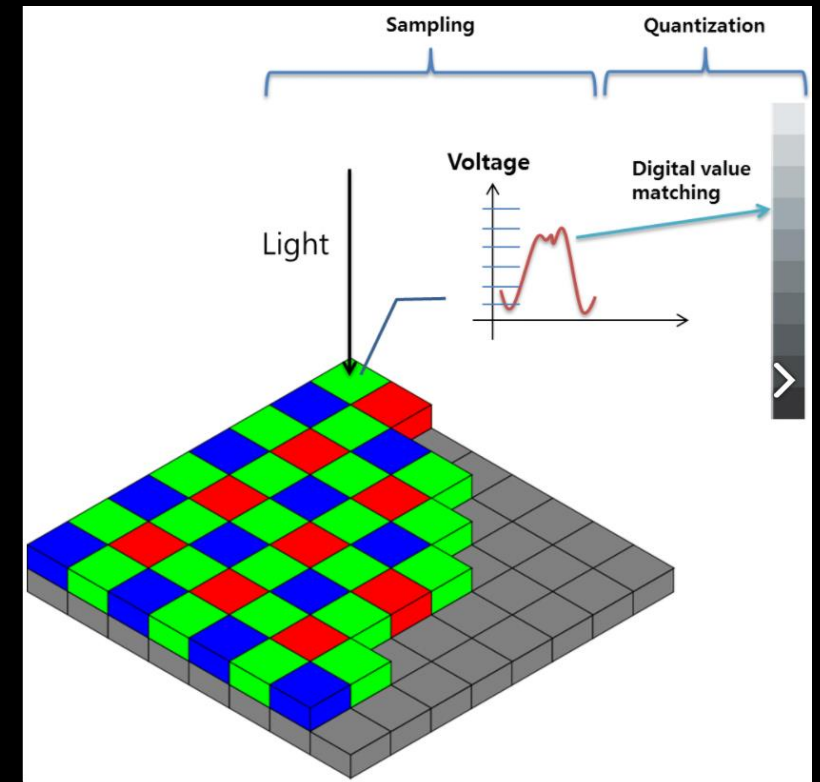
ex) 8bit (gray scale)

24bit (true RGB)

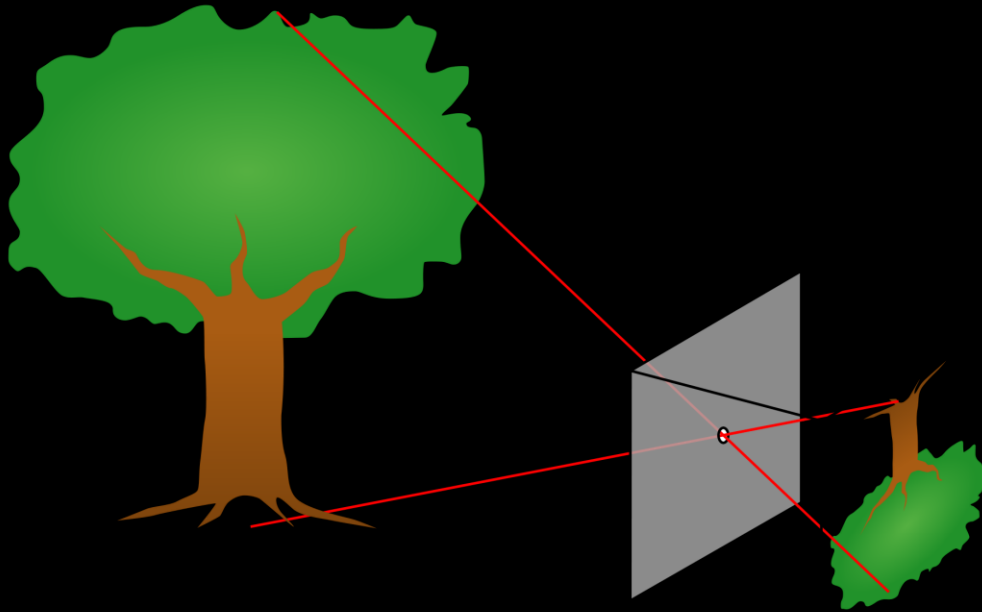
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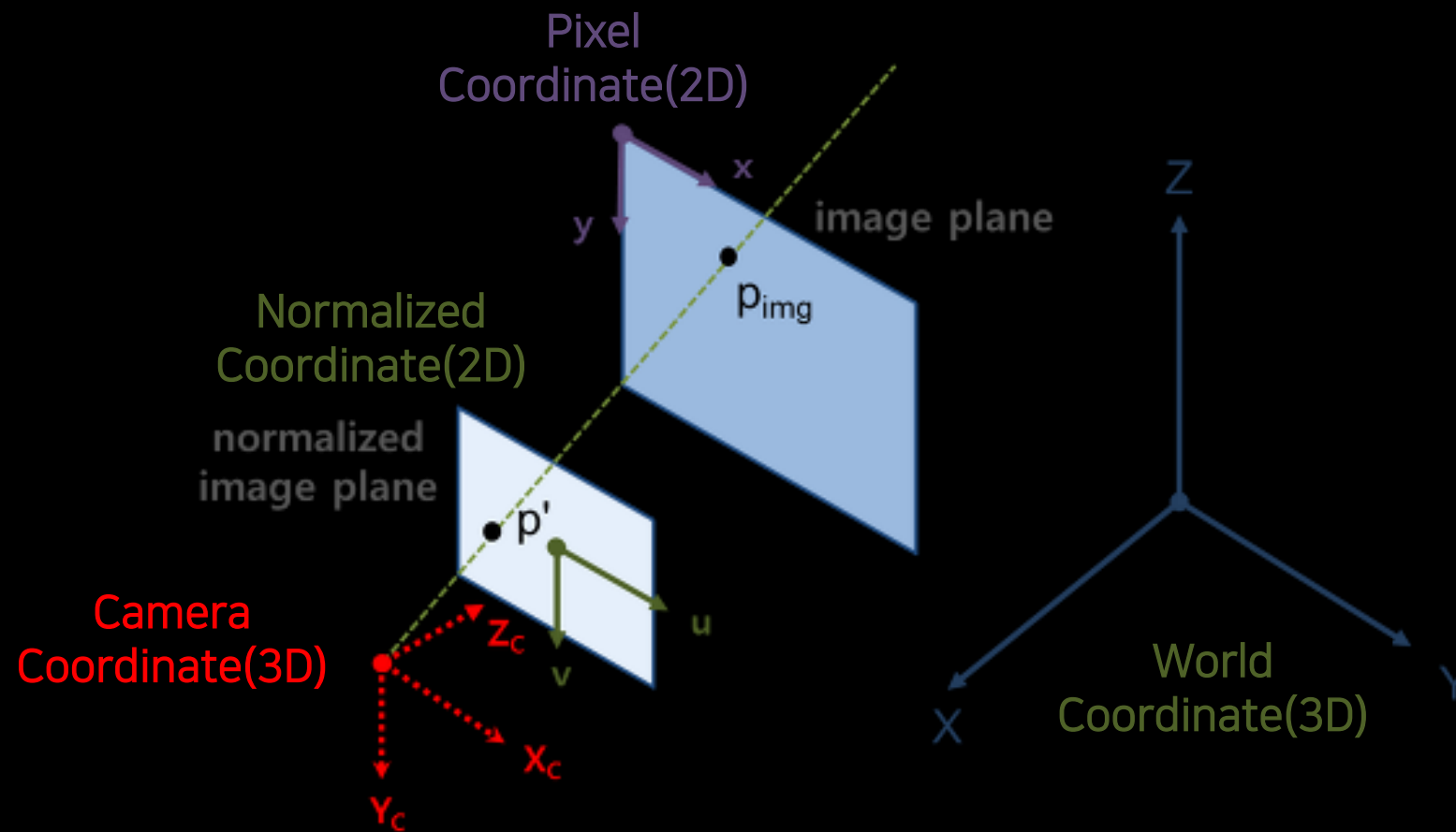


# Image Formation

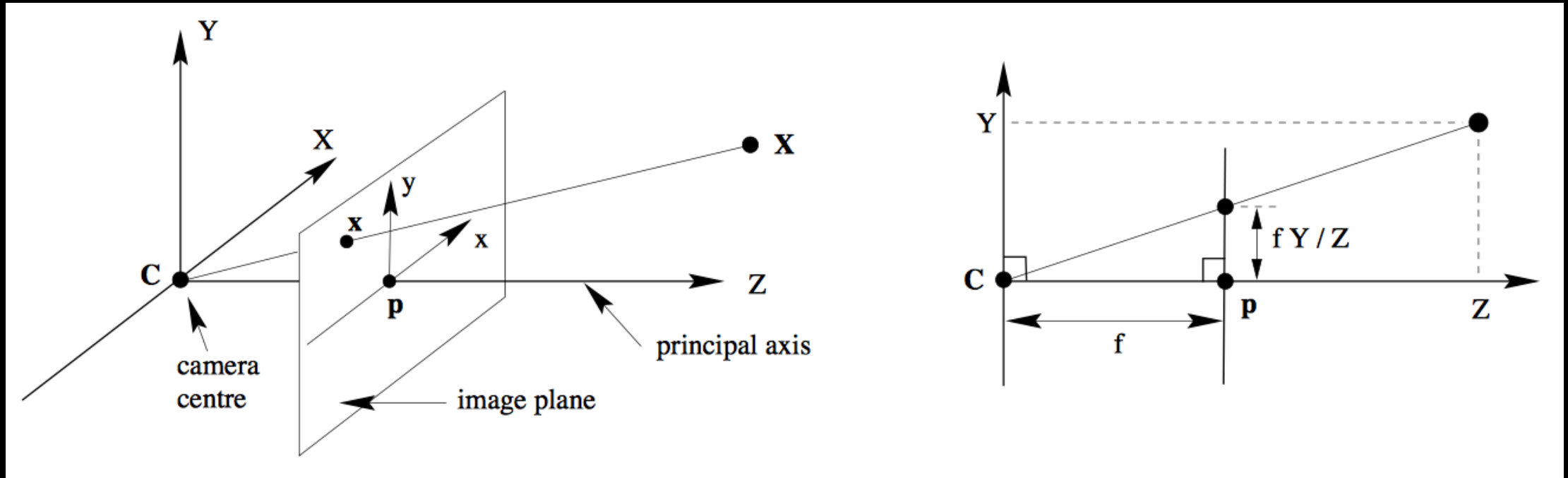


- A good lens can be modeled by a **pinhole camera**; each ray from the scene passes undeflected to the image plane.
- Simple equations describe projection of a scene point onto the image plane("perspective projection").

# 4-Coordinate System



# A Simple Pinhole Camera Model



$$x = \frac{f \cdot X}{Z} \quad y = \frac{f \cdot Y}{Z}$$

We can see the **relation between** a point in **3D space** and to a point on the **focal plane**.

# Image Geometry

- This 3x4 matrix **P** is known as the **Camera Projection Matrix**. To adjust for the reference frame in the image plane – origin at corner v/s origin at center, we add a translation component to the left 3x3 matrix of P.
- This 3x3 matrix **K** is called the **Camera Calibration Matrix**.

$$\begin{bmatrix} fX \\ fY \\ Z \end{bmatrix} = \begin{bmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} \quad K = \begin{bmatrix} f & 0 & p_x \\ 0 & f & p_y \\ 0 & 0 & 1 \end{bmatrix} \rightarrow K = \begin{bmatrix} \alpha_x & s & x_0 \\ 0 & \alpha_y & y_0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$x = PX$$

In the Image plane

In world coordinate

Consider  
Nomalization & distortion factor

# Image Geometry

- In most cases, the camera coordinates will be with respect to a different coordinate system where it is not at the origin in the world coordinate system.
- Hence, any coordinate can be shifted from the world coordinate space to the camera coordinate space (where the camera is the origin) with the equation.

$$X_{camera} = R(X_{world} - C)$$

# Image Geometry

$$X_{camera} = R(X_{world} - C)$$

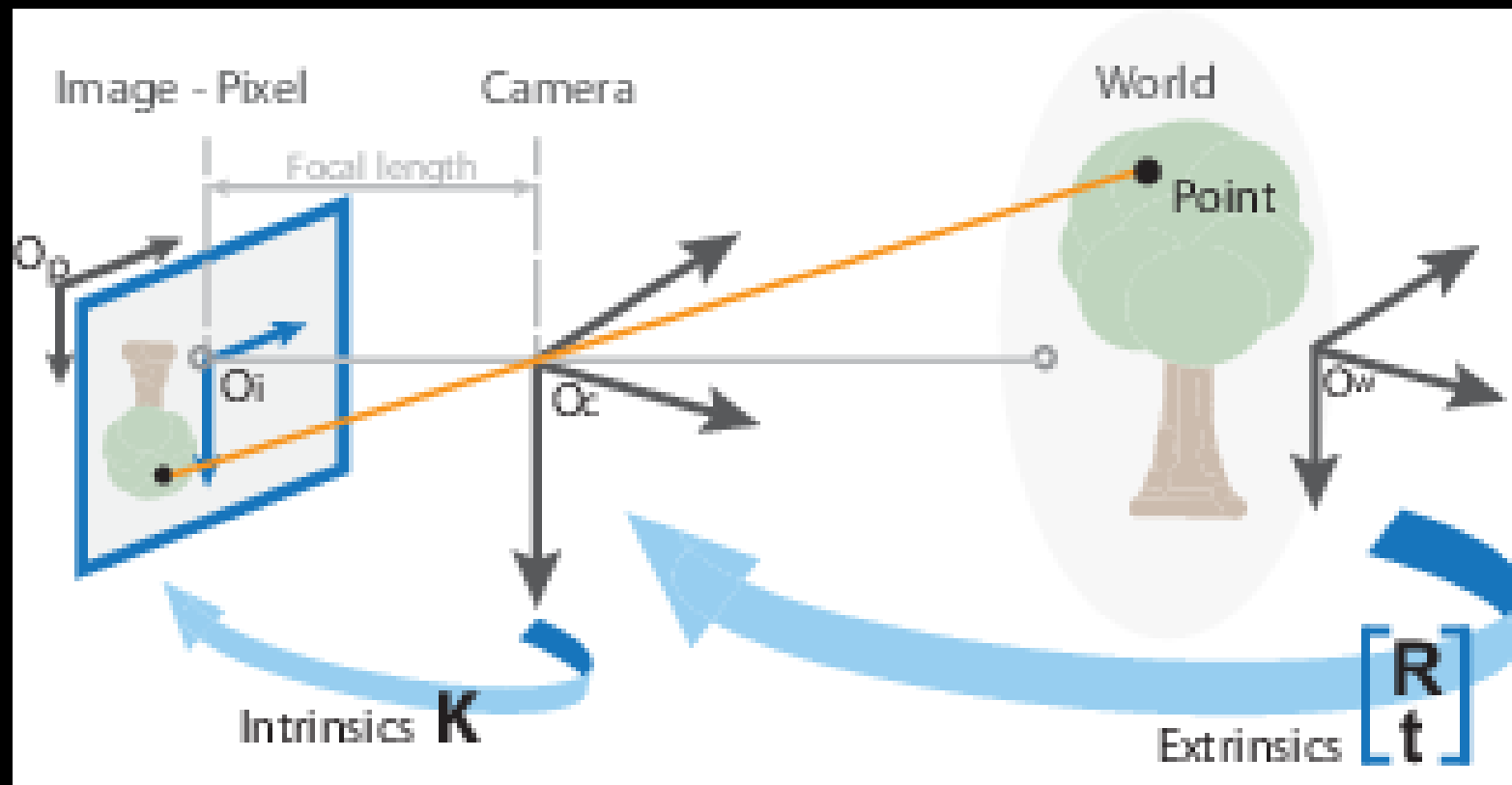
- where  $R$  is the rotation matrix and  $-C$  represents a translation with respect to the camera center to make it the origin.
- Combining the *camera calibration matrix* and the coordinate frame shifting above, we can draw a mapping between the point in world coordinate system  $X$  and the point  $x$  in the image plane, represented by

$$x = KR[I | -C]X$$

$$P = KR[I | -C]$$

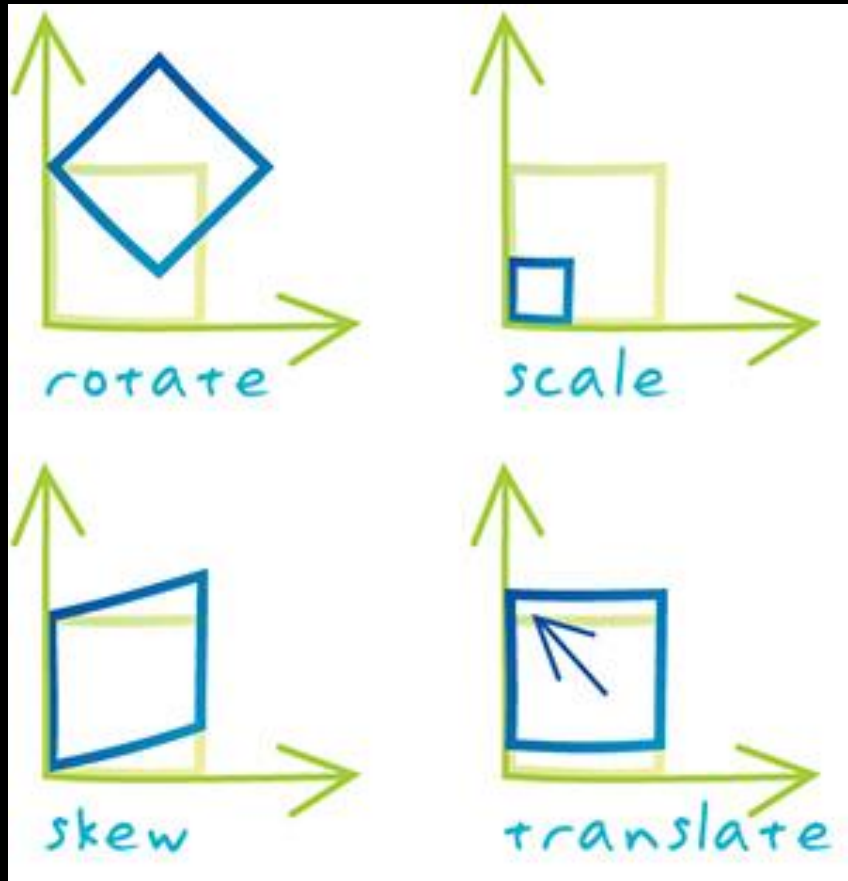
Parameters in  $K$  are called the **camera intrinsics** (they never change) and the remaining parameters  $R$  and  $C$  are called the **camera extrinsics**.

# Image Geometry



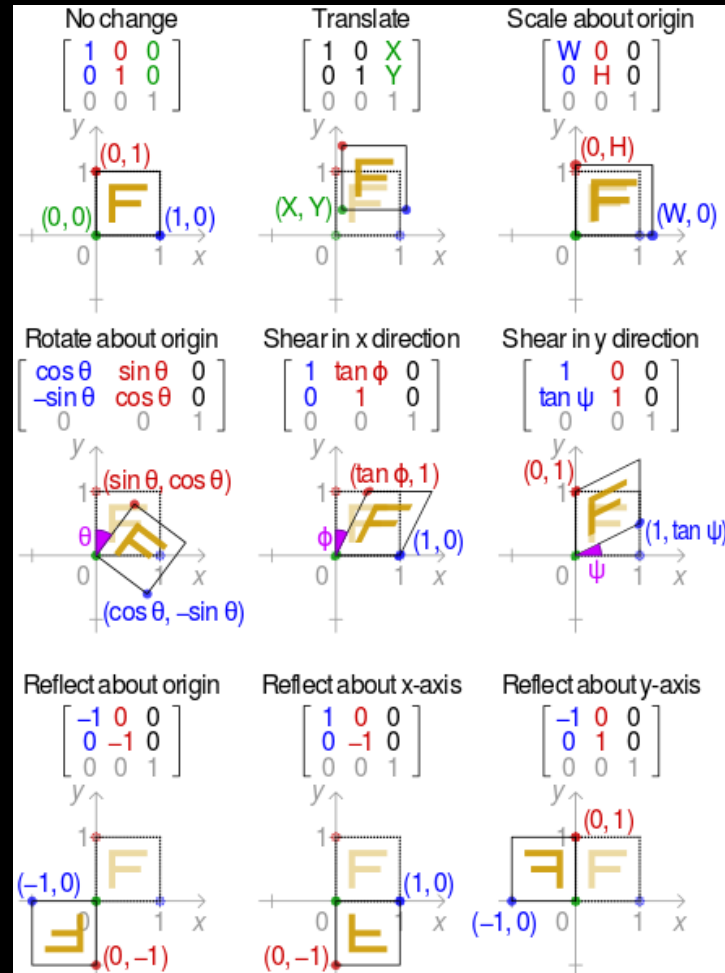


# Geometric Transformations of Images

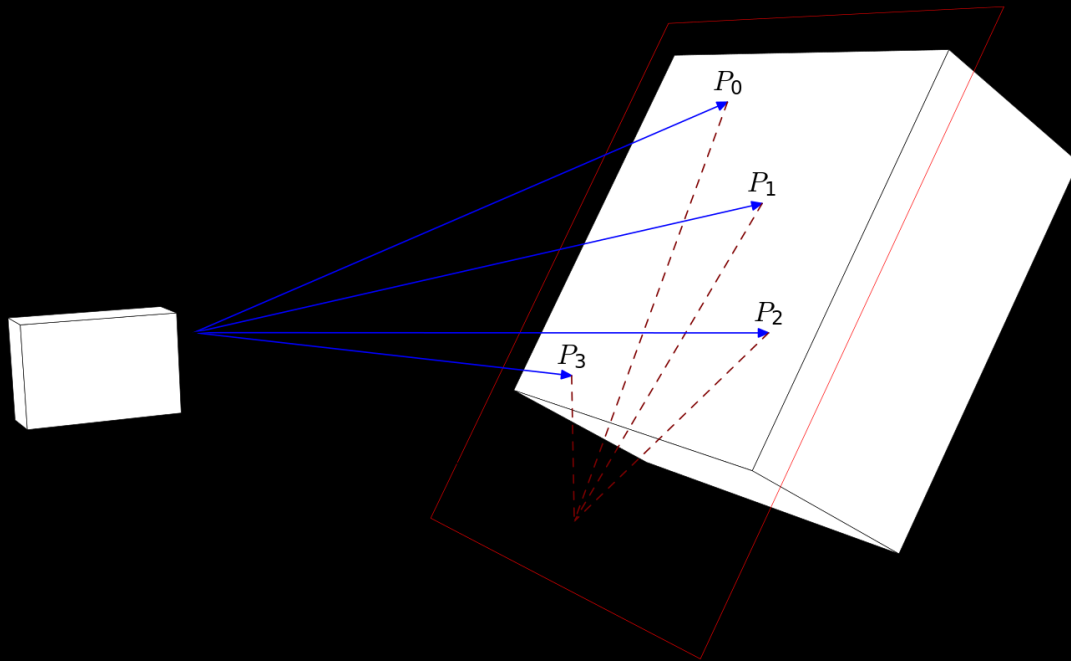


- Also called spatial transformations, 2D transformations
- Include: translation, rotation, scaling, nonlinear warping, or perspective angle adjustment.
- It is actually a **rearrangement of pixels** on the image plane.
- The coordinates of input image are transformed into coordinates of output image using a **transformation function**.

# Transformations Matrix



# Homography

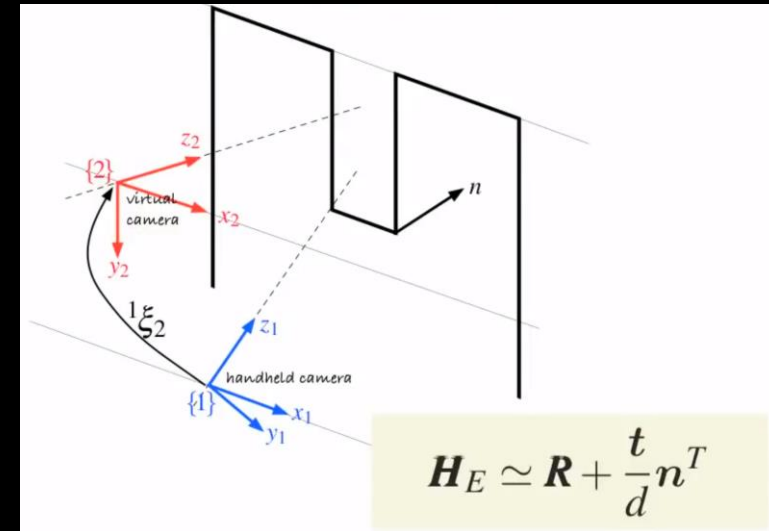


- For a Planer surface object, you can model a random perspective projection transformation from 3D space to 2D images as a **homography** between two images.

# Perspective rectification



$${}^2p = H {}^1p$$



By using Homography matrix  $H$ , We can get an image that it seems from **virtual camera view**.

# Demo #1

- 1) Image Alignment
- 2) Virtual Ads on buildings

# Features in Image

- **Correlation-based approaches**

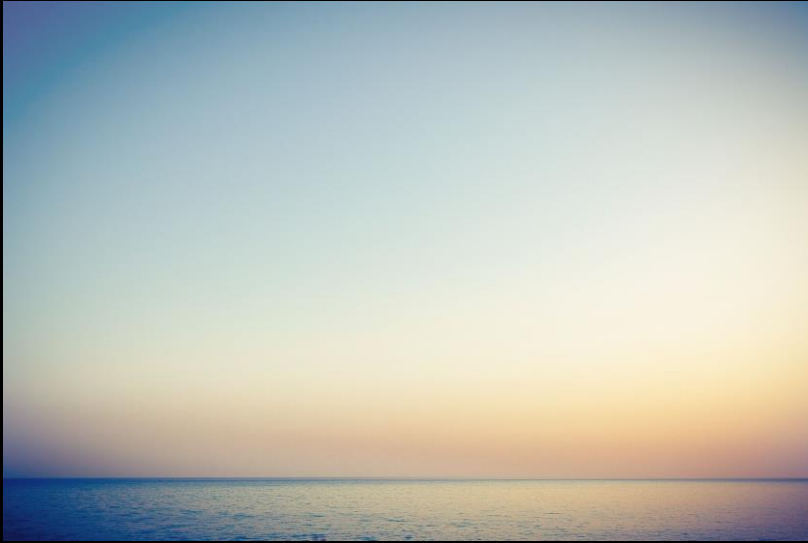
- Matches image patches using correlation.
- Assumes only a translational difference between the two local patches. ( no rotation, or differences in appearance due to perspective)
- A good assumption if patch covers a single surface, and surface is far away compared to baseline between cameras.
- Works well for scenes with lots of texture.

- **Feature-based approaches**

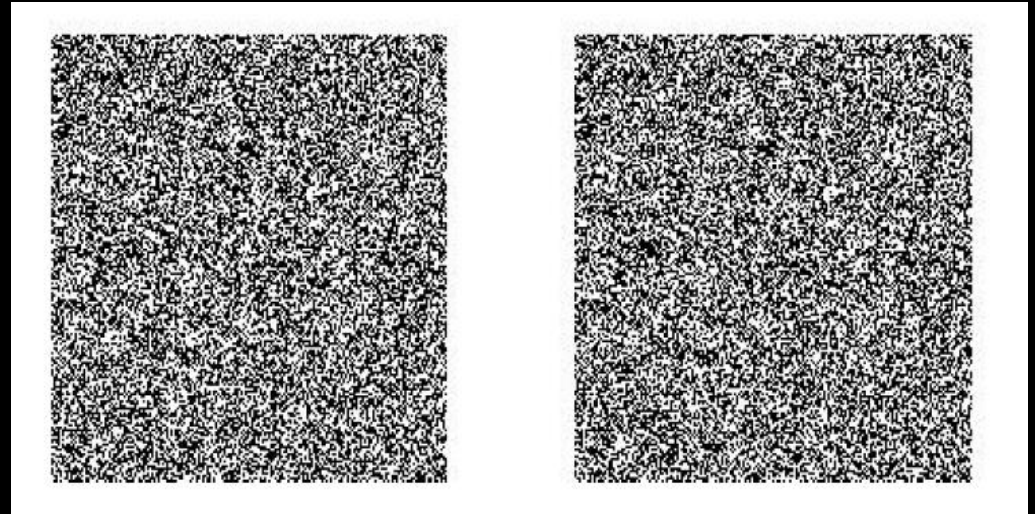
- Matches edges, line, or corners
- Gives a sparse reconstruction

# Correspondence Problem

- Worst case scenarios



No features



Ambiguous matches

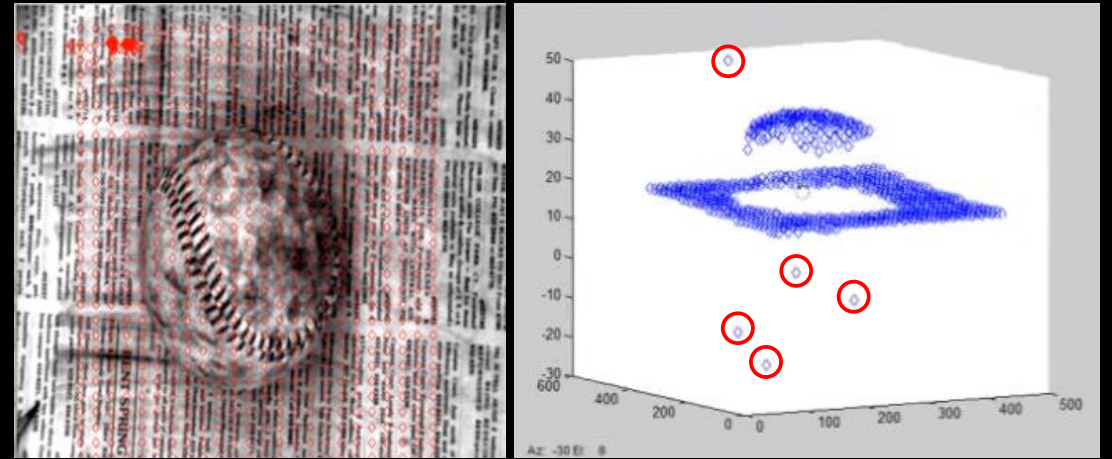


# Correspondence Problem

- Mismatching makes errors when calculating Depth-map.



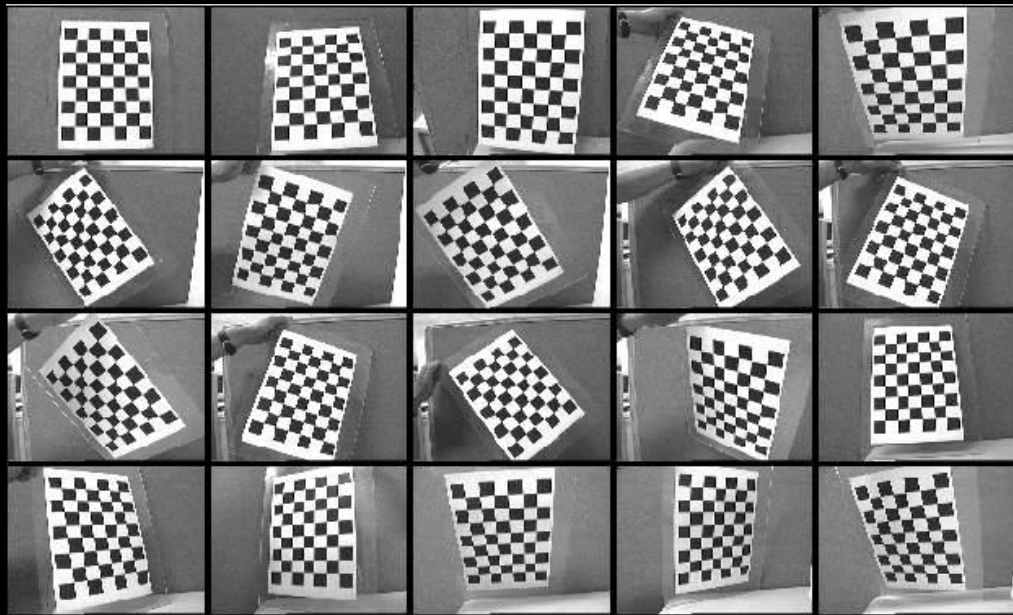
Scattering reflection of light.



Error

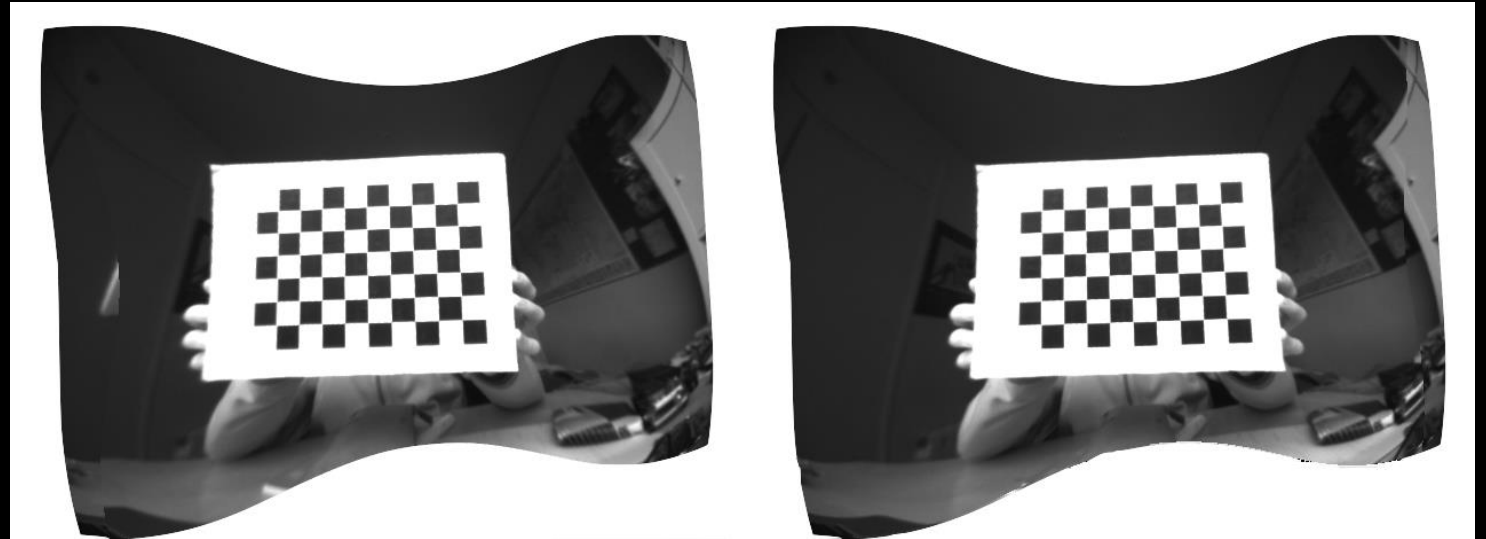


# Camera Calibration



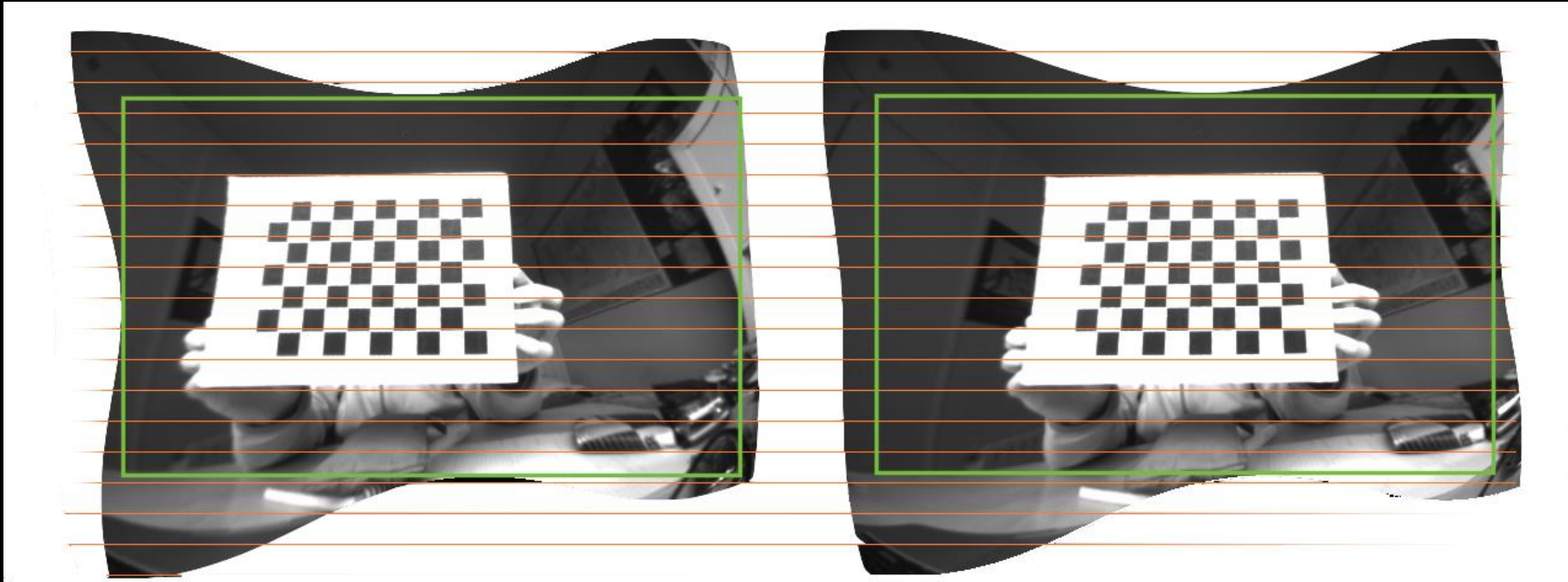
- Geometric camera calibration, also referred to as camera resectioning, **estimates the parameters of a lens and image sensor** of an image or video camera.
- You can use these parameters to correct for **lens distortion**, **measure the size of an object in world units**, or **determine the location of the camera in the scene**.
- These tasks are used in applications such as machine vision to detect and measure objects. They are also used in robotics, for navigation systems, and 3D scene reconstruction.

# Camera Calibration



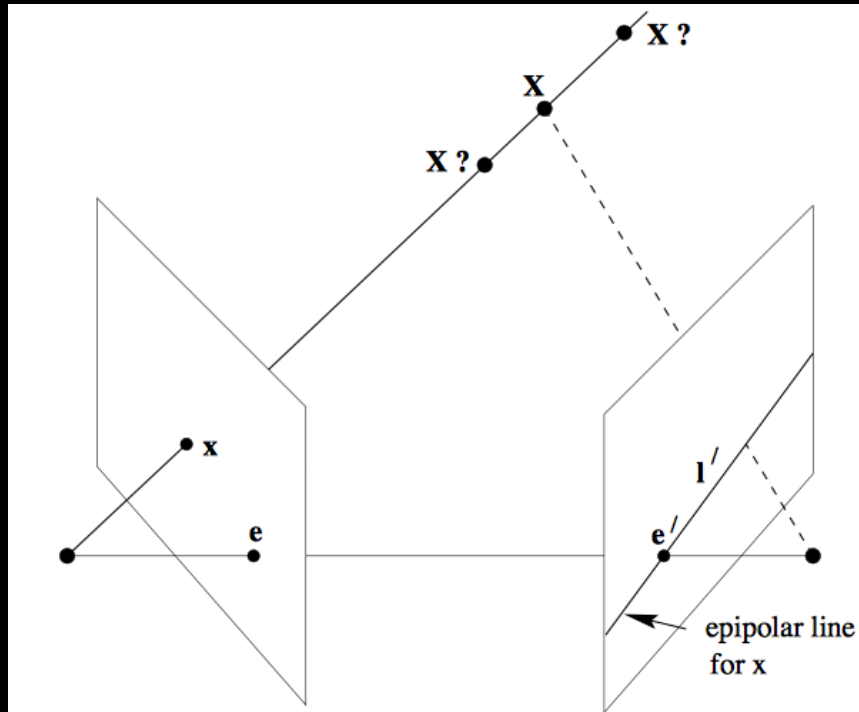
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# Camera Calibration



- Corrected parameters **reduce errors to accurately build Depth-map**.
- These tasks are used in applications such as machine vision **to detect and measure objects**. They are also used in **robotics, for navigation systems, autonomous driving system and 3D scene reconstruction**.

# Epipolar Geometry



When two cameras view a 3D scene from two distinct positions, there are a number of geometric relations between the 3D points and their projections onto the 2D images that lead to constraints between the image points.



# Epipolar Geometry



(a)



(b)



(c)



(d)

Green points are **matching point from features** in image and Green lines are **epipole lines**.

If the epipole lines in the two images are **parallel to each other**, the most **accurate Depth-map** can be calculated.

# Demo#2

## – 3D Reconstruction with Stereo Image



Calibrated Left Image



Calibrated Right Image



What is disparity map?

# Conclusion of this project

## Use open-source

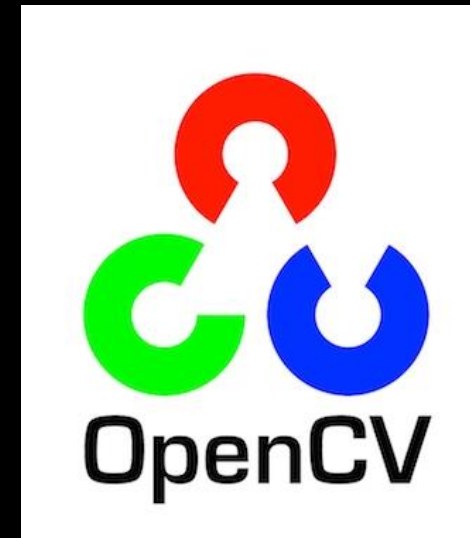
- Ubuntu
  - Free and well made GUI Linux package
  - Good Portability
  - License : GNU Public license
  - Platform : Linux
  - Supports open sources much better than Windows  
(OpenGL, ffmpeg, Tensorflow etc.)



# Conclusion of this project

## Use open-source

- OpenCV
  - Free Software package
  - Image Processing & Computer Vision Libraries
  - License : Modified BSD lisence
  - Platform : Linux/Mac/Windows/etc.
  - Language : C++/Python/Java/etc.



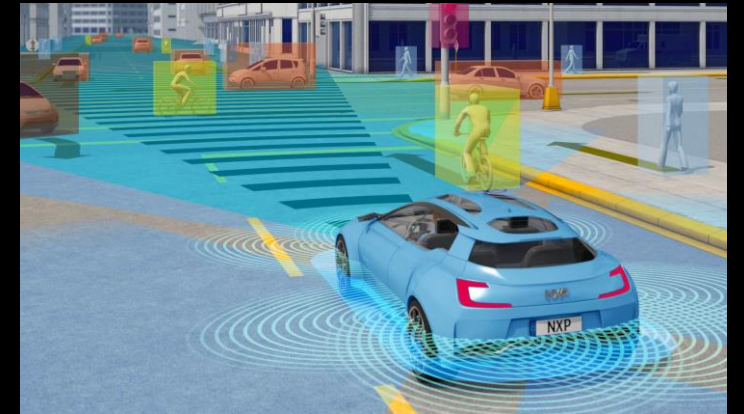
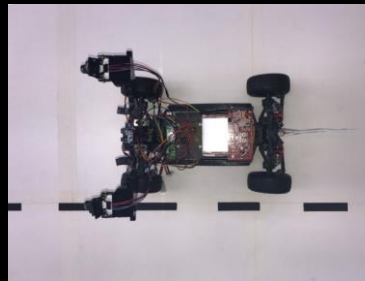
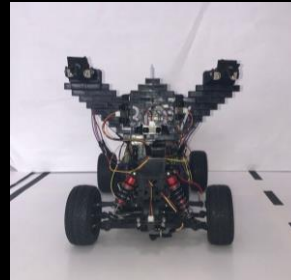
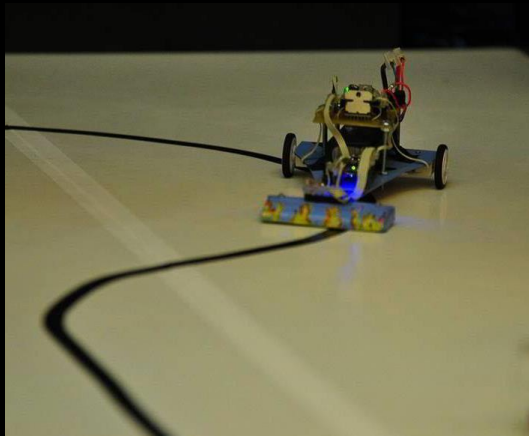
My Project Repository : [github.com/ghbae92](https://github.com/ghbae92)

Team Repository : [github.com/teamHMD](https://github.com/teamHMD)



# Conclusion of this project

What is next?



**Q&A**

**End of this presentation**

**Thanks for your attention**