```
x, y variables
i, n
          indicies
                    ::=
                                                                            expressions
                             proc pat \rightarrow cmd
                     patterns
pat
                    ::=
binds
                                                                            bindings
                    ::=
α, σ, τ
                                                                            types
                                                                                variables
                                                                                application

\begin{array}{ccc}
\tau_1 & \tau_2 \\
\tau_1 & \to & \dots & \to & \tau_n \\
\forall x. & \tau \\
\end{array}

'[]

\tau_1 ': \dots ': \tau_n

                                                                                functions
                                                                                quantification
                                                                                promoted nil
                                                                                promoted cons
Γ, Δ
                    ::=
                                                                            contexts
                             \emptyset
                            \Gamma_1, \ldots, \Gamma_n
                                                                                concatenation
                                                                            commands
cmd
                             e_1 \rightarrow e_2
                                                                                arrow application (first-order)
                             e_1 \prec\!\!\!\prec e_2
                                                                                arrow application (higher-order)
                             if e then cmd_1 else cmd_2
                                                                                branching
                             case e of { alts }
                                                                                case analysis
                             let binds in cmd
                                                                                local binding
                             \lambda pat \rightarrow cmd
                                                                                command abstraction
                             cmd e
                                                                                command application
                             (e \ cmd_1 \dots cmd_n)
                                                                                control operator
                             do { stmt; cmd }
                                                                                sequencing
alts
                    ::=
                            \overline{pat_i \rightarrow cmd_i}^i
stmt
                                                                            statements
                    ::=
                             let binds
                             pat \leftarrow cmd
                         pattern typing
pat :: \tau \Rightarrow \Delta
                   binding typing
binds \Rightarrow \Delta
\Gamma \vdash e :: \tau
                    expression typing
                                               pat :: \tau_1 \Rightarrow \Delta
                                          \frac{\Gamma \mid \Delta \vdash_{\alpha} cmd :: '[] \rightharpoonup \tau_{2}}{\Gamma \vdash \mathbf{proc} \ pat \rightarrow cmd :: \alpha \ \tau_{1} \ \tau_{2}} \quad \mathsf{Expr\_Proc}
\Gamma \mid \Delta \vdash_{\alpha} cmd :: \sigma \rightharpoonup \tau \mid
                                        command typing
```

$$\begin{array}{c} \Gamma \vdash e_1 :: \alpha \left( \operatorname{STK} \llbracket \tau_1 ': \sigma \rrbracket \right) \tau_2 \\ \Gamma, \Delta \vdash e_2 :: \tau_1 \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \multimap e_2 :: \sigma \rightharpoonup \tau_2 \end{array} \right) \subset \operatorname{MD-APF} \\ \hline \Gamma, \Delta \vdash e_1 :: \alpha \left( \operatorname{STK} \llbracket \tau_1 ': \sigma \rrbracket \right) \tau_2 \\ \hline \Gamma, \Delta \vdash e_2 :: \tau_1 \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \multimap e_2 :: \sigma \rightharpoonup \tau_2 \end{array} \right) \subset \operatorname{CMD-APPH} \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \bowtie e_2 :: \sigma \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \bowtie e_2 :: \sigma \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \bowtie e_2 :: \sigma \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \bowtie e_2 :: \sigma \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \bowtie e_2 :: \sigma \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \bowtie e_2 :: \sigma \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} e_1 \bowtie e_2 :: \sigma \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \wedge pat \rightharpoonup cmd :: \sigma \rightharpoonup \tau_2 \\ \hline \Gamma | \Delta \vdash_{\alpha} \wedge pat \rightharpoonup cmd :: (\tau_1 ': \sigma) \rightharpoonup \tau_2 \end{array} \right] \subset \operatorname{CMD-APPC} \\ \hline \Gamma \vdash e :: \forall x. \ \alpha_i \left( \operatorname{ENV} \llbracket x, \sigma_i \rrbracket \right) \tau_i \stackrel{i}{\longrightarrow} \Delta_1 \left( \operatorname{ENV} \llbracket x, \sigma_1 \rrbracket \right) \tau_1 \\ \hline \Gamma | \Delta \vdash_{\alpha_i} e_1 \bowtie e_1 \bowtie e_1 \stackrel{i}{\longrightarrow} e_1 \implies e_1 \implies$$

Definition rules: 11 good 0 bad Definition rule clauses: 35 good 0 bad